

\* To get rid of parentheses we

have 3 stacks: prefix, expression and "no brackets expression".

Initially prefix stack and "no brackets expression" are empty and expression stack is original expression. Top of expression stack is left most token.

For example:

$(1 + 2 - (3 + 4 / (2 - 5) * 6))$

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Diagram illustrating the expression and its components:

- The expression is  $(1 + 2 - (3 + 4 / (2 - 5) * 6))$ .
- The prefix part is  $(1 + 2 -$ .
- The expression part is  $(3 + 4 / (2 - 5) * 6)$ .
- The "no brackets expression" part is  $)$ .
- Arrows indicate the flow of tokens from the expression to the prefix stack and from the expression to the "no brackets expression" stack.
- Labels: "prefix", "token", "expression", "top of prefix stack", "top of expression stack".

We go in expression from left to right and push all tokens (and push them to prefix stack) until we hit  $)$ .

We then pop back from prefix stack all tokens (and push them to "no brackets expression" stack) until we hit  $)$ .

We then evaluate "no brackets  
expression" and push result back to  
prefix and clear  
nbe.

expression = "(1+2-(3+4/(2-5)\*6))"  
prefix = ""  
nbe = ""  
token = ""

prefix = "(1+2-(3+4/(2-5"  
token = ")"  
expression = "\*6))"  
nbe = ""

prefix = "(1+2-(3+4/"  
token = "("  
expression = "\*6))"  
nbe = "2-5"

Evaluate (nbe) = "-3"

clear nbe

push "-" to prefix

prefix = "(1+2-(3+4/-3)"

expression = "\*6))"

nbe = ""

We continue until we reach end of expression.

Resulting prefix will be expression without parentheses.

We then evaluate prefix.

\* Evaluate expression without parentheses:

x We have prefix and expression stacks.

\* Initially prefix stack is empty and expression stack is equal to expression

without parentheses.

\* If there are 4 operations we evaluate

expression 4 times in order of  
operation precedence.

When the evaluation is completed,  
expression is empty and prefix  
has no occurrence of "operation"  
operand.

\* Evaluation works as follows:

We pop from expression stack  
and push to prefix stack  
until we hit "operation"  
token.

We then pop left operand  
from prefix stack and right  
operand from expression stack.

We calculate result and push  
it to prefix stack.

We until we reach end  
of expression.

For example to evaluate / :  
prefix = ""

expression = "1 + 2 - 3 / 5 \* 6 / 7"

prefix = "1 + 2 -"

expression = "/ 5 \* 6 / 7"

prefix = "1 + 2 -"

op1 = 3

result = 2 / 5 = 0

op2 = 5

expression = "\* 6 / 7"

prefix = "1 + 2 - 0"

expression = "\* 6 / 7"

prefix = "1 + 2 - 0 \* 6"

expression = "/ 7"

prefix = "1 + 2 - 0 \* 6"

op1 = 6

result = 6 / 7 = 0

op2 = 7

expression = ""

prefix = "1+2-0 \* 0"

expression = ""