

Regression Diagnostics Applications Solutions

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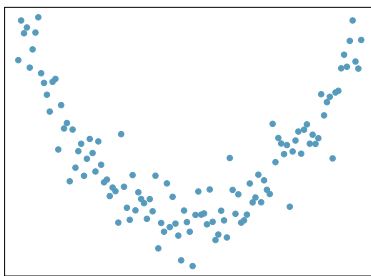
Professor Bradley Warner

11 August, 2020

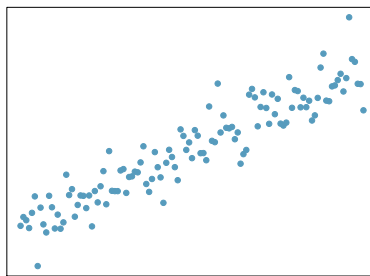
Exercises

1. Identify relationships

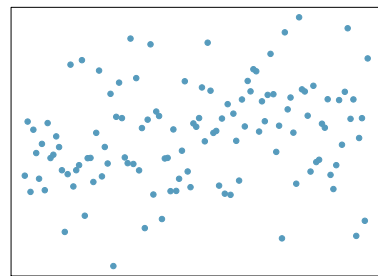
For each of the six plots, identify the strength of the relationship (e.g. weak, moderate, or strong) in the data and whether fitting a linear model would be reasonable.



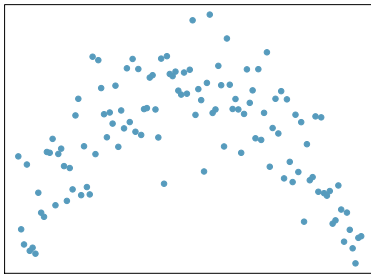
(a)



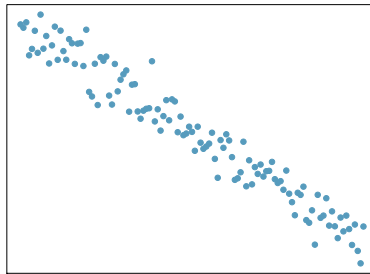
(b)



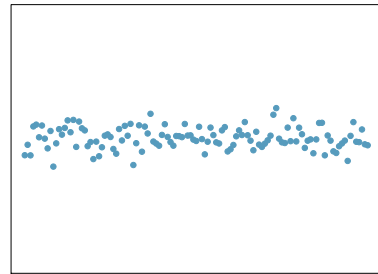
(c)



(d)



(e)



(f)

- (a) Strong relationship, but a straight line would not fit the data.
- (b) Strong relationship, and a linear fit would be reasonable.
- (c) Weak relationship, and trying a linear fit would be reasonable.
- (d) Moderate relationship, but a straight line would not fit the data.
- (e) Strong relationship, and a linear fit would be reasonable.
- (f) Weak relationship, and trying a linear fit would be reasonable.

2. Beer and blood alcohol content

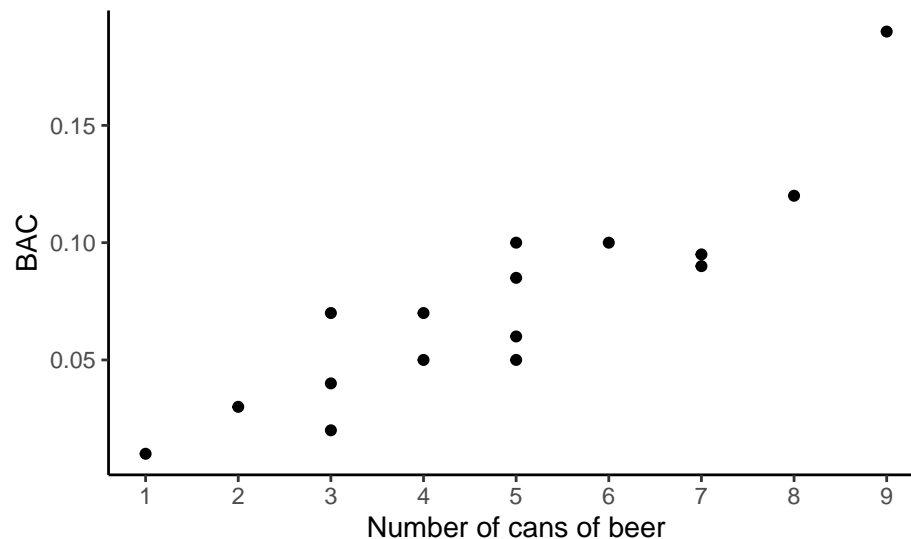
We will use the blood alcohol content data again. As a reminder this is the description: *Many people believe that gender, weight, drinking habits, and many other factors are much more important in predicting blood alcohol content (BAC) than simply considering the number of drinks a person consumed. Here we examine data from sixteen student volunteers at Ohio State University who each drank a randomly assigned number of cans of beer. These students were evenly divided between men and women, and they differed in weight and drinking habits. Thirty minutes later, a police officer measured their blood alcohol content (BAC) in grams of alcohol per deciliter of blood.*

The data is in the `openintro` package under `bac`.

- Obtain and interpret R -squared for this model.

```
library(openintro)
```

```
bac %>%  
  gf_point(bac~beers) %>%  
  gf_labs(x="Number of cans of beer",y="BAC") %>%  
  gf_theme(theme_classic()) %>%  
  gf_refine(scale_x_continuous(breaks = c(1,2,3,4,5,6,7,8,9)))
```



```
bac_mod <- lm(bac~beers,data=bac)
```

```
summary(bac_mod)
```

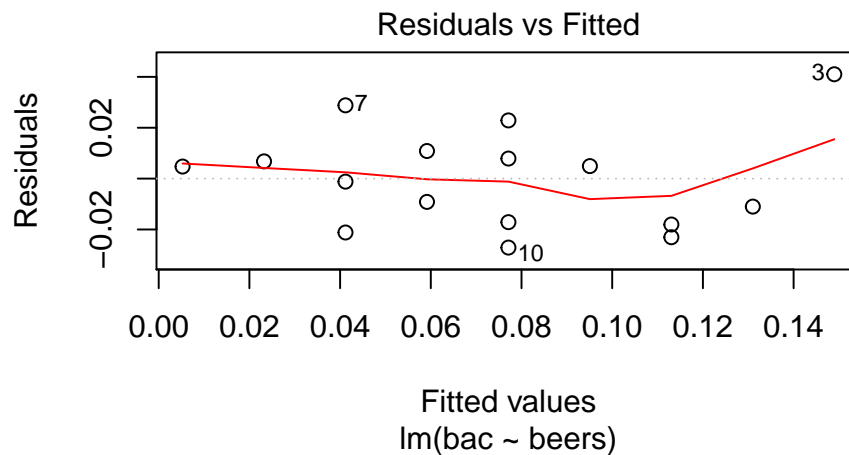
```
##  
## Call:  
## lm(formula = bac ~ beers, data = bac)  
##  
## Residuals:  
##      Min       1Q   Median       3Q      Max   
## -0.027118 -0.017350  0.001773  0.008623  0.041027   
##
```

```
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.012701  0.012638  -1.005   0.332
## beers       0.017964  0.002402   7.480 2.97e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02044 on 14 degrees of freedom
## Multiple R-squared:  0.7998, Adjusted R-squared:  0.7855
## F-statistic: 55.94 on 1 and 14 DF,  p-value: 2.969e-06
```

The R -squared is 0.7998, this means that almost 80% of the variance in blood alcohol content is explained by the number of beers consumed. This is not surprising. The remaining variance may be due to measurement errors, differences in the students, and environmental impacts.

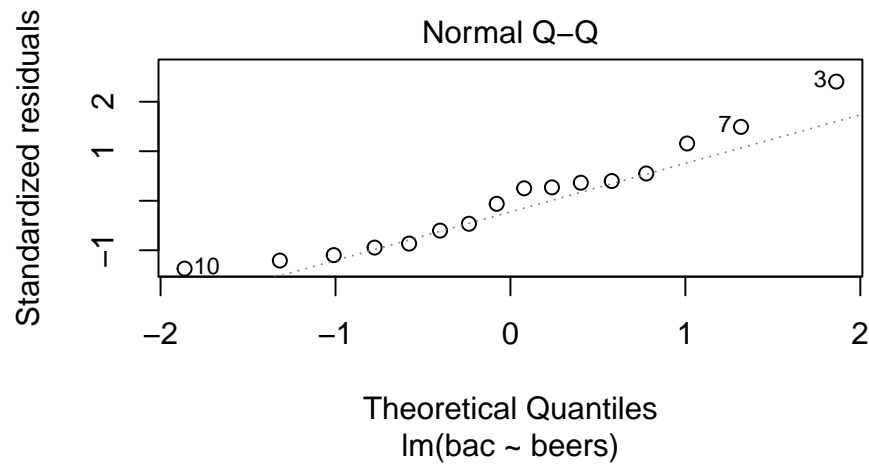
b. Evaluate the assumptions of this model. Do we have anything to be concerned about?

```
plot(bac_mod,1)
```



The fit is pretty good, there is one data point that is an outlier, the student that drank 9 beers.

```
plot(bac_mod,2)
```

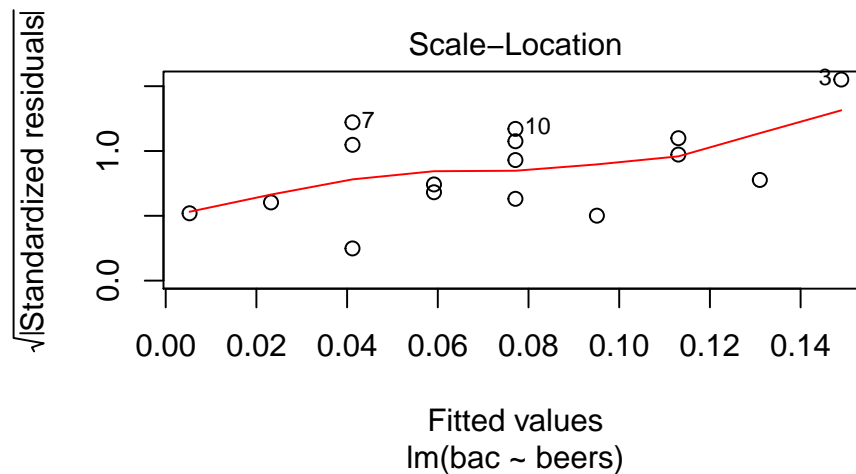


```
bac
```

```
## # A tibble: 16 x 3
##   student beers  bac
##   <int> <int> <dbl>
## 1     1     5 0.1
## 2     2     2 0.03
## 3     3     9 0.19
## 4     4     8 0.12
## 5     5     3 0.04
## 6     6     7 0.095
## 7     7     3 0.07
## 8     8     5 0.06
## 9     9     3 0.02
## 10    10     5 0.05
## 11    11     4 0.07
## 12    12     6 0.1
## 13    13     5 0.085
## 14    14     7 0.09
## 15    15     1 0.01
## 16    16     4 0.05
```

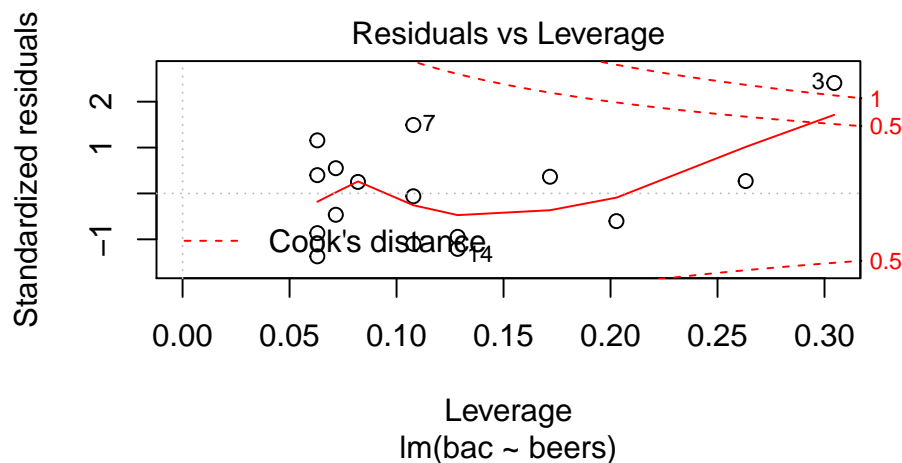
The 3rd, 7th, and 10th data points stand out. This data set is too small to make any decisions about normality. It is suspect though.

```
plot(bac_mod,3)
```



We have higher variance at the higher number of beers. Again this appears to be caused by the small number of data points and the influence of observation number 3.

```
plot(bac_mod, 5)
```

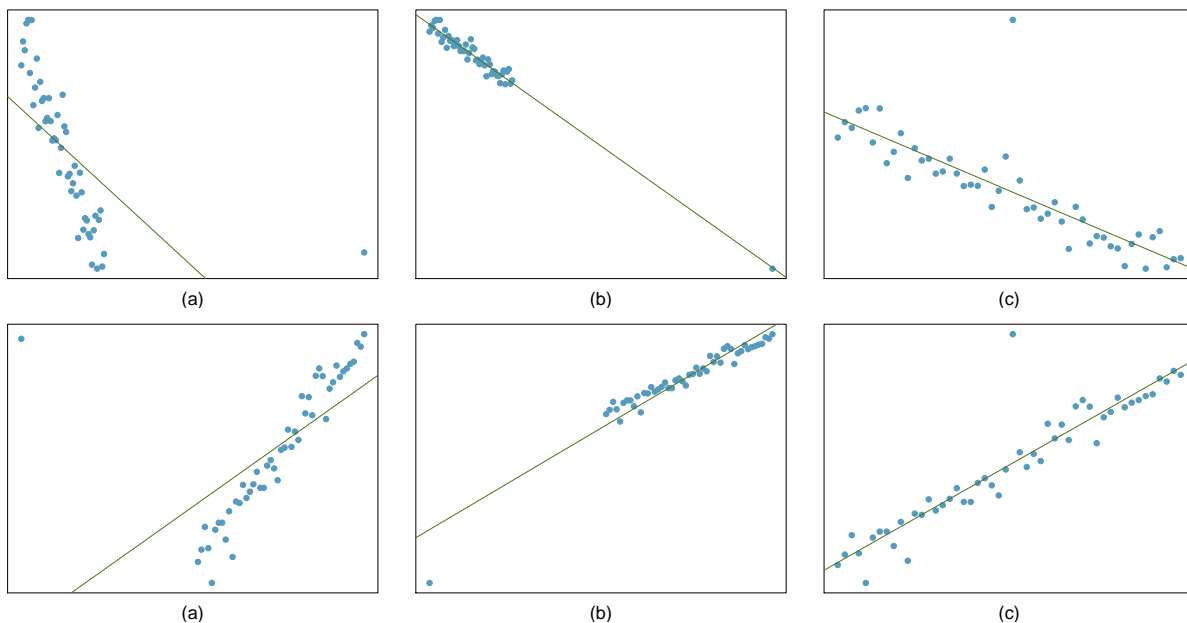


The points we're looking for (or not looking for) are values in the upper right or lower right corners, which are outside the red dashed Cook's distance line. These are points that would be influential in the model and removing them would likely noticeably alter the regression results. Now we see that observation 3 has extreme leverage on the model. Removing it would potentially drastically alter the model.

To learn more about measures of influence, see https://cran.r-project.org/web/packages/olsrr/vignettes/influence_measures.html

3. Outliers

Identify the outliers in the scatterplots shown below and determine what type of outliers they are. Explain your reasoning.



- (a) The outlier is located in the bottom right corner of the plot. If we were to exclude this point from the analysis, the slope of the regression line would be notably affected, which means this is a high-leverage and influential point.
- (b) The outlier is located in the bottom right corner of the plot. It is a point with high leverage since it is horizontally away from the center of the data, but it is not influential since the regression line would change little if it was removed.
- (c) The outlier is located in the center and top of the plot. Though the point is unlike the rest of the data, it is not a high-leverage point since it is not far on the x-axis from the center of the data. This also means it is not an influential point since its presence has little influence on the slope of the regression line.
- (d) The outlier is in the upper-left corner. Since it is horizontally far from the center of the data, it is an influential point. Additionally, since the fit of the regression line is greatly influenced by this point, it is a point with high leverage.
- (e) The outlier is located in the lower-left corner. It is horizontally far from the rest of the data, so it is a high-leverage point. The regression line also would fall relatively far from this point if the fit excluded this point, meaning it the outlier is influential.
- (f) The outlier is in the upper-middle of the plot. Since it is near the horizontal center of the data, it is not a high-leverage point. This means it also will have little or no influence on the slope of the regression line.

File Creation Information

- File creation date: 2020-08-11
- Windows version: Windows 10 x64 (build 18362)
- R version 3.6.3 (2020-02-29)
- `mosaic` package version: 1.7.0
- `tidyverse` package version: 1.3.0

- openintro package version: 2.0.0