### 1 SchemeIBBME

This scheme is applicable to symmetric and asymmetric groups of prime orders.

## 1.1 Setup() $\rightarrow$ (mpk, msk)

```
generate g,v\in\mathbb{G}_1 randomly generate h\in\mathbb{G}_2 randomly generate \vec{r}_1=(r_{1,0},r_{1,1},\cdots,r_1,l)\in\mathbb{Z}_r^{l+1} randomly generate \vec{r}_2=(r_{2,0},r_{2,1},\cdots,r_2,l)\in\mathbb{Z}_r^{l+1} randomly generate t_1,t_2,\beta_1,\beta_2,\alpha,\rho,b,\tau\in\mathbb{Z}_r randomly generate t_1,t_2,\beta_1,\beta_2,\alpha,\rho,b,\tau\in\mathbb{Z}_r randomly \vec{r}=(r_0,r_1,\cdots,r_l)\leftarrow\vec{r}_1+b\vec{r}_2=(r_{1,0}+br_{2,0},r_{1,1}+br_{2,1},\cdots,r_{1,l}+br_{2,l}) t\leftarrow t_1+bt_2 \beta\leftarrow\beta_1+b\beta_2 \vec{R}\leftarrow g^{\vec{r}}=(g^{r_0},g^{r_1},\cdots,g^{r_l}) T\leftarrow g^t H_0:\{0,1\}^*\to\mathbb{G}_2 H_1:\{0,1\}^*\to\mathbb{G}_1 H_2:\{0,1\}^*\to\mathbb{Z}_r H_3:\mathbb{G}_T\to\mathbb{Z}_r mpk\leftarrow(v,v^\rho,g,g^b,\vec{R},T,e(g,h)^\beta,h,h^{\vec{r}_1},h^{\vec{r}_2},h^{t_1},h^{t_2},g^{\tau\beta},h^{\tau\beta_1},h^{\tau\beta_2},h^{1/\tau},H_0,H_1,H_2,H_3) msk\leftarrow(h^{\beta_1},h^{\beta_2},\alpha,\rho) return (mpk,msk)
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# $1.2 \quad ext{EKGen}(id^*) ightarrow ek_{id^*}$

$$ek_{id^*} \leftarrow H_1(id^*)^{\alpha}$$
  
**return**  $ek_{id^*}$ 

### $1.3 \quad \mathrm{DKGen}(id) ightarrow dk_{id}$

```
generate z \in \mathbb{Z}_r randomly

generate rtags = (rtag_1, rtag_2, \cdots, rtag_l) \in \mathbb{Z}_r^l randomly

dk_1 \leftarrow H_0(id)^{\rho}

dk_2 \leftarrow H_0(id)^{\alpha}

dk_3 \leftarrow H_0(id)

dk_4 \leftarrow h^{\beta_1}(h^{t_1})^z

dk_5 \leftarrow h^{\beta_2}(h^{t_2})^z

dk_6 \leftarrow h^z

dk_{7,j} \leftarrow ((h^{t_1})^{rtag_j}h^{r_{1,j}}/(h^{r_{1,0}})^{H_2(id)^j})^z, \forall j \in \{1, 2, \cdots, l\}

dk_{8,j} \leftarrow (dk_1, dk_2, \cdots, dk_8, rtags)

return dk_{id}
```

# 1.4 $\operatorname{Enc}(S, ek_{id^*}, m) \to ct$

Compute 
$$y_0, y_1, y_2, \dots y_n$$
 that satisfy  $\forall x \in \mathbb{Z}_r$ , we have  $F(x) = \prod_{i d_j \in S} (x - H_2(id_j)) = y_0 + \sum_{i=1}^n y_i x^i$ 

$$\vec{y} \leftarrow (y_0, y_1, \cdots, y_n, y_{n+1}, y_{n+2}, \cdots, y_l) = (y_0, y_1, \cdots, y_n, 0, 0, \cdots, 0)$$
generate  $s, d_2, ctag \in \mathbb{Z}_r$  randomly
$$C_0 \leftarrow m \cdot e(g, h)^{\beta s}$$

$$C_1 \leftarrow g^s$$

$$C_2 \leftarrow g^{bs}$$

$$C_3 \leftarrow \left(T^{ctag} \prod_{i=0}^n (g^{r_i})^{y_i}\right)^{d_2 s}$$

$$C_4 \leftarrow v^s$$

$$V_{id_i} \leftarrow H_3(e(H_0(id_i), ek_{id^*} \cdot g^{bs} \cdot v^{\rho s})), \forall id_i \in S$$
Compute  $\vec{b} \leftarrow (b_0, b_1, b_2, \cdots b_n)$  that satisfy  $\forall y \in \mathbb{Z}_r$ , we have  $g(y) = \prod_{V_{id_k} \in V_{id}} (y - V_{id_k}) + d_2 = b_0 + \sum_{k=1}^n b_k y^k$ 

$$ct \leftarrow (C_0, C_1, C_2, C_3, C_4, ctag, \vec{y}, \vec{b})$$
return  $ct$ 

1.5  $\mathbf{Dec}(S, dk_{id_i}, id^*, ct) \rightarrow m$ 

$$\begin{split} V(id_i) \leftarrow H_3(e(dk_{i,3}, C_2)e(dk_{i,2}, H_1(id^*))e(dk_{i,1}, C_4)) \\ d_2 \leftarrow g(V_{id_i}) &= b_0 + \sum\limits_{j=1}^n b_j V_{id_i}^j \\ rtag \leftarrow \sum\limits_{i=1}^l y_i rtags_i \end{split}$$

$$rtag \leftarrow \sum_{i=1}^{n} y_i rtag s_i$$
  
**if**  $rtag = ctag$  **then**

else 
$$A \leftarrow e\left(C_1, \prod_{j=1}^l dk_{7,j}^{y_j}\right) e\left(C_2, \prod_{j=1}^l dk_{8,j}^{y_j}\right) / e(C_3^{1/d_2}, dk_6)$$
 
$$B \leftarrow e(C_1, dk_4) \cdot e(C_2, dk_5)$$
 
$$m \leftarrow C_0 \cdot A^{1/(rtag-ctag)} \cdot B^{-1}$$

end if return m

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