1 SchemeAIBE

This scheme is only applicable to symmetric groups of prime orders.

1.1 Setup() \rightarrow (mpk, msk)

```
\begin{split} g &\leftarrow 1_{\mathbb{G}_1} \\ \text{generate } g_0, g_1 \in \mathbb{G}_1 \text{ randomly} \\ \text{generate } w, t_1, t_2, t_3, t_4 \in \mathbb{Z}_r \\ \Omega &\leftarrow e(g, g)^{t_1 t_2 w} \\ v &\leftarrow g^{t_1} \\ v &\leftarrow g^{t_2} \\ v &\leftarrow g^{t_3} \\ v &\leftarrow g^{t_4} \\ mpk &\leftarrow (Omega, g, g_0, g_1, v_1, v_2, v_3, v_4) \\ msk &\leftarrow (w, t_1, t_2, t_3, t_4) \\ \mathbf{return } &(mpk, msk) \end{split}
```

$1.2 \quad ext{Extract}(\textit{Id}) ightarrow \textit{Pvk}_{\textit{Id}}$

```
generate r1, r2 \in \mathbb{Z}_r randomly d_0 \leftarrow g^{r_1t_1t_2+r_2t_3t_4} d_1 \leftarrow g^{-wt_2} \cdot (g_0g_1^{Id})^{-r_1t_2} d_2 \leftarrow g^{-wt_1} \cdot (g_0g_1^{Id})^{-r_1t_1} d_3 \leftarrow (g_0g_1^{Id})^{-r_2t_4} d_4 \leftarrow (g_0g_1^{Id})^{-r_2t_3} Pvk_{Id} \leftarrow (d_0, d_1, d_2, d_3, d_4) return Pvk_{Id}
```

1.3 Encrypt $(Id, m) \rightarrow CT$

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generate s, s_1, s_2 \in \mathbb{Z}_r randomly C' \leftarrow \Omega^s M (g_0 g_1^{Id})^s C_1 \leftarrow v_1^{s-s_1} C_2 \leftarrow v_2^{s_1} C_3 \leftarrow v_3^{s-s_2} C_4 \leftarrow v_4^{s_2} CT \leftarrow (C', C_0, C_1, C_2, C_3, C_4) return CT
```

1.4 Decrypt $(Pvk_{id}, CT) \rightarrow M$

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M \leftarrow C' \cdot e(C_0,d_0) \cdot e(C_1,d_1) \cdot e(C_2,d_2) \cdot e(C_3,d_3) \cdot e(C_4,d_4) return M
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