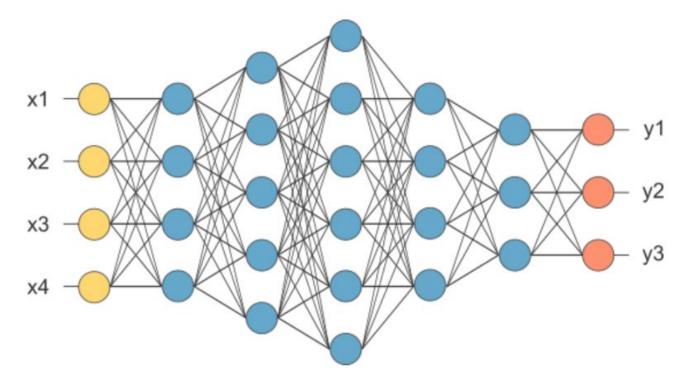
THIS IS CS5045!

GCR:ioc7cdl

Fully Connected Network



This is our fully connected network. If $x_1 x_n$, n is very large and growing, this network would become too large. We now will input one x_i at a time, and re-use the same edge weights.

Examples of sequence data

Speech recognition

Music generation

Sentiment classification

DNA sequence analysis

Machine translation

Video activity recognition

Name entity recognition



"There is nothing to like in this movie."

AGCCCCTGTGAGGAACTAG

Voulez-vous chanter avec moi?

双连旋样

Yesterday, Harry Potter met Hermione Granger. "The quick brown fox jumped over the lazy dog."



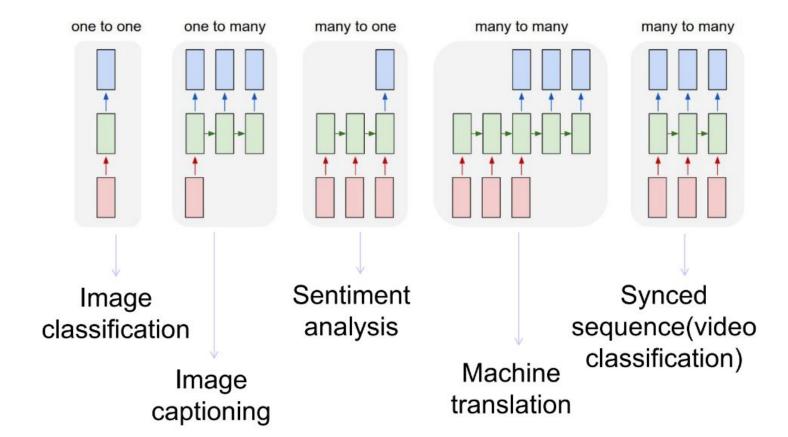
AGCCCCTGTGAGGAACTAG

Do you want to sing with me?

Running

Yesterday, Harry Potter met Hermione Granger. Andrew Ng

Motivation



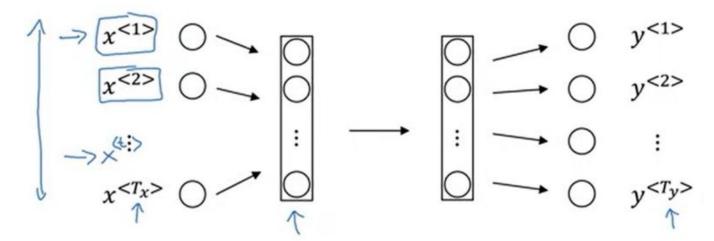
Motivation

 Feed forward networks accept a fixed-sized vector as input and produce a fixed-sized vector as output

fixed amount of computational steps

 recurrent nets allow us to operate over sequences of vectors

Why not a standard network?



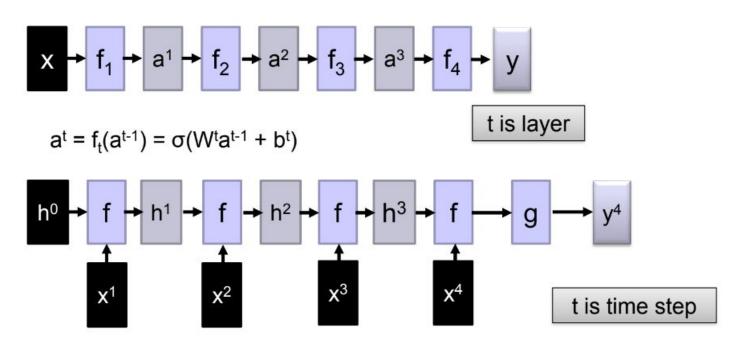
Problems:

- Inputs, outputs can be different lengths in different examples.
- Doesn't share features learned across different positions of text.

Andrew Ng

Feed-forward vs Recurrent Network

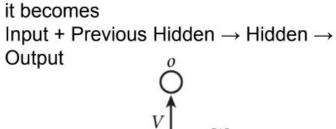
- 1. Feedforward network does not have input at each step
- 2. Feedforward network has different parameters for each layer

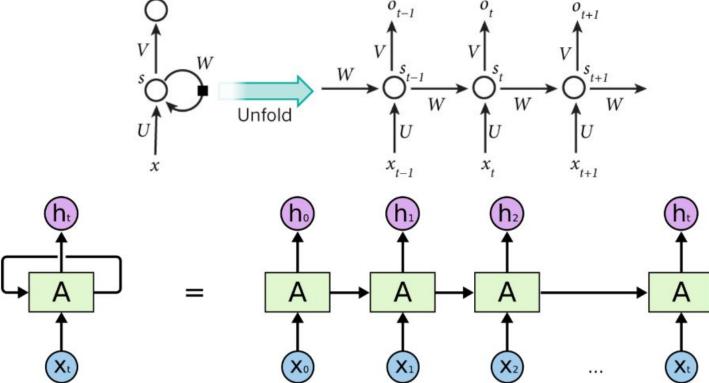


$$h^{t}= f(h^{t-1}, x^{t}) = \sigma(W^{h} h^{t-1} + W^{i}x^{t} + b^{i})$$

Recurrent Neural Network

Input → Hidden → Output

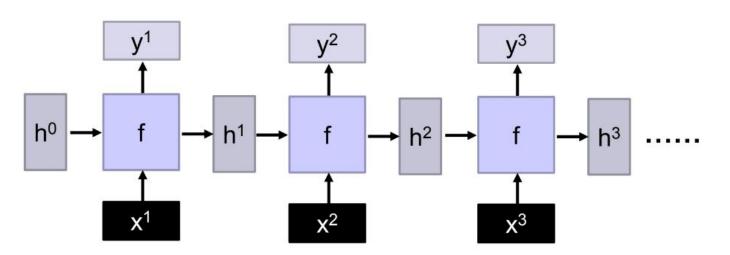




How does RNN reduce complexity?

Given function f: h',y=f(h,x)

h and h' are vectors with the same dimension



No matter how long the input/output sequence is, we only need one function f. If f's are different, then it becomes a feedforward NN. This may be treated as another compression from fully connected network.

APPLICATION

Generating Text

Machine Translation

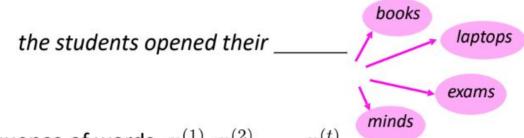
Speech Recognition

Generating Image Descriptions

Chatbots

Language Modeling

Language Modeling is the task of predicting what word comes next



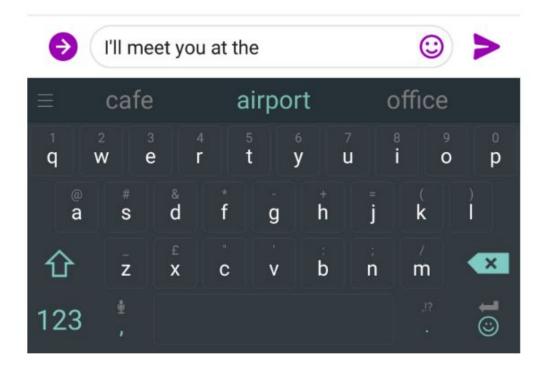
• More formally: given a sequence of words $x^{(1)}, x^{(2)}, \ldots, x^{(t)}$, compute the probability distribution of the next word $x^{(t+1)}$

$$P(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})$$

where $m{x}^{(t+1)}$ can be any word in the vocabulary $\ V = \{m{w}_1,...,m{w}_{|V|}\}$

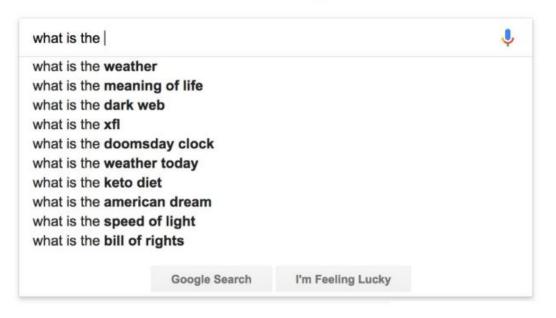
A system that does this is called a Language Model

You use Language Models every day!



You use Language Models every day!





A fixed-window neural Language Model

output distribution

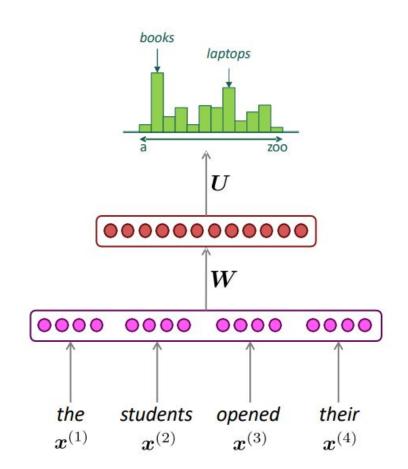
$$\hat{\boldsymbol{y}} = \operatorname{softmax}(\boldsymbol{U}\boldsymbol{h} + \boldsymbol{b}_2) \in \mathbb{R}^{|V|}$$

hidden layer

$$h = f(We + b_1)$$

concatenated word embeddings $oldsymbol{e} = [oldsymbol{e}^{(1)}; oldsymbol{e}^{(2)}; oldsymbol{e}^{(3)}; oldsymbol{e}^{(4)}]$

words / one-hot vectors $oldsymbol{x}^{(1)}, oldsymbol{x}^{(2)}, oldsymbol{x}^{(3)}, oldsymbol{x}^{(4)}$



A fixed-window neural Language Model

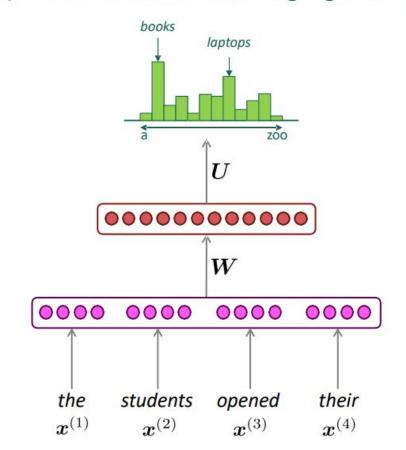
Approximately: Y. Bengio, et al. (2000/2003): A Neural Probabilistic Language Model

Improvements over *n*-gram LM:

- No sparsity problem
- Don't need to store all observed n-grams

Remaining problems:

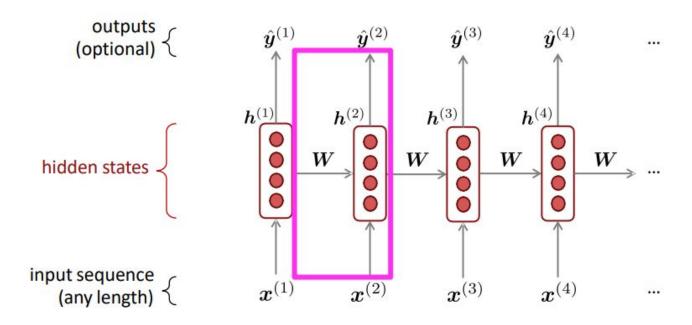
- Fixed window is too small
- Enlarging window enlarges W
- Window can never be large enough!
- x⁽¹⁾ and x⁽⁾⁾ are multiplied by completely different weights in W.
 No symmetry in how the inputs are processeded a neural architecture that can process any length input



Recurrent Neural Networks (RNN)

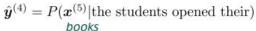
A family of neural architectures

Core idea: Apply the same weights W repeatedly



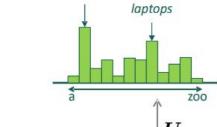
A Simple RNN Language Model

$\hat{m{y}}^{(}$



output distribution

$$\hat{\boldsymbol{y}}^{(t)} = \operatorname{softmax}\left(\boldsymbol{U}\boldsymbol{h}^{(t)} + \boldsymbol{b}_2\right) \in \mathbb{R}^{|V|}$$



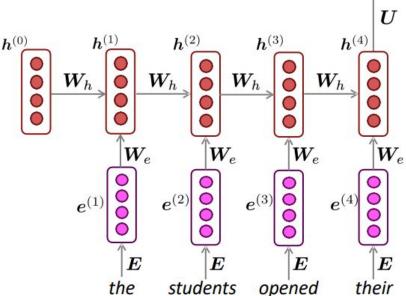
hidden states

$$m{h}^{(t)} = \sigma \left(m{W}_hm{h}^{(t-1)} + m{W}_em{e}^{(t)} + m{b}_1
ight) \ m{h}^{(0)}$$
 is the initial hidden state

word embeddings $oldsymbol{e}^{(t)} = oldsymbol{E} oldsymbol{x}^{(t)}$

 $\boldsymbol{x}^{(t)} \in \mathbb{R}^{|V|}$

words / one-hot vectors



 $x^{(2)}$

 $x^{(3)}$

 $x^{(4)}$

Note: this input sequence could be much longer now!

 $x^{(1)}$

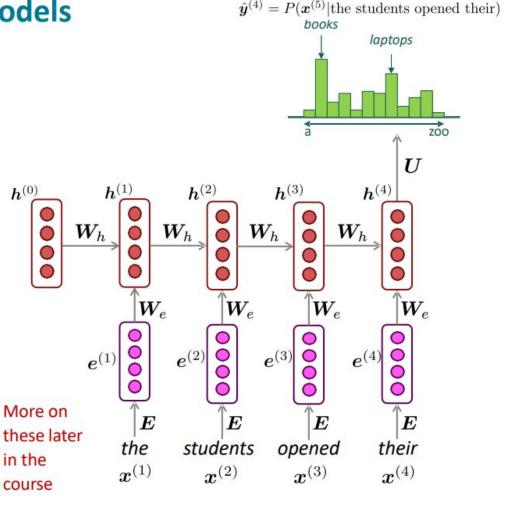
RNN Language Models

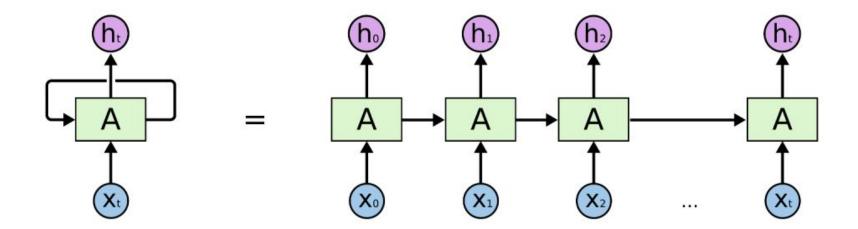
RNN Advantages:

- Can process any length input
- Computation for step t can (in theory) use information from many steps back
- Model size doesn't increase for longer input context
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

RNN Disadvantages:

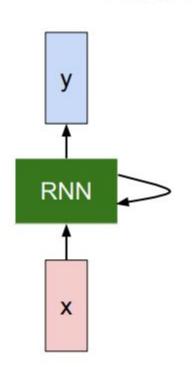
- Recurrent computation is slow
- In practice, difficult to access information from many steps back





(Simple) Recurrent Neural Network

The state consists of a single "hidden" vector h:



$$h_t = f_W(h_{t-1}, x_t)$$

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

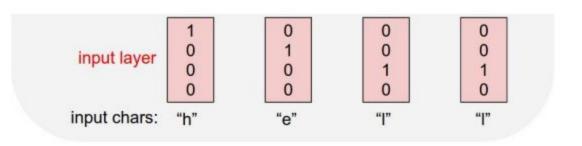
$$y_t = W_{hy} h_t$$

Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman

Vocabulary: [h,e,l,o]

Example training sequence:

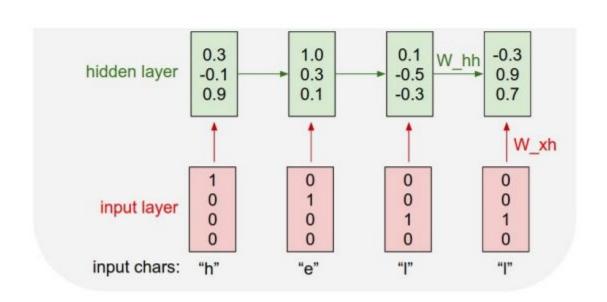
"hello"



$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

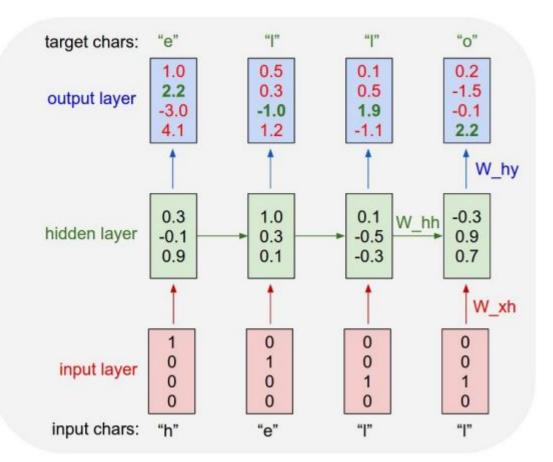
Vocabulary: [h,e,l,o]

Example training sequence: "hello"

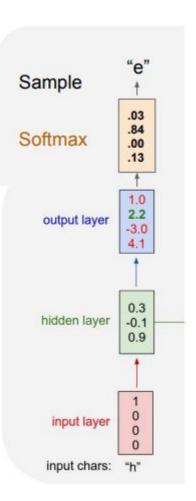


Vocabulary: [h,e,l,o]

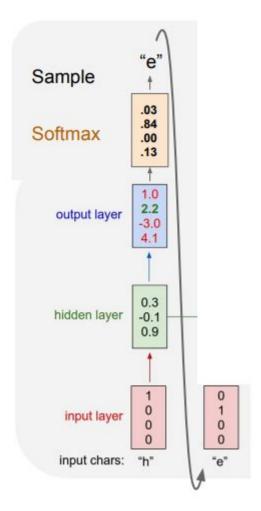
Example training sequence: "hello"



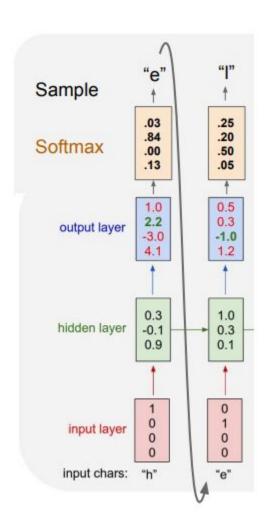
Vocabulary: [h,e,l,o]



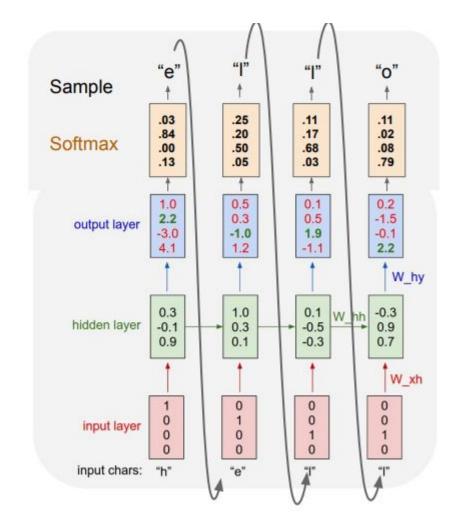
Vocabulary: [h,e,l,o]



Vocabulary: [h,e,l,o]



Vocabulary: [h,e,l,o]



CODE

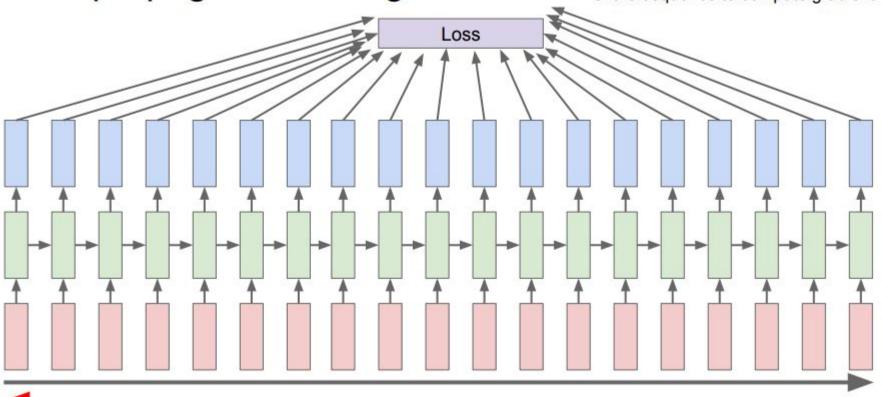
```
import numpy as np
import tensorflow as tf
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Embedding, SimpleRNN, Dense
from tensorflow.keras.preprocessing.text import Tokenizer
from tensorflow.keras.preprocessing.sequence import pad sequences
texts = ["I love this product", "This is terrible", "Awesome!", "Waste of money"]
labels = [1, 0, 1, 0] # 1 for positive, 0 for negative
# Tokenize the text data
tokenizer = Tokenizer()
tokenizer.fit on texts(texts)
sequences = tokenizer.texts_to_sequences(texts)
# Padding sequences to have the same length
max_sequence_length = max([len(seq) for seq in sequences])
sequences = pad_sequences(sequences, maxlen=max_sequence_length, padding='post')
```

CODE

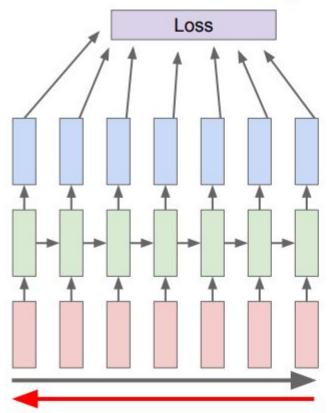
```
model = Sequential()
model.add(Embedding(input_dim=len(tokenizer.word_index) + 1, output_dim=16,
input_length=max_sequence_length))
model.add(SimpleRNN(8, activation='tanh'))
model.add(Dense(1, activation='sigmoid'))
model.compile(optimizer='adam', loss='binary_crossentropy',
metrics=['accuracy'])
labels = np.array(labels)
model.fit(sequences, labels, epochs=10, batch_size=2)
test_text = ["I hate it", "Amazing product"]
test_sequences = tokenizer.texts_to_sequences(test_text)
test_sequences = pad_sequences(test_sequences, maxlen=max_sequence_length,
padding='post')
predictions = model.predict(test_sequences)
print(predictions)
```

Backpropagation through time

Forward through entire sequence to compute loss, then backward through entire sequence to compute gradient

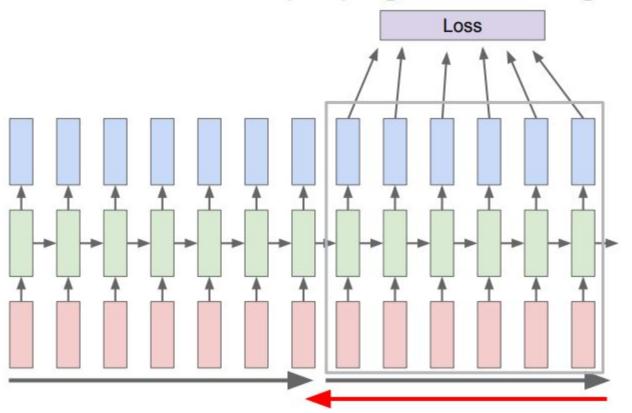


Truncated Backpropagation through time



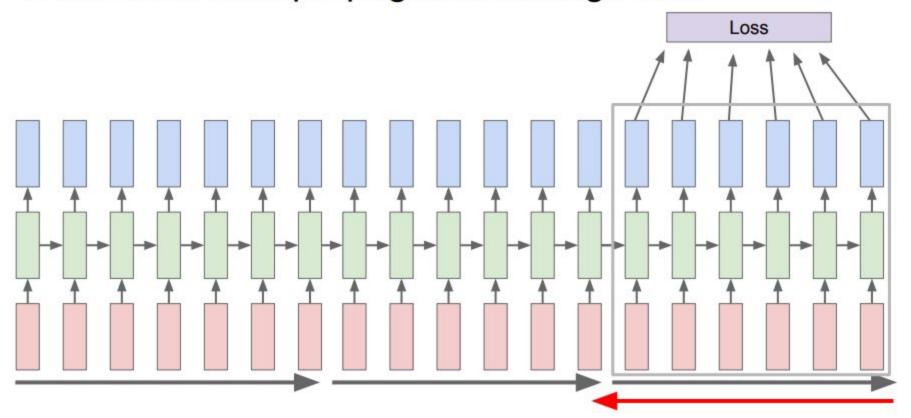
Run forward and backward through chunks of the sequence instead of whole sequence

Truncated Backpropagation through time

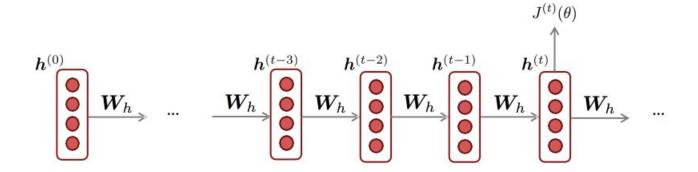


Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

Truncated Backpropagation through time



Backpropagation for RNNs

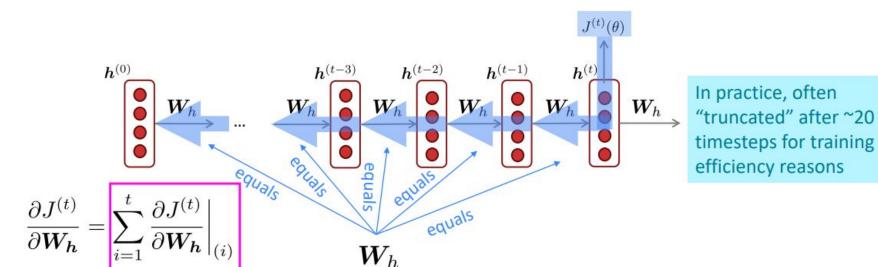


Question: What's the derivative of $J^{(t)}(\theta)$ w.r.t. the repeated weight matrix W_h ?

Answer:
$$\frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}} = \sum_{i=1}^{t} \frac{\partial J^{(t)}}{\partial \boldsymbol{W_h}} \Big|_{(i)}$$

"The gradient w.r.t. a repeated weight is the sum of the gradient w.r.t. each time it appears"

Training the parameters of RNNs: Backpropagation for RNNs



Question: How do we calculate this?

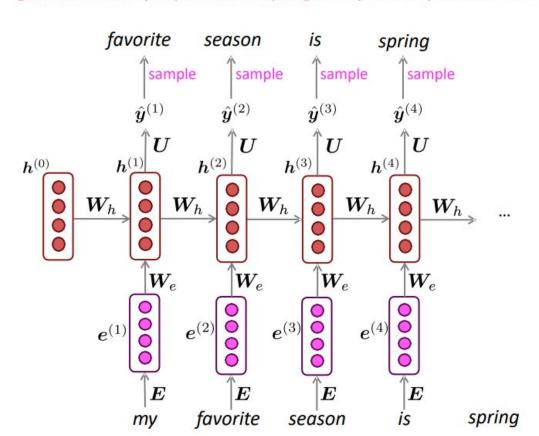
Answer: Backpropagate over timesteps i = t, ..., 0, summing gradients as you go. This algorithm is called "backpropagation through time" [Werbos, P.G., 1988, Neural Networks 1, and others]

$$\frac{\partial J^{(t)}}{\partial \mathbf{W}_h} = \sum_{i=1}^t \frac{\partial J^{(t)}}{\partial \mathbf{W}_h} \Big|_{(i)} \frac{\partial \mathbf{W}_h \Big|_{(i)}}{\partial \mathbf{W}_h}$$
$$= \sum_{i=1}^t \frac{\partial J^{(t)}}{\partial \mathbf{W}_h} \Big|_{(i)}$$

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Generating text with a RNN Language Model

Just like a n-gram Language Model, you can use a RNN Language Model to generate text by repeated sampling. Sampled output becomes next step's input.



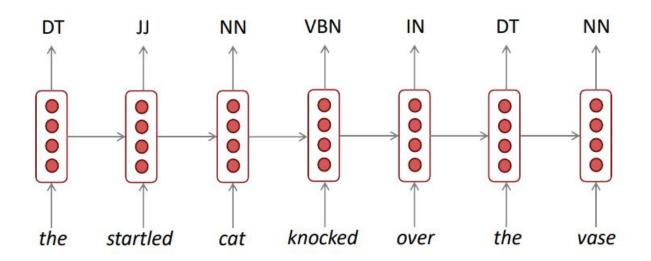
Recap

- Language Model: A system that predicts the next word
- Recurrent Neural Network: A family of neural networks that:
 - Take sequential input of any length
 - Apply the same weights on each step
 - Can optionally produce output on each step

- Recurrent Neural Network ≠ Language Model
- · We've shown that RNNs are a great way to build a LM.
- But RNNs are useful for much more!

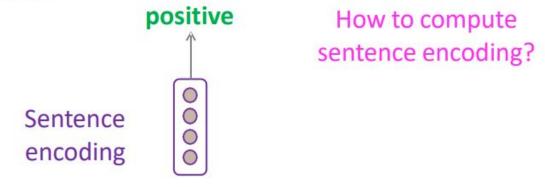
RNNs can be used for tagging

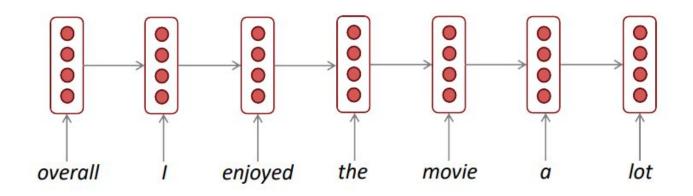
e.g., part-of-speech tagging, named entity recognition



RNNs can be used for sentence classification

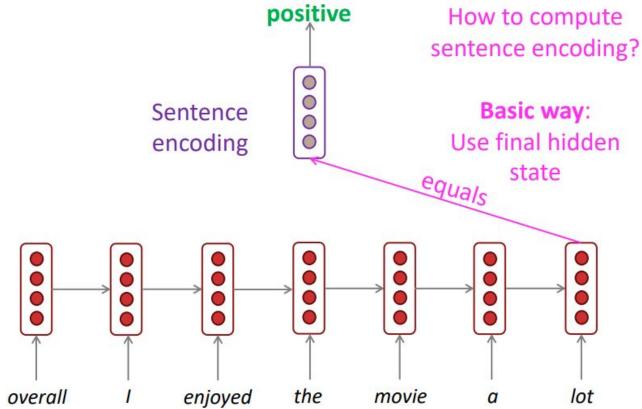
e.g., sentiment classification





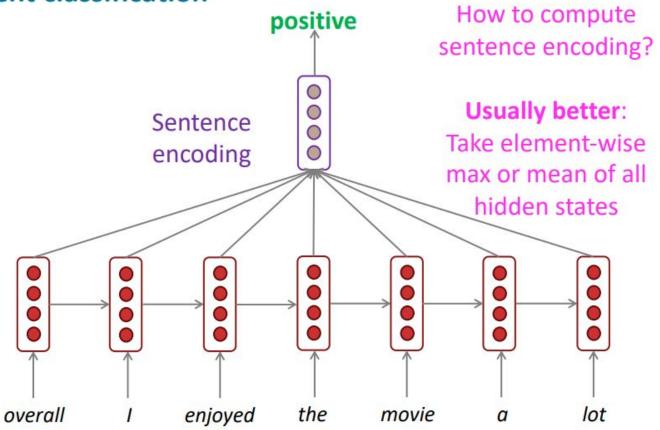
RNNs can be used for sentence classification

e.g., sentiment classification



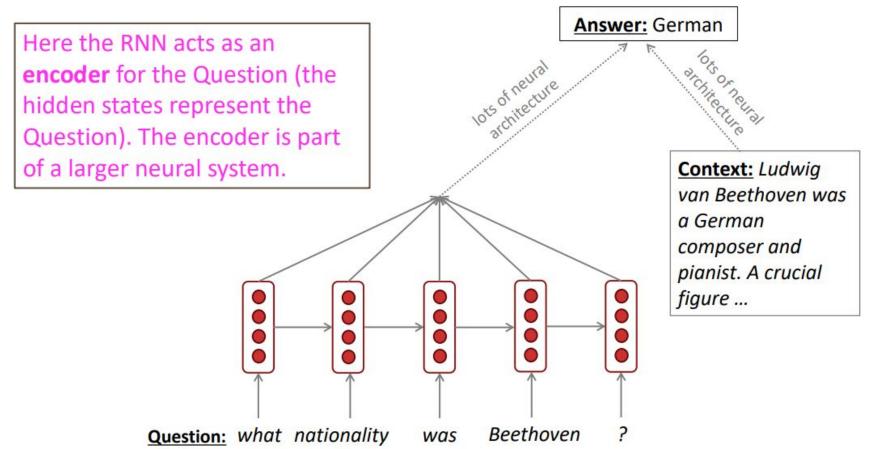
RNNs can be used for sentence classification

e.g., sentiment classification



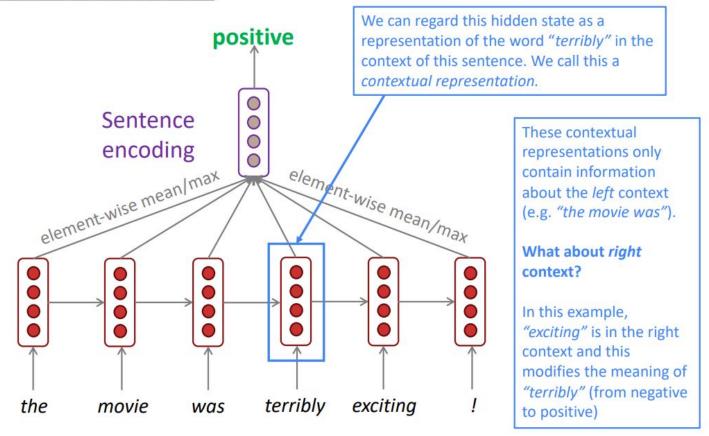
RNNs can be used as an encoder module

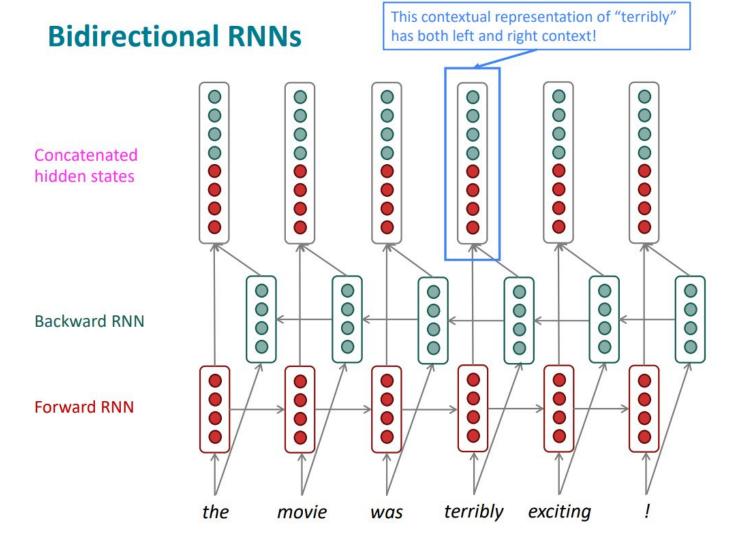
e.g., question answering, machine translation, many other tasks!



Bidirectional and Multi-layer RNNs: motivation

Task: Sentiment Classification





Bidirectional RNNs

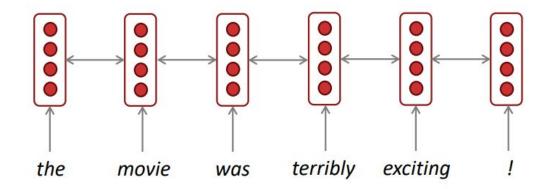
On timestep t:

This is a general notation to mean "compute one forward step of the RNN" – it could be a simple RNN or LSTM computation.

Forward RNN
$$\overrightarrow{h}^{(t)} = \overline{\text{RNN}_{\text{FW}}}(\overrightarrow{h}^{(t-1)}, \boldsymbol{x}^{(t)})$$
Backward RNN $\overleftarrow{h}^{(t)} = \overline{\text{RNN}_{\text{BW}}}(\overleftarrow{h}^{(t+1)}, \boldsymbol{x}^{(t)})$
Concatenated hidden states $\boldsymbol{h}^{(t)} = [\overrightarrow{h}^{(t)}; \overleftarrow{h}^{(t)}]$

We regard this as "the hidden state" of a bidirectional RNN. This is what we pass on to the next parts of the network.

Bidirectional RNNs: simplified diagram



The two-way arrows indicate bidirectionality and the depicted hidden states are assumed to be the concatenated forwards+backwards states

Bidirectional RNNs

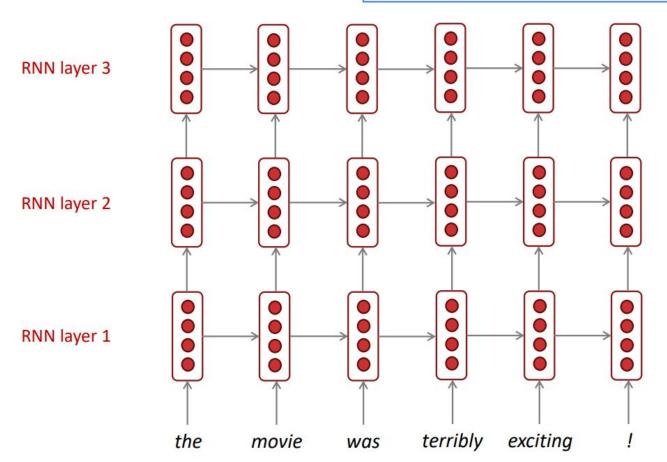
- Note: bidirectional RNNs are only applicable if you have access to the entire input sequence
 - They are **not** applicable to Language Modeling, because in LM you *only* have left context available.
- If you do have entire input sequence (e.g., any kind of encoding), bidirectionality is powerful (you should use it by default).
- For example, BERT (Bidirectional Encoder Representations from Transformers) is a powerful pretrained contextual representation system built on bidirectionality.
 - You will learn more about transformers, including BERT, in a couple of weeks!

Multi-layer RNNs

- RNNs are already "deep" on one dimension (they unroll over many timesteps)
- We can also make them "deep" in another dimension by applying multiple RNNs – this is a multi-layer RNN.
- This allows the network to compute more complex representations
 - The lower RNNs should compute lower-level features and the higher RNNs should compute higher-level features.
- Multi-layer RNNs are also called stacked RNNs.

Multi-layer RNNs

The hidden states from RNN layer *i* are the inputs to RNN layer *i*+1



Multi-layer RNNs in practice

- Multi-layer or stacked RNNs allow a network to compute more complex representations
 - they work better than just have one layer of high-dimensional encodings!
 - The lower RNNs should compute lower-level features and the higher RNNs should compute higher-level features.
- High-performing RNNs are usually multi-layer (but aren't as deep as convolutional or feed-forward networks)
- For example: In a 2017 paper, Britz et al. find that for Neural Machine Translation, 2 to 4 layers is best for the encoder RNN, and 4 layers is best for the decoder RNN
 - Often 2 layers is a lot better than 1, and 3 might be a little better than 2
 - Usually, skip-connections/dense-connections are needed to train deeper RNNs (e.g., 8 layers)
- Transformer-based networks (e.g., BERT) are usually deeper, like 12 or 24 layers.
 - You will learn about Transformers later; they have a lot of skipping-like connections

REFERENCES

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ture05-rnnlm.pdf

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https://web.stanford.edu/class/cs224n/slides/cs224n-2021-lec
ture06-fancy-rnn.pdf