1 SchemeARES

1.1 Setup() \rightarrow (mpk, msk)

```
generate g, g_0, g_1 \in \mathbb{G}_1 randomly
generate w, t_1, t_2, t_3, t_4 \in \mathbb{Z}_p^*
\Omega \leftarrow e(g, g)^{t_1 t_2 w}
v \leftarrow g^{t_1}
v \leftarrow g^{t_2}
v \leftarrow g^{t_3}
v \leftarrow g^{t_4}
mpk \leftarrow (Omega, g, g_0, g_1, v_1, v_2, v_3, v_4)
msk \leftarrow (w, t_1, t_2, t_3, t_4)
return (mpk, msk)
```

1.2 $\operatorname{Extract}(Id) \to Pvk_{Id}$

```
generate r1, r2 \in \mathbb{Z}_p^* randomly d_0 \leftarrow g^{r_1t_1t_2+r_2t_3t_4} d_1 \leftarrow g^{-wt_2} \cdot (g_0g_1^{Id})^{-r_1t_2} d_2 \leftarrow g^{-wt_1} \cdot (g_0g_1^{Id})^{-r_1t_1} d_3 \leftarrow (g_0g_1^{Id})^{-r_2t_4} d_4 \leftarrow (g_0g_1^{Id})^{-r_2t_3} Pvk_{Id} \leftarrow (d_0, d_1, d_2, d_3, d_4) return Pvk_{Id}
```

1.3 $\mathbf{TSK}(\mathbf{Id}) \rightarrow \mathbf{Pvk_{Id}}$

```
generate r1, r2 \in \mathbb{Z}_p^* randomly d_0 \leftarrow g^{r_1t_1t_2+r_2t_3t_4} d_1 \leftarrow (g_0g_1^{Id})^{-r_1t_2} d_2 \leftarrow (g_0g_1^{Id})^{-r_1t_1} d_3 \leftarrow (g_0g_1^{Id})^{-r_2t_4} d_4 \leftarrow (g_0g_1^{Id})^{-r_2t_3} Pvk_{Id} \leftarrow (d_0, d_1, d_2, d_3, d_4) return Pvk_{Id}
```

1.4 Encrypt $(Id, m) \rightarrow CT$

```
generate s, s_1, s_2 \in \mathbb{Z}_p^* randomly C' \leftarrow \Omega^s M (g_0 g_1^{Id})^s C_1 \leftarrow v_1^{s-s_1} C_2 \leftarrow v_2^{s_1} C_3 \leftarrow v_3^{s-s_2} C_4 \leftarrow v_4^{s_2} CT \leftarrow (C', C_0, C_1, C_2, C_3, C_4) return CT
```

1.5 $\mathbf{Decrypt}(\mathbf{\textit{Pvk}}_{id}, \mathbf{\textit{CT}}) \rightarrow M$

 $M \leftarrow C' \cdot e(C_0,d_0) \cdot e(C_1,d_1) \cdot e(C_2,d_2) \cdot e(C_3,d_3) \cdot e(C_4,d_4)$ return M

1.6 TVerify(
$$Pvk_{id}$$
, CT) $\rightarrow y, y \in \{0, 1\}$

return $e(C_0, d_0) \cdot e(C_1, d_1) \cdot e(C_2, d_2) \cdot e(C_3, d_3) \cdot e(C_4, d_4) = 1(\mathbb{G}_T)$