1 SchemeIBMETR

This scheme is only applicable to symmetric groups of prime orders.

1.1 Setup() \rightarrow (mpk, msk)

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\begin{split} p &\leftarrow \|\mathbb{G}\| \\ g &\leftarrow 1_{\mathbb{G}_1} \\ H_1 : \{0,1\}^* \rightarrow \mathbb{G}_1 \\ H_2 : \{0,1\}^* \rightarrow \mathbb{G}_2 \\ \hat{H} : \{0,1\}^* \rightarrow \{0,1\}^{\lambda} \\ \text{generate } g_0, g_1 \in \mathbb{G}_1 \text{ randomly} \\ \text{generate } w, alpha, t_1, t_2 \in \mathbb{Z}_r \\ \Omega &\leftarrow e(g,g)^w \\ v &\leftarrow g^{t_1} \\ v &\leftarrow g^{t_2} \\ mpk &\leftarrow (p,g,g_0,g_1,v_1,v_2,\Omega,H_1,H_2,\hat{H}) \\ msk &\leftarrow (w,\alpha,t_1,t_2) \\ \mathbf{return } (mpk,msk) \end{split}
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$1.2 \quad \mathrm{EKGen}(id_S) ightarrow ek_{id_S}$

$$ek_{id_S} \leftarrow H_1(id_S)$$

return ek_{id_S}

$1.3 \quad \mathrm{DKGen}(id_R) ightarrow dk_{id_R}$

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generate r \in \mathbb{Z}_r randomly dk_0 \leftarrow H_2(id_R)^{\alpha} dk_1 \leftarrow g^r dk_2 \leftarrow g^{-\frac{w}{t_1}}(g_0g_1^{id_R})^{-\frac{r}{t_1}} dk_3 \leftarrow g^{-\frac{w}{t_2}}(g_0g_1^{id_R})^{-\frac{r}{t_2}} dk_{ID_R} \leftarrow (dk_0, dk_1, dk_2, dk_3) return dk_{id_R}
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1.4 $\mathbf{TKGen}(id_R) \rightarrow tk_{id_R}$

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generate k \in \mathbb{Z}_r randomly tk_1 \leftarrow g^k tk_2 \leftarrow g^{\frac{1}{t_1}} (g_0 g_1^{id_R})^{-\frac{k}{t_1}} tk_3 \leftarrow g^{\frac{1}{t_2}} (g_0 g_1^{id_R})^{-\frac{k}{t_2}} tk_{ID_R} \leftarrow (tk_1, tk_2, tk_3) return tk_{id_R}
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1.5 $\operatorname{Enc}(\boldsymbol{ek_{id_S}}, \boldsymbol{id_{Rev}}, m) \rightarrow \boldsymbol{ct}$

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generate s_1, s_2, beta \in \mathbb{Z}_r randomly s = s_1 + s_2 R = \Omega^{-s} T \leftarrow g^{\beta}
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$$\begin{split} K &\leftarrow e(H_2(id_{Rev}), ek_{id_S} \cdot T) \\ ct_0 &\leftarrow \hat{H}(R) \oplus \hat{H}(K) \oplus m \\ ct_1 &\leftarrow (g_0g_1^{id_{Rev}})^s \\ ct_2 &\leftarrow v_1^{s_1} \\ ct_3 &\leftarrow v_2^{s_2} \\ e(g,g)^s \\ ct &\leftarrow (ct_0, ct_1, ct_2, ct_3, T, V) \\ \mathbf{return} \ ct \end{split}$$

1.6 $\operatorname{Dec}(dk_{id_R}, id_{Rev}, id_{Snd}, ct) \rightarrow m$

$$R' \leftarrow e(dk_1, ct_1) \cdot e(dk_2, ct_2) \cdot e(dk_3, ct_3)$$

$$K' \leftarrow e(dk_0, H_1(id_{Snd})) \cdot e(H_2(id_R), T)$$

$$m \leftarrow ct_0 \oplus \hat{H}(R') \oplus \hat{H}(K')$$
return m

1.7 TVerify $(\textit{tk}_{\textit{id}_R}, \textit{ct}) \rightarrow y, y \in \{0, 1\}$

$$\mathbf{return}\ V = e(\mathit{tk}_1, \mathit{ct}_1) \cdot e(\mathit{tk}_2, \mathit{ct}_2) \cdot e(\mathit{tk}_3, \mathit{ct}_3)$$