Probability Rules Applications

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Exercises

- 1. Let A, B and C be events such that P(A) = 0.5, P(B) = 0.3, and P(C) = 0.4. Also, we know that $P(A \cap B) = 0.2$, $P(B \cap C) = 0.12$, $P(A \cap C) = 0.1$, and $P(A \cap B \cap C) = 0.05$. Find the following:
 - a) $P(A \cup B)$
 - b) $P(A \cup B \cup C)$
 - c) $P(B' \cap C')$
 - d) $P(A \cup (B \cap C))$
 - e) $P((A \cup B \cup C) \cap (A \cap B \cap C)')$
 - f) Advanced: Find P(A|B), the probability of A given we know B has occurred.
- 2. Consider the example of the family in the reading. What is the probability that the family has at least one boy?
- 3. The Birthday Problem Revisted.
 - a) Suppose there are n=20 people in a classroom. My birthday is April 3rd. What is the probability that at least one other person shares my birthday? Assume only 365 days in a year and assume that all birthdays are equally likely.
 - b) In R, find the probability that at least one other person shares my birthday for each value of n from 1 to 80. Plot these probabilities with n on the x-axis and probability on the y-axis. At what value of n would the probability be at least 50%?
 - 4. Thinking of the cards again. Answer the following questions:
 - a) Define two events that are mutually exclusive.
 - b) Define two events that are independent.
 - c) Define an event and its complement.
 - 5. Consider the license plate example from the reading.
 - a) What is the probability that a license plate contains exactly one "B"?

- b) What is the probability that a license plate contains at least one "B"?
- 6. Consider party example in the reading.
- a) Suppose 8 people showed up to the party dressed as zombies. What is the probability that all three awards are won by people dressed as zombies?
- b) What is the probability that zombies win "most creative" and "funniest" but not "scariest"?
- 7. Consider the cards example from the reading.
- a) How many ways can we obtain a "two pairs" (2 of one number, 2 of another, and the final different)?
- b) Consider all of the distinct outcomes of the dice rolls. Is each outcome equally likely? Explain why or why not.
- c) What is the probability of drawing a "four of a kind" (four cards of the same value)?
- 8. Advanced Question: Consider rolling 5 dice. What is the **probability** of a pour resulting in a full house?