Case Study with Data Applications

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```
library(mosaic)
library(tidyverse)

days <- seq(1,365)</pre>
```

Exercises

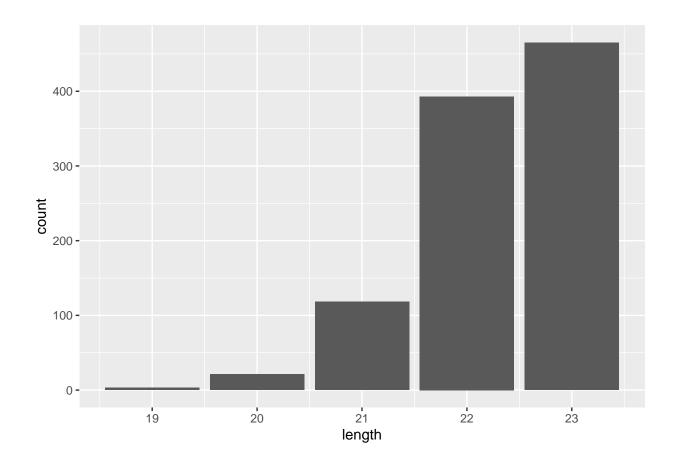
1 0.3743

- 1. Exactly 2 people with the same birthday Simulation. Complete a similar analysis for case where exactly 2 people in a room of 23 people have the same birthday. In this exercise you will use a computational simulation.
- a. Create a new R Markdown file and create a report. Yes, we know you could use this file but we want you to practice generating your own report.
- b. Simulate having 23 people in the class with each day of the year equally likely. Find the cases where exactly 2 people have the same birthday, you will have to alter the code from the Notes more than changing 18 to 23.
- c. Plot the frequency of occurrences as a bar chart.
- d. Estimate the probability of exactly two people having the same birthday.

```
(do(10000)*length(unique(sample(days,size=23,replace = TRUE)))) %>%
  mutate(match=if_else(length==22,1,0)) %>%
  summarise(prob=mean(match))

## prob
```

```
(do(1000)*length(unique(sample(days,size=23,replace = TRUE)))) %>%
    gf_bar(~length)
```



- 2. Exactly 2 people with the same birthday Mathematical. Repeat problem 1 but do it mathematically. As a big hint, you will need to use the choose() function. The idea is that with 23 people we need to choose 2 of them to match. We thus need to multiply, the multiplication rule again, by choose(23,2). If you are having trouble, work with a total of 3 people in the room first.
- a. Find a formula to determine the exact probability of exactly 2 people in a room of 23 having the same birthday.
- b. Generalize your solution to any number n people in the room and create a function.
- c. Vectorize the function.
- d. Plot the probability of exactly 2 people have the same birthday versus number of people in the room.
- e. Comment on the shape of the curve and explain it.
- f. knit and compile your report.

For two people we have

choose(23,2)*prod(365:344)/365²³

[1] 0.3634222

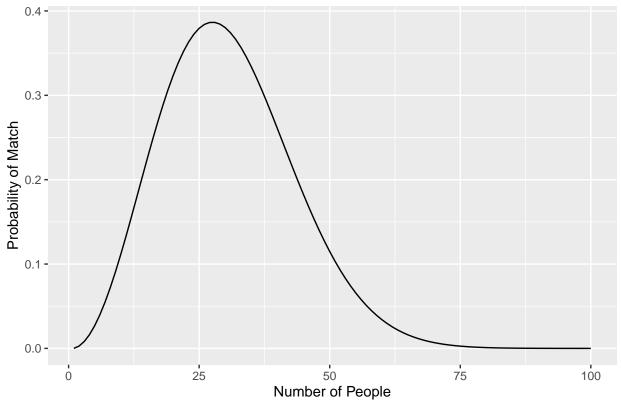
```
exactly_two <- function(n){
  choose(n,2)*prod(365:(365-(n-2)))/365^n
}</pre>
```

```
exactly_two(23)
```

[1] 0.3634222

```
exactly_two <- Vectorize(exactly_two)</pre>
```

Probability of exactly least 2 people with matching birthdays



By the way, exactly three matches in simulation is hard. We have to table the data

```
set.seed(10)
temp <- table(sample(days,size=23,replace = TRUE))
temp</pre>
```

```
##
            1 1 1 1 1 1 1 1 1 1 1
## 365
##
(sum(temp==2) == 2)+0
## [1] 1
(do(10000)*((sum(table(sample(days,size=23,replace = TRUE)) == 3)==1)+0)) %>%
  summarise(prob=mean(result))
##
      prob
## 1 0.0117
Two sets that have same but different birthday
(do(10000)*((sum(table(sample(days,size=23,replace = TRUE)) == 2)==2)+0)) %>%
  summarise(prob=mean(result))
##
      prob
## 1 0.1139
(do(10000)*length(unique(sample(days,size=23,replace = TRUE)))) %>%
 mutate(match=if_else(length==21,1,0)) %>%
  summarise(prob=mean(match))
      prob
## 1 0.1187
Mathematically exactly 3 is easy. Simulation seems to be off a little or the math formula is off.
choose(23,3)*prod(365:345)/365^23
## [1] 0.007395218
```

File Creation Information

File creation date: 2020-08-27
R version 3.6.3 (2020-02-29)
mosaic package version: 1.7.0
tidyverse package version: 1.3.0