# BCurve

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# October 15, 2017

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# Introduction

BCurve is C library to manipulate Bezier curves of any dimension and order.

It offers function to create, clone, load, save and modify a curve, to print it, to scale, rotate (in 2D) or translate it, to get its approximate length (sum of distance between control points), to create a BCurve connecting points of a point cloud, and to get the weights (coefficients of each control point given the value of the parameter of the curve).

## 1 Definitions

#### 1.1 BCurve definition

A BCurve B is defined by its dimension  $D \in \mathbb{N}_+^*$ , its order  $O \in \mathbb{N}_+$  and its (O+1) control points  $\overrightarrow{C_i}$  (vectors of dimension D). The curve in dimension D associated to the BCurve B is defined by  $\overrightarrow{B(t)}$ :

$$\begin{cases}
\overrightarrow{B(t)} = \sum_{i=0}^{O} W_i^O(t) \overrightarrow{C_i} & \text{if } t \in [0.0, 1.0] \\
\overrightarrow{B(t)} = \overrightarrow{C_0} & \text{if } t < 0.0 \\
\overrightarrow{B(t)} = \overrightarrow{C_O} & \text{if } t > 1.0
\end{cases} \tag{1}$$

where, if O = 0

$$W_0^0(t) = 1.0 (2)$$

and if  $O \neq 0$ 

$$\begin{cases} W_0^1(t) = 1.0 - t \\ W_1^1(t) = t \\ W_{-1}^i(t) = 0.0 \\ W_j^i(t) = (1.0 - t)W_j^{i-1}(t) + tW_{j-1}^{i-1}(t) \text{ for } i \in [2, O], j \in [0, i] \end{cases}$$
(3)

### 1.2 BCurve from cloud points

Given the cloud points made of N points  $\overrightarrow{P_i}$ , the  $\overrightarrow{BCurve}$  of order N-1 passing through the N points (in the same order  $\overrightarrow{P_0}, \overrightarrow{P_1}, \overrightarrow{P_2}, \dots$  as given in input) can be obtained as follow.

If N=1 the solution is trivial:  $\overrightarrow{C_0}=\overrightarrow{P_0}$ . As well, if N=2 the solution is trivial:  $\overrightarrow{C_0}=\overrightarrow{P_0}$  and  $\overrightarrow{C_1}=\overrightarrow{P_1}$ .

If N > 2, we need first to define the N values  $t_i$  corresponding to each  $\overrightarrow{P_i}$   $(\overrightarrow{B(t_i)} = \overrightarrow{P_i})$ . We will consider here  $t_i$  such as

$$t_i = \frac{L(\overrightarrow{P_i})}{L(\overrightarrow{P_{N-1}})} \tag{4}$$

where

$$\begin{cases}
L(P_0) = 0.0 \\
L(P_i) = \sum_{j=1}^{i} \left| \left| \overrightarrow{P_{j-1}P_j} \right| \right|
\end{cases}$$
(5)

then we can calculate the  $C_i$  as follow. We have  $\overrightarrow{C_0} = \overrightarrow{P_0}$  and  $\overrightarrow{C_{N-1}} = \overrightarrow{P_{N-1}}$ , and others  $\overrightarrow{C_i}$  can be obtained by solving the linear system below for each dimension:

$$\begin{bmatrix} W_1^{N-1}(t_1) & \dots & W_{N-2}^{N-1}(t_1) \\ \dots & \dots & \dots \\ W_1^{N-1}(t_{N-2}) & \dots & W_{N-2}^{N-1}(t_{N-2}) \end{bmatrix} \begin{bmatrix} C_1 \\ \dots \\ C_{N-2} \end{bmatrix} = \\ \begin{bmatrix} P_1 - \left(W_0^{N-1}(t_1)P_0 + W_{N-1}^{N-1}(t_1)P_{N-1}\right) \\ \dots \\ P_{N-2} - \left(W_0^{N-1}(t_{N-2})P_0 + W_{N-1}^{N-1}(t_{N-2})P_{N-1}\right) \end{bmatrix}$$

$$(6)$$

# 2 Interface

```
// ====== BCURVE.H ========
#ifndef BCURVE_H
#define BCURVE_H
// ========= Include =========
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <stdbool.h>
#include "pbmath.h"
#include "gset.h"
// ======= Define ========
// ====== Data structure =========
typedef struct BCurve {
  // Order
 int _order;
 // Dimension
 int _dim;
  // array of (_order + 1) control points defining the curve
 VecFloat **_ctrl;
} BCurve;
// ========= Functions declaration ==========
// Create a new BCurve of order 'order' and dimension 'dim'
// Return NULL if we couldn't create the BCurve
BCurve* BCurveCreate(int order, int dim);
// Clone the BCurve
// Return NULL if we couldn't clone the BCurve
BCurve* BCurveClone(BCurve *that);
// Load the BCurve from the stream
// If the BCurve is already allocated, it is freed before loading
```

```
// Return 0 in case of success, or:
// 1: invalid arguments
// 2: can't allocate memory
// 3: invalid data
// 4: fscanf error
// 5: VecLoad error
int BCurveLoad(BCurve **that, FILE *stream);
// Save the BCurve to the stream
// Return 0 upon success, else
// 1: invalid arguments
// 2: fprintf error
// 3: VecSave error
int BCurveSave(BCurve *that, FILE *stream);
// Free the memory used by a BCurve
// Do nothing if arguments are invalid
void BCurveFree(BCurve **that);
// Print the BCurve on 'stream'
// Do nothing if arguments are invalid
void BCurvePrint(BCurve *that, FILE *stream);
// Set the value of the iCtrl-th control point to v
// Do nothing if arguments are invalid
void BCurveSet(BCurve *that, int iCtrl, VecFloat *v);
// Get the value of the BCurve at paramater 'u' (in [0.0, 1.0])
// Return NULL if arguments are invalid or malloc failed
// if 'u' < 0.0 it is replaced by 0.0
// if 'u' > 1.0 it is replaced by 1.0
VecFloat* BCurveGet(BCurve *that, float u);
// Get the order of the BCurve
// Return -1 if argument is invalid
int BCurveOrder(BCurve *that);
// Get the dimension of the BCurve
// Return 0 if argument is invalid
int BCurveDim(BCurve *that);
// Get the approximate length of the BCurve (sum of dist between
// control points)
// Return 0.0 if argument is invalid
float BCurveApproxLen(BCurve *that);
// Rotate the curve CCW by 'theta' radians relatively to the origin
// Do nothing if arguments are invalid
void BCurveRot2D(BCurve *that, float theta);
// Scale the curve by 'v' relatively to the origin
// Do nothing if arguments are invalid
void BCurveScale(BCurve *that, VecFloat *v);
// Translate the curve by 'v'
// Do nothing if arguments are invalid
void BCurveTranslate(BCurve *that, VecFloat *v);
// Create a BCurve which pass through the points given in the GSet 'set'
// The GSet must contains VecFloat of same dimensions
\ensuremath{//} The BCurve pass through the points in the order they are given
// in the GSet. The points don't need to be uniformly distributed
```

```
// The created BCurve is of same dimension as the VecFloat and of order
// equal to the number of VecFloat in 'set' minus one
// Return NULL if it couldn't create the BCurve or the arguments are
// invalid
BCurve* BCurveFromCloudPoint(GSet *set);

// Get a VecFloat of dimension equal to the number of control points
// Values of the VecFloat are the weight of each control point in the
// BCurve given the curve's order and the value of 't' (in [0.0,1.0])
// Return null if the arguments are invalid or memory allocation failed
VecFloat* BCurveGetWeightCtrlPt(BCurve *curve, float t);
```

#endif

## 3 Code

```
// ====== BCURVE.C =======
// ========= Include =========
#include "bcurve.h"
// ======== Define =========
// ====== Functions implementation =========
// Create a new BCurve of order 'order' and dimension 'dim'
// Return NULL if we couldn't create the BCurve
BCurve* BCurveCreate(int order, int dim) {
 // Check arguments
 if (order < 0 || dim < 1)
   return NULL;
  // Allocate memory
  BCurve *that = (BCurve*)malloc(sizeof(BCurve));
  //If we could allocate memory
  if (that != NULL) {
   // Set the values
   that->_dim = dim;
   that->_order = order;
   // Allocate memory for the array of control points
   that->_ctrl = (VecFloat**)malloc(sizeof(VecFloat*) * (order + 1));
   // If we couldn't allocate memory
   if (that->_ctrl == NULL) {
     // Free memory
     free(that);
     // Stop here
     return NULL;
   // For each control point
   for (int iCtrl = 0; iCtrl < order + 1; ++iCtrl) {</pre>
     // Allocate memory
     that->_ctrl[iCtrl] = VecFloatCreate(dim);
     // If we couldn't allocate memory
     if (that->_ctrl[iCtrl] == NULL) {
       // Free memory
       BCurveFree(&that);
       // Stop here
       return NULL;
```

```
}
 // Return the new BCurve
 return that;
// Clone the BCurve
// Return NULL if we couldn't clone the BCurve
BCurve* BCurveClone(BCurve *that) {
 // Check argument
 if (that == NULL)
   return NULL;
  // Allocate memory for the clone
 BCurve *clone = (BCurve*)malloc(sizeof(BCurve));
  // If we could allocate memory
  if (clone != NULL) {
   // Clone the properties
    clone->_dim = that->_dim;
    clone->_order = that->_order;
    // Allocate memory for the array of control points
    clone->_ctrl = (VecFloat**)malloc(sizeof(VecFloat*) *
      (clone->_order + 1));
    // If we couldn't allocate memory
    if (that->_ctrl == NULL) {
     // Free memory
     free(clone);
     // Stop here
     return NULL;
    // For each control point
    for (int iCtrl = 0; iCtrl < clone->_order + 1; ++iCtrl) {
      // Clone the control point
     clone->_ctrl[iCtrl] = VecClone(that->_ctrl[iCtrl]);
      // If we couldn't clone the control point
      if (clone->_ctrl[iCtrl] == NULL) {
        // Free memory
        BCurveFree(&clone);
        // Stop here
       return NULL;
     }
 // Return the clone
 return clone;
// Load the BCurve from the stream
// If the BCurve is already allocated, it is freed before loading
// Return 0 in case of success, or:
// 1: invalid arguments
// 2: can't allocate memory
// 3: invalid data
// 4: fscanf error
// 5: VecLoad error
int BCurveLoad(BCurve **that, FILE *stream) {
 // Check arguments
 if (that == NULL || stream == NULL)
   return 1;
  // If 'that' is already allocated
 if (*that != NULL) {
    // Free memory
   BCurveFree(that);
```

```
// Read the order and dimension
  int order;
  int dim;
  int ret = fscanf(stream, "%d %d", &order, &dim);
  // If we couldn't read
  if (ret == EOF) {
   return 4;
  }
  // Allocate memory
  *that = BCurveCreate(order, dim);
  // If we coudln't allocate memory
  if (*that == NULL) {
   return 2;
  }
  // For each control point
  for (int iCtrl = 0; iCtrl < (order + 1); ++iCtrl) {</pre>
    \ensuremath{//} Load the control point
    ret = VecLoad((*that)->_ctrl + iCtrl, stream);
    // If we couldn't read the control point or the conrtol point
    // is not of the correct dimension
    if (ret != 0 || VecDim((*that)->_ctrl[iCtrl]) != (*that)->_dim) {
      // Free memory
      BCurveFree(that);
      // Stop here
      return 5;
   }
  }
  // Return success code
 return 0;
// Save the BCurve to the stream
// Return 0 upon success, or
// 1: invalid arguments
// 2: fprintf error
// 3: VecSave error
int BCurveSave(BCurve *that, FILE *stream) {
 // Check arguments
  if (that == NULL || stream == NULL)
   return 1;
  \ensuremath{//} Save the order and dimension
  int ret = fprintf(stream, "%d %d\n", that->_order, that->_dim);
  // If the fprintf failed
  if (ret < 0) \{
   // Stop here
   return 2;
  // For each control point
  for (int iCtrl = 0; iCtrl < that->_order + 1; ++iCtrl) {
    // Save the control point
    ret = VecSave(that->_ctrl[iCtrl], stream);
    // If we couldn't save the control point
    if (ret != 0) {
      // Stop here
      return 3;
  // Return success code
 return 0;
```

```
// Free the memory used by a BCurve
// Do nothing if arguments are invalid
void BCurveFree(BCurve **that) {
 // Check argument
 if (that == NULL || *that == NULL)
   return;
  // If there are control points
  if ((*that)->_ctrl != NULL) {
   // For each control point
    for (int iCtrl = 0; iCtrl < (*that)->_order + 1; ++iCtrl) {
     // Free the control point
     VecFree((*that)->_ctrl + iCtrl);
   }
 \ensuremath{//} Free the array of control points
 free((*that)->_ctrl);
 // Free memory
 free(*that);
 *that = NULL;
// Print the BCurve on 'stream'
// Do nothing if arguments are invalid
void BCurvePrint(BCurve *that, FILE *stream) {
 // Check arguments
 if (that == NULL || stream == NULL)
   return;
  // Print the order and dim
 fprintf(stream, "order(%d) dim(%d) ", that->_order, that->_dim);
 // For each control point
 for (int iCtrl = 0; iCtrl < that->_order + 1; ++iCtrl) {
    VecPrint(that->_ctrl[iCtrl], stream);
   fprintf(stream, " ");
 }
// Set the value of the iCtrl-th control point to v
// Do nothing if arguments are invalid
void BCurveSet(BCurve *that, int iCtrl, VecFloat *v) {
 // Check arguments
 if (that == NULL || v == NULL || iCtrl < 0 ||
   iCtrl > that->_order || VecDim(v) != BCurveDim(that))
    return;
  // Set the values
 VecCopy(that->_ctrl[iCtrl], v);
// Get the value of the BCurve at paramater 'u' (in [0.0, 1.0])
// Return NULL if arguments are invalid or malloc failed
// if 'u' < 0.0 it is replaced by 0.0
// if 'u' > 1.0 it is replaced by 1.0
VecFloat* BCurveGet(BCurve *that, float u) {
 // Check arguments
 if (that == NULL)
   return NULL;
  if (u < 0.0)
   u = 0.0;
 if (u > 1.0)
   u = 1.0;
  // Allocate memory for the result
 VecFloat *v = VecFloatCreate(that->_dim);
 // If we couldn't allocate memory
```

```
if (v == NULL)
    return NULL;
  // Declare a variable for calcul
  float *val = (float*)malloc(sizeof(float) * (that->_order + 1));
  // Loop on dimension
  for (int dim = that->_dim; dim--;) {
    // Initialise the temporary variable with the value in current
    // dimension of the control points
    for (int iCtrl = 0; iCtrl < that->_order + 1; ++iCtrl)
      val[iCtrl] = VecGet(that->_ctrl[iCtrl], dim);
    // Loop on order
    int subOrder = that->_order;
    while (subOrder != 0) {
      // Loop on sub order
      for (int order = 0; order < subOrder; ++order) {</pre>
        val[order] = (1.0 - u) * val[order] + u * val[order + 1];
      --subOrder;
    // Set the value for the current dim
    VecSet(v, dim, val[0]);
  // Free memory
  free(val);
  // Return the result
 return v;
}
// Get the order of the BCurve
// Return -1 if argument is invalid
int BCurveOrder(BCurve *that) {
  // Check arguments
 if (that == NULL)
    return -1;
 return that->_order;
// Get the dimension of the BCurve
// Return 0 if argument is invalid
int BCurveDim(BCurve *that) {
  // Check arguments
  if (that == NULL)
    return 0;
 return that->_dim;
// Get the approximate length of the BCurve (sum of dist between
// control points)
// Return 0.0 if argument is invalid
float BCurveApproxLen(BCurve *that) {
  // Check arguments
  if (that == NULL)
    return 0.0;
  // Declare a variable to calculate the length
  float res = 0.0;
  // Calculate the length
  for (int iCtrl = 0; iCtrl < that->_order; ++iCtrl)
    res += VecDist(that->_ctrl[iCtrl], that->_ctrl[iCtrl + 1]);
  // Return the length
 return res;
```

```
// Rotate the curve CCW by 'theta' radians relatively to the origin
// Do nothing if arguments are invalid
void BCurveRot2D(BCurve *that, float theta) {
  // Check arguments
  if (that == NULL || that->_dim != 2)
    return;
  // For each control point
  for (int iCtrl = 0; iCtrl <= that->_order; ++iCtrl)
    // Rotate the control point
    VecRot2D(that->_ctrl[iCtrl], theta);
}
// Scale the curve by 'v' relatively to the origin
// Do nothing if arguments are invalid
void BCurveScale(BCurve *that, VecFloat *v) {
  // Check arguments
  if (that == NULL || v == NULL)
    return;
  // For each control point
  for (int iCtrl = 0; iCtrl <= that->_order; ++iCtrl)
    // Scale the control point
    for (int dim = 0; dim < VecDim(that->_ctrl[iCtrl]); ++dim)
      VecSet(that->_ctrl[iCtrl], dim,
        VecGet(that->_ctrl[iCtrl], dim) * VecGet(v, dim));
}
// Translate the curve by 'v'
// Do nothing if arguments are invalid
void BCurveTranslate(BCurve *that, VecFloat *v) {
  // Check arguments
  if (that == NULL || v == NULL)
    return;
  // For each control point
  for (int iCtrl = 0; iCtrl <= that->_order; ++iCtrl)
    // Translate the control point
    VecOp(that->_ctrl[iCtrl], 1.0, v, 1.0);
}
// Create a BCurve which pass through the points given in the GSet 'set'
// The GSet must contains VecFloat of same dimensions
// The BCurve pass through the points in the order they are given
\ensuremath{//} in the GSet. The points don't need to be uniformly distributed
// The created BCurve is of same dimension as the VecFloat and of order
// equal to the number of VecFloat in 'set' minus one
// Return NULL if it couldn't create the BCurve or the arguments are
// invalid
BCurve* BCurveFromCloudPoint(GSet *set) {
  // Check arguments
  if (set == NULL || set->_nbElem < 1)</pre>
    return NULL;
  // Declare a variable to memorize the result
  int order = set-> nbElem - 1:
  int dim = VecDim((VecFloat*)(set->_head->_data));
  BCurve *curve = BCurveCreate(order, dim);
  // If we could allocate memory
  if (curve != NULL) {
    // Set the first control point to the first point in the point cloud
    BCurveSet(curve, 0, (VecFloat*)(set->_head->_data));
    // If the order is greater than 0
    if (order > 0) {
      // Set the last control point to the last point in the point cloud
      BCurveSet(curve, order, (VecFloat*)(set->_tail->_data));
```

```
// If the order is greater than 1
if (order > 1) {
  // Calculate the t values for intermediate control points
  // They are equal to the relative distance on the polyline
  // linking the point in the point cloud
  // Declare a variable to memorize the dimension of the matrix
  // in the linear system to solve
  VecShort *dimMat = VecShortCreate(2);
  // Declare a variable to memorize the t values
  VecFloat *t = VecFloatCreate(order + 1);
  // If we could allocate memory
  if (t != NULL && dimMat != NULL) {
    // Set the dimensions of the matrix of the linear system
    VecSet(dimMat, 0, order - 1);
    VecSet(dimMat, 1, order - 1);
    // For each point
    GSetElem *elem = set->_head->_next;
    int iPoint = 1;
    while (elem != NULL) {
      // Get the distance from the previous point
      float d = VecDist((VecFloat*)(elem->_prev->_data),
        (VecFloat*)(elem->_data));
      VecSet(t, iPoint, d + VecGet(t, iPoint - 1));
      ++iPoint;
      elem = elem->_next;
    // Normalize t
    for (iPoint = 1; iPoint <= order; ++iPoint)</pre>
      VecSet(t, iPoint, VecGet(t, iPoint) / VecGet(t, order));
    // For each dimension
    for (int iDim = dim; iDim--;) {
      // Declare a variable to memorize the matrix and vector {\bf v}
      // of the linear system
      MatFloat *m = MatFloatCreate(dimMat);
      VecFloat *v = VecFloatCreate(VecGet(dimMat, 0));
      // If we could allocate memory
      if (m != NULL && v != NULL) {
        // Set the values of the linear system
        // For each line (equivalent to each intermediate point
        // in point cloud)
        for (VecSet(dimMat, 1, 0);
          VecGet(dimMat, 1) < order - 1;</pre>
          VecSet(dimMat, 1, VecGet(dimMat, 1) + 1)) {
          // Get the weight of the control point at the value
          // of t for this point
          VecFloat *weight =
            BCurveGetWeightCtrlPt(curve, VecGet(t,
            VecGet(dimMat, 1) + 1));
          // If we could get the weights
          if (weight != NULL) {
            // For each intermediate control point
            for (VecSet(dimMat, 0, 0);
              VecGet(dimMat, 0) < order - 1;</pre>
              VecSet(dimMat, 0, VecGet(dimMat, 0) + 1))
              \ensuremath{//} Set the matrix value with the corresponding
              // weight
              MatSet(m, dimMat, VecGet(weight,
                VecGet(dimMat, 0) + 1));
          // Set the vector value with the corresponding point
          // coordinate
          float x = VecGet((VecFloat*)(GSetGet(set,
```

```
VecGet(dimMat, 1) + 1)), iDim);
                x \rightarrow VecGet(weight, 0) *
                  VecGet((VecFloat*)(set->_head->_data), iDim);
                x -= VecGet(weight, order) *
                  VecGet((VecFloat*)(set->_tail->_data), iDim);
                VecSet(v, VecGet(dimMat, 1), x);
                // Free memory
                VecFree(&weight);
              // Declare a variable to memorize the linear system
              EqLinSys *sys = EqLinSysCreate(m, v);
              // If we could allocate memory
              if (sys != NULL) {
                // Solve the system
                VecFloat *solSys = EqLinSysSolve(sys);
                // If we could solve the linear system
                if (solSys != NULL) {
                  // Memorize the values of control points for the
                  // current dimension
                  for (int iCtrl = 1; iCtrl < order; ++iCtrl)</pre>
                    VecSet(curve->_ctrl[iCtrl], iDim,
                      VecGet(solSys, iCtrl - 1));
                  // Free memory
                  VecFree(&solSys);
               }
              // Free memory
             EqLinSysFree(&sys);
             VecFree(&v);
             MatFree(&m);
           }
         }
        // Free memory
        VecFree(&dimMat);
        VecFree(&t);
     }
   }
 // Return the result
 return curve;
// Get a VecFloat of dimension equal to the number of control points
// Values of the VecFloat are the weight of each control point in the
// BCurve given the curve's order and the value of 't' (in [0.0,1.0])
// Return null if the arguments are invalid or memory allocation failed
VecFloat* BCurveGetWeightCtrlPt(BCurve *curve, float t) {
 // Check arguments
 if (curve == NULL || t < 0.0 || t > 1.0)
   return NULL;
 // Declare a variable to memorize the result
 VecFloat *res = VecFloatCreate(curve->_order + 1);
 // If we could allocate memory
 if (res != NULL) {
   // Initilize the two first weights
   VecSet(res, 0, 1.0 - t);
   VecSet(res, 1, t);
   // For each higher order
   for (int order = 1; order < curve->_order; ++order) {
     // For each control point at this order, starting by the last one
     // to avoid using a temporary buffer
```

# 4 Makefile

```
OPTIONS_DEBUG=-ggdb -g3 -Wall
OPTIONS_RELEASE=-03
OPTIONS=$(OPTIONS_RELEASE)
INCPATH=/home/bayashi/Coding/Include
LIBPATH=/home/bayashi/Coding/Include
all : main
main: main.o bcurve.o $(LIBPATH)/pbmath.o $(LIBPATH)/gset.o Makefile
gcc $(OPTIONS) main.o bcurve.o $(LIBPATH)/pbmath.o $(LIBPATH)/gset.o -o main -lm
main.o : main.c bcurve.h Makefile
gcc $(OPTIONS) -I$(INCPATH) -c main.c
bcurve.o : bcurve.c bcurve.h $(INCPATH)/pbmath.h $(INCPATH)/gset.h Makefile
gcc $(OPTIONS) -I$(INCPATH) -c bcurve.c
clean :
rm -rf *.o main
valgrind:
valgrind -v --track-origins=yes --leak-check=full --gen-suppressions=yes --show-leak-kinds=all ./main
cp bcurve.h ../Include; cp bcurve.o ../Include
```

# 5 Usage

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
#include <string.h>
#include "bcurve.h"

float CloudCurveX(float t) {
   return t * t;
   //return 2.0 * cos(t * PBMATH_HALFPI);
}

float CloudCurveY(float t) {
```

```
return sqrt(t);
 //return sin(t * PBMATH_HALFPI);
int main(int argc, char **argv) {
 // Create a BCurve
 int order = 3;
 int dim = 2;
 BCurve *curve = BCurveCreate(order, dim);
 // If we couldn't create the BCurve
 if (curve == NULL) {
   // Print a message
fprintf(stderr, "BCurveCreate failed\n");
   // Stop here
   return 1;
 // Print the BCurve
 BCurvePrint(curve, stdout);
 fprintf(stdout, "\n");
  // Create a VecFloat to set the values
 VecFloat *v = VecFloatCreate(dim);
  // If we couldn't create the VecFloat
 if (v == NULL) {
   // Release memory
   BCurveFree(&curve);
    // Stop here
   return 2;
 \ensuremath{//} Set the control points
 float ctrlPts[8] = \{0.0, 1.0, 2.0, 5.0, 4.0, 3.0, 6.0, 7.0\};
 for (int iCtrl = 0; iCtrl < order + 1; ++iCtrl) {</pre>
    VecSet(v, 0, ctrlPts[2 * iCtrl]);
    VecSet(v, 1, ctrlPts[2 * iCtrl + 1]);
   BCurveSet(curve, iCtrl, v);
 // Print the BCurve
 BCurvePrint(curve, stdout);
 fprintf(stdout, "\n");
  // Save the curve
 FILE *file = fopen("./curve.txt", "w");
  // If we couldn't open the file
 if (file == NULL) {
   // Print a message
   fprintf(stderr, "Can't open file\n");
    // Free memory
    VecFree(&v);
   BCurveFree(&curve);
    // Stop here
   return 3;
 int ret = BCurveSave(curve, file);
 // If we couldn't save
 if (ret != 0) {
   // Print a message
   fprintf(stderr, "BCurveSave failed (%d)\n", ret);
    // Free memory
    VecFree(&v);
   BCurveFree(&curve);
    // Stop here
   return 4;
 fclose(file);
```

```
// Load the curve
file = fopen("./curve.txt", "r");
// If we couldn't open the file
if (file == NULL) {
  // Print a message
  fprintf(stderr, "Can't open file\n");
  // Free memory
  VecFree(&v);
 BCurveFree(&curve);
  // Stop here
 return 5;
BCurve *loaded = NULL;
ret = BCurveLoad(&loaded, file);
// If we couldn't load
if (ret != 0) {
 // Print a message
  fprintf(stderr, "BCurveLoad failed (%d)\n", ret);\\
  // Free memory
  VecFree(&v);
 BCurveFree(&curve);
 BCurveFree(&loaded);
 // Stop here
 return 6;
fclose(file);
// Print the loaded curve
BCurvePrint(loaded, stdout);
fprintf(stdout, "\n");
// Get some values of the curve
for (float u = 0.0; u \le 1.01; u += 0.1) {
  VecFloat *w = BCurveGet(curve, u);
  // If we couldn't get the values
  if (w == NULL) {
    // Free memory
    VecFree(&v);
   BCurveFree(&curve);
   BCurveFree(&loaded);
   // Stop here
   return 7;
  fprintf(stdout, "%.1f: ", u);
  VecPrint(w, stdout);
  fprintf(stdout, "\n");
  VecFree(&w);
// Scale the curve
VecSet(v, 0, 0.5);
VecSet(v, 1, 1.0);
BCurveScale(curve, v);
// Rotate the curve
BCurveRot2D(curve, PBMATH_PI * 0.5);
// Translate the curve
VecSet(v, 0, -0.5);
VecSet(v, 1, 1.0);
BCurveTranslate(curve, v);
// Get some values of the curve
fprintf(stdout, "After transformation:\n");
for (float u = 0.0; u \le 1.01; u += 0.1) {
 VecFloat *w = BCurveGet(curve, u);
  // If we couldn't get the values
  if (w == NULL) {
```

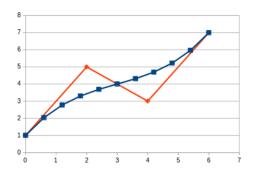
```
// Free memory
   VecFree(&v);
    BCurveFree(&curve);
   BCurveFree(&loaded);
    // Stop here
   return 7;
  fprintf(stdout, "%.1f: ", u);
  VecPrint(w, stdout);
  fprintf(stdout, "\n");
  VecFree(&w);
// Print the curve approximate length
fprintf(stdout, "approx length: %.3f\n", BCurveApproxLen(curve));
// Print the weight of control points
fprintf(stdout, "Control points weight:\n");
for (float t = 0.0; t <= 1.01; t += 0.05) {
  if (t > 1.0) t = 1.0;
  VecFloat *w = BCurveGetWeightCtrlPt(curve, t);
 if (w != NULL) {
   fprintf(stdout, "%.3f ", t);
    VecPrint(w, stdout);
   fprintf(stdout, "\n");
  VecFree(&w);
// Get a curve from a cloud point
GSet *cloud = GSetCreate();
if (cloud != NULL) {
 VecFloat *w = NULL;
  fprintf(stdout, "cloud:\n");
  //for (float t = 0.0; t < 1.01; t += 0.25) {
  //for (float t = 0.0; t < 1.01; t += 0.334) {
  for (float t = 0.0; t < 1.01; t += 0.5) {
   w = VecFloatCreate(2);
   GSetAppend(cloud, w);
   VecSet(w, 0, CloudCurveX(t));
   VecSet(w, 1, CloudCurveY(t));
   VecPrint(w, stdout);
   fprintf(stdout, "\n");
 }
 w = NULL;
  BCurve *cloudCurve = BCurveFromCloudPoint(cloud);
  if (cloudCurve == NULL) {
   fprintf(stdout, "Couldn't get curve from cloud\n");
   return 8;
 }
  fprintf(stdout, "cloudCurve: ");
 BCurvePrint(cloudCurve, stdout);
  fprintf(stdout, "\n");
  for (float t = 0.0; t < 1.01; t += 0.1) {
   if (t > 1.0) t = 1.0;
   fprintf(stdout, "%.3f ", t);
    w = BCurveGet(cloudCurve, t);
   VecPrint(w, stdout);
   fprintf(stdout, "\n");
    VecFree(&w);
 BCurveFree(&cloudCurve);
}
// Free memory
GSetElem *elem = cloud->_head;
```

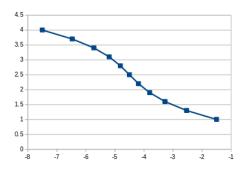
```
while (elem != NULL) {
   VecFree((VecFloat**)(&(elem->_data)));
   elem = elem->_next;
}
GSetFree(&cloud);
VecFree(&v);
BCurveFree(&curve);
BCurveFree(&loaded);
// Return success code
return 0;
```

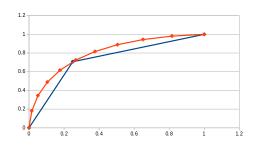
#### Output:

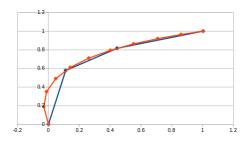
```
order(3) dim(2) <0.000,0.000> <0.000,0.000> <0.000,0.000> <0.000,0.000>
order(3) dim(2) <0.000,1.000> <2.000,5.000> <4.000,3.000> <6.000,7.000>
order(3) dim(2) <0.000,1.000> <2.000,5.000> <4.000,3.000> <6.000,7.000>
0.0: <0.000,1.000>
0.1: <0.600,2.032>
0.2: <1.200,2.776>
0.3: <1.800,3.304>
0.4: <2.400,3.688>
0.5: <3.000,4.000>
0.6: <3.600,4.312>
0.7: <4.200,4.696>
0.8: <4.800,5.224>
0.9: <5.400,5.968>
1.0: <6.000,7.000>
After transformation:
0.0: <-1.500,1.000>
0.1: <-2.532,1.300>
0.2: <-3.276,1.600>
0.3: <-3.804,1.900>
0.4: <-4.188,2.200>
0.5: <-4.500,2.500>
0.6: <-4.812,2.800>
0.7: <-5.196,3.100>
0.8: <-5.724,3.400>
0.9: <-6.468,3.700>
1.0: <-7.500,4.000>
approx length: 10.482
Control points weight:
0.000 <1.000,0.000,0.000,0.000>
0.050 <0.857,0.135,0.007,0.000>
0.100 <0.729,0.243,0.027,0.001>
0.150 < 0.614, 0.325, 0.057, 0.003>
0.200 < 0.512, 0.384, 0.096, 0.008>
0.250 < 0.422, 0.422, 0.141, 0.016>
0.300 < 0.343, 0.441, 0.189, 0.027>
0.350 <0.275,0.444,0.239,0.043>
0.400 < 0.216, 0.432, 0.288, 0.064>
0.450 < 0.166, 0.408, 0.334, 0.091>
0.500 <0.125,0.375,0.375,0.125>
0.550 < 0.091, 0.334, 0.408, 0.166>
0.600 < 0.064, 0.288, 0.432, 0.216>
0.650 <0.043,0.239,0.444,0.275>
0.700 < 0.027, 0.189, 0.441, 0.343>
0.750 < 0.016, 0.141, 0.422, 0.422>
0.800 < 0.008, 0.096, 0.384, 0.512>
0.850 < 0.003, 0.057, 0.325, 0.614>
```

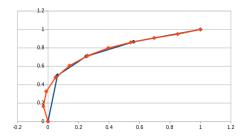
```
0.900 <0.001,0.027,0.243,0.729>
0.950 <0.000,0.007,0.135,0.857>
1.000 <0.000,0.000,0.000,1.000>
cloud:
<0.000,0.000>
<0.250,0.707>
<1.000,1.000>
cloudCurve: order(2) dim(2) <0.000,0.000> <0.035,0.950> <1.000,1.000>
0.000 <0.000,0.000>
0.100 <0.016,0.181>
0.200 <0.051,0.344>
0.300 <0.105,0.489>
0.400 <0.177,0.616>
0.500 <0.267,0.725>
0.600 <0.377,0.816>
0.700 <0.505,0.889>
0.800 < 0.651, 0.944>
0.900 <0.816,0.981>
1.000 <1.000,1.000>
```











#### curve.txt:

- 3 2 2 0.000000 1.000000 2 2.000000 5.000000 2 4.000000 3.000000 2 6.000000 7.000000