## 1 SchemeIBME

This scheme is only applicable to symmetric groups of prime orders.

#### 1.1 Setup() $\rightarrow$ (mpk, msk)

```
generate r, s \in \mathbb{Z}_p^* randomly generate P \in \mathbb{G}_1 randomly P_0 \leftarrow r \cdot P H_1 : \mathbb{Z}_p^* \to \mathbb{G}_1 H' : \mathbb{Z}_p^* \oplus mask \to \mathbb{G}_1 mpk \leftarrow (P, P_0, H, H') msk \leftarrow (r, s) return (mpk, msk)
```

## 1.2 $SKGen(S) \rightarrow ek_S$

 $ek_S \leftarrow s \cdot H'(S)$  $textbfreturnek_S$ 

# 1.3 $\mathbf{SKGen}(S) \to d\mathbf{k}_R$

```
\begin{split} H_R \leftarrow H(R) \\ dk_1 \leftarrow r \cdot H_R \\ dk_2 \leftarrow s \cdot H_R \\ dk_3 \leftarrow H_R \\ dk_R \leftarrow (dk_1, dk_2, dk_3) \\ textbfreturndk_R \end{split}
```

### 1.4 $\operatorname{Enc}(\boldsymbol{ek_S}, R, M) \to C$

```
\begin{array}{l} \text{generate } u,t \in \mathbb{Z}_p^* \text{ randomly} \\ T \leftarrow t \cdot P \\ U \leftarrow u \cdot P \\ H_R \leftarrow H(R) \\ k_R \leftarrow e(H_R, u \cdot P_0) \\ k_S \leftarrow e(H_R, T + ek_S) \\ V \leftarrow M \oplus k_R \oplus k_S \\ C \leftarrow (T, U, V) \\ \textbf{return } C \end{array}
```

## 1.5 $\mathbf{Dec}(d\mathbf{k}_R, S, C) \to M$

```
k_R \leftarrow e(dk_1, U)
H_S' \leftarrow H'(S)
k_S \leftarrow e(dk_3, T)
M \leftarrow V \oplus k_R \oplus k_S
return M
```