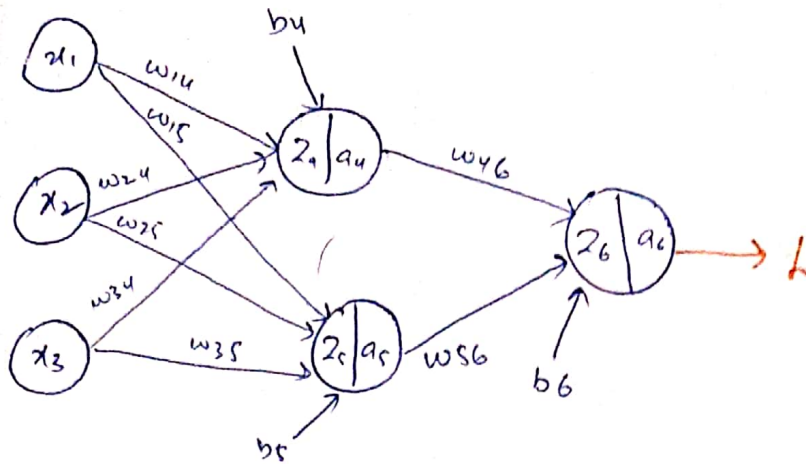


Activation Function is  
Sigmoid in all layers.



For Log Loss / Cross Entropy Loss:

$$L = -[y \log(a) + (1-y) \log(1-a)]$$

$$\frac{\partial L}{\partial a_6} = \frac{\partial}{\partial a_6} [y \log(a_6) + (1-y) \log(1-a_6)]$$

$$= \frac{-y}{a_6} - \frac{(1-y)(-1)}{1-a_6}$$

$$\boxed{\frac{\partial L}{\partial a_6} = \frac{-y}{a_6} + \frac{1-y}{1-a_6}}$$

$$\frac{\partial L}{\partial w_{46}} = \frac{\partial L}{\partial a_6} \cdot \frac{\partial a_6}{\partial z_6} \cdot \frac{\partial z_6}{\partial w_{46}}$$

$$\frac{\partial L}{\partial w_{46}} = \left[ \frac{-y}{a_6} + \frac{1-y}{1-a_6} \right] a_6 (1-a_6) a_4$$

$$= \left[ \frac{-y(1-a_6) + a_6(1-y)}{\cancel{a_6(1-a_6)}} \right] \cancel{a_6(1-a_6)} a_4$$

$$= [-y + \cancel{a_6 y} + a_6 - \cancel{a_6 y}] a_4$$

$$\boxed{\frac{\partial L}{\partial w_{46}} = [a_6 - y] a_4}$$

$$\boxed{\frac{\partial L}{\partial w_{56}} = [a_6 - y] a_5}$$

$$\boxed{\frac{\partial L}{\partial b_6} = [a_6 - y]}$$

For Hidden Layer:

$$\frac{\partial L}{\partial w_{14}} = \frac{\partial L}{\partial a_4} \cdot \frac{\partial a_4}{\partial z_4} \cdot \frac{\partial z_4}{\partial w_{14}}$$

$$\frac{\partial L}{\partial a_4} = \frac{\partial L}{\partial a_6} \cdot \frac{\partial a_6}{\partial z_6} \cdot \frac{\partial z_6}{\partial a_4}$$

$$= (a_6 - y) w_{46}$$

$$\boxed{\frac{\partial L}{\partial w_{14}} = (a_6 - y) w_{46} a_4 (1-a_4) a_1}$$

$$\frac{\partial L}{\partial w_{24}} = (a_6 - y) w_{46} a_u (1 - a_u) x_2$$

$$\frac{\partial L}{\partial w_{34}} = (a_6 - y) w_{46} a_u (1 - a_u) x_3$$

$$\frac{\partial L}{\partial b_u} = (a_6 - y) w_{46} \cdot a_u \cdot (1 - a_u)$$

$$\frac{\partial L}{\partial w_{15}} = (a_6 - y) w_{56} a_s (1 - a_s) x_1$$

$$\frac{\partial L}{\partial w_{25}} = (a_6 - y) w_{56} a_s (1 - a_s) x_2$$

$$\frac{\partial L}{\partial w_{35}} = (a_6 - y) w_{56} a_s (1 - a_s) x_3$$

$$\frac{\partial L}{\partial b_s} = (a_6 - y) w_{56} a_s (1 - a_s)$$