
Financial Education - basics

basics

Jul 03, 2025

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This book is meant to collect some notes about financial instruments and methods for financial education, and mainly focused asset allocation.

This material is part of the **basics-books project**. It is also available as a .pdf document.

Main goal

The ultimate goal of this material is to develop an understanding of how to manage personal savings efficiently, in line with one's own reasonable objectives.

To achieve this, some intermediate goals include:

- gaining knowledge of the **macroeconomic environment**
- familiarizing with some of the most common **investment tools** (mainly bonds and stocks);
- getting used to some **common-sense** and **investing principles**: minimizing certain costs when conditions are equal, risk/reward, diversification, liquidity, and other constraints/inefficiencies
- learning **what not to do**
- and once the poor choices have been ruled out, evaluating the reasonable options for building and managing an investment portfolio, using mainly *ETFs* as a natural choice of a (usually) liquid asset providing diversification at low cost, even for small capitals.

-
- Introduction
 - *Summary*
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 - *Introduction to principles of investing*
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- *Strategic and Tactical Asset Allocation*
 - *Rebalancing*
- Extra
 - *Extra and Random*
 - *Euristhics and historical correlations*
- People
 - *Resources, People and Firms*
 - *The Bull*

Part I

Introduction

SUMMARY

Introduction

Financial goals; money; inflation (BC and inflation target);

Asset classes

Asset allocation

REFERENCES

Here some references to other sources, in order to reasonably organize the contents of this book

Investment and Portfolio Management - RICE - coursera - A.Ozoguz, J.Foote

Global Financial Markets

- Intro and Review of Elementary Finance Tools
- Financial system and financial assets: fixed income, equity and derivatives
- Organization of financial markets and securities trading

Portfolio Selection and Risk Management

- Intro and R/R: R/R trade-off
- Ptf construction and diversification
- Investor choices: utility functions, mean-variance preferences
- Optimal capital allocation and portfolio choice: mean-variance optimization (Modern Portfolio Theory)
- Equilibrium asset pricing models: CAPM, return-beta; multi-factor models (e.g. Fama-French)

Biases and Portfolio Selection

- Efficient Market Hypothesis (EMH), and anomalies
- Biases and realistic preferences
- Inefficient markets: equity premium, volatility puzzle (?), long-run reversal to the mean, value effect, momentum
- Investor behavior

Investment Strategies and Portfolio Analysis

- Performance measurement and benchmarking
- Active vs passive investing: R^* risk-adjusted return measurements: Sharpe, Sortino, Treynor's ratio, Jensen's alpha, ...; comparing the R^*
- Performance evaluation: style analysis and performance attribution

Capstone: Build a Winning Investment Portfolio

Using software for building ptf and assess its properties

- ...

Part II

Macroeconomic Context for Investing

ACTORS

3.1 People

3.2 Private companies

3.3 Government - public

3.4 Banks

3.4.1 Central banks

3.4.2 Investment banks

3.5 Foreign regions

INFLATION

- Definition and measurements of inflation
- Example: Italy (ISTAT). NIC, FOI, IPCA; sectors: weights, and sector IPC
- Who controls inflation, and how? One of *CB* goals: inflation target; tools: monetary policy
- Origin of inflation?
 - short-, medium-run: cost-push, demand-pull, built-in (triangle model)
 - long-run: “monetary always and everywhere a monetary phenomenon” M.Friedman

INFLATION

5.1 Load libraries and import data

```
# Load libraries
import numpy as np
import pandas as pd

import plotly.graph_objects as go
import plotly.express as px
```

```
# Import data
# conditioning for being in Colab or not
if 'google.colab' in str(get_ipython()):
    from google.colab import drive
    drive.mount('/content/drive')
    folder = '/content/drive/MyDrive/basics-books/repos/financial-edu/bbooks-
↳financial-edu/code/data/'
else:
    folder = ''

#> Files
# FOI-prices: 2016-.../2025-...
# IPCA-weights: 2018/2025
# IPCA-prices: 2018-.../2025-...
# NIC-weights: 2018/2025
# NIC-prices: 2018-.../2025-...
filen = {
    'FOI-prices' : folder+'monthly-FOI.xlsx' ,
    'IPCA-weights': folder+'Classificazione Ecoicop (4 cifre) (IT1,168_6_DF_DCSP_
↳IPCA3_1,1.0).xlsx',
    'IPCA-prices' : folder+'Classificazione Ecoicop (4 cifre) (IT1,168_760_DF_DCSP_
↳IPCA1B2015_1,1.0).xlsx',
    'NIC-weights' : folder+'Classificazione Ecoicop (5 cifre) (IT1,167_743_DF_DCSP_
↳NIC3B2015_3,1.0).xlsx',
    'NIC-prices' : folder+'Classificazione Ecoicop (5 cifre) (IT1,167_744_DF_DCSP_
↳NIC1B2015_4,1.0).xlsx'
}
```

```
df = {
    'prices' : pd.read_excel(filen['IPCA-prices'], sheet_name='data', decimal=','),
    'weights': pd.read_excel(filen['IPCA-weights'], sheet_name='data', decimal=',')
}
```

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```

for kdf, idf in df.items():
    idf.columns = idf.columns.str.strip() # strip whitespaces
    idf = idf.set_index(['Tempo'])
    idf = idf.transpose()
    idf = idf.rename(columns={'index': 'Tempo'})

```

```

-----
FileNotFoundError                                Traceback (most recent call last)
Cell In[3], line 2
      1 df = {
----> 2     'prices' : pd.read_excel(filen['IPCA-prices'], sheet_name='data',
    decimal=','),
      3     'weights': pd.read_excel(filen['IPCA-weights'], sheet_name='data',
    decimal=',')
      4 }
      5
      6 for kdf, idf in df.items():
      7     idf.columns = idf.columns.str.strip() # strip whitespaces

File ~/local/lib/python3.8/site-packages/pandas/io/excel/_base.py:478, in read_
    excel(io, sheet_name, header, names, index_col, usecols, dtype, engine,
    converters, true_values, false_values, skiprows, nrows, na_values, keep_default_
    na, na_filter, verbose, parse_dates, date_parser, date_format, thousands,
    decimal, comment, skipfooter, storage_options, dtype_backend)
    476 if not isinstance(io, ExcelFile):
    477     should_close = True
--> 478     io = ExcelFile(io, storage_options=storage_options, engine=engine)
    479 elif engine and engine != io.engine:
    480     raise ValueError(
    481         "Engine should not be specified when passing "
    482         "an ExcelFile - ExcelFile already has the engine set"
    483     )

File ~/local/lib/python3.8/site-packages/pandas/io/excel/_base.py:1496, in
    ExcelFile.__init__(self, path_or_buffer, engine, storage_options)
    1494     ext = "xls"
    1495 else:
-> 1496     ext = inspect_excel_format(
    1497         content_or_path=path_or_buffer, storage_options=storage_options
    1498     )
    1499     if ext is None:
    1500         raise ValueError(
    1501             "Excel file format cannot be determined, you must specify "
    1502             "an engine manually."
    1503         )

File ~/local/lib/python3.8/site-packages/pandas/io/excel/_base.py:1371, in
    inspect_excel_format(content_or_path, storage_options)
    1368 if isinstance(content_or_path, bytes):
    1369     content_or_path = BytesIO(content_or_path)
-> 1371 with get_handle(
    1372     content_or_path, "rb", storage_options=storage_options, is_text=False
    1373 ) as handle:
    1374     stream = handle.handle
    1375     stream.seek(0)

```

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```

File ~/local/lib/python3.8/site-packages/pandas/io/common.py:868, in get_
↪handle(path_or_buf, mode, encoding, compression, memory_map, is_text, errors,
↪storage_options)
    859         handle = open(
    860             handle,
    861             ioargs.mode,
    (...
    864             newline="",
    865         )
    866     else:
    867         # Binary mode
--> 868         handle = open(handle, ioargs.mode)
    869     handles.append(handle)
    871 # Convert BytesIO or file objects passed with an encoding

FileNotFoundError: [Errno 2] No such file or directory: 'Classificazione Ecoicop_
↪(4 cifre) (IT1,168_760_DF_DCSP_IPCA1B2015_1,1.0).xlsx'

```

```
df['prices'].head()
```

```

                                Tempo 2018-01 2018-02 2018-03 \
0                                [00] Indice generale    100.6    100.1    102.4
1  [01] -- prodotti alimentari e bevande analcoli...    103.9      103    103.2
2                                [011] Prodotti alimentari      104    103.2    103.4
3                                [0111] Pane e cereali      101.6    100.6    101.1
4                                [0112] Carni      102.9    102.4    102.6

    2018-04 2018-05 2018-06 2018-07 2018-08 2018-09 ... 2024-09 2024-10 \
0    102.9    103.2    103.4     102    101.8    103.5 ...     123    123.4
1    103.6    104.3    103.9    103.1    103.1     103 ...    130.8    132.3
2    103.7    104.5    104.2    103.2    103.2    103.2 ...    131.2    132.9
3    101.8    101.4     102    101.7    102.1    101.3 ...    127.2    127.6
4    102.9    102.7    102.8    102.8    102.7     103 ...    125.6    125.9

    2024-11 2024-12 2025-01 2025-02 2025-03 2025-04 2025-05 2025-06
0    123.3    123.4    122.4    122.5    124.4    124.9    124.8     125
1    133.3    132.6    133.8    133.7    133.8    134.8    135.4    135.7
2    133.8      133    134.1     134     134    134.9    135.5       ..
3    127.8    127.8    128.5    128.2    128.4    129.2    129.3       ..
4    126.7     127    127.9     128    128.7    129.5    130.2       ..

[5 rows x 91 columns]

```

```
df['weights'].head()
```

```

                                Tempo    2015    2016 \
0                                [00] Indice generale  1000000  1000000
1  [01] -- prodotti alimentari e bevande analcoli...  175648  176326
2                                [011] Prodotti alimentari  162005  162805
3                                [0111] Pane e cereali    30036   30342
4                                [0112] Carni    41803   40944

```

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	2017	2018	2019	2020	2021	2022	2023	2024	\
0	1000000	1000000	1000000	1000000	1000000	1000000	1000000	1000000	
1	175240	175418	173257	172583	205912	194554	181443	181801	
2	161810	161903	159432	158644	189091	179008	166582	167112	
3	29853	29558	29717	29778	35767	33586	31994	31422	
4	40876	39914	39286	38162	45695	43159	39770	40253	
	2025								
0	1000000								
1	181425								
2	166336								
3	31513								
4	40080								

```

# Set 'Tempo' as index
# df = df.set_index('Tempo')

# Transpose the DataFrame
df_T = df.transpose()

# Create a figure
fig = go.Figure()

# Add a trace for each row (now a column in df_T)
for column in df_T.columns:
    fig.add_trace(go.Scatter(
        x=df_T.index,
        y=df_T[column],
        mode='lines',
        name=column[:50]
    ))

# Customize layout
fig.update_layout(
    title='IPCA price indices - 2015:100',
    xaxis_title='Time',
    yaxis_title='Value',
    # xaxis_tickangle=-45,
    # hovermode='x unified',
    # template='plotly_white',
    height=600,
    width=1000,
    # legend=dict(orientation="v", x=1.02, y=1)
)

fig.show()

```

```

#> Extract code and label
ddf = {}

ddf = pd.DataFrame()
ddf['code'] = df['weights']['Tempo'].str.extract(r'([\d+\\])')
ddf['label'] = df['weights']['Tempo'].str.strip()

```

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```

#> Determine parent code
def get_parent_code(code):
    if code is None or pd.isna(code):
        return None
    code_str = str(code).strip('[]')
    if len(code_str) <= 2:
        return None # no parent
    elif len(code_str) == 3:
        return f"[{code_str[:2]}]"
    elif len(code_str) == 4:
        return f"[{code_str[:3]}]"
    else:
        return None

#> Determine parent code
def get_value(code):
    if code is None or pd.isna(code):
        return None
    code_str = str(code).strip('[]')
    if len(code_str) == 4:
        return int(1)
    else:
        return int(0)

ddf['parent'] = ddf['code'].map( get_parent_code )
# ddf['value'] = ddf['code'].map( get_value )
ddf['value'] = df['weights']['2025'] / 1e4

#> Drop [00] Indice generale
ddf = ddf[ddf['code'] != '[00]']

ddf.head(30)

# # Step 4: Map parent code to label
# code_label_map = dict(zip(df['code'], df['label']))
# df['parent_label'] = df['parent_code'].map(code_label_map)

# # Step 5: Full parent id
# df['parent'] = df['parent_code'] + ' ' + df['parent_label']
# df['parent'] = df['parent'].where(df['parent_code'].notnull()) # top-level parent_
↳ stays NaN

```

	code		label	parent	value
1	[01]	[01] -- prodotti alimentari e bevande analcoliche		None	18.1425
2	[011]		[011] Prodotti alimentari	[01]	16.6336
3	[0111]		[0111] Pane e cereali	[011]	3.1513
4	[0112]		[0112] Carni	[011]	4.0080
5	[0113]		[0113] Pesci e prodotti ittici	[011]	1.2412
6	[0114]		[0114] Latte, formaggi e uova	[011]	2.5141
7	[0115]		[0115] Oli e grassi	[011]	0.6514
8	[0116]		[0116] Frutta	[011]	1.4763
9	[0117]		[0117] Vegetali	[011]	2.4341
10	[0118]	[0118] Zucchero, confetture, miele, cioccolato...		[011]	0.8321
11	[0119]	[0119] Prodotti alimentari n.a.c.		[011]	0.3251

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12	[012]	[012] Bevande analcoliche	[01]	1.5089
13	[0121]	[0121] Caffè, tè e cacao	[012]	0.5413
14	[0122]	[0122] Acque minerali, bevande analcoliche, su...	[012]	0.9676
15	[02]	[02] -- bevande alcoliche e tabacchi	None	3.1911
16	[021]	[021] Bevande alcoliche	[02]	1.0174
17	[0211]	[0211] Alcolici	[021]	0.1377
18	[0212]	[0212] Vini	[021]	0.5587
19	[0213]	[0213] Birre	[021]	0.3210
20	[022]	[022] Tabacchi	[02]	2.1737
21	[03]	[03] -- abbigliamento e calzature	None	6.7911
22	[031]	[031] Abbigliamento	[03]	5.7829
23	[0312]	[0312] Indumenti	[031]	5.2618
24	[0313]	[0313] Altri articoli d'abbigliamento e access...	[031]	0.2103
25	[0314]	[0314] Servizi di lavanderia, riparazione e no...	[031]	0.3108
26	[032]	[032] Calzature	[03]	1.0082
27	[0321]	[0321] Scarpe ed altre calzature	[032]	0.9866
28	[0322]	[0322] Riparazione e noleggio calzature	[032]	0.0216
29	[04]	[04] -- abitazione, acqua, elettricità e combu...	None	12.6003
30	[041]	[041] Affitti reali per abitazione	[04]	2.9507

```
fig = px.sunburst(
    ddf,
    names='code',
    parents='parent',
    values='value',
    hover_data = ['label'],
    title='IPCA weights - 2025',
    branchvalues="total" # "toatal" or "remainder"
)
fig.show()
```

```
import plotly.graph_objects as go

years = [str(y) for y in range(2018, 2026)] # list of year strings

for year in years:
    ddf[str(year)] = df['weights'][str(year)] / 1e4

# Create the initial figure for the first year
fig = go.Figure()

fig.add_trace(go.Sunburst(
    ids=ddf['code'],
    labels=ddf['code'],
    parents=ddf['parent'],
    values=ddf['2025'], # initial year
    hoverinfo='label+value+text',
    branchvalues="total", # "toatal" or "remainder"
    sort=False,
    text=ddf['label'],
))
fig.update_layout(title="IPCA weights - 2025")
```

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```

# Create one frame per year
frames = []
for year in years:
    frames.append(go.Frame(
        data=[go.Sunburst(
            ids=ddf['code'],
            labels=ddf['code'],
            parents=ddf['parent'],
            values=ddf[year],
            branchvalues="total", # "toatal" or "remainder"
            sort=False,
            text=ddf['label']
        )],
        name=year,
        layout=go.Layout(title_text=f"IPCA weights - {year}")
    ))

fig.frames = frames

# Add slider steps for each year
steps = []
for year in years:
    steps.append(dict(
        method='animate',
        args=[[year], # frame name
              dict(mode='immediate',
                    frame=dict(duration=500, redraw=True),
                    transition=dict(duration=300))],
        label=year
    ))

# Layout with slider
fig.update_layout(
    width=800, height=800,
    margin=dict(t=50, l=0, r=0, b=0),
    sliders=[dict(
        active=years.index('2025'),
        currentvalue={"prefix": "Year: "},
        pad={"t": 50},
        steps=steps
    )],
)

fig.show()

```


POLICY

	Monetary Policy	Fiscal Policy
Controlled by	CB	Government
Main tools	IR, Money supply	Taxes, Spending, Transfers
Speed	Usually faster	Politically slower, debated
Focus	Inflation, lliquidity, credit	Employment, Income distribution
Independence		

6.1 Monetary policy

6.2 Fiscal policy

Part III

Investing Principles

INTRODUCTION TO PRINCIPLES OF INVESTING

Investing is a core part of personal financial management—it's how individuals navigate uncertainty to meet their financial goals under real-world constraints. The most basic objective is to preserve the real value of wealth, protecting it against *inflation*; more ambitious goals include growing capital to fund retirement, education, or other life plans.

Sound investing requires understanding *return* and *risk* of available assets, and the fundamental *R/R trade off*. It also demands attention to **constraints** such as *liquidity* needs, *time horizon*, *acceptable volatility*, and *risk tolerance*. One of the main principle is *diversification* - which can reduce risk and, in some cases, enhance returns.

This section introduces the core concepts needed to build a robust investment strategy: how *compound returns* shape long-term growth, how *volatility drag* reduces expected performance, and how a clear, principle-based approaches - like *rebalancing* - may improve performance under uncertainties.

Given its set of constraints, an informed and intelligent agent, see *Portfolio construction* would take actions that try to maximise return for a given accepted risk, or minimize risk for a given desired return: this behavior can be summarized in choosing actions on a *Pareto front*, i.e. within the set of all Pareto efficient solutions.

Sections

Section	Key Concepts
1. <i>Return</i>	
2. <i>Risk</i>	
3. <i>Risk-Return Trade-Off</i>	
4. <i>Diversification</i>	
5. <i>Portfolio Construction</i>	
6. <i>Time and Compounding</i>	Compounding and volatility drag
7. <i>Disciplined Investing</i>	PIC/PAC, rebalancing,...

7.1 Return

Return is the reward for investing. It can come from **capital gain** (price increase of assets bought), or **periodic cashflows**, like interest (from bonds), or dividends (from stocks). Some assets produce predictable return (either nominal, or real), other assets have less predictable returns. Any asset has some level of uncertainty, or *risk*¹.

Most returns are quoted on a **per-period** basis - usually annually - and expressed as the percentage of the reward over the initial amount of the investment.

Example 7.1.1 (1-period returns)

An amount of 1000€ in saving account returning 2% per year, returns $0.02 \cdot 1000\text{€} = 20\text{€}$ at the end of the year, so that the amount in the saving account becomes $1000\text{€} \cdot 1.02 = 1020\text{€}$. Usually some *costs* must be also considered. ...

Example 7.1.2 (1-period return of equity investment)

...given costs, dividends, taxes, buying and selling prices, evaluate return...

For a many-year investment, single-period returns *compound* over time.

7.1.1 Costs

While return are uncertain, at least to a certain level, usually costs - fees, expenses, taxes - or part of them, are certain. With equal other conditions, the intelligent investor should reduce costs (known), as higher costs reduce returns w/o changing the level of risk.

7.2 Risk

Risk measures uncertainty and its effects, combining probability of events and consequences of specific events. *All the assets have some systematic and some specific risks*.

Key measures (*should give info about magnitude, frequency/probability, and duration*) include:

- standard deviation or **volatility**: how much returns may deviate from their expected value),
- max loss (usually 100% can't be neglected for catastrophic although rare events), value at risk (VaR, max loss with a given probability), drawdown (maximum peak-to-trough loss)
- time-to-recover (time to recover drawdowns, in a temporal perspective)

Usually, risk metrics measure uncertainty, without discerning from positive and negative events: these metrics perceive a higher-than-expected return as a risk as well. Some metrics instead, see *Sortino ratio* in *risk-return* section, aims at quantifying only negative events as risk.

Example 7.2.1 (Value at Risk)

A 1-year 5% VaR of 1000€ of an investment it means that there's 5% probability of losing at least 1000€ in a year with that investment.

¹ Even the most safe assets could undergo some (really) **rare**, but usually (really) **catastrophic events**. Just as an example, it's hard to imagine what could happen even to bonds issued by the most (perceived and priced) safe government or institution, in case of its participation in a war.

7.3 Risk-Return Trade Off

“There’s no free lunch”

Higher expected returns usually come with higher risk.

...but high risk doesn’t imply high expected return

Very stupid actions usually implies poor return with high risk. Just as an example, playing Russian roulette for fun implies an expected return worse than an alternative “do-nothing and have an ice-cream instead” scenario (at least, if your goal is not to kill yourself, and your return function does not positively weight this outcome) with higher uncertainty on the final status of your health.

Sometimes the same could happen if one plays doing trading with some random meme-stocks or shit-coins.

Risk-adjusted return provides an indication of the expected return per unit of risk. Common metrics are:

- **Sharpe ratio**, comparing excess return and volatility compared with a “risk-free” asset - or a benchmark

$$S := \frac{\mathbb{E}[R - R_b]}{\sqrt{\text{var}[R - R_b]}}$$

- **Sortino ratio**

$$So := \frac{\mathbb{E}[R] - T}{\text{DR}},$$

with T target return, and DR the downside deviation, i.e. the deviation w.r.t the target return evaluated only for returns r lower than the target return T

$$\text{DR}^2 = \int_{r=-\infty}^T (T - r)^2 f(r) dr,$$

being $f(r)$ the probability density function of the (continuous) random variable R representing return

Example 7.3.1

7.4 Diversification

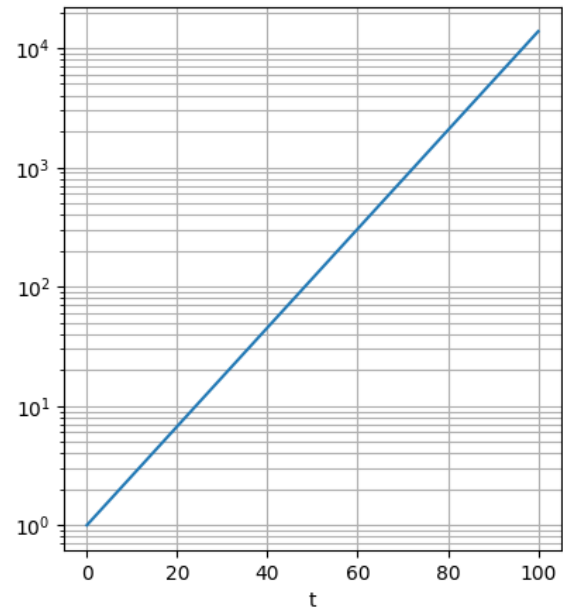
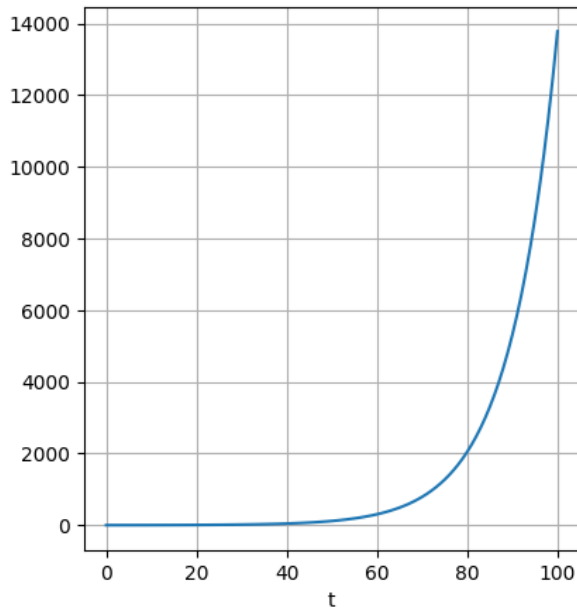
Diversification spreads risk across different investments so no single event can ruin your portfolio. Diversification works well with assets that are not - or at least they’re loosely - correlated: in this case, diversification could increase return per unit of risk.

7.5 Portfolio Construction

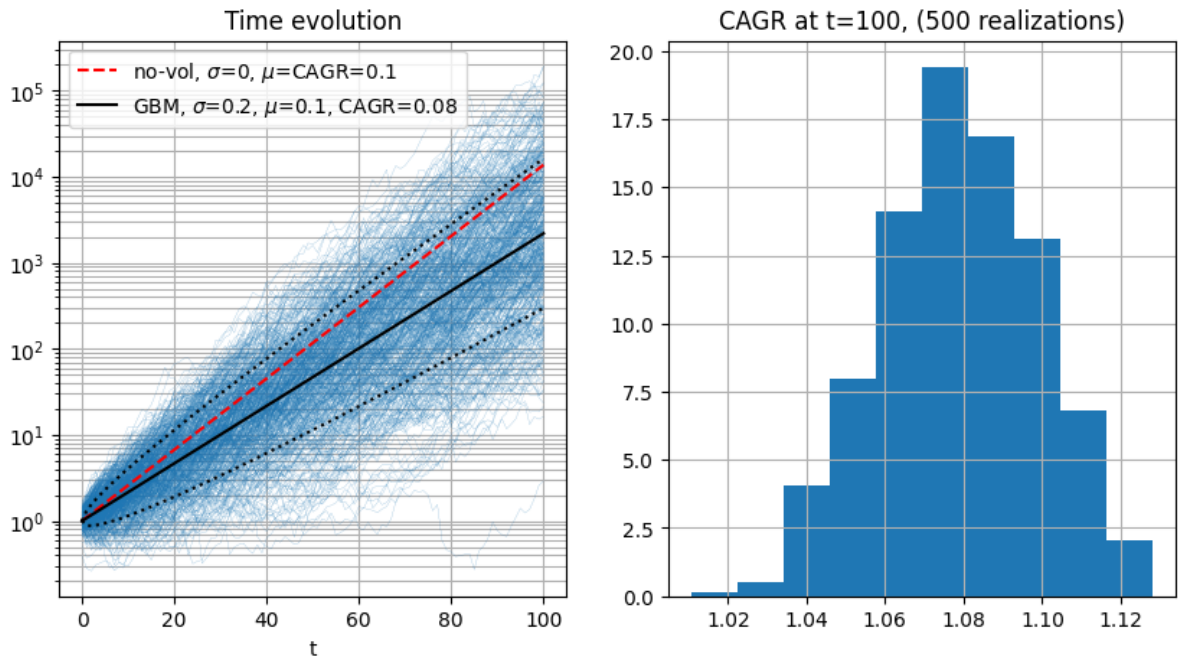
7.6 Time

7.6.1 Compound Return

```
(Text(0.5, 0, 't'), None)
```



Volatility Drag



todo

- “Time and risk?” *Listen to The Logic of Risk*

7.7 Disciplined Investing

7.7.1 Rebalancing

Colab Notebook, [rebalancing.ipynb](#)

Rebalancing premium

REBALANCING

In this Notebook, two strategies on a 2-asset portfolio are discussed and compared:

- **rebalanced portfolio**, after each period
- **buy-and-hold portfolio**, without rebalancing

Effects of rebalancing and conditions for **rebalancing premium** are discussed: sometimes the expected log-return of the rebalanced portfolio may exceed the expected log-return of each single asset.

8.1 Libraries, parameters and useful functions

Libraries are imported and useful functions to treat conics below are defined here

8.1.1 Libraries

8.1.2 Parameters

8.1.3 Functions for conics

8.2 Rebalanced portfolio

Let the **1-period return** of the assets be normal (**todo** is this necessary? Can't one rely on central limit theorem? How long the summation must be for convergence to normal distribution, in presence of **heavy-tails** distribution? If one can't rely on central limit theorem, let use numerical methods to investigate the effect of heavy tails distributions),

$$\mathbf{r} \sim \mathcal{N}(\mu, \sigma^2) .$$

Compound return of the portfolio has **expected value**

$$\mu_p^c = \mathbb{E}[r_p^c] = \mathbf{w}^T \mu - \frac{1}{2} \mathbf{w}^T \sigma^2 \mathbf{w}$$

and **variance**

$$\sigma_{r_p^c}^2 = \mathbb{E}[(r_p^c - \mu_p^c)^2] = \dots = \mathbf{w}^T \sigma \mathbf{w}$$

8.2.1 Shannon demon

Sometimes the expected value of the compound return of the rebalanced portfolio can be larger than the expected return of each asset class.

$$\mu_k^c = \mathbb{E}[r_k^c] = \mu_k - \frac{\sigma_k^2}{2}$$

Example: 2-asset portfolio. As an example, the expected value of the compound return of a 2-asset rebalanced portfolio,

$$\mathbb{E}[r_p^c] = w_1\mu_1 + w_2\mu_2 - \frac{1}{2}(w_1^2\sigma_1^2 + 2w_1w_2\rho\sigma_1\sigma_2 + w_2^2\sigma_2^2)$$

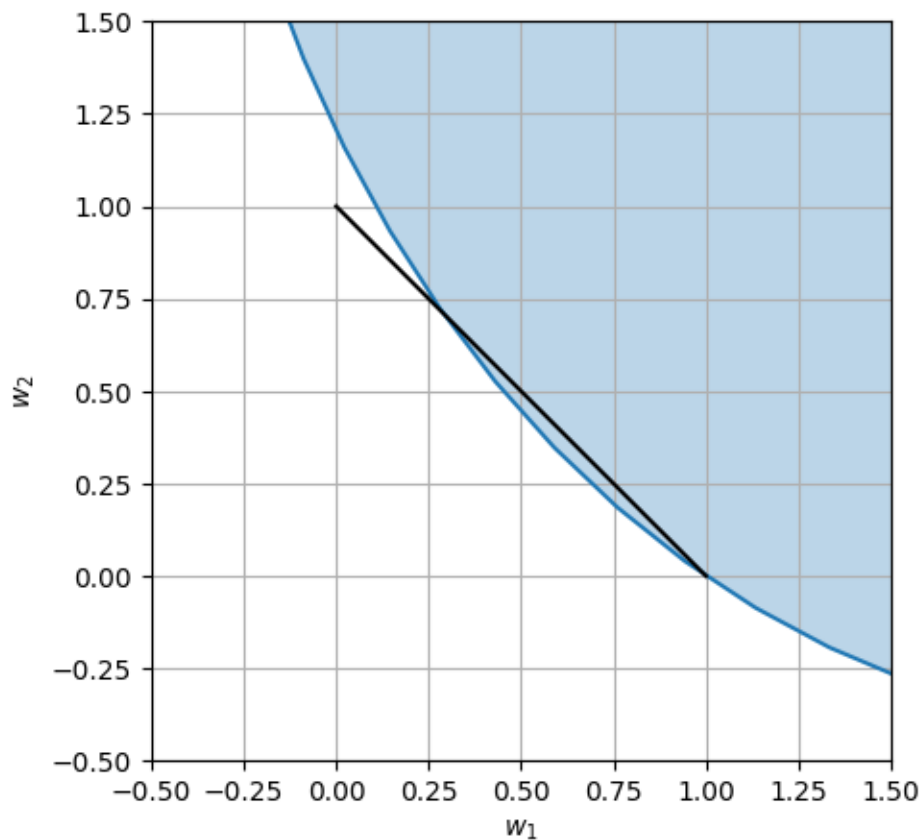
Using w_1, w_2 as independent variables, for any value of the expected return, the expression of the return itself can be represented as a **conic section** in the w_1, w_2 -plane. In particular,

- for $\rho \neq 1$, it's an **ellipse** ($\Delta = B^2 - 4AC < 0$),
- for $\rho = 1$, it's a **parabola** ($\Delta = 0$)

Portfolio allocation. Some constraints may hold on portfolio allocation:

- fully-invested: $w_1 + w_2 = 1$
- no short-selling: $w_1, w_2 \geq 0$
- no leverage: $w_1, w_2 \leq 1$

```
interactive(children=(FloatSlider(value=-0.25, description='rho', max=1.0, min=-1.0, step=0.01), FloatSlider(v...
```



This plot represents in **blue** asset allocations of the balanced 2-asset portfolio with expected value of the compound return larger than the compound return of any individual asset. **Black line** represents all the possible allocations of a fully invested portfolio, $w_1 + w_2 = 1$ with no leverage $w_k \leq 1$ and not short selling $w_k \geq 0$.

8.3 Comparison of portfolios: realizations of stochastic processes

In this section, rebalanced portfolio and buy-and-hold portfolio are compared. Different realizations of these two portfolio strategies are built, and used to build statistics, and discuss their properties in terms of **compound return**, **drawdowns**,...

Note. Here, 1-period returns are modelled as *normal random variable* so far. Anyways, it's possible (and suggested) to implement the most suited random process for modelling the return of the desired assets.

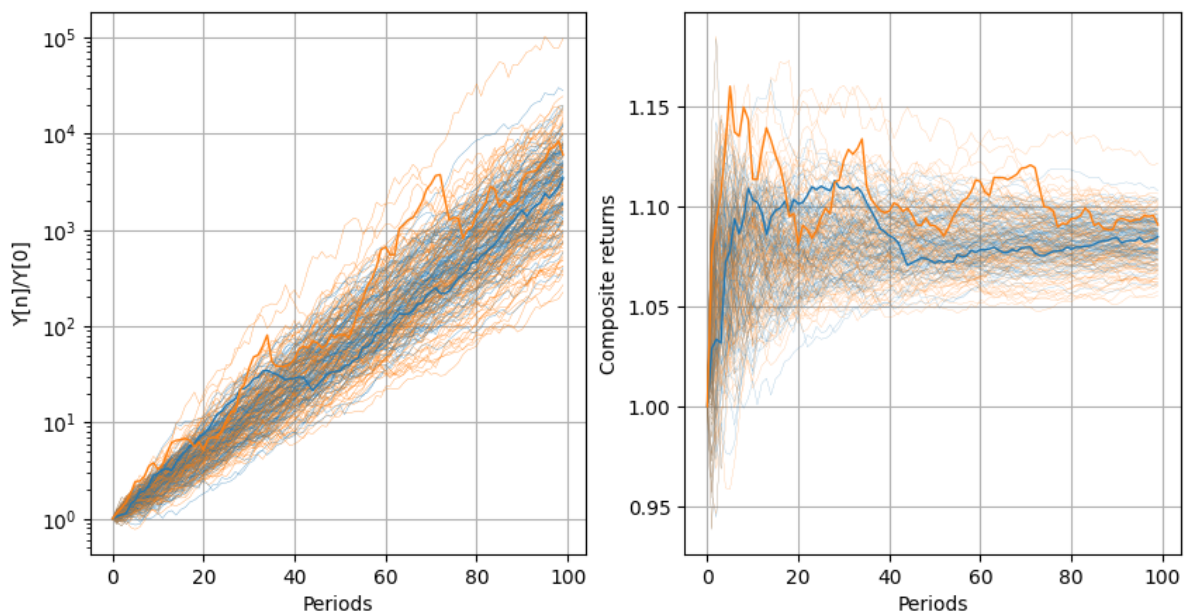
8.3.1 Useful functions

A useful function is introduced here to build correlated random variables with the desired expected values and covariance.

Main Colab notebook can be found here: https://colab.research.google.com/drive/1n5py0Zf8i3_jrTTk0AR7Noq2kBYwpaqx?authuser=1#scrollTo=gmbjbprjCHto

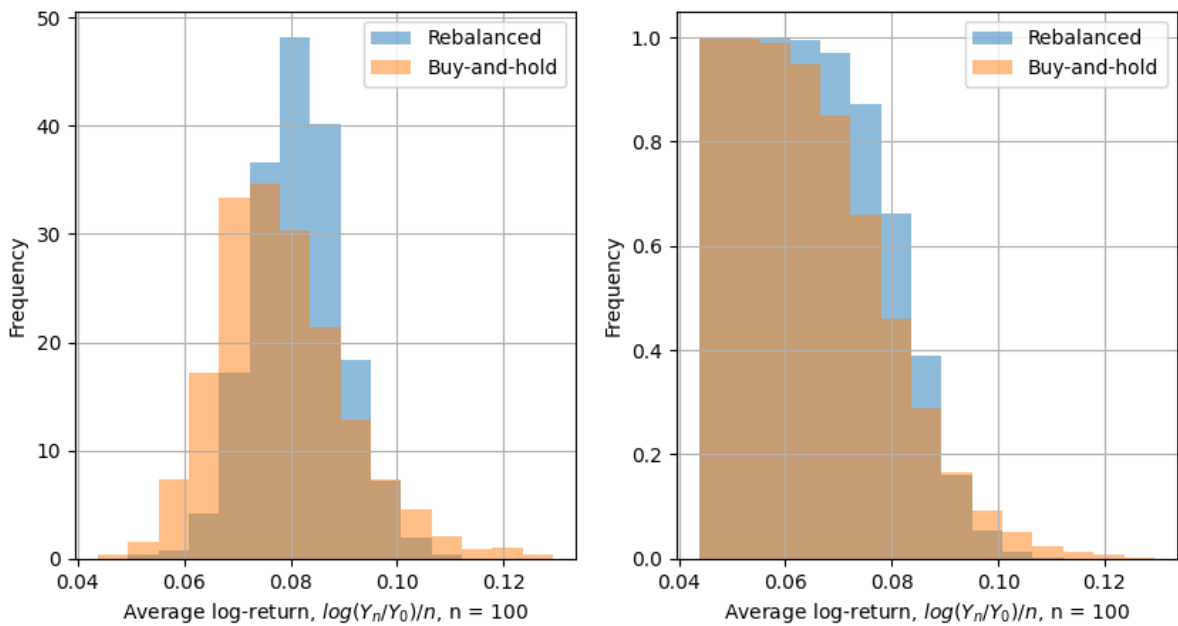
8.3.2 Realizations

```
[<matplotlib.lines.Line2D at 0x7fe290ffa0>]
```



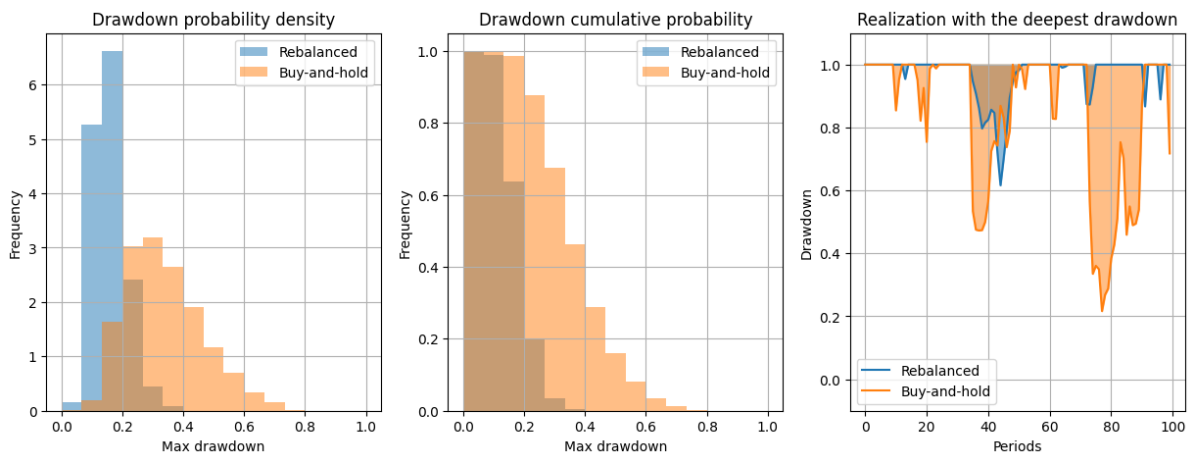
8.3.3 Composite return

```
Rebalanced portfolio. Compsite return
Exp. value: 0.085
Std. dev. : 0.009
Buy-and-Hold portfolio. Compsite return
Exp. value: 0.081
Std. dev. : 0.013
```



8.3.4 Maximum drawdown

```
Text(0.5, 1.0, 'Realization with the deepest drawdown')
```



SEQUENCE RISK

9.1 Introduction

Sequence risk occurs when investment or withdrawal is distributed in time. These two scenarios may be representative of:

- Dollar Cost Averaging (**DCA**, or **PAC** in Italian for “Piano di Accumulo di Capitale”)
- **Withdrawal** during old age

Sequence in time of 1-period returns may strongly influence the composite return of a portfolio.

9.1.1 Mathematical model

In a continuous-time model, sequence risk of constant-amount DCA or withdrawal can be modeled with a Geometric Brownian Motion with “drift”,

$$dX_t = \mu X_t dt + \sigma X_t dW_t + C dt ,$$

being C_t the rate of investment (> 0) or withdrawal (< 0), μ, σ the expected value and variance of the rate of return. A discrete-time counterpart may be

$$\Delta X_{n,n+1} = (\mu_{n,n+1} + \sigma_{n,n+1} W_{n,n+1}) X_n + C_{n,n+1} ,$$

with $\mu_{n,n+1}, \sigma_{n,n+1}$ the expected value and the variance of the 1-period return, $W_{n,n+1}$ a unit-variance random variable representing the distribution of the returns from n to $n + 1$, and $C_{n,n+1}$ the investment of withdrawal from n to $n + 1$.

9.1.2 Constant investment or withdrawal rate: analytical solution

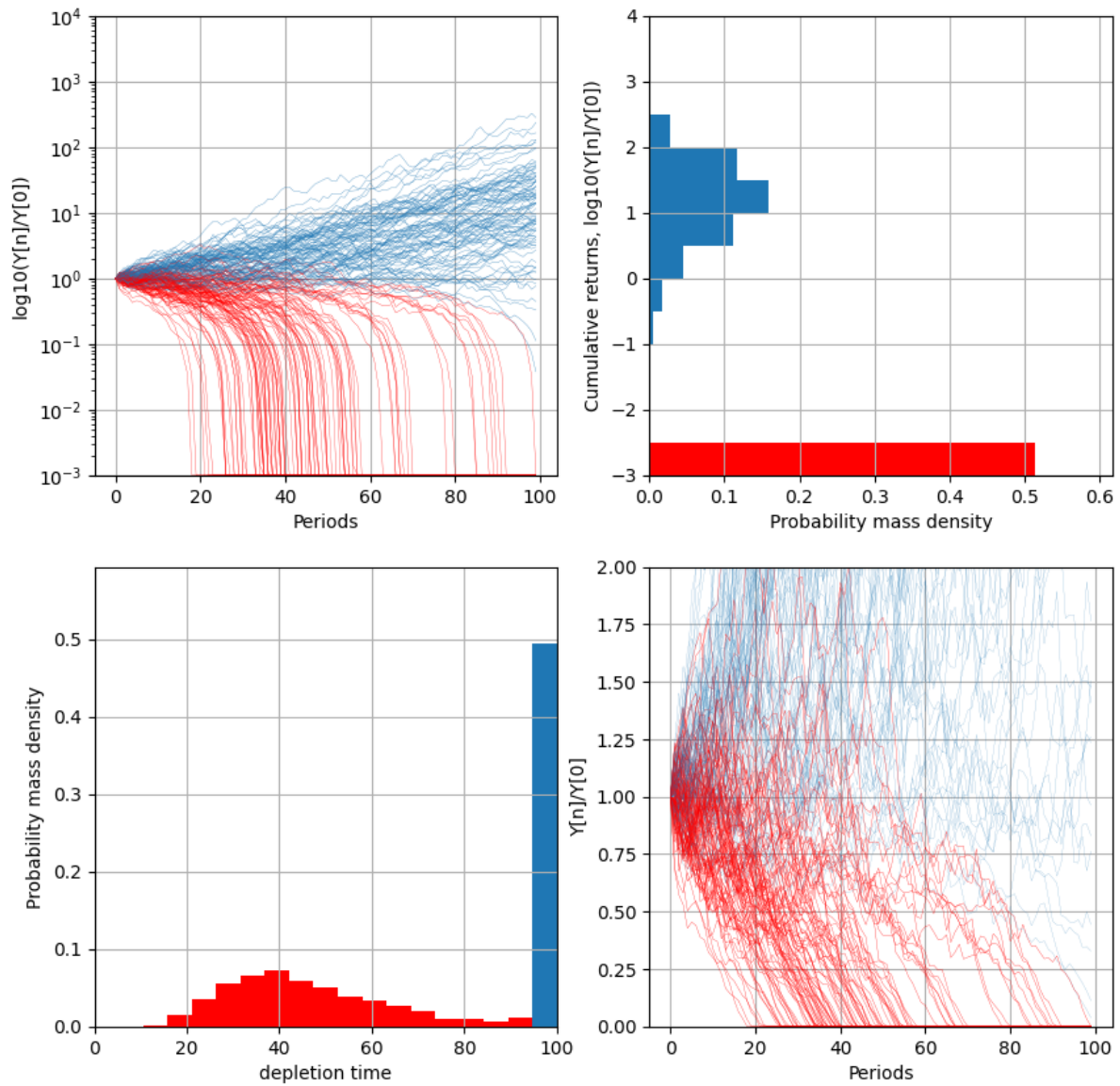
The solution of the continuous-time equation with reads

$$X_t = X_0 e^{\left(\mu - \frac{\sigma^2}{2}\right)t + \sigma W_t} + C \int_{s=0}^t e^{\left(\mu - \frac{\sigma^2}{2}\right)(t-s) + \sigma(W_t - W_s)} ds$$

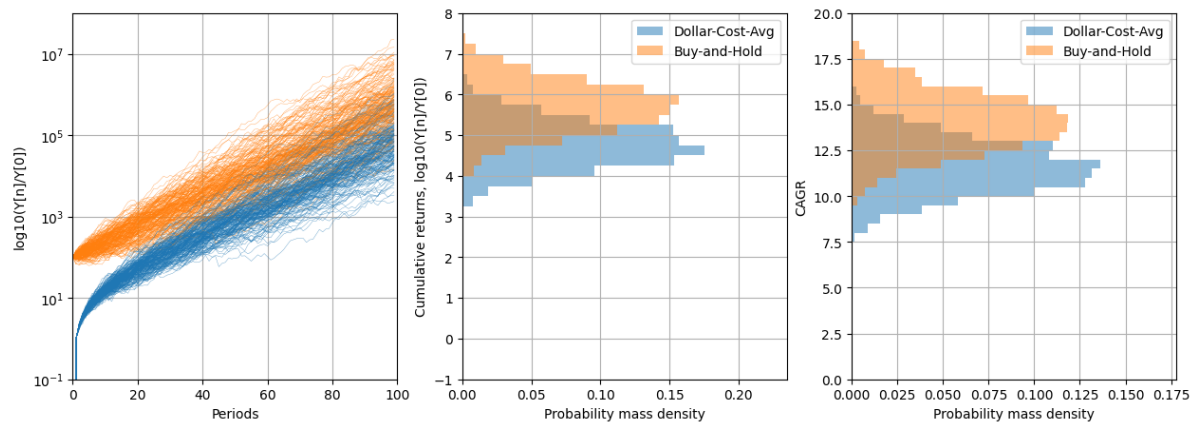
9.2 Realizations

9.2.1 Libraries and parameters

9.2.2 Constant Withdrawals



9.2.3 Dollar Cost Averaging (DCA)



Part IV

Asset classes

INTRODUCTION TO ASSET CLASSES

BONDS

...

Here the most general expression for nominal and real **yield** are derived as a function of prices, face value of coupon, taxation and year to maturity, both in case of coupon reinvestment or not (reinvestment not always possible); a closed form solution is then derived under some assumptions, like constant (or average) rates; the effect on price and yield of credit rating and rating change, coupon, year to maturity are discussed on both examples and real-world cases.

Extra:

- definition of duration
- risks: inflation; reinvestment (at lower rates) for bonds with same maturity and different coupons
- inflation linked

11.1 Constant coupon bonds

11.1.1 W/o reinvestment

At time t_0 the unit price of a bond is p_0 ; investing Y_0 allows to buy $N_0 = \frac{Y_0}{p_0}$ titles; each title has the right of receiving net coupon $C(1-t)$, with t taxation rate, per period (here assumed 1-year coupon range).

$$N_0 = \frac{Y_0}{p_0} = \frac{Y_0}{p_{in}} \frac{p_{in}}{p_0}$$

W/o reinvestment, the number of titles hold is constant and equal to N_0 . As capital Y_i can be written as the product of unit price and number of bond in portfolio, the DCF of a bond w/o coupon reinvestment reads

$$\begin{aligned} \widetilde{DCF} &= -Y_0 + Y_N \prod_{k=1}^N (1+r_k)^{-1} + \sum_{k=1}^N N_0 C(1-t) \prod_{j=1}^k (1+r_j)^{-1} \\ &= N_0 \left[-p_0 + p_N \prod_{k=1}^N (1+r_k)^{-1} + C(1-t) \sum_{k=1}^N \prod_{j=1}^k (1+r_j)^{-1} \right], \end{aligned}$$

This DCF must be corrected a CF at time t_N corresponding to tax on capital gain if $p_N > p_0$, discounted as

$$-N_0(p_N - p_0)t \prod_{k=1}^N (1+r_k)^{-1} \quad (\text{only if } p_N > p_0)$$

The cumulative real return (if the discount ratio is inflation) is the ratio between the DCF and the actual value of the investment Y_0 ,

$$\frac{\widetilde{DCF}}{Y_0} = -1 + \frac{p_N}{p_0} \prod_{k=1}^N (1+r_k)^{-1} + \frac{C}{p_0} (1-t) \sum_{k=1}^N \prod_{j=1}^k (1+r_j)^{-1}$$

If the discount rate is constant, or the average (which average) discount rate is used, the expression of the cumulative return reads

$$\frac{\widetilde{DCF}}{Y_0} = -1 + \frac{p_N}{p_0}(1+r)^{-N} + \frac{C}{p_0}(1-t) \sum_{k=1}^N (1+r)^{-k}$$

11.1.2 W/ reinvestment

Time	Cashflows	Δ Quantity	Quantity	DF
0	$-Y_0$	$N_0 = \frac{Y_0}{p_0}$	$N_0 = \frac{Y_0}{p_0}$	1
1	$+N_0 C(1-t)$			$(1+r_1)^{-1}$
1	$-N_0 C(1-t)$	$N_1 = \frac{N_0 C(1-t)}{p_1}$	$N_{0:1} = N_0 + N_1$	$(1+r_1)^{-1}$
2	$+N_{0:1} C(1-t)$			$(1+r_1)^{-1}(1+r_2)^{-1}$
2	$-N_{0:1} C(1-t)$	$N_2 = \frac{N_{0:1} C(1-t)}{p_2}$	$N_{0:2} = N_0 + N_1 + N_2$	$(1+r_1)^{-1}(1+r_2)^{-1}$
...				
$T-1$	$+N_{0:T-2} C(1-t)$			$\prod_{k=1}^{T-1} (1+r_k)^{-1}$
$T-1$	$-N_{0:T-2} C(1-t)$	$N_{T-1} = \frac{N_{0:T-2} C(1-t)}{p_{T-1}}$	$N_{0:T-1} = \sum_{k=0}^{T-1} N_k$	$\prod_{k=1}^{T-1} (1+r_k)^{-1}$
T	$+N_{0:T-1} C(1-t)$			$\prod_{k=1}^T (1+r_k)^{-1}$
T	$+N_{0:T-1} p_T$			$\prod_{k=1}^T (1+r_k)^{-1}$

All the cashflows from coupons are immediately reinvested so the DCF is

$$\begin{aligned} DCF &= -Y_0 + \underbrace{N_{0:T-1} (p_T + C(1-t))}_{Y_T} \underbrace{\prod_{k=1}^T (1+r_k)^{-1}}_{DF_T} = \\ &= -Y_0 + Y_T DF_T, \end{aligned}$$

with

$$\begin{aligned} N_{0:T-1} &= N_{0:T-2} + N_{T-1} = N_{0:T-2} + N_{0:T-2} \frac{C(1-t)}{p_{T-1}} = N_{0:T-2} \left[1 + \frac{C(1-t)}{p_{T-1}} \right] = \\ &= N_{0:T-3} \left[1 + \frac{C(1-t)}{p_{T-2}} \right] \left[1 + \frac{C(1-t)}{p_{T-1}} \right] = \\ &= \dots = \\ &= N_{0:1} \prod_{k=2}^{T-1} \left[1 + \frac{C(1-t)}{p_k} \right] = \\ &= N_0 \prod_{k=1}^{T-1} \left[1 + \frac{C(1-t)}{p_k} \right]. \end{aligned}$$

Cumulative discounted return reads

$$\begin{aligned}
 \frac{DCF}{Y_0} &= -1 + \frac{Y_T}{Y_0} DF_T = \\
 &= -1 + \frac{N_0}{N_0 p_0} \prod_{k=1}^{T-1} \left(1 + \frac{C(1-t)}{p_k} \right) (p_T + C(t-1)) DF_T \\
 &= -1 + \frac{p_T}{p_0} \prod_{k=1}^T \left(1 + \frac{C(1-t)}{p_k} \right) DF_T \\
 &= -1 + \frac{p_T}{p_0} \prod_{k=1}^T \left(\frac{1 + \frac{C(1-t)}{p_k}}{1 + r_k} \right) .
 \end{aligned}$$

Composite discounted return is obtained, after writing the diiscounted cashflow as the difference between discounted cashflow at time t_T and t_0 , $DCF = Y_T DF_T - T_0$,

$$\begin{aligned}
 (1 + DCAGR)^T &= \frac{Y_T DF_T}{Y_0} = \frac{DCF}{Y_0} + 1 = \frac{p_T}{p_0} \prod_{k=1}^T \left(\frac{1 + \frac{C(1-t)}{p_k}}{1 + r_k} \right) \\
 DCAGR &= \left(\frac{p_T}{p_0} \prod_{k=1}^T \frac{1 + \frac{C(1-t)}{p_k}}{1 + r_k} \right)^{\frac{1}{T}} - 1
 \end{aligned}$$

If¹ price of the bond is constant throughout its whole life, $p_k = 1, \forall k = 0 : T$, and discount rate r is constant, the number of held bonds at time $T - 1$ is

$$N_{0:T-1} = N_0 (1 + C(1-t))^{T-1} ,$$

the discounted cashflow is

$$\begin{aligned}
 DCF &= -N_0 + N_0 (1 + C(1-t))^{T-1} (1 + C(1-t)) (1+r)^{-T} = \\
 &= N_0 \left[-1 + \left(\frac{1 + C(1-t)}{1+r} \right)^T \right] ,
 \end{aligned}$$

cumulative discounted return

$$\frac{DCF}{Y_0} = -1 + \left(\frac{1 + C(1-t)}{1+r} \right)^T$$

and the composite discounted return reads

$$DCAGR = \frac{1 + C(1-t)}{1+r} - 1 .$$

¹ It's a big if. Even if credit rating and inflation are constant throughout the life of the bond, years to maturity decreases and thus - usually - the required rate decreases as well.

EQUITY

Equity valuation is a mix of **common sense**, math, expectations and estimation, and cooking: buying shares of a firm (directly or with a fund) means buying a (tiny) share of the company, a business producing goods and/or services, able to generate earnings/free cash flows. When you hold shares, you're participating to the business and have rights to the profits.

Detailed introduction

Equity valuation blends common sense, mathematics, expectations, estimation—and a bit of art. Buying shares in a company, whether directly or through a fund, means owning a (tiny) stake in a real business that produces goods and/or services and has the potential to generate earnings or free cash flows. As a shareholder, you are not just investing in market prices—you're becoming a part-owner of the enterprise. This ownership entitles you to a share of the company's profits through dividends or capital appreciation. It also comes with certain rights and responsibilities, especially during difficult periods.

When companies face financial stress or pursue growth opportunities, they may issue new shares to raise capital. This can lead to dilution, reducing the percentage ownership of existing shareholders. However, shareholders often have preemptive rights, allowing them to participate in new issuances to maintain their ownership stake. Moreover, owning equity means having a claim on the residual value of the company—what's left after all debts are paid—in both prosperous and challenging times. Understanding these dynamics is crucial to valuing equity: you're not just buying into today's performance, but into a stream of future cash flows and the complex, evolving structure of ownership.

Sensitivity analysis could provide an estimate of the effects of different parameters/assumptions on the final result.

Different valuation methods exist, and can be broadly classified in

- **comparison** approach: P/E, EV/EBITDA, or other indices used to compare companies of the same sector, marked, dimension,...¹
- **intrinsic value** approach, based on **DCF**
- ...other methods for general firms (cost approach,...); valuation of financials;...

¹ It's not always possible to find "equivalent" companies for the comparison...; P/E, EV/EBITDA,... would be projected into the future to keep into account future in the value of a firm.

12.1 Comparison

12.2 Intrinsic value

- Future cash flows are estimated,
- CFs are discounted, usually for the *WACC* (Weighted Average Cost of Capital) to find the *NPV* (net present value) of the **enterprise value** *EV*
- Cash and equivalents are added to the *NPV* to find the **equity value**

WACC

$$WACC = \frac{E}{V}R_e + \frac{D}{V}R_d(1 - t)$$

being R_e the **cost of equity** and R_d the **cost of debt** (maybe the easiest part to estimated accurately, since the debt structure is usually known/programmed). The factor $(1 - t)$ usually appears as interest payments are tax-deductible.

Equity Risk Premium R_e - Sharpe

Following W.Sharpe, equity risk premium can be estimated as

$$R_e = R_f + (R_m - R_f)\beta,$$

being R_f the risk-free rate (usually 10Y US Treasuries), and R_m the annual return of the market/sector of the investment, β is a measure of risk or stock volatility of returns of the investment relative to that of the market/sector.

12.3 Three Financial Statements

Financial statements are written records that illustrates the business activities and the financial performance of a company. In most cases they are audited to ensure accuracy for tax, financing, or investing purposes.

Uses. *Management* uses them for decision-making, budgeting and performance evaluation. *Investors* use them to asses profitability, financial health, future performance, and creditworthiness (especially *lenders*).

- **Income statement:** company performance (profit and loss) over a period. Broadly speaking:

$$\text{net earnings} = (\text{revenues} - \text{total expenses}) \times (1 - \text{tax rate}),$$

with total expenses = operative (labor + non-labor + DA) + Interest (due to debt holders), and “partial earnings” EBITDA, EBIT, EBT with trivial definition (Earnings Before: I:interest, DA: depreciation and amortization, T: tax)

- **Balance sheet:** financial position at a specific point in time, in terms of:
 - assets: cash and equivalent + acc.receiveiv. + inventory + PPE (Plant property and equipment, subject to CapEx and depreciation, $PPE(n) = PPE(n - 1) + \text{CapEx}(n) + \text{DA}(n)$)
 - liabilities: debt + acc.pay.

- equity:

$$\text{retained earnings}(n) = \text{retained earnings}(n-1) + \text{net earnings}(n) - \text{dividends}(n)$$

$$\text{shareholder equity}(n) = \text{equity capital}(n) + \text{retained earnings}(n),$$

being retained earnings(n) the **cumulative** retained earnings not distributed to shareholders.

The 2 contributions shareholder equity, total liabilities shows how the company's asset are financed: either through capital raised or retained earnings (equity), or through debt (liabilities). The **identity**

$$\text{total liabilities} + \text{shareholders equity} = \text{total asset}$$

must hold in a proper filled balance.

- **Cash flow statement** tracks the flows of cash in and out of the business over a period. Cashflows over a period modifies cash,

$$\text{closing cash}(n) = \text{opening cash}(n) + \text{total cashflow}(n)$$

$$\text{opening cash}(n) = \text{closing cash}(n-1)$$

Cashflows are usually classified as:

- operating CF (DA is added back to net income, since it's not a cashflow going anywhere; it lowers income, but it's not a cashflow)
- investing CF
- financing CF

$$\text{Op.CF}(n) = \text{net earnings}(n) + \text{DA}(n) - \Delta \text{WC}(n)$$

$$\text{Inv.CF}(n) = \text{investment in PPE}(n)$$

$$\text{Fin.CF}(n) = \text{issuance of debt}(n) + \text{issuance of equity}(n) - \text{dividends}(n)$$

being $\text{WC}(n) = \text{acc.rec}(n) + \text{inventory}(n) - \text{acc.pay}(n)$ the **working capital**.

CHAPTER
THIRTEEN

ETFS

Part V

Asset allocation

INTRODUCTION TO INVESTING

MODERN PORTFOLIO THEORY

Modern portfolio theory results in a strategy of asset allocation minimizing portfolio risk - measured as volatility - for a given value of the portfolio expected return.

Asset Modeling

A set of N assets is available. Their return (over a defined period)¹ is represented by a multi-dimensional random variable, \mathbf{X} , with expected value and variance

$$\begin{aligned}\bar{\mathbf{X}} &:= \mathbb{E}[\mathbf{X}] \\ \sigma^2 &:= \mathbb{E}[\Delta\mathbf{X} \Delta\mathbf{X}^T]\end{aligned}$$

with $\Delta\mathbf{X} := \mathbf{X} - \bar{\mathbf{X}}$.

Asset allocation. Constraints

A portfolio, without short or leverage positions on these assets, can be represented with the set of weights (proportion) of the assets \mathbf{w} , with

$$\begin{aligned}\sum_n w_n &= 1 \\ 0 \leq w_n \leq 1 \quad , \quad \forall n = 1 : N\end{aligned}$$

Portfolio return

Portfolio return is

$$\mathbf{X} = \mathbf{w}^T \mathbf{X} ,$$

From linearity, its expected value reads

$$\bar{X} = \mathbb{E}[X] = \mathbb{E}[\mathbf{w}^T \mathbf{X}] = \mathbf{w}^T \bar{\mathbf{X}}$$

and its variance

$$\begin{aligned}\sigma^2 &= \mathbb{E}[(X - \bar{X})^2] = \mathbb{E}[\mathbf{w}^T (\mathbf{X} - \bar{\mathbf{X}}) (\mathbf{X} - \bar{\mathbf{X}})^T \mathbf{w}] = \\ &= \mathbf{w}^T \mathbb{E}[\Delta\mathbf{X} \Delta\mathbf{X}^T] \mathbf{w} = \mathbf{w}^T \sigma^2 \mathbf{w}\end{aligned}$$

¹ How to estimate asset return, at least in terms of expected value and variance? And how to estimate correlation of the random variables?

Example 15.1 (Properties of variance matrix)

Covariance matrix is symmetric definite positive. Symmetry readily follows

$$\sigma_{ij} = \mathbb{E} [\Delta X_i \Delta X_j]$$

The matrix is definite positive as

...

Modern Portfolio Theory, as a constrained optimization problem

Modern portfolio theory has its own “optimal” asset allocation $\mathbf{w}^*(\bar{X})$ - with the desired expected return as the parameter, fixed during the optimization - as the asset allocation for which

$$\min_{\mathbf{w}} \sigma^2 \quad \text{s.t.} \quad \begin{aligned} \mathbf{w}^T \bar{\mathbf{X}} &= \bar{X} \\ \mathbf{w}^T \mathbf{1} &= 1 \\ 0 &\leq w_i \leq 1 \end{aligned}$$

CAPITAL ASSET PRICING MODEL

STRATEGIC AND TACTICAL ASSET ALLOCATION

Strategic Asset Allocation, (SAA). SAA is a long-term portfolio strategy, choosing asset class allocation following investor goals and constraints^[^ips]. SAA involves **rebalancing**, to keep deviation from the desired asset allocation and volatility of the portfolio within a desired range.

Tactical Asset Allocation, (TAA). A TAA strategy uses a discretionary or quantitative investment model to take advantage of **inefficiencies or temporary imbalances** among different asset classes.

How many actively managed funds beats the market?

todo

REBALANCING

Reasons.

- risk management:
 - adjust risk for the period of life, and risk-level
 - correct drift towards the asset with highest return, as it affects the

Strategies. In a passive investment strategy, rebalancing should be triggered by some rules, to be applied automatically. As an example:

- periodic rebalancing: rebalancing with constant time interval
- deviation-triggered: rebalancing when asset allocation deviation from the target allocation exceeds a prescribed threshold. E.g. approximately 10% of a 60-40 portfolio going to 65-35 (introduction of episode **152**, as a summary of episode **117**)
- using contributions/withdrawals

Effects of rebalancing. In different situations one of the following effects occurs:

- Volatility is reduced
- Risk-adjusted return improves
- Return of the portfolio is increased

Often, a rebalanced-portfolio return is larger than the weighted average of the returns of the assets of the portfolio. Shannon demon is the mathematical reason for that, *for creating return “out of thin air”*.

Example 18.1 (Shannon demon - on a coin flip)

Starting with 100€, and a fair coin with 50% probability of for each outcome, either H :head or T :tail. If outcome is H you gain 50%, if outcome is T you lose 33.3%.

- If I play with all the money I have, what is the expected amount at the end of the game, for a sufficiently large number of toss?

Now, let's change the strategy: I bet only 50% of the amount I have. What's the expected amount at the end of the game?

Example 18.2 (Nassim Taleb, is the coin fair?)

After 10 tosses with 10 heads, how would you bet on the next toss?

Example 18.3 (Kelly criterion)

Example 18.4 (Does rebalancing improve return, thanks to Shannon demon?)

Yes, for a portfolio with 2 assets with similar returns and low correlation. E.g.:

- **S&P500** and **gold** (50%-50%) from 1972 to 2008 (cherry-picking?): CAGR with annual rebalancing: 10.3%, while S&P: 9.4% and gold: 8.2%.
- S&P500 and gold (50%-50%) from 1972 to 2023 (cherry-picking?): CAGR with annual rebalancing: 10.2%, while S&P: 10.5% and gold: 7.5%, but with lower volatility, lower max drawdown and a better Sharpe ratio
- S&P500 and Treasury (50%-50%) from 1972 to 2023 (cherry-picking?): CAGR with annual rebalancing: 9.3%, while S&P: 10.5% and gold: 6.4%, but with lower volatility, lower max drawdown and a better Sharpe ratio. Without rebalancing: 9.6% (higher!) as equity has much higher return and drift occurs over 50-year period.
- MSCI World and FTSE G7...

No, with 2 assets with 2 assets with very different returns. Anyways, if they have low correlation, rebalancing (may?) reduce volatility, improves risk-adjusted return, or both.

18.1 Resources

- *The Bull*
 - 217. Il modo migliore per Ribilanciare il portafoglio
 - 152. La magia del ribilanciamento e il demone di Shannon
 - 117. Come ribilanciare il portafoglio (e previsioni per i prossimi 10 anni)
- *R.Arnett*. Over-rebalancing
- [market sentiment about Shannon demon](#)

Part VI

Extra

CHAPTER
NINETEEN

EXTRA AND RANDOM

EURISTHICS AND HISTORICAL CORRELATIONS

20.1 Expected returns in the stoch market

20.1.1 Shiller P/E and S&P500 10-year annualised forward returns

- from Invesco, Applied philosophy: The Shiller P/E and the S&P500 returns

20.1.2 Bogle Expected Return Formula

- Comment by *Ben Carlson*, on his website

Part VII

People

RESOURCES, PEOPLE AND FIRMS

21.1 Tools

These tools have not been tested and verified here. I decline any responsibility about their use.

21.1.1 Simple tools for investors

[Simple tools for investors] (<https://www.simpletoolsforinvestors.eu/index.shtml>): **bond** monitor, calculators, tools (minus-eater, laddering,...)

21.1.2 Interactive Asset Allocation - by Research Affiliates

Expected return vs. volatility plot of different asset classes on different time horizons by *Research Affiliates*.

21.1.3 Gregory Gundersen Blog

Gregory Gundersen blog

21.2 People

21.2.1 Arnott, Robert

Founder of *Research Affiliates*.

21.2.2 Faber, Meb(ane)

Co-founder and Chief Investment Officer at *Cambria Investment Management*.

21.2.3 Wigglesworth, Robin

Financial Times' global finance correspondent, author of *Trillions* a book on the past, present and future of passive investing.

21.2.4 Zweig, Jason

Columnist for the Wall Street Journal since 2008. *A Safe Heaven for Intelligent Investor*.

21.2.5 Ritholtz, Barry

21.2.6 Maggiulli, Nick

21.2.7 Carlson, Ben

Director of Institutional Asset Management at *Ritholtz Wealth Management*. Author of the website *A Wealth of Common Sense*

21.2.8 Green, Micheal

Forseen “**Volmageddon**” of the 5 February 2018, the collapse of inverse ETFs or ETP: VIX, SVXY and VMIN, as a consequence of the VIX daily surge from 17 to 37 (approximately +115%, that erased daily inverse products)

Even a moderate (~4%) equity sell-off can unleash devastating volatility swings if the short-vol market is crowded. Rebalancing demands can worsen volatility when liquidity dries up near market close.

- *The Bull*, 192. Micheal Green: perché l'investimento passivo distorce il mercato (e come comportarci)

21.2.9 Yardeni, Edward

21.3 Firms

21.3.1 Reserach Affiliates

Founded by *Robert Arnott*

21.3.2 Cambria Investment Management

Co-founded by *Mebane Faber*

21.3.3 Ritholtz Wealth Management

Barry Ritholtz, Nick Maggiulli, Ben Carlson

THE BULL

“The Bull, il tuo podcast di finanza personale”, Riccardo Spada. [Youtube channel](#)

- Jason Zweig, American financial journalist, columnist for the WSJ since 2008. [Jason Zweig - A Safe Haven for Intelligent Investor](#)
 - **224** what it takes to become an intelligent investor
- Nick Maggiulli, COO for Ritholtz Wealth Management LCC, financial blogger at [Of Dollars And Data - Act Smarter. Live Richer](#). Author of “Just Keep Buying” about the power of compounding.
 - **221** Just keep buying
- Davide Serra, founder and CEO of Algebris Investment
 - **216** The change we’re living and consequences for investors
- William Bernstein, american financial theorist and neurologist
 - **214** The 4 pillars of investing and how to manage risk and uncertainty
- Barry Ritholtz
 - **206** How **not** to invest
- Robin Wigglesworth
 - **203** the case for passive investing: navigative crises through simplicity
- Ben Carlson, Director of Institutional Asset Management at [Ritholtz Wealth Management](#). Author of the webiste [A Wealth of Common Sense](#)
 - **200** Investing is mostly a matter of common sense (and patience)
- Robert Arnott
 - **196** Fundamental investing
- Micheal Green
 - **192** Why passive investing is distorting the markets
 - [Haddad, Valentin](#), associate professor at the UCLA: how competitive is stock market? why is asset demand inelastic?
- Edward Yardeni,
 - **183** Why should we be optimistic?
- Meb Faber,
 - **180** Investing with Common Sense
- Eugene Fama, efficient market, **factor** investing, and factor ETFs

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