1 SchemeIBME

This scheme is only applicable to symmetric groups of prime orders.

1.1 Setup() \rightarrow (mpk, msk)

```
generate r, s \in \mathbb{Z}_r randomly P \leftarrow 1\mathbb{G}_1 P_0 \leftarrow r \cdot P H_1 : \mathbb{Z}_r \to \mathbb{G}_1 generate mask, \|mask\| \leftarrow \|e\|, e \in \mathbb{Z}_r randomly H' : \mathbb{Z}_r \oplus mask \to \mathbb{G}_1 mpk \leftarrow (P, P_0, H, H') msk \leftarrow (r, s) return (mpk, msk)
```

1.2 $SKGen(S) \rightarrow ek_S$

$$ek_S \leftarrow s \cdot H'(S)$$

return ek_S

1.3 $\mathbf{RKGen}(S) \rightarrow \mathbf{dk}_R$

```
\begin{aligned} H_R &\leftarrow H(R) \\ dk_1 &\leftarrow r \cdot H_R \\ dk_2 &\leftarrow s \cdot H_R \\ dk_3 &\leftarrow H_R \\ dk_R &\leftarrow (dk_1, dk_2, dk_3) \end{aligned} return dk_R
```

1.4 $\mathbf{Enc}(\mathbf{ek}_S, R, M) \to C$

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\begin{array}{l} \text{generate } u,t \in \mathbb{Z}_r \text{ randomly} \\ T \leftarrow t \cdot P \\ U \leftarrow u \cdot P \\ H_R \leftarrow H(R) \\ k_R \leftarrow e(H_R, u \cdot P_0) \\ k_S \leftarrow e(H_R, T + ek_S) \\ V \leftarrow M \oplus k_R \oplus k_S \\ C \leftarrow (T, U, V) \\ \textbf{return } C \end{array}
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1.5 $\mathbf{Dec}(d\mathbf{k}_R, S, C) \to M$

```
k_R \leftarrow e(dk_1, U)
H_S' \leftarrow H'(S)
k_S \leftarrow e(dk_3, T)
M \leftarrow V \oplus k_R \oplus k_S
return M
```