# Scientific Experimentation and Evaluation - Assignment 09 -Handwritten Data Recognition

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#### 1 ABSTRACT

This report describes how we applied a machine learning technique to the task of recognizing handwritten digits. It presents our approach, analyses the results and compares them to the results of others that have applied some ML techniques to this task as well.

#### 2 THE DATA

The MNIST dataset is a collection of 70000 images representing handwritten digits ranging from 0 to 9. The dataset is divided into a training and a test set. The training set consists of 60000 single images and the test set of 10000 images. Each image is stored as a 784 row vector, where each vector represents 28x28 pixels. An example can be seen in figure 2.1.

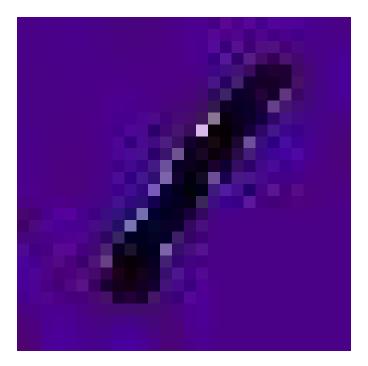


Figure 2.1: Sample Image from MNIST dataset

#### 3 APPROACH

To classify the handwritten data we used a multilayer perceptron and trained it using the backpropagation of error algorithm. We used the implementation of David Stutz (david-stutz.de) and adjusted the parameters to our needs. The MLP uses 784 inputs, 700 hidden neurons in its hidden layer and ten outputs - one for each digit. As the activation function we used a locistic sigmoid:

$$y = \frac{1}{1 + exp(-x)}$$

We set the learning rate to 0.1. The training was done for 500 epochs, where in every epoch we presented 100 randomly chosen samples from the training set and computed the error over the whole batch to adjust the weights.

We trained MLP with this settings 50 times and computed its mean and best performance. The results can be seen in section 4.

#### 4 RESULTS

On average the MLP was able to classify 91.91% correctly with a standard deviation of 0.35. In the best run the performance was about 92.5%. The mean error progression while training can be seen in figure 4.1. The gradient of the error curve in the figure suggests that continuing the training could possibly lead to an even smaller error.

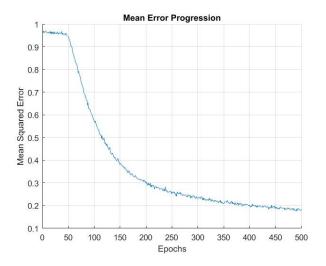


Figure 4.1: Error Progression While Training

In table 4.1 and figure 4.2 the confusion matrix of one of the nets can be seen. Table 4.2 shows the relative values with respect to the overall appearance of each digit and figure 4.3 shows the logarithmic confusion matrix, where more details can be seen.

The best recognition rate is for zeros and ones (more than 96%). Five and seven have the worst results with a rate lower than 87%. Some common misclassifications are 2 as 8 (2.71%), 3 as 5 (2.08%) or 8 (2.38%), 4 as 9 (3.67%), 5 as 3 (4.15%) or 8 (4.6%), 7 as 2 (2.82%) or 9 (6.13%) and 9 as 4 (4.36%).

Table 4.1: Confusion Matrix

| classified\real | 0   | 1    | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   |
|-----------------|-----|------|-----|-----|-----|-----|-----|-----|-----|-----|
| 0               | 945 | 0    | 4   | 1   | 1   | 8   | 10  | 3   | 4   | 6   |
| 1               | 0   | 1102 | 0   | 0   | 3   | 2   | 3   | 18  | 5   | 7   |
| 2               | 2   | 2    | 952 | 21  | 5   | 2   | 4   | 29  | 4   | 0   |
| 3               | 2   | 6    | 9   | 923 | 0   | 37  | 0   | 4   | 12  | 8   |
| 4               | 0   | 1    | 13  | 1   | 916 | 9   | 11  | 14  | 11  | 44  |
| 5               | 13  | 2    | 3   | 21  | 0   | 761 | 11  | 1   | 14  | 15  |
| 6               | 12  | 5    | 12  | 4   | 11  | 18  | 914 | 0   | 11  | 1   |
| 7               | 1   | 1    | 7   | 4   | 1   | 6   | 0   | 894 | 2   | 3   |
| 8               | 5   | 16   | 28  | 24  | 9   | 41  | 5   | 2   | 900 | 15  |
| 9               | 0   | 0    | 4   | 11  | 36  | 8   | 0   | 63  | 11  | 910 |

Table 4.2: Relative Confusion Matrix

| classified\real | 0     | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8    | 9     |
|-----------------|-------|-------|-------|-------|-------|-------|-------|-------|------|-------|
| 0               | 96.43 | 0     | 0.39  | 0.09  | 0.1   | 0.9   | 1.04  | 0.29  | 0.41 | 0.59  |
| 1               | 0     | 97.09 | 0     | 0     | 0.31  | 0.22  | 0.31  | 1.75  | 0.51 | 0.69  |
| 2               | 0.2   | 0.18  | 92.25 | 2.08  | 0.51  | 0.22  | 0.42  | 2.82  | 0.41 | 0     |
| 3               | 0.2   | 0.53  | 0.87  | 91.39 | 0     | 4.15  | 0     | 0.39  | 1.23 | 0.79  |
| 4               | 0     | 0.09  | 1.26  | 0.09  | 93.28 | 1.01  | 1.15  | 1.36  | 1.13 | 4.36  |
| 5               | 1.33  | 0.18  | 0.29  | 2.08  | 0     | 85.31 | 1.15  | 0.09  | 1.44 | 1.49  |
| 6               | 1.22  | 0.44  | 1.16  | 0.4   | 1.12  | 2.02  | 95.41 | 0     | 1.13 | 0.09  |
| 7               | 0.1   | 0.08  | 0.68  | 0.4   | 0.1   | 0.67  | 0     | 86.96 | 0.21 | 0.3   |
| 8               | 0.51  | 1.41  | 2.71  | 2.38  | 0.92  | 4.6   | 0.52  | 0.19  | 92.4 | 1.49  |
| 9               | 0     | 0     | 0.39  | 1.09  | 3.67  | 0.9   | 0     | 6.13  | 1.13 | 90.19 |

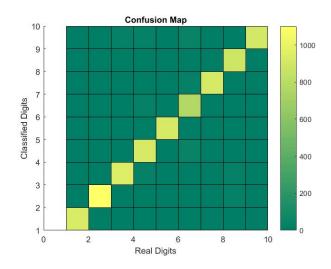


Figure 4.2: Graphical Confusion Matrix of Classifications

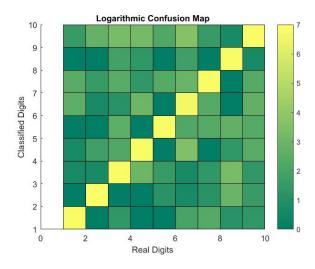


Figure 4.3: Graphical Logartihmic Confusion Matrix of Classifications

### 5 COMPARISON

We compared the accuracies of the MLP approach with two other approaches. One approach was to use PCA to reduce the dimensionality of the problem and then use an SVM to classify the images. The other approach also used an SVM for classification, but it used a method named *Sparse Coding* for preprocessing.

The results can be seen in table 5.1. Using PCA in combination with SVM performed best and significantly outperformed the other methods. The MLP achieved a slightly better performance than the sparse coding approach.

Table 5.1: Accuracies of Different Approaches

| Method           | MLP    | Sparse Coding + SVM | PCA + SVM |
|------------------|--------|---------------------|-----------|
| Average Accuracy | 91.91% | 89.92%              | 98%       |

## 6 CONCLUSION

Using PCA in combination with SVM seems to be the best method to use here. On the other hand some more information are missing to be sure about it. No runtime or memory usage analysis could be done due to lack of information.

For the PCA/SVM approach no information about the number of performed experiments were available, so it may be possible that this result is an outlier. For the Sparse Coding approach the average accuracy is based on three runs only, which is also not enough to make a statistically sound statement.