

1 SchemeHIBME

This scheme is applicable to symmetric and asymmetric groups of prime orders.

1.1 Setup(l) \rightarrow (mpk, msk)

$g \leftarrow 1_{\mathbb{G}_1}$
 generate $\alpha, b_1, b_2 \in \mathbb{Z}_r$ randomly
 generate $s_1, s_2, \dots, s_l, a_1, a_2, \dots, a_l \in \mathbb{Z}_r$ randomly
 generate $g_2, g_3 \in \mathbb{G}_2$ randomly
 generate $h_1, h_2, \dots, h_l \in \mathbb{G}_2$ randomly (Note that the indexes in implementations are 1 smaller than those in theory)
 $H_1 : \mathbb{Z}_r \rightarrow \mathbb{G}_1$
 $H_2 : \mathbb{Z}_r \rightarrow \mathbb{G}_2$
 $\hat{H} : \mathbb{G}_T \rightarrow \{0, 1\}^\lambda$
 $g_1 \leftarrow g^\alpha$
 $A \leftarrow e(g_1, g_2)$
 $\bar{g} \leftarrow g^{b_1}$
 $\tilde{g} \leftarrow g^{b_2}$
 $\bar{g}_3 \leftarrow g_3^{\frac{1}{b_1}}$
 $\tilde{g}_3 \leftarrow g_3^{\frac{1}{b_2}}$
 $mpk \leftarrow (g, g_1, g_2, g_3, \bar{g}, \tilde{g}, \bar{g}_3, \tilde{g}_3, h_1, h_2, \dots, h_l, H_1, H_2, \hat{H}, A)$
 $msk \leftarrow (g_2^\alpha, b_1, b_2, s_1, s_2, \dots, s_l, a_1, a_2, \dots, a_l)$
return (mpk, msk)

1.2 EKGen(ID_k) \rightarrow ek_{ID_k}

$A_k \leftarrow \prod_{j=1}^k a_j$
 $ek_{1,i} \leftarrow H_1(I_i)^{s_i A_k}, \forall i \in \{1, 2, \dots, k\}$
 $ek_{2,i} \leftarrow s_{k+i} A_k, \forall i \in \{1, 2, \dots, l-k\}$
 $ek_3 \leftarrow (a_{k+1}, a_{k+2}, \dots, a_l)$
 $ek_{ID_k} \leftarrow (ek_1, ek_2, ek_3)$
return ek_{ID_k}

1.3 DerivedEKGen($ek_{ID_{k-1}}, ID_k$) \rightarrow ek_{ID_k}

$ek'_{1,i} \leftarrow ek_{1,i}^{a_k}, \forall i \in \{1, 2, \dots, k-1\}$
 $ek'_{1,k} \leftarrow H_1(I_k)^{ek_{2,1} a_k}$
 $ek'_1 \leftarrow ek'_1 || \langle ek'_{1,k} \rangle$
 $ek'_{2,i} \leftarrow ek_{2,i} \cdot a_k, \forall i \in \{2, 3, \dots, l-k+1\}$
 $ek'_3 \leftarrow (a_{k+1}, a_{k+2}, \dots, a_l)$
 $ek_{ID_k} \leftarrow (ek'_1, ek'_2, ek'_3)$
return ek_{ID_k}

1.4 DKGen(ID_k) $\rightarrow dk_{ID_k}$

generate $r \in \mathbb{Z}_r$ randomly

$$HI \leftarrow h_1^{I_1} h_2^{I_2} \cdots h_k^{I_k}$$

$$a_0 \leftarrow g_2^{\frac{\alpha}{b_1}} \cdot HI^{\frac{r}{b_1}} \cdot \tilde{g}_3^r$$

$$a_1 \leftarrow g_2^{\frac{\alpha}{b_2}} \cdot HI^{\frac{r}{b_2}} \cdot \tilde{g}_3^r$$

$$A_k \leftarrow \prod_{j=1}^k a_j$$

$$dk_1 \leftarrow (a_0, a_1, g^r, h_{k+1}^{\frac{r}{b_1}}, h_{k+2}^{\frac{r}{b_1}}, \dots, h_l^{\frac{r}{b_1}}, h_{k+1}^{\frac{r}{b_2}}, h_{k+2}^{\frac{r}{b_2}}, \dots, h_l^{\frac{r}{b_2}}, h_{k+1}^{b_1^{-1}}, h_{k+2}^{b_1^{-1}}, \dots, h_l^{b_1^{-1}}, h_{k+1}^{b_2^{-1}}, h_{k+2}^{b_2^{-1}}, \dots, h_l^{b_2^{-1}}, HI^{\frac{1}{b_1}}, HI^{\frac{1}{b_2}})$$

$$dk_{2,i} \leftarrow H_2(I_i)^{s_i A_k}, \forall i \in \{1, 2, \dots, k\}$$

$$dk_{3,i} \leftarrow s_{k+i} A_k, \forall i \in \{1, 2, \dots, l-k\}$$

$$dk_4 \leftarrow (a_{k+1}, a_{k+2}, \dots, a_l)$$

$$dk_{ID_k} \leftarrow (dk_1, dk_2, dk_3, dk_4)$$

return dk_{ID_k}

1.5 DerivedDKGen($dk_{ID_{k-1}}, ID_k$) $\rightarrow dk_{ID_k}$

generate $t \in \mathbb{Z}_r$ randomly

$$a'_0 \leftarrow a_0 \cdot c_{0,k}^{I_k} \cdot (f_0 \cdot d_{0,k}^{I_k} \cdot \tilde{g}_3)^t$$

$$a'_1 \leftarrow a_1 \cdot c_{1,k}^{I_k} \cdot (f_1 \cdot d_{1,k}^{I_k} \cdot \tilde{g}_3)^t$$

$$dk'_1 \leftarrow (a'_0, a'_1, b \cdot g^t, c_{0,k+1} \cdot d_{0,k+1}^t, c_{0,k+2} \cdot d_{0,k+2}^t, \dots, c_{0,l} \cdot d_{0,l}^t, c_{1,k+1} \cdot d_{1,k+1}^t, c_{1,k+2} \cdot d_{1,k+2}^t, \dots, c_{1,l} \cdot d_{1,l}^t, d_{0,k+1}, d_{0,k+2}, \dots, d_{0,l}, d_{1,k+1}, d_{1,k+2}, \dots, d_{1,l}, f_0 \cdot c_{0,k}^{I_k}, f_1 \cdot c_{1,k}^{I_k})$$

$$dk'_{2,i} \leftarrow dk_{2,i}^{a_k}, \forall i \in \{1, 2, \dots, k-1\}$$

$$dk'_{2,k} \leftarrow H_2(I_k)^{dk_{3,1} a_k}$$

$$dk'_2 \leftarrow dk'_{2,k} \parallel \langle dk'_{2,k} \rangle$$

$$dk'_{3,i} \leftarrow dk_{3,i} \cdot a_k, \forall i \in \{2, 3, \dots, l-k+1\}$$

$$dk'_4 \leftarrow (a_{k+1}, a_{k+2}, \dots, a_l)$$

$$dk_{ID_k} \leftarrow (dk'_1, dk'_2, dk'_3, dk'_4)$$

return dk_{ID_k}

1.6 Enc(ek_{ID_S}, ID_{Rev}, M) $\rightarrow CT$

generate $s_1, s_2, \eta \in \mathbb{Z}_r$ randomly

$$T \leftarrow A^{s_1+s_2}$$

if $m = n$ **then**

$$K \leftarrow \prod_{i=1}^n e(g^\eta \cdot ek_{1,i}, H_2(I'_i))$$

else if $m > n$ **then**

$$A_n \leftarrow \prod_{i=1}^n a_i$$

$$B_n^m \leftarrow \prod_{i=n+1}^m a_i$$

$$K \leftarrow (\prod_{i=1}^n e(ek_{1,i}, H_2(I'_i)) \cdot \prod_{i=n+1}^m e(H_1(I_n), H_2(I'_i))^{s_i A_n})^{B_n^m} \cdot e(g^\eta, \prod_{i=1}^m H_2(I'_i))$$

else if $m < n$ **then**

$$\begin{aligned}
K &\leftarrow \prod_{i=1}^m e(ek_{1,i}, H_2(I'_i)) \prod_{i=m+1}^n e(ek_{1,i}, H_2(I'_m)) e(g^n, \prod_{i=1}^m H_2(I'_i)) \\
C_1 &\leftarrow M \oplus \hat{H}(T) \oplus \hat{H}(K) \\
C_2 &\leftarrow \bar{g}^{s_1} \\
C_3 &\leftarrow \tilde{g}^{s_2} \\
C_4 &\leftarrow (h_1^{I_1} h_2^{I_2} \cdots h_n^{I_n} \cdot g_3)^{s_1+s_2} \\
C_5 &\leftarrow g^\eta \\
CT &\leftarrow (C_1, C_2, C_3, C_4, C_5) \\
\textbf{return } &CT
\end{aligned}$$

1.7 Dec($dk_{ID_R}, ID_{Rev}, ID_{Snd}, CT$) $\rightarrow M$

$$\begin{aligned}
T' &= \frac{e(dk_{1,3}, C_4)}{e(C_2, dk_{1,1})e(C_3, dk_{1,2})} \\
\textbf{if } m = n &\textbf{ then} \\
K' &\leftarrow \prod_{i=1}^n e(H_1(I_i), dk_{2,i}) \cdot e(C_5, \prod_{i=1}^n H_2(I'_i)) \\
\textbf{else if } m > n &\textbf{ then} \\
K' &\leftarrow \prod_{i=1}^n e(H_1(I_i), dk_{2,i}) \cdot \prod_{i=n+1}^m e(H_1(I_n), dk_{2,i}) \cdot e(C_5, \prod_{i=1}^m H_2(I'_i)) \\
\textbf{else if } m < n &\textbf{ then} \\
A_m &\leftarrow \prod_{i=1}^m a_i \\
B_n^m &\leftarrow \prod_{i=m+1}^n a_i \\
K' &\leftarrow (\prod_{i=1}^m e(H_1(I_i), dk_{2,i}) \cdot \prod_{i=m+1}^n e(H_1(I_i), H_2(I'_m))^{s_i A_m})^{B_m^n} \cdot e(C_5, \prod_{i=1}^m H_2(I'_i)) \\
M &\leftarrow C_1 \oplus \hat{H}(T') \oplus \hat{H}(K') \\
\textbf{return } &M
\end{aligned}$$