1 SchemeCANIFPPCT

1.1 Setup(l) \rightarrow (mpk, msk)

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\begin{split} p &\leftarrow \|\mathbb{G}\| \\ \text{generate } g_1, g_3 \in \mathbb{G}_1 \text{ randomly} \\ \text{generate } r, s, t, \omega, t_1, t_2, t_3, t_4 \in \mathbb{Z}_r \text{ randomly} \\ R &\leftarrow g_1^r \\ S &\leftarrow g_2^s \\ T &\leftarrow g_1^t \\ \Omega &\leftarrow e(g_1, g_2)^{t_1 t_2 \omega} \\ v_1 &\leftarrow g_2^{t_2} \\ v_2 &\leftarrow g_2^{t_2} \\ v_3 &\leftarrow g_2^{t_3} \\ v_4 &\leftarrow g_2^{t_4} \\ mpk &\leftarrow (g_1, g_2, p, g_3, H_1, H_2, H_3, H_4, R, S, T, \Omega, v_1, v_2, v_3, v_4) \\ msk &\leftarrow (r, s, t, \omega, t_1, t_2, t_3, t_4) \\ \mathbf{return} \ (mpk, msk) \end{split}
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$1.2 \quad \mathbf{KGen}(extbf{\emph{ID}}_k) ightarrow extbf{\emph{sk}}_{ extbf{\emph{ID}}_k}$

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\begin{aligned} &\text{generate } k_i, x_i \in \mathbb{Z}_r \text{ randomly} \\ &z_i \leftarrow (r - x_i)(sx_i)^{-1} \in \mathbb{Z}_r \\ &Z_i \leftarrow g_1^{z_i} \in \mathbb{G}_1 \\ &sk_{ID_i} \leftarrow k_i \\ &ek_{ID_i} \leftarrow (x_i, Z_i) \\ &HI \leftarrow h_1^{I_1} h_2^{I_2} \cdots h_k^{I_k} \\ &sk_{ID_k} \leftarrow (g_2^{\frac{\alpha}{b_1}} \cdot HI^{\frac{r}{b_1}} \cdot \bar{g}_3^r, g_2^{\frac{\alpha}{b_2}} \cdot HI^{\frac{r}{b_2}} \cdot \tilde{g}_3^r, g^r, h_{k+1}^{\frac{r}{b_1}}, h_{k+2}^{\frac{r}{b_1}}, \cdots, h_l^{\frac{r}{b_1}}, h_{k+2}^{\frac{r}{b_1}}, \cdots, h_l^{\frac{r}{b_1}}, h_{k+1}^{b_1-1}, h_{k+2}^{b_1-1}, \cdots, h_l^{\frac{r}{b_1}}, h_{k+1}^{b_1-1}, h_{k+1}^{b_1-
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$1.3 \quad \mathrm{DerivedKGen}(\mathit{sk}_{\mathit{ID}_{k-1}}, \mathit{ID}_k) ightarrow \mathit{sk}_{\mathit{ID}_k}$

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generate t \in \mathbb{Z}_r randomly sk_{ID_k} \leftarrow (a_0 \cdot c_{0,k}^{I_k} \cdot (f_0 \cdot d_{0,k}^{I_k} \cdot \bar{g}_3)^t, a_1 \cdot c_{1,k}^{I_k} \cdot (f_1 \cdot d_{1,k}^{I_k} \cdot \tilde{g}_3)^t, b \cdot g^t, c_{0,k+1} \cdot d_{0,k+1}^t, c_{0,k+2} \cdot d_{0,k+1}^t, c_{0,k+2} \cdot d_{0,k+2}^t, \cdots, c_{0,l} \cdot d_{0,l}^t, c_{1,k+1} \cdot d_{1,k+1}^t, c_{1,k+2} \cdot d_{1,k+2}^t, \cdots, c_{1,l} \cdot d_{1,l}^t, d_{0,k+1}, d_{0,k+2}, \cdots, d_{0,l}, d_{1,k+1}, d_{1,k+2}, \cdots, d_{1,l}, f_0 \cdot c_{0,k}^{I_k}, f_1 \cdot c_{1,k}^{I_k})
return sk_{ID_k}
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1.4 $\operatorname{Enc}(ID_k, M) \to CT$

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generate s_1, s_2 \in \mathbb{Z}_r randomly CT \leftarrow (e(g_1, g_2)^{s_1 + s_2} \cdot M, \bar{g}^{s_1}, \tilde{g}^{s_2}, (h_1^{I_1} h_2^{I_2} \cdots h_k^{I_k} \cdot g_3)^{s_1 + s_2}) return CT
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1.5 $\operatorname{Dec}(sk_{ID_k}, CT) \to M$

$$\begin{aligned} M \leftarrow \frac{e(b,D) \cdot A}{e(B,a_0) \cdot e(C,a_1)} \\ \mathbf{return} \ M \end{aligned}$$