

ALGO ASSIGNMENT #02.

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20K-0477

Question # 01

⇒ Brute force ($O(n^2)$):

```
int func (int arr[], int n) {  
    int profit = 0, temp;  
    for (i=0 to n-1) {  
        temp = 0;  
        for (j=0 to n-1) {  
            temp = temp + arr[j];  
            if (temp > profit) {  
                profit = temp;  
            }  
        }  
    }  
    return profit;  
}
```

⇒ Dynamic ($O(n)$):

```
int func (int arr[], int n) {  
    int temp[n];  
    temp[0] = arr[0];  
    for (i=0 to n-1) {  
        if (arr[i] + temp[i-1] > 0) {  
            temp[i] = arr[i] + temp[i-1];  
        }  
        else {  
            temp[i] = arr[i];  
        }  
    }  
    profit = max (profit, temp[i]);  
}  
return profit;
```

Question #02

→ Algorithm $O(n \log n)$:

```
void func (int arr[], int n) {  
    mergesort (arr); → n log n  
    for (i = 0 to n-1) {  
        int temp = arr - unsorted arr[i];  
        if (Binary search (arr, 0, n-1, temp))  
            print result.  
    }.
```

A → Algorithm $O(n)$

→ Push one array in mordered set $\{ \text{int} > \text{temp} \}$.

~~first passes~~
for (i = 0 to arr.length() - 1) {
 if (temp < (value - arr[i]) & temp != end[i])
 print

}

Question #03

→ Binary search

```
int search (int arr[], int l, int h) {  
    if (h >= 1) {  
        mid = (h+1)/2;  
        if (mid == arr[mid])  
            return mid;  
    }
```

}

~~else search (arr, l, mid-1);~~

```
if (mid + 1 <= arr[h]) {
```

```
    result = search (arr, mid+1; h);
```

3.

~~QUESTION 7 = PRACTICE~~

if ($\text{mid} - 1 \geq \text{arr}[\text{i}]$)
return search($\text{arr}, \text{i}, \text{mid} - 1$);

}

return -1;

}

Question # 04 :

```
int func (int arr, int n) {  
    int index;  
    for (i=0 to n-1) {  
        if (arr[i] != 0) {  
            swap (arr[index], arr[i]);  
            index++;  
        }  
    }  
}
```

Question # 05

⇒ Binary Search :

low = 0, ~~high = 9~~, mid = 4.
 $A[\text{mid}] \neq 9 \rightarrow \text{low} = 5$ b/c $A[\text{mid}] < 9$.
low = 5, high = 7, mid = 6.
 $A[\text{mid}] \neq 9 \rightarrow \text{low} = 8$ ~~because~~ b/c $A[\text{mid}] < 9$.
low = 8, high = 9, mid = 8
 $A[\text{mid}] \neq 9 \rightarrow \text{low} = 9$ b/c $A[8] < 9$.
low = 9, high = 9, mid = 9
 $A[9] = 9 \rightarrow \underline{\text{found}}$.

→ Jump Search :

element to be searched \Rightarrow 100

prev = 0, step-size = $\sqrt{100} = 2 \rightarrow \sqrt{100} = 2 \cdot 8 = 2$

$\Rightarrow 1, 4, 5, 6, 9, 10, 11, 100 : \text{arr}[10]$
 $\text{arr}[1] < 100$.

prev = 2, step-size = 4.

$\Rightarrow 1, 4, 5, 6, 9, 10, 11, 100$
 $\text{arr}[3] < 100$

prev = 4, step-size = 6.

$\Rightarrow 1, 4, 5, 6, 9, 10, 11, 100$
 $\text{arr}[6] < 100$

prev = 6, step-size = 8.

Now linear search from prev to step-size.

$1, 4, 5, 6, 9, 10, 11, 100$

$\text{arr}[prev] == 100$

\Rightarrow return $\text{arr}[prev]$

→ Jump Search :

→ less comparison than linear search

→ only works on sorted array

→ worst case complexity $O(\sqrt{n})$

→ If element in beginning then jump search will be faster.

→ Binary Search :

→ less comparisons than linear search

→ needs stack space for recursive method.

→ If element in middle then binary search is faster.

(5) INTERPOLATION SEARCH:

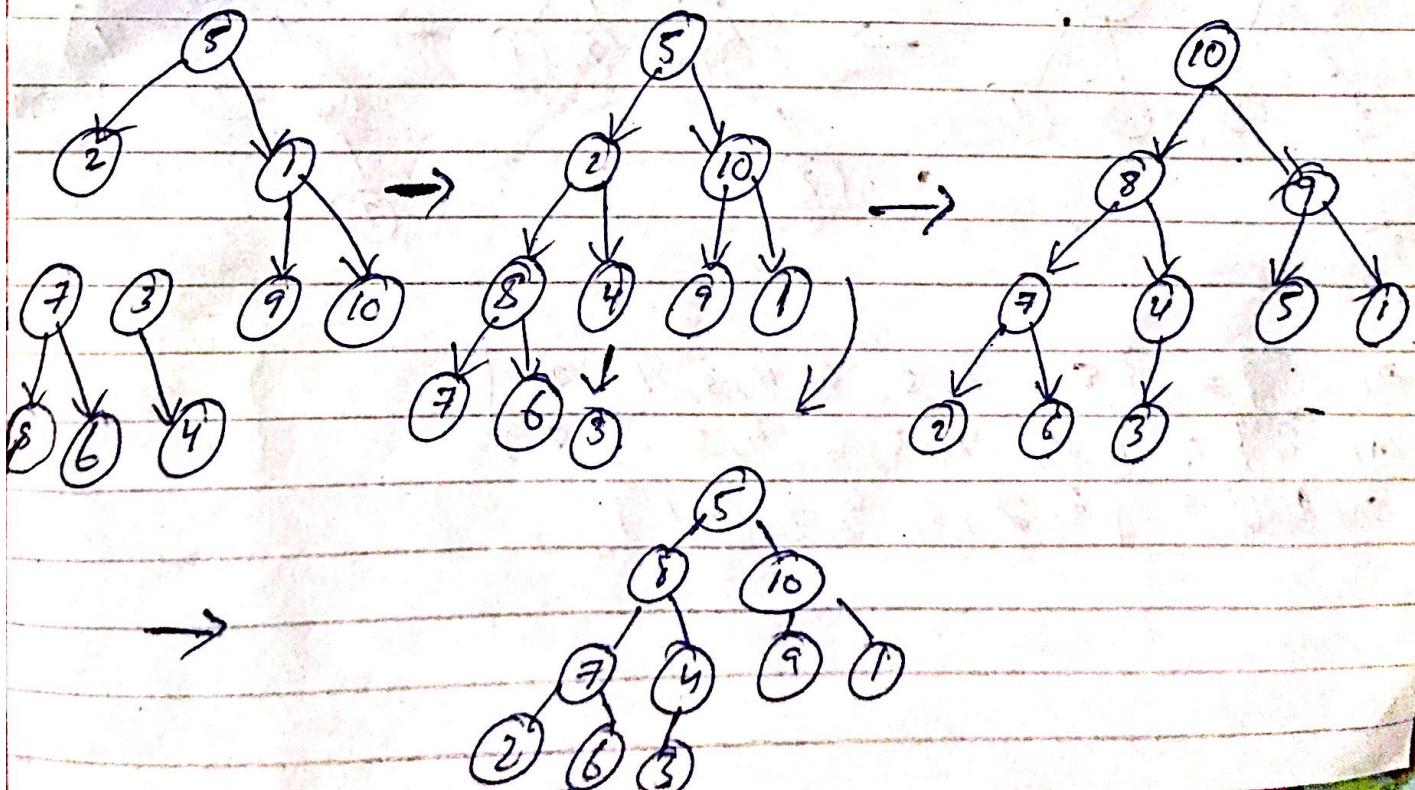
- used when sorted values are evenly distributed.
- creates new pivot values to reduce number of searches. select closest pivot to the value.
- time complexity $\rightarrow O(\log(\log n))$ → average case.
- $O(n)$ → worst case.

Exponential Search:

- find the range where element may lie
- then do binary search
- starts array with 1 element then double it
- keeps on doubling until last element greater than value to find.
- then binary search

Question #06:

$$\text{arr}[10] = \{5, 2, 1, 7, 3, 9, 10, 8, 6, 4\}$$



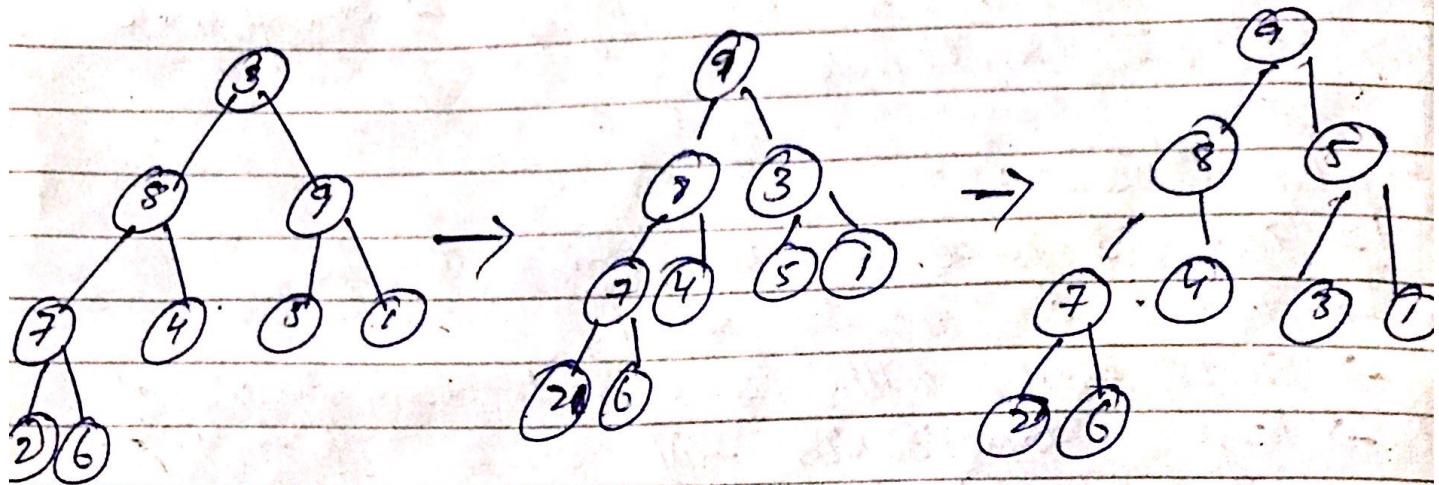
$$\text{arr}[10] = \{10, 8, 9, 7, 4, 5, 1, 2, 6, 3\}$$

\rightarrow Swap first & last element

$$\text{arr}[10] = \{3, 8, 9, 7, 4, 5, 1, 2, 6, 10\}$$

\rightarrow Then remove last when making heap.

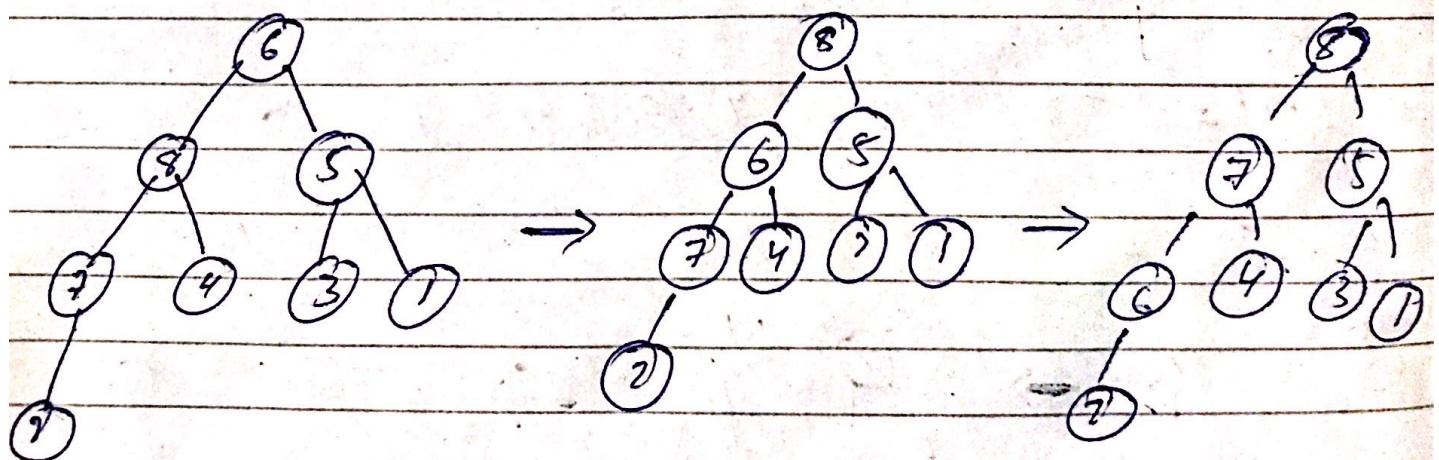
$$\text{arr}[10] = \{8, 8, 9, 7, 4, 5, 1, 2, 6, 10\}$$



$$\text{arr}[\text{arr}] = \{9, 8, 5, 7, 4, 3, 1, 2, 6\}$$

$$\text{arr}[\text{arr}] = \{6, 8, 5, 7, 4, 3, 1, 2, 9\}$$

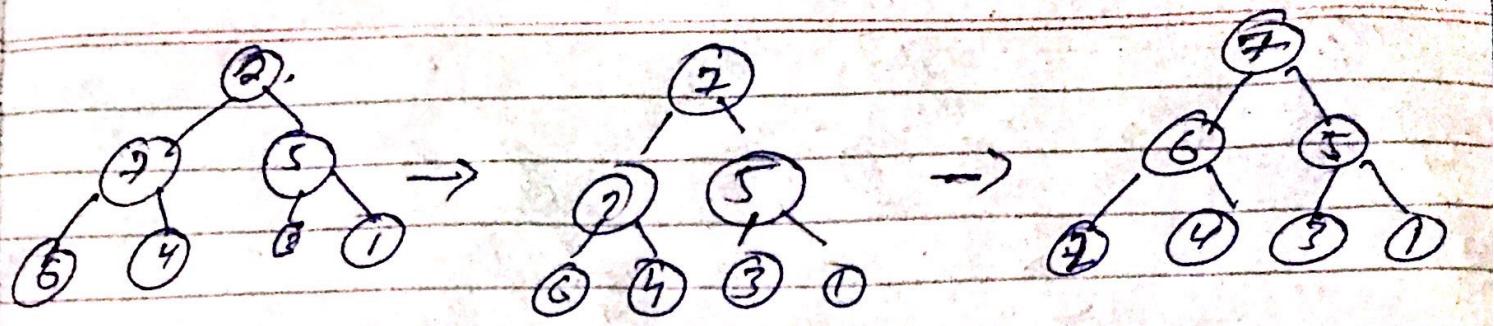
$$\text{arr}[\text{arr}] = \{6, 8, 5, 7, 4, 3, 1, 2\}$$



$$\text{arr}[\text{arr}] = \{8, 7, 5, 6, 4, 3, 1, 2\}$$

$$\text{arr}[\text{arr}] = \{2, 7, 5, 6, 4, 3, 1, 8\}$$

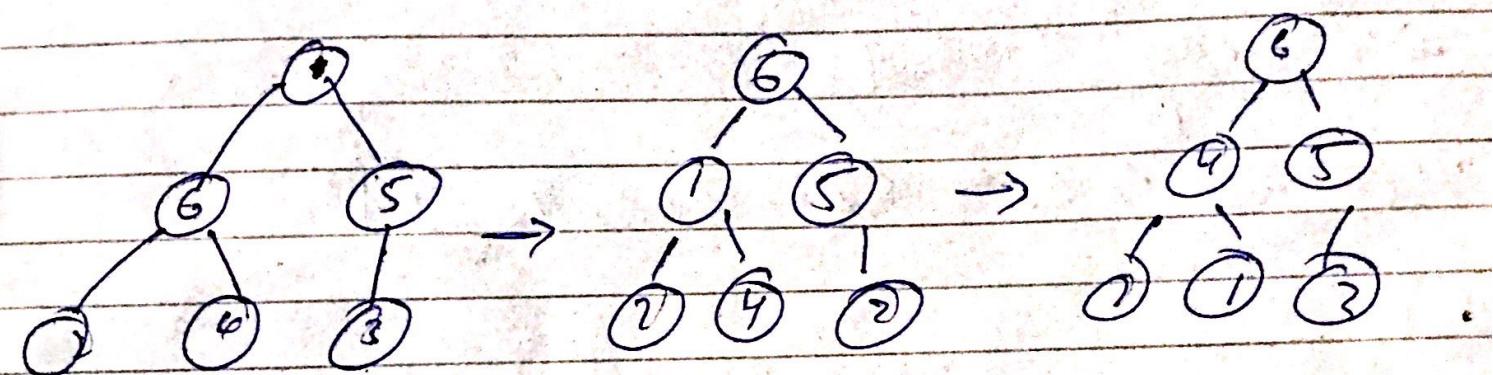
$$\text{arr}[\text{arr}] = \{2, 7, 5, 6, 4, 3, 1\}$$



$$\text{arr} = \{7, 6, 5, 2, 4, 3, 1\}$$

$$\text{arr} = \{1, 6, 5, 2, 4, 3, 7\}$$

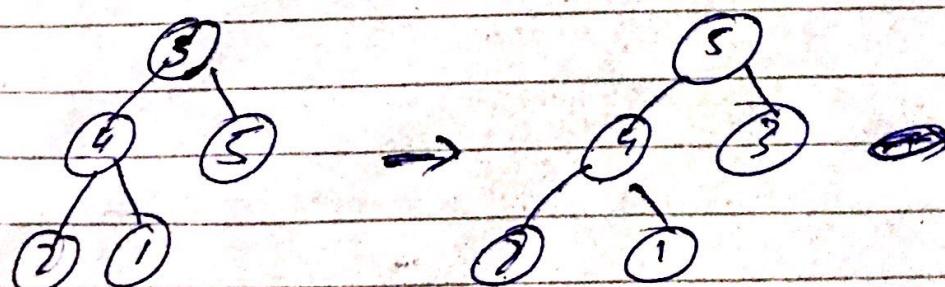
$$\text{arr} = \{1, 6, 5, 2, 4, 3\}$$



$$\text{arr} = \{6, 4, 5, 2, 1, 3\}$$

$$\text{arr} = \{3, 4, 5, 2, 1, 6\}$$

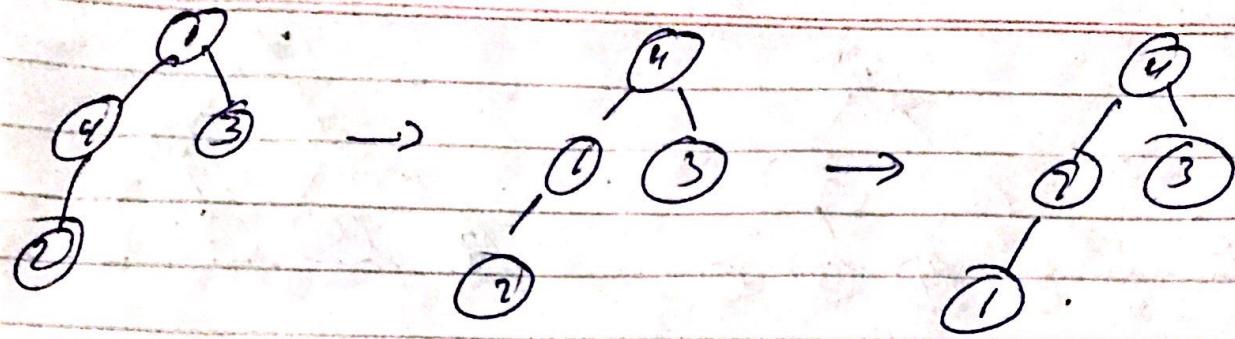
$$\text{arr} = \{3, 4, 5, 2, 1\}$$



$$\text{arr} = \{5, 4, 3, 2, 1\}$$

$$\text{arr} = \{1, 4, 3, 2, 5\}$$

$$\text{arr} = \{1, 4, 3, 2\}$$



~~arr = [4, 2, 3, 1]~~

~~arr = [1, 2, 3, 4]~~

~~arr = [1, 2, 3]~~

⇒ Array Sorted

arr[10] = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]