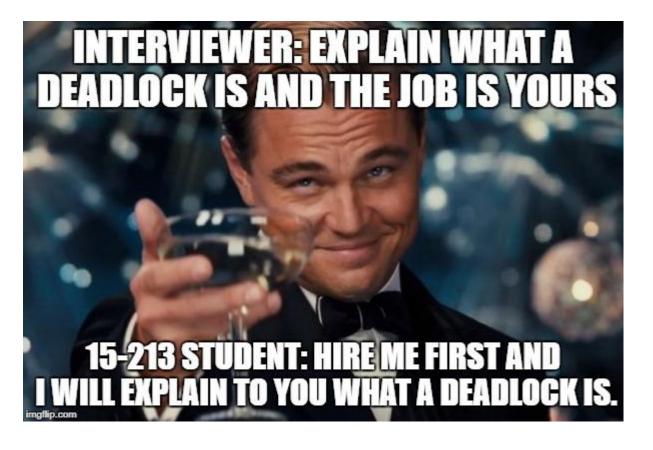
15-213: Final Exam Review

Minji, Harsha, and Ishita



Problem Statement:

- 15-213 TAs now want to begin a new procedure for daily office hours:
- When a student enters the room, he/she will see a table inside the room with several pens and several notebooks on it (if the pens and notebooks haven't been claimed by other students). TAs are inside the room waiting to help them.

Procedure for students:

- Wait until you get called, claim a pen and a notebook.
- Use the pen to write your questions on the notebook.
- After you are done with question writing, release the pen.
- Hold the notebook and wait until a TA is free to help you.
- After you are done with talking to a TA about the question, go back to claim a pen and write the solutions on the notebook.
- Release the pen and the notebook and go home.

Typical Code to launch threads and wait for them to finish:

```
sem t pen;
sem t notebook;
sem t ta;
int main(int argc, char** argv)
    int P = 5, N = 5, T = 3, S = 50;
    sem init(&pen, 0, P);
    sem init(&notebook, 0, N);
    sem init(&ta, 0, T);
    int* students = malloc(S * sizeof(int));
    launch threads();
    reap threads();
```

```
void launch threads()
  for (int i = 0; i < S; i++)
    students[s] =
          pthread create(students+i,
                  NULL, student fn, NULL);
void reap threads()
  for (int i = 0; i < S; i++)
    pthread join(students[i]);
```

A student writes the following worker thread to simulate the given procedure

```
void* student_fn(void* varp)
{
  P(&pen);
  P(&notebook);
  sleep(genrand() % 60); // Time for you to write questions

  V(&pen);
  P(&ta);
  sleep(genrand() % 900); // Time for you to ask TA

  V(&ta);
  P(&pen);
  sleep(genrand() % 60); // Time for you to write solutions

  V(&notebook);
  V(&pen);
  return 0;
}
```

- However, the code sometimes gets stuck by a deadlock. Which of the following is correct?
- A: The deadlock is caused by the pen and the notebook.
- B: The deadlock is caused by the notebook and the TA.
- C: The deadlock is caused by the TA and the pen.

A student writes the following program to simulate the given procedures

```
void* student fn(void* varp)
  P(&pen);
  P(&notebook);
  sleep(genrand() % 60); // Time for you to write questions
  V(&pen);
  P(&ta);
  sleep(genrand() % 900); // Time for you to ask TA
  V(&ta);
  P(&pen);
  sleep(genrand() % 60); // Time for you to write solutions
  V(&notebook);
  V(&pen);
  return 0;
```

Let us consider a simple example:

Pens: 5

Notebooks: 5

TAs:

Students: 50

Let's analyse the semaphores

```
void* student fn(void* varp)
S: Signal
W: Wait
                P(&pen);
    W:Get a pen
                                                                       W:Get a Notebook
                P(&notebook);
                sleep(genrand() % 60); // Time for you to write questions
    S: Give up pen
                V(&pen);
                P(&ta);
    W:Get a TA
                sleep(genrand() % 900); // Time for you to ask TA
    S:Give up TA
                V(&ta);
                P(&pen);
    W:Get a pen
                sleep(genrand() % 60); // Time for you to write solutions
                                                                   S:Give up Notebook
                V(&notebook);
                V(&pen);
    S: Give up pen
                return 0;
```

Case C: TAs and Pens

- There is no overlap
- There can't be a case where a student who is talking to a TA is waiting on a pen.
- There can't be a case where a student who is holding a pen is waiting on a TA

Let's analyse the semaphores

```
void* student fn(void* varp)
S: Signal
W: Wait
                P(&pen);
    W:Get a pen
                                                                       W:Get a Notebook
                P(&notebook);
                sleep(genrand() % 60); // Time for you to write questions
    S: Give up pen
                V(&pen);
                P(&ta);
    W:Get a TA
                sleep(genrand() % 900); // Time for you to ask TA
    S:Give up TA
                V(&ta);
                P(&pen);
    W:Get a pen
                sleep(genrand() % 60); // Time for you to write solutions
                                                                   S:Give up Notebook
                V(&notebook);
                V(&pen);
    S: Give up pen
                return 0;
```

Case B: TAs and Notebooks

- There is an overlap
- A student who is holding a notebook may be waiting on a TA
- But....A student who is talking to a TA will not be waiting on a notebook

Let's analyse the semaphores

```
S: Signal
              void* student fn(void* varp)
W: Wait
                P(&pen);
    W:Get a pen
                                                                       W:Get a Notebook
                P(&notebook);
                sleep(genrand() % 60); // Time for you to write questions
    S: Give up pen
                V(&pen);
                P(&ta);
    W:Get a TA
                sleep(genrand() % 900); // Time for you to ask TA
    S:Give up TA
                V(&ta);
                P(&pen);
    W:Get a pen
                sleep(genrand() % 60); // Time for you to write solutions
                                                                   S:Give up Notebook
                V(&notebook);
                V(&pen);
    S: Give up pen
                return 0;
```

Case A: Pens and Notebooks

There is an overlap

A student who is holding a notebook may be waiting on a pen

A student who is holding a pen may be waiting on a notebook

Let's analyse the semaphores

```
S: Signal
             void* student fn(void* varp)
W: Wait
                P(&pen);
   W:Get a pen
                                                                      W:Get a Notebook
                P(&notebook);
                                                                                           sleep(genrand() %
                                   80); // Time for you to write guestions
    S: Give up pen
                V(&pen);
                P(&ta);
    W:Get a TA
                sleep(genrand() % 900); // Time for you to ask TA
    S:Give up TA
                V(&ta);
                P(&pen);◀
    W:Get a pen
                sleep(genrand() % 60); // Time for you to write solutions
                                                                  S:Give up Notebook
                V(&notebook);
                V(&pen);
   S: Give up pen
                return 0;
```

Case A: Pens and Notebooks

Consider this likely scenario:

- 5 Students (group A) enter the room
- They grab all 5 pens and all 5 notebooks on the table.
- Every student behind them is waiting on a pen and a notebook. (Group B)
- All 5 students in Group A give up their pens, but not their notebooks.
- 5 students in Group B immediately grab the 5 pens.
- Group B are now waiting on notebooks.
- After talking to the TAs, all students in Group A are now waiting on pens, which students in Group B have.
 - Group B is waiting on the notebooks which students in Group A have.

DEADLOCK!!

A student writes the following program to simulate the given procedures

```
void* student fn(void* varp)
  P(&pen);
  P(&notebook);
  sleep(genrand() % 60); // Time for you to write questions
  V(&pen);
  P(&ta);
  sleep(genrand() % 900); // Time for you to ask TA
  V(&ta);
  P(&pen);
  sleep(genrand() % 60); // Time for you to write solutions
  V(&notebook);
  V(&pen);
  return 0;
```

- However, the code sometimes gets stuck by a deadlock. Which of the following is correct?
- A: The deadlock is caused by the pen and the notebook.
- B: The deadlock is caused by the notebook and the ta.
- C: The deadlock is caused by the ta and the pen.

ANSWER: A

Can we fix this without changing the Office Hour procedure?

Can we fix this without changing the Office Hour procedure?

YES!

Let's analyse the semaphores

S: Signal W: Wait

```
void* student fn(void* varp)
                                                              W:Get a Notebook
              P(&notebook);
              P(&pen);
W:Get a pen
              sleep(genrand() % 60); // Time for you to write questions
S: Give up pen
              V(&pen);
               P(&ta);
W:Get a TA
              sleep(genrand() % 900); // Time for you to ask TA
S:Give up TA
              V(&ta);
              P(&pen);
W:Get a pen
              sleep(genrand() % 60); // Time for you to write solutions
S: Give up pen
              V(&pen);
              V(&notebook);
                                                        S:Give up Notebook
               return 0;
```

Let's just re-order the locks and analyse it again.

 A student who is holding a notebook may wait on a pen or a TA

However...

- A student who is holding a pen will already have a notebook (and never wait on it).
- A student who is talking to a TA will already have a notebook (and never wait on it).

who would win?

several hundred lines of tshlab code

one asynchronous boi



- Examples in these slides are important "gotchas"
 - NOT an all inclusive list
 - In particular, these do NOT go over signals sent between multiple processes
- Many more examples in:
 - Recitation slides
 - Lecture slides
 - Past exams
- Reminder: solve the questions on your own when studying before looking at the answer

Does the following code ever terminate?

```
void handler(int sig) {
    while(1);
}
int main() {
    Signal(SIGUSR1, handler);
    Kill(0, SIGUSR1);
    return 0;
}
```

Does the following code ever terminate?

```
void handler(int sig) {
                        // stuck here forever!
   while (1);
int main() {
   Signal(SIGUSR1, handler);
   // Spec says signal sent to self must be handled
   // before kill() returns
   Kill(0, SIGUSR1);
   return 0;
```

What about now?

```
void handler(int sig) {
   Kill(0, SIGUSR1);
int main() {
   Signal(SIGUSR1, handler);
   Kill(0, SIGUSR1);
   return 0;
```

What about now?

```
void handler(int sig) {
   Kill(0, SIGUSR1);
int main() {
   Signal(SIGUSR1, handler);
   Kill(0, SIGUSR1);
   return 0;
```

Does not terminate:

```
main: Kill(0, SIGUSR1);
<SIGUSR1 handler invoked,
SIGUSR1 blocked in handler>
handler: Kill(0, SIGUSR1);
<SIGUSR1 pending>
<handler returns>
<SIGUSR1 unblocked, SIGUSR1
handler invoked, SIGUSR1
blocked in handler>
handler: Kill(0, SIGUSR);
...repeat...
```



Draw a Process Graph!!!

(it does not have to be like mine)

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

What is printed?

Assume printf is atomic, and all system calls succeed.

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
   printf("%d", count);
```

How many processes?

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

How many processes?

Parent: forks child

Parent and child: each fork another child

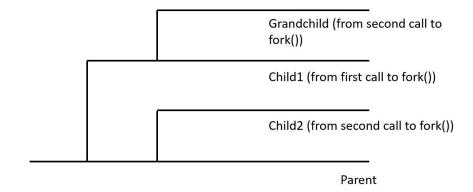
Total: 4 processes

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
   printf("%d", count);
```

What does the process diagram look like?

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

What does the process diagram look like?



```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

What does count look like?

Parent: pid1 != 0 and pid2 != 0
Child1: pid1 == 0 and pid2 != 0
Child2: pid1 != 0 and pid2 == 0
Grandchild: pid1 == 0 and pid2 == 0

```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

What does count look like?

Parent: pid1 != 0 and pid2 != 0

• count = 3

Child1: pid1 == 0 and pid2 != 0

• count = 2

Child2: pid1 != 0 and pid2 == 0

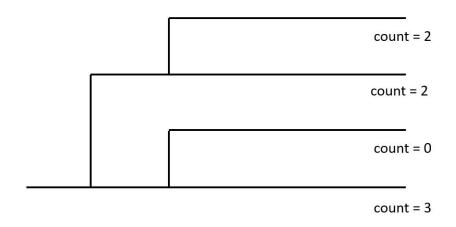
• count = 0

Grandchild: pid1 == 0 and pid2 == 0

• count = 2

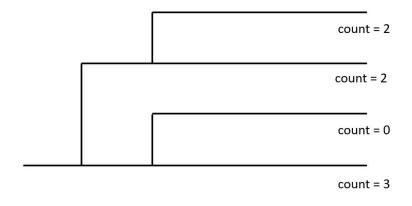
```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

Given the process diagram, what are the different permutations that can be printed out?



```
int main() {
    int count = 1;
    int pid1 = fork();
    int pid2 = fork();
    if(pid1 == 0)
         count++;
    else{
         if(pid2 == 0)
               count--;
         else
           count += 2;
    printf("%d", count);
```

Given the process diagram, what are the different permutations that can be printed out?



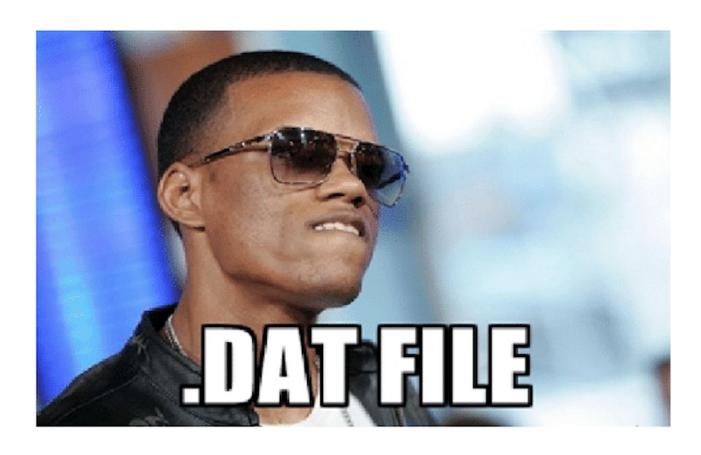
Math! 4! / 2 = 12 different possible outcomes



Remember:

- Processes can occur in any order
- Watch out for a wait or a waitpid!
 - What if I included a wait (NULL) before I printed out count?
- Good luck!

File IO



File IO

Main ideas:

- How does read offset?
- How does dup2 work?
 - What is the order of arguments?
 - Does fd3 share offset with fd2?

File IO

```
foo.txt: abcdefgh...xyz
int main() {
    int fd1, fd2, fd3;
    char c;
    pid_t pid;
    fd1 = open("foo.txt", O_RDONLY);
    fd2 = open("foo.txt", O_RDONLY);
    fd3 = open("foo.txt", O_RDONLY);
    read(fd1, &c, sizeof(c));
    read(fd2, &c, sizeof(c));
    // c = a
    dup2(fd2, fd3);
    read(fd3, &c, sizeof(c));
    // c = b
    read(fd2, &c, sizeof(c));
    // c = c
```

- How does read offset?
 - Incremented by number of bytes read
- How does dup2 work?
 - Any read/write from fd3 now happen from fd2
 - All file offsets are shared

```
read(fd1, &c, sizeof(c)); // a
read(fd2, \&c, sizeof(c)); // a
dup2(fd2, fd3);
read(fd3, \&c, sizeof(c)); // b
read(fd2, \&c, sizeof(c)); // c
pid = fork();
if (pid==0) {
     read(fd1, &c, sizeof(c));
     printf("c = %c\n'', c);
     dup2(fd1, fd2);
     read(fd3, &c, sizeof(c));
     printf("c = %c\n'', c);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
read(fd1, &c, sizeof(c));
printf("c = %c\n'', c);
```

Main ideas:

- How are fd shared between processes?
- How does dup2 work from parent to child?
- How are file offsets shared between processes?

```
read(fd1, \&c, sizeof(c)); // a
read(fd2, &c, sizeof(c)); // a
dup2(fd2, fd3);
read(fd3, \&c, sizeof(c)); // b
read(fd2, \&c, sizeof(c)); // c
pid = fork();
if (pid==0) {
    read(fd1, &c, sizeof(c));
    printf("c = %c\n", c);
    dup2(fd1, fd2);
    read(fd3, &c, sizeof(c));
    printf("c = %c\n'', c);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
read(fd1, &c, sizeof(c));
printf("c = %c\n'', c);
```

What would this program print?

```
read(fd1, &c, sizeof(c)); // a
read(fd2, \&c, sizeof(c)); // a
dup2(fd2, fd3);
read(fd3, \&c, sizeof(c)); // b
read(fd2, \&c, sizeof(c)); // c
pid = fork();
if (pid==0) {
    read(fd1, &c, sizeof(c));
    printf("c = %c\n'', c);
    dup2(fd1, fd2);
    read(fd3, &c, sizeof(c));
    printf("c = %c\n", c);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
read(fd1, &c, sizeof(c));
printf("c = %c\n'', c);
```

```
Possible output 1:
    c = d // in parent
    c = b // in parent
    c = c // in child from fd1
    c = e // in child from fd3
    c = d // in child
    c = e // in child
```

```
read(fd1, &c, sizeof(c)); // a
read(fd2, \&c, sizeof(c)); // a
dup2 (fd2, fd3);
read(fd3, \&c, sizeof(c)); // b
read(fd2, \&c, sizeof(c)); // c
pid = fork();
if (pid==0) {
    read(fd1, &c, sizeof(c));
    printf("c = %c\n", c);
    dup2(fd1, fd2);
    read(fd3, &c, sizeof(c));
    printf("c = %c\n", c);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
read(fd1, &c, sizeof(c));
printf("c = %c\n'', c);
```

Possible output 2:

c = b // in child c = d // in child

c = c // in child

c = d // in child

c = e // in parent

c = e // in parent

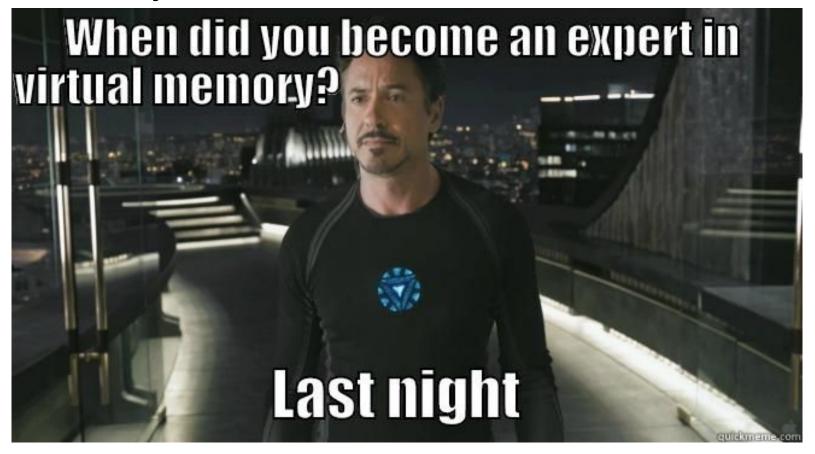
```
pid = fork();
if (pid==0) {
    read(fd1, &c, sizeof(c));
    printf("c = %c\n", c);
    dup2(fd1, fd2);
    read(fd3, &c, sizeof(c));
    printf("c = %c\n", c);
if (pid!=0) waitpid(-1, NULL, 0);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
read(fd1, &c, sizeof(c));
printf("c = %c\n", c);
return 0;
```

What are the possible outputs now?

```
Possible output:
pid = fork();
                                         c = b // in child
if (pid==0) {
                                         c = d // in child
    read(fd1, &c, sizeof(c));
    printf("c = %c\n", c);
                                         c = c // in child
    dup2(fd1, fd2);
                                         c = d // in child
    read(fd3, &c, sizeof(c));
    printf("c = %c\n'', c);
                                         c = e // in parent
                                         c = e // in parent
if (pid!=0) waitpid(-1, NULL, 0);
read(fd1, &c, sizeof(c));
printf("c = %c\n", c);
read(fd2, &c, sizeof(c));
printf("c = %c\n", c);
return 0;
```

```
read(fd1, \&c, sizeof(c)); // a
read(fd2, &c, sizeof(c)); // a
dup2(fd2, fd3);
read(fd3, \&c, sizeof(c)); // b
read(fd2, \&c, sizeof(c)); // c
pid = fork();
if (pid==0) {
    read(fd1, &c, sizeof(c));
    dup2(fd1, fd2);
    read(fd3, &c, sizeof(c));
if (pid!=0) waitpid(-1, NULL, 0);
read(fd2, &c, sizeof(c));
read(fd1, &c, sizeof(c));
```

- Child creates a copy of the parent fd table
 - dup2/open/close in parent only before fork() affect the child
 - dup2/open/close in child do NOT affect the parent
- File descriptors across process share the same file offset.



Virtual Address - 18 Bits

Physical Address - 12 Bits

Page Size - 512 Bytes

TLB is 8-way set associative

Cache is 2-way set associative

Final S-02 (#5)

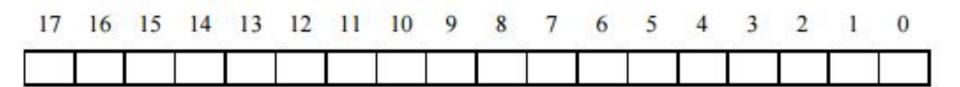
Lecture 18: VM - Systems

| V/DX: | DDM | - | Table | DDAT | 37-17-1 |
|-------|-----|-------|-------|------|---------|
| VPN | PPN | Valid | VPN | PPN | Valid |
| 000 | 7 | 0 | 010 | 1 | 0 |
| 001 | 5 | 0 | 011 | 3 | 0 |
| 002 | 1 | 1 | 012 | 3 | 0 |
| 003 | 5 | 0 | 013 | 0 | 0 |
| 004 | 0 | 0 | 014 | 6 | 1 |
| 005 | 5 | 0 | 015 | 5 | 0 |
| 006 | 2 | 0 | 016 | 7 | 0 |
| 007 | 4 | 1 | 017 | 2 | 1 |
| 008 | 7 | 0 | 018 | 0 | 0 |
| 009 | 2 | 0 | 019 | 2 | 0 |
| 00A | 3 | 0 | 01A | 1 | 0 |
| 00B | 0 | 0 | 01B | 3 | 0 |
| 00C | 0 | 0 | 01C | 2 | 0 |
| 00D | 3 | 0 | 01D | 7 | 0 |
| 00E | 4 | 0 | 01E | 5 | 1 |
| 00F | 7 | 1 | 01F | 0 | 0 |

| Index | Tag | PPN | Valid |
|-------|-----|-----|-------|
| 0 | 55 | 6 | 0 |
| | 48 | F | 1 |
| | 00 | A | 0 |
| | 32 | 9 | 1 |
| | 6A | 3 | 1 |
| | 56 | 1 | 0 |
| | 60 | 4 | 1 |
| | 78 | 9 | 0 |
| 1 | 71 | 5 | 1 |
| | 31 | A | 1 |
| | 53 | F | 0 |
| | 87 | 8 | 0 |
| | 51 | D | 0 |
| | 39 | E | 1 |
| | 43 | В | 0 |
| | 73 | 2 | 1 |

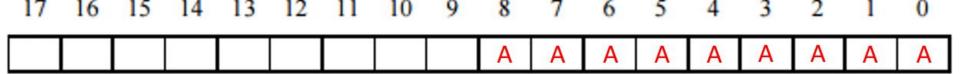
| | 2-way Set Associative Cache | | | | | | | | | | | | | |
|-------|-----------------------------|-------|--------|--------|--------|--------|-----|-------|--------|--------|--------|--------|--|--|
| Index | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | | |
| 0 | 7A | 1 | 09 | EE | 12 | 64 | 00 | 0 | 99 | 04 | 03 | 48 | | |
| 1 | 02 | 0 | 60 | 17 | 18 | 19 | 7F | 1 | FF | BC | 0B | 37 | | |
| 2 | 55 | 1 | 30 | EB | C2 | 0D | 0B | 0 | 8F | E2 | 05 | BD | | |
| 3 | 07 | 1 | 03 | 04 | 05 | 06 | 5D | 1 | 7A | 08 | 03 | 22 | | |

- (A) VPO: Virtual Page Offset
- (B) VPN: Virtual Page Number
- (C) TLBI: TLB Index
- (D) TLBT: TLB Tag

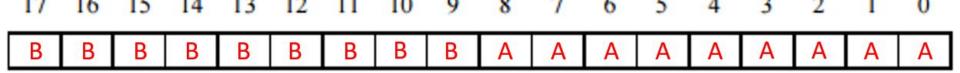


Label the following:

(A) VPO: Virtual Page Offset - Location in the page
 Page Size = 512 Bytes = 2⁹ → Need 9 bits



- (A) VPO: Virtual Page Offset
- (B) VPN: Virtual Page Number Everything Else

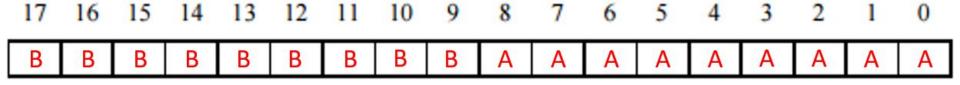


- (A) VPO: Virtual Page Offset
- (B) VPN: Virtual Page Number
- (C) TLBI: TLB Index Location in the TLB Cache



Label the following:

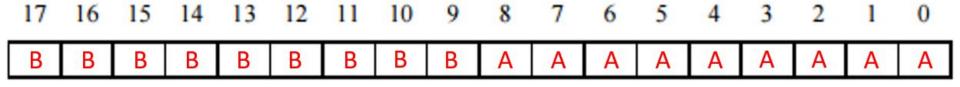
- (A) VPO: Virtual Page Offset
- (B) VPN: Virtual Page Number
- (C) TLBI: TLB Index Location in the TLB Cache
 2 Indices → 1 Bit



TLBI

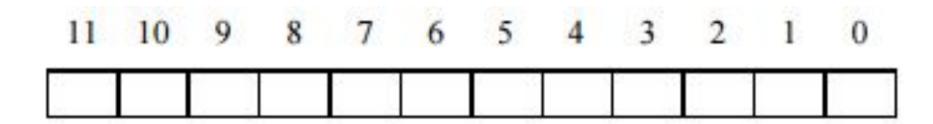
Label the following:

- (A) VPO: Virtual Page Offset
- (B) VPN: Virtual Page Number
- (C) TLBI: TLB Index
- (D) TLBT: TLB Tag Everything Else



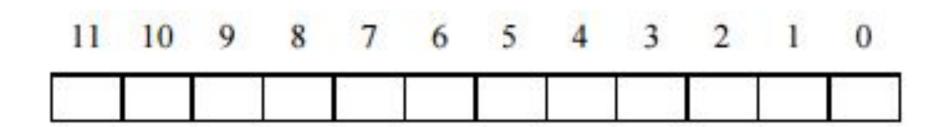
TLBT TLBI

- (A) PPO: Physical Page Offset
- (B) PPN: Physical Page Number
- (C) CO: Cache Offset
- (D) CI: Cache Index
- (E) CT: Cache Tag



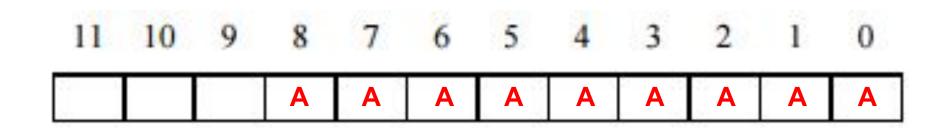
Label the following:

(A) PPO: Physical Page Offset

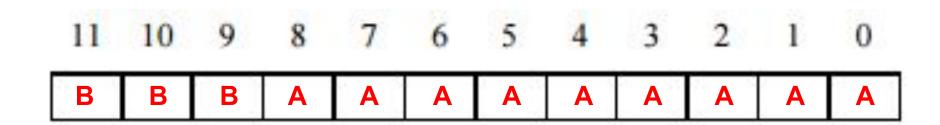


Label the following:

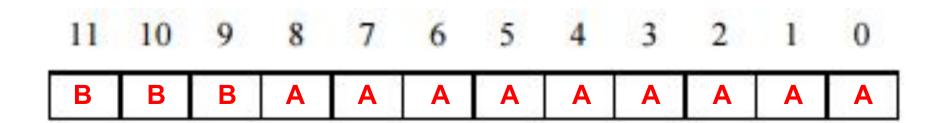
(A) PPO: Physical Page Offset - Same as VPO



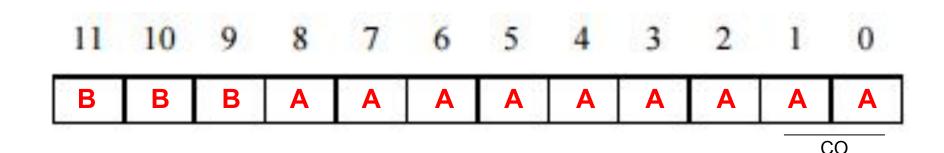
- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else



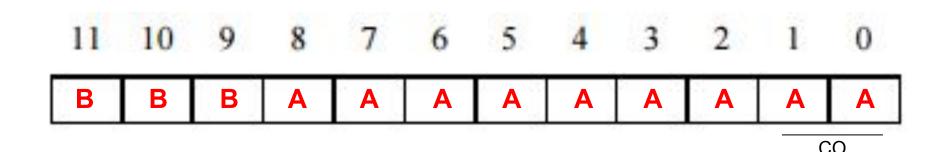
- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else
- (C) CO: Cache Offset Offset in Block



- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else
- (C) CO: Cache Offset Offset in Block4 Byte Blocks → 2 Bits



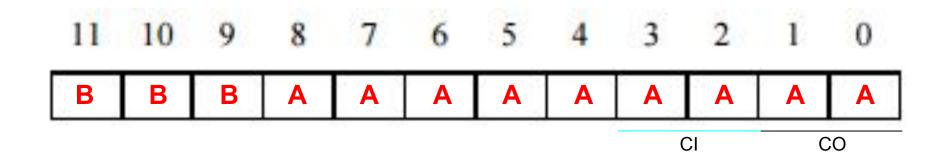
- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else
- (C) CO: Cache Offset Offset in Block
- (D) CI: Cache Index



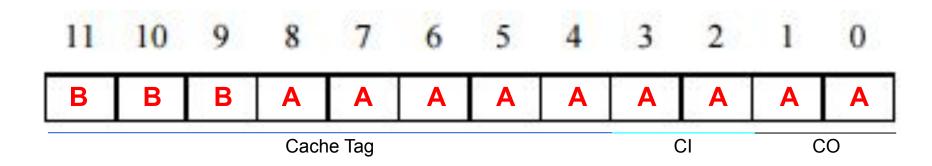
Label the following:

- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else
- (C) CO: Cache Offset Offset in Block
- (D) CI: Cache Index

4 Indices → 2 Bits

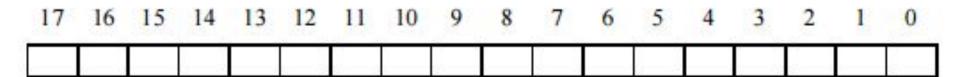


- (A) PPO: Physical Page Offset Same as VPO
- (B) PPN: Physical Page Number Everything Else
- (C) CO: Cache Offset Offset in Block
- (D) CI: Cache Index
- (E) CT: Cache Tag Everything Else



Now to the actual question!

Q) Translate the following address: 0x1A9F4

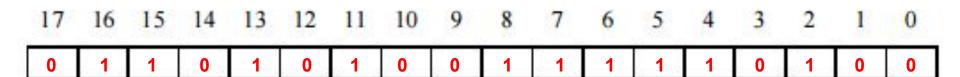


Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation

$$1 = 0001$$
 A = 1010

$$4 = 0100$$



Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- Extract Information:

VPN: 0x?? TLBI: 0x?? TLBT: 0x?? TLB Hit: Y/N? Page Fault: Y/N? PPN: 0x??

17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0

Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- Extract Information:

VPN: 0xD4 TLBI: 0x?? TLBT: 0x?? TLB Hit: Y/N? Page Fault: Y/N? PPN: 0x??

 17
 16
 15
 14
 13
 12
 11
 10
 9
 8
 7
 6
 5
 4
 3
 2
 1
 0

 0
 1
 1
 0
 1
 0
 1
 1
 1
 1
 1
 0
 0
 0

Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- Extract Information:

VPN: 0xD4 TLBI: 0x00 TLBT: 0x?? TLB Hit: Y/N? Page Fault: Y/N? PPN: 0x??

 17
 16
 15
 14
 13
 12
 11
 10
 9
 8
 7
 6
 5
 4
 3
 2
 1
 0

 0
 1
 1
 0
 1
 0
 1
 1
 1
 1
 1
 0
 1
 0
 0

Now to the actual question!

Q) Translate the following address: 0x1A9F4

- Write down bit representation
- 2. Extract Information:

TLBT: 0x6A VPN: 0xD4 TLBI: 0x00

PPN: 0x?? TLB Hit: Y/N? Page Fault: Y/N?

| Index | Tag | PPN | Valid |
|-------|-----|-----|-------|
| 0 | 55 | 6 | 0 |
| | 48 | F | 1 |
| | 00 | A | 0 |
| | 32 | 9 | 1 |
| | 6A | 3 | 1 |
| | 56 | 1 | 0 |
| | 60 | 4 | 1 |
| | 78 | 9 | 0 |
| 1 | 71 | 5 | 1 |
| | 31 | A | 1 |
| | 53 | F | 0 |
| | 87 | 8 | 0 |
| | 51 | D | 0 |
| | 39 | E | 1 |
| | 43 | В | 0 |
| | 73 | 2 | 1 |

| 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| | | | | | | | | | | | | | | | | | |

| | 0 |
|--|---|
|--|---|

Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- 2. Extract Information:

VPN: 0xD4 TLBI: 0x00 TLBT: 0x6A TLB Hit: Y! Page Fault: Y/N? PPN: 0x??

TEB THE TET AGO FACILITY TO THE OXI !

| | TI | B | |
|-------|-----|-----|-------|
| Index | Tag | PPN | Valid |
| 0 | 55 | 6 | 0 |
| 7,000 | 48 | F | 1 |
| | 00 | A | 0 |
| | 32 | 9 | 1 |
| | 6A | 3 | 1 |
| | 56 | 1 | 0 |
| | 60 | 4 | 1 |
| | 78 | 9 | 0 |
| 1 | 71 | 5 | 1 |
| | 31 | A | 1 |
| | 53 | F | 0 |
| | 87 | 8 | 0 |
| | 51 | D | 0 |
| | 39 | E | 1 |
| | 43 | В | 0 |
| | 73 | 2 | 1 |

| | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
|---|-------|------|----|----|------|------|----|----|-----|-----|---|---|------|----|-------|-----|---|-------|
| , | 0.000 | 2544 | | | 1000 | 2.33 | | | 277 | 900 | | | 2000 | 50 | 5-003 | 100 | | 10000 |

| | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 |
|--|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
|--|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Now to the actual question!

Q) Translate the following address: 0x1A9F4

- 1. Write down bit representation
- 2. Extract Information:

VPN: 0xD4 TLBI: 0x00 TLBT: 0x6A

TLB Hit: Y! Page Fault: N! PPN: 0x??

| ny . | TI | LB | |
|-------|-----|-----|-------|
| Index | Tag | PPN | Valid |
| 0 | 55 | 6 | 0 |
| 1,000 | 48 | F | 1 |
| | 00 | A | 0 |
| | 32 | 9 | 1 |
| | 6A | 3 | 1 |
| | 56 | 1 | 0 |
| | 60 | 4 | 1 |
| | 78 | 9 | 0 |
| 1 | 71 | 5 | 1 |
| | 31 | A | 1 |
| | 53 | F | 0 |
| | 87 | 8 | 0 |
| | 51 | D | 0 |
| | 39 | E | 1 |
| | 43 | В | 0 |
| | 73 | 2 | 1 |

| | | | | | | 3 | | 3/200 | 7.77 | 55 | | V | | | 35 70 10 | 4 | |
|---|---|---|---|-----|---|---|---|-------|------|----|---|---|---|---|----------|---|---|
| 0 | 1 | 1 | 0 | _1_ | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | _1_ | 0 | 0 |

Now to the actual question!

Q) Translate the following address: 0x1A9F4

- 1. Write down bit representation
- 2. Extract Information:

VPN: 0xD4 TLBI: 0x00 TLBT: 0x6A

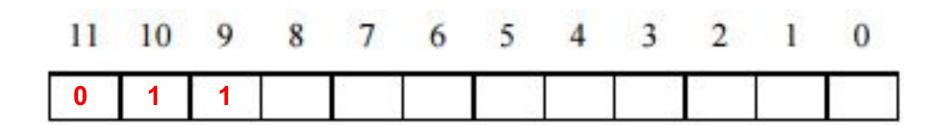
TLB Hit: Y! Page Fault: N! PPN: 0x3

| | TI | B | 7. 1910 |
|-------|-----|-----|---------|
| Index | Tag | PPN | Valid |
| 0 | 55 | 6 | 0 |
| | 48 | F | 1 |
| | 00 | A | 0 |
| | 32 | 9 | 1 |
| | 6A | 3 | 1 |
| | 56 | 1 | 0 |
| | 60 | 4 | 1 |
| | 78 | 9 | 0 |
| 1 | 71 | 5 | 1 |
| | 31 | A | 1 |
| | 53 | F | 0 |
| | 87 | 8 | 0 |
| | 51 | D | 0 |
| | 39 | E | 1 |
| | 43 | В | 0 |
| v | 73 | 2 | 1 |

| | | | | | 258 | 1000 | | - | 300 | 79 | | | | (6) | -7% | . T. | . R | L. Comment |
|---|---|---|---|---|-----|------|---|---|-----|----|---|---|---|-----|-----|------|-----|------------|
| ĵ | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 |

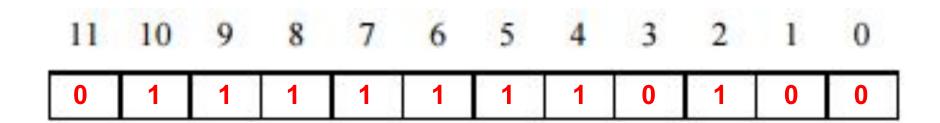
Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- Extract Information
- 3. Put it all together: PPN: 0x3, PPO = 0x??



Now to the actual question!

- Q) Translate the following address: 0x1A9F4
- 1. Write down bit representation
- Extract Information
- 3. Put it all together: PPN: 0x3, PPO = VPO = 0x1F4



Q) What is the value of the address?

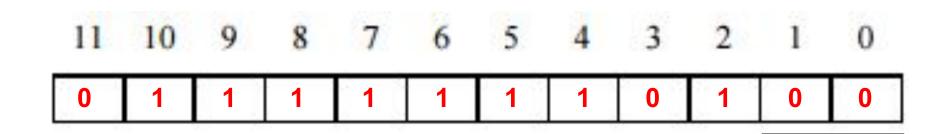
CO: 0x?? CI: 0x?? CT: 0x?? Cache Hit: Y/N? Value:0x??



Q) What is the value of the address?

1. Extract more information

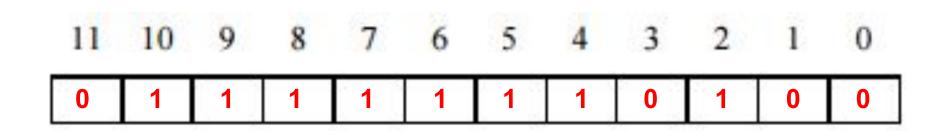
CO: 0x00 CI: 0x?? CT: 0x?? Cache Hit: Y/N? Value:0x??



Q) What is the value of the address?

Extract more information

CO: 0x00 CI: 0x01 CT: 0x?? Cache Hit: Y/N? Value:0x??



Q) What is the value of the address?

- 1. Extract more information
- 2. Go to Cache Table

CO: 0x00 CI: 0x01 CT: 0x7F Cache Hit: Y/N? Value:0x??

| | 2-way Set Associative Cache | | | | | | | | | | | |
|-------|-----------------------------|-------|--------|--------|--------|--------|-----|-------|--------|--------|--------|--------|
| Index | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 |
| 0 | 7A | 1 | 09 | EE | 12 | 64 | 00 | 0 | 99 | 04 | 03 | 48 |
| 1 | 02 | 0 | 60 | 17 | 18 | 19 | 7F | 1 | FF | BC | 0B | 37 |
| 2 | 55 | 1 | 30 | EB | C2 | 0D | 0B | 0 | 8F | E2 | 05 | BD |
| 3 | 07 | 1 | 03 | 04 | 05 | 06 | 5D | 1 | 7A | 08 | 03 | 22 |

11 10 9 8 7 6 5 4 3 2 1 0

Q) What is the value of the address?

- 1. Extract more information
- 2. Go to Cache Table

CO: 0x00 CI: 0x01 CT: 0x7F Cache Hit: Y Value:0x??

| | 2-way Set Associative Cache | | | | | | | | | | | |
|-------|-----------------------------|-------|--------|--------|--------|--------|-----|-------|--------|--------|--------|--------|
| Index | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 |
| 0 | 7A | 1 | 09 | EE | 12 | 64 | 00 | 0 | 99 | 04 | 03 | 48 |
| 1 | 02 | 0 | 60 | 17 | 18 | 19 | 7F | 1 | FF | BC | 0B | 37 |
| 2 | 55 | 1 | 30 | EB | C2 | 0D | 0B | 0 | 8F | E2 | 05 | BD |
| 3 | 07 | 1 | 03 | 04 | 05 | 06 | 5D | 1 | 7A | 08 | 03 | 22 |

11 10 9 8 7 6 5 4 3 2 1 0

0 1 1 1 1 1 1 1 1 0 1 0 0

Q) What is the value of the address?

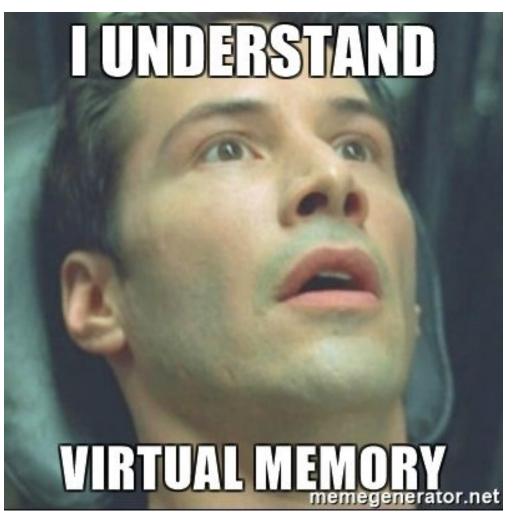
- 1. Extract more information
- 2. Go to Cache Table

CO: 0x00 CI: 0x01 CT: 0x7F Cache Hit: Y Value:0xFF

| | 2-way Set Associative Cache | | | | | | | | | | | |
|-------|-----------------------------|-------|--------|--------|--------|--------|-----|-------|--------|--------|--------|--------|
| Index | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 | Tag | Valid | Byte 0 | Byte 1 | Byte 2 | Byte 3 |
| 0 | 7A | 1 | 09 | EE | 12 | 64 | 00 | 0 | 99 | 04 | 03 | 48 |
| 1 | 02 | 0 | 60 | 17 | 18 | 19 | 7F | 1 | FF | BC | 0B | 37 |
| 2 | 55 | 1 | 30 | EB | C2 | 0D | 0B | 0 | 8F | E2 | 05 | BD |
| 3 | 07 | 1 | 03 | 04 | 05 | 06 | 5D | 1 | 7A | 08 | 03 | 22 |

11 10 9 8 7 6 5 4 3 2 1 0

0 1 1 1 1 1 1 1 1 0 1 0 0



Good luck!



Malloc



Malloc

- Fit algorithms first/next/best/good
- Fragmentation
 - Internal inside blocks
 - External between blocks
- Organization
 - Implicit
 - Explicit
 - Segregated













- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|----|----|----|----|----|----|
| a = malloc(32) | | | | | | |
| b = malloc(16) | | | | | | |
| c = malloc(16) | | | | | | |
| d = malloc(40) | | | | | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|-----|----|----|----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | | | | | | |
| c = malloc(16) | | | | | | |
| d = malloc(40) | | | | | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|-----|-----|----|----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | | | | | | |
| d = malloc(40) | | | | | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|-----|-----|-----|----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | | | | | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|-----|-----|-----|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|-----|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | 48a | 32a | 80a | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | 48a | 32a | 80a | | | |
| free(b) | 48a | 32f [0] | 80a | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal?

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | 48a | 32a | 80a | | | |
| free(b) | 48a | 32f [0] | 80a | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal
 - (48-16) + (80-48) = 64
 - external?

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | 48a | 32a | 80a | | | |
| free(b) | 48a | 32f [0] | 80a | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal
 - (48-16) + (80-48) = 64
 - external
 - **32**

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48a | 32a | 32f [0] | 48a | | |
| free(d) | 48a | 32a | 80f [0] | | | |
| f = malloc(48) | 48a | 32a | 80a | | | |
| free(b) | 48a | 32f [0] | 80a | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|----|----|----|----|----|----|
| a = malloc(32) | | | | | | |
| b = malloc(16) | | | | | | |
| c = malloc(16) | | | | | | |
| d = malloc(40) | | | | | | |
| free(c) | | | | | | |
| free(a) | | | | | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | | | | | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|-----|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | | | | | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | | | | | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|-----|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | 48f [0] | 32a | 32a | 54a | | |
| free(b) | | | | | | |

- 16 byte align
- coalesced
- footerless
- 32 min size

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | 48f [0] | 32a | 32a | 54a | | |
| free(b) | 48f [1] | 32f [0] | 32a | 54a | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal?

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | 48f [0] | 32a | 32a | 54a | | |
| free(b) | 48f [1] | 32f [0] | 32a | 54a | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal
 - (32-16) + (54-48) = 24
 - external?

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | 48f [0] | 32a | 32a | 54a | | |
| free(b) | 48f [1] | 32f [0] | 32a | 54a | | |

- 16 byte align
- coalesced
- footerless
- 32 min size
- fragmentation?
 - internal
 - (32-16) + (54-48) = 24
 - external
 - **48+32 = 80**

| | #1 | #2 | #3 | #4 | #5 | #6 |
|----------------|---------|---------|---------|---------|----|----|
| a = malloc(32) | 48a | | | | | |
| b = malloc(16) | 48a | 32a | | | | |
| c = malloc(16) | 48a | 32a | 32a | | | |
| d = malloc(40) | 48a | 32a | 32a | 48a | | |
| free(c) | 48a | 32a | 32f [0] | 48a | | |
| free(a) | 48f [0] | 32a | 32f [1] | 48a | | |
| e = malloc(16) | 48f [0] | 32a | 32a | 48a | | |
| free(d) | 48f [1] | 32a | 32a | 48f [0] | | |
| f = malloc(48) | 48f [0] | 32a | 32a | 54a | | |
| free(b) | 48f [1] | 32f [0] | 32a | 54a | | |

Good luck!

