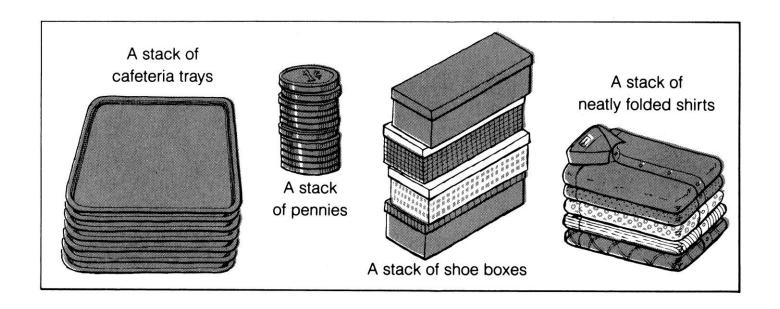
Stack and Queue

Overview

- Introduction to Stack Data structure
- Static vs Dynamic stack
- Implementation details of stack
- Applications of stack
- Introduction to Queue Data structure
- Implementation details of Queue
- Applications of Queue

Introduction to the Stack

- Stack: a LIFO (last in, first out) data structure
- Examples:
 - plates in a cafeteria serving area
 - return addresses for function calls



Stack Basics

- Stack is usually implemented as a list, with additions and removals taking place at one end of the list
- The active end of the list implementing the stack is the top of the stack
- Stack types:
 - Static fixed size, often implemented using an array
 - Dynamic size varies as needed, often implemented using a linked list

Stack Operations and Functions

Operations:

- push: add a value at the top of the stack
- pop: remove a value from the top of the stack

Functions:

- isEmpty: true if the stack currently contains no elements
- isFull: true if the stack is full; only useful for static stacks

Push Operation

- Function: Adds newItem to the top of the stack.
- Preconditions: Stack has been initialized and is not full.
- Postconditions: newItem is at the top of the stack.

Pop Operation

- Function: Removes topItem from stack and returns it in item.
- Preconditions: Stack has been initialized and is not empty.
- Postconditions: Top element has been removed from stack and item is a copy of the removed element.

Stack Overflow and Underflow

Stack overflow

 The condition resulting from trying to push an element onto a full stack.

```
if(!stack.IsFull())
  stack.Push(item);
```

Stack underflow

The condition resulting from trying to pop an empty stack.

```
if(!stack.IsEmpty())
  stack.Pop(item);
```

Static Stack Implementation

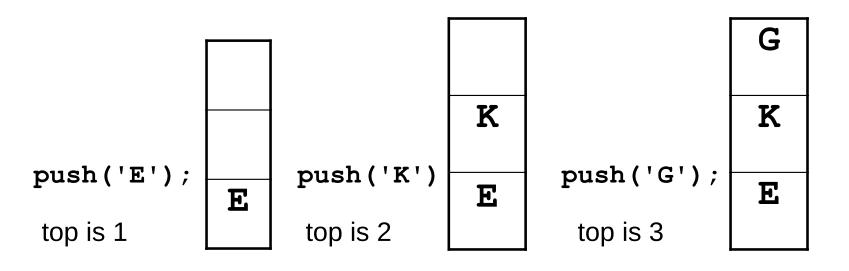
- Uses an array of a fixed size
- Bottom of stack is at index 0. A variable called top tracks the current top of the stack

```
const int STACK_SIZE = 3;
char s[STACK_SIZE];
int top = 0;
```

top is where the next item will be added

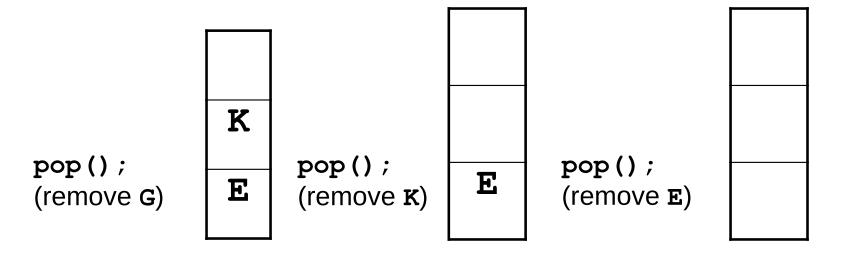
Array Implementation Example

This stack has max capacity 3, initially top = 0 and stack is empty.



Stack Operations Example

After three pops, **top** == 0 and the stack is empty



Array Implementation

```
char s[STACK SIZE];
  int top=0;
To check if stack is empty:
   bool isEmpty()
     if (top == 0)
        return true;
  else return
     false;
```

```
char s[STACK SIZE];
  int top=0;
To check if stack is full:
 bool isFull()
   if (top == STACK SIZE)
          return true;
else return false;
```

```
To add an item to the stack
 void push(char x)
   if (isFull())
     {error(); exit(1);}
   // or could throw an
  exception
  s[top] = x;
    top++;
```

```
To remove an item from the stack
 void pop(char &x)
   if (isEmpty())
     {error(); exit(1);}
   // or could throw an
  exception
    top--;
    x = s[top];
```

Dynamic Stacks

- Implemented as a linked list
- Can grow and shrink as necessary
- Can't ever be full as long as memory is available

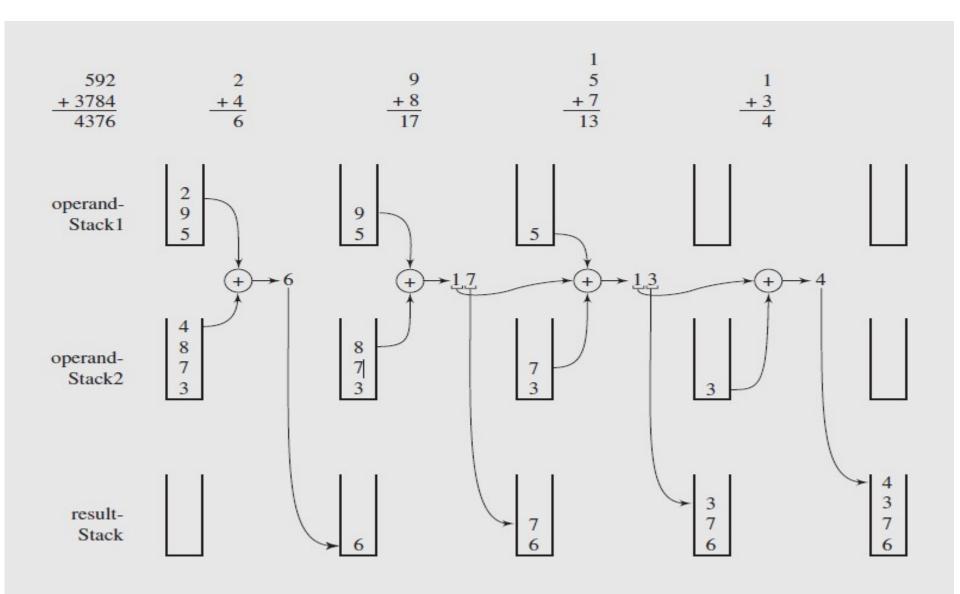
Discussion

 How we will implement a dynamic stack using linked list?

Application of Stacks

- Adding large numbers
- Infix to Postfix Conversion
- Evaluating Postfix notations
- Bracket Matching
- Tower of Hanoi
- Identifying Palindromes
- Searching in Graphs (Depth First Search)
- Undo Redo
- Backtracking

Adding large numbers



Infix to Postfix conversion

Examples of infix to prefix and post fix

Infix	Postfix	Prefix
A+B	AB+	+AB
(A+B) * (C + D)	AB+CD+*	*+AB+CD
A-B/(C*D^E)	ABCDE^*/-	-A/B*C^DE

Rules of Operator Precedence

Operator(s)	Precedence & Associativity Evaluated first. If nested (embedded), innermost first. If on same level, left to right.	
()		
* / %	Evaluated second. If there are several, evaluated left to right	
+ -	Evaluated third. If there are several, evaluated left to right.	
=	Evaluated last, right to left.	

Infix to postfix conversion

Rules to follow:

- Print operands as they arrive.
- If the stack is empty or contains a left parenthesis on top, push the incoming operator onto the stack.
- If the incoming symbol is a left parenthesis, push it on the stack.
- If the incoming symbol is a right parenthesis, pop the stack and print the operators until
 you see a left parenthesis. Discard the pair of parentheses.
- If the incoming symbol has higher precedence than the top of the stack, push it on the stack.
- If the incoming symbol has equal precedence with the top of the stack, use association.
 If the association is left to right, pop and print the top of the stack and then push the incoming operator.
 If the association is right to left, push the incoming operator.
- If the incoming symbol has lower precedence than the symbol on the top of the stack, pop the stack and print the top operator. Then test the incoming operator against the new top of stack.
- At the end of the expression, pop and print all operators on the stack. (No parentheses should remain.)

Example Expression

Suppose we want to convert 2*3/(2-1)+5*3 into Postfix form,

Expression	Stack	Output
2	Empty	2
*	*	2
3	*	23
1	1	23*
(/(23*
2	/(23*2
-	/(-	23*2
1	/(-	23*21
)	1	23*21-
+	+	23*21-/
5 *	+	23*21-/5
*	+*	23*21-/53
3	+*	23*21-/53
	Empty	23*21-/53*+

Postfix Evaluation

- Rules to follow
 - If the element is a number, push it into the stack
 - If the element is a operator, pop operands for the operator from stack. Evaluate the operator and push the result back to the stack

Postfix Evaluation

23*21-/53*+

Read 2	Stack 2 23 6
2 3 *	23 6
2	62
2 1 -	621 61
_	6
/ 5 3 *	65 653
3	615
+	21
	21

Implementation Details

```
int prec(char c)
{
    if(c == '^') return 3;
    else if(c == '*' || c == '/')
    return 2;
    else if(c == '+' || c == '-')
    return 1; else return -1;
}
```

```
If the scanned character is operand
   if((s[i] \ge 'a' \&\& s[i] \le 'z') ||(s[i] \ge 'A' \&\& s[i] \le 'a
  'Z')) ns+=s[i];
If the scanned character is '('
        if(s[i] == '(')
                                               st.push('(');
           If the scanned character is Operator
             If(s[i] == Operator) then
                                                                       while(!st.IsEmpty && prec(s[i]) \le prec(st.top())) do
                                                                                           char c = st.top();
                                                                       st.pop();
                                                                                         ns += c;
                                                                       end while
                                                                       st.push(s[i]);
                                End if
```

```
If the scanned character is ')'
if(s[i] == ')') then
    while(st.top() != '(') do
             char c =
          st.top();
          st.pop();
         ns += c;
              end
       while
       if(st.top() == '(') then
           char c = st.top();
          st.pop();
     end if
End if
```

Postfix Evaluation Algorithm

```
Algorithm postfix (String S) Input:
An expression
Output: Result of an expression
for each character ch in the postfix expression,
do
if ch is an operator ①, then
   a := pop first element from stack
   b := pop second element from the stack res := b <math>\bigcirc
        a
       push res into the stack else if ch
   is an operand, then
        add ch into the stack end if
    return element of stack top
End Procedure
```

Tasks to be implemented

Infix to prefix conversion

- Expression = (A+B^C)*D+E^5
- Step 1. Reverse the infix expression.

- Step 2. Make Every '(' as ')' and every ')' as '(' 5^E+D*(C^B+A)
- Step 3. Convert expression to postfix form.

Step 4. Reverse the expression.

Question:

--/ab+cde

Adding Large numbers using two additional stacks

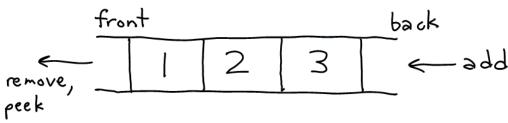
644

+238

Queue

- It is an ordered group of homogeneous items of elements.
- Queues have two ends:
 - Elements are added at one end.
 - Elements are removed from the other end.
- The element added first is also removed first (FIFO: First In, First Out).





Queue Locations and Operations

- rear: position where elements are added
- front: position from which elements are removed
- enqueue: add an element to the rear of the queue
- dequeue: remove an element from the front of a queue

Enqueu Operation

- Function: Adds newItem to the rear of the queue.
- Preconditions: Queue has been initialized and is not full.
- Postconditions: newItem is at rear of queue.

Dequeue Operation

- Function: Removes front item from queue and returns it in item.
- Preconditions: Queue has been initialized and is not empty.
- Postconditions: Front element has been removed from queue and item is a copy of removed element.

Queue overflow

 The condition resulting from trying to add an element onto a full queue.

```
if(!q.IsFull())
  q.Enqueue(item);
```

Queue underflow

 The condition resulting from trying to remove an element from an empty queue.

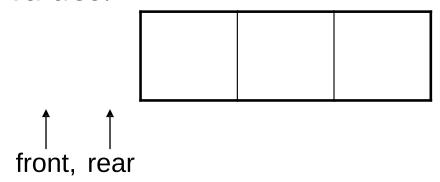
```
if(!q.lsEmpty())
  q.Dequeue(item);
```

Queue Applications

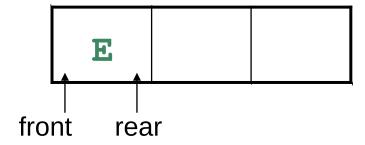
- Operating systems:
 - queue of print jobs to send to the printer
 - queue of programs / processes to be run
 - queue of network data packets to send
- Programming:
 - modeling a line of customers or clients
 - storing a queue of computations to be performed in order
- Real world examples:
 - people on an escalator or waiting in a line
 - cars at a gas station (or on an assembly line)

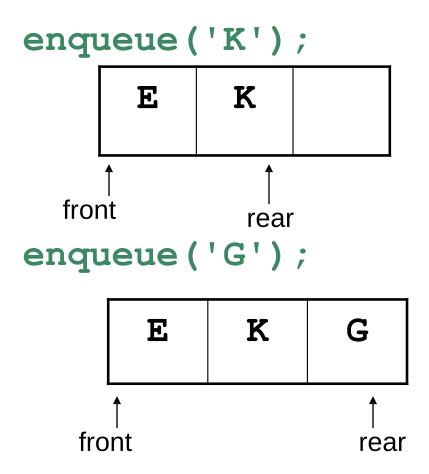
Implementation Details

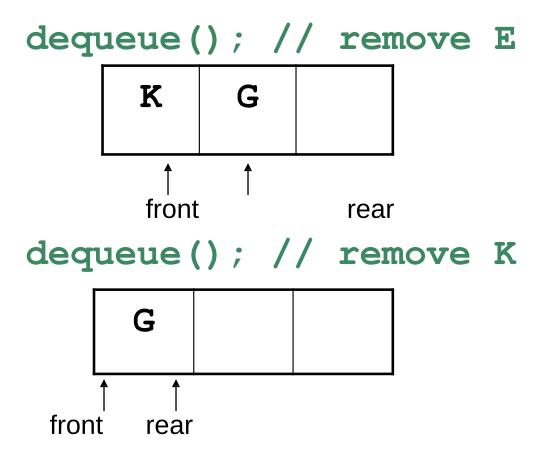
An empty queue that can hold **char** values:



enqueue('E');







Array Implementation Issues

- In the preceding example, Front never moves.
- Whenever dequeue is called, all remaining queue entries move up one position.
 - This takes time.
- Alternate approach:
 - Circular array: front and rear both move when items are added and removed. Both can 'wrap around' from the end of the array to the front if warranted.
- Other conventions are possible

Variables needed

```
-const int QSIZE = 100;
-char q[QSIZE];
-int front = -1;
-int rear = -1;
-int number = 0; //how many
in queue
```

```
Check if queue is empty
  bool isEmpty()
    if (number > 0)
        return
       false;
  else
    return true;
```

```
Check if queue is full
  bool isFull()
     if (number < QSIZE)</pre>
        return false;
  else
     return true;
```

 To enqueue, we need to add an item x to the rear of the queue if(!isFull) { rear = (rear + 1) % QSIZE; // mod operator for wrap-around q[rear] = x;number ++;

To dequeue, we need to remove an item
x from the front of the queue if(!
isEmpty)
{ front = (front + 1) %
 QSIZE; x = q[front];
number--;
}

- enqueue moves rear to the right as it fills positions in the array
- dequeue moves front to the right as it empties positions in the array
- When enqueue gets to the end, it wraps around to the beginning to use those positions that have been emptied
- When dequeue gets to the end, it wraps around to the beginning use those positions that have been filled

Enqueue wraps around by executing

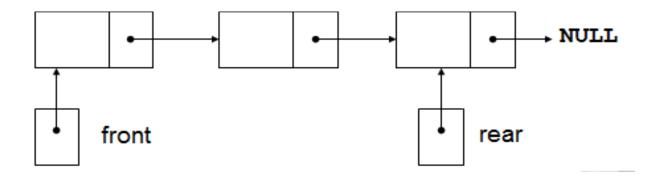
```
rear = (rear + 1) % QSIZE;
```

Dequeue wraps around by executing

```
front = (front + 1) % QSIZE;
```

Dynamic Queues

- Like a stack, a queue can be implemented using a linked list
- Allows dynamic sizing, avoids issue of wrapping indices



Discussion

How to implement a queue using linked list??

Summary

- This lecture is summarized as:
 - The concepts of queue and stack are discussed in detail along with their implementation.
 - The underlying implementation of array as well as linked list data structure is covered.
 - Real life applications are also discussed.