2025-2 IMEN891M – Financial BigData Analysis

Final Presentation



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Introduction (Revisited)



Background

- High dimensional data analysis is essential, yet poses significant challenges in modern econometrics.
- Classic mean-variance Markowitz portfolio theory often fails into higher dimension of data due to unstable covariance estimation, omitted network dependencies and the curse of dimensionality.
- To address these challenges, various methodologies has before been proposed, a few important ones are:

Dimensional Overfitting Data Challenges

Image Source: Van Ottten, Neri; Spotintelligence.com

POET - High dimensional covariance estimation (Fan, Liao & Mincheva, 2013)

By applying factor models and sparsity in the residual covariance matrix, it efficiently estimates high-dimensional covariance matrices.

SAR - Spatial Autoregression (Cliff & Ord, 1981; Baltegi et al., 2014)

- Model that **captures dependencies** structures across assets and markets.
- From here, we take some ideas with subgrouping.

LASSO - Regularized regression (Tibshirani, 1996)

Imposes sparsity on portfolio weights, which improves stability in portfolio optimization in high dimensions.



Image Source: OpenAl

Therefore, we integrate these High-Dimensional Methods for **Robust Portfolio Construction.**



DATA SELECTION

- We employ a cross-asset dataset (2015.01.01 - 2024.12.31) spanning totally **71** series. (Data Source : <u>investing.com</u>, <u>Yahoo Finance</u>, <u>etc.</u>)

Equities

 Global indices and stocks (From S&P 500 and it's sectoral indices, MSCI World, Major regional stocks and indexes like Nikkei, KOSPI etc...)

Fixed Income

- U.S. Treasury yields (3M, 5Y, 10Y, 30Y, corporate bond spreads)

Commodities

- Gold, Oil(Brent, WTI), industrial metals, agricultural futures, etc..

Currencies

- USDKRW, JPYKRW, EURKRW, CNYKRW

Others

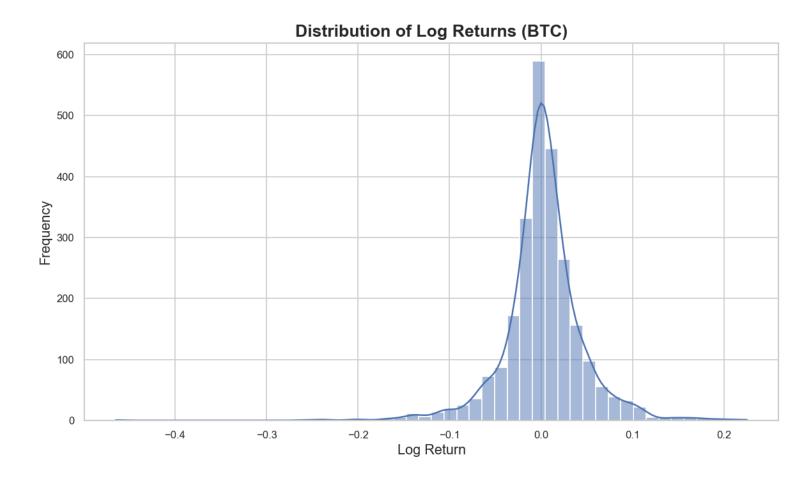
- Bitcoin (Cryptocurrencies)
- VIX(Volatility Measures)
- Macro indicator proxies (ex. CPI, Dollar Index, etc..)



Explanatory Data Analysis

Distribution of Log Returns

- As a representative of all assets, **Bitcoin**, the asset with the highest average return and volatility, has been selected.
- The distribution of BTC log returns is sharply peaked around zero, indicating most daily changes are small.
- The **heavy tails** on both sides show the presence of large price swings compared to a normal distribution.
- The curve is **slightly asymmetric**, suggesting mild skewness in return behavior.
- This pattern reflects Bitcoin's high volatility and non-Gaussian nature, common in crypto markets.

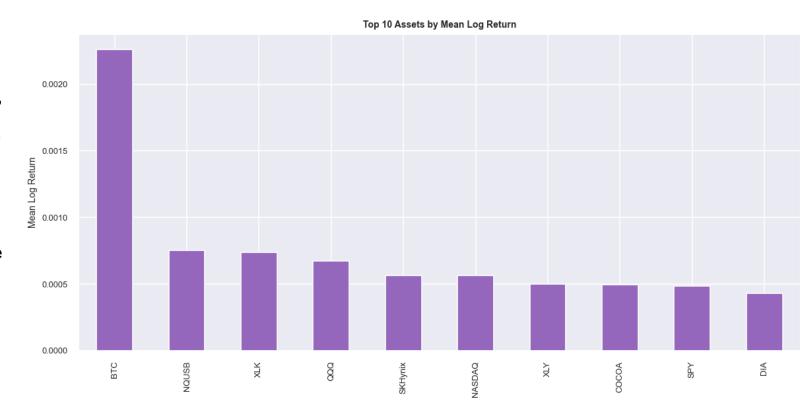




Explanatory Data Analysis

Mean Log Return

- BTC shows the highest mean log return, significantly outperforming all other assets, reflecting its high volatility and long-term upward trend.
- Tech-related assets such as NQUSB, XLK, and QQQ follow, indicating strong performance from the digital and technology sectors.
- Traditional indices (SPY, DIA) and commodities (COCOA) exhibit lower mean returns, consistent with their relatively stable nature.
- Overall, the pattern highlights a clear riskreturn trade-off, where higher-risk assets yield higher average log returns.



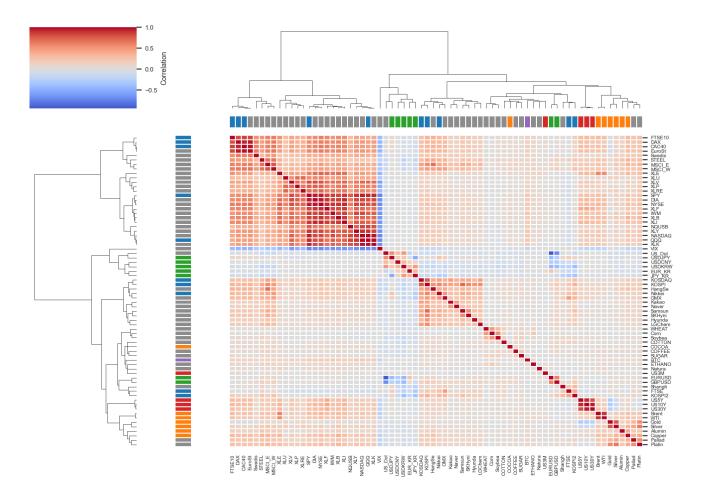


Explanatory Data Analysis

Correlation Matrix

- The correlation heatmap with hierarchical clustering reveals distinct asset groupings based on return co-movements.
- Equity indices and ETFs (e.g., SPY, QQQ, NASDAQ, NQUSB) form a tight cluster with strong positive correlations, shown in deep red.
- Commodities and currencies exhibit weaker or negative correlations, suggesting diversification benefits across asset classes.
- The blue patches indicate negatively correlated pairs, mainly between volatility indices (e.g., VIX) and risk-on assets, consistent with market stress dynamics.

Correlation Matrix (Truncated Labels)

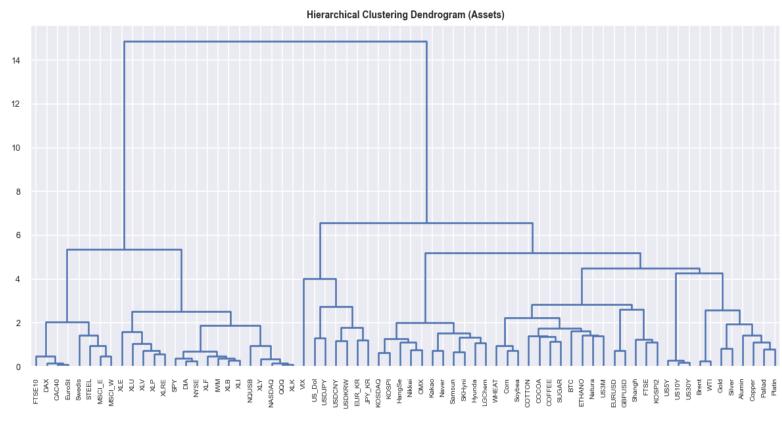




Explanatory Data Analysis

Dendrogram Analyis

- The hierarchical clustering dendrogram visualizes the structural relationships among assets, grouping those with similar return dynamics.
- Unlike the baseline EDA clustering, our integrated model captures clearer and more economically consistent clusters, separating equities, commodities, and currencies more distinctly.
- This suggests that the integrated framework enhances cross-asset structure recognition, aligning with intuitive market linkages.
- Overall, it demonstrates improved cluster interpretability and coherence compared to standard correlation-based grouping.

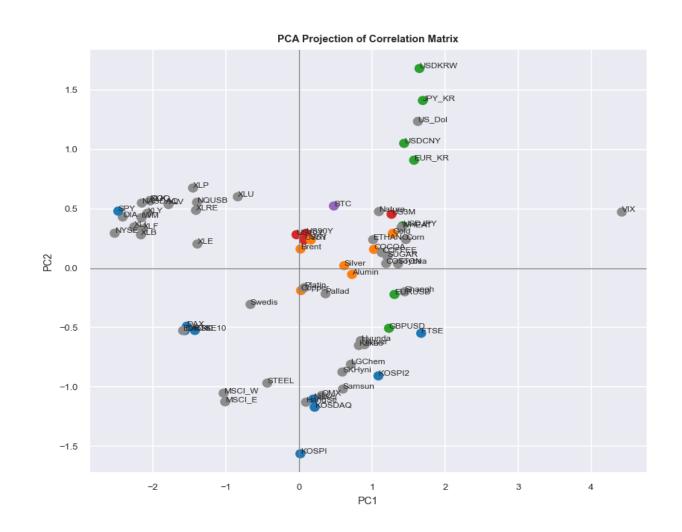




Explanatory Data Analysis

PCA Projection Analyis

- Even with four principal components, PCA explains only 43% of total variance, revealing limited ability to capture complex market dynamics.
- This suggests that a large portion of assetspecific or nonlinear variation remains unexplained.
- Our integrated model combines multiple covariance estimators to better capture both systematic and idiosyncratic risk factors.
- We expect it to explain a substantially larger share of market variance compared to PCA.

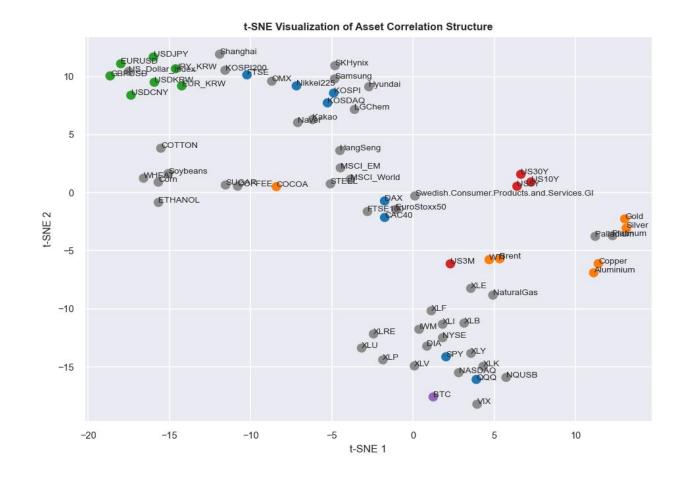




Explanatory Data Analysis

t-SNE Visualization

- The t-SNE visualization maps highdimensional correlations into a 2D space, revealing clear clusters across asset classes.
- Equities (e.g., QQQ, XLK, NASDAQ) form a
 distinct group, while commodities (e.g., Gold,
 Copper, Aluminium) and FX pairs (e.g.,
 USDKRW, EURUSD) occupy separate regions.
- BTC and VIX are positioned far from other assets, highlighting their unique, uncorrelated behavior.
- Compared to raw data clustering, the integrated model produces a more coherent and interpretable structure, capturing both global and local dependencies among assets.





Step 0. Notation & Setup

- Let the time index be $t=1,\ldots,T$, the number of assets be N, and the rolling window length be N, and the rolling window length be W.
- The return matrix is denoted by $R \in \mathbb{R}^{T \times N}$, where each element $R_{t,i}$ represents the log return of asset i at time t.
- The **test period** is defined as $T_{test} \subset \{1, ..., T\}$, and the forecasting horizon is $h \in \mathbb{N}$ (in code: h = 2).
- The **gross exposure constraint** is controlled by $G \in [1, \infty)$, where G = 1 corresponds to a long-only portfolio and G > 1 allows long-short positions.
- The **composite macro factor** y_t is constructed as the average of three major U.S. market indices: $y_t = \frac{1}{3}(R_{t,SPY} + R_{t,NASDAQ} + R_{t,DIA})$, representing the aggregate market-wide movement
- The **rolling window** used for estimation at time t is defined as : $\mathcal{W}_t = \{t W, ..., t 1\}$, which corresponds to the past W trading days immediately preceding t.

Step 1: LASSO-Based Asset Selection

- To identify assets that move consistently with the overall market factor and reduce dimensionality and remove noisy, uninformative assets.
- Regress the composite macro factor y_t on asset returns X_t :

$$\min_{\beta} \frac{1}{W} \sum_{s \in \mathcal{W}_t} (y_s - X_s^T \beta)^2 + \lambda ||\beta||_1$$

- Rolling window of W = 250 days.
- λ determined by cross-validation (LassoCV).
- Each day's regression uses the most-recent window → adaptive over time.

LASSO - Regularized regression (Tibshirani, 1996)

- To avoid overfitting and spurious correlations, we apply LASSO regression : $\hat{\beta} = \arg\min_{\beta} ||y X\beta||_2^2 + \lambda ||\beta||_1$ where y is the asset return or factor proxy, and X is the predictor matrix.
- LASSO selects a sparse subject of variables, forming the observed macro-finance block f_t^{Macro} .



Step 2. Hierarchical Clustering of Selected Assets

- To group the selected assets A_t into structurally similar clusters.
- To capture sector, style, or co-movement patterns in return-behavior.

1) Correlation Matrix

- Using the selected assets' returns within the same rolling window: $\rho_{i,i} = \operatorname{Corr}(R_i, R_i)$
- Convert to a distance measure (Highly correlated assets have similar dist.):

 $D_{ij} = 1 - \rho_{ij}$

2) Hierarchical Linkage

- Apply Ward linkage, which merges clusters to minimize within-cluster variance.
- Iteratively combine the most similar pairs until all assets from a hierarchy.
- Determine the final number of clusters using a distance threshold.

3) Cluster Assignment

- Each assets receives a cluster label : $c_t(i) \in \{1,2,\ldots,K_t\}$ where K_t = # of clusters at time t.

Step 3: Factor Decomposition by PCA (POET Framework)

- To decompose asset returns into **systematic (factor)** and **idiosyncratic** components.
- Form the foundation for **POET** (**Principal Orthogonal complement Thresholding**) covariance estimation.

1) PCA Decomposition

- On the selected asset returns $R^{(t)} \in \mathbb{R}^{W \times N_t}$: $R^{(t)} \approx F_t L_t^T$ where F_t denotes factor return matrix (common components), and L_t : factor loading matrix(exposures of each asset).

2) Covariance Components (Fan, Liao & Mincheva, 2013)

- Compute two covariance parts (Factor, Idiosyncratic Part):

$$\Sigma_t^{factor} = L_t \text{Cov}(F_t) L_t^T, \qquad \Sigma_t^{id,raw} = Cov(R^{(t)} - F_t L_t^T)$$

3) POET Integration

- Combine both parts after applying thresholding on the idiosyncratic covariance. (Next step).
- Produces a low-rank + sparse covariance estimator.



Step 4. Integrated Covariance Construction (POET-Based)

 To construct a stable covariance estimator combining low-rank factor structure (POET) and block-sparse residuals and incorporate clustering information to reflect market structure.

1) Cluster-based Hard Thresholding

- Build a binary mask using hierarchical clustering results:

$$M_{ij} = \begin{cases} 1, & c_t(i) = c_t(j) \\ 0, & \text{otherwise} \end{cases}$$

- Apply thresholding to the idiosyncratic covariance:

$$\Sigma_t^{id,blk} = \Sigma_t^{id,raw} \odot M_t$$

- It retains correlations within the same cluster, sets cross-cluster elements to zero.

2) Integrated Covariance Estimator

$$\hat{\Sigma}_{t}^{integrated} = \Sigma_{t}^{factor} + \Sigma_{t}^{id,blk}$$

- Low-rank factor component from POET
- Block-sparse residual component from clustering

Step 5: Benchmark Covariance Models

- Construct baseline covariance estimators for comparison against the proposed integrated model.

A) LASSO-only Model

$$\Sigma_t^{LASSO} = Cov(R_t^{(\mathcal{A}_t)})$$

- Uses only asset selected by LASSO (no factor or clustering).
- Simple Empirical covariance within the active asset set.
- Measures how well pure statistical selection performs.

B) POET-only Model

$$\Sigma_t^{POET} = L_t Cov(F_t) L_t^T + diag(Cov(R^{(t)} - F_t L_t^T))$$

- Implements the **standard POET framework** (Fan et al., 2013).
- Uses low-rank factor structure + diagonal residuals.
- Captures global systematic risk, but ignores cross-asset structure.

C) OLS(Shrinkage) Model

$$\Sigma_t^{Shrinkage} = (1 - \alpha)\Sigma_t^{sample} + \alpha\Sigma_t^{target}$$

- Estimated using Ledoit–Wolf shrinkage method.
- Shrinks noisy sample covariance toward a well-conditioned target.



Step 6. Portfolio Optimization & Performance Evaluation

- Evaluate each covariance estimator (Integrated & Benchmarks) through **Global Minimum Variance (GMV)** portfolio backtesting.

1) Global Minimum Variance (GMV) Optimization Problem

- For each covariance matrix Σ_t , find portfolio weights w_t minimizing portfolio variance: $\min_w w^T \Sigma_t w$ subject to $\sum_i w_i = 1$, $\sum_i |w_i| = G$
- *G* : Gross exposure constraint (1.0, 1.25, ..., 3.0)
- w_i: Portfolio weight of asset i
- Solved via SLSQP (Sequential Least Squares Quadratic Programming)

2) Backtesting Framework

- Rolling-window optimization over years 2022-2024.
- Forecast horizon : h = 2 days ahead
- Compute realized returns using future data:

$$r_{p,t+1:t+h} = w_t^T R_{t+1:t+h}$$

3) Metrics

Metric	Definition	Interpretation
Annualized Return (%)	$\overline{r_p} \times 252$	Profitability
Annualized Risk (%)	$\sigma_p \times \sqrt{252}$	Volatility
Sharpe Ratio	$rac{\overline{r_p}}{\sigma_p}\sqrt{252}$	Risk-adjusted return
Frobenius Loss	$\frac{\left \left \Sigma_t^{real} - \Sigma_t^{forecast}\right \right _F}{N}$	Covariance prediction error
KL Divergence	$\frac{1}{2} \left[\operatorname{tr} \left(\left(\Sigma^{forecast} \right)^{-1} \Sigma^{real} \right) - n + \log \frac{\left \Sigma^{forecast} \right }{\left \Sigma^{real} \right } \right]$	Distributional gap
Risk Gap	$ \sigma_{ex-post} - \sigma_{ex-ante} /\sigma_{ex-post}$	Accuracy of Risk Prediction



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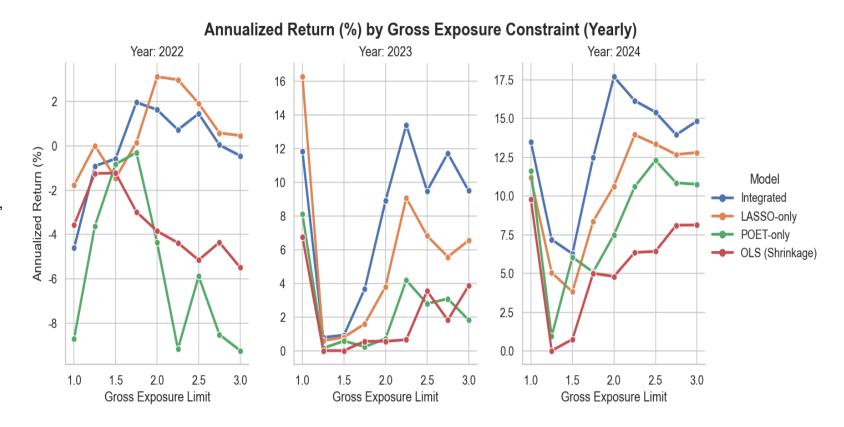
Summary of Methodology

Step	Method	Mathematical Role	Expected Benefit
1	LASSO	Sparse regression	Select market-linked assets
2	Clustering	Structural grouping	Reflect sector/style patterns
3	POET (PCA)	Factor decomposition	Capture common systematic risk
4	Hard-Thresholding	Block sparsity	Preserve intra-cluster correlation
5	GMV Optimization	Quadratic programming	Stable portfolio weights
6	Evaluation Metrics	Frobenius / KL / Risk Gap	Validate predictive accuracy



Annualized Return

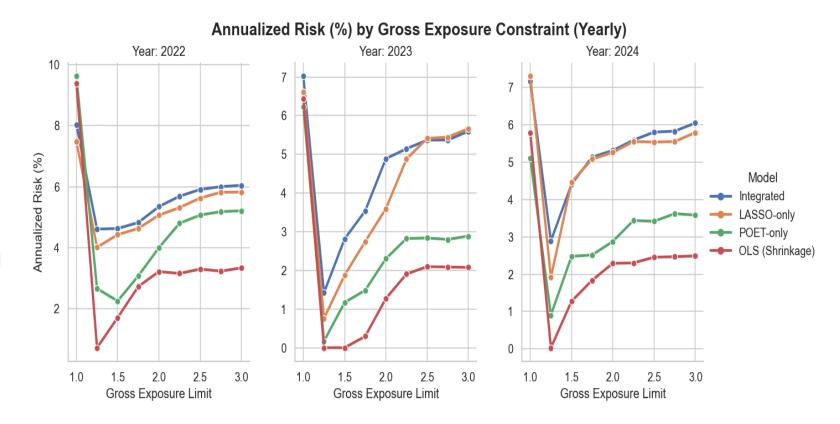
- Integrated model shows the most consistent and robust performance across years, maintaining positive and stable returns even at high exposure levels.
- In 2022 (down market), it effectively suppressed noise and avoided overfitting through block-sparse covariance.
- During 2023–2024 (recovery and expansion), Integrated model achieved higher responsiveness and efficient risk-return balance, outperforming benchmarks.
- LASSO-only fluctuates under regime shifts, POET-only underfits, and OLS (Shrinkage) remains overly conservative with limited upside.





Annualized Risk

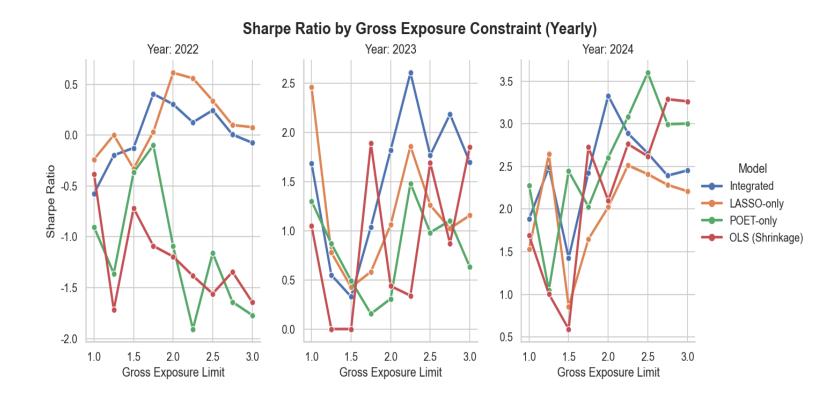
- Across all years, the Integrated model
 maintains a moderate and controlled risk
 profile, showing smooth increases with
 exposure and no abrupt volatility spikes.
- In low-exposure regimes (G ≤ 1.5), all models experience a sharp risk drop, but Integrated stabilizes faster than others, indicating better covariance regularization.
- POET-only and OLS (Shrinkage) display the lowest absolute risk, but at the cost of under-exposure and limited returns, implying over-conservatism.
- LASSO-only becomes unstable at higher exposures, while Integrated sustains consistent risk scaling aligned with expected leverage effects.





Sharpe Ratio

- Integrated model consistently achieves the highest or near-highest Sharpe ratios, showing balanced risk-return efficiency across all years.
- In 2022 (volatile market), it maintains positive Sharpe while others fluctuate, reflecting effective noise suppression and stable covariance estimation.
- During 2023–2024, Integrated and OLS models both improve sharply, but Integrated remains more responsive to exposure scaling and market recovery.
- LASSO-only delivers short-lived peaks, and POET-only exhibits delayed improvements, confirming that hybrid integration yields superior risk-adjusted performance.

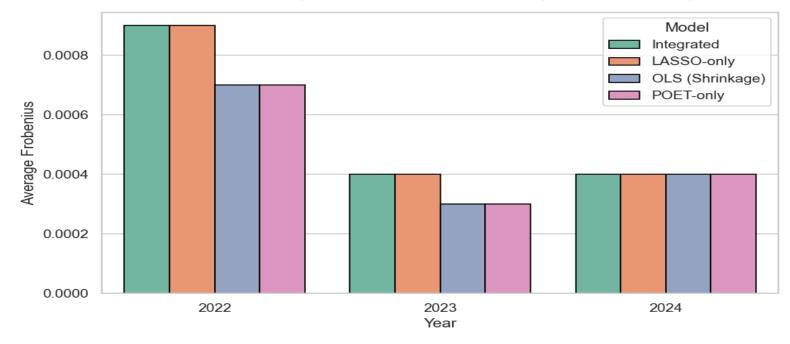




Mean Frobenius Dist. (Cross-sectional accuracy)

- Integrated model and LASSO-only show higher errors in 2022, likely due to unstable covariance dynamics under market stress.
- From 2023 onward, all models converge to lower Frobenius norms, indicating stabilization and improved estimation consistency.
- OLS (Shrinkage) and POET-only consistently maintain the smallest deviations, highlighting their strong baseline stability but limited adaptability.
- Integrated model's error reduction over time suggests that its hybrid structure learns and regularizes better across regimes.

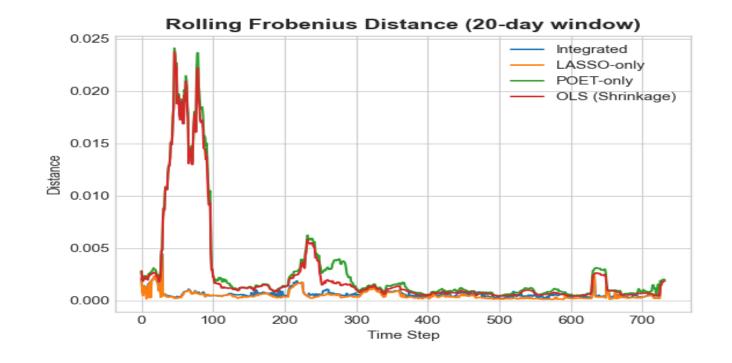
Frobenius (Mean across Gross Exposure Levels)





Rolling Frobenius Dist. (Temporal Stability)

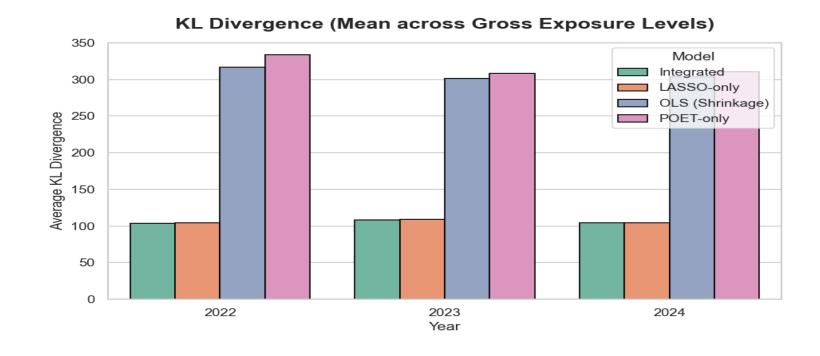
- Despite higher average Frobenius distance in annual means, the Integrated model maintains the lowest rolling error across time.
- It exhibits remarkable temporal consistency, showing minimal spikes even during early highvolatility periods.
- OLS and POET-only display large transient deviations, indicating sensitivity to regime shifts and local covariance shocks.
- The Integrated estimator thus demonstrates superior stability and robust adaptation under evolving market conditions.





KL Divergence

- Integrated model consistently records the lowest KL divergence, meaning it captures true covariance structure with minimal information loss.
- OLS and POET-only show extremely high divergences, reflecting rigid shrinkage or over-simplified factor structures.
- LASSO-only performs moderately well but lacks cross-cluster coherence, while the Integrated model balances sparsity and dependency learning.
- Overall, the Integrated estimator achieves the most faithful approximation of market risk distribution across all years.



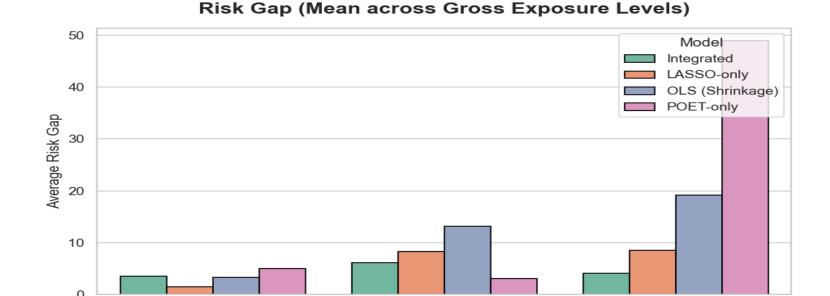
2022



2024

Risk Gap

- Integrated model maintains consistently low risk gaps across all years, showing strong alignment between predicted and realized volatility.
- OLS and especially POET-only exhibit rapidly widening gaps in 2024, implying systematic underestimation of true portfolio risk.
- LASSO-only achieves moderate accuracy but fluctuates over time, lacking robustness under regime transitions.
- Overall, the Integrated model provides the most reliable volatility forecasts, balancing flexibility and structural stability in covariance updates.



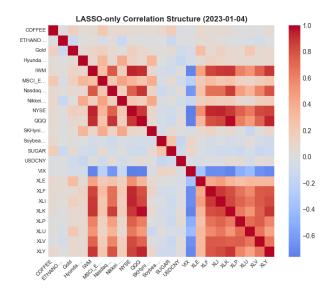
2023

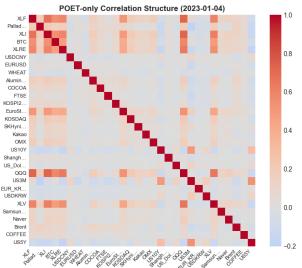
Year

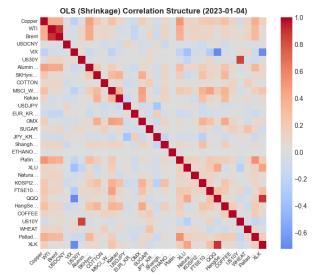


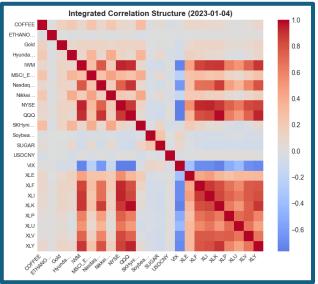
Correlation Structure Analysis

- LASSO-only captures clear cluster blocks (e.g., sector-wise correlations), but tends to over-sparsify and lose inter-cluster dependencies.
- OLS and POET-only produce diffuse, unstructured correlations, indicating over-smoothed or noisy covariance patterns.
- Integrated model preserves the interpretable block structures observed in LASSO while suppressing spurious noise — effectively balancing sparsity and continuity in correlation geometry.
- Visually, the Integrated estimator inherits the structural clarity of LASSO and the global stability of shrinkage, achieving the best of both approaches.





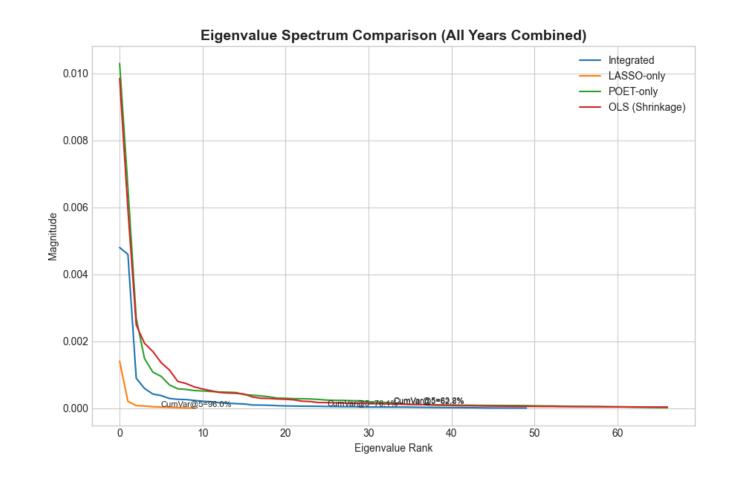






Eigenvalue Spectrum Comparison

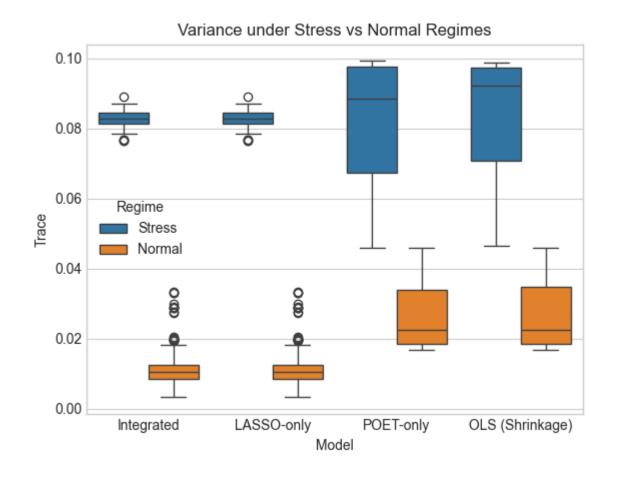
- Integrated model shows a smooth and gradual eigenvalue decay, indicating balanced factor contributions and improved diversification.
- LASSO-only collapses rapidly with few dominant eigenvalues, suggesting oversparsification and loss of secondary risk structure.
- OLS and POET-only display heavier tails, implying redundant or noisy factor components.
- Overall, the Integrated estimator captures richer latent structure, preserving essential covariance geometry while suppressing noise.





Variance under Stress vs. Normal Periods

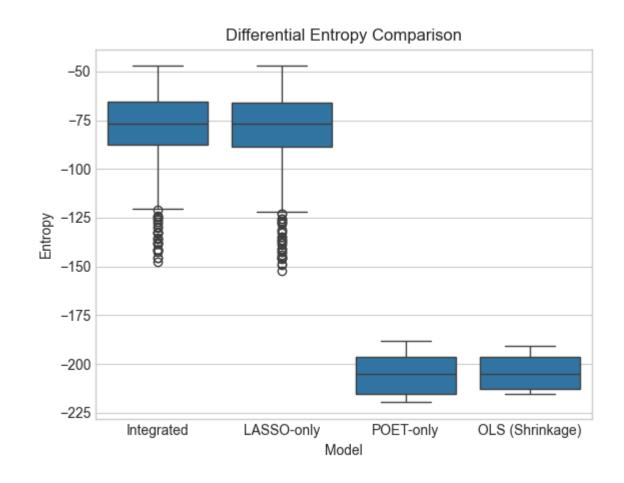
- Integrated model maintains the most stable variance across both stress and normal regimes, showing controlled volatility and strong adaptability under market shocks.
- Even during high-volatility periods, its total portfolio variance remains well-controlled, reflecting **robust adaptability** and **effective suppression of noise-driven covariance inflation**.
- LASSO-only remains relatively stable but underestimates systemic risk due to over-sparsification.
- POET-only and OLS exhibit large variance jumps and dispersion, indicating instability and overreaction during stress periods.
- Overall, the Integrated model achieves balanced risk sensitivity, reacting appropriately to market stress while preserving estimation stability.





Differential Entropy Comparison

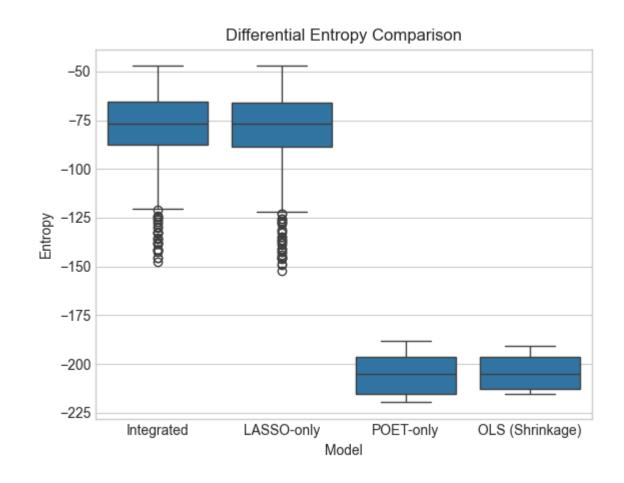
- Integrated and LASSO-only models exhibit significantly higher entropy, capturing richer dependency structures and a broader spread of risk factors.
- In contrast, POET-only and OLS (Shrinkage) show very low entropy, reflecting over-compressed or oversmoothed covariance structures that may ignore meaningful cross-asset variations.
- The Integrated model preserves LASSO's structural diversity while maintaining stability — balancing information richness and robustness.
- High entropy combined with stable variance (previous slide) suggests that the Integrated estimator captures complexity without instability.





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- Integrated and LASSO-only models exhibit significantly higher entropy, capturing richer dependency structures and a broader spread of risk factors.
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Discussion / Interpretation



Why does the Integrated Model perform better?

Cluster-based Residual Sparsifiaction

- The Integrated estimator applies hard-thresholding within correlation clusters, retaining intra-cluster dependencies while suppressing cross-cluster noise.
- This yields a block-sparse covariance structure that mirrors real market segmentation — e.g., sectoral or macro-style partitions (Equity / Commodity / FX).
- As a result, estimation noise is reduced without erasing genuine structural relationships, achieving a rare balance between bias reduction and variance control.

Statistical Implications: Bias-Variance Tradeoff

- LASSO-only induces high bias (over-sparsification), while OLS and POET suffer from high variance (overfitting / dense noise).
- The Integrated approach acts as a **structural regularizer** as shrinking noise-dominated correlations across clusters and preserving informative variance within clusters.
- This mechanism reduces estimation error (Frobenius, KL) and stabilizes volatility forecasts (Risk Gap) simultaneously.

Discussion / Interpretation



Why does the Integrated Model perform better?

Dynamic Robustness Under Market Regime Shifts

- Cluster structures evolve slowly compared to individual asset correlations — thus providing **natural regularization** across rolling windows.
- Under stress regimes, Integrated maintains bounded covariance trace, preventing blow-ups that appear in POETonly and OLS.
- The model reacts to systemic shocks (entropy remains high) but avoids unstable noise amplification ensuring regime-consistent sensitivity.

Information-Theoretic Interpretation

- High differential entropy in Integrated and LASSO models implies richer latent dependency capture, whereas low-entropy OLS/POET estimates indicate information loss via oversmoothing.
- Integrated's moderate entropy dispersion shows it retains structural complexity while maintaining predictive stability.

The Integrated model succeeds because it embeds structural prior knowledge (cluster topology) into statistical regularization.

It exploits the **natural modularity of financial markets** — filtering noise *across* clusters while preserving dependence *within* clusters.

This structural sparsification translates into **lower estimation error**, **higher Sharpe efficiency**, and **superior stability across regimes**.

Conclusion



Model Design Adjustment

- In the original proposal, we intended to extend the framework with a Spatial Autoregressive (SAR) layer to explicitly model inter-asset dependencies within local subgroups.
- However, during implementation, we found that the subgroupbased autoregressive structure in SAR plays a similar role to the latent factor extraction in POET — both capture crosssectional dependency compression.
- To avoid redundant modeling of local dependency, we adopted only the subgrouping mechanism from SAR, applying it prior to POET decomposition to form the group masks used in idiosyncratic thresholding.
- This modification ensures that grouping precedes factor extraction, aligning the cluster topology consistently across both systematic and idiosyncratic components.

Summary

- We proposed an Integrated covariance estimation framework combining LASSO-based asset selection, cluster-wise residual sparsification, and POET-style factor decomposition.
- The model achieves lower estimation error, stronger regime stability, and higher Sharpe efficiency by preserving meaningful intra-cluster dependencies while suppressing cross-cluster noise.
- Empirical results confirm that cluster-aware structural regularization improves both risk forecast reliability and distributional fidelity compared to standalone methods.