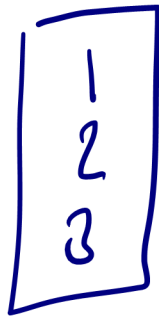
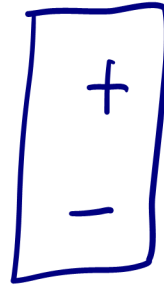


* No parenthesis case:

$$1 + 2 - 3$$



operands



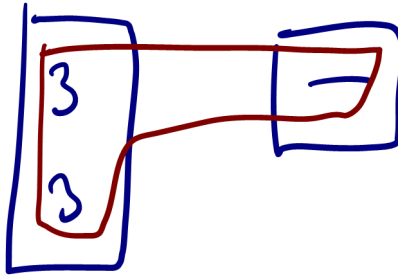
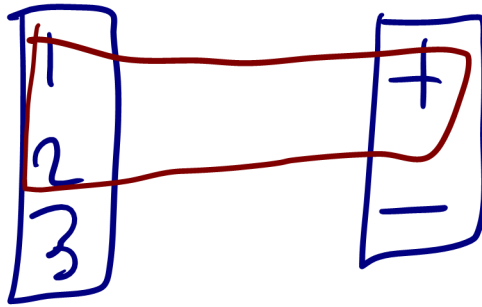
operators

precedence: $/$, $*$, $+$, $-$

* First evaluate all $/$ in order

* Then evaluate all $*$ in order

:



result



empty

$$1 + 2 * 4 / 5 + 6 - 7 / 2 * 3$$

3
2 *
7 /
6 -
5 +
4 /
2 *
1 +

1 +
2 *
4 /
5 +
6 -
7 /
2 *
3

1 +
2 *
0 +
6 -
7 /
2 *
3

1 +
2 *
0 +
6 -
3 *
3

1 +
0 +
6 -
3 *
3

1 +
0 +
6 -
9

1 +
6 -
9

7 -
9

-2

empty

$$1 + 2 * 4 / 5 + 6 - 7 / 2 * 3$$

3	*				
2	/	3		*	
7	-	7		/	
6	+	6		-	
5	/	5	1	+	+
4	*	4	2	1	*
2	+				
1					

3		*	
2		/	+
7	1	-	*
6	2	+	

$$4 / 5 = 0$$

3		*	
2		/	+
7	1	-	*
6	2	+	
0			

3		1	+
2	*	2	*
7	/	0	+
		6	-

3	*	1	+
		2	*
		0	+
		6	-

$$7 / 2 = 3$$

3
3 *

1
2
0
6
+
*
+
—

1
2
0
0
6
3
3
+
*
+
—
*

3
3
6
0
2
1
*
—
+
*
+

↙ return to the original stack

* C++ with parentheses

$$(1+2/3 + (3-4)) + 2$$

* Get rid of parentheses:

$$(1+2/3 + (3-4) \quad \boxed{)}) + 2$$

temp stack
stack

$$(1+2/3 + \quad \text{evaluate } 3-4=-1 \quad) + 2$$

temp stack
stack

$$(1+2/3 + \quad -1 \quad \boxed{)}) + 2$$

temp stack
stack

$$\phi \quad 1+2/3 -1 \quad +2$$

temp stack
 $= 0$
stack

$$0 \quad +2$$

temp stack
stack

$$0+2$$

stack with no parentheses.

$$(1 + (1 + (2 + (3 + 4/5))))$$

$$(1 + (1 + (2 + (3 + 4/5) \boxed{) })))$$

$R = 3 + 4/5 \rightarrow$ evaluate "no parameters"

push R

$$(1 + (1 + (2 + R \boxed{) })))$$

$$R = 2 + R$$

$$(1 + (1 + R \boxed{) })))$$

$$R = 1 + R$$

$$(1 + R \boxed{) })))$$

$$R = 1 + R$$

R

$$(1 + (1 + 3 / (2 + 3))) + (1 + 2 + 3)$$

$$(1 + (1 + 3 / (2 + 3) \boxed{2})) + (1 + 2 + 3)$$

$$R = 2 + 3$$

$$(1 + (1 + 3 / R \boxed{2})) + (1 + 2 + 3)$$

$$R = 1 + 3 / R$$

$$(1 + R \boxed{2}) + (1 + 2 + 3)$$

$$R = 1 + R$$

$$R + (1 + 2 + 3) \boxed{}$$

$$R = 1 + 2 + 3$$

$$R + R \quad \text{"no parentheses"}$$



* Prefix stack will only have "(" or no brackets

* When expression stack is empty, prefix stack will have an expression without brackets