

1 SchemeARES

This scheme is only applicable to symmetric groups of prime orders.

1.1 Setup() \rightarrow (*mpk*, *msk*)

```

 $g \leftarrow 1_{\mathbb{G}_1}$ 
generate  $g_0, g_1 \in \mathbb{G}_1$  randomly
generate  $w, t_1, t_2, t_3, t_4 \in \mathbb{Z}_r$ 
 $\Omega \leftarrow e(g, g)^{t_1 t_2 w}$ 
 $v \leftarrow g^{t_1}$ 
 $v \leftarrow g^{t_2}$ 
 $v \leftarrow g^{t_3}$ 
 $v \leftarrow g^{t_4}$ 
 $mpk \leftarrow (\Omega, g, g_0, g_1, v_1, v_2, v_3, v_4)$ 
 $msk \leftarrow (w, t_1, t_2, t_3, t_4)$ 
return (mpk, msk)

```

1.2 Extract(*Id*) \rightarrow *Pvk_{Id}*

```

generate  $r_1, r_2 \in \mathbb{Z}_r$  randomly
 $d_0 \leftarrow g^{r_1 t_1 t_2 + r_2 t_3 t_4}$ 
 $d_1 \leftarrow g^{-w t_2} \cdot (g_0 g_1^{Id})^{-r_1 t_2}$ 
 $d_2 \leftarrow g^{-w t_1} \cdot (g_0 g_1^{Id})^{-r_1 t_1}$ 
 $d_3 \leftarrow (g_0 g_1^{Id})^{-r_2 t_4}$ 
 $d_4 \leftarrow (g_0 g_1^{Id})^{-r_2 t_3}$ 
 $Pvk_{Id} \leftarrow (d_0, d_1, d_2, d_3, d_4)$ 
return PvkId

```

1.3 TSK(*Id*) \rightarrow *Pvk_{Id}*

```

generate  $r_1, r_2 \in \mathbb{Z}_r$  randomly
 $d_0 \leftarrow g^{r_1 t_1 t_2 + r_2 t_3 t_4}$ 
 $d_1 \leftarrow (g_0 g_1^{Id})^{-r_1 t_2}$ 
 $d_2 \leftarrow (g_0 g_1^{Id})^{-r_1 t_1}$ 
 $d_3 \leftarrow (g_0 g_1^{Id})^{-r_2 t_4}$ 
 $d_4 \leftarrow (g_0 g_1^{Id})^{-r_2 t_3}$ 
 $Pvk_{Id} \leftarrow (d_0, d_1, d_2, d_3, d_4)$ 
return PvkId

```

1.4 Encrypt(*Id*, *m*) \rightarrow *CT*

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generate  $s, s_1, s_2 \in \mathbb{Z}_r$  randomly
 $C' \leftarrow \Omega^s M$ 
 $(g_0 g_1^{Id})^s$ 
 $C_1 \leftarrow v_1^{s-s_1}$ 
 $C_2 \leftarrow v_2^{s_1}$ 
 $C_3 \leftarrow v_3^{s-s_2}$ 
 $C_4 \leftarrow v_4^{s_2}$ 
 $CT \leftarrow (C', C_0, C_1, C_2, C_3, C_4)$ 

```

return CT

1.5 Decrypt(Pvk_{id}, CT) $\rightarrow M$

$M \leftarrow C' \cdot e(C_0, d_0) \cdot e(C_1, d_1) \cdot e(C_2, d_2) \cdot e(C_3, d_3) \cdot e(C_4, d_4)$
return M

1.6 TVerify(Pvk_{id}, CT) $\rightarrow y, y \in \{0, 1\}$

return $e(C_0, d_0) \cdot e(C_1, d_1) \cdot e(C_2, d_2) \cdot e(C_3, d_3) \cdot e(C_4, d_4) = 1(\mathbb{G}_T)$