#### 1 SchemeAAIBME

#### 1.1 Setup $(n,d) \rightarrow (mpk, msk)$

```
g \leftarrow 1_{\mathbb{G}_1}
generate \alpha, \beta, t_1, t_2, t_3, t_4 \in \mathbb{Z}_r randomly
generate g_2, g_3 \in \mathbb{G}_1 randomly
generate T \leftarrow (T_0, T_1, \cdots, T_n) \in \mathbb{G}_1^{n+1} randomly
generate T' \leftarrow (T_0, T_1, \cdots, T_n) \in \mathbb{G}_1 randomly generate T' \leftarrow (T_0', T_1', \cdots, T_n') \in \mathbb{G}_1^{n+1} randomly generate u \leftarrow (u_0, u_1, \cdots, u_n) \in \mathbb{G}_{\mathcal{V}}^{n+1} randomly generate u' \leftarrow (u_0', u_1', \cdots, u_n') \in \mathbb{G}_1^{n+1} randomly
H_1: \{0,1\}^* \to \mathbb{G}_1
g_1 \leftarrow g^{\alpha}
g_1' \leftarrow g^\beta
Y_1 \leftarrow e(g_1, g_2)^{t_1 t_2}
Y_2 \leftarrow e(g_3, g)^{\beta}
v_1 \leftarrow g^{t_1}
v_2 \leftarrow g^{t_2}
v_3 \leftarrow g^{t_3}
v_4 \leftarrow g^{t_4}
 mpk \leftarrow (g_1, g'_1, g_2, g_3, Y_1, Y_2, v_1, v_2, v_3, v_4, \boldsymbol{u}, \boldsymbol{T}, \boldsymbol{u}', \boldsymbol{T}', H_1)
 msk \leftarrow (g_2^{\alpha}, \beta, t_1, t_2, t_3, t_4)
return (mpk, msk)
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## $1.2 \quad \mathrm{EKGen}(\mathit{ID}_A) o ek_{\mathit{ID}_A}$

```
g \leftarrow 1_{\mathbb{G}_1}

H : \boldsymbol{u} \leftarrow (\boldsymbol{u}_0, \boldsymbol{u}_1, \cdots, \boldsymbol{u}_n), ID \leftarrow (ID_1, ID_2, \cdots, ID_n) \rightarrow \boldsymbol{u}_0 \prod_{j \in [1, n]} \boldsymbol{u}_j^{ID_j}

generate \vec{r} = (r_1, r_2, \cdots, r_n) \in \mathbb{Z}_r^n randomly

generate a (d-1) degree polynominal q(x) s.t. q(0) = \beta randomly

ek_{ID_{A_i}} \leftarrow (g_3^{q(i)}[H(\boldsymbol{u}', ID_A)T_i']^{r_i}, g^{r_i}), \forall i \in \{1, 2, \cdots, n\}

generate ek_{ID_A}(S) \subset ek_{ID_A} s.t. \|ek_{ID_A}(S)\| = d randomly

ek_{ID_A}(S)
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### $1.3 \quad \mathrm{DKGen}(id_B) ightarrow dk_{ID_B}$

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g \leftarrow 1_{\mathbb{G}_{1}} \\ H : \boldsymbol{u} \leftarrow (\boldsymbol{u}_{0}, \boldsymbol{u}_{1}, \cdots, \boldsymbol{u}_{n}), ID \leftarrow (ID_{1}, ID_{2}, \cdots, ID_{n}) \rightarrow \boldsymbol{u}_{0} \prod_{j \in [1, n]} \boldsymbol{u}_{j}^{ID_{j}} \\ \text{generate } \vec{k}_{1} = (k_{1,1}, k_{1,2}, \cdots, k_{1,n}) \in \mathbb{Z}_{r}^{n} \text{ randomly} \\ \text{generate } \vec{k}_{2} = (k_{2,1}, k_{2,2}, \cdots, k_{2,n}) \in \mathbb{Z}_{r}^{n} \text{ randomly} \\ dk_{ID_{B_{i}}} \leftarrow (g^{k_{1,i}t_{1}t_{2} + k_{2,i}t_{3}t_{4}}g_{2}^{-\alpha t_{2}}[H(\boldsymbol{u}, ID_{B})T_{i}]^{k_{1,i}t_{2}}g_{2}^{-\alpha t_{1}}[H(\boldsymbol{u}, ID_{B})T_{i}]^{k_{1,i}t_{1}}[H(\boldsymbol{u}, ID_{B})T_{i}]^{k_{2,i}t_{4}}[H(\boldsymbol{u}, ID_{B})T_{i}]^{k} \\ \{1, 2, \cdots, n\} \\ \text{generate } dk_{ID_{B}}(S') \subset dk_{ID_{B}} \text{ s.t. } \|dk_{ID_{B}}(S')\| = d \text{ randomly} \\ \mathbf{return } dk_{ID_{B}}(S')
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#### 1.4 $\operatorname{Enc}(ek_{ID_A}, M) \to CT$

```
g \leftarrow 1_{\mathbb{G}_1}
\Delta : i, S, x \rightarrow \prod_{j \in S, j \neq i} \frac{x - j}{i - j}
N \leftarrow (1, 2, \dots, n + 1)
T: x \to g_2^{x^n} \prod_{i=1}^{n+1} t_i^{\Delta(i,N,x)}
H: x \to g_3^{x^n} \prod_{i=1}^{n+1} l_i^{\Delta(i,N,x)}
generate s, s_1, s_2, \tau \in \mathbb{Z}_r randomly
 K_s \leftarrow Y_1^s
K_{l} \leftarrow Y_{2}^{s} \cdot \hat{e}(g_{3}, g^{-\tau})
C_{0} \leftarrow M \cdot K_{s} \cdot K_{l}
C_{1} \leftarrow \eta_{1}^{s-s_{1}}
C_1 \leftarrow \eta_1^1
C_2 \leftarrow \eta_2^{s_1}
C_3 \leftarrow \eta_3^{s-s_2}
C_4 \leftarrow \eta_4^{s_2}
 C_{1,i} \leftarrow T(b_i)^s, \forall b_i \in P_B
 C_{2,i} \leftarrow H(a_i)^s, \forall a_i \in ID_A
 generate a (d-1) degree polynominal l(x) s.t. l(0) = \tau randomly
 generate \vec{\xi} = (\xi_1, \xi_2, \cdots, \xi_n) \in \mathbb{Z}_r^n randomly
 generate \vec{\chi} = (\chi_1, \chi_2, \cdots, \chi_n) \in \mathbb{Z}_r^n randomly
 C_{3,i} \leftarrow e_i \cdot g^{\xi_i}, \forall i \in \{1, 2, \cdots, n\}
 C_{4,i} \leftarrow g^{\chi_i}, \forall i \in \{1, 2, \cdots, n\}
C_{5,i} \leftarrow E_i^s \cdot g_3^{l(a_i)} H(a_i)^{s \cdot \xi_i} \cdot H_1(C_0 || C_1 || C_2 || C_3 || C_4 || C_{1,i} || C_{2,i} || C_{3,i} || C_{4,i})^{\chi_i}
 CT \leftarrow (C_0, C_1, C_2, C_3, C_4, \vec{C}_1, \vec{C}_2, \vec{C}_3, \vec{C}_4, \vec{C}_5)
\mathbf{return}\ \mathit{CT}
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# 1.5 $\operatorname{Dec}(d\mathbf{k}_{S_B,P_A},S_B,P_A,\mathbf{CT})\to M$

return M

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\begin{split} W_A' &\leftarrow ID_A \cap P_A \\ W_B' &\leftarrow S_B \cap P_B \\ \text{if } |W_A'| &\leq d \land |W_B'| \leq d \text{ then} \\ \text{generate } W_A \subset W_A' \text{ s.t. } |W_A| = d \text{ randomly} \\ \text{generate } W_B \subset W_B' \text{ s.t. } |W_B| = d \text{ randomly} \\ g \leftarrow 1_{\mathbb{G}_1} \\ \Delta &: i, S, x \to \prod_{j \in S, j \neq i} \frac{x-j}{i-j} \\ K_s' &\leftarrow \prod_{b_i \in W_B} (\hat{e}(C_{1,i}, dk_{S_{B_{0,i}}}) \hat{e}(C_1, dk_{S_{B_{1,i}}}) \hat{e}(C_2, dk_{S_{B_{2,i}}}) \hat{e}(C_3, dk_{S_{B_{3,i}}}) \hat{e}(C_4, dk_{S_{B_{4,i}}}))^{\Delta(b_i, W_B, 0)} \\ CT_i &\leftarrow C_0 ||C_1||C_2||C_3||C_4||C_{1,i}||C_{2,i}||C_{3,i}||C_{4,i}, \forall i \in \{1, 2, \cdots, n\} \\ K_l' &\leftarrow \prod_{a_i \in W_A} \left(\frac{\hat{e}(C_{1,i}, dk_{P_{A_{0,i}}}) \hat{e}(C_1, dk_{P_{A_{1,i}}}) \hat{e}(C_2, dk_{P_{A_{i,2}}})}{\hat{e}(H_1(CT_i), C_{4,i}) \cdot \hat{e}(C_{3,i}, C_{2,i})} \cdot \hat{e}(C_3, dk_{P_{A_{i,3}}}) \hat{e}(C_4, dk_{P_{A_{i,4}}}) \hat{e}(C_{5,i}, g)\right)^{\Delta(a_i, W_A, 0)} \\ M &\leftarrow C_0 \cdot K_s' \cdot K_l' \\ \text{else} \\ M &\leftarrow \bot \\ \text{end if} \end{split}
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