PBMath

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Introduction

PBMath is a C library providing mathematical structures and functions.

The VecFloat structure and its functions can be used to manipulate vectors of float values.

The VecShort structure and its functions can be used to manipulate vectors of short values.

The MatFloat structure and its functions can be used to manipulate matrices of float values.

The **Gauss** structure and its functions can be used to get values of the Gauss function and random values distributed accordingly with a Gauss distribution.

The Smoother functions can be used to get values of the SmoothStep and SmootherStep functions.

The EqLinSys structure and its functions can be used to solve systems of linear equation.

The Ratio structure and its functions can be used to manipulate rationals.

It uses the PBErr library.

1 Definitions

1.1 Vector

1.1.1 Distance between two vectors

For VecShort:

$$Dist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$

$$HamiltonDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$

$$PixelDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$
(1)

For VecFloat:

$$Dist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} (v_i - w_i)^2$$

$$HamiltonDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_i - w_i|$$

$$PixelDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |\lfloor v_i \rfloor - \lfloor w_i \rfloor|$$
(2)

1.1.2 Angle between two vectors

The problem is as follow: given two vectors \vec{V} and \vec{W} not null, how to calculate the angle θ from \vec{V} to \vec{W} .

Let's call M the rotation matrix: $M\vec{V} = \vec{W}$, and the components of M as follow:

$$M = \begin{bmatrix} Ma & Mb \\ Mc & Md \end{bmatrix} = \begin{bmatrix} cos(\theta) & -sin(\theta) \\ sin(\theta) & cos(\theta) \end{bmatrix}$$
(3)

Then, $M\vec{V} = \vec{W}$ can be written has

$$\begin{cases}
W_x = M_a V_x + M_b V_y \\
W_y = M_c V_x + M_d V_y
\end{cases}$$
(4)

Equivalent to

$$\begin{cases}
W_x = M_a V_x + M_b V_y \\
W_y = -M_b V_x + M_a V_y
\end{cases}$$
(5)

where $M_a = cos(\theta)$ and $M_b = -sin(\theta)$.

If $Vx \neq 0.0$, we can write

$$\begin{cases}
M_b = \frac{M_a V_y - W_y}{V_x} \\
M_a = \frac{W_x + W_y V_y / V_x}{V_x + V_y^2 / V_x}
\end{cases}$$
(6)

Or, if Vx = 0.0, we can write

$$\begin{cases}
Ma = \frac{W_y + M_b V_x}{V_y} \\
Mb = \frac{W_x - W_y V_x / V_y}{V_y + V_x^2 / V_y}
\end{cases}$$
(7)

Then we have $\theta = \pm \cos^{-1}(M_a)$ where the sign can be determined by verifying that the sign of $sin(\theta)$ matches the sign of $-M_b$: if $sin(cos^{-1}(M_a))*M_b > 0.0$ then multiply $\theta = -cos^{-1}(M_a)$ else $\theta = cos^{-1}(M_a)$.

1.1.3 Rotation

Rotation if a vector is only defined in 2D and 3D. In 2D, for a right-handed rotation of angle θ the rotation matrix is equal to:

$$R = \begin{bmatrix} cos(\theta) & -sin(\theta) \\ sin(\theta) & cos(\theta) \end{bmatrix}$$
 (8)

In 3D, for a right-handed rotation of angle θ around axis \overrightarrow{u} the rotation is equal to (to shorten notation θ is not written in the matrix below):

$$R = \begin{bmatrix} \cos + u_x^2 (1 - \cos) & u_x u_y (1 - \cos) - u_z \sin & u_x u_z (1 - \cos) + u_y \sin \\ u_x u_y (1 - \cos) + u_z \sin & \cos + u_y^2 (1 - \cos) & u_y u_z (1 - \cos) - u_x \sin \\ u_x u_z (1 - \cos) - u_y \sin & u_y u_z (1 - \cos) + u_x \sin & \cos + u_z^2 (1 - \cos) \end{bmatrix}$$
(9)

1.2 Matrix

1.2.1 Inverse matrix

The inverse of a matrix is only implemented for square matrices less than 3x3. It is computed directly, based on the determinant and the adjoint matrix.

For a 2x2 matrix M:

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} M_3 & -M_2 \\ -M_1 & M_0 \end{bmatrix}$$
 (10)

where

$$M = \begin{bmatrix} M_0 & M_2 \\ M_1 & M_3 \end{bmatrix} \tag{11}$$

and

$$det = M_0 M_3 - M_1 M_2 (12)$$

For a 3x3 matrix M:

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} (M_4 M_8 - M_5 M_7) & -(M_3 M_8 - M_5 M_6) & (M_3 M_7 - M_4 M_6) \\ -(M_1 M_8 - M_2 M_7) & (M_0 M_8 - M_2 M_6) & -(M_0 M_7 - M_1 M_6) \\ (M_1 M_5 - M_2 M_4) & -(M_0 M_5 - M_2 M_3) & (M_0 M_4 - M_1 M_3) \end{bmatrix}$$

$$(13)$$

where

$$M = \begin{bmatrix} M_0 & M_3 & M_6 \\ M_1 & M_4 & M_7 \\ M_2 & M_5 & M_8 \end{bmatrix}$$
 (14)

and

$$det = M_0(M_4M_8 - M_5M_7) - M_3(M_1M_8 - M_2M_7) + M_6(M_1M_5 - M_2M_4)$$
(15)

1.2.2 QR factorization

The QR factorization is performed using the Householder algorithm:

```
Compute Q and R such as A = QR
A[i][j] <=> value of matrix A at the i-th column and j-th row
Must have nbCol(A) <= nbRow(A)</pre>
QQtilde := matrix identity of dimensions (nbRow(A) columns, nbRow(A) rows)
for k := 0 to nbCol(A):
  w := vector null of dimension (nbRow(A) - k)
  for i := 0 to dim(w)
    w[i] := A[k][k + i]
  sign := if w[0] >= 0.0 then 1.0 else -1.0
  w[0] := w[0] + sign * norm(w)
  v = w / nom(w)
  H := matrix identity of dimensions (dim(v) columns, dim(v) rows)
  vvt := v * transpose(v)
  H := H - 2.0 * vvt
  \texttt{reflector} := \texttt{matrix} \texttt{ identity} \texttt{ of dimensions (nbRow(A) columns, nbRow(A) rows)}
  for i := 0 to nbCol(H)
    for j := 0 to nbRow(H)
      reflector[i + k][j + k] := H[i][j]
  A := reflector * A
  QQtilde := QQtilde * reflector
R := matrix of dimensions (nbCol(A) columns, nbCol(A) rows)
for i := 0 to nbCol(A)
  for j := 0 to nbCol(A)
    R[i][j] := A[i][j]
Q := matrix of dimensions (nbCol(A) columns, nbRow(A) rows)
for i := 0 to nbCol(A)
  for j := 0 to nbRow(A)
    Q[i][j] := QQtilde[i][j]
    Example of execution step by step:
[-1.000, -1.000, 1.000
 1.000, 3.000, 3.000
 -1.000, -1.000, 5.000
1.000, 3.000, 7.000]
k: 0
w: <-3.000,1.000,-1.000,1.000>
v: <-0.866,0.289,-0.289,0.289>
[ 0.750, -0.250, 0.250, -0.250
```

```
-0.250, 0.083, -0.083, 0.083
 0.250, -0.083, 0.083, -0.083
 -0.250, 0.083, -0.083, 0.083]
H:
[-0.500, 0.500, -0.500, 0.500
 0.500, 0.833, 0.167, -0.167
-0.500, 0.167, 0.833, 0.167
 0.500, -0.167, 0.167, 0.833]
reflector:
[-0.500, 0.500, -0.500, 0.500
 0.500, 0.833, 0.167, -0.167
 -0.500, 0.167, 0.833, 0.167
0.500, -0.167, 0.167, 0.833]
reflector.A:
[ 2.000, 4.000, 2.000
0.000, 1.333, 2.667
-0.000, 0.667, 5.333
 0.000, 1.333, 6.667]
QQtilde:
[-0.500, 0.500, -0.500, 0.500
 0.500, 0.833, 0.167, -0.167
-0.500, 0.167, 0.833, 0.167
0.500, -0.167, 0.167, 0.833]
k: 1
w: <3.333,0.667,1.333>
v: <0.913,0.183,0.365>
vvt:
[ 0.833, 0.167, 0.333
  0.167, 0.033, 0.067
0.333, 0.067, 0.133]
[-0.667, -0.333, -0.667
 -0.333, 0.933, -0.133
-0.667, -0.133, 0.733]
reflector:
[ 1.000, 0.000, 0.000, 0.000
0.000, -0.667, -0.333, -0.667
  0.000, -0.333, 0.933, -0.133
  0.000, -0.667, -0.133, 0.733]
reflector.A:
[ 2.000, 4.000, 2.000
 -0.000, -2.000, -8.000
-0.000, 0.000, 3.200
  0.000, -0.000, 2.400]
QQtilde:
[-0.500, -0.500, -0.700, 0.100
 0.500, -0.500, -0.100, -0.700
 -0.500, -0.500, 0.700, -0.100
0.500, -0.500, 0.100, 0.700]
k: 2
w: <7.200,2.400>
v: <0.949,0.316>
vvt:
[ 0.900, 0.300
  0.300, 0.100]
Η:
[-0.800, -0.600
 -0.600, 0.800]
```

```
reflector:
[ 1.000, 0.000, 0.000, 0.000
  0.000, 1.000, 0.000, 0.000
0.000, 0.000, -0.800, -0.600
  0.000, 0.000, -0.600, 0.800]
reflector.A:
[ 2.000, 4.000, 2.000
 -0.000, -2.000, -8.000
  0.000, -0.000, -4.000
0.000, -0.000, -0.000]
QQtilde:
[-0.500, -0.500, 0.500, 0.500
0.500, -0.500, 0.500, -0.500
 -0.500, -0.500, -0.500, -0.500
  0.500, -0.500, -0.500, 0.500]
[-0.500, -0.500, 0.500
  0.500, -0.500, 0.500
 -0.500, -0.500, -0.500
  0.500, -0.500, -0.500]
R:
[ 2.000, 4.000, 2.000
 -0.000, -2.000, -8.000
 0.000, -0.000, -4.000]
[-1.000, -1.000, 1.000
 1.000, 3.000, 3.000
-1.000, -1.000, 5.000
 1.000, 3.000, 7.000]
```

1.2.3 Eigen values and vectors

The Eigen values and vectors are obtained using the QR algorithm:

```
Compute Eigen values and vectors of A
A[i][j] <=> value of matrix A at the i-th column and j-th row
Must have nbCol(A) = nbRow(A)

err := 1.0
M := matrix identity of dimensions(nbCol(A) columns, nbRow(A) rows)
loop until err < epsilon
Q,R := QRDecomposition(A)
A := R * Q
M := M * Q
err := max(abs(non diagonal values of A))
for i := 0 to NbCol(A)
   eigenValue[i] := A[i][i]
   for j := 0 to nbRow(A)
        eigenVector_i[j] := M[i][j]

Example of execution step by step:
```

```
-1.150000, 3.320000, 4.570000]
k: 0
A:
[ 3.893980, 0.051622, -0.542073
 0.051622, 8.916388, 0.802225
-0.542073, 0.802225, 1.189634]
Μ:
[-0.897358, 0.044696, -0.439034]
 -0.264290, -0.851147, 0.453541
  0.353411, -0.523021, -0.775596]
k: 1
A:
[ 3.989910, -0.007497, -0.141512
-0.007497, 8.997707, 0.092890
-0.141512, 0.092890, 1.012387]
Μ:
[ 0.827596, -0.005324, 0.561300
  0.335447, 0.806451, -0.486943
 -0.450068, 0.591278, 0.669201]
k: 2
Α:
[ 3.996253, -0.020544, -0.035648
 -0.020544, 8.998704, 0.010273
-0.035648, 0.010273, 1.005045]
Μ:
[-0.807189, -0.002264, -0.590289
 -0.350981, -0.802184, 0.483025
0.474614, -0.597072, -0.646720]
k: 3
[ 3.996995, -0.046356, -0.008962
-0.046356, 8.998370, 0.001080
-0.008962, 0.001080, 1.004634]
[ 0.801869, 0.007056, 0.597458
 0.351147, 0.803462, -0.480776
-0.483427, 0.595315, 0.641793]
k: 4
Α:
[ 3.998767, -0.104343, -0.002252
 -0.104343, 8.996623, 0.000083
 -0.002252, 0.000083, 1.004609]
Μ:
[-0.800392, -0.016405, -0.599253
 -0.342883, -0.807440, 0.480075
0.491736, -0.589721, -0.640644]
k: 5
A:
[ 4.007611, -0.234525, -0.000566
 -0.234525, 8.987781, -0.000012
-0.000566, -0.000012, 1.004607]
Μ:
[ 0.799354, 0.037270, 0.599703
 0.321974, 0.816115, -0.479884
 -0.507312, 0.576686, 0.640365]
k: 6
```

```
A:
[ 4.051963, -0.523369, -0.000142
 -0.523369, 8.943428, -0.000013
 -0.000142, -0.000013, 1.004607]
M:
[-0.795727, -0.083897, -0.599817
 -0.273814, -0.833538, 0.479834
  0.540226, -0.546055, -0.640296]
k: 7
Α:
[ 4.265212, -1.127628, -0.000035
 -1.127628, 8.730177, -0.000008
 -0.000035, -0.000008, 1.004607]
Μ:
[ 0.778403, 0.185133, 0.599845
 0.164799, 0.861750, -0.479822
-0.605747, 0.472348, 0.640279]
k: 8
A:
[ 5.114194, -2.083614, -0.000008
 -2.083614, 7.881196, -0.000004
-0.000008, -0.000004, 1.004607]
[-0.705223, -0.377938, -0.599852]
  0.060932, -0.875249, 0.479818
0.706362, -0.301829, -0.640275]
A:
[ 6.964207, -2.457212, -0.000001
 -2.457211, 6.031182, -0.000002
-0.000001, -0.000002, 1.004607]
Μ:
[\ 0.510500,\ 0.616088,\ 0.599854
 -0.386664, 0.787570, -0.479818
-0.768037, 0.013005, 0.640274]
k: 10
Α:
[ 8.402923, -1.620381, -0.000000
-1.620380, 4.592468, -0.000001
-0.000000, -0.000001, 1.004607]
[-0.276422, -0.750843, -0.599854
0.626681, -0.614041, 0.479817
  0.728603, 0.243285, -0.640273]
k: 11
Α:
[ 8.868839, -0.795746, 0.000000
 -0.795745, 4.126554, -0.000000
-0.000000, -0.000000, 1.004607]
Μ:
[ 0.129251, 0.789600, 0.599855 -0.731611, 0.484273, -0.479817
 -0.669357, -0.376843, 0.640273]
k: 12
A:
```

```
[ 8.972622, -0.360938, 0.000000
 -0.360938, 4.022771, -0.000000
 -0.000000, -0.000000, 1.004607]
Μ:
[-0.058172, -0.797991, -0.599855
  0.771961, -0.416956, 0.479817
0.633003, 0.435152, -0.640273]
k: 13
[ 8.993616, -0.160978, 0.000000
-0.160978, 4.001777, -0.000000
-0.000000, -0.000000, 1.004607]
[ 0.026050, 0.799685, 0.599855
-0.788096, 0.385590, -0.479817
-0.615001, -0.460244, 0.640273]
k: 14
Α:
[ 8.997777, -0.071554, 0.000000
-0.071554, 3.997614, -0.000000
-0.000000, -0.000000, 1.004607]
[-0.011735, -0.800023, -0.599855
  0.794871, -0.371425, 0.479817
  0.606666, 0.471176, -0.640273]
k: 15
A:
[ 8.998597, -0.031784, 0.000000
-0.031784, 3.996793, -0.000000
-0.000000, -0.000000, 1.004607]
Μ:
[ 0.005373, 0.800091, 0.599855
 -0.797799, 0.365092, -0.479817
 -0.602899, -0.475986, 0.640273]
k: 16
A:
[ 8.998760, -0.014117, 0.000000
-0.014117, 3.996630, -0.000000
 -0.000000, -0.000000, 1.004607]
Μ:
[-0.002547, -0.800105, -0.599855
  0.799084, -0.362272, 0.479817
  0.601215, 0.478112, -0.640273]
k: 17
[ 8.998793, -0.006270, 0.000000
 -0.006270, 3.996598, -0.000000
 -0.000000, -0.000000, 1.004607]
Μ:
[ 0.001291, 0.800108, 0.599855
 -0.799651, 0.361018, -0.479817
-0.600464, -0.479055, 0.640273]
k: 18
Α:
[ 8.998798, -0.002785, 0.000000
 -0.002784, 3.996592, -0.000000
```

```
-0.000000, -0.000000, 1.004607]
Μ:
[-0.000734, -0.800108, -0.599855
  0.799902, -0.360460, 0.479817
  0.600130, 0.479473, -0.640273]
k: 19
A:
[ 8.998800, -0.001237, 0.000000
-0.001237, 3.996591, -0.000000
 -0.000000, -0.000000, 1.004607]
Μ:
[ 0.000486, 0.800109, 0.599855
-0.800014, 0.360213, -0.479817
-0.599982, -0.479659, 0.640273]
k: 20
A:
[ 8.998800, -0.000550, 0.000000
 -0.000549, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
Μ:
[-0.000376, -0.800109, -0.599855
  0.800063, -0.360103, 0.479817
  0.599916, 0.479741, -0.640273]
k: 21
Α:
[ 8.998800, -0.000244, 0.000000
-0.000244, 3.996590, -0.000000
-0.000000, -0.000000, 1.004607]
Μ:
[\ 0.000328,\ 0.800109,\ 0.599855
 -0.800085, 0.360054, -0.479817
-0.599886, -0.479778, 0.640273]
k: 22
A:
[ 8.998800, -0.000109, 0.000000
 -0.000108, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
[-0.000306, -0.800109, -0.599855
  0.800095, -0.360032, 0.479817
0.599873, 0.479794, -0.640273]
k: 23
Α:
[ 8.998800, -0.000048, 0.000000
 -0.000048, 3.996590, -0.000000
-0.000000, -0.000000, 1.004607]
[\ 0.000296,\ 0.800109,\ 0.599855
 -0.800099, 0.360023, -0.479817
-0.599868, -0.479801, 0.640273]
k: 24
[8.998800, -0.000022, 0.000000
-0.000021, 3.996590, -0.000000
-0.000000, -0.000000, 1.004607]
```

```
[-0.000292, -0.800109, -0.599855

0.800101, -0.360019, 0.479817

0.599865, 0.479804, -0.640273]

k: 25

----

A:

[ 8.998800, -0.000010, 0.000000

-0.000009, 3.996590, -0.000000

-0.000000, -0.000000, 1.004607]

M:

[ 0.000290, 0.800109, 0.599855

-0.800102, 0.360017, -0.479817

-0.599864, -0.479806, 0.640273]

Eigen values: <8.999,3.997,1.005>

Eigen vector 1: <0.000,-0.800,-0.600>

Eigen vector 2: <0.800,0.360,-0.480>

Eigen vector 3: <0.600,-0.480,0.640>
```

2 Interface

```
// ======= PBMATH.H ========
#ifndef PBMATH_H
#define PBMATH_H
// ========= Include ========
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <stdbool.h>
#include <stddef.h>
#include "pberr.h"
#include "pbjson.h"
// ========= Define =========
#define PBMATH_EPSILON 0.00001
#define PBMATH_TWOPI 6.283185307
#define PBMATH_TWOPI_DIV_360 0.01745329252
#define PBMATH_PI 3.141592654
#define PBMATH_HALFPI 1.570796327
#define PBMATH_QUARTERPI 0.7853981634
#define PBMATH_SQRTTWO 1.414213562
#define PBMATH_SQRTONEHALF 0.707106781
#ifndef MAX
 #define MAX(a,b) ((a)>(b)?(a):(b))
#endif
#ifndef MIN
 #define MIN(a,b) ((a)<(b)?(a):(b))
#endif
#define ISEQUALF(a,b) (fabs((a)-(b))<PBMATH_EPSILON)</pre>
#define SHORT(a) ((short)(round(a)))
#define INT(a) ((int)(round(a)))
#define rnd() (float)(rand())/(float)(RAND_MAX)
// ----- VecLong
```

```
// ========= Data structure ==========
// Vector of long values
typedef struct VecLong {
  // Dimension
  long _dim;
// Values
  long _val[0];
} VecLong;
typedef struct VecLong2D {
  // Dimension
  long _dim;
  // Values
  long _val[2];
} VecLong2D;
typedef struct VecLong3D {
  // Dimension
  long _dim;
  // Values
  long _val[3];
} VecLong3D;
typedef struct VecLong4D {
  // Dimension
  long _dim;
  // Values
  long _val[4];
} VecLong4D;
// ====== Functions declaration =========
// Create a new VecLong of dimension 'dim'
// Values are initalized to 0.0
VecLong* VecLongCreate(const long dim);
// Static constructors for VecLong
#if BUILDMODE != 0
static inline
#endif
VecLong2D VecLongCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
VecLong3D VecLongCreateStatic3D();
#if BUILDMODE != 0
static inline
#endif
VecLong4D VecLongCreateStatic4D();
// Clone the VecLong
// Return NULL if we couldn't clone the VecLong
VecLong* _VecLongClone(const VecLong* const that);
// Function which return the JSON encoding of 'that'
JSONNode* _VecLongEncodeAsJSON(const VecLong* const that);
// Function which decode from JSON encoding 'json' to 'that'
bool _VecLongDecodeAsJSON(VecLong** that, const JSONNode* const json);
// Load the VecLong from the stream
```

```
// If the VecLong is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecLongLoad(VecLong** that, FILE* const stream);
// Save the VecLong to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecLongSave(const VecLong* const that,
 FILE* const stream, const bool compact);
// Free the memory used by a VecLong
// Do nothing if arguments are invalid
void _VecLongFree(VecLong** that);
// Print the VecLong on 'stream'
void _VecLongPrint(const VecLong* const that,
 FILE* const stream);
// Return the i-th value of the VecLong
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet(const VecLong* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet2D(const VecLong2D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet3D(const VecLong3D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet4D(const VecLong4D* const that, const long i);
// Set the i-th value of the VecLong to v
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet(VecLong* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet2D(VecLong2D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
\label{thm:const_long} \verb|void_VecLong3D*| const_that, const_long_i, const_long_v); \\
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet4D(VecLong4D* const that, const long i, const long v);
// Set the i-th value of the VecLong to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd(VecLong* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
```

```
void _VecLongSetAdd2D(VecLong2D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd3D(VecLong3D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd4D(VecLong4D* const that, const long i, const long v);
// Return the dimension of the VecLong
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetDim(const VecLong* const that);
// Return the Hamiltonian distance between the VecLong 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist(const VecLong* const that, const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist2D(const VecLong2D* const that, const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist3D(const VecLong3D* const that, const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist4D(const VecLong4D* const that, const VecLong4D* const tho);
// Return true if the VecLong 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecLongIsEqual(const VecLong* const that,
  const VecLong* const tho);
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _VecLongCopy(VecLong* const that, const VecLong* const w);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd(const VecLong* const that,
 const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd2D(const VecLong2D* const that,
 const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
```

```
long _VecLongDotProd3D(const VecLong3D* const that,
  const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd4D(const VecLong4D* const that,
  const VecLong4D* const tho);
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetNull(VecLong* const that);
// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAll(VecLong* const that, long v);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStep(VecLong* const that, const VecLong* const bound);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStep(VecLong* const that, const VecLong* const bound);
// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecLongShiftStep(VecLong* const that,
  const VecLong* const from, const VecLong* const to);
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])</pre>
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStepDelta(VecLong* const that,
  const VecLong* const bound, const VecLong* const delta);
```

```
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStepDelta(VecLong* const that,
  const VecLong* const bound, const VecLong* const delta);
// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp(VecLong* const that, const long a,
  const VecLong* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp2D(VecLong2D* const that, const long a,
  const VecLong2D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp3D(VecLong3D* const that, const long a,
  const VecLong3D* const tho, const long b);
#if BUTLDMODE != 0
static inline
#endif
void _VecLongOp4D(VecLong4D* const that, const long a,
  const VecLong4D* const tho, const long b);
// Return a VecLong equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetOp(const VecLong* const that, const long a,
  const VecLong* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetOp2D(const VecLong2D* const that, const long a,
  const VecLong2D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetOp3D(const VecLong3D* const that, const long a,
  const VecLong3D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetOp4D(const VecLong4D* const that, const long a,
  const VecLong4D* const tho, const long b);
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
```

```
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd(VecLong* const that,
  const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd2D(VecLong2D* const that,
  const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd3D(VecLong3D* const that,
  const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd4D(VecLong4D* const that,
  const VecLong4D* const tho);
// Return a VecLong equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetHadamardProd(const VecLong* const that,
  const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetHadamardProd2D(const VecLong2D* const that,
  const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetHadamardProd3D(const VecLong3D* const that,
  const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetHadamardProd4D(const VecLong4D* const that,
  const VecLong4D* const tho);
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxVal(const VecLong* const that);
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinVal(const VecLong* const that);
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
```

```
long _VecLongGetMaxValAbs(const VecLong* const that);
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinValAbs(const VecLong* const that);
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetIMaxVal(const VecLong* const that);
// ----- VecShort
// ======= Data structure =========
// Vector of short values
typedef struct VecShort {
  // Dimension
  long _dim;
  // Values
  short _val[0];
} VecShort;
typedef struct VecShort2D {
  // Dimension
  long _dim;
  // Values
  short _val[2];
} VecShort2D;
typedef struct VecShort3D {
  // Dimension
  long _dim;
  // Values
  short _val[3];
} VecShort3D;
typedef struct VecShort4D {
 // Dimension
  long _dim;
  // Values
 short _val[4];
} VecShort4D;
// ========= Functions declaration ==========
// Create a new VecShort of dimension 'dim'
// Values are initalized to 0.0
VecShort* VecShortCreate(const long dim);
// Static constructors for VecShort
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecShortCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
```

```
VecShort3D VecShortCreateStatic3D();
#if BUILDMODE != 0
static inline
#endif
VecShort4D VecShortCreateStatic4D();
// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(const VecShort* const that);
// Function which return the JSON encoding of 'that'
JSONNode* _VecShortEncodeAsJSON(const VecShort* const that);
// Function which decode from JSON encoding 'json' to 'that'
bool _VecShortDecodeAsJSON(VecShort** that, const JSONNode* const json);
// Load the VecShort from the stream
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* const stream);
// Save the VecShort to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecShortSave(const VecShort* const that,
 FILE* const stream, const bool compact);
// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that);
// Print the VecShort on 'stream'
void _VecShortPrint(const VecShort* const that,
 FILE* const stream);
// Return the i-th value of the VecShort
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet(const VecShort* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet2D(const VecShort2D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet3D(const VecShort3D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet4D(const VecShort4D* const that, const long i);
// Set the i-th value of the VecShort to v
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet(VecShort* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
```

```
void _VecShortSet2D(VecShort2D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet3D(VecShort3D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet4D(VecShort4D* const that, const long i, const short v);
// Set the i-th value of the VecShort to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd(VecShort* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd2D(VecShort2D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd3D(VecShort3D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd4D(VecShort4D* const that, const long i, const short v);
// Return the dimension of the {\tt VecShort}
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetDim(const VecShort* const that);
// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
#if BUTLDMODE != 0
static inline
#endif
short _VecShortHamiltonDist(const VecShort* const that, const VecShort* const tho);
#if BUILDMODE != 0
static inline
short _VecShortHamiltonDist2D(const VecShort2D* const that, const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist3D(const VecShort3D* const that, const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist4D(const VecShort4D* const that, const VecShort4D* const tho);
// Return true if the VecShort 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
bool _VecShortIsEqual(const VecShort* const that,
  const VecShort* const tho);
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
```

```
static inline
#endif
void _VecShortCopy(VecShort* const that, const VecShort* const w);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd(const VecShort* const that,
 const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd2D(const VecShort2D* const that,
  const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd3D(const VecShort3D* const that,
  const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd4D(const VecShort4D* const that,
  const VecShort4D* const tho);
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetNull(VecShort* const that);
// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAll(VecShort* const that, short v);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* const that, const VecShort* const bound);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* const that, const VecShort* const bound);
// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
```

```
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* const that,
  const VecShort* const from, const VecShort* const to);
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])</pre>
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStepDelta(VecShort* const that,
  const VecShort* const bound, const VecShort* const delta);
// Step the values of the vector incrementally by delta from {\tt 0}
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStepDelta(VecShort* const that,
  const VecShort* const bound, const VecShort* const delta);
// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp(VecShort* const that, const short a,
  const VecShort* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp2D(VecShort2D* const that, const short a,
  const VecShort2D* const tho, const short b);
#if BUILDMODE != 0
static inline
void _VecShortOp3D(VecShort3D* const that, const short a,
  const VecShort3D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp4D(VecShort4D* const that, const short a,
  const VecShort4D* const tho, const short b);
// Return a VecShort equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetOp(const VecShort* const that, const short a,
  const VecShort* const tho, const short b);
#if BUTI.DMODE != 0
static inline
```

```
#endif
VecShort2D _VecShortGetOp2D(const VecShort2D* const that, const short a,
  const VecShort2D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetOp3D(const VecShort3D* const that, const short a,
  const VecShort3D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetOp4D(const VecShort4D* const that, const short a,
  const VecShort4D* const tho, const short b);
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd(VecShort* const that,
 const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd2D(VecShort2D* const that,
  const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd3D(VecShort3D* const that,
  const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd4D(VecShort4D* const that,
  const VecShort4D* const tho);
// Return a VecShort equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetHadamardProd(const VecShort* const that,
  const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetHadamardProd2D(const VecShort2D* const that,
  const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetHadamardProd3D(const VecShort3D* const that,
  const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetHadamardProd4D(const VecShort4D* const that,
  const VecShort4D* const tho);
```

```
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxVal(const VecShort* const that);
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinVal(const VecShort* const that);
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxValAbs(const VecShort* const that);
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinValAbs(const VecShort* const that);
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetIMaxVal(const VecShort* const that);
// ----- VecFloat
// ========= Data structure ==========
// Vector of float values
typedef struct VecFloat {
  // Dimension
 long _dim;
  // Values
  float _val[0];
} VecFloat;
typedef struct VecFloat2D {
  // Dimension
  long _dim;
  // Values
 float _val[2];
} VecFloat2D;
typedef struct VecFloat3D {
  // Dimension
  long _dim;
  // Values
  float _val[3];
} VecFloat3D;
// ======= Functions declaration =========
// Create a new VecFloat of dimension 'dim'
// Values are initalized to 0.0
```

```
VecFloat* VecFloatCreate(const long dim);
// Static constructors for VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecFloatCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecFloatCreateStatic3D();
// Clone the VecFloat
VecFloat* _VecFloatClone(const VecFloat* const that);
// Function which return the JSON encoding of 'that'
JSONNode* _VecFloatEncodeAsJSON(const VecFloat* const that);
// Function which decode from JSON encoding 'json' to 'that'
bool _VecFloatDecodeAsJSON(VecFloat** that, const JSONNode* const json);
// Load the VecFloat from the stream
// If the VecFloat is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecFloatLoad(VecFloat** that, FILE* const stream);
// Save the VecFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecFloatSave(const VecFloat* const that,
  FILE* const stream, const bool compact);
// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that);
// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(const VecFloat* const that, FILE* const stream,
  const unsigned int prec);
static inline void _VecFloatPrintDef(const VecFloat* const that,
  FILE* const stream) {
  VecFloatPrint(that, stream, 3);
// Return the 'i'-th value of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet(const VecFloat* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
{\tt float \_VecFloatGet2D(const\ VecFloat2D*\ const\ that,\ const\ long\ i);}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet3D(const VecFloat3D* const that, const long i);
// Set the 'i'-th value of the VecFloat to 'v'
#if BUILDMODE != 0
```

```
static inline
#endif
void _VecFloatSet(VecFloat* const that, const long i, const float v);
#if BUILDMODE != 0
static inline
#endif
\label{thm:const_long} \verb"void_VecFloatSet2D(VecFloat2D* const that, const long i, const float v); \\
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet3D(VecFloat3D* const that, const long i, const float v);
// Set the 'i'-th value of the VecFloat to 'v' plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd(VecFloat* const that, const long i, const float v);
#if BUILDMODE != 0
#endif
void _VecFloatSetAdd2D(VecFloat2D* const that, const long i,
 const float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd3D(VecFloat3D* const that, const long i,
  const float v);
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull(VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull2D(VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull3D(VecFloat3D* const that);
// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
void _VecFloatSetAll(VecFloat* const that, float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll2D(VecFloat2D* const that, float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll3D(VecFloat3D* const that, float v);
// Return the dimension of the VecFloat
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetDim(const VecFloat* const that);
```

```
// Return a new VecFloat as a copy of the VecFloat 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0.0
// If it is shrinked, values are discarded from the end of the vector
VecFloat* _VecFloatGetNewDim(const VecFloat* const that, const long dim);
// Copy the values of 'w' in 'that' (must have same dimensions)
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void _VecFloatCopy(VecFloat* const that, const VecFloat* const w);
// Return the norm of the VecFloat
// Return 0.0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm(const VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm2D(const VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm3D(const VecFloat3D* const that);
// Normalise the VecFloat
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise(VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise2D(VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise3D(VecFloat3D* const that);
// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist(const VecFloat* const that,
 const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist2D(const VecFloat2D* const that,
 const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
float _VecFloatDist3D(const VecFloat3D* const that,
  const VecFloat3D* const tho);
// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
```

```
static inline
#endif
float _VecFloatHamiltonDist(const VecFloat* const that,
 const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist2D(const VecFloat2D* const that,
 const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist3D(const VecFloat3D* const that,
 const VecFloat3D* const tho);
// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist(const VecFloat* const that,
  const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist2D(const VecFloat2D* const that,
  const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist3D(const VecFloat3D* const that,
  const VecFloat3D* const tho);
// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecFloatIsEqual(const VecFloat* const that,
  const VecFloat* const tho);
// Calculate (that \ast a) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale(VecFloat* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale2D(VecFloat2D* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale3D(VecFloat3D* const that, const float a);
// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0
static inline
VecFloat* _VecFloatGetScale(const VecFloat* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetScale2D(const VecFloat2D* const that,
```

```
const float a);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetScale3D(const VecFloat3D* const that,
  const float a);
// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloat0p(VecFloat* const that, const float a,
  const VecFloat* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp2D(VecFloat2D* const that, const float a,
  const VecFloat2D* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
\verb|void_VecFloatOp3D(VecFloat3D*| const that, const float a,
  const VecFloat3D* const tho, const float b);
// Return a VecFloat equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetOp(const VecFloat* const that, const float a,
  const VecFloat* const tho, const float b);
#if BUILDMODE != 0
static inline
VecFloat2D _VecFloatGetOp2D(const VecFloat2D* const that, const float a,
  const VecFloat2D* const tho, const float b);
#if BUILDMODE != 0
static inline
VecFloat3D _VecFloatGetOp3D(const VecFloat3D* const that, const float a,
  const VecFloat3D* const tho, const float b);
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd(VecFloat* const that,
 const VecFloat* const tho);
#if BUILDMODE != 0
static inline
void _VecFloatHadamardProd2D(VecFloat2D* const that,
  const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
```

```
void _VecFloatHadamardProd3D(VecFloat3D* const that,
  const VecFloat3D* const tho);
// Return a VecFloat equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetHadamardProd(const VecFloat* const that,
 const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetHadamardProd2D(const VecFloat2D* const that,
  const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetHadamardProd3D(const VecFloat3D* const that,
  const VecFloat3D* const tho);
// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRot2D(VecFloat2D* const that, const float theta);
// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetRot2D(const VecFloat2D* const that,
  const float theta);
// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotAxis(VecFloat3D* const that,
  const VecFloat3D* const axis, const float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
VecFloat3D _VecFloatGetRotAxis(const VecFloat3D* const that,
  const VecFloat3D* const axis, const float theta);
// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0
static inline
void _VecFloatRotX(VecFloat3D* const that, const float theta);
// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
```

```
static inline
#endif
void _VecFloatRotY(VecFloat3D* const that, const float theta);
// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotZ(VecFloat3D* const that, const float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(const VecFloat3D* const that,
  const float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(const VecFloat3D* const that,
  const float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Z
VecFloat3D _VecFloatGetRotZ(const VecFloat3D* const that,
 const float theta);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd(const VecFloat* const that,
  const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd2D(const VecFloat2D* const that,
  const VecFloat2D* const tho):
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd3D(const VecFloat3D* const that,
  const VecFloat3D* const tho);
// Return the cross product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetCrossProd(const VecFloat* const that,
 const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetCrossProd3D(const VecFloat3D* const that,
 const VecFloat3D* const tho);
// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
float _VecFloatAngleTo2D(const VecFloat2D* const that,
  const VecFloat2D* const tho);
// Return the conversion of VecFloat 'that' to a VecShort using round()
```

```
#if BUILDMODE != 0
static inline
#endif
VecShort* VecFloatToShort(const VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecFloatToShort2D(const VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecFloatToShort3D(const VecFloat3D* const that);
// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecShortToFloat(const VecShort* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecShortToFloat2D(const VecShort2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecShortToFloat3D(const VecShort3D* const that);
// Return the conversion of VecLong 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecLongToFloat(const VecLong* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecLongToFloat2D(const VecLong2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecLongToFloat3D(const VecLong3D* const that);
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxVal(const VecFloat* const that);
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinVal(const VecFloat* const that);
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxValAbs(const VecFloat* const that);
// Get the min value (in absolute value) in components of the
// vector 'that'
```

```
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinValAbs(const VecFloat* const that);
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* const that,
  const VecFloat* const bound, const VecFloat* const delta);
// Step the values of the vector incrementally by delta
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* const that,
  const VecFloat* const from, const VecFloat* const to,
  const VecFloat* const delta);
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetIMaxVal(const VecFloat* const that);
// Return a set of two vectors containing the bounds of the vectors in
// the GSet 'that'
// The set must have at least one element
// The returned set is ordered as follow: (boundMin, boundMax)
GSetVecFloat _GSetVecFloatGetBounds(const GSetVecFloat* const that);
// ----- MatFloat
// ======= Data structure ========
// Vector of float values
typedef struct MatFloat {
  // Dimension (nbCol, nbLine)
  const VecShort2D _dim;
  // Values (memorized by lines)
  float _val[0];
} MatFloat;
// Simple pod to hold the result of a QR decomposition
typedef struct QRDecomp {
  MatFloat* _Q;
  MatFloat* _R;
} QRDecomp;
// ====== Functions declaration =========
// Free memory used by the QRDecomp 'that'
```

```
#if BUILDMODE != 0
static inline
#endif
void QRDecompFreeStatic(QRDecomp* const that);
// Create a new MatFloat of dimension 'dim' (nbCol, nbLine)
// Values are initalized to 0.0
MatFloat* MatFloatCreate(const VecShort2D* const dim);
// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSetIdentity(MatFloat* const that);
// Clone the MatFloat
MatFloat* _MatFloatClone(const MatFloat* const that);
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _MatFloatCopy(MatFloat* const that, const MatFloat* const tho);
// Function which return the JSON encoding of 'that'
JSONNode* _MatFloatEncodeAsJSON(MatFloat* const that);
// Function which decode from JSON encoding 'json' to 'that'
bool _MatFloatDecodeAsJSON(MatFloat** that, JSONNode* json);
// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream);
// Save the MatFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true upon success, else false
bool _MatFloatSave(MatFloat* const that, FILE* stream, bool compact);
// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that);
// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* const that, FILE* stream, unsigned int prec);
static inline void _MatFloatPrintlnDef(MatFloat* const that, FILE* stream) {
 MatFloatPrintln(that, stream, 3);
// Return the value at index (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
float _MatFloatGet(const MatFloat* const that,
  VecShort2D* index);
// Set the value at index (col, line) of the MatFloat to 'v'
```

```
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSet(MatFloat* const that, VecShort2D* index, float v);
// Return the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
const VecShort2D* _MatFloatDim(const MatFloat* const that);
// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
VecShort2D _MatFloatGetDim(const MatFloat* const that);
// Return the number of rows of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbRow(const MatFloat* const that);
// Return the number of columns of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbCol(const MatFloat* const that);
// Return the inverse matrix of 'that'
// The matrix must be a square matrix
// Return NULL if the matrix is not invertible, or in some case when
// the matrix's diagonal contains null values and the matrix's size
// is greater than 3
MatFloat* _MatFloatGetInv(const MatFloat* const that);
// Return the product of matrix 'that' and vector 'v'
// Number of columns of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(
 const MatFloat* const that, const VecFloat* v);
// Return the product of vector 'v' and transpose of vector 'w'
MatFloat* _MatFloatGetProdVecVecTransposeFloat(
  const VecFloat* const v,
 const VecFloat* const w);
// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(const MatFloat* const that, const MatFloat* tho);
// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
MatFloat* _MatFloatGetAdd(MatFloat* const that, MatFloat* tho);
// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
```

```
#endif
void _MatFloatAdd(MatFloat* const that, MatFloat* tho);
// Multiply the matrix 'that' by 'a'
#if BUILDMODE != 0
static inline
#endif
void _MatFloatScale(MatFloat* const that, const float a);
// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* const that, MatFloat* tho);
// Calculate the Eigen values and vectors of the MatFloat 'that'
// Return a set of VecFloat. The first VecFloat of the set contains
// the Eigen values, with values sorted from biggest to
// smallest (in absolute value). The following VecFloat are the
// respectiev Eigen vectors
// 'that' must be a 2D square matrix
// Return the identity if the QR decompostion fails
// http://madrury.github.io/jekyll/update/statistics/2017/10/04/qr-algorithm.html
// TODO: should be improved with the Hessenberg QR method
// https://www.math.kth.se/na/SF2524/matber15/qrmethod.pdf
GSetVecFloat _MatFloatGetEigenValues(const MatFloat* const that);
// Calculate the QR decomposition of the MatFloat 'that' using the
// Householder algorithm
// Return {NULL, NULL} if the MatFloat couldn't be decomposed
// http://www.seas.ucla.edu/~vandenbe/133A/lectures/qr.pdf
QRDecomp _MatFloatGetQR(const MatFloat* const that);
// Calculate the transposed of the MatFloat 'that'
MatFloat* _MatFloatGetTranspose(const MatFloat* const that);
// ---- Gauss
// ====== Define ========
// ====== Data structure =========
// Should be vector of float values
typedef struct Gauss {
  // Mean
  float _mean;
  // Sigma
  float _sigma;
} Gauss;
// ======== Functions declaration ==========
// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(const float mean, const float sigma);
Gauss GaussCreateStatic(const float mean, const float sigma);
// Free the memory used by a Gauss
// Do nothing if arguments are invalid
void GaussFree(Gauss** that);
// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
static inline
#endif
```

```
float GaussGet(const Gauss* const that, const float x);
// Return a random value according to the Gauss 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
static inline
#endif
float GaussRnd(Gauss* const that);
// ----- Smoother
// ========= Define =========
// ====== Data structure =========
// ======= Functions declaration =========
// Return the order 1 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmoothStep(const float x);
// Return the order 2 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmootherStep(const float x);
// ----- Conversion functions
// ======= Functions declaration =========
// Convert radians to degrees
static inline float ConvRad2Deg(const float rad) {
 return rad / PBMATH_TWOPI_DIV_360;
// Convert degrees to radians
static inline float ConvDeg2Rad(const float deg) {
 return PBMATH_TWOPI_DIV_360 * deg;
// ----- SysLinEq
// ====== Data structure =========
// Linear system of equalities
typedef struct SysLinEq {
 // Matrix
 MatFloat* _M;
 \ensuremath{//} Inverse of the matrix
 MatFloat* _Minv;
 // Vector
 VecFloat* _V;
} SysLinEq;
// ======= Functions declaration ===========
```

```
// Create a new SysLinEq with matrix 'm' and vector 'v'
// The dimension of 'v' must be equal to the number of column of 'm'
// If 'v' is null the vector null is used instead
// The matrix 'm' must be a square matrix
// Return NULL if we couldn't create the SysLinEq
{\tt SysLinEq*\_SLECreate(const~MatFloat*~const~m,~const~VecFloat*~const~v);}
// Free the memory used by the SysLinEq
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that);
// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(const SysLinEq* const that);
// Solve the SysLinEq _M.x = _V
// Return the solution vector, or null if there is no solution or the
// arguments are invalid
#if BUILDMODE != 0
static inline
#endif
VecFloat* SysLinEqSolve(const SysLinEq* const that);
// Set the matrix of the SysLinEq to a clone of 'm'
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void SysLinEqSetM(SysLinEq* const that, const MatFloat* const m);
// Set the vector of the SysLinEq to a clone of 'v'
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void _SLESetV(SysLinEq* const that, const VecFloat* const v);
// ----- Ratio
// ========= Data structure ==========
// Linear system of equalities
typedef struct Ratio {
  // Components
  long _base;
  unsigned int _numerator;
  unsigned int _denominator;
} Ratio;
// ====== Functions declaration =======
// Create a new static Ratio
Ratio RatioCreateStatic(long b, unsigned int n, unsigned int d);
// Convert the float 'v' into the nearest Ratio using the Farey's algorithm
// given the precision 'prec'
Ratio RatioFromFloatPrec(float v, float prec);
\verb|#define RatioFromFloat(v) RatioFromFloatPrec((v), PBMATH_EPSILON)|\\
```

```
// Convert the Ratio 'that' into a float
float RatioToFloat(const Ratio* that);
// Reduce the fractional part of the Ratio 'that' and update the base such as
// numerator < denominator</pre>
void RatioReduce(Ratio* that);
// Get the base of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
long RatioGetBase(const Ratio* that);
// Get the numerator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetNumerator(const Ratio* that);
// Get the denominator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetDenominator(const Ratio* that);
// Set the base of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetBase(Ratio* that, long v);
// Set the numerator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetNumerator(Ratio* that, unsigned int v);
// Set the denominator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetDenominator(Ratio* that, unsigned int v);
// Print the Ratio on 'stream' as a+b/c
void RatioPrint(const Ratio* that, FILE* stream);
#define RatioPrintln(R, S) do{RatioPrint(R,S);fprintf(S,"\n");}while(0)
// ----- LeastSquareLinReg
// ----- Data structure -----
// Linear system of equalities
typedef struct LeastSquareLinReg {
  // Component
  const MatFloat* X;
  // Matrix for computation
  MatFloat* Xp;
  // Bias of the last computed solution
  float bias;
```

```
} LeastSquareLinReg;
// ========= Functions declaration =========
// Create a new static LeastSquareLinReg
LeastSquareLinRegCreateStatic({\tt MatFloat*~X});\\
// Free the static LeastSquareLinReg 'that'
void LeastSquareLinRegFreeStatic(LeastSquareLinReg* that);
// Compute the solution of the LeastSquareLinReg 'that' for 'Y'
VecFloat* LSLRSolve(LeastSquareLinReg* that, const VecFloat* Y);
// Set the component of the LeastSquareLinReg 'that' to 'X'
#if BUILDMODE != 0
static inline
#endif
void LSLRSetComp(LeastSquareLinReg* that, const MatFloat* X);
// Get the bias of the last computed solution of the LeastSquareLinReg 'that'
#if BUILDMODE != 0
static inline
#endif
float LSLRGetBias(const LeastSquareLinReg* that);
// Return true if the LeastSquareLinReg 'that' is solvable
#if BUILDMODE != 0
static inline
#endif
bool LSLRIsSolvable(const LeastSquareLinReg* that);
// ----- Usefull basic functions
// ======== Functions declaration ==========
// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/
// does-pow-work-for-int-data-type-in-c
#if BUILDMODE != 0
static inline
#endif
int powi(const int base, const int exp);
// Compute a^n, faster than std::pow for n<~100
static inline float fastpow(const float a, const int n) { }
  double ret = 1.0;
  double b = a;
  for (int i = n; i--;) ret *= b;
 return (float)ret;
// Compute a^2
static inline float fsquare(const float a) {
 return a * a;
// Compute the 'iElem'-th element of the 'base'-ary version of the
// Thue-Morse sequence
// 'iElem' >= 0
// 'base' >= 2
```

```
long ThueMorseSeqGetNthElem(long iElem, long base);
// Compute the area of a triangle knowing its 3 sides length 'a', 'b', 'c'
// using the Hero's formula
double GetAreaTriangleHero(
  const double a,
  const double b.
  const double c);
// Return the Fibonacci sequence up to the 'n'-th element in a dynamically
// allocated array of unsigned long
unsigned long* GetFibonacciSeq(unsigned int n);
// Return the Fibonacci grid lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [0,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciGridLattice(
    unsigned int n,
  unsigned long* nbPoints);
// Return the Fibonacci polar lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [-1,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciPolarLattice(
    unsigned int n,
  unsigned long* nbPoints);
// Return the greatest common divisor using the Stein's algorithm
// https://en.wikipedia.org/wiki/Binary_GCD_algorithm
unsigned int GetGCD(unsigned int u, unsigned int v);
// ========= Polymorphism =========
#define VecClone(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatClone, \
  VecShort*: _VecShortClone, \
  VecLong*: _VecLongClone, \
  const VecFloat*: _VecFloatClone, \
  const VecShort*: _VecShortClone, \
  const VecLong*: _VecLongClone, \
  default: PBErrInvalidPolymorphism)(Vec)
#define VecEncodeAsJSON(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatEncodeAsJSON, \
VecShort*: _VecShortEncodeAsJSON, \
  VecLong*: _VecLongEncodeAsJSON, \
  const VecShort*: _VecShortEncodeAsJSON, \
  const VecLong*: _VecLongEncodeAsJSON, \
  default: PBErrInvalidPolymorphism)(Vec)
#define VecDecodeAsJSON(VecRef, Json) _Generic(VecRef, \
  VecFloat**: _VecFloatDecodeAsJSON, \
  VecShort**: _VecShortDecodeAsJSON, \
  VecLong**: _VecLongDecodeAsJSON, \
  default: PBErrInvalidPolymorphism)(VecRef, Json)
#define VecLoad(VecRef, Stream) _Generic(VecRef, \
  VecFloat**: _VecFloatLoad, \
  VecShort**: _VecShortLoad, \
VecLong**: _VecLongLoad, \
  default: PBErrInvalidPolymorphism) (VecRef, Stream)
```

```
#define VecSave(Vec, Stream, Compact) _Generic(Vec, \
  VecFloat*: _VecFloatSave, \
 {\tt VecFloat2D*: \_VecFloatSave, \ } \\
 VecFloat3D*: _VecFloatSave, \
  VecShort*: _VecShortSave, \
  VecShort2D*: _VecShortSave, \
  VecShort3D*: _VecShortSave, \
  VecShort4D*: _VecShortSave, \
  VecLong*: _VecLongSave, \
  VecLong2D*: _VecLongSave, \
 VecLong3D*: _VecLongSave, \
VecLong4D*: _VecLongSave, \
 const VecFloat*: _VecFloatSave, \
 const VecFloat2D*: _VecFloatSave, \
const VecFloat3D*: _VecFloatSave, \
 const VecShort*: _VecShortSave, \
  const VecShort2D*: _VecShortSave, \
  const VecShort3D*: _VecShortSave, \
  const VecShort4D*: _VecShortSave, \
  const VecLong*: _VecLongSave, \
 const VecLong2D*: _VecLongSave, \
const VecLong3D*: _VecLongSave, \
  const VecLong4D*: _VecLongSave, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat2D*: (const VecFloat*)(Vec), \
      VecFloat3D*: (const VecFloat*)(Vec), \
      VecShort2D*: (const VecShort*)(Vec), \
      VecShort3D*: (const VecShort*)(Vec), \
      VecShort4D*: (const VecShort*)(Vec), \
      VecLong2D*: (const VecLong*)(Vec), \
      VecLong3D*: (const VecLong*)(Vec), \
      VecLong4D*: (const VecLong*)(Vec), \
      const VecFloat2D*: (const VecFloat*)(Vec), \
      const VecFloat3D*: (const VecFloat*)(Vec), \
      const VecShort2D*: (const VecShort*)(Vec), \
      const VecShort3D*: (const VecShort*)(Vec), \
      const VecShort4D*: (const VecShort*)(Vec), \
      const VecLong2D*: (const VecLong*)(Vec), \
      const VecLong3D*: (const VecLong*)(Vec), \
      const VecLong4D*: (const VecLong*)(Vec), \
      default: Vec), \
    Stream, Compact)
#define VecFree(VecRef) _Generic(VecRef, \
  VecFloat**: _VecFloatFree, \
  VecShort**: _VecShortFree, \
  VecLong**: _VecLongFree, \
 default: PBErrInvalidPolymorphism)(VecRef)
#define VecPrint(Vec, Stream) _Generic(Vec, \
 VecFloat*: _VecFloatPrintDef, \
  VecFloat2D*: _VecFloatPrintDef, \
 VecFloat3D*: _VecFloatPrintDef, \
  VecShort*: _VecShortPrint, \
  VecShort2D*: _VecShortPrint, \
  VecShort3D*: _VecShortPrint, \
  VecShort4D*: _VecShortPrint, \
  VecLong*: _VecLongPrint, \
  VecLong2D*: _VecLongPrint, \
  VecLong3D*: _VecLongPrint, \
```

```
VecLong4D*: _VecLongPrint, \
  const VecFloat*: _VecFloatPrintDef, \
  const VecFloat3D*: _VecFloatPrintDef, \
  const VecShort*: _VecShortPrint, \
 const VecShort2D*: _VecShortPrint, \
const VecShort3D*: _VecShortPrint, \
  const VecShort4D*: _VecShortPrint, \
  const VecLong*: _VecLongPrint, \
  const VecLong2D*: _VecLongPrint, \
  const VecLong3D*: _VecLongPrint, \
  const VecLong4D*: _VecLongPrint, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat2D*: (const VecFloat*)(Vec), \
      VecFloat3D*: (const VecFloat*)(Vec), \
      VecShort2D*: (const VecShort*)(Vec), \
      VecShort3D*: (const VecShort*)(Vec), \
      VecShort4D*: (const VecShort*)(Vec), \
      VecLong2D*: (const VecLong*)(Vec), \
      VecLong3D*: (const VecLong*)(Vec), \
      VecLong4D*: (const VecLong*)(Vec), \
      const VecFloat2D*: (const VecFloat*)(Vec), \
      const VecFloat3D*: (const VecFloat*)(Vec), \
      const VecShort2D*: (const VecShort*)(Vec), \
      const VecShort3D*: (const VecShort*)(Vec), \
      const VecShort4D*: (const VecShort*)(Vec), \
      const VecLong2D*: (const VecLong*)(Vec), \
      const VecLong3D*: (const VecLong*)(Vec), \
      const VecLong4D*: (const VecLong*)(Vec), \
      default: Vec), \
    Stream)
#define VecPrintln(V, S) do {VecPrint(V, S); fprintf(S, "\n");} while(0)
#define VecGet(Vec, Index) _Generic(Vec, \
 VecFloat*: _VecFloatGet, \
  VecFloat2D*: _VecFloatGet2D, \
 VecFloat3D*: _VecFloatGet3D, \
 VecShort*: _VecShortGet, \
  VecShort2D*: _VecShortGet2D, \
 VecShort3D*: _VecShortGet3D, \
  VecShort4D*: _VecShortGet4D, \
  VecLong*: _VecLongGet, \
  VecLong2D*: _VecLongGet2D, \
  VecLong3D*: _VecLongGet3D, \
  VecLong4D*: _VecLongGet4D, \
  const VecFloat*: _VecFloatGet, \
 const VecFloat2D*: _VecFloatGet2D, \
  const VecFloat3D*: _VecFloatGet3D, \
  const VecShort*: _VecShortGet, \
 const VecShort2D*: _VecShortGet2D, \
  const VecShort3D*: _VecShortGet3D, \
  const VecShort4D*: _VecShortGet4D, \
  const VecLong*: _VecLongGet, \
  const VecLong2D*: _VecLongGet2D, \
 const VecLong3D*: _VecLongGet3D, \
const VecLong4D*: _VecLongGet4D, \
  default: PBErrInvalidPolymorphism)(Vec, Index)
#define VecSet(Vec, Index, Val) _Generic(Vec, \
  VecFloat*: _VecFloatSet, \
```

```
VecFloat2D*: _VecFloatSet2D, \
  VecFloat3D*: _VecFloatSet3D, \
  VecShort*: _VecShortSet, \
 VecShort2D*: _VecShortSet2D, \
  VecShort3D*: _VecShortSet3D, \
  VecShort4D*: _VecShortSet4D, \
  VecLong*: _VecLongSet, \
  VecLong2D*: _VecLongSet2D, \
 VecLong3D*: _VecLongSet3D, \
VecLong4D*: _VecLongSet4D, \
  default: PBErrInvalidPolymorphism)(Vec, Index, Val)
#define VecSetAdd(Vec, Index, Val) _Generic(Vec, \
  VecFloat*: _VecFloatSetAdd, \
  VecFloat2D*: _VecFloatSetAdd2D, \
 VecFloat3D*: _VecFloatSetAdd3D, \
 VecShort*: _VecShortSetAdd, \
 VecShort2D*: _VecShortSetAdd2D, \
  VecShort3D*: _VecShortSetAdd3D, \
  VecShort4D*: _VecShortSetAdd4D, \
  VecLong*: _VecLongSetAdd, \
  VecLong2D*: _VecLongSetAdd2D, \
 VecLong3D*: _VecLongSetAdd3D, \
 VecLong4D*: _VecLongSetAdd4D, \
 default: PBErrInvalidPolymorphism)(Vec, Index, Val)
#define VecSetNull(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatSetNull, \
  VecFloat2D*: _VecFloatSetNull, \
  VecFloat3D*: _VecFloatSetNull, \
 VecShort*: _VecShortSetNull, \
 VecShort2D*: _VecShortSetNull, \
  VecShort3D*: _VecShortSetNull, \
  VecShort4D*: _VecShortSetNull, \
  VecLong*: _VecLongSetNull, \
  VecLong2D*: _VecLongSetNull, \
 VecLong3D*: _VecLongSetNull, \
VecLong4D*: _VecLongSetNull, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
VecFloat2D*: (VecFloat*)(Vec), \
      VecFloat3D*: (VecFloat*)(Vec), \
      VecShort2D*: (VecShort*)(Vec), \
      VecShort3D*: (VecShort*)(Vec), \
      VecShort4D*: (VecShort*)(Vec), \
      VecLong2D*: (VecLong*)(Vec), \
      VecLong3D*: (VecLong*)(Vec), \
VecLong4D*: (VecLong*)(Vec), \
      default: Vec))
#define VecSetAll(Vec, Val) _Generic(Vec, \
 VecFloat*: _VecFloatSetAll, \
  VecFloat2D*: _VecFloatSetAll, \
  VecFloat3D*: _VecFloatSetAll, \
 VecShort*: _VecShortSetAll, \
  VecShort2D*: _VecShortSetAll, \
 VecShort3D*: _VecShortSetAll, \
VecShort4D*: _VecShortSetAll, \
  VecLong*: _VecLongSetAll, \
 VecLong2D*: _VecLongSetAll, \
VecLong3D*: _VecLongSetAll, \
  VecLong4D*: _VecLongSetAll, \
```

```
default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat2D*: (VecFloat*)(Vec), \
      VecFloat3D*: (VecFloat*)(Vec), \
      VecShort2D*: (VecShort*)(Vec), \
      VecShort3D*: (VecShort*)(Vec), \
      VecShort4D*: (VecShort*)(Vec), \
      VecLong2D*: (VecLong*)(Vec), \
      VecLong3D*: (VecLong*)(Vec), \
      VecLong4D*: (VecLong*)(Vec), \
      default: Vec), Val)
#define VecCopy(VecDest, VecSrc) _Generic(VecDest, \
  VecFloat*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat2D*: _VecFloatCopy, \
    VecFloat3D*: _VecFloatCopy, \
    const VecFloat*: _VecFloatCopy, \
   const VecFloat2D*: _VecFloatCopy, \
const VecFloat3D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecFloat2D*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat2D*: _VecFloatCopy, \
    const VecFloat*: _VecFloatCopy, \
    const VecFloat2D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecFloat3D*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat3D*: _VecFloatCopy, \
    const VecFloat*: _VecFloatCopy, \
    const VecFloat3D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort2D*: _VecShortCopy, \
    VecShort3D*: _VecShortCopy, \
    VecShort4D*: _VecShortCopy, \
    const VecShort*: _VecShortCopy, \
    const VecShort3D*: _VecShortCopy, \
const VecShort4D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecSrc, \
  VecShort*: _VecShortCopy, \
    VecShort2D*: _VecShortCopy, \
    const VecShort*: _VecShortCopy, \
    const VecShort2D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort3D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort3D*: _VecShortCopy, \
    const VecShort*: _VecShortCopy, \
    const VecShort3D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort4D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort4D*: _VecShortCopy, \
    const VecShort*: _VecShortCopy, \
    const VecShort4D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecLong*: _Generic(VecSrc, \
```

```
VecLong*: _VecLongCopy, \
    VecLong2D*: _VecLongCopy, \
    VecLong3D*: _VecLongCopy, \
VecLong4D*: _VecLongCopy, \
    \begin{tabular}{ll} \hline \tt const & \bar{\tt VecLong*: \_VecLongCopy, $\setminus$} \\ \hline \end{tabular}
    const VecLong2D*: _VecLongCopy, \
const VecLong3D*: _VecLongCopy, \
    const VecLong4D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
  VecLong2D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong2D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong2D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
  VecLong3D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong3D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong3D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
  VecLong4D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong4D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong4D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)( \
    _Generic(VecDest, \
      VecFloat2D*: (VecFloat*)(VecDest), \
      VecFloat3D*: (VecFloat*)(VecDest), \
      VecShort2D*: (VecShort*)(VecDest), \
      VecShort3D*: (VecShort*)(VecDest), \
      VecShort4D*: (VecShort*)(VecDest), \
      VecLong2D*: (VecLong*)(VecDest), \
      VecLong3D*: (VecLong*)(VecDest), \
      VecLong4D*: (VecLong*)(VecDest), \
      default: VecDest),
    _Generic(VecSrc, \
      VecFloat2D*: (const VecFloat*)(VecSrc), \
      VecFloat3D*: (const VecFloat*)(VecSrc), \
      VecShort2D*: (const VecShort*)(VecSrc), \
      VecShort3D*: (const VecShort*)(VecSrc), \
      VecShort4D*: (const VecShort*)(VecSrc), \
      VecLong2D*: (const VecLong*)(VecSrc), \
      VecLong3D*: (const VecLong*)(VecSrc), \
      VecLong4D*: (const VecLong*)(VecSrc), \
      const VecFloat2D*: (const VecFloat*)(VecSrc), \
      const VecFloat3D*: (const VecFloat*)(VecSrc), \
      const VecShort2D*: (const VecShort*)(VecSrc), \
      const VecShort3D*: (const VecShort*)(VecSrc), \
      const VecShort4D*: (const VecShort*)(VecSrc), \
      const VecLong2D*: (const VecLong*)(VecSrc), \
      const VecLong3D*: (const VecLong*)(VecSrc), \
      const VecLong4D*: (const VecLong*)(VecSrc), \
      default: VecSrc))
#define VecGetDim(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatGetDim, \
  VecFloat2D*: _VecFloatGetDim, \
  VecFloat3D*: _VecFloatGetDim, \
  VecShort*: _VecShortGetDim, \
```

```
VecShort2D*: _VecShortGetDim, \
  VecShort3D*: _VecShortGetDim, \
  VecShort4D*: _VecShortGetDim, \
  VecLong*: _VecLongGetDim, \
  VecLong2D*: _VecLongGetDim, \
 VecLong3D*: _VecLongGetDim, \
VecLong4D*: _VecLongGetDim, \
  const VecFloat*: _VecFloatGetDim, \
 const VecFloat2D*: _VecFloatGetDim, \
const VecFloat3D*: _VecFloatGetDim, \
  const VecShort*: _VecShortGetDim, \
 const VecShort2D*: _VecShortGetDim, \
const VecShort3D*: _VecShortGetDim, \
  const VecShort4D*: _VecShortGetDim, \
  const VecLong*: _VecLongGetDim, \
  const VecLong2D*: _VecLongGetDim, \
  const VecLong3D*: _VecLongGetDim, \
  const VecLong4D*: _VecLongGetDim, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat*: (const VecFloat*)(Vec), \
      VecFloat2D*: (const VecFloat*)(Vec), \
      VecFloat3D*: (const VecFloat*)(Vec), \
      VecShort*: (const VecShort*)(Vec), \
      VecShort2D*: (const VecShort*)(Vec), \
      VecShort3D*: (const VecShort*)(Vec), \
      VecShort4D*: (const VecShort*)(Vec), \
      VecLong*: (const VecLong*)(Vec), \
      VecLong2D*: (const VecLong*)(Vec), \
      VecLong3D*: (const VecLong*)(Vec), \
      VecLong4D*: (const VecLong*)(Vec), \
      const VecFloat2D*: (const VecFloat*)(Vec), \
      const VecFloat3D*: (const VecFloat*)(Vec), \
      const VecShort2D*: (const VecShort*)(Vec), \
      const VecShort3D*: (const VecShort*)(Vec), \
      const VecShort4D*: (const VecShort*)(Vec), \
      const VecLong2D*: (const VecLong*)(Vec), \
      const VecLong3D*: (const VecLong*)(Vec), \
      const VecLong4D*: (const VecLong*)(Vec), \
      default: Vec))
#define VecGetNewDim(Vec, Dim) _Generic(Vec, \
  VecFloat*: _VecFloatGetNewDim, \
  const VecFloat*: _VecFloatGetNewDim, \
 default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat*: Vec, \
      const VecFloat*: Vec, \
      default: Vec), Dim)
#define VecNorm(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatNorm, \
  VecFloat2D*: _VecFloatNorm2D, \
 VecFloat3D*: _VecFloatNorm3D, \
 const VecFloat*: _VecFloatNorm, \
  const VecFloat2D*: _VecFloatNorm2D, \
  const VecFloat3D*: _VecFloatNorm3D, \
 default: PBErrInvalidPolymorphism)(Vec)
#define VecNormalise(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatNormalise, \
  VecFloat2D*: _VecFloatNormalise2D, \
```

```
VecFloat3D*: _VecFloatNormalise3D, \
 default: PBErrInvalidPolymorphism)(Vec)
#define VecDist(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatDist, \
   const VecFloat*: _VecFloatDist, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatDist2D, \
   const VecFloat2D*: _VecFloatDist2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatDist3D, \
   const VecFloat3D*: _VecFloatDist3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHamiltonDist,\
   const VecShort*: _VecShortHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHamiltonDist2D,\
   const VecShort2D*: _VecShortHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortHamiltonDist3D,\
   const VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   const VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 VecLong*: _Generic(VecB, \
   VecLong*: _VecLongHamiltonDist,\
   const VecLong*: _VecLongHamiltonDist,\
   {\tt default:\ PBErrInvalidPolymorphism),\ } \\
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongHamiltonDist2D,\
   const VecLong2D*: _VecLongHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongHamiltonDist3D,\
   const VecLong3D*: _VecLongHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongHamiltonDist4D,\
   const VecLong4D*: _VecLongHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 const VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatDist, \
   const VecFloat*: _VecFloatDist, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatDist2D, \
   const VecFloat2D*: _VecFloatDist2D, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatDist3D, \
   const VecFloat3D*: _VecFloatDist3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHamiltonDist,\
```

```
const VecShort*: _VecShortHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 const VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHamiltonDist2D,\
   const VecShort2D*: _VecShortHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 const VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortHamiltonDist3D,\
   const VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 const VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   const VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong*: _Generic(VecB, \
   VecLong*: _VecLongHamiltonDist,\
   const VecLong*: _VecLongHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 const VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongHamiltonDist2D,\
   const VecLong2D*: _VecLongHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongHamiltonDist3D,\
   const VecLong3D*: _VecLongHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongHamiltonDist4D,\
   const VecLong4D*: _VecLongHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecHamiltonDist(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatHamiltonDist, \
   const VecFloat*: _VecFloatHamiltonDist, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatHamiltonDist2D, \
   \verb|const VecFloat2D*: _VecFloatHamiltonDist2D, \\ \\ \\ \\ \\ \\
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatHamiltonDist3D, \
   const VecFloat3D*: _VecFloatHamiltonDist3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHamiltonDist,\
   const VecShort*: _VecShortHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHamiltonDist2D,\
   const VecShort2D*: _VecShortHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortHamiltonDist3D,\
   const VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   const VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 VecLong*: _Generic(VecB, \
```

```
VecLong*: _VecLongHamiltonDist,\
   const VecLong*: _VecLongHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongHamiltonDist2D,\
   const VecLong2D*: _VecLongHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongHamiltonDist3D,\
   const VecLong3D*: _VecLongHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongHamiltonDist4D,\
   const VecLong4D*: _VecLongHamiltonDist4D,\
   {\tt default:\ PBErrInvalidPolymorphism),\ } \\
 const VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatHamiltonDist, \
   const VecFloat*: _VecFloatHamiltonDist, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatHamiltonDist2D, \
   const VecFloat2D*: _VecFloatHamiltonDist2D, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatHamiltonDist3D, \
   const VecFloat3D*: _VecFloatHamiltonDist3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHamiltonDist,\
   const VecShort*: _VecShortHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 const VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHamiltonDist2D,\
   const VecShort2D*: _VecShortHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 const VecShort3D*: Generic(VecB. \
   VecShort3D*: _VecShortHamiltonDist3D,\
   const VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 const VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   const VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong*: _Generic(VecB, \
   VecLong*: _VecLongHamiltonDist,\
   const VecLong*: _VecLongHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 const VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongHamiltonDist2D,\
   const VecLong2D*: _VecLongHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongHamiltonDist3D,\
   const VecLong3D*: _VecLongHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 const VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongHamiltonDist4D,\
   const VecLong4D*: _VecLongHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecPixelDist(VecA, VecB) _Generic(VecA, \
```

```
VecFloat*: _Generic(VecB, \
 VecFloat*: _VecFloatPixelDist, \
 const VecFloat*: _VecFloatPixelDist, \
 default: PBErrInvalidPolymorphism), \
VecFloat2D*: _Generic(VecB, \
 VecFloat2D*: _VecFloatPixelDist2D, \
 const VecFloat2D*: _VecFloatPixelDist2D, \
 default: PBErrInvalidPolymorphism), \
VecFloat3D*: _Generic(VecB, \
 VecFloat3D*: _VecFloatPixelDist3D, \
 const VecFloat3D*: _VecFloatPixelDist3D, \
 default: PBErrInvalidPolymorphism), \
VecShort*: _Generic(VecB, \
 VecShort*: _VecShortHamiltonDist,\
 const VecShort*: _VecShortHamiltonDist,\
 default: PBErrInvalidPolymorphism), \
VecShort2D*: _Generic(VecB, \
 VecShort2D*: _VecShortHamiltonDist2D,\
 const VecShort2D*: _VecShortHamiltonDist2D,\
 default: PBErrInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
 VecShort3D*: _VecShortHamiltonDist3D,\
 const VecShort3D*: _VecShortHamiltonDist3D,\
 default: PBErrInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
 VecShort4D*: _VecShortHamiltonDist4D,\
 const VecShort4D*: _VecShortHamiltonDist4D,\
 default: PBErrInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
 VecLong*: _VecLongHamiltonDist,\
 const VecLong*: _VecLongHamiltonDist,\
 default: PBErrInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
 VecLong2D*: _VecLongHamiltonDist2D,\
 const VecLong2D*: _VecLongHamiltonDist2D,\
 {\tt default:\ PBErrInvalidPolymorphism),\ } \\
VecLong3D*: _Generic(VecB, \
 VecLong3D*: _VecLongHamiltonDist3D,\
 const VecLong3D*: _VecLongHamiltonDist3D,\
 default: PBErrInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
 VecLong4D*: _VecLongHamiltonDist4D,\
 const VecLong4D*: _VecLongHamiltonDist4D,\
 default: PBErrInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
 VecFloat*: _VecFloatPixelDist, \
 const VecFloat*: _VecFloatPixelDist, \
 default: PBErrInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
 VecFloat2D*: _VecFloatPixelDist2D, \
 const VecFloat2D*: _VecFloatPixelDist2D, \
 default: PBErrInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
 VecFloat3D*: _VecFloatPixelDist3D, \
 const VecFloat3D*: _VecFloatPixelDist3D, \
 default: PBErrInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
 VecShort*: _VecShortHamiltonDist,\
 const VecShort*: _VecShortHamiltonDist,\
 default: PBErrInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
 VecShort2D*: _VecShortHamiltonDist2D,\
```

```
const VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErrInvalidPolymorphism), \
  const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    const VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErrInvalidPolymorphism), \
  const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    const VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErrInvalidPolymorphism), \
  const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHamiltonDist,\
    const VecLong*: _VecLongHamiltonDist,\
    default: PBErrInvalidPolymorphism), \
  const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHamiltonDist2D,\
    const VecLong2D*: _VecLongHamiltonDist2D,\
    default: PBErrInvalidPolymorphism), \
  const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHamiltonDist3D,\
    const VecLong3D*: _VecLongHamiltonDist3D,\
    default: PBErrInvalidPolymorphism), \
  const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHamiltonDist4D,\
    const VecLong4D*: _VecLongHamiltonDist4D,\
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecIsEqual(VecA, VecB) _Generic(VecA, \
  VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatIsEqual, \
    VecFloat2D*: _VecFloatIsEqual, \
    VecFloat3D*: _VecFloatIsEqual, \
    const VecFloat*: _VecFloatIsEqual, \
   const VecFloat2D*: _VecFloatIsEqual, \
const VecFloat3D*: _VecFloatIsEqual, \
    default: PBErrInvalidPolymorphism), \
  VecFloat2D*: _Generic(VecB, \
    VecFloat*: _VecFloatIsEqual, \
    VecFloat2D*: _VecFloatIsEqual, \
    const VecFloat*: _VecFloatIsEqual, \
    const VecFloat2D*: _VecFloatIsEqual, \
    default: PBErrInvalidPolymorphism), \
  VecFloat3D*: _Generic(VecB, \
    VecFloat*: _VecFloatIsEqual, \
    VecFloat3D*: _VecFloatIsEqual, \
    const VecFloat3D*: _VecFloatIsEqual, \
    default: PBErrInvalidPolymorphism), \
  VecShort*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual,\
    VecShort2D*: _VecShortIsEqual,\
    VecShort3D*: _VecShortIsEqual,\
    VecShort4D*: _VecShortIsEqual,\
    const VecShort*: _VecShortIsEqual,\
    const VecShort2D*: _VecShortIsEqual,\
   const VecShort3D*: _VecShortIsEqual,\
const VecShort4D*: _VecShortIsEqual,\
    default: PBErrInvalidPolymorphism), \
  VecShort2D*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual,\
    VecShort2D*: _VecShortIsEqual,\
```

```
const VecShort*: _VecShortIsEqual,\
 const VecShort2D*: _VecShortIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
 VecShort*: _VecShortIsEqual,\
 VecShort3D*: _VecShortIsEqual,\
 const VecShort*: _VecShortIsEqual,\
 const VecShort3D*: _VecShortIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
 VecShort*: _VecShortIsEqual,\
 VecShort4D*: _VecShortIsEqual,\
 const VecShort*: _VecShortIsEqual,\
 const VecShort4D*: _VecShortIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
 VecLong*: _VecLongIsEqual,\
 VecLong2D*: _VecLongIsEqual,\
 VecLong3D*: _VecLongIsEqual,\
 VecLong4D*: _VecLongIsEqual,\
 const VecLong*: _VecLongIsEqual,\
 const VecLong2D*: _VecLongIsEqual,\
const VecLong3D*: _VecLongIsEqual,\
 const VecLong4D*: _VecLongIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
 VecLong*: _VecLongIsEqual,\
 VecLong2D*: _VecLongIsEqual,\
 const VecLong*: _VecLongIsEqual,\
 const VecLong2D*: _VecLongIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
 VecLong*: _VecLongIsEqual,\
 VecLong3D*: _VecLongIsEqual,\
 const VecLong*: _VecLongIsEqual,\
 const VecLong3D*: _VecLongIsEqual,\
 default: PBErrInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
 VecLong*: _VecLongIsEqual,\
 VecLong4D*: _VecLongIsEqual,\
 const VecLong*: _VecLongIsEqual,\
 const VecLong4D*: _VecLongIsEqual,\
 default: PBErrInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
 VecFloat*: _VecFloatIsEqual, \
 VecFloat2D*: _VecFloatIsEqual, \
 VecFloat3D*: _VecFloatIsEqual, \
 const VecFloat*: _VecFloatIsEqual, \
 const VecFloat3D*: _VecFloatIsEqual, \
 default: PBErrInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
 VecFloat*: _VecFloatIsEqual, \
 VecFloat2D*: _VecFloatIsEqual, \
 const VecFloat*: _VecFloatIsEqual, \
 const VecFloat2D*: _VecFloatIsEqual, \
 default: PBErrInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
 VecFloat*: _VecFloatIsEqual, \
 VecFloat3D*: _VecFloatIsEqual, \
 const VecFloat*: _VecFloatIsEqual, \
 const VecFloat3D*: _VecFloatIsEqual, \
```

```
default: PBErrInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
  VecShort*: _VecShortIsEqual,\
  VecShort2D*: _VecShortIsEqual,\
  VecShort3D*: _VecShortIsEqual,\
  VecShort4D*: _VecShortIsEqual,\
  const VecShort*: _VecShortIsEqual,\
  const VecShort2D*: _VecShortIsEqual,\
 const VecShort3D*: _VecShortIsEqual,\
const VecShort4D*: _VecShortIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
  VecShort*: _VecShortIsEqual,\
  VecShort2D*: _VecShortIsEqual,\
  const VecShort*: _VecShortIsEqual,\
  const VecShort2D*: _VecShortIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
  VecShort*: _VecShortIsEqual,\
  VecShort3D*: _VecShortIsEqual,\
  const VecShort*: _VecShortIsEqual,\
  const VecShort3D*: _VecShortIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
  VecShort*: _VecShortIsEqual,\
  VecShort4D*: _VecShortIsEqual,\
  const VecShort*: _VecShortIsEqual,\
  const VecShort4D*: _VecShortIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
  VecLong*: _VecLongIsEqual,\
  VecLong2D*: _VecLongIsEqual,\
  VecLong3D*: _VecLongIsEqual,\
  VecLong4D*: _VecLongIsEqual,\
  const VecLong*: _VecLongIsEqual,\
  const VecLong2D*: _VecLongIsEqual,\
  {\tt const~VecLong3D*:~\_VecLongIsEqual,} \\
  const VecLong4D*: _VecLongIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
  VecLong*: _VecLongIsEqual,\
  VecLong2D*: _VecLongIsEqual,\
  const VecLong*: _VecLongIsEqual,\
  const VecLong2D*: _VecLongIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecLong3D*: _Generic(VecB, \
  VecLong*: _VecLongIsEqual,\
  VecLong3D*: _VecLongIsEqual,\
  const VecLong*: _VecLongIsEqual,\
  const VecLong3D*: _VecLongIsEqual,\
  default: PBErrInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
  VecLong*: _VecLongIsEqual,\
  VecLong4D*: _VecLongIsEqual,\
  \verb|const VecLong*: _VecLongIsEqual, \\ \\ \\ \\ \\ \\
  const VecLong4D*: _VecLongIsEqual,\
  default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)( \
  _Generic(VecA, \
    VecFloat2D*: (const VecFloat*)(VecA), \
    VecFloat3D*: (const VecFloat*)(VecA), \
    VecShort2D*: (const VecShort*)(VecA), \
```

```
VecShort3D*: (const VecShort*)(VecA), \
     VecShort4D*: (const VecShort*)(VecA), \
     VecLong2D*: (const VecLong*)(VecA), \
     VecLong3D*: (const VecLong*)(VecA), \
     VecLong4D*: (const VecLong*)(VecA), \
      const VecFloat2D*: (const VecFloat*)(VecA), \
     const VecFloat3D*: (const VecFloat*)(VecA), \
      const VecShort2D*: (const VecShort*)(VecA), \
     const VecShort3D*: (const VecShort*)(VecA), \
     const VecShort4D*: (const VecShort*)(VecA), \
      const VecLong2D*: (const VecLong*)(VecA), \
      const VecLong3D*: (const VecLong*)(VecA), \
     const VecLong4D*: (const VecLong*)(VecA), \
     default: VecA), \
   _Generic(VecB, \
     VecFloat2D*: (const VecFloat*)(VecB), \
     VecFloat3D*: (const VecFloat*)(VecB), \
     VecShort2D*: (const VecShort*)(VecB), \
     VecShort3D*: (const VecShort*)(VecB), \
     VecShort4D*: (const VecShort*)(VecB), \
     VecLong2D*: (const VecLong*)(VecB), \
     VecLong3D*: (const VecLong*)(VecB), \
     VecLong4D*: (const VecLong*)(VecB), \
      const VecFloat2D*: (const VecFloat*)(VecB), \
     const VecFloat3D*: (const VecFloat*)(VecB), \
     const VecShort2D*: (const VecShort*)(VecB), \
      const VecShort3D*: (const VecShort*)(VecB), \
      const VecShort4D*: (const VecShort*)(VecB), \
     const VecLong2D*: (const VecLong*)(VecB), \
     const VecLong3D*: (const VecLong*)(VecB), \
      const VecLong4D*: (const VecLong*)(VecB), \
     default: VecB))
#define VecOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatOp, \
   const VecFloat*: _VecFloatOp, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloat0p2D, \
   const VecFloat2D*: _VecFloat0p2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloat0p3D, \
   const VecFloat3D*: _VecFloat0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \)
   VecShort*: _VecShortOp, \
   const VecShort*: _VecShortOp, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShort0p2D, \
   const VecShort2D*: _VecShort0p2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShort0p3D, \
   const VecShort3D*: _VecShort0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShort0p4D, \
   const VecShort4D*: _VecShort0p4D, \
   default: PBErrInvalidPolymorphism), \
```

```
VecLong*: _Generic(VecB, \
   VecLong*: _VecLongOp, \
   const VecLong*: _VecLongOp, \
   default: PBErrInvalidPolymorphism), \
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLong0p2D, \
   const VecLong2D*: _VecLong0p2D, \
   default: PBErrInvalidPolymorphism), \
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLong0p3D, \
   const VecLong3D*: _VecLong0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLong0p4D, \
   const VecLong4D*: _VecLong0p4D, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, CoeffA, VecB, CoeffB)
#define VecGetOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatGetOp, \
   const VecFloat*: _VecFloatGetOp, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatGetOp2D, \
   const VecFloat2D*: _VecFloatGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatGet0p3D, \
   const VecFloat3D*: _VecFloatGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortGetOp, \
   const VecShort*: _VecShortGetOp, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortGetOp2D, \
   const VecShort2D*: _VecShortGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortGetOp3D, \
   const VecShort3D*: _VecShortGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortGet0p4D, \
   const VecShort4D*: _VecShortGet0p4D, \
   default: PBErrInvalidPolymorphism), \
 VecLong*: _Generic(VecB, \
   VecLong*: _VecLongGetOp, \
   const VecLong*: _VecLongGetOp, \
   default: PBErrInvalidPolymorphism), \
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongGet0p2D, \
   const VecLong2D*: _VecLongGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongGet0p3D, \
   const VecLong3D*: _VecLongGet0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongGet0p4D, \
   const VecLong4D*: _VecLongGet0p4D, \
```

```
default: PBErrInvalidPolymorphism), \
 const VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatGetOp, \
   const VecFloat*: _VecFloatGetOp, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatGetOp2D, \
   const VecFloat2D*: _VecFloatGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatGet0p3D, \
   const VecFloat3D*: _VecFloatGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort*: _Generic(VecB, \
   VecShort*: _VecShortGetOp, \
   const VecShort*: _VecShortGetOp, \
   default: PBErrInvalidPolymorphism), \
 const VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortGetOp2D, \
   const VecShort2D*: _VecShortGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortGetOp3D, \
   const VecShort3D*: _VecShortGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortGet0p4D, \
   const VecShort4D*: _VecShortGetOp4D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong*: _Generic(VecB, \
   VecLong*: _VecLongGetOp, \
   const VecLong*: _VecLongGetOp, \
   default: PBErrInvalidPolymorphism), \
 const VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongGet0p2D, \
   const VecLong2D*: _VecLongGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongGetOp3D, \
   const VecLong3D*: _VecLongGet0p3D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongGet0p4D, \
   const VecLong4D*: _VecLongGet0p4D, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, CoeffA, VecB, CoeffB)
#define VecHadamardProd(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatHadamardProd, \
   const VecFloat*: _VecFloatHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatHadamardProd2D, \
   const VecFloat2D*: _VecFloatHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatHadamardProd3D, \
   const VecFloat3D*: _VecFloatHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHadamardProd, \
```

```
const VecShort*: _VecShortHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHadamardProd2D, \
   const VecShort2D*: _VecShortHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortHadamardProd3D, \
   const VecShort3D*: _VecShortHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHadamardProd4D, \
   const VecShort4D*: _VecShortHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 VecLong*: _Generic(VecB, \
   VecLong*: _VecLongHadamardProd, \
   const VecLong*: _VecLongHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongHadamardProd2D, \
   const VecLong2D*: _VecLongHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongHadamardProd3D, \
   const VecLong3D*: _VecLongHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongHadamardProd4D, \
   const VecLong4D*: _VecLongHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecGetHadamardProd(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatGetHadamardProd, \
   const VecFloat*: _VecFloatGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatGetHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatGetHadamardProd3D, \
   const VecFloat3D*: _VecFloatGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortGetHadamardProd, \
   const VecShort*: _VecShortGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortGetHadamardProd2D, \
   const VecShort2D*: _VecShortGetHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortGetHadamardProd3D, \
   const VecShort3D*: _VecShortGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortGetHadamardProd4D, \
   const VecShort4D*: _VecShortGetHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 VecLong*: _Generic(VecB, \
```

```
VecLong*: _VecLongGetHadamardProd, \
   const VecLong*: _VecLongGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongGetHadamardProd2D, \
   const VecLong2D*: _VecLongGetHadamardProd2D, \
   {\tt default:\ PBErrInvalidPolymorphism),\ } \\
 VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongGetHadamardProd3D, \
   const VecLong3D*: _VecLongGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongGetHadamardProd4D, \
   const VecLong4D*: _VecLongGetHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatGetHadamardProd, \
   const VecFloat*: _VecFloatGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat2D*: Generic(VecB. \
   VecFloat2D*: _VecFloatGetHadamardProd2D, \
   const VecFloat2D*: _VecFloatGetHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatGetHadamardProd3D, \
   const VecFloat3D*: _VecFloatGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort*: _Generic(VecB, \
   VecShort*: _VecShortGetHadamardProd, \
   const VecShort*: _VecShortGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 const VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortGetHadamardProd2D, \
   const VecShort2D*: _VecShortGetHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort3D*: Generic(VecB. \
   VecShort3D*: _VecShortGetHadamardProd3D, \
   const VecShort3D*: _VecShortGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 const VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortGetHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong*: _Generic(VecB, \
   VecLong*: _VecLongGetHadamardProd, \
   const VecLong*: _VecLongGetHadamardProd, \
   default: PBErrInvalidPolymorphism), \
 const VecLong2D*: _Generic(VecB, \
   VecLong2D*: _VecLongGetHadamardProd2D, \
   const VecLong2D*: _VecLongGetHadamardProd2D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong3D*: _Generic(VecB, \
   VecLong3D*: _VecLongGetHadamardProd3D, \
   const VecLong3D*: _VecLongGetHadamardProd3D, \
   default: PBErrInvalidPolymorphism), \
 const VecLong4D*: _Generic(VecB, \
   VecLong4D*: _VecLongGetHadamardProd4D, \
   const VecLong4D*: _VecLongGetHadamardProd4D, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecScale(Vec, Scale) _Generic(Vec, \
```

```
VecFloat*: _VecFloatScale, \
  VecFloat2D*: _VecFloatScale2D, \
  VecFloat3D*: _VecFloatScale3D, \
  default: PBErrInvalidPolymorphism)(Vec, Scale)
#define VecGetScale(Vec, Scale) _Generic(Vec, \
 VecFloat*: _VecFloatGetScale, \
  const VecFloat*: _VecFloatGetScale, \
 VecFloat2D*: _VecFloatGetScale2D, \
  const VecFloat2D*: _VecFloatGetScale2D, \
  VecFloat3D*: _VecFloatGetScale3D, \
  const VecFloat3D*: _VecFloatGetScale3D, \
 default: PBErrInvalidPolymorphism) (Vec, Scale)
#define VecRot(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRot2D, \
 VecFloat2D*: _VecFloatRot2D, \
 default: PBErrInvalidPolymorphism)((VecFloat2D*)(Vec), Theta)
#define VecGetRot(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRot2D, \
  const VecFloat*: _VecFloatGetRot2D, \
 VecFloat2D*: _VecFloatGetRot2D, \
  \verb|const VecFloat2D*: _VecFloatGetRot2D, \  \  \setminus \\
 default: PBErrInvalidPolymorphism)((const VecFloat2D*)(Vec), Theta)
#define VecRotAxis(Vec, Axis, Theta) _Generic(Vec, \
 VecFloat*: _VecFloatRotAxis, \
  VecFloat3D*: _VecFloatRotAxis, \
 default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), \
    ({\tt VecFloat3D*})({\tt Axis}), Theta)
#define VecGetRotAxis(Vec, Axis, Theta) _Generic(Vec, \
 VecFloat*: _VecFloatGetRotAxis, \
  const VecFloat*: _VecFloatGetRotAxis, \
 VecFloat3D*: _VecFloatGetRotAxis, \
  const VecFloat3D*: _VecFloatGetRotAxis, \
 default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), \
    (const VecFloat3D*)(Axis), Theta)
#define VecRotX(Vec, Theta) _Generic(Vec, \
 VecFloat*: _VecFloatRotX, \
  VecFloat3D*: _VecFloatRotX, \
 default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecGetRotX(Vec, Theta) _Generic(Vec, \
 VecFloat*: _VecFloatGetRotX, \
  const VecFloat*: _VecFloatGetRotX, \
 VecFloat3D*: _VecFloatGetRotX, \
 const VecFloat3D*: _VecFloatGetRotX, \
  default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)
#define VecRotY(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRotY, \
 VecFloat3D*: _VecFloatRotY, \
 default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecGetRotY(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRotY, \
  const VecFloat*: _VecFloatGetRotY, \
  VecFloat3D*: _VecFloatGetRotY, \
 const VecFloat3D*: _VecFloatGetRotY, \
```

```
default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)
#define VecRotZ(Vec, Theta) _Generic(Vec, \
 \label{eq:VecFloatRotZ} \mbox{VecFloatRotZ, $$\backslash$}
 VecFloat3D*: _VecFloatRotZ, \
 default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecGetRotZ(Vec, Theta) _Generic(Vec, \
 VecFloat*: _VecFloatGetRotZ, \
  const VecFloat*: _VecFloatGetRotZ, \
  VecFloat3D*: _VecFloatGetRotZ, \
 const VecFloat3D*: _VecFloatGetRotZ, \
 default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)
#define VecDotProd(VecA, VecB) _Generic(VecA, \
  VecShort*: _VecShortDotProd,\
 const VecShort*: _VecShortDotProd,\
 VecShort2D*: _VecShortDotProd2D,\
  const VecShort2D*: _VecShortDotProd2D,\
 VecShort3D*: _VecShortDotProd3D,\
  const VecShort3D*: _VecShortDotProd3D,\
  VecShort4D*: _VecShortDotProd4D,\
  const VecShort4D*: _VecShortDotProd4D,\
  VecLong*: _VecLongDotProd,\
  const VecLong*: _VecLongDotProd,\
  VecLong2D*: _VecLongDotProd2D,\
  const VecLong2D*: _VecLongDotProd2D,\
  VecLong3D*: _VecLongDotProd3D,\
  const VecLong3D*: _VecLongDotProd3D,\
  VecLong4D*: _VecLongDotProd4D,\
  const VecLong4D*: _VecLongDotProd4D,\
  VecFloat*: _VecFloatDotProd, \
 const VecFloat*: _VecFloatDotProd, \
  VecFloat2D*: _VecFloatDotProd2D, \
  const VecFloat2D*: _VecFloatDotProd2D, \
  VecFloat3D*: _VecFloatDotProd3D, \
  const VecFloat3D*: _VecFloatDotProd3D, \
  default: PBErrInvalidPolymorphism) (VecA, VecB) \
#define VecCrossProd(VecA, VecB) _Generic(VecA, \
 VecFloat*: _VecFloatGetCrossProd, \
  const VecFloat*: _VecFloatGetCrossProd, \
  VecFloat3D*: _VecFloatGetCrossProd3D, \
  const VecFloat3D*: _VecFloatGetCrossProd3D, \
 default: PBErrInvalidPolymorphism) (VecA, VecB) \
#define VecAngleTo(VecFrom, VecTo) _Generic(VecFrom, \
 VecFloat*: _VecFloatAngleTo2D, \
 const VecFloat*: _VecFloatAngleTo2D, \
 VecFloat2D*: _VecFloatAngleTo2D, \
  const VecFloat2D*: _VecFloatAngleTo2D, \
 default: PBErrInvalidPolymorphism)((const VecFloat2D*)(VecFrom), \
    (const VecFloat2D*)(VecTo))
#define VecStep(Vec, VecBound) _Generic(Vec, \
 VecShort*: _VecShortStep, \
  VecShort2D*: _VecShortStep, \
 VecShort3D*: _VecShortStep, \
  VecShort4D*: _VecShortStep, \
  VecLong*: _VecLongStep, \
  VecLong2D*: _VecLongStep, \
  VecLong3D*: _VecLongStep, \
```

```
VecLong4D*: _VecLongStep, \
 default: PBErrInvalidPolymorphism)(_Generic(Vec, \
   VecShort*: (VecShort*)(Vec), \
   VecShort2D*: (VecShort*)(Vec), \
   VecShort3D*: (VecShort*)(Vec), \
   VecShort4D*: (VecShort*)(Vec), \
   VecLong*: (VecLong*)(Vec), \
   VecLong2D*: (VecLong*)(Vec), \
   VecLong3D*: (VecLong*)(Vec), \
   VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
   VecShort*: (const VecShort*)(VecBound), \
   VecShort2D*: (const VecShort*)(VecBound), \
   VecShort3D*: (const VecShort*)(VecBound), \
   VecShort4D*: (const VecShort*)(VecBound), \
   const VecShort*: (const VecShort*)(VecBound), \
   const VecShort2D*: (const VecShort*)(VecBound), \
   const VecShort3D*: (const VecShort*)(VecBound), \
   const VecShort4D*: (const VecShort*)(VecBound), \
   VecLong*: (const VecLong*)(VecBound), \
   VecLong2D*: (const VecLong*)(VecBound), \
   VecLong3D*: (const VecLong*)(VecBound), \
   VecLong4D*: (const VecLong*)(VecBound), \
   const VecLong*: (const VecLong*)(VecBound), \
   const VecLong2D*: (const VecLong*)(VecBound), \
   const VecLong3D*: (const VecLong*)(VecBound), \
   const VecLong4D*: (const VecLong*)(VecBound)))
#define VecPStep(Vec, VecBound) _Generic(Vec, \
 VecShort*: _VecShortPStep, \
 VecShort2D*: _VecShortPStep, \
 VecShort3D*: _VecShortPStep, \
 VecShort4D*: _VecShortPStep, \
 VecLong*: _VecLongPStep, \
 VecLong2D*: _VecLongPStep, \
 VecLong3D*: _VecLongPStep, \
VecLong4D*: _VecLongPStep, \
 default: PBErrInvalidPolymorphism)(_Generic(Vec, \
   VecShort*: (VecShort*)(Vec), \
   VecShort2D*: (VecShort*)(Vec), \
   VecShort3D*: (VecShort*)(Vec), \
   VecShort4D*: (VecShort*)(Vec), \
   VecLong*: (VecLong*)(Vec), \
   VecLong2D*: (VecLong*)(Vec), \
   VecLong3D*: (VecLong*)(Vec), \
   VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
   VecShort*: (const VecShort*)(VecBound), \
   VecShort2D*: (const VecShort*)(VecBound), \
   VecShort3D*: (const VecShort*)(VecBound), \
   VecShort4D*: (const VecShort*)(VecBound), \
   const VecShort*: (const VecShort*)(VecBound), \
   const VecShort2D*: (const VecShort*)(VecBound), \
   const VecShort3D*: (const VecShort*)(VecBound), \
   const VecShort4D*: (const VecShort*)(VecBound), \
   VecLong*: (const VecLong*)(VecBound), \
   VecLong2D*: (const VecLong*)(VecBound), \
   VecLong3D*: (const VecLong*)(VecBound), \
   VecLong4D*: (const VecLong*)(VecBound), \
   const VecLong*: (const VecLong*)(VecBound), \
   const VecLong2D*: (const VecLong*)(VecBound), \
   const VecLong3D*: (const VecLong*)(VecBound), \
   const VecLong4D*: (const VecLong*)(VecBound)))
```

```
#define VecShiftStep(Vec, VecFrom, VecTo) _Generic(Vec, \
 VecShort*: _VecShortShiftStep, \
 VecShort2D*: _VecShortShiftStep, \
 VecShort3D*: _VecShortShiftStep, \
 VecShort4D*: _VecShortShiftStep, \
 VecLong*: _VecLongShiftStep, \
 VecLong2D*: _VecLongShiftStep, \
 VecLong3D*: _VecLongShiftStep, \
 VecLong4D*: _VecLongShiftStep, \
 default: PBErrInvalidPolymorphism)(_Generic(Vec, \
   VecShort*: (VecShort*)(Vec), \
   VecShort2D*: (VecShort*)(Vec), \
   VecShort3D*: (VecShort*)(Vec), \
   VecShort4D*: (VecShort*)(Vec), \
   VecLong*: (VecLong*)(Vec), \
   VecLong2D*: (VecLong*)(Vec), \
   VecLong3D*: (VecLong*)(Vec), \
   VecLong4D*: (VecLong*)(Vec)), _Generic(VecFrom, \
   VecShort*: (const VecShort*)(VecFrom), \
   VecShort2D*: (const VecShort*)(VecFrom), \
   VecShort3D*: (const VecShort*)(VecFrom), \
   VecShort4D*: (const VecShort*)(VecFrom), \
   const VecShort*: (const VecShort*)(VecFrom), \
   const VecShort2D*: (const VecShort*)(VecFrom), \
   const VecShort3D*: (const VecShort*)(VecFrom), \
   const VecShort4D*: (const VecShort*)(VecFrom), \
   VecLong*: (const VecLong*)(VecFrom), \
   VecLong2D*: (const VecLong*)(VecFrom), \
   VecLong3D*: (const VecLong*)(VecFrom), \
   VecLong4D*: (const VecLong*)(VecFrom), \
   const VecLong*: (const VecLong*)(VecFrom), \
   const VecLong2D*: (const VecLong*)(VecFrom), \
   const VecLong3D*: (const VecLong*)(VecFrom), \
   const VecLong4D*: (const VecLong*)(VecFrom)), _Generic(VecTo, \
   VecShort*: (const VecShort*)(VecTo), \
   VecShort2D*: (const VecShort*)(VecTo), \
   VecShort3D*: (const VecShort*)(VecTo), \
   VecShort4D*: (const VecShort*)(VecTo), \
   const VecShort*: (const VecShort*)(VecTo), \
   const VecShort2D*: (const VecShort*)(VecTo), \
   const VecShort3D*: (const VecShort*)(VecTo), \
   const VecShort4D*: (const VecShort*)(VecTo), \
   VecLong*: (const VecLong*)(VecTo), \
   VecLong2D*: (const VecLong*)(VecTo), \
   VecLong3D*: (const VecLong*)(VecTo), \
   VecLong4D*: (const VecLong*)(VecTo), \
   const VecLong*: (const VecLong*)(VecTo), \
   const VecLong2D*: (const VecLong*)(VecTo), \
   const VecLong3D*: (const VecLong*)(VecTo), \
   const VecLong4D*: (const VecLong*)(VecTo)))
#define VecPStepDelta(Vec, VecBound, VecDelta) _Generic(Vec, \
 VecShort*: _VecShortPStepDelta, \
 VecShort2D*: _VecShortPStepDelta, \
 VecShort3D*: _VecShortPStepDelta, \
 VecShort4D*: _VecShortPStepDelta, \
 VecLong*: _VecLongPStepDelta, \
 VecLong2D*: _VecLongPStepDelta, \
 VecLong3D*: _VecLongPStepDelta, \
 VecLong4D*: _VecLongPStepDelta, \
 default: PBErrInvalidPolymorphism)(_Generic(Vec, \
   VecShort*: (VecShort*)(Vec), \
```

```
VecShort2D*: (VecShort*)(Vec), \
   VecShort3D*: (VecShort*)(Vec), \
   VecShort4D*: (VecShort*)(Vec), \
   VecLong*: (VecLong*)(Vec), \
   VecLong2D*: (VecLong*)(Vec), \
   VecLong3D*: (VecLong*)(Vec), \
   VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
   VecShort*: (const VecShort*)(VecBound), \
   VecShort2D*: (const VecShort*)(VecBound), \
   VecShort3D*: (const VecShort*)(VecBound), \
   VecShort4D*: (const VecShort*)(VecBound), \
   const VecShort*: (const VecShort*)(VecBound), \
   const VecShort2D*: (const VecShort*)(VecBound), \
   const VecShort3D*: (const VecShort*)(VecBound), \
   const VecShort4D*: (const VecShort*)(VecBound), \
   VecLong*: (const VecLong*)(VecBound), \
   VecLong2D*: (const VecLong*)(VecBound), \
   VecLong3D*: (const VecLong*)(VecBound), \
   VecLong4D*: (const VecLong*)(VecBound), \
   const VecLong*: (const VecLong*)(VecBound), \
   const VecLong2D*: (const VecLong*)(VecBound), \
   const VecLong3D*: (const VecLong*)(VecBound), \
   const VecLong4D*: (const VecLong*)(VecBound)), _Generic(VecDelta, \
   VecShort*: (const VecShort*)(VecDelta), \
   VecShort2D*: (const VecShort*)(VecDelta), \
   VecShort3D*: (const VecShort*)(VecDelta), \
   VecShort4D*: (const VecShort*)(VecDelta), \
   const VecShort*: (const VecShort*)(VecDelta), \
   const VecShort2D*: (const VecShort*)(VecDelta), \
   const VecShort3D*: (const VecShort*)(VecDelta), \
   const VecShort4D*: (const VecShort*)(VecDelta), \
   VecLong*: (const VecLong*)(VecDelta), \
   VecLong2D*: (const VecLong*)(VecDelta), \
   VecLong3D*: (const VecLong*)(VecDelta), \
   VecLong4D*: (const VecLong*)(VecDelta), \
   const VecLong*: (const VecLong*)(VecDelta), \
   const VecLong2D*: (const VecLong*)(VecDelta), \
   const VecLong3D*: (const VecLong*)(VecDelta), \
   const VecLong4D*: (const VecLong*)(VecDelta)))
#define VecGetMaxVal(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMaxVal, \
 const VecFloat*: _VecFloatGetMaxVal, \
 VecFloat2D*: _VecFloatGetMaxVal, \
 const VecFloat2D*: VecFloatGetMaxVal. \
 VecFloat3D*: _VecFloatGetMaxVal, \
 const VecFloat3D*: _VecFloatGetMaxVal, \
 VecShort*: _VecShortGetMaxVal, \
 const VecShort*: _VecShortGetMaxVal, \
 VecShort2D*: _VecShortGetMaxVal, \
 const VecShort2D*: _VecShortGetMaxVal, \
 VecShort3D*: _VecShortGetMaxVal, \
 const VecShort3D*: _VecShortGetMaxVal, \
 VecShort4D*: _VecShortGetMaxVal, \
 const VecShort4D*: _VecShortGetMaxVal, \
 VecLong*: _VecLongGetMaxVal, \
 const VecLong*: _VecLongGetMaxVal, \
 VecLong2D*: _VecLongGetMaxVal, \
 const VecLong2D*: _VecLongGetMaxVal, \
 VecLong3D*: _VecLongGetMaxVal, \
 const VecLong3D*: _VecLongGetMaxVal, \
 VecLong4D*: _VecLongGetMaxVal, \
```

```
const VecLong4D*: _VecLongGetMaxVal, \
 default: PBErrInvalidPolymorphism) (_Generic(Vec, \
   VecFloat2D*: (const VecFloat*)(Vec), \
   const VecFloat2D*: (const VecFloat*)(Vec), \
   VecFloat3D*: (const VecFloat*)(Vec), \
   const VecFloat3D*: (const VecFloat*)(Vec), \
   VecShort2D*: (const VecShort*)(Vec), \
   const VecShort2D*: (const VecShort*)(Vec), \
   VecShort3D*: (const VecShort*)(Vec), \
   const VecShort3D*: (const VecShort*)(Vec), \
   VecShort4D*: (const VecShort*)(Vec), \
   const VecShort4D*: (const VecShort*)(Vec), \
   VecLong2D*: (const VecLong*)(Vec), \
   const VecLong2D*: (const VecLong*)(Vec), \
   VecLong3D*: (const VecLong*)(Vec), \
   const VecLong3D*: (const VecLong*)(Vec), \
   VecLong4D*: (const VecLong*)(Vec), \
   const VecLong4D*: (const VecLong*)(Vec), \
   default: Vec))
#define VecGetMinVal(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMinVal, \
 const VecFloat*: _VecFloatGetMinVal, \
 VecFloat2D*: _VecFloatGetMinVal, \
 const VecFloat2D*: _VecFloatGetMinVal, \
 VecFloat3D*: _VecFloatGetMinVal, \
 const VecFloat3D*: _VecFloatGetMinVal, \
 VecShort*: _VecShortGetMinVal, \
 const VecShort*: _VecShortGetMinVal, \
 VecShort2D*: _VecShortGetMinVal, \
 const VecShort2D*: _VecShortGetMinVal, \
 VecShort3D*: _VecShortGetMinVal, \
 const VecShort3D*: _VecShortGetMinVal, \
 VecShort4D*: _VecShortGetMinVal, \
 const VecShort4D*: _VecShortGetMinVal, \
 VecLong*: _VecLongGetMinVal, \
 const VecLong*: _VecLongGetMinVal, \
 VecLong2D*: _VecLongGetMinVal, \
 const VecLong2D*: _VecLongGetMinVal, \
 VecLong3D*: _VecLongGetMinVal, \
 const VecLong3D*: _VecLongGetMinVal, \
 VecLong4D*: _VecLongGetMinVal, \
 const VecLong4D*: _VecLongGetMinVal, \
 default: PBErrInvalidPolymorphism) (_Generic(Vec, \
   VecFloat2D*: (const VecFloat*)(Vec), \
   const VecFloat2D*: (const VecFloat*)(Vec), \
   VecFloat3D*: (const VecFloat*)(Vec), \
   const VecFloat3D*: (const VecFloat*)(Vec), \
   VecShort2D*: (const VecShort*)(Vec), \
   const VecShort2D*: (const VecShort*)(Vec), \
   VecShort3D*: (const VecShort*)(Vec), \
   const VecShort3D*: (const VecShort*)(Vec), \
   VecShort4D*: (const VecShort*)(Vec), \
   const VecShort4D*: (const VecShort*)(Vec), \
   VecLong2D*: (const VecLong*)(Vec), \
   const VecLong2D*: (const VecLong*)(Vec), \
   VecLong3D*: (const VecLong*)(Vec), \
   const VecLong3D*: (const VecLong*)(Vec), \
   VecLong4D*: (const VecLong*)(Vec), \
   const VecLong4D*: (const VecLong*)(Vec), \
   default: Vec))
```

```
#define VecGetMaxValAbs(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMaxValAbs, \
 const VecFloat*: _VecFloatGetMaxValAbs, \
 VecFloat2D*: _VecFloatGetMaxValAbs, \
 const VecFloat2D*: _VecFloatGetMaxValAbs, \
 VecFloat3D*: _VecFloatGetMaxValAbs, \
 const VecFloat3D*: _VecFloatGetMaxValAbs, \
 VecShort*: _VecShortGetMaxValAbs, \
 const VecShort*: _VecShortGetMaxValAbs, \
 VecShort2D*: _VecShortGetMaxValAbs, \
 const VecShort2D*: _VecShortGetMaxValAbs, \
 VecShort3D*: _VecShortGetMaxValAbs, \
 const VecShort3D*: _VecShortGetMaxValAbs, \
 VecShort4D*: _VecShortGetMaxValAbs, \
 const VecShort4D*: _VecShortGetMaxValAbs, \
 VecLong*: _VecLongGetMaxValAbs, \
 const VecLong*: _VecLongGetMaxValAbs, \
 VecLong2D*: _VecLongGetMaxValAbs, \
 const VecLong2D*: _VecLongGetMaxValAbs, \
 VecLong3D*: _VecLongGetMaxValAbs, \
 const VecLong3D*: _VecLongGetMaxValAbs, \
 VecLong4D*: _VecLongGetMaxValAbs, \
 const VecLong4D*: _VecLongGetMaxValAbs, \
 default: PBErrInvalidPolymorphism) (_Generic(Vec, \
   VecFloat2D*: (const VecFloat*)(Vec), \
   const VecFloat2D*: (const VecFloat*)(Vec), \
   VecFloat3D*: (const VecFloat*)(Vec), \
   const VecFloat3D*: (const VecFloat*)(Vec), \
   VecShort2D*: (const VecShort*)(Vec), \
   const VecShort2D*: (const VecShort*)(Vec), \
   VecShort3D*: (const VecShort*)(Vec), \
   const VecShort3D*: (const VecShort*)(Vec), \
   VecShort4D*: (const VecShort*)(Vec), \
   const VecShort4D*: (const VecShort*)(Vec), \
   VecLong2D*: (const VecLong*)(Vec), \
   const VecLong2D*: (const VecLong*)(Vec), \
   VecLong3D*: (const VecLong*)(Vec), \
   const VecLong3D*: (const VecLong*)(Vec), \
   VecLong4D*: (const VecLong*)(Vec), \
   const VecLong4D*: (const VecLong*)(Vec), \
   default: Vec))
#define VecGetMinValAbs(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMinValAbs, \
 const VecFloat*: _VecFloatGetMinValAbs, \
 VecFloat2D*: _VecFloatGetMinValAbs, \
 const VecFloat2D*: _VecFloatGetMinValAbs, \
 VecFloat3D*: _VecFloatGetMinValAbs, \
 const VecFloat3D*: _VecFloatGetMinValAbs, \
 VecShort*: _VecShortGetMinValAbs, \
 const VecShort*: _VecShortGetMinValAbs, \
 VecShort2D*: _VecShortGetMinValAbs, \
 const VecShort2D*: _VecShortGetMinValAbs, \
 VecShort3D*: _VecShortGetMinValAbs, \
 const VecShort3D*: _VecShortGetMinValAbs, \
 VecShort4D*: _VecShortGetMinValAbs, \
 const VecShort4D*: _VecShortGetMinValAbs, \
 VecLong*: _VecLongGetMinValAbs, \
 const VecLong*: _VecLongGetMinValAbs, \
 VecLong2D*: _VecLongGetMinValAbs, \
 const VecLong2D*: _VecLongGetMinValAbs, \
 VecLong3D*: _VecLongGetMinValAbs, \
```

```
const VecLong3D*: _VecLongGetMinValAbs, \
  VecLong4D*: _VecLongGetMinValAbs, \
  const VecLong4D*: _VecLongGetMinValAbs, \
  default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (const VecFloat*)(Vec), \
    const VecFloat2D*: (const VecFloat*)(Vec), \
    VecFloat3D*: (const VecFloat*)(Vec). \
    const VecFloat3D*: (const VecFloat*)(Vec), \
    VecShort2D*: (const VecShort*)(Vec), \
    const VecShort2D*: (const VecShort*)(Vec), \
    VecShort3D*: (const VecShort*)(Vec), \
    const VecShort3D*: (const VecShort*)(Vec), \
    VecShort4D*: (const VecShort*)(Vec), \
    const VecShort4D*: (const VecShort*)(Vec), \
    VecLong2D*: (const VecLong*)(Vec), \
    const VecLong2D*: (const VecLong*)(Vec), \
    VecLong3D*: (const VecLong*)(Vec), \
    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))
#define VecStepDelta(Vec, VecBound, Delta) _Generic(Vec, \
  VecFloat*: _VecFloatStepDelta, \
  VecFloat2D*: _VecFloatStepDelta, \
 VecFloat3D*: _VecFloatStepDelta, \
  VecShort*: _VecShortStepDelta, \
 VecShort2D*: _VecShortStepDelta, \
VecShort3D*: _VecShortStepDelta, \
  VecShort4D*: _VecShortStepDelta, \
  VecLong*: _VecLongStepDelta, \
  VecLong2D*: _VecLongStepDelta, \
  VecLong3D*: _VecLongStepDelta, \
  VecLong4D*: _VecLongStepDelta, \
  default: PBErrInvalidPolymorphism)(_Generic(Vec, \
    VecFloat*: Vec, \
    VecFloat2D*: (VecFloat*)(Vec), \
    VecFloat3D*: (VecFloat*)(Vec), \
    VecShort*: Vec, \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    VecLong*: Vec, \
    VecLong2D*: (VecLong*)(Vec), \
    VecLong3D*: (VecLong*)(Vec), \
    VecLong4D*: (VecLong*)(Vec)), _Generic(Vec, \
    VecFloat*: VecBound, \
    VecFloat2D*: (VecFloat*)(VecBound), \
    VecFloat3D*: (VecFloat*)(VecBound), \
    VecShort*: VecBound, \
    VecShort2D*: (VecShort*)(VecBound), \
    VecShort3D*: (VecShort*)(VecBound), \
    VecShort4D*: (VecShort*)(VecBound), \
    VecLong*: VecBound, \
    VecLong2D*: (VecLong*)(VecBound), \
    VecLong3D*: (VecLong*)(VecBound), \
    VecLong4D*: (VecLong*)(VecBound)), _Generic(Vec, \
    VecFloat*: Delta, \
    VecFloat2D*: (VecFloat*)(Delta), \
    VecFloat3D*: (VecFloat*)(Delta), \
    VecShort*: Delta, \
    VecShort2D*: (VecShort*)(Delta), \
```

```
VecShort3D*: (VecShort*)(Delta), \
   VecShort4D*: (VecShort*)(Delta), \
   VecLong*: Delta, \
   VecLong2D*: (VecLong*)(Delta), \
   VecLong3D*: (VecLong*)(Delta), \
   VecLong4D*: (VecLong*)(Delta)))
#define VecShiftStepDelta(Vec, VecFrom, VecTo, Delta) _Generic(Vec, \
 VecFloat*: _VecFloatShiftStepDelta, \
 VecFloat2D*: _VecFloatShiftStepDelta, \
 VecFloat3D*: _VecFloatShiftStepDelta, \
 (VecFloat*)(VecFrom), (VecFloat*)(VecTo), (VecFloat*)(Delta))
#define VecGetIMaxVal(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetIMaxVal, \
 const VecFloat*: _VecFloatGetIMaxVal, \
 VecFloat2D*: _VecFloatGetIMaxVal, \
 const VecFloat2D*: _VecFloatGetIMaxVal, \
 VecFloat3D*: _VecFloatGetIMaxVal, \
 const VecFloat3D*: _VecFloatGetIMaxVal, \
 VecShort*: _VecShortGetIMaxVal, \
 const VecShort*: _VecShortGetIMaxVal, \
 VecShort2D*: _VecShortGetIMaxVal, \
 const VecShort2D*: _VecShortGetIMaxVal, \
 VecShort3D*: _VecShortGetIMaxVal, \
 const VecShort3D*: _VecShortGetIMaxVal, \
 VecShort4D*: _VecShortGetIMaxVal, \
 const VecShort4D*: _VecShortGetIMaxVal, \
 VecLong*: _VecLongGetIMaxVal, \
 const VecLong*: _VecLongGetIMaxVal, \
 VecLong2D*: _VecLongGetIMaxVal, \
 const VecLong2D*: _VecLongGetIMaxVal, \
 VecLong3D*: _VecLongGetIMaxVal, \
 const VecLong3D*: _VecLongGetIMaxVal, \
 VecLong4D*: _VecLongGetIMaxVal, \
 const VecLong4D*: _VecLongGetIMaxVal, \
 default: PBErrInvalidPolymorphism) (_Generic(Vec, \
   VecFloat2D*: (const VecFloat*)(Vec), \
   const VecFloat2D*: (const VecFloat*)(Vec), \
   VecFloat3D*: (const VecFloat*)(Vec), \
   const VecFloat3D*: (const VecFloat*)(Vec), \
   VecShort2D*: (const VecShort*)(Vec), \
   const VecShort2D*: (const VecShort*)(Vec), \
   VecShort3D*: (const VecShort*)(Vec), \
   const VecShort3D*: (const VecShort*)(Vec), \
   VecShort4D*: (const VecShort*)(Vec), \
   const VecShort4D*: (const VecShort*)(Vec), \
   VecLong2D*: (const VecLong*)(Vec), \
   const VecLong2D*: (const VecLong*)(Vec), \
   VecLong3D*: (const VecLong*)(Vec), \
   const VecLong3D*: (const VecLong*)(Vec), \
   VecLong4D*: (const VecLong*)(Vec), \
   const VecLong4D*: (const VecLong*)(Vec), \
   default: Vec))
#define MatClone(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatClone, \
 const MatFloat*: _MatFloatClone, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatEncodeAsJSON(Mat) _Generic(Mat, \
```

```
MatFloat*: _MatFloatEncodeAsJSON, \
  const MatFloat*: _MatFloatEncodeAsJSON, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatDecodeAsJSON(MatRef, Json) _Generic(MatRef, \
 MatFloat**: _MatFloatDecodeAsJSON, \
  default: PBErrInvalidPolymorphism)(MatRef, Json)
#define MatLoad(MatRef, Stream) _Generic(MatRef, \
 MatFloat**: _MatFloatLoad, \
  default: PBErrInvalidPolymorphism)(MatRef, Stream)
#define MatSave(Mat, Stream, Compact) _Generic(Mat, \
 MatFloat*: _MatFloatSave, \
  const MatFloat*: _MatFloatSave, \
  default: PBErrInvalidPolymorphism)(Mat, Stream, Compact)
#define MatFree(MatRef) _Generic(MatRef, \
  MatFloat**: _MatFloatFree, \
 default: PBErrInvalidPolymorphism)(MatRef)
#define MatPrintln(Mat, Stream) _Generic(Mat, \
 MatFloat*: _MatFloatPrintlnDef, \
  const MatFloat*: _MatFloatPrintlnDef, \
 default: PBErrInvalidPolymorphism)(Mat, Stream)
#define MatGet(Mat, VecIndex) _Generic(Mat, \
 MatFloat*: _MatFloatGet, \
  const MatFloat*: _MatFloatGet, \
 default: PBErrInvalidPolymorphism) (Mat, VecIndex)
#define MatSet(Mat, VecIndex, Val) _Generic(Mat, \
 MatFloat*: _MatFloatSet, \
 default: PBErrInvalidPolymorphism) (Mat, VecIndex, Val)
#define MatCopy(MatDest, MatSrc) _Generic(MatDest, \
 MatFloat*: _Generic (MatSrc, \
    MatFloat*: _MatFloatCopy, \
    const MatFloat*: _MatFloatCopy, \
    default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(MatDest, MatSrc)
#define MatDim(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatDim, \
 const MatFloat*: _MatFloatDim, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatGetDim(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetDim, \
  const MatFloat*: _MatFloatGetDim, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatGetEigenValues(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetEigenValues, \
 const MatFloat*: _MatFloatGetEigenValues, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatGetQR(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetQR, \
  const MatFloat*: _MatFloatGetQR, \
  default: PBErrInvalidPolymorphism)(Mat)
```

```
#define MatGetInv(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetInv, \
 const MatFloat*: _MatFloatGetInv, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatGetTranspose(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetTranspose, \
 const MatFloat*: _MatFloatGetTranspose, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatGetNbRow(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetNbRow, \
 const MatFloat*: _MatFloatGetNbRow, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatGetNbCol(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetNbCol, \
 const MatFloat*: _MatFloatGetNbCol, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatGetProdMat(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatGetProdMatFloat, \
   const MatFloat*: _MatFloatGetProdMatFloat, \
   default: PBErrInvalidPolymorphism), \
 const MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatGetProdMatFloat, \
   const MatFloat*: _MatFloatGetProdMatFloat, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (MatA, MatB)
#define MatGetProdVec(Mat, Vec) _Generic(Mat, \
 MatFloat*: _Generic(Vec, \
   VecFloat*: _MatFloatGetProdVecFloat, \
   const VecFloat*: _MatFloatGetProdVecFloat, \
   VecFloat2D*: _MatFloatGetProdVecFloat, \
   const VecFloat2D*: _MatFloatGetProdVecFloat, \
   VecFloat3D*: _MatFloatGetProdVecFloat, \
   const VecFloat3D*: _MatFloatGetProdVecFloat, \
   default: PBErrInvalidPolymorphism), \
 const MatFloat*: _Generic(Vec, \
   VecFloat*: _MatFloatGetProdVecFloat, \
   const VecFloat*: _MatFloatGetProdVecFloat, \
   VecFloat2D*: _MatFloatGetProdVecFloat, \
   const VecFloat2D*: _MatFloatGetProdVecFloat, \
   VecFloat3D*: _MatFloatGetProdVecFloat, \
   const VecFloat3D*: _MatFloatGetProdVecFloat, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))
#define MatGetProdVecVecTranspose(VecA, VecB) _Generic(VecA, \
 VecFloat*: Generic(VecB. \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat*: _Generic(VecB, \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
```

```
VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   default: PBErrInvalidPolymorphism), \
  VecFloat2D*: _Generic(VecB, \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat2D*: _Generic(VecB, \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: MatFloatGetProdVecVecTransposeFloat. \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   default: PBErrInvalidPolymorphism), \
 const VecFloat3D*: _Generic(VecB, \
   VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
   VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)((VecFloat*)(VecA), \
    (VecFloat*)(VecB))
#define MatAdd(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatAdd, \
   const MatFloat*: _MatFloatAdd, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(MatA, MatB)
#define MatScale(MatA, A) _Generic(MatA, \
 MatFloat*: _MatFloatScale, \
 const MatFloat*: _MatFloatScale, \
 default: PBErrInvalidPolymorphism)(MatA, A)
#define MatGetAdd(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatGetAdd, \
   const MatFloat*: _MatFloatGetAdd, \
   default: PBErrInvalidPolymorphism), \
 const MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatGetAdd, \
   const MatFloat*: _MatFloatGetAdd, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(MatA, MatB)
```

```
#define MatSetIdentity(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatSetIdentity, \
 default: PBErrInvalidPolymorphism)(Mat)
#define MatIsEqual(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatIsEqual, \
   const MatFloat*: _MatFloatIsEqual, \
   {\tt default:\ PBErrInvalidPolymorphism),\ } \setminus
 const MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatIsEqual, \
    const MatFloat*: _MatFloatIsEqual, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(MatA, MatB)
#define SysLinEqCreate(Mat, Vec) _Generic(Vec, \
 VecFloat*: _SLECreate, \
 const VecFloat*: _SLECreate, \
 VecFloat2D*: _SLECreate, \
 const VecFloat2D*: _SLECreate, \
 VecFloat3D*: _SLECreate, \
 const VecFloat3D*: _SLECreate, \setminus
  default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))
#define SysLinEqSetV(Sys, Vec) _Generic(Vec, \
 VecFloat*: _SLESetV, \
 const VecFloat*: _SLESetV, \
 VecFloat2D*: _SLESetV, \
 const VecFloat2D*: _SLESetV, \
 VecFloat3D*: _SLESetV, \
 const VecFloat3D*: _SLESetV, \
 default: PBErrInvalidPolymorphism)(Sys, (VecFloat*)(Vec))
// ========= static inliner ==========
#if BUILDMODE != 0
#include "pbmath-inline.c"
#endif
#endif
```

3 Code

3.1 pbmath.c

```
// ======= Functions implementation ==========
// Create a new Vec of dimension 'dim'
// Values are initalized to 0.0
VecShort* VecShortCreate(const long dim) {
#if BUILDMODE == 0
  if (dim <= 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
    PBErrCatch(PBMathErr);
#endif
  // Allocate memory
  VecShort* that = PBErrMalloc(PBMathErr,
    offsetof(VecShort, _val) + sizeof(short) * dim);
  // Set the default values
  that->_dim = dim;
  for (long i = dim; i--;)
    that->_val[i] = 0;
  // Return the new VecShort
  return that;
// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Create a clone
  VecShort* clone = VecShortCreate(that->_dim);
  // Copy the values
  memcpy(clone, that, sizeof(VecShort) + sizeof(short) * that->_dim);
  // Return the clone
  return clone;
// Function which return the JSON encoding of 'that'
JSONNode* _VecShortEncodeAsJSON(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Create the JSON structure
  JSONNode* json = JSONCreate();
  // Declare a buffer to convert value into string
  char val[100];
  \ensuremath{//} Encode the dimension
  sprintf(val, "%ld", VecGetDim(that));
JSONAddProp(json, "_dim", val);
  // Encode the values
  JSONArrayVal setVal = JSONArrayValCreateStatic();
  for (long i = 0; i < VecGetDim(that); ++i) {
   sprintf(val, "%d", VecGet(that, i));</pre>
    JSONArrayValAdd(&setVal, val);
```

```
JSONAddProp(json, "_val", &setVal);
  // Free memory
  JSONArrayValFlush(&setVal);
  // Return the created JSON
  return json;
// Function which decode from JSON encoding 'json' to 'that'
bool _VecShortDecodeAsJSON(VecShort** that, const JSONNode* const json) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (json == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'json' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // If 'that' is already allocated
  if (*that != NULL)
    // Free memory
    _VecShortFree(that);
  // Get the dimension from the {\tt JSON}
  JSONNode* prop = JSONProperty(json, "_dim");
  if (prop == NULL) {
   return false;
  long dim = atol(JSONLblVal(prop));
  // If data are invalid
  if (dim < 1)
    return false;
  // Allocate memory
  *that = VecShortCreate(dim);
  // Get the values
  prop = JSONProperty(json, "_val");
  if (prop == NULL) {
   return false;
  for (long i = 0; i < dim; ++i) {
    long val = atol(JSONLabel(JSONValue(prop, i)));
    VecSet(*that, i, val);
  \ensuremath{//} Return the success code
  return true;
// Load the VecShort from the stream
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* const stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a json to load the encoded data
  JSONNode* json = JSONCreate();
  // Load the whole encoded data
  if (!JSONLoad(json, stream)) {
   return false;
  // Decode the data from the {\tt JSON}
  if (!VecDecodeAsJSON(that, json)) {
    return false;
  // Free the memory used by the JSON
  JSONFree(&json);
  // Return the success code
 return true;
// Save the VecShort to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecShortSave(const VecShort* const that,
 FILE* const stream, const bool compact) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Get the JSON encoding
  JSONNode* json = VecEncodeAsJSON(that);
  // Save the JSON
  if (!JSONSave(json, stream, compact)) {
   return false;
  // Free memory
  JSONFree(&json);
  // Return success code
  return true;
// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that) {
  // Check argument
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  free(*that);
  *that = NULL;
// Print the VecShort on 'stream' with 'prec' digit precision
```

```
void _VecShortPrint(const VecShort* const that,
 FILE* const stream) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
 // Print the values
 fprintf(stream, "<");</pre>
 for (long i = 0; i < that->_dim; ++i) {
   fprintf(stream, "%hi", that->_val[i]);
    if (i < that->_dim - 1)
     fprintf(stream, ",");
 fprintf(stream, ">");
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* const that, const VecShort* const bound) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
 bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 long iDim = that->_dim - 1;
  \ensuremath{//} Declare a flag for the loop condition
 bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
   if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
      --iDim;
```

```
} else {
     flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
   ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* const that, const VecShort* const bound) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != bound->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = 0;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
      that->_val[iDim] = 0;
      ++iDim;
    } else {
     flag = false;
  } while (iDim < that->_dim && flag == true);
  if (iDim == that->_dim)
   ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
```

```
// The upper limit for each value is given by 'to' (val[i] < to[i])</pre>
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* const that,
  const VecShort* const from, const VecShort* const to) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (from == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'from' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != from->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
      that->_dim, from->_dim);
    PBErrCatch(PBMathErr);
  if (to == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'to' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != to->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
      that->_dim, to->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= to->_val[iDim]) {
      that->_val[iDim] = from->_val[iDim];
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by delta from 0
\ensuremath{//} in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
```

```
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])</pre>
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStepDelta(VecShort* const that,
 const VecShort* const bound, const VecShort* const delta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (delta == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
 7
#endif
 // Declare a variable for the returned flag
 bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
 bool flag = true;
 // Increment
   that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
      --iDim;
   } else {
     flag = false;
  } while (iDim >= 0 && flag == true);
 if (iDim == -1)
   ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by delta from \boldsymbol{0}
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
```

```
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStepDelta(VecShort* const that,
 const VecShort* const bound, const VecShort* const delta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 }
 if (delta == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg, "dimensions don't match (\%ld==\%ld)",}
     that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable for the returned flag
 bool ret = true;
 // Declare a variable to memorise the dimension currently increasing
 long iDim = 0;
  // Declare a flag for the loop condition
 bool flag = true;
  // Increment
 do {
   that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
     ++iDim:
   } else {
     flag = false;
 } while (iDim < that->_dim && flag == true);
  if (iDim == that->_dim)
    ret = false;
  // Return the flag
 return ret;
// ----- VecLong
// ====== Functions implementation =========
// Create a new Vec of dimension 'dim'
// Values are initalized to 0.0
VecLong* VecLongCreate(const long dim) {
```

```
#if BUILDMODE == 0
  if (\dim \le 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
    PBErrCatch(PBMathErr);
#endif
  // Allocate memory
  VecLong* that = PBErrMalloc(PBMathErr,
    offsetof(VecLong, _val) + sizeof(long) * dim);
  // Set the default values
  that->_dim = dim;
  for (long i = dim; i--;)
    that->_val[i] = 0;
  // Return the new VecLong
  return that;
// Clone the VecLong
// Return NULL if we couldn't clone the VecLong
VecLong* _VecLongClone(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create a clone
  VecLong* clone = VecLongCreate(that->_dim);
  // Copy the values
  memcpy(clone, that, sizeof(VecLong) + sizeof(long) * that->_dim);
  // Return the clone
 return clone;
// Function which return the JSON encoding of 'that'
JSONNode* _VecLongEncodeAsJSON(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Create the JSON structure
  JSONNode* json = JSONCreate();
  // Declare a buffer to convert value into string
  char val[100];
  // Encode the dimension
  sprintf(val, "%ld", VecGetDim(that));
JSONAddProp(json, "_dim", val);
  // Encode the values
  JSONArrayVal setVal = JSONArrayValCreateStatic();
  for (long i = 0; i < VecGetDim(that); ++i) {
    sprintf(val, "%ld", VecGet(that, i));
    JSONArrayValAdd(&setVal, val);
  JSONAddProp(json, "_val", &setVal);
  // Free memory
  JSONArrayValFlush(&setVal);
  // Return the created JSON
```

```
return json;
}
// Function which decode from JSON encoding 'json' to 'that'
bool _VecLongDecodeAsJSON(VecLong** that, const JSONNode* const json) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (json == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'json' is null");
    PBErrCatch(PBMathErr);
#endif
  // If 'that' is already allocated
  if (*that != NULL)
   // Free memory
    _VecLongFree(that);
  // Get the dimension from the JSON
  JSONNode* prop = JSONProperty(json, "_dim");
  if (prop == NULL) {
   return false;
  long dim = atol(JSONLblVal(prop));
  // If data are invalid
  if (dim < 1)
   return false;
  // Allocate memory
  *that = VecLongCreate(dim);
  // Get the values
  prop = JSONProperty(json, "_val");
  if (prop == NULL) {
   return false;
  for (long i = 0; i < dim; ++i) {
    long val = atol(JSONLabel(JSONValue(prop, i)));
    VecSet(*that, i, val);
  \ensuremath{//} Return the success code
 return true;
// Load the VecLong from the stream
// If the VecLong is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecLongLoad(VecLong** that, FILE* const stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a json to load the encoded data
```

```
JSONNode* json = JSONCreate();
  // Load the whole encoded data
  if (!JSONLoad(json, stream)) {
   return false;
  // Decode the data from the JSON
 if (!VecDecodeAsJSON(that, json)) {
   return false;
  // Free the memory used by the {\tt JSON}
 JSONFree(&json);
 // Return the success code
 return true;
// Save the VecLong to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecLongSave(const VecLong* const that,
 FILE* const stream, const bool compact) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
  // Get the JSON encoding
  JSONNode* json = VecEncodeAsJSON(that);
 // Save the JSON
 if (!JSONSave(json, stream, compact)) {
   return false;
  // Free memory
 JSONFree(&json);
 // Return success code
 return true;
// Free the memory used by a VecLong
// Do nothing if arguments are invalid
void _VecLongFree(VecLong** that) {
 // Check argument
 if (that == NULL || *that == NULL)
    return;
  // Free memory
 free(*that);
 *that = NULL;
// Print the VecLong on 'stream' with 'prec' digit precision
void _VecLongPrint(const VecLong* const that,
 FILE* const stream) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Print the values
  fprintf(stream, "<");</pre>
  for (long i = 0; i < that->_dim; ++i) {
    fprintf(stream, "%ld", that->_val[i]);
    if (i < that->_dim - 1)
      fprintf(stream, ",");
 fprintf(stream, ">");
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStep(VecLong* const that, const VecLong* const bound) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != bound->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, bound->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
      that->_val[iDim] = 0;
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
```

```
ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStep(VecLong* const that, const VecLong* const bound) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != bound->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, bound->_dim);
    PBErrCatch(PBMathErr):
 }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = 0;
  \ensuremath{//} Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
      that->_val[iDim] = 0;
      ++iDim;
    } else {
      flag = false;
  } while (iDim < that->_dim && flag == true);
  if (iDim == that->_dim)
   ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by 1
\ensuremath{//} in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
```

```
// Return true else
\verb|bool_VecLongShiftStep(VecLong* const that,\\
  const VecLong* const from, const VecLong* const to) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (from == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'from' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != from->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
      that->_dim, from->_dim);
    PBErrCatch(PBMathErr);
  if (to == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'to' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != to->_dim) \{
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
      that->_dim, to->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= to->_val[iDim]) {
      that->_val[iDim] = from->_val[iDim];
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
 return ret;
}
// Step the values of the vector incrementally by delta from \boldsymbol{0}
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= \dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStepDelta(VecLong* const that,
```

```
const VecLong* const bound, const VecLong* const delta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (delta == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable for the returned flag
 bool ret = true;
 // Declare a variable to memorise the dimension currently increasing
 long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
 bool flag = true;
  // Increment
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
      --iDim;
   } else {
     flag = false;
 } while (iDim >= 0 && flag == true);
 if (iDim == -1)
    ret = false;
 // Return the flag
 return ret;
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStepDelta(VecLong* const that,
 const VecLong* const bound, const VecLong* const delta) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (delta == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
 bool ret = true;
 // Declare a variable to memorise the dimension currently increasing
 // Declare a flag for the loop condition
 bool flag = true;
  // Increment
 do {
   that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
     ++iDim;
   } else {
     flag = false;
 } while (iDim < that->_dim && flag == true);
 if (iDim == that->_dim)
   ret = false;
  // Return the flag
 return ret;
// ----- VecFloat
// ====== Functions implementation =========
// Create a new Vec of dimension 'dim'
// Values are initalized to 0.0
VecFloat* VecFloatCreate(const long dim) {
#if BUILDMODE == 0
 if (dim <= 0) {
   PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
    PBErrCatch(PBMathErr);
```

```
}
#endif
 // Allocate memory
 VecFloat* that = PBErrMalloc(PBMathErr,
   offsetof(VecFloat, _val) + sizeof(float) * dim);
  // Set the default values
 that->_dim = dim;
  for (long i = dim; i--;)
   that->_val[i] = 0.0;
  // Return the new VecFloat
 return that;
// Clone the VecFloat
VecFloat* _VecFloatClone(const VecFloat* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 // Create a clone
 VecFloat* clone = VecFloatCreate(that->_dim);
 // Clone the properties
 memcpy(clone, that, sizeof(VecFloat) + sizeof(float) * that->_dim);
 // Return the clone
 return clone;
// Function which return the JSON encoding of 'that'
JSONNode* _VecFloatEncodeAsJSON(const VecFloat* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the JSON structure
 JSONNode* json = JSONCreate();
  // Declare a buffer to convert value into string
 char val[100];
  // Encode the dimension
  sprintf(val, "%ld", VecGetDim(that));
  JSONAddProp(json, "_dim", val);
  // Encode the values
  JSONArrayVal setVal = JSONArrayValCreateStatic();
 for (long i = 0; i < VecGetDim(that); ++i) {</pre>
    sprintf(val, "%f", VecGet(that, i));
    JSONArrayValAdd(&setVal, val);
 JSONAddProp(json, "_val", &setVal);
  // Free memory
 JSONArrayValFlush(&setVal);
  // Return the created JSON
 return json;
// Function which decode from JSON encoding 'json' to 'that'
bool _VecFloatDecodeAsJSON(VecFloat** that, const JSONNode* const json) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
                 PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'that' is null");
                PBErrCatch(PBMathErr);
        if (json == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'json' is null");
                PBErrCatch(PBMathErr);
#endif
        \ensuremath{//} If 'that' is already allocated
        if (*that != NULL)
               // Free memory
                  _VecFloatFree(that);
         // Get the dimension from the JSON
        JSONNode* prop = JSONProperty(json, "_dim");
         if (prop == NULL) {
               return false;
        long dim = atol(JSONLblVal(prop));
         // If data are invalid
        if (dim < 1)
               return false;
         // Allocate memory
         *that = VecFloatCreate(dim);
         // Get the values
         prop = JSONProperty(json, "_val");
         if (prop == NULL) {
             return false;
        for (long i = 0; i < dim; ++i) {
                float val = atof(JSONLabel(JSONValue(prop, i)));
                 VecSet(*that, i, val);
        \ensuremath{//} Return the success code
        return true;
 // Load the VecFloat from the stream
 // If the VecFloat is already allocated, it is freed before loading
bool _VecFloatLoad(VecFloat** that, FILE* const stream) {
#if BUILDMODE == 0
        if (that == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'that' is null");
                PBErrCatch(PBMathErr);
        if (stream == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'stream' is null");
                PBErrCatch(PBMathErr);
        }
#endif
        // Declare a json to load the encoded data % \left( 1\right) =\left( 1\right) \left( 
        JSONNode* json = JSONCreate();
         // Load the whole encoded data
        if (!JSONLoad(json, stream)) {
                return false;
         // Decode the data from the JSON
        if (!VecDecodeAsJSON(that, json)) {
```

```
return false;
 }
  // Free the memory used by the JSON
 JSONFree(&json);
  // Return the success code
 return true;
// Save the VecFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecFloatSave(const VecFloat* const that,
 FILE* const stream, const bool compact) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
 // Get the JSON encoding
  JSONNode* json = VecEncodeAsJSON(that);
  // Save the JSON
 if (!JSONSave(json, stream, compact)) {
   return false;
 // Free memory
 JSONFree(&json);
  // Return success code
 return true;
// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that) {
 // Check argument
 if (that == NULL || *that == NULL)
   return;
  // Free memory
 free(*that);
 *that = NULL;
// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(const VecFloat* const that, FILE* const stream,
 const unsigned int prec) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
```

```
PBErrCatch(PBMathErr);
  }
#endif
  // Create the format string
  char format[100] = {'\0'};
  sprintf(format, "%%.%df", prec);
  // Print the values
  fprintf(stream, "<");</pre>
  for (long i = 0; i < that->_dim; ++i) {
    fprintf(stream, format, that->_val[i]);
    if (i < that->_dim - 1)
      fprintf(stream, ",");
 fprintf(stream, ">");
}
// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
float _VecFloatAngleTo2D(const VecFloat2D* const that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(that), 1.0)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' is not a normed vector");
    PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(tho), 1.0)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'tho' is not a normed vector");
   PBErrCatch(PBMathErr);
 7
#endif
  // Declare a variable to memorize the result
  float theta = 0.0;
  // Calculate the angle
  VecFloat2D m = VecFloatCreateStatic2D();
  if (fabs(VecGet(that, 0)) > fabs(VecGet(that, 1))) {
    VecSet(&m, 0,
      (VecGet(tho, 0) + VecGet(tho, 1) * VecGet(that, 1) /
      VecGet(that, 0)) /
      (VecGet(that, 0) + fsquare(VecGet(that, 1)) / VecGet(that, 0)));
    VecSet(&m, 1,
      (VecGet(&m, 0) * VecGet(that, 1) - VecGet(tho, 1)) /
      VecGet(that, 0));
  } else {
    VecSet(&m, 1,
      (VecGet(tho, 0) - VecGet(tho, 1) * VecGet(that, 0) /
      VecGet(that, 1)) /
      (VecGet(that, 1) + fsquare(VecGet(that, 0)) / VecGet(that, 1)));
    VecSet(&m, 0,
      (VecGet(tho, 1) + VecGet(&m, 1) * VecGet(that, 0)) /
```

```
VecGet(that, 1));
  }
  // Due to numerical imprecision m[0] may be slightly out of [-1,1]
  \ensuremath{//} which makes acos return NaN, prevent this
  if (VecGet(\&m, 0) < -1.0)
    theta = PBMATH_PI;
  else if (VecGet(\&m, 0) > 1.0)
    theta = 0.0;
  else
    theta = acos(VecGet(&m, 0));
  if (\sin(\text{theta}) * \text{VecGet}(\&m, 1) > 0.0)
    theta *= -1.0;
  // Return the result
 return theta;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
VecFloat3D _VecFloatGetRotAxis(const VecFloat3D* const that,
  const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (axis == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'axis' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld=3)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
  if (VecGetDim(axis) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%1d=3)",
      VecGetDim(axis));
   PBErrCatch(PBMathErr);
  if (ISEQUALF(VecNorm(axis), 1.0) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' is not normalized");
    PBErrCatch(PBMathErr);
  7
#endif
  // Declare variable for optimisation
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  \ensuremath{//} Create the rotation matrix
  VecShort2D d = VecShortCreateStatic2D();
  VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = cosTheta + fastpow(VecGet(axis, 0), 2) * (1.0 - cosTheta);
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
```

```
v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) -
   VecGet(axis, 2) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 0);
 v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) +
   VecGet(axis, 1) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 1);
 v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) +
   VecGet(axis, 2) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 1);
 v = cosTheta + fastpow(VecGet(axis, 1), 2) * (1.0 - cosTheta);
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 1);
 v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) -
   VecGet(axis, 0) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 2);
 v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) -
   VecGet(axis, 1) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 2);
 v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) +
   VecGet(axis, 0) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 2);
 v = cosTheta + fastpow(VecGet(axis, 2), 2) * (1.0 - cosTheta);
 MatSet(rot, &d, v);
 // Calculate the result vector
 VecFloat* w = MatGetProdVec(rot, that);
 VecFloat3D res = VecFloatCreateStatic3D();
 VecCopy(&res, w);
 // Free memory
 VecFree(&w);
 MatFree(&rot):
 // Return the result
 return res;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(const VecFloat3D* const that,
 const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (VecGetDim(that) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
   sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%1d=3)",
     VecGetDim(that));
   PBErrCatch(PBMathErr);
 }
 // Declare variable for optimisation
 float cosTheta = cos(theta);
 float sinTheta = sin(theta);
 // Create the rotation matrix
 VecShort2D d = VecShortCreateStatic2D();
```

```
VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = 1.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
  v = 0.0:
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 1);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 1);
  v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = -sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 2);
  v = sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 2);
  v = cosTheta;
  MatSet(rot, &d, v);
  // Calculate the result vector
  VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = VecFloatCreateStatic3D();
  VecCopy(&res, w);
  // Free memory
  VecFree(&w);
  MatFree(&rot);
  // Return the result
 return res;
}
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(const VecFloat3D* const that,
  const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%1d=3)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Declare variable for optimisation
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  \ensuremath{//} Create the rotation matrix
  VecShort2D d = VecShortCreateStatic2D();
```

```
VecSet(&d, 0, 3); VecSet(&d, 1, 3);
 MatFloat* rot = MatFloatCreate(&d);
 VecSet(&d, 0, 0); VecSet(&d, 1, 0);
 float v = cosTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 0);
 v = 0.0:
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 0);
 v = sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 1);
 v = 0.0;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 1);
 v = 1.0;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = 0.0;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 2);
 v = -sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 2);
 v = 0.0;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 2);
 v = cosTheta;
 MatSet(rot, &d, v);
 // Calculate the result vector
 VecFloat* w = MatGetProdVec(rot, that);
 VecFloat3D res = VecFloatCreateStatic3D();
 VecCopy(&res, w);
 // Free memory
 VecFree(&w);
 MatFree(&rot);
 // Return the result
 return res;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Z
VecFloat3D _VecFloatGetRotZ(const VecFloat3D* const that,
 const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (VecGetDim(that) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%1d=3)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
 }
#endif
 // Declare variable for optimisation
 float cosTheta = cos(theta);
 float sinTheta = sin(theta);
 \ensuremath{//} Create the rotation matrix
 VecShort2D d = VecShortCreateStatic2D();
```

}

```
VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
  v = -sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 1);
  v = sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 1);
  v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 2);
  v = 1.0:
  MatSet(rot, &d, v);
  // Calculate the result vector
  VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = VecFloatCreateStatic3D();
  VecCopy(&res, w);
  // Free memory
  VecFree(&w);
  MatFree(&rot);
  // Return the result
 return res;
}
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper</pre>
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* const that,
  const VecFloat* const bound, const VecFloat* const delta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
    PBErrCatch(PBMathErr);
  if (delta == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'delta' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != bound->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'bound' 's dimensions don't match (%ld==%ld)",
      that->_dim, bound->_dim);
    PBErrCatch(PBMathErr);
  if (that->_dim != delta->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'delta' 's dimensions don't match (%ld==%ld)",
      that->_dim, delta->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = that->_dim - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > bound->_val[iDim] + PBMATH_EPSILON) {
      that->_val[iDim] = 0;
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
 return ret;
}
// Step the values of the vector incrementally by delta
\ensuremath{//} in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])</pre>
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* const that,
  const VecFloat* const from, const VecFloat* const to,
  const VecFloat* const delta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (from == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'from' is null");
```

```
PBErrCatch(PBMathErr);
  }
  if (that->_dim != from->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
      that->_dim, from->_dim);
    PBErrCatch(PBMathErr);
  if (to == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'to' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != to->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
      that->_dim, to->_dim);
    PBErrCatch(PBMathErr);
  if (delta == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != delta->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'delta' dimensions don't match (%ld==%ld)",
      that->_dim, delta->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  long iDim = that->_dim - 1;
  \ensuremath{//} Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > to->_val[iDim] + PBMATH_EPSILON) {
      that->_val[iDim] = from->_val[iDim];
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
 return ret;
// Return a new VecFloat as a copy of the VecFloat 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0.0
// If it is shrinked, values are discarded from the end of the vector
{\tt VecFloat*} \ \_{\tt VecFloatGetNewDim} ({\tt const} \ {\tt VecFloat*} \ {\tt const} \ {\tt long} \ {\tt dim}) \ \{
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
```

```
PBErrCatch(PBMathErr);
  }
  if (dim <= 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'dim' is invalid match (%ld>0)", dim);
   PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} If the new dimension is the same as the current one
  if (dim == VecGetDim(that)) {
   // Return the clone of the vector
    return VecClone(that);
  // Else, the new dimension is actually different
    // Declare the returned vector
    VecFloat* ret = VecFloatCreate(dim);
    // Copy the components
    for (long iAxis = MIN(VecGetDim(that), dim); iAxis--;)
      VecSet(ret, iAxis, VecGet(that, iAxis));
    // Return the new vector
    return ret;
// ----- MatFloat
// ======== Define ========
// ====== Functions implementation =======
// Create a new MatFloat of dimension 'dim' (nbcol, nbline)
// Values are initalized to 0.0
MatFloat* MatFloatCreate(const VecShort2D* const dim) {
#if BUILDMODE == 0
  if (dim == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'dim' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Allocate memory
  long d = VecGet(dim, 0) * VecGet(dim, 1);
  MatFloat* that = PBErrMalloc(PBMathErr, offsetof(MatFloat, _val) +
    sizeof(float) * d);
  // Set the dimensions
  *(VecShort2D*)&(that->_dim) = *dim;
  // Set the default values
  for (long i = d; i--;)
    that->_val[i] = 0.0;
  // Return the new MatFloat
 return that;
// Clone the MatFloat
MatFloat* _MatFloatClone(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
```

```
// Create a clone
  MatFloat* clone = MatFloatCreate(&(that->_dim));
  // Copy the values
  long d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
  for (long i = d; i--;)
    clone->_val[i] = that->_val[i];
  // Return the clone
  return clone;
// Function which return the JSON encoding of 'that'
JSONNode* _MatFloatEncodeAsJSON(MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the JSON structure
  JSONNode* json = JSONCreate();
  // Declare a buffer to convert value into string
  char val[100];
  // Encode the dimensions
  sprintf(val, "%d", VecGet(&(that->_dim), 0));
JSONAddProp(json, "_nbRow", val);
sprintf(val, "%d", VecGet(&(that->_dim), 1));
JSONAddProp(json, "_nbCol", val);
  // Encode the values
  JSONArrayVal setVal = JSONArrayValCreateStatic();
  VecShort2D index = VecShortCreateStatic2D();
  do {
    sprintf(val, "%f", MatGet(that, &index));
    JSONArrayValAdd(&setVal, val);
  } while (VecStep(&index, &(that->_dim)));
  JSONAddProp(json, "_val", &setVal);
  // Free memory
  JSONArrayValFlush(&setVal);
  // Return the created JSON
  return json;
// Function which decode from JSON encoding 'json' to 'that'
bool _MatFloatDecodeAsJSON(MatFloat** that, JSONNode* json) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (json == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'json' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // If 'that' is already allocated
  if (*that != NULL)
    // Free memory
    _MatFloatFree(that);
  // Get the dimensions from the JSON
  JSONNode* prop = JSONProperty(json, "_nbRow");
```

```
if (prop == NULL) {
               return false;
        VecShort2D dim = VecShortCreateStatic2D();
        VecSet(&dim, 0, atoi(JSONLblVal(prop)));
        prop = JSONProperty(json, "_nbCol");
        if (prop == NULL) {
              return false;
        VecSet(&dim, 1, atoi(JSONLblVal(prop)));
        // If data are invalid
        if (VecGet(\&dim, 0) < 1 \mid | VecGet(\&dim, 1) < 1)
               return false;
        // Allocate memory
        *that = MatFloatCreate(&dim);
        // Get the values
        prop = JSONProperty(json, "_val");
        if (prop == NULL) {
             return false;
        VecShort2D index = VecShortCreateStatic2D();
        int i = 0;
        do {
                MatSet(*that, &index, atof(JSONLabel(JSONValue(prop, i))));
        } while (VecStep(&index, &dim));
        // Return the success code
      return true;
// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream) {
#if BUILDMODE == 0
        if (that == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'that' is null");
               PBErrCatch(PBMathErr);
        }
        if (stream == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                 sprintf(PBMathErr->_msg, "'stream' is null");
               PBErrCatch(PBMathErr);
#endif
        // Declare a json to load the encoded data % \left( 1\right) =\left( 1\right) \left( 
        JSONNode* json = JSONCreate();
        // Load the whole encoded data
        if (!JSONLoad(json, stream)) {
             return false;
        // Decode the data from the JSON
        if (!MatDecodeAsJSON(that, json)) {
             return false;
        // Free the memory used by the JSON
        JSONFree(&json);
        // Return the success code
        return true;
```

```
// Save the MatFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true upon success, else false
bool _MatFloatSave(MatFloat* const that, FILE* stream, bool compact) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
  // Get the JSON encoding
  JSONNode* json = MatEncodeAsJSON(that);
  // Save the JSON
  if (!JSONSave(json, stream, compact)) {
   return false;
  // Free memory
  JSONFree(&json);
  // Return success code
  return true;
// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that) {
  // Check argument
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  free(*that);
  *that = NULL;
}
// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* const that, FILE* stream, unsigned int prec) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the format string
  char format[100] = {'\0'};
  sprintf(format, "%% .%df", prec);
  // Print the values
  fprintf(stream, "[");
  VecShort2D index = VecShortCreateStatic2D();
```

```
if (VecGet(&index, 1) != 0 || VecGet(&index, 0) != 0)
      fprintf(stream, " ");
    fprintf(stream, format, MatGet(that, &index));
    if (VecGet(\&index, 0) < VecGet(\&(that->_dim), 0) - 1)
      fprintf(stream, ",");
    if (VecGet(&index, 0) == VecGet(&(that->_dim), 0) - 1) {
      if (VecGet(&index, 1) == VecGet(&(that->_dim), 1) - 1)
        fprintf(stream, "]");
      fprintf(stream, "\n");
 } while (VecPStep(&index, &(that->_dim)));
// Return the inverse matrix of 'that'
// The matrix must be a square matrix
// Return NULL if the matrix is not invertible, or in some case when
// the matrix's diagonal contains null values and the matrix's size
// is greater than 3
MatFloat* _MatFloatGetInv(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(\&(that->_dim), 0) != VecGet(\&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "the\ matrix\ is\ not\ square\ (\%dx\%d)",}
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  }
#endif
  // Allocate memory for the result
  MatFloat* res = NULL;
  // If the matrix is of dimension 1x1
  if (VecGet(\&(that->_dim), 0) == 1) {
    if (fabs(that->_val[0]) > PBMATH_EPSILON) {
      // Allocate memory for the result
      res = MatFloatCreate(&(that->_dim));
      res->_val[0] = 1.0 / that->_val[0];
  // If the matrix is of dimension 2x2
  } else if (VecGet(\&(that->_dim), 0) == 2) {
    float det = that->_val[0] * that->_val[3] -
      that->_val[2] * that->_val[1];
    if (!ISEQUALF(det, 0.0)) {
      // Allocate memory for the result
      res = MatFloatCreate(&(that->_dim));
      res->_val[0] = that->_val[3] / det;
      res->_val[1] = -1.0 * that->_val[1] / det;
      res->_val[2] = -1.0 * that->_val[2] / det;
      res->_val[3] = that->_val[0] / det;
   }
  // Else, the matrix dimension is 3x3
  } else if (VecGet(\&(that->_dim), 0) == 3) {
    float det =
      that->_val[0] *
        (that->_val[4] * that->_val[8] -
        that->_val[5] * that->_val[7]) -
      that->_val[3] *
        (that->_val[1] * that->_val[8] -
        that->_val[2] * that->_val[7]) +
```

```
that->_val[6] *
      (that->_val[1] * that->_val[5] -
      that->_val[2] * that->_val[4]);
  if (!ISEQUALF(det, 0.0)) {
    // Allocate memory for the result
   res = MatFloatCreate(&(that->_dim));
   res->_val[0] = (that->_val[4] * that->_val[8] -
        that->_val[5] * that->_val[7]) / det;
   res->_val[1] = -(that->_val[1] * that->_val[8] -
        that->_val[2] * that->_val[7]) / det;
    res->_val[2] = (that->_val[1] * that->_val[5] -
        that->_val[2] * that->_val[4]) / det;
    res->_val[3] = -(that->_val[3] * that->_val[8] -
       that->_val[5] * that->_val[6]) / det;
   res->_val[4] = (that->_val[0] * that->_val[8] -
        that->_val[2] * that->_val[6]) / det;
   res->_val[5] = -(that->_val[0] * that->_val[5] -
        that->_val[2] * that->_val[3]) / det;
    res->_val[6] = (that->_val[3] * that->_val[7] -
        that->_val[4] * that->_val[6]) / det;
   res->_val[7] = -(that->_val[0] * that->_val[7] -
       that->_val[1] * that->_val[6]) / det;
    res->_val[8] = (that->_val[0] * that->_val[4] -
        that->_val[1] * that->_val[3]) / det;
 }
} else {
  // Clone the matrix to be inverted
  res = MatClone(that);
  // Farooq Hamid algorithm (modified to handle some matrix with null
  // values on the diagonal)
  // https://www.researchgate.net/publication/
  // 220337322_An_Efficient_and_Simple_Algorithm_for_Matrix_Inversion
  //float det = 1.0;
  short size = VecGet(&(that->_dim), 0);
  float* mat = res->_val;
  bool flagHasChanged = true;
  short nbRemaining = size;
  bool* hasPivotChanged = PBErrMalloc(PBMathErr, size * sizeof(bool));
  for(short p = 0; p < size; ++p) {
   hasPivotChanged[p] = false;
  while (flagHasChanged == true && nbRemaining > 0) {
   flagHasChanged = false;
    for(short p = 0; p < size; ++p) {</pre>
      float pivot = mat[p * size + p];
      if (!ISEQUALF(pivot, 0.0) && !(hasPivotChanged[p])) {
        flagHasChanged = true;
        --nbRemaining;
        hasPivotChanged[p] = true;
        //det *= pivot;
        for (short i = 0; i < size; ++i) {</pre>
         mat[i * size + p] = -1.0 * mat[i * size + p] / pivot;
        for (short i = 0; i < size; ++i) {</pre>
          if (i != p) {
            for (short j = 0; j < size; ++j) {
              if (j != p) {
                mat[i * size + j] =
                  mat[i * size + j] + mat[p * size + j] * mat[i * size + p];
              }
           }
```

```
for (short j = 0; j < size; ++j) {
           mat[p * size + j] = mat[p * size + j] / pivot;
          mat[p * size + p] = 1.0 / pivot;
     }
   }
    free(hasPivotChanged);
    if (nbRemaining > 0) {
     MatFree(&res);
     return NULL;
 // Return the result
 return res;
// Return the product of matrix 'that' and vector 'v'
// Number of colum of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(
 const MatFloat* const that, const VecFloat* v) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (v == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'v' is null");
   PBErrCatch(PBMathErr);
 if (VecGet(\&(that->_dim), 0) != VecGetDim(v)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "the matrix and vector have incompatible dimensions (d==1d)",
      VecGet(&(that->_dim), 0), VecGetDim(v));
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to memorize the index in the matrix
  VecShort2D i = VecShortCreateStatic2D();
  // Allocate memory for the solution
 VecFloat* ret = VecFloatCreate(VecGet(&(that->_dim), 1));
 // If we could allocate memory
 if (ret != NULL)
    for \ (VecSet(\&i,\ 0,\ 0);\ VecGet(\&i,\ 0)\ <\ VecGet(\&(that->\_dim),\ 0);\ VecSetAdd(\&i,\ 0,\ 1))
     for (VecSet(&i, 1, 0); VecGet(&i, 1) < VecGet(&(that->_dim), 1); VecSetAdd(&i, 1, 1))
        VecSetAdd(ret, VecGet(&i, 1),
          VecGet(v, VecGet(&i, 0)) * MatGet(that, &i));
  // Return the result
 return ret;
// Return the product of vector 'v' and transpose of vector 'w'
MatFloat* _MatFloatGetProdVecVecTransposeFloat(
 const VecFloat* const v,
 const VecFloat* const w) {
#if BUILDMODE == 0
 if (v == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'v' is null");
   PBErrCatch(PBMathErr);
 if (w == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'w' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to memorize the position in the matrix
  VecShort2D pos = VecShortCreateStatic2D();
  // Allocate memory for the solution
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, VecGetDim(w));
  VecSet(&dim, 1, VecGetDim(v));
 MatFloat* ret = MatFloatCreate(&dim);
 // Calculate the result
 do {
    MatSet(ret, &pos,
      VecGet(v, VecGet(&pos, 1)) * VecGet(w, VecGet(&pos, 0)));
  } while(VecStep(&pos, &dim));
  // Return the result
 return ret;
// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(const MatFloat* const that, const MatFloat* tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (VecGet(\&(that->_dim), 0) != VecGet(\&(tho->_dim), 1)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "the matrices have incompatible dimensions (%d==%d)",
      VecGet(&(that->_dim), 0), VecGet(&(tho->_dim), 1));
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare 3 variables to memorize the index in the matrix
 VecShort2D i = VecShortCreateStatic2D();
 VecShort2D j = VecShortCreateStatic2D();
  VecShort2D k = VecShortCreateStatic2D();
  // Allocate memory for the solution
  VecSet(&i, 0, VecGet(&(tho->_dim), 0));
  VecSet(&i, 1, VecGet(&(that->_dim), 1));
 MatFloat* ret = MatFloatCreate(&i);
  for (VecSet(&i, 0, 0); VecGet(&i, 0) < VecGet(&(tho->_dim), 0); VecSetAdd(&i, 0, 1))
    for (VecSet(&i, 1, 0); VecGet(&i, 1) < VecGet(&(that->_dim), 1); VecSetAdd(&i, 1, 1))
      for (VecSet(\&j, 0, 0), VecSet(\&j, 1, VecGet(\&i, 1)),
        VecSet(&k, 0, VecGet(&i, 0)), VecSet(&k, 1, 0);
        VecGet(&j, 0) < VecGet(&(that->_dim), 0);
        VecSetAdd(&j, 0, 1),
        VecSetAdd(&k, 1, 1)) {
```

```
MatSet(ret, &i, MatGet(ret, &i) +
          MatGet(that, &j) * MatGet(tho, &k));
  // Return the result
 return ret;
// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* const that, MatFloat* tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 if (!VecIsEqual(&(that->_dim), &(tho->_dim)))
   return false;
 VecShort2D v = VecShortCreateStatic2D();
 do {
    if (!ISEQUALF(MatGet(that, &v), MatGet(tho, &v)))
     return false;
 } while (VecStep(&v, &(that->_dim)));
 return true;
// Calculate the Eigen values and vectors of the MatFloat 'that'
// Return a set of VecFloat. The first VecFloat of the set contains
// the Eigen values, with values sorted from biggest to
// smallest (in absolute value). The following VecFloat are the
// respectiev Eigen vectors
// 'that' must be a 2D square matrix
// Return the identity if the QR decompostion fails
// http://madrury.github.io/jekyll/update/statistics/2017/10/04/qr-algorithm.html
// TODO: should be improved with the Hessenberg QR method
// https://www.math.kth.se/na/SF2524/matber15/qrmethod.pdf
GSetVecFloat _MatFloatGetEigenValues(const MatFloat* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (VecGet(MatDim(that), 0) != VecGet(MatDim(that), 1)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' is not squared");
   PBErrCatch(PBMathErr);
 }
#endif
 \ensuremath{//} Declare the result set
 GSetVecFloat set = GSetVecFloatCreateStatic();
  // Clone the original matrix
 MatFloat* A = MatClone(that);
  // Create a matrix to compute the Eigen vectors
 MatFloat* Q = MatFloatCreate(MatDim(that));
 MatSetIdentity(Q);
  // Apply the QR algorithm
```

```
VecShort2D pos = VecShortCreateStatic2D();
  float err = 0.0;
  do {
   QRDecomp QR = MatGetQR(A);
    if (QR._Q != NULL) {
     MatFloat* RQ = MatGetProdMat(QR._R, QR._Q);
     MatFree(&A);
      A = RQ;
     MatFloat* M = MatGetProdMat(Q, QR._Q);
     MatFree(&Q);
     Q = M;
     err = 0.0;
     do {
       if (VecGet(&pos, 0) != VecGet(&pos, 1))
          err = MAX(err, fabs(MatGet(A, &pos)));
     } while (VecStep(&pos, MatDim(A)));
     QRDecompFreeStatic(&QR);
    } else {
     MatSetIdentity(A);
     MatSetIdentity(Q);
     err = 0.0;
 } while (err > PBMATH_EPSILON);
  // Extract the results
  VecFloat* values = VecFloatCreate(MatGetNbCol(that));
 GSetPush(&set, values);
  for (int i = 0; i < MatGetNbCol(that); ++i) {</pre>
    VecSet(&pos, 0, i);
    VecSet(&pos, 1, i);
    VecSet(values, i, MatGet(A, &pos));
   GSetAppend(&set, VecFloatCreate(MatGetNbCol(that)));
 VecSetNull(&pos);
 do {
    VecSet(GSetGet(&set, 1 + VecGet(&pos, 0)), VecGet(&pos, 1),
     MatGet(Q, &pos));
  } while (VecStep(\&pos, MatDim(Q)));
  // Free memory
 MatFree(&A);
 MatFree(&Q);
 // Return the result
 return set;
// Calculate the QR decomposition of the MatFloat 'that' using the
// Householder algorithm
// Return {NULL, NULL} if the MatFloat couldn't be decomposed
// http://www.seas.ucla.edu/~vandenbe/133A/lectures/qr.pdf
QRDecomp _MatFloatGetQR(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (MatGetNbCol(that) > MatGetNbRow(that)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' must have at least as many rows as columns (d<=d)",
     MatGetNbCol(that), MatGetNbRow(that));
   PBErrCatch(PBMathErr);
```

```
#endif
```

```
// Allocate memory for the final R matrix
VecShort2D dimR = VecShortCreateStatic2D();
VecSet(&dimR, 0, MatGetNbCol(that));
VecSet(&dimR, 1, MatGetNbCol(that));
MatFloat* R = MatFloatCreate(&dimR);
// Allocate memory for the final Q matrix
MatFloat* Q = MatFloatCreate(MatDim(that));
// Allocate memory for the QQ^{\sim} matrix
VecShort2D dimQQtilde = VecShortCreateStatic2D();
VecSet(&dimQQtilde, 0, MatGetNbRow(that));
VecSet(&dimQQtilde, 1, MatGetNbRow(that));
MatFloat* QQtilde = MatFloatCreate(&dimQQtilde);
MatSetIdentity(QQtilde);
// Create a clone of that to be overwritten during computation
MatFloat* A = MatClone(that);
// Declare two vectors to access value in the arrays
VecShort2D pos = VecShortCreateStatic2D();
VecShort2D shiftPos = VecShortCreateStatic2D();
// Householder algorithm
for (short k = 0; k < MatGetNbCol(that); ++k) {</pre>
  // Calculate w
  VecFloat* w = VecFloatCreate(MatGetNbRow(that) - k);
  VecSet(&pos, 0, k);
  for (short i = 0; i < VecGetDim(w); ++i) {</pre>
   VecSet(&pos, 1, k + i);
   VecSet(w, i, MatGet(A, &pos));
  if(ISEQUALF(VecNorm(w), 0.0)) {
   MatFree(&R);
   MatFree(&Q);
   MatFree(&QQtilde);
   MatFree(&A);
   VecFree(&w);
   return (QRDecomp){._Q = NULL, ._R = NULL};
  float sign = (VecGet(w, 0) >= 0.0 ? 1.0 : -1.0);
  VecSet(w, 0, VecGet(w, 0) + sign * VecNorm(w));
  // Calculate v = w / ||w||
  VecFloat* v = VecClone(w);
  VecNormalise(v);
                             I O
  // Calculate the reflector O H where H = I - 2vv^t
  VecShort2D dimH = VecShortCreateStatic2D();
  VecSet(&dimH, 0, VecGetDim(v));
  VecSet(&dimH, 1, VecGetDim(v));
  MatFloat* H = MatFloatCreate(&dimH);
  MatSetIdentity(H);
  MatFloat* vvt = MatGetProdVecVecTranspose(v, v);
  MatScale(vvt, -2.0);
  MatAdd(H, vvt);
  MatFloat* reflector = MatFloatCreate(&dimQQtilde);
  MatSetIdentity(reflector);
```

```
VecSetNull(&pos);
    do {
      VecSet(&shiftPos, 0, VecGet(&pos, 0) + k);
      VecSet(&shiftPos, 1, VecGet(&pos, 1) + k);
      MatSet(reflector, &shiftPos, MatGet(H, &pos));
    } while (VecStep(&pos, &dimH));
    // Update A := reflector . A
    MatFloat* M = MatGetProdMat(reflector, A);
    MatFree(&A);
    A = M;
    // Update QQtilde := QQtilde.reflector
    M = MatGetProdMat(QQtilde, reflector);
    MatFree(&QQtilde);
    QQtilde = M;
    // Free memory
    MatFree(&reflector);
    MatFree(&H);
    MatFree(&vvt);
    VecFree(&v);
    VecFree(&w);
  // Extract R from the final A
  VecSetNull(&pos);
  do {
   MatSet(R, &pos, MatGet(A, &pos));
  } while (VecStep(&pos, &dimR));
  // Extract Q from the final QQtilde
  VecSetNull(&pos);
  do {
    MatSet(Q, &pos, MatGet(QQtilde, &pos));
  } while (VecStep(&pos, MatDim(that)));
  // Create the result QR decomposition
  QRDecomp qr = \{._Q = Q, ._R = R\};
  // Free memory
  MatFree(&A);
  MatFree(&QQtilde);
  // Return the decomposition
  return qr;
// Calculate the transposed of the MatFloat 'that'
MatFloat* _MatFloatGetTranspose(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Allocate memory for the result matrix
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, VecGet(MatDim(that), 1));
VecSet(&dim, 1, VecGet(MatDim(that), 0));
  MatFloat* res = MatFloatCreate(&dim);
```

```
// Calculate the transposed matrix
  VecShort2D pos = VecShortCreateStatic2D();
  VecShort2D posB = VecShortCreateStatic2D();
  do {
    VecSet(&posB, 0, VecGet(&pos, 1));
    VecSet(&posB, 1, VecGet(&pos, 0));
   MatSet(res, &pos, MatGet(that, &posB));
  } while (VecStep(&pos, &dim));
  // Return the transposed matrix
 return res;
// ----- Gauss
// ======== Define ========
// ======== Functions implementation ===========
// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(const float mean, const float sigma) {
  // Allocate memory
  Gauss *that = PBErrMalloc(PBMathErr, sizeof(Gauss));
  // Set properties
  that->_mean = mean;
  that->_sigma = sigma;
  // Return the new Gauss
  return that;
Gauss GaussCreateStatic(const float mean, const float sigma) {
  // Allocate memory
  Gauss that = {._mean = mean, ._sigma = sigma};
  // Return the new Gauss
 return that;
// Free the memory used by a Gauss
// Do nothing if arguments are invalid
void GaussFree(Gauss** that) {
  // Check argument
  if (that == NULL || *that == NULL)
   return;
  // Free memory
  free(*that);
  *that = NULL;
// ----- SysLinEq
// ======= Functions implementation ==========
// Create a new SysLinEq with matrix 'm' and vector 'v'
// The dimension of 'v' must be equal to the number of column of 'm'
// If 'v' is null the vector null is used instead
// The matrix 'm' must be a square matrix
// Return NULL if we couldn't create the SysLinEq
SysLinEq* _SLECreate(const MatFloat* const m, const VecFloat* const v) {
#if BUILDMODE == 0
  if (m == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'m' is null");
```

```
PBErrCatch(PBMathErr);
  }
  if (VecGet(\&(m->_dim), 0) != VecGet(\&(m->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "the\ matrix\ is\ not\ square\ (\%dx\%d)",}
      VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1));
    PBErrCatch(PBMathErr);
  }
  if (v != NULL) {
    if (VecGet(\&(m->_dim), 0) != VecGetDim(v)) {
      PBMathErr->_type = PBErrTypeInvalidArg;
      sprintf(PBMathErr->_msg,
        "the matrix and vector have incompatible dimensions (%d==%1d)",
        VecGet(&(m->_dim), 0), VecGetDim(v));
      PBErrCatch(PBMathErr);
  }
#endif
  // Allocate memory
  SysLinEq* that = PBErrMalloc(PBMathErr, sizeof(SysLinEq));
  that->_M = MatClone(m);
  that->_Minv = MatGetInv(that->_M);
  if (v != NULL)
    that->_V = VecClone(v);
  else
    that->_V = VecFloatCreate(VecGet(&(m->_dim), 0));
  if (that->_M == NULL || that->_V == NULL || that->_Minv == NULL) {
#if BUILDMODE == 0
    if (that->_M == NULL) {
      PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't create the matrix");
      PBErrCatch(PBMathErr);
    if (that->_Minv == NULL) {
      PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
      PBErrCatch(PBMathErr);
    if (that->_V == NULL) {
      PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't create the vector");
      PBErrCatch(PBMathErr);
    }
#endif
    SysLinEqFree(&that);
  // Return the new SysLinEq
  return that;
// Free the memory used by the SysLinEq
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that) {
  // Check arguments
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  MatFree(&((*that)->_M));
  MatFree(&((*that)->_Minv));
  VecFree(&((*that)->_V));
  free(*that);
  *that = NULL;
```

```
}
// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(const SysLinEq* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the result
  SysLinEq* ret = PBErrMalloc(PBMathErr, sizeof(SysLinEq));
  ret->_M = MatClone(that->_M);
  ret->_Minv = MatClone(that->_Minv);
 ret->_V = VecClone(that->_V);
  if (ret->_M == NULL || ret->_V == NULL || ret->_Minv == NULL)
    SysLinEqFree(&ret);
  // Return the new SysLinEq
  return ret;
// ---- Ratio
// ====== Functions implementation =========
// Create a new static Ratio
#if BUILDMODE == 0
  if (d == 0) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'d' is invalid (%u > 0)", d);
   PBErrCatch(PBMathErr);
#endif
  // Create the Ratio
  Ratio ratio = {
    .\_base = b,
    ._numerator = n,
    ._denominator = d
  // Return the Ratio
 return ratio;
// Convert the float 'v' into the nearest Ratio using the Farey's algorithm
// given the precision 'prec'
Ratio RatioFromFloatPrec(float v, float prec) {
  // Create the two bounding Ratio
  Ratio ratioLow = RatioCreateStatic(0, 0, 1);
  Ratio ratioHigh = RatioCreateStatic(0, 1, 1);
  // Create the result ratio
  Ratio ratio = RatioCreateStatic(floor(v), 0, 1);
  // Get the decimals of 'v'
  float dec = v - RatioGetBase(&ratio);
```

```
\ensuremath{//} Loop until the bounding Ratio reachs the requested precision
  Ratio mediant;
  while(
    RatioToFloat(&ratioHigh) - RatioToFloat(&ratioLow) > prec &&
    fabs(RatioToFloat(&ratioHigh) - dec) > prec &&
    fabs(RatioToFloat(&ratioLow) - dec) > prec) {
    mediant = RatioCreateStatic(0,
      RatioGetNumerator(&ratioLow) + RatioGetNumerator(&ratioHigh),
      RatioGetDenominator(&ratioLow) + RatioGetDenominator(&ratioHigh));
    if (RatioToFloat(&mediant) > dec) {
      ratioHigh = mediant;
    } else {
      ratioLow = mediant;
    }
  }
  // Update the fractional part of the result
  if (fabs(RatioToFloat(&ratioHigh) - dec) <= prec) {</pre>
    RatioSetNumerator(&ratio, RatioGetNumerator(&ratioHigh));
    RatioSetDenominator(&ratio, RatioGetDenominator(&ratioHigh));
  } else if (fabs(RatioToFloat(&ratioLow) - dec) <= prec) {</pre>
    RatioSetNumerator(&ratio, RatioGetNumerator(&ratioLow));
    RatioSetDenominator(&ratio, RatioGetDenominator(&ratioLow));
  } else {
    RatioSetNumerator(&ratio, RatioGetNumerator(&mediant));
    RatioSetDenominator(&ratio, RatioGetDenominator(&mediant));
  // Reduce the result
  RatioReduce(&ratio);
  // Return the result
  return ratio;
// Convert the Ratio 'that' into a float
float RatioToFloat(const Ratio* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the Ratio converted to float
  return (float)RatioGetBase(that) +
    (float)RatioGetNumerator(that) / (float)RatioGetDenominator(that);
```

}

```
}
// Reduce the fractional part of the Ratio 'that' and update the base such as
// numerator < denominator</pre>
void RatioReduce(Ratio* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // If the numerator is greater than the denominator
  if (RatioGetNumerator(that) >= RatioGetDenominator(that)) {
    // Update the component to keep the fractional part less than 1.0
    unsigned int delta = RatioGetNumerator(that) / RatioGetDenominator(that);
    RatioSetBase(that, RatioGetBase(that) + delta);
    RatioSetNumerator(that.
      RatioGetNumerator(that) - delta * RatioGetDenominator(that));
  }
  // Get the GCD of the numerator and denominator
  unsigned int div = GetGCD(
    RatioGetNumerator(that), RatioGetDenominator(that));
  // Divide the numerator and denominator by the gcd
  RatioSetNumerator(that, RatioGetNumerator(that) / div);
  RatioSetDenominator(that, RatioGetDenominator(that) / div);
}
// Print the Ratio on 'stream' as a+b/c
void RatioPrint(const Ratio* that, FILE* stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  fprintf(stream, "%ld+%u/%u",
    RatioGetBase(that), RatioGetNumerator(that), RatioGetDenominator(that));
// ----- Usefull basic functions
// ====== Functions implementation =========
// Compute the 'iElem'-th element of the 'base'-ary version of the
// Thue-Morse sequence
// 'iElem' >= 0
// 'base' >= 2
long ThueMorseSeqGetNthElem(long iElem, long base) {
```

```
#if BUILDMODE == 0
  if (iElem < 0) \{
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'iElem' is invalid (%ld>=0)", iElem);
    PBErrCatch(PBMathErr);
  if (base < 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'base' is invalid (%ld>=2)", base);
    PBErrCatch(PBMathErr);
#endif
  if (base > iElem) {
   return iElem;
  } else {
    ldiv_t d = ldiv(iElem, base);
    return (ThueMorseSeqGetNthElem(d.quot, base) + d.rem) % base;
 }
// Return a set of two vectors containing the bounds of the vectors in
// the GSet 'that'
// The set must have at least one element
// The returned set is ordered as follow: (boundMin, boundMax)
GSetVecFloat _GSetVecFloatGetBounds(const GSetVecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (GSetNbElem(that) < 1) {</pre>
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' is empty");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the set containing the bounds
  GSetVecFloat bounds = GSetVecFloatCreateStatic();
  // Create the two bounds vector, initialised with the first vector of
  // the set
  VecFloat* boundMin = _VecFloatClone(GSetGet(that, 0));
  VecFloat* boundMax = _VecFloatClone(GSetGet(that, 0));
  GSetAppend(&bounds, boundMin);
  GSetAppend(&bounds, boundMax);
  // Get the dimension of the vectors, supposes they are all with same
  // dimension
  long dim = _VecFloatGetDim(boundMin);
  // Loop on the vectors of the set, expect the first one
  GSetIterForward iter = GSetIterForwardCreateStatic(that);
  while (GSetIterStep(&iter)) {
    VecFloat* v = GSetIterGet(&iter);
    // Loop on dimension
    for (int iDim = dim; iDim--;) {
      // Update bounds
      if (_VecFloatGet(boundMin, iDim) > _VecFloatGet(v, iDim))
        _VecFloatSet(boundMin, iDim, _VecFloatGet(v, iDim));
      if (_VecFloatGet(boundMax, iDim) < _VecFloatGet(v, iDim))</pre>
        _VecFloatSet(boundMax, iDim, _VecFloatGet(v, iDim));
    }
  }
  // Return the set containing the bounds
```

```
return bounds;
}
// Compute the area of a triangle knowing its 3 sides length 'a', 'b', 'c'
// using the Hero's formula
double GetAreaTriangleHero(
  const double a,
  const double b,
  const double c) {
  double s = 0.5 * (a + b + c);
  double area = sqrt(s * (s - a) * (s - b) * (s - c));
  return area;
}
// Return the Fibonacci sequence up to the 'n'-th element in a dynamically
\//\ {\it allocated\ array\ of\ unsigned\ long}
unsigned long* GetFibonacciSeq(unsigned int n) {
  if (n == 0) {
    return NULL;
  } else {
    unsigned long* seq =
      PBErrMalloc(
        PBMathErr,
        sizeof(unsigned long) * n);
    for (
      unsigned int i = 0;
      i < n && i < 2;
      ++i) {
      seq[i] = 1L;
    for (
      unsigned int i = 2;
      i < n;
      ++i) {
      seq[i] = seq[i - 1] + seq[i - 2];
    }
    return seq;
  }
}
// Return the Fibonacci grid lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [0,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciGridLattice(
    unsigned int n,
  unsigned long* nbPoints) {
#if BUILDMODE == 0
```

```
if (nbPoints == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'nbPoints' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  if (n == 0) {
    *nbPoints = 0;
    return NULL;
  } else {
    // Get the Fibonacci sequence
    unsigned long* seq = GetFibonacciSeq(n);
    // Update the number of points
    *nbPoints = seq[n - 1];
    // Allocate memory for the result
    float* lattice =
      PBErrMalloc(
        PBMathErr,
        sizeof(float) * 2L * (*nbPoints));
    // Generate the lattice points
    for (
      unsigned long iPoint = 0;
      iPoint < *nbPoints;</pre>
      ++iPoint) {
      lattice[iPoint * 2L] =
        fmodf(
          (float)iPoint / (float)seq[n > 1 ? n - 1 : 0],
          1.0);
      lattice[iPoint * 2L + 1L] =
        fmodf(
          (float)iPoint * (float)seq[n > 2 ? n - 2 : 0] /
            (float)seq[n > 1 ? n - 1 : 0],
          1.0);
    }
    // Free memory
    free(seq);
    // Return the lattice
    return lattice;
}
// Return the Fibonacci polar lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [-1,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciPolarLattice(
    unsigned int n,
```

```
unsigned long* nbPoints) {
#if BUILDMODE == 0
  if (nbPoints == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'nbPoints' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Get the grid lattice
  float* lattice =
    GetFibonacciGridLattice(
      n,
      nbPoints);
  // Convert each points to polar coordinates
  for (
    unsigned long iPoint = *nbPoints;
    iPoint--;) {
    lattice[iPoint * 2L] = sqrt(lattice[iPoint * 2L]);
    lattice[iPoint * 2L + 1L] = 2.0 * PBMATH_PI * lattice[iPoint * 2L + 1L];
  // Return the lattice
  return lattice;
}
// Return the greatest common divisor using the Stein's algorithm
// https://en.wikipedia.org/wiki/Binary_GCD_algorithm
unsigned int GetGCD(unsigned int u, unsigned int v) {
    unsigned int shift = 0;
    if (u == 0)
     return v;
    if (v == 0)
     return u;
    while (((u \mid v) \& 1) == 0) \{
       ++shift;
        u >>= 1;
        v >>= 1;
    while ((u \& 1) == 0)
       u >>= 1;
    do {
        while ((v \& 1) == 0)
           v >>= 1;
        if (u > v) {
           unsigned int t = v;
            v = u;
            u = t;
        }
        v -= u;
    } while (v != 0);
    return u << shift;
```

```
}
// ----- LeastSquareLinReg
// ======== Functions implementation ==========
// Create a new static LeastSquareLinReg
LeastSquareLinReg LeastSquareLinRegCreateStatic(MatFloat* X) {
#if BUILDMODE == 0
  if (X == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'X' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare the new LeastSquareLin
  LeastSquareLinReg that;
  \ensuremath{//} Set the properties
  that.Xp = NULL;
  LSLRSetComp(
    &that,
   X);
  that.bias = 0.0;
  // Return the new LeastSquareLin
  return that;
// Free the static LeastSquareLinReg 'that'
void LeastSquareLinRegFreeStatic(LeastSquareLinReg* that) {
  if (that == NULL) {
    return;
  // Free memory
  MatFree(&(that->Xp));
// Compute the solution of the LeastSquareLinReg 'that' for 'Y'
VecFloat* LSLRSolve(LeastSquareLinReg* that, const VecFloat* Y) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (that->X == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'that->X' is null");
   PBErrCatch(PBMathErr);
  if (that->Xp == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'that->Xp' is null");
   PBErrCatch(PBMathErr);
  if (Y == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'Y' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Get the result
  VecFloat* beta =
   MatGetProdVec(
     that->Xp,
     Y);
  // Calculate the bias
  VecFloat* Ybeta =
   MatGetProdVec(
     that->X,
     beta);
  VecOp(
   Ybeta,
   1.0,
   Υ,
   -1.0);
  that->bias = VecNorm(Ybeta);
  VecFree(&Ybeta);
  // Return the result
 return beta;
}
        pbmath-inline.c
// ======= PBMATH_static inline.C =========
// ======== Functions implementation ===========
// ----- VecShort
```

}

```
// Static constructors for VecShort
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecShortCreateStatic2D() {
  VecShort2D v = \{.\_val = \{0, 0\}, .\_dim = 2\};
 return v;
}
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecShortCreateStatic3D() {
  VecShort3D v = \{.\_val = \{0, 0, 0\}, .\_dim = 3\};
 return v:
}
#if BUILDMODE != 0
static inline
#endif
VecShort4D VecShortCreateStatic4D() {
 VecShort4D v = {._val = {0, 0, 0, 0}, ._dim = 4};
// Return the i-th value of the VecShort
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet(const VecShort* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
      that->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
 return ((short*)(((void*)that) + sizeof(long)))[i];
#if BUILDMODE != 0
static inline
short _VecShortGet2D(const VecShort2D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (i < 0 | | i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);</pre>
    PBErrCatch(PBMathErr);
 7
#endif
 return that->_val[i];
#if BUILDMODE != 0
```

```
static inline
#endif
short _VecShortGet3D(const VecShort3D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
   PBErrCatch(PBMathErr);
 }
#endif
 return that->_val[i];
#if BUILDMODE != 0
#endif
short _VecShortGet4D(const VecShort4D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 4) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);</pre>
   PBErrCatch(PBMathErr);
#endif
 return that->_val[i];
// Set the i-th value of the VecShort to v
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet(VecShort* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%ld<\%ld)", i,
      that->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  ((short*)(((void*)that) + sizeof(long)))[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet2D(VecShort2D* const that, const long i, const short v) {
#if BUILDMODE == 0
 if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
   PBErrCatch(PBMathErr);
#endif
 that->_val[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet3D(VecShort3D* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
   PBErrCatch(PBMathErr);
 }
#endif
 that->_val[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet4D(VecShort4D* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (i < 0 || i >= 4) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    PBErrCatch(PBMathErr);
#endif
 that->_val[i] = v;
// Set the i-th value of the VecShort to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd(VecShort* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
```

```
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,</pre>
      that->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  ((short*)(((void*)that) + sizeof(long)))[i] += v;
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd2D(VecShort2D* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);</pre>
    PBErrCatch(PBMathErr);
 }
#endif
 that->_val[i] += v;
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd3D(VecShort3D* const that, const long i, const short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
   PBErrCatch(PBMathErr);
 }
#endif
 that->_val[i] += v;
#if BUILDMODE != 0
static inline
\label{thm:const_long} \verb"void _VecShortSetAdd4D(VecShort4D* const that, const long i, const short v) \ \{ \\
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (i < 0 | | i >= 4) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);</pre>
    PBErrCatch(PBMathErr);
 7
#endif
 that->_val[i] += v;
```

```
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetNull(VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Set values
 for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = 0;
// Set all values of the vector 'that' to 'd'
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAll(VecShort* const that, short v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 // Set values
  for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = v;
// Return the dimension of the VecShort
#if BUILDMODE != 0
static inline
long _VecShortGetDim(const VecShort* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 return that->_dim;
// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist(const VecShort* const that, const VecShort* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
```

```
PBErrCatch(PBMathErr);
  }
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to calculate the distance
  short ret = 0;
  for (long iDim = VecGetDim(that); iDim--;)
    ret += abs(VecGet(that, iDim) - VecGet(tho, iDim));
  // Return the distance
 return ret;
#if BUILDMODE != 0
static inline
short _VecShortHamiltonDist2D(const VecShort2D* const that, const VecShort2D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
    abs(VecGet(that, 1) - VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist3D(const VecShort3D* const that, const VecShort3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
    abs(VecGet(that, 1) - VecGet(tho, 1)) +
    abs(VecGet(that, 2) - VecGet(tho, 2));
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist4D(const VecShort4D* const that, const VecShort4D* const tho) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
    abs(VecGet(that, 1) - VecGet(tho, 1)) +
    abs(VecGet(that, 2) - VecGet(tho, 2)) +
    abs(VecGet(that, 3) - VecGet(tho, 3));
// Return true if the VecShort 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecShortIsEqual(const VecShort* const that,
  const VecShort* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
    ({\tt memcmp(that->\_val, tho->\_val, sizeof(short) * that->\_dim}) == 0);
// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecShortCopy(VecShort* const that, const VecShort* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
```

```
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Copy the values
 memcpy(that->_val, tho->_val, sizeof(short) * that->_dim);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd(const VecShort* const that,
 const VecShort* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Declare a variable ot memorise the result
  short res = 0;
  // For each component
  for (long iDim = that->_dim; iDim--;)
    // Calculate the product
    res += VecGet(that, iDim) * VecGet(tho, iDim);
  \ensuremath{//} Return the result
  return res;
#if BUILDMODE != 0
static inline
#endif
\verb|short_VecShortDotProd2D| (const_VecShort2D* const_that|,
 const VecShort2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  return VecGet(that, 0) * VecGet(tho, 0) +
```

```
VecGet(that, 1) * VecGet(tho, 1);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd3D(const VecShort3D* const that,
 const VecShort3D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
 return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd4D(const VecShort4D* const that,
 const VecShort4D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2) +
    VecGet(that, 3) * VecGet(tho, 3);
// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp(VecShort* const that, const short a,
 const VecShort* const tho, const short b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
```

```
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim,
      a * VecGet(that, iDim) + b * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp2D(VecShort2D* const that, const short a,
 const VecShort2D* const tho, const short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp3D(VecShort3D* const that, const short a,
  const VecShort3D* const tho, const short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp4D(VecShort4D* const that, const short a,
  const VecShort4D* const tho, const short b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
```

```
PBErrCatch(PBMathErr);
 }
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
 VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
 VecSet(that, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
// Return a VecShort equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetOp(const VecShort* const that, const short a,
 const VecShort* const tho, const short b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "dimensions\ don't\ match\ (\%ld==\%ld)",}
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
 VecShort* res = VecShortCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
   VecSet(res, iDim,
     a * VecGet(that, iDim) + b * VecGet(tho, iDim));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetOp2D(const VecShort2D* const that, const short a,
 const VecShort2D* const tho, const short b) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 VecShort2D res = VecShortCreateStatic2D();
```

```
VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetOp3D(const VecShort3D* const that, const short a,
 const VecShort3D* const tho, const short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecShort3D res = VecShortCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
 return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGet0p4D(const VecShort4D* const that, const short a,
  const VecShort4D* const tho, const short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecShort4D res = VecShortCreateStatic4D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  \label{lem:vecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));}
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  VecSet(&res, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
 return res;
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd(VecShort* const that,
 const VecShort* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd2D(VecShort2D* const that,
  const VecShort2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd3D(VecShort3D* const that,
  const VecShort3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
#if BUILDMODE != 0
static inline
```

```
void _VecShortHadamardProd4D(VecShort4D* const that,
 const VecShort4D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
 VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
 VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
 VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
 VecSet(that, 3, VecGet(that, 3) * VecGet(tho, 3));
// Return a VecShort equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetHadamardProd(const VecShort* const that,
 const VecShort* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
 VecShort* res = VecShortCreate(that->_dim);
 for (long iDim = that->_dim; iDim--;)
   VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
VecShort2D _VecShortGetHadamardProd2D(const VecShort2D* const that,
 const VecShort2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecShort2D res = VecShortCreateStatic2D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetHadamardProd3D(const VecShort3D* const that,
 const VecShort3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecShort3D res = VecShortCreateStatic3D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
  return res;
#if BUILDMODE != 0
static inline
VecShort4D _VecShortGetHadamardProd4D(const VecShort4D* const that,
  const VecShort4D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecShort4D res = VecShortCreateStatic4D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
  VecSet(&res, 3, VecGet(that, 3) * VecGet(tho, 3));
 return res;
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
```

```
static inline
#endif
short _VecShortGetMaxVal(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short max = VecGet(that, 0);
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   max = MAX(max, VecGet(that, i));
  // Return the result
 return max;
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetIMaxVal(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  long iMax = 0;
  // Declare a variable to memorize the max value
  short max = VecGet(that, iMax);
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;) {
    if (max < VecGet(that, i)) {</pre>
      max = VecGet(that, i);
      iMax = i;
  // Return the result
 return iMax;
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinVal(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short min = VecGet(that, 0);
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
```

```
min = MIN(min, VecGet(that, i));
  // Return the result
 return min;
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxValAbs(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short max = abs(VecGet(that, 0));
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   max = (abs(max) > abs(VecGet(that, i)) ? max : VecGet(that, i));
  // Return the result
 return max;
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinValAbs(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to memorize the result
  short min = abs(VecGet(that, 0));
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   min = (abs(min) < abs(VecGet(that, i)) ? min : VecGet(that, i));</pre>
  // Return the result
 return min;
// ----- VecLong
// Static constructors for VecLong
#if BUILDMODE != 0
static inline
#endif
VecLong2D VecLongCreateStatic2D() {
  VecLong2D v = \{.\_val = \{0, 0\}, .\_dim = 2\};
 return v;
#if BUILDMODE != 0
static inline
#endif
```

```
VecLong3D VecLongCreateStatic3D() {
  VecLong3D v = \{.\_val = \{0, 0, 0\}, .\_dim = 3\};
  return v;
#if BUILDMODE != 0
static inline
#endif
VecLong4D VecLongCreateStatic4D() {
 VecLong4D v = {._val = {0, 0, 0, 0}, ._dim = 4};
 return v;
}
// Return the i-th value of the VecLong
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet(const VecLong* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%ld<\%ld)", i,
      that->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  return ((long*)(((void*)that) + sizeof(long)))[i];
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet2D(const VecLong2D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
    PBErrCatch(PBMathErr);
  }
#endif
 return that->_val[i];
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet3D(const VecLong3D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
```

```
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
    PBErrCatch(PBMathErr);
#endif
 return that->_val[i];
#if BUILDMODE != 0
static inline
#endif
\label{long_veclongGet4D} \mbox{long $\bot$VecLong4D* const that, const long $i$) $\{$}
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 4) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);</pre>
   PBErrCatch(PBMathErr);
  }
#endif
 return that->_val[i];
// Set the i-th value of the VecLong to \boldsymbol{v}
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet(VecLong* const that, const long i, const long v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
      that->_dim);
   PBErrCatch(PBMathErr);
 7
  ((long*)(((void*)that) + sizeof(long)))[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet2D(VecLong2D* const that, const long i, const long v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);</pre>
    PBErrCatch(PBMathErr);
  }
#endif
  that->_val[i] = v;
```

```
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet3D(VecLong3D* const that, const long i, const long v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
   PBErrCatch(PBMathErr);
#endif
  that->_val[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet4D(VecLong4D* const that, const long i, const long v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 4) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    PBErrCatch(PBMathErr);
 }
#endif
 that->_val[i] = v;
// Set the i-th value of the VecLong to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd(VecLong* const that, const long i, const long v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
   sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
     that->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  ((long*)(((void*)that) + sizeof(long)))[i] += v;
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd2D(VecLong2D* const that, const long i, const long v) {
```

```
#if BUILDMODE == 0
     if (that == NULL) {
         PBMathErr->_type = PBErrTypeNullPointer;
          sprintf(PBMathErr->_msg, "'that' is null");
         PBErrCatch(PBMathErr);
     if (i < 0 || i >= 2) {
         PBMathErr->_type = PBErrTypeInvalidArg;
          sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);</pre>
         PBErrCatch(PBMathErr);
#endif
     that->_val[i] += v;
#if BUILDMODE != 0
static inline
#endif
\label{thm:const_long} \verb|void_VecLong3D*| const_that, const_long_i, const_long_v) = \{ (a,b) : (a,b) 
#if BUILDMODE == 0
     if (that == NULL) {
         PBMathErr->_type = PBErrTypeNullPointer;
          sprintf(PBMathErr->_msg, "'that' is null");
         PBErrCatch(PBMathErr);
     if (i < 0 || i >= 3) {
         PBMathErr->_type = PBErrTypeInvalidArg;
          sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
         PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd4D(VecLong4D* const that, const long i, const long v) {
#if BUILDMODE == 0
     if (that == NULL) {
         PBMathErr->_type = PBErrTypeNullPointer;
          sprintf(PBMathErr->_msg, "'that' is null");
         PBErrCatch(PBMathErr);
     if (i < 0 || i >= 4) {
         PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
         PBErrCatch(PBMathErr);
    }
#endif
   that->_val[i] += v;
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetNull(VecLong* const that) {
#if BUILDMODE == 0
     if (that == NULL) {
         PBMathErr->_type = PBErrTypeNullPointer;
          sprintf(PBMathErr->_msg, "'that' is null");
         PBErrCatch(PBMathErr);
```

```
#endif
  // Set values
  for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = 0;
// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAll(VecLong* const that, long v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Set values
  for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = v;
// Return the dimension of the VecLong
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetDim(const VecLong* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 return that->_dim;
// Return the Hamiltonian distance between the VecLong 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist(const VecLong* const that, const VecLong* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  }
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to calculate the distance
  long ret = 0;
```

```
for (long iDim = VecGetDim(that); iDim--;)
    ret += labs(VecGet(that, iDim) - VecGet(tho, iDim));
  // Return the distance
  return ret;
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist2D(const VecLong2D* const that, const VecLong2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return labs(VecGet(that, 0) - VecGet(tho, 0)) +
    labs(VecGet(that, 1) - VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist3D(const VecLong3D* const that, const VecLong3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return labs(VecGet(that, 0) - VecGet(tho, 0)) +
    labs(VecGet(that, 1) - VecGet(tho, 1)) +
labs(VecGet(that, 2) - VecGet(tho, 2));
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist4D(const VecLong4D* const that, const VecLong4D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
```

```
// Return the distance
  return labs(VecGet(that, 0) - VecGet(tho, 0)) +
    labs(VecGet(that, 1) - VecGet(tho, 1)) +
labs(VecGet(that, 2) - VecGet(tho, 2)) +
    labs(VecGet(that, 3) - VecGet(tho, 3));
// Return true if the VecLong 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecLongIsEqual(const VecLong* const that,
  const VecLong* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  return
    (memcmp(that->_val, tho->_val, sizeof(long) * that->_dim) == 0);
// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecLongCopy(VecLong* const that, const VecLong* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  // Copy the values
  memcpy(that->_val, tho->_val, sizeof(long) * that->_dim);
```

```
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd(const VecLong* const that,
 const VecLong* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
 // Declare a variable ot memorise the result
 long res = 0;
  // For each component
 for (long iDim = that->_dim; iDim--;)
    // Calculate the product
   res += VecGet(that, iDim) * VecGet(tho, iDim);
 // Return the result
 return res;
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd2D(const VecLong2D* const that,
 const VecLong2D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
 return VecGet(that, 0) * VecGet(tho, 0) +
   VecGet(that, 1) * VecGet(tho, 1);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd3D(const VecLong3D* const that,
 const VecLong3D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
```

```
PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
 return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd4D(const VecLong4D* const that,
 const VecLong4D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
 return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2) +
    VecGet(that, 3) * VecGet(tho, 3);
}
// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp(VecLong* const that, const long a,
 const VecLong* const tho, const long b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim,
      a * VecGet(that, iDim) + b * VecGet(tho, iDim));
```

```
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp2D(VecLong2D* const that, const long a,
 const VecLong2D* const tho, const long b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp3D(VecLong3D* const that, const long a,
 const VecLong3D* const tho, const long b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp4D(VecLong4D* const that, const long a,
 #if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 7
#endif
 VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
```

```
VecSet(that, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
}
// Return a VecLong equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetOp(const VecLong* const that, const long a,
 const VecLong* const tho, const long b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 7
#endif
  VecLong* res = VecLongCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
      a * VecGet(that, iDim) + b * VecGet(tho, iDim));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetOp2D(const VecLong2D* const that, const long a,
  const VecLong2D* const tho, const long b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecLong2D res = VecLongCreateStatic2D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetOp3D(const VecLong3D* const that, const long a,
 const VecLong3D* const tho, const long b) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecLong3D res = VecLongCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  return res;
#if BUILDMODE != 0
static inline
VecLong4D _VecLongGetOp4D(const VecLong4D* const that, const long a,
  const VecLong4D* const tho, const long b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecLong4D res = VecLongCreateStatic4D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  \label{lem:vecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));}
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  VecSet(&res, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
 return res;
}
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd(VecLong* const that,
  const VecLong* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
```

```
sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd2D(VecLong2D* const that,
  const VecLong2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd3D(VecLong3D* const that,
  const VecLong3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd4D(VecLong4D* const that,
 const VecLong4D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
  VecSet(that, 3, VecGet(that, 3) * VecGet(tho, 3));
// Return a VecLong equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetHadamardProd(const VecLong* const that,
  const VecLong* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  VecLong* res = VecLongCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetHadamardProd2D(const VecLong2D* const that,
  const VecLong2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecLong2D res = VecLongCreateStatic2D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
  return res;
```

```
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetHadamardProd3D(const VecLong3D* const that,
  const VecLong3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecLong3D res = VecLongCreateStatic3D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  \label{lem:VecSet(\&res, 1, VecGet(that, 1) * VecGet(tho, 1));} \\
  VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
 return res;
#if BUILDMODE != 0
static inline
VecLong4D _VecLongGetHadamardProd4D(const VecLong4D* const that,
  const VecLong4D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecLong4D res = VecLongCreateStatic4D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
  VecSet(&res, 3, VecGet(that, 3) * VecGet(tho, 3));
  return res;
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxVal(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
```

```
long max = VecGet(that, 0);
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
    max = MAX(max, VecGet(that, i));
  // Return the result
 return max;
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetIMaxVal(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  long iMax = 0;
  \ensuremath{//}\xspace Declare a variable to memorize the max value
  long max = VecGet(that, iMax);
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;) {
    if (max < VecGet(that, i)) {</pre>
      max = VecGet(that, i);
      iMax = i;
    }
  }
  // Return the result
 return iMax;
}
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinVal(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to memorize the result
  long min = VecGet(that, 0);
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
    min = MIN(min, VecGet(that, i));
  // Return the result
  return min;
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxValAbs(const VecLong* const that) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  long max = labs(VecGet(that, 0));
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   max = (labs(max) > labs(VecGet(that, i)) ? max : VecGet(that, i));
  // Return the result
 return max;
}
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinValAbs(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  long min = labs(VecGet(that, 0));
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
    min = (labs(min) < labs(VecGet(that, i)) ? min : VecGet(that, i));</pre>
  // Return the result
 return min;
// ----- VecFloat
// Static constructors for VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecFloatCreateStatic2D() {
 VecFloat2D v = \{.\_val = \{0.0, 0.0\}, .\_dim = 2\};
 return v;
#if BUILDMODE != 0
static inline
VecFloat3D VecFloatCreateStatic3D() {
 VecFloat3D v = {.\_val = {0.0, 0.0, 0.0}, .\_dim = 3};
// Return the i-th value of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet(const VecFloat* const that, const long i) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the value
  return that->_val[i];
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet2D(const VecFloat2D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%1d<2)", i);</pre>
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the value
 return that->_val[i];
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet3D(const VecFloat3D* const that, const long i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);</pre>
    PBErrCatch(PBMathErr);
#endif
  // Return the value
 return that->_val[i];
// Set the i-th value of the VecFloat to \boldsymbol{v}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet(VecFloat* const that, const long i, const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
    PBErrCatch(PBMathErr);
#endif
 // Set the value
 that->_val[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet2D(VecFloat2D* const that, const long i, const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%ld<2)", i);\\
    PBErrCatch(PBMathErr);
#endif
 // Set the value
  that->_val[i] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet3D(VecFloat3D* const that, const long i, const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
   PBErrCatch(PBMathErr);
 }
#endif
 // Set the value
 that->_val[i] = v;
// Set the i-th value of the VecFloat to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd(VecFloat* const that, const long i, const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Set the value
  that->_val[i] += v;
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd2D(VecFloat2D* const that, const long i,
  const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);</pre>
    PBErrCatch(PBMathErr);
  }
#endif
  // Set the value
  that->_val[i] += v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd3D(VecFloat3D* const that, const long i,
 const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
   PBErrCatch(PBMathErr);
 }
#endif
 // Set the value
 that->_val[i] += v;
// Set all values of the vector 'that' to 0.0
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull(VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
}
#endif
  // Set values
  for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = 0.0;
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull2D(VecFloat2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Set values
  that->_val[0] = 0.0;
  that->_val[1] = 0.0;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull3D(VecFloat3D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Set values
  that->_val[0] = 0.0;
  that->_val[1] = 0.0;
 that->_val[2] = 0.0;
// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll(VecFloat* const that, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Set values
  for (long iDim = that->_dim; iDim--;)
    that->_val[iDim] = v;
#if BUILDMODE != 0
static inline
void _VecFloatSetAll2D(VecFloat2D* const that, float v) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
```

```
PBErrCatch(PBMathErr);
 }
#endif
 // Set values
  that->_val[0] = v;
 that->_val[1] = v;
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll3D(VecFloat3D* const that, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Set values
  that->_val[0] = v;
  that->_val[1] = v;
 that->_val[2] = v;
// Return the dimension of the VecFloat
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetDim(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 return that->_dim;
// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatCopy(VecFloat* const that, const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
```

```
// Copy the values
 memcpy(that->_val, tho->_val, sizeof(float) * that->_dim);
// Return the norm of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm(const VecFloat* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
 // Declare a variable to calculate the norm
  float ret = 0.0;
  // Calculate the norm
  for (long iDim = that->_dim; iDim--;)
   ret += fsquare(VecGet(that, iDim));
  ret = sqrt(ret);
  // Return the result
 return ret;
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm2D(const VecFloat2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Return the result
 return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)));
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm3D(const VecFloat3D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the result
  return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)) +
    fsquare(VecGet(that, 2)));
// Normalise the VecFloat
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise(VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Normalise
  float norm = VecNorm(that);
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim, VecGet(that, iDim) / norm);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise2D(VecFloat2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Normalise
  float norm = _VecFloatNorm2D(that);
  VecSet(that, 0, VecGet(that, 0) / norm);
  VecSet(that, 1, VecGet(that, 1) / norm);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise3D(VecFloat3D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Normalise
  float norm = _VecFloatNorm3D(that);
  VecSet(that, 0, VecGet(that, 0) / norm);
  VecSet(that, 1, VecGet(that, 1) / norm);
  VecSet(that, 2, VecGet(that, 2) / norm);
// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
```

```
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (long iDim = that->_dim; iDim--;)
   ret += fsquare(VecGet(that, iDim) - VecGet(tho, iDim));
  ret = sqrt(ret);
  // Return the distance
 return ret;
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist2D(const VecFloat2D* const that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
    fsquare(VecGet(that, 1) - VecGet(tho, 1)));
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist3D(const VecFloat3D* const that,
 const VecFloat3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
    fsquare(VecGet(that, 1) - VecGet(tho, 1)) +
    fsquare(VecGet(that, 2) - VecGet(tho, 2)));
7
// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
```

```
float _VecFloatHamiltonDist(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (long iDim = that->_dim; iDim--;)
   ret += fabs(VecGet(that, iDim) - VecGet(tho, iDim));
  // Return the distance
 return ret;
#if BUILDMODE != 0
static inline
#endif
\verb|float_VecFloatHamiltonDist2D| (const_VecFloat2D* const_that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
    fabs(VecGet(that, 1) - VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist3D(const VecFloat3D* const that,
 const VecFloat3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
  fabs(VecGet(that, 1) - VecGet(tho, 1)) +
    fabs(VecGet(that, 2) - VecGet(tho, 2));
// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (long iDim = that->_dim; iDim--;)
    ret += fabs(floor(VecGet(that, iDim)) - floor(VecGet(tho, iDim)));
  // Return the distance
  return ret;
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist2D(const VecFloat2D* const that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) + fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1)));
```

```
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist3D(const VecFloat3D* const that,
  const VecFloat3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) +
    fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1))) +
    fabs(floor(VecGet(that, 2)) - floor(VecGet(tho, 2)));
// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecFloatIsEqual(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  }
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  // For each component
  for (long iDim = that->_dim; iDim--;)
    // If the values of this components are different
    if (!ISEQUALF(VecGet(that, iDim), VecGet(tho, iDim)))
      // Return false
      return false;
  // Return true
 return true;
// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp(VecFloat* const that, const float a,
```

```
const VecFloat* const tho, const float b) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
     that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
 for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim,
     a * VecGet(that, iDim) + b * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp2D(VecFloat2D* const that, const float a,
 #if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
void _VecFloatOp3D(VecFloat3D* const that, const float a,
 const VecFloat3D* const tho, const float b) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
 VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
 VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
```

```
VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
}
// Return a VecFloat equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetOp(const VecFloat* const that, const float a,
 const VecFloat* const tho, const float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
#endif
  VecFloat* res = VecFloatCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
      a * VecGet(that, iDim) + b * VecGet(tho, iDim));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetOp2D(const VecFloat2D* const that, const float a,
  const VecFloat2D* const tho, const float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecFloat2D res = VecFloatCreateStatic2D();
  \label{lem:vecSet(lambdares, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));}
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetOp3D(const VecFloat3D* const that, const float a,
 const VecFloat3D* const tho, const float b) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
 return res;
// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd(VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
 7
  for (long iDim = that->_dim; iDim--;)
    VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd2D(VecFloat2D* const that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
```

```
VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd3D(VecFloat3D* const that,
 const VecFloat3D* const tho) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
// Return a VecFloat equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetHadamardProd(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  VecFloat* res = VecFloatCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
   VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetHadamardProd2D(const VecFloat2D* const that,
  const VecFloat2D* const tho) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
 return res;
#if BUILDMODE != 0
static inline
VecFloat3D _VecFloatGetHadamardProd3D(const VecFloat3D* const that,
 const VecFloat3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
  VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
  VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
 return res;
// Calculate (that * a) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale(VecFloat* const that, const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 for (long iDim = that->_dim; iDim--;)
   VecSet(that, iDim, a * VecGet(that, iDim));
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale2D(VecFloat2D* const that, const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0));
  VecSet(that, 1, a * VecGet(that, 1));
#if BUILDMODE != 0
static inline
void _VecFloatScale3D(VecFloat3D* const that, const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecSet(that, 0, a * VecGet(that, 0));
  VecSet(that, 1, a * VecGet(that, 1));
  VecSet(that, 2, a * VecGet(that, 2));
// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetScale(const VecFloat* const that, const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  VecFloat* res = VecFloatCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
   VecSet(res, iDim, a * VecGet(that, iDim));
 return res;
#if BUILDMODE != 0
static inline
VecFloat2D _VecFloatGetScale2D(const VecFloat2D* const that,
 const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, a * VecGet(that, 0));
  VecSet(&res, 1, a * VecGet(that, 1));
 return res;
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetScale3D(const VecFloat3D* const that,
```

```
const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0));
  VecSet(&res, 1, a * VecGet(that, 1));
  VecSet(&res, 2, a * VecGet(that, 2));
 return res;
// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRot2D(VecFloat2D* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%1d==2)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
#endif
  *that = _VecFloatGetRot2D(that, theta);
// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetRot2D(const VecFloat2D* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==2)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to memorize the result
  VecFloat2D res = VecFloatCreateStatic2D();
  // Declare variable for optimization
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  // Calculate the rotation
  VecSet(&res, 0,
    cosTheta * VecGet(that, 0) - sinTheta * VecGet(that, 1));
```

```
VecSet(&res, 1,
    sinTheta * VecGet(that, 0) + cosTheta * VecGet(that, 1));
  // Return the result
 return res;
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd(const VecFloat* const that,
  const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "dimensions\ don't\ match\ (\%ld==\%ld)",}
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} Declare a variable to memorize the result
  float res = 0.0;
  // Calculate
  for (long iDim = that->_dim; iDim--;)
    res += that->_val[iDim] * tho->_val[iDim];
  // Return the result
 return res;
#if BUILDMODE != 0
static inline
float _VecFloatDotProd2D(const VecFloat2D* const that,
  const VecFloat2D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
#endif
 return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1];
#if BUILDMODE != 0
#endif
float _VecFloatDotProd3D(const VecFloat3D* const that,
  const VecFloat3D* const tho) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
 return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1] +
    that->_val[2] * tho->_val[2];
// Return the cross product of 'that' and 'tho'
#if BUILDMODE != 0
#endif
VecFloat* _VecFloatGetCrossProd(const VecFloat* const that,
 const VecFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim || tho->_dim != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "invalid dimensions (%ld==%ld==3)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to memorize the result
  VecFloat* res = VecFloatCreate(3);
  // Calculate
  VecSet(res. 0.
    VecGet(that, 1) * VecGet(tho, 2) -
    VecGet(that, 2) * VecGet(tho, 1));
  VecSet(res, 1, -1.0 \ast
    (VecGet(that, 0) * VecGet(tho, 2) -
    VecGet(that, 2) * VecGet(tho, 0)));
  VecSet(res, 2,
    VecGet(that, 0) * VecGet(tho, 1) -
    VecGet(that, 1) * VecGet(tho, 0));
  // Return the result
 return res;
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetCrossProd3D(const VecFloat3D* const that,
 const VecFloat3D* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  VecFloat3D res = VecFloatCreateStatic3D();
  // Calculate
  VecSet(&res, 0,
    VecGet(that, 1) * VecGet(tho, 2) -
    VecGet(that, 2) * VecGet(tho, 1));
  VecSet(&res, 1, -1.0 *
    (VecGet(that, 0) * VecGet(tho, 2) -
    VecGet(that, 2) * VecGet(tho, 0)));
  VecSet(&res, 2,
    VecGet(that, 0) * VecGet(tho, 1) -
    VecGet(that, 1) * VecGet(tho, 0));
  // Return the result
 return res;
// Return the conversion of VecFloat 'that' to a VecShort using round()
#if BUILDMODE != 0
static inline
#endif
VecShort* VecFloatToShort(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecShort* res = VecShortCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
   VecSet(res, iDim, SHORT(VecGet(that, iDim)));
  // Return the result
 return res;
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecFloatToShort2D(const VecFloat2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Create the result
  VecShort2D res = VecShortCreateStatic2D();
  VecSet(&res, 0, SHORT(VecGet(that, 0)));
  VecSet(&res, 1, SHORT(VecGet(that, 1)));
  // Return the result
  return res;
```

```
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecFloatToShort3D(const VecFloat3D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecShort3D res = VecShortCreateStatic3D();
  VecSet(&res, 0, SHORT(VecGet(that, 0)));
  VecSet(&res, 1, SHORT(VecGet(that, 1)));
  VecSet(&res, 2, SHORT(VecGet(that, 2)));
  // Return the result
 return res;
// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecShortToFloat(const VecShort* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the result
  VecFloat* res = VecFloatCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim, (float)VecGet(that, iDim));
  // Return the result
 return res;
}
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecShortToFloat2D(const VecShort2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
  // Return the result
 return res;
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecShortToFloat3D(const VecShort3D* const that) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Create the result
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
  VecSet(&res, 2, (float)VecGet(that, 2));
  // Return the result
 return res;
}
// Return the conversion of VecLong 'that' to a VecFloat
#if BUILDMODE != 0
#endif
VecFloat* VecLongToFloat(const VecLong* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecFloat* res = VecFloatCreate(that->_dim);
  for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim, (float)VecGet(that, iDim));
  // Return the result
 return res;
#if BUILDMODE != 0
static inline
VecFloat2D VecLongToFloat2D(const VecLong2D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the result
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
  // Return the result
 return res;
}
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecLongToFloat3D(const VecLong3D* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
}
#endif
  // Create the result
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
VecSet(&res, 2, (float)VecGet(that, 2));
  // Return the result
 return res;
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxVal(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} Declare a variable to memorize the result
  float max = VecGet(that, 0);
  \ensuremath{//} Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
    max = MAX(max, VecGet(that, i));
  // Return the result
 return max;
// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetIMaxVal(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to memorize the result
  long iMax = 0;
  // Declare a variable to memorize the max value
  float max = VecGet(that, iMax);
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;) {
    if(max < VecGet(that, i)) {</pre>
      max = VecGet(that, i);
      iMax = i;
  // Return the result
 return iMax;
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
```

```
float _VecFloatGetMinVal(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to memorize the result
  float min = VecGet(that, 0);
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   min = MIN(min, VecGet(that, i));
  // Return the result
 return min;
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxValAbs(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float max = fabs(VecGet(that, 0));
  // Search for the maximum value
  for (long i = VecGetDim(that); i-- && i != 0;)
   max = (fabs(max) > fabs(VecGet(that, i)) ? max : VecGet(that, i));
  // Return the result
 return max;
}
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinValAbs(const VecFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float min = fabs(VecGet(that, 0));
  // Search for the minimum value
  for (long i = VecGetDim(that); i-- && i != 0;)
    min = (fabs(min) < fabs(VecGet(that, i)) ? min : VecGet(that, i));</pre>
  // Return the result
 return min;
```

```
// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSetIdentity(MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(&(that->_dim), 0) != VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "the\ matrix\ is\ not\ square\ (\%dx\%d)",}
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  }
#endif
  // Set the values
  VecShort2D i = VecShortCreateStatic2D();
  do {
    if (VecGet(&i, 0) == VecGet(&i, 1))
      MatSet(that, &i, 1.0);
      MatSet(that, &i, 0.0);
 } while (VecStep(&i, &(that->_dim)));
// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
MatFloat* _MatFloatGetAdd(MatFloat* const that, MatFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' and 'tho' have different dimensions");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable for the result
  MatFloat* res = MatFloatCreate(MatDim(that));
  // Add each values
  VecShort2D i = VecShortCreateStatic2D();
  do {
   MatSet(res, &i, MatGet(that, &i) + MatGet(tho, &i));
  } while (VecStep(&i, MatDim(that)));
  // Return the result
  return res;
```

```
// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
void _MatFloatAdd(MatFloat* const that, MatFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' and 'tho' have different dimensions");
   PBErrCatch(PBMathErr);
#endif
  // Add each values
  VecShort2D i = VecShortCreateStatic2D();
  do {
    MatSet(that, &i, MatGet(that, &i) + MatGet(tho, &i));
 } while (VecStep(&i, MatDim(that)));
// Multiply the matrix 'that' by 'a'
#if BUILDMODE != 0
static inline
#endif
void _MatFloatScale(MatFloat* const that, const float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Multiply each values
  VecShort2D i = VecShortCreateStatic2D();
    MatSet(that, &i, MatGet(that, &i) * a);
 } while (VecStep(&i, MatDim(that)));
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _MatFloatCopy(MatFloat* const that, const MatFloat* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&(that->_dim), &(tho->_dim))) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
       "'that' and 'tho' have different dimensions (%dx%d==%dx%d)",
      VecGet(\&(that->_dim), 0), VecGet(\&(that->_dim), 1),
      \label{lem:vecGet} $\operatorname{VecGet}(\&(\operatorname{tho}{>}_{-}\operatorname{dim}),\ 0),\ \operatorname{VecGet}(\&(\operatorname{tho}{>}_{-}\operatorname{dim}),\ 1));$
    PBErrCatch(PBMathErr);
#endif
  // Copy the matrix values
  int d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
  memcpy(that->_val, tho->_val, d * sizeof(float));
// Return the value at index 'i' (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
float _MatFloatGet(const MatFloat* const that,
  VecShort2D* index) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (index == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'index' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(index, 0) < 0 | |
    VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
    VecGet(index, 1) < 0 | |
    VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
       "'index' is invalid (0,0 \le d,d < d,d)",
      VecGet(index, 0), VecGet(index, 1),
      \label{lem:vecGet} $\operatorname{VecGet}(\&(\operatorname{that}{\operatorname{->\_dim}})\,,\,\,0)\,,\,\,\operatorname{VecGet}(\&(\operatorname{that}{\operatorname{->\_dim}})\,,\,\,1))\,;
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the value
  return that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
    VecGet(index, 0)];
// Set the value at index 'i' (col, line) of the MatFloat to 'v'
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSet(MatFloat* const that, VecShort2D* index, float v) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (index == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'index' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(index, 0) < 0 ||</pre>
    VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
    VecGet(index, 1) < 0 ||</pre>
    VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'index' is invalid (0,0 \le %d,%d < %d,%d)",
      VecGet(index, 0), VecGet(index, 1),
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  }
#endif
  // Set the value
  that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
    VecGet(index, 0)] = v;
// Return the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
const VecShort2D* _MatFloatDim(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Return the dimension
 return &(that->_dim);
// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
VecShort2D _MatFloatGetDim(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Return the dimension
 return that->_dim;
// Return the number of rows of the MatFloat 'that'
#if BUILDMODE != 0
static inline
```

```
#endif
short _MatFloatGetNbRow(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the nb of rows
 return VecGet(&(that->_dim), 1);
// Return the number of columns of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbCol(const MatFloat* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the nb of cols
  return VecGet(&(that->_dim), 0);
// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
static inline
#endif
float GaussGet(const Gauss* const that, const float x) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Calculate the value
  float a = 1.0 / (that->_sigma * sqrt(2.0 * PBMATH_PI));
  float ret = a * exp(-1.0 * fsquare(x - that->_mean) /
    (2.0 * fsquare(that->_sigma)));
  // Return the value
  return ret;
// Return a random value (in ]0.0, 1.0[)according to the
// Gauss distribution 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
static inline
#endif
float GaussRnd(Gauss* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
}
#endif
  // Declare variable for calcul
  float v1,v2,s;
  // Calculate the value
  do {
   v1 = (rnd() - 0.5) * 2.0;
    v2 = (rnd() - 0.5) * 2.0;
   s = v1 * v1 + v2 * v2;
  } while (s >= 1.0);
  // Return the value
  float ret = 0.0;
  if (s > PBMATH_EPSILON)
   ret = v1 * sqrt(-2.0 * log(s) / s);
 return ret * that->_sigma + that->_mean;
// Return the order 1 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmoothStep(const float x) {
  if (x > 0.0)
    if (x < 1.0)
     return x * x * (3.0 - 2.0 * x);
    else
     return 1.0;
  else
    return 0.0;
// Return the order 2 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmootherStep(const float x) {
 if (x > 0.0)
   if (x < 1.0)
    return x * x * x * (x * (x * 6.0 - 15.0) + 10.0);
      return 1.0;
 else
   return 0.0;
// Solve the SysLinEq _{M.x} = _{V}
// Return the solution vector, or null if there is no solution or the
// arguments are invalid
#if BUILDMODE != 0
static inline
#endif
VecFloat* SysLinEqSolve(const SysLinEq* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
```

```
#endif
        // Declare a variable to memorize the solution
        VecFloat* ret = NULL;
        // Calculate the solution
        ret = MatGetProdVec(that->_Minv, that->_V);
        // Return the solution vector
      return ret;
}
 // Set the matrix of the SysLinEq to a copy of 'm'
// 'm' must have same dimensions has the current matrix
 \ensuremath{//} Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void SysLinEqSetM(SysLinEq* const that, const MatFloat* const m) {
#if BUILDMODE == 0
        if (that == NULL) {
                PBMathErr->_type = PBErrTypeNullPointer;
                sprintf(PBMathErr->_msg, "'that' is null");
               PBErrCatch(PBMathErr);
        if (m == NULL) {
               PBMathErr->_type = PBErrTypeNullPointer;
                sprintf(PBMathErr->_msg, "'m' is null");
               PBErrCatch(PBMathErr);
        if (!VecIsEqual(&(m->_dim), &(that->_M->_dim))) {
               PBMathErr->_type = PBErrTypeInvalidArg;
                sprintf(PBMathErr->\_msg, "'m' has invalid dimension (%dx%d==%dx%d)",
                       VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1),
                      \label{lem:vecGet} $\operatorname{VecGet}(\&(\operatorname{that}{>}_{-}M{-}{>}_{-}\dim),\ 0),\ \operatorname{VecGet}(\&(\operatorname{that}{-}{>}_{-}M{-}{>}_{-}\dim),\ 1));
               PBErrCatch(PBMathErr);
        7
 #endif
        // Update the matrix values % \left( 1\right) =\left( 1\right) \left( 1
        MatCopy(that->_M, m);
        // Update the inverse matrix
        MatFree(&(that->_Minv));
        that->_Minv = MatGetInv(that->_M);
#if BUILDMODE == 0
        if (that->_Minv == NULL) {
               PBMathErr->_type = PBErrTypeOther;
                sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
               PBErrCatch(PBMathErr);
      }
#endif
 // Set the vector of the SysLinEq to a copy of 'v'
 // 'v' must have same dimensions has the current vector
 // Do nothing if arguments are invalid
 #if BUILDMODE != 0
 static inline
#endif
void _SLESetV(SysLinEq* const that, const VecFloat* const v) {
#if BUILDMODE == 0
        if (that == NULL) {
               PBMathErr->_type = PBErrTypeNullPointer;
                sprintf(PBMathErr->_msg, "'that' is null");
               PBErrCatch(PBMathErr);
```

```
if (v == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'v' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(v) != VecGetDim(that->_V)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'v' has invalid dimension (%ld==%ld)",
      VecGetDim(v), VecGetDim(that->_V));
    PBErrCatch(PBMathErr);
  }
#endif
  // Update the vector values
  VecCopy(that->_V, v);
// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/
// does-pow-work-for-int-data-type-in-c
#if BUILDMODE != 0
static inline
#endif
int powi(const int base, const int exp) {
  // Declare a variable to memorize the result and init to 1
  int res = 1;
  // Loop on exponent
  int e = exp;
  int b = base;
  while (e) {
    // Do some magic trick
    if (e & 1)
     res *= b;
    e /= 2;
   b *= b;
  // Return the result
 return res;
// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotAxis(VecFloat3D* const that,
  const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (axis == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'axis' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
```

```
sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  if (VecGetDim(axis) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%1d==3)",
      VecGetDim(axis));
   PBErrCatch(PBMathErr);
  if (ISEQUALF(VecNorm(axis), 1.0) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' is not normalized");
   PBErrCatch(PBMathErr);
  }
#endif
  VecFloat3D v = _VecFloatGetRotAxis(that, axis, theta);
  VecCopy(that, &v);
// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotX(VecFloat3D* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
      VecGetDim(that)):
   PBErrCatch(PBMathErr);
#endif
  VecFloat3D v = _VecFloatGetRotX(that, theta);
  VecCopy(that, &v);
// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotY(VecFloat3D* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%1d==3)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
 }
#endif
```

```
VecFloat3D v = _VecFloatGetRotY(that, theta);
 VecCopy(that, &v);
// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
     VecGetDim(that)):
   PBErrCatch(PBMathErr);
#endif
  VecFloat3D v = _VecFloatGetRotZ(that, theta);
  VecCopy(that, &v);
// Free memory used by the QRDecomp 'that'
#if BUILDMODE != 0
static inline
#endif
void QRDecompFreeStatic(QRDecomp* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 MatFree(&(that->_Q));
 MatFree(&(that->_R));
// Get the base of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
long RatioGetBase(const Ratio* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 return that->_base;
// Get the numerator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
```

```
unsigned int RatioGetNumerator(const Ratio* that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 return that->_numerator;
// Get the denominator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetDenominator(const Ratio* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 return that->_denominator;
// Set the base of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetBase(Ratio* that, long v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
 that->_base = v;
// Set the numerator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetNumerator(Ratio* that, unsigned int v) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
 that->_numerator = v;
// Set the denominator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetDenominator(Ratio* that, unsigned int v) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (v == 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'v' is invalid (%u > 0)", v);
   PBErrCatch(PBMathErr);
  7
#endif
 that->_denominator = v;
// ----- LeastSquareLinReg
// Set the component of the LeastSquareLinReg 'that' to 'X'
#if BUILDMODE != 0
static inline
#endif
void LSLRSetComp(LeastSquareLinReg* that, const MatFloat* X) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (X == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'X' is null");
   PBErrCatch(PBMathErr);
#endif
  that->X = X;
  if (that->Xp != NULL) {
   MatFree(&(that->Xp));
  MatFloat* transp = MatGetTranspose(that->X);
  MatFloat* A = MatGetProdMat(transp, that->X);
  MatFloat* inv = MatGetInv(A);
  if (inv != NULL) {
   that->Xp = MatGetProdMat(inv, transp);
 MatFree(&transp);
 MatFree(&A):
 MatFree(&inv);
}
// Get the bias of the last computed solution of the LeastSquareLinReg 'that'
#if BUILDMODE != 0
static inline
#endif
float LSLRGetBias(const LeastSquareLinReg* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
 return that->bias;
```

```
// Return true if the LeastSquareLinReg 'that' is solvable
#if BUILDMODE != 0
static inline
#endif
bool LSLRIsSolvable(const LeastSquareLinReg* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return (that->Xp != NULL);
}
```

4 Makefile

```
# Build mode
# 0: development (max safety, no optimisation)
# 1: release (min safety, optimisation)
# 2: fast and furious (no safety, optimisation)
BUILD_MODE?=1
all: pbmake_wget main
# Automatic installation of the repository PBMake in the parent folder
pbmake_wget:
if [ ! -d ../PBMake ]; then wget https://github.com/BayashiPascal/PBMake/archive/master.zip; unzip master.zip; rm -f
# Makefile definitions
MAKEFILE_INC=../PBMake/Makefile.inc
include $(MAKEFILE_INC)
# Rules to make the executable
repo=pbmath
$($(repo)_EXENAME): \
$($(repo)_EXENAME).o \
$($(repo)_EXE_DEP) \
$($(repo)_DEP)
$(COMPILER) 'echo "$($(repo)_EXE_DEP) $($(repo)_EXENAME).o" | tr ' ' '\n' | sort -u' $(LINK_ARG) $($(repo)_LINK_ARG)
$($(repo)_EXENAME).o: \
((po)_DIR)/((po)_EXENAME).c 
$($(repo)_INC_H_EXE) \
$($(repo)_EXE_DEP)
$(COMPILER) $(BUILD_ARG) $($(repo)_BUILD_ARG) 'echo "$($(repo)_INC_DIR)" | tr ', ', '\n' | sort -u' -c $($(repo)_DIR)/
```

5 Unit tests

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
#include <string.h>
#include <time.h>
```

```
#include <unistd.h>
#include <sys/time.h>
#include "pberr.h"
#include "pbmath.h"
#define RANDOMSEED 0
void UnitTestPowi() {
  int a;
  int n;
  for (n = 1; n \le 5; ++n) {
    for (a = 0; a <= 10; ++a) {
      int b = powi(a, n);
      int c = 1;
      int m = n;
      for (; m--;) c *= a;
      if (b != c) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg,
          "powi(%d, %d) = %d , %d^%d = %d",
          a, n, b, a, n, c);
        PBErrCatch(PBMathErr);
   }
printf("powi OK\n");
}
void UnitTestFastPow() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  float sumErr = 0.0;
  float maxErr = 0.0;
  int i = nbTest;
  for (; i--;) {
    float a = (rnd() - 0.5) * 1000.0;
    int n = INT(rnd() * 5.0);
    float b = fastpow(a, n);
    float c = pow(a, n);
    float err = fabs(b - c);
    sumErr += err;
    if (maxErr < err)
      maxErr = err;
  float avgErr = sumErr / (float)nbTest;
  printf("average error: %f < %f, max error: %f < %f\n",</pre>
    avgErr, PBMATH_EPSILON, maxErr, PBMATH_EPSILON * 10.0);
  if (avgErr >= PBMATH_EPSILON ||
    maxErr >= PBMATH_EPSILON * 10.0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "fastpow NOK");
    PBErrCatch(PBMathErr);
 printf("fastpow OK\n");
void UnitTestSpeedFastPow() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  int i = nbTest;
  clock_t clockBefore = clock();
  for (; i--;) {
```

```
float a = (rnd() - 0.5) * 1000.0;
    int n = INT(rnd() * 5.0);
    float b = fastpow(a, n);
    b = b;
  }
  clock_t clockAfter = clock();
  double timeFastpow = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  for (; i--;) {
    float a = (rnd() - 0.5) * 1000.0;
    int n = INT(rnd() * 5.0);
    float c = pow(a, n);
    c = c;
  clockAfter = clock();
  double timePow = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("fastpow: %fms, pow: %fms\n",
    timeFastpow / (float)nbTest, timePow / (float)nbTest);
  if (timeFastpow >= timePow) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    PBMathErr->_fatal = false;
sprintf(PBMathErr->_msg, "speed fastpow NOK");
    PBErrCatch(PBMathErr);
printf("speed fastpow OK\n");
}
void UnitTestFSquare() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  for (; nbTest--;) {
    float a = (rnd() - 0.5) * 2000.0;
    float b = fsquare(a);
    float c = a * a;
    if (!ISEQUALF(b, c)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      PBMathErr->_fatal = false;
      sprintf(PBMathErr->_msg,
        "fsquare(%f) = %f , %f*%f = %f",
        a, b, a, a, c);
      PBErrCatch(PBMathErr);
printf("fsquare OK\n");
}
void UnitTestVecShortCreateFree() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecPrintln(v, stdout);
  VecPrintln(&v2, stdout);
  VecPrintln(&v3, stdout);
  VecPrintln(&v4, stdout);
  VecFree(&v);
  if (v != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "VecShort is not null after VecFree");
    PBErrCatch(PBMathErr);
 printf("VecShortCreateFree OK\n");
void UnitTestVecShortClone() {
  VecShort* v = VecShortCreate(5);
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  VecShort* w = VecClone(v);
  if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortClone NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
 printf("_VecShortClone OK\n");
void UnitTestVecShortLoadSave() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  for (long i = 5; i--;) VecSet(v, i, i + 1);
  for (long i = 2; i--;) VecSet(&v2, i, i + 1);
  for (long i = 3; i--;) VecSet(&v3, i, i + 1);
  for (long i = 4; i--;) VecSet(&v4, i, i + 1);
  FILE* f = fopen("./UnitTestVecShortLoadSave.txt", "w");
  if (f == NULL) {
    PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecShortLoadSave.txt for writing");
    PBErrCatch(PBMathErr);
  bool compact = false;
  if (!VecSave(v, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
   PBErrCatch(PBMathErr);
  if (!VecSave(&v2, f, compact)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortSave NOK");
    PBErrCatch(PBMathErr);
  if (!VecSave(&v3, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
    PBErrCatch(PBMathErr);
  if (!VecSave(&v4, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
    PBErrCatch(PBMathErr);
  fclose(f);
  VecShort* w = VecShortCreate(2);
  f = fopen("./UnitTestVecShortLoadSave.txt", "r");
  if (f == NULL) {
    PBMathErr->_type = PBErrTypeOther;
```

```
sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecShortLoadSave.txt for reading");
   PBErrCatch(PBMathErr);
  if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(\&v2, w, sizeof(VecShort) + sizeof(short) * 2) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(&v3, w, sizeof(VecShort) + sizeof(short) * 3) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
  if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(\&v4, w, sizeof(VecShort) + sizeof(short) * 4) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFree(&v);
 VecFree(&w);
 int ret = system("cat ./UnitTestVecShortLoadSave.txt");
 printf("_VecShortLoadSave OK\n");
 ret = ret;
void UnitTestVecShortGetSetDim() {
  VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
 if (VecGetDim(v) != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGetDim NOK");
   PBErrCatch(PBMathErr);
```

```
for (int i = 5; i--;) VecSet(v, i, i + 1);
for (int i = 2; i--;) VecSet(&v2, i, i + 1);
for (int i = 3; i--;) VecSet(&v3, i, i + 1);
for (int i = 4; i--;) VecSet(&v4, i, i + 1);
for (int i = 5; i--;)
  if (v->_val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (v2._val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (v3._val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 4; i--;)
  if (v4.\_val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 5; i--;)
  if (VecGet(v, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(&v2, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (VecGet(&v3, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 4; i--;)
  if (VecGet(\&v4, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 5; i--;) VecSetAdd(v, i, i + 1);
for (int i = 2; i--;) VecSetAdd(&v2, i, i + 1);
for (int i = 3; i--;) VecSetAdd(&v3, i, i + 1);
for (int i = 4; i--;) VecSetAdd(&v4, i, i + 1);
for (int i = 5; i--;)
  if (VecGet(v, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK1");
   PBErrCatch(PBMathErr);
```

```
for (int i = 2; i--;)
  if (VecGet(\&v2, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK2");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (VecGet(\&v3, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK3");
   PBErrCatch(PBMathErr);
for (int i = 4; i--;)
  if (VecGet(\&v4, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK4");
   PBErrCatch(PBMathErr);
 }
VecSetNull(v);
VecSetNull(&v2):
VecSetNull(&v3);
VecSetNull(&v4);
for (int i = 5; i--;)
  if (VecGet(v, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortNull NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(&v2, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortNull NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
 if (VecGet(&v3, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortNull NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 4; i--;)
  if (VecGet(\&v4, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortNull NOK");
   PBErrCatch(PBMathErr);
 }
VecSetAll(v, 1);
VecSetAll(&v2, 1);
VecSetAll(&v3, 1);
VecSetAll(&v4, 1);
for (int i = 5; i--;)
  if (VecGet(v, i) != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortAll NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(&v2, i) != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortAll NOK");
   PBErrCatch(PBMathErr);
```

```
for (int i = 3; i--;)
    if (VecGet(&v3, i) != 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortAll NOK");
     PBErrCatch(PBMathErr);
 for (int i = 4; i--;)
    if (VecGet(&v4, i) != 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortAll NOK");
     PBErrCatch(PBMathErr);
 VecFree(&v);
 printf("_VecShortGetSetDim OK\n");
void UnitTestVecShortStep() {
 VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
  VecShort* bv = VecShortCreate(5);
 VecShort2D bv2 = VecShortCreateStatic2D();
 VecShort3D bv3 = VecShortCreateStatic3D();
  VecShort4D bv4 = VecShortCreateStatic4D();
  short b[5] = \{2, 3, 4, 5, 6\};
  for (int i = 5; i--;) VecSet(bv, i, b[i]);
 for (int i = 2; i--;) VecSet(&bv2, i, b[i]);
 for (int i = 3; i--;) VecSet(&bv3, i, b[i]);
 for (int i = 4; i--;) VecSet(&bv4, i, b[i]);
  int acheck[2 * 3 * 4 * 5 * 6];
  for (int i = 0; i < 2 * 3 * 4 * 5 * 6; ++i)
   acheck[i] = i;
  int iCheck = 0;
  do {
   int a = VecGet(v, 0);
    for (int i = 1; i < VecGetDim(v); ++i)</pre>
     a = a * b[i] + VecGet(v, i);
    if (a != acheck[iCheck]) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecShortStep NOK");
     PBErrCatch(PBMathErr);
    ++iCheck;
 } while (VecStep(v, bv));
  iCheck = 0;
  do {
    int a = VecGet(&v2, 0);
    for (int i = 1; i < 2; ++i)
     a = a * b[i] + VecGet(&v2, i);
    if (a != acheck[iCheck]) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecShortStep NOK");
     PBErrCatch(PBMathErr);
   ++iCheck;
  } while (VecStep(&v2, &bv2));
 iCheck = 0;
   int a = VecGet(&v3, 0);
   for (int i = 1; i < 3; ++i)
     a = a * b[i] + VecGet(&v3, i);
```

```
if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortStep NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecStep(&v3, &bv3));
iCheck = 0;
do {
 int a = VecGet(&v4, 0);
  for (int i = 1; i < 4; ++i)
   a = a * b[i] + VecGet(&v4, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecStep(&v4, &bv4));
iCheck = 0;
do {
  int a = VecGet(v, VecGetDim(v) - 1);
 for (int i = VecGetDim(v) - 2; i \ge 0; --i)
   a = a * b[i] + VecGet(v, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecPStep(v, bv));
iCheck = 0;
do {
 int a = VecGet(&v2, 1);
  a = a * b[0] + VecGet(&v2, 0);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecPStep(\&v2, \&bv2));
iCheck = 0;
do {
  int a = VecGet(&v3, 2);
  for (int i = 1; i >= 0; --i)
   a = a * b[i] + VecGet(&v3, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecPStep(&v3, &bv3));
iCheck = 0;
do {
  int a = VecGet(&v4, 3);
  for (int i = 2; i \ge 0; --i)
   a = a * b[i] + VecGet(&v4, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
```

```
PBErrCatch(PBMathErr);
    }
    ++iCheck;
  } while (VecPStep(&v4, &bv4));
  VecFree(&v);
  VecFree(&bv);
  VecShort2D w = VecShortCreateStatic2D();
  VecShort2D wDelta = VecShortCreateStatic2D();
  VecShort2D wBound = VecShortCreateStatic2D();
  VecSet(&wDelta, 0, 2);
  VecSet(&wDelta, 1, 3);
  VecSet(&wBound, 0, 4);
  VecSet(&wBound, 1, 6);
  int checkDelta[8] = \{0, 0, 0, 3, 2, 0, 2, 3\};
  iCheck = 0:
  do {
    if (VecGet(&w, 0) != checkDelta[iCheck * 2] ||
      VecGet(&w, 1) != checkDelta[iCheck * 2 + 1]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortStepDelta NOK");
      PBErrCatch(PBMathErr);
    ++iCheck;
  } while (VecStepDelta(&w, &wBound, &wDelta));
  int checkDeltaB[8] = {0, 0, 2, 0, 0, 3, 2, 3};
  VecSetNull(&w);
  iCheck = 0;
  do {
    if (VecGet(&w, 0) != checkDeltaB[iCheck * 2] ||
      VecGet(&w, 1) != checkDeltaB[iCheck * 2 + 1]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortStepDelta NOK");
      PBErrCatch(PBMathErr);
    }
    ++iCheck;
  } while (VecPStepDelta(&w, &wBound, &wDelta));
printf("UnitTestVecShortStep OK\n");
}
void UnitTestVecShortHamiltonDist() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  short b[5] = \{-2, -1, 0, 1, 2\};
  for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
  for (int i = 3; i--;) VecSet(&v3, i, b[i]);
  for (int i = 4; i--;) VecSet(&v4, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
  for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
  short dist = VecHamiltonDist(v, w);
  if (dist != 13) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
```

```
PBErrCatch(PBMathErr);
 }
 dist = VecHamiltonDist(&v2, &w2);
 if (dist != 2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v3, &w3);
 if (dist != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v4, &w4);
 if (dist != 8) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortHamiltonDist OK\n");
void UnitTestVecShortIsEqual() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 VecShort* w = VecShortCreate(5);
 VecShort2D w2 = VecShortCreateStatic2D();
 VecShort3D w3 = VecShortCreateStatic3D();
 VecShort4D w4 = VecShortCreateStatic4D();
 if (VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 }
 if (VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 for (int i = 5; i--;) VecSet(w, i, i + 1);
 for (int i = 2; i--;) VecSet(&w2, i, i + 1);
 for (int i = 3; i--;) VecSet(&w3, i, i + 1);
 for (int i = 4; i--;) VecSet(&w4, i, i + 1);
```

```
if (!VecIsEqual(v, w)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortIsEqual OK\n");
void UnitTestVecShortCopy() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  VecCopy(w, v);
  VecCopy(&w2, &v2);
  VecCopy(&w3, &v3);
  VecCopy(&w4, &v4);
  if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v3, &w3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v4, &w4)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
```

```
VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortCopy OK\n");
void UnitTestVecShortDotProd() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
 VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  short b[5] = \{-2, -1, 0, 1, 2\};
  for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
  for (int i = 4; i--;) VecSet(&v4, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
  for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
 for (int i = 3; i--;) VecSet(\&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(\&w4, i, b[3 - i] + 1);
  short prod = VecDotProd(v, w);
  if (prod != -10) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v2, &w2);
  if (prod != 1) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v3, &w3);
  if (prod != -2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v4, &w4);
  if (prod != -6) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortDotProd OK\n");
void UnitTestSpeedVecShort() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 int nbTest = 100000;
 srandom(RANDOMSEED);
 int i = nbTest;
  clock_t clockBefore = clock();
```

```
for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
    short val = 1;
    VecSet(v, j, val);
    short valb = VecGet(v, j);
   valb = valb;
 clock_t clockAfter = clock();
 double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 short* array = malloc(sizeof(short) * 5);
 for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
   short val = 1;
   array[j] = val;
   short valb = array[j];
   valb = valb;
 }
 clockAfter = clock();
 double timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
 printf("VecShort: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 5.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 7
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
   short val = 1;
   VecSet(&v2, j, val);
   short valb = VecGet(&v2, j);
   valb = valb;
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 short array2[2];
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
   short val = 1;
    array2[j] = val;
   short valb = array2[j];
   valb = valb;
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
```

```
printf("VecShort2D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
   short val = 1;
   VecSet(&v3, j, val);
   short valb = VecGet(&v3, j);
   valb = valb;
 }
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 short array3[3];
 for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
   short val = 1;
    array3[j] = val;
   short valb = array3[j];
   valb = valb;
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecShort3D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
 if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
    short val = 1;
   VecSet(&v4, j, val);
   short valb = VecGet(&v4, j);
   valb = valb;
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
```

```
srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  short array4[4];
  for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
    short val = 1;
    array4[j] = val;
    short valb = array4[j];
    valb = valb;
  clockAfter = clock();
  timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("VecShort4D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  free(array);
  printf("UnitTestSpeedVecShort OK\n");
void UnitTestVecShortToFloat() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  VecFloat* w = VecShortToFloat(v);
  VecFloat2D w2 = VecShortToFloat2D(&v2);
  VecFloat3D w3 = VecShortToFloat3D(&v3);
  VecPrintln(w, stdout);
  VecPrintln(&w2, stdout);
  VecPrintln(&w3, stdout);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecShortToFloat OK\n");
void UnitTestVecLongToFloat() {
  VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  VecFloat* w = VecLongToFloat(v);
  VecFloat2D w2 = VecLongToFloat2D(&v2);
  VecFloat3D w3 = VecLongToFloat3D(&v3);
```

```
VecPrintln(w, stdout);
  VecPrintln(&w2, stdout);
  VecPrintln(&w3, stdout);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecLongToFloat OK\n");
void UnitTestVecShortOp() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  short a[2] = \{-1, 2\};
  short b[5] = \{-2, -1, 0, 1, 2\};
for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
  for (int i = 3; i--;) VecSet(&v3, i, b[i]);
  for (int i = 4; i--;) VecSet(&v4, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
  for (int i = 2; i--;) VecSet(\&w2, i, b[1 - i] + 1);
for (int i = 3; i--;) VecSet(\&w3, i, b[2 - i] + 1);
  for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
  VecShort* u = VecGetOp(v, a[0], w, a[1]);
  VecShort2D u2 = VecGet0p(&v2, a[0], &w2, a[1]);
  VecShort3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
  VecShort4D u4 = VecGetOp(&v4, a[0], &v4, a[1]);
  short checku[5] = \{8,5,2,-1,-4\};
  short checku2[2] = \{2,-1\};
  short checku3[3] = \{4,1,-2\};
  short checku4[4] = \{6,3,0,-3\};
  for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(u, i), checku[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
      PBErrCatch(PBMathErr);
  for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
      PBErrCatch(PBMathErr);
  for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
      PBErrCatch(PBMathErr);
  for (int i = 4; i--;)
    if (!ISEQUALF(VecGet(&u4, i), checku4[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
      PBErrCatch(PBMathErr);
```

```
VecOp(v, a[0], w, a[1]);
  VecOp(&v2, a[0], &w2, a[1]);
  VecOp(&v3, a[0], &w3, a[1]);
  VecOp(&v4, a[0], &w4, a[1]);
  if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &u2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v3, &u3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v4, &u4)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
  VecFree(&u);
  printf("UnitTestVecShortOp OK\n");
void UnitTestVecShortShiftStep() {
  VecShort3D v = VecShortCreateStatic3D();
  VecShort3D from = VecShortCreateStatic3D();
  VecShort3D to = VecShortCreateStatic3D();
  VecSet(&from, 0, 0);
  VecSet(&from, 1, 1);
  VecSet(&from, 2, 2);
  VecSet(&to, 0, 3);
  VecSet(&to, 1, 4);
  VecSet(&to, 2, 5);
  VecCopy(&v, &from);
  short check[81] = {
    0, 1, 2, 0, 1, 3, 0, 1, 4,
    0, 2, 2, 0, 2, 3, 0, 2, 4,
    0, 3, 2, 0, 3, 3, 0, 3, 4,
    1, 1, 2, 1, 1, 3, 1, 1, 4,
    1, 2, 2, 1, 2, 3, 1, 2, 4,
    1, 3, 2, 1, 3, 3, 1, 3, 4,
    2, 1, 2, 2, 1, 3, 2, 1, 4,
    2, 2, 2, 2, 3, 2, 2, 4,
    2, 3, 2, 2, 3, 3, 2, 3, 4
    };
  int iCheck = 0;
  do {
    for (int i = 0; i < 3; ++i) {
      if (ISEQUALF(check[iCheck], VecGet(&v, i)) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecShiftStep NOK");
        PBErrCatch(PBMathErr);
      ++iCheck;
```

```
} while(VecShiftStep(&v, &from, &to));
 printf("UnitTestVecShortShiftStep OK\n");
void UnitTestVecShortGetMinMax() {
 VecShort3D v = VecShortCreateStatic3D();
 VecSet(&v, 0, 2); VecSet(&v, 1, 4); VecSet(&v, 2, 3);
 short val = VecGetMaxVal(&v);
 if (val != 4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
   PBErrCatch(PBMathErr);
 if (VecGetIMaxVal(&v) != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetIMaxVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinVal(&v);
 if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, -4); VecSet(&v, 2, 3);
 val = VecGetMaxValAbs(&v);
 if (val != -4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, -2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinValAbs(&v);
 if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecShortGetMinMax OK\n");
void UnitTestVecShortHadamardProd() {
 VecShort* u = VecShortCreate(3);
 for (int i = 3; i--;)
   VecSet(u, i, i + 2);
 VecShort* uprod = VecGetHadamardProd(u, u);
 VecHadamardProd(u, u);
 short checku[3] = \{4, 9, 16\};
 for (int i = 3; i--;)
   if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(uprod, u) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&uprod);
 VecFree(&u);
```

```
VecShort2D v = VecShortCreateStatic2D();
 for (int i = 2; i--;)
   VecSet(\&v, i, i + 2);
 VecShort2D vprod = VecGetHadamardProd(&v, &v);
 VecHadamardProd(&v, &v);
 short checkv[2] = \{4, 9\};
 for (int i = 2; i--;)
   if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&vprod, &v) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecShort3D w = VecShortCreateStatic3D();
 for (int i = 3; i--;)
   VecSet(\&w, i, i + 2);
 VecShort3D wprod = VecGetHadamardProd(&w, &w);
 VecHadamardProd(&w, &w);
 short checkw[3] = \{4, 9, 16\};
 for (int i = 3; i--;)
   if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&wprod, &w) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecShort4D x = VecShortCreateStatic4D();
 for (int i = 4; i--;)
   VecSet(&x, i, i + 2);
 VecShort4D xprod = VecGetHadamardProd(&x, &x);
 VecHadamardProd(&x, &x);
 short checkx[4] = \{4, 9, 16, 25\};
 for (int i = 4; i--;)
   if (ISEQUALF(VecGet(&xprod, i), checkx[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&xprod, &x) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecShortHadamardProd OK\n");
void UnitTestVecShort() {
 UnitTestVecShortCreateFree();
 UnitTestVecShortClone();
 UnitTestVecShortLoadSave();
 UnitTestVecShortGetSetDim();
 UnitTestVecShortStep();
 UnitTestVecShortHamiltonDist();
 UnitTestVecShortIsEqual();
```

```
UnitTestVecShortDotProd();
  UnitTestVecShortCopy();
  UnitTestSpeedVecShort();
  UnitTestVecShortToFloat();
  UnitTestVecLongToFloat();
  UnitTestVecShortOp();
  UnitTestVecShortShiftStep();
  UnitTestVecShortGetMinMax();
  UnitTestVecShortHadamardProd();
 printf("UnitTestVecShort OK\n");
void UnitTestVecLongCreateFree() {
  VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
  VecPrintln(v, stdout);
  VecPrintln(&v2, stdout);
  VecPrintln(&v3, stdout);
  VecPrintln(&v4, stdout);
  VecFree(&v);
  if (v != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecLong is not null after VecFree");
    PBErrCatch(PBMathErr);
printf("VecLongCreateFree OK\n");
}
void UnitTestVecLongClone() {
  VecLong* v = VecLongCreate(5);
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  VecLong* w = VecClone(v);
  if (memcmp(v, w, sizeof(VecLong) + sizeof(long) * 5) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongClone NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
 printf("_VecLongClone OK\n");
void UnitTestVecLongLoadSave() {
  VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  FILE* f = fopen("./UnitTestVecLongLoadSave.txt", "w");
  if (f == NULL) {
    PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecLongLoadSave.txt for writing");
    PBErrCatch(PBMathErr);
  bool compact = false;
  if (!VecSave(v, f, compact)) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongSave NOK");
  PBErrCatch(PBMathErr);
if (!VecSave(&v2, f, compact)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongSave NOK");
  PBErrCatch(PBMathErr);
if (!VecSave(&v3, f, compact)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongSave NOK");
  PBErrCatch(PBMathErr);
if (!VecSave(&v4, f, compact)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongSave NOK");
  PBErrCatch(PBMathErr);
fclose(f);
VecLong* w = VecLongCreate(2);
f = fopen("./UnitTestVecLongLoadSave.txt", "r");
if (f == NULL) {
  PBMathErr->_type = PBErrTypeOther;
  sprintf(PBMathErr->_msg,
    "Can't open ./UnitTestVecLongLoadSave.txt for reading");
  PBErrCatch(PBMathErr);
if (!VecLoad(&w, f)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
 PBErrCatch(PBMathErr);
if (memcmp(v, w, sizeof(VecLong) + sizeof(long) * 5) != 0) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
  PBErrCatch(PBMathErr);
if (!VecLoad(&w, f)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
  PBErrCatch(PBMathErr);
if (memcmp(\&v2, w, sizeof(VecLong) + sizeof(long) * 2) != 0) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
  PBErrCatch(PBMathErr);
if (!VecLoad(&w, f)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
  PBErrCatch(PBMathErr);
}
if (memcmp(&v3, w, sizeof(VecLong) + sizeof(long) * 3) != 0) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
  PBErrCatch(PBMathErr);
if (!VecLoad(&w, f)) {
 PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
  PBErrCatch(PBMathErr);
```

```
if (memcmp(\&v4, w, sizeof(VecLong) + sizeof(long) * 4) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFree(&v);
 VecFree(&w);
 int ret = system("cat ./UnitTestVecLongLoadSave.txt");
 printf("_VecLongLoadSave OK\n");
 ret = ret;
void UnitTestVecLongGetSetDim() {
  VecLong* v = VecLongCreate(5);
 VecLong2D v2 = VecLongCreateStatic2D();
 VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
 if (VecGetDim(v) != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGetDim NOK");
   PBErrCatch(PBMathErr);
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 for (int i = 5; i--;)
   if (v->_val[i] != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongSet NOK");
     PBErrCatch(PBMathErr);
  for (int i = 2; i--;)
    if (v2._val[i] != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongSet NOK");
     PBErrCatch(PBMathErr);
   }
 for (int i = 3; i--;)
    if (v3._val[i] != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongSet NOK");
     PBErrCatch(PBMathErr);
 for (int i = 4; i--;)
    if (v4.\_val[i] != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongSet NOK");
     PBErrCatch(PBMathErr);
 for (int i = 5; i--;)
    if (VecGet(v, i) != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongGet NOK");
     PBErrCatch(PBMathErr);
  for (int i = 2; i--;)
    if (VecGet(&v2, i) != i + 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongGet NOK");
```

```
PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (VecGet(&v3, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 4; i--;)
  if (VecGet(&v4, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 5; i--;) VecSetAdd(v, i, i + 1);
for (int i = 2; i--;) VecSetAdd(&v2, i, i + 1);
for (int i = 3; i--;) VecSetAdd(&v3, i, i + 1);
for (int i = 4; i--;) VecSetAdd(&v4, i, i + 1);
for (int i = 5; i--;)
  if (VecGet(v, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(\&v2, i) != 2 * (i + 1)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (VecGet(\&v3, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
   PBErrCatch(PBMathErr);
for (int i = 4; i--;)
  if (VecGet(\&v4, i) != 2 * (i + 1)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
   PBErrCatch(PBMathErr);
 }
VecSetNull(v);
VecSetNull(&v2);
VecSetNull(&v3):
VecSetNull(&v4);
for (int i = 5; i--;)
  if (VecGet(v, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(&v2, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGet NOK");
   PBErrCatch(PBMathErr);
 7
for (int i = 3; i--;)
  if (VecGet(&v3, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGet NOK");
```

```
PBErrCatch(PBMathErr);
   }
  for (int i = 4; i--;)
    if (VecGet(&v4, i) != 0) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongGet NOK");
     PBErrCatch(PBMathErr);
   }
  VecSetAll(v, 1);
 VecSetAll(&v2, 1);
  VecSetAll(&v3, 1);
  VecSetAll(&v4, 1);
  for (int i = 5; i--;)
    if (VecGet(v, i) != 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongAll NOK");
     PBErrCatch(PBMathErr);
   }
  for (int i = 2; i--;)
    if (VecGet(&v2, i) != 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongAll NOK");
     PBErrCatch(PBMathErr);
 for (int i = 3; i--;)
    if (VecGet(&v3, i) != 1) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongAll NOK");
     PBErrCatch(PBMathErr);
   }
 for (int i = 4; i--;)
    if (VecGet(&v4, i) != 1) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecLongAll NOK");
     PBErrCatch(PBMathErr);
 VecFree(&v);
 printf("_VecLongGetSetDim OK\n");
void UnitTestVecLongStep() {
 VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
 VecLong4D v4 = VecLongCreateStatic4D();
  VecLong* bv = VecLongCreate(5);
 VecLong2D bv2 = VecLongCreateStatic2D();
 VecLong3D bv3 = VecLongCreateStatic3D();
  VecLong4D bv4 = VecLongCreateStatic4D();
 long b[5] = \{2, 3, 4, 5, 6\};
  for (int i = 5; i--;) VecSet(bv, i, b[i]);
 for (int i = 2; i--;) VecSet(&bv2, i, b[i]);
  for (int i = 3; i--;) VecSet(&bv3, i, b[i]);
  for (int i = 4; i--;) VecSet(&bv4, i, b[i]);
 int acheck[2 * 3 * 4 * 5 * 6];
  for (int i = 0; i < 2 * 3 * 4 * 5 * 6; ++i)
   acheck[i] = i;
  int iCheck = 0;
  do {
   int a = VecGet(v, 0);
   for (int i = 1; i < VecGetDim(v); ++i)</pre>
     a = a * b[i] + VecGet(v, i);
```

```
if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongStep NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecStep(v, bv));
iCheck = 0;
do {
 int a = VecGet(&v2, 0);
  for (int i = 1; i < 2; ++i)
   a = a * b[i] + VecGet(&v2, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongStep NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecStep(&v2, &bv2));
iCheck = 0;
do {
  int a = VecGet(&v3, 0);
 for (int i = 1; i < 3; ++i)
   a = a * b[i] + VecGet(&v3, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecStep(&v3, &bv3));
iCheck = 0;
do {
 int a = VecGet(&v4, 0);
  for (int i = 1; i < 4; ++i)
   a = a * b[i] + VecGet(&v4, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecStep(&v4, &bv4));
iCheck = 0;
do {
  int a = VecGet(v, VecGetDim(v) - 1);
  for (int i = VecGetDim(v) - 2; i >= 0; --i)
   a = a * b[i] + VecGet(v, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
   PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecPStep(v, bv));
iCheck = 0;
do {
 int a = VecGet(&v2, 1);
  a = a * b[0] + VecGet(&v2, 0);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
```

```
PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecPStep(&v2, &bv2));
iCheck = 0;
do {
 int a = VecGet(&v3, 2);
  for (int i = 1; i >= 0; --i)
   a = a * b[i] + VecGet(&v3, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecPStep(&v3, &bv3));
iCheck = 0;
do {
  int a = VecGet(&v4, 3);
  for (int i = 2; i \ge 0; --i)
   a = a * b[i] + VecGet(&v4, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecPStep(&v4, &bv4));
VecFree(&v);
VecFree(&bv);
VecLong2D w = VecLongCreateStatic2D();
VecLong2D wDelta = VecLongCreateStatic2D();
VecLong2D wBound = VecLongCreateStatic2D();
VecSet(&wDelta, 0, 2);
VecSet(&wDelta, 1, 3);
VecSet(&wBound, 0, 4);
VecSet(&wBound, 1, 6);
int checkDelta[8] = \{0, 0, 0, 3, 2, 0, 2, 3\};
iCheck = 0;
do {
 if (VecGet(&w, 0) != checkDelta[iCheck * 2] ||
   VecGet(&w, 1) != checkDelta[iCheck * 2 + 1]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongStepDelta NOK");
   PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecStepDelta(&w, &wBound, &wDelta));
int checkDeltaB[8] = {0, 0, 2, 0, 0, 3, 2, 3};
VecSetNull(&w);
iCheck = 0;
do {
  if (VecGet(&w, 0) != checkDeltaB[iCheck * 2] ||
    VecGet(&w, 1) != checkDeltaB[iCheck * 2 + 1]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongStepDelta NOK");
   PBErrCatch(PBMathErr);
  ++iCheck;
} while (VecPStepDelta(&w, &wBound, &wDelta));
printf("UnitTestVecLongStep OK\n");
```

```
void UnitTestVecLongHamiltonDist() {
 VecLong* v = VecLongCreate(5);
 VecLong2D v2 = VecLongCreateStatic2D();
 VecLong3D v3 = VecLongCreateStatic3D();
 VecLong4D v4 = VecLongCreateStatic4D();
 VecLong* w = VecLongCreate(5);
 VecLong2D w2 = VecLongCreateStatic2D();
 VecLong3D w3 = VecLongCreateStatic3D();
 VecLong4D w4 = VecLongCreateStatic4D();
 long b[5] = \{-2, -1, 0, 1, 2\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 4; i--;) VecSet(&v4, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
 for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
 for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
 long dist = VecHamiltonDist(v, w);
 if (dist != 13) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v2, &w2);
 if (dist != 2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v3, &w3);
 if (dist != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v4, &w4);
 if (dist != 8) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecLongHamiltonDist OK\n");
void UnitTestVecLongIsEqual() {
 VecLong* v = VecLongCreate(5);
 VecLong2D v2 = VecLongCreateStatic2D();
 VecLong3D v3 = VecLongCreateStatic3D();
 VecLong4D v4 = VecLongCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 VecLong* w = VecLongCreate(5);
 VecLong2D w2 = VecLongCreateStatic2D();
 VecLong3D w3 = VecLongCreateStatic3D();
 VecLong4D w4 = VecLongCreateStatic4D();
```

```
if (VecIsEqual(v, w)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
 for (int i = 5; i--;) VecSet(w, i, i + 1);
  for (int i = 2; i--;) VecSet(&w2, i, i + 1);
 for (int i = 3; i--;) VecSet(&w3, i, i + 1);
  for (int i = 4; i--;) VecSet(&w4, i, i + 1);
  if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v4, &w4)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecLongIsEqual OK\n");
void UnitTestVecLongCopy() {
  VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  VecLong* w = VecLongCreate(5);
  VecLong2D w2 = VecLongCreateStatic2D();
  VecLong3D w3 = VecLongCreateStatic3D();
  VecLong4D w4 = VecLongCreateStatic4D();
```

```
VecCopy(w, v);
 VecCopy(&w2, &v2);
 VecCopy(&w3, &v3);
 VecCopy(&w4, &v4);
 if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecLongCopy OK\n");
void UnitTestVecLongDotProd() {
 VecLong* v = VecLongCreate(5);
 VecLong2D v2 = VecLongCreateStatic2D();
 VecLong3D v3 = VecLongCreateStatic3D();
 VecLong4D v4 = VecLongCreateStatic4D();
 VecLong* w = VecLongCreate(5);
 VecLong2D w2 = VecLongCreateStatic2D();
 VecLong3D w3 = VecLongCreateStatic3D();
 VecLong4D w4 = VecLongCreateStatic4D();
 long b[5] = \{-2, -1, 0, 1, 2\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 4; i--;) VecSet(&v4, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
 for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
 for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
 long prod = VecDotProd(v, w);
 if (prod != -10) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
   PBErrCatch(PBMathErr);
 }
 prod = VecDotProd(&v2, &w2);
 if (prod != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v3, &w3);
 if (prod != -2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v4, &w4);
  if (prod != -6) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecLongDotProd OK\n");
void UnitTestSpeedVecLong() {
 VecLong* v = VecLongCreate(5);
 VecLong2D v2 = VecLongCreateStatic2D();
 VecLong3D v3 = VecLongCreateStatic3D();
 VecLong4D v4 = VecLongCreateStatic4D();
 int nbTest = 100000;
 srandom(RANDOMSEED);
 int i = nbTest;
  clock_t clockBefore = clock();
 for (; i--;) {
    int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
    long val = 1;
   VecSet(v, j, val);
long valb = VecGet(v, j);
   valb = valb;
 }
  clock_t clockAfter = clock();
 double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 long* array = malloc(sizeof(long) * 5);
  for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
   long val = 1;
    array[j] = val;
   long valb = array[j];
   valb = valb;
 clockAfter = clock();
 double timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecLong: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
```

```
for (; i--;) {
          int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
          long val = 1;
         VecSet(&v2, j, val);
long valb = VecGet(&v2, j);
        valb = valb;
     clockAfter = clock();
     timeV = ((double)(clockAfter - clockBefore)) /
         CLOCKS_PER_SEC * 1000.0;
     srandom(RANDOMSEED);
     i = nbTest;
     clockBefore = clock();
     long array2[2];
     for (; i--;) {
          int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
          long val = 1;
          array2[j] = val;
          long valb = array2[j];
         valb = valb;
     }
     clockAfter = clock();
     timeRef = ((double)(clockAfter - clockBefore)) /
          CLOCKS_PER_SEC * 1000.0;
     \label{lem:printf("VecLong2D: $\%fms, array: $\%fms\n", a
          timeV / (float)nbTest, timeRef / (float)nbTest);
     if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
         PBMathErr->_fatal = false;
#endif
         PBMathErr->_type = PBErrTypeUnitTestFailed;
          sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
         PBErrCatch(PBMathErr);
    7
     srandom(RANDOMSEED);
     i = nbTest;
     clockBefore = clock();
     for (; i--;) {
          int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
          long val = 1;
         VecSet(&v3, j, val);
long valb = VecGet(&v3, j);
        valb = valb;
     clockAfter = clock();
     timeV = ((double)(clockAfter - clockBefore)) /
         CLOCKS_PER_SEC * 1000.0;
     srandom(RANDOMSEED);
     i = nbTest;
     clockBefore = clock();
     long array3[3];
     for (; i--;) {
          int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
          long val = 1;
          array3[j] = val;
          long valb = array3[j];
         valb = valb;
     clockAfter = clock();
     timeRef = ((double)(clockAfter - clockBefore)) /
          CLOCKS_PER_SEC * 1000.0;
```

```
printf("VecLong3D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
   PBErrCatch(PBMathErr);
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
    long val = 1;
    VecSet(&v4, j, val);
long valb = VecGet(&v4, j);
   valb = valb;
  }
  clockAfter = clock();
  timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  long array4[4];
  for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
    long val = 1;
    array4[j] = val;
    long valb = array4[j];
    valb = valb;
  clockAfter = clock();
  timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("VecLong4D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
   PBErrCatch(PBMathErr);
  VecFree(&v);
  free(array);
 printf("UnitTestSpeedVecLong OK\n");
void UnitTestVecLongOp() {
  VecLong* v = VecLongCreate(5);
  VecLong2D v2 = VecLongCreateStatic2D();
  VecLong3D v3 = VecLongCreateStatic3D();
  VecLong4D v4 = VecLongCreateStatic4D();
  VecLong* w = VecLongCreate(5);
  VecLong2D w2 = VecLongCreateStatic2D();
  VecLong3D w3 = VecLongCreateStatic3D();
```

```
VecLong4D w4 = VecLongCreateStatic4D();
for (int i = 5; i--;) VecSet(v, i, i + 1);
for (int i = 2; i--;) VecSet(&v2, i, i + 1);
for (int i = 3; i--;) VecSet(&v3, i, i + 1);
long a[2] = \{-1, 2\};
long b[5] = \{-2, -1, 0, 1, 2\};
for (int i = 5; i--;) VecSet(v, i, b[i]);
for (int i = 2; i--;) VecSet(&v2, i, b[i]);
for (int i = 3; i--;) VecSet(&v3, i, b[i]);
for (int i = 4; i--;) VecSet(&v4, i, b[i]);
for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
for (int i = 2; i--;) VecSet(\&w2, i, b[1 - i] + 1);
for (int i = 3; i--;) VecSet(\&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
VecLong* u = VecGetOp(v, a[0], w, a[1]);
VecLong2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
VecLong3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
VecLong4D u4 = VecGetOp(&v4, a[0], &w4, a[1]);
long checku[5] = \{8,5,2,-1,-4\};
long checku2[2] = \{2,-1\};
long checku3[3] = \{4,1,-2\};
long checku4[4] = \{6,3,0,-3\};
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(u, i), checku[i])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
    PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
    PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
    PBErrCatch(PBMathErr);
  }
for (int i = 4; i--;)
  if (!ISEQUALF(VecGet(&u4, i), checku4[i])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
    PBErrCatch(PBMathErr);
VecOp(v, a[0], w, a[1]);
VecOp(&v2, a[0], &w2, a[1]);
VecOp(&v3, a[0], &w3, a[1]);
VecOp(&v4, a[0], &w4, a[1]);
if (!VecIsEqual(v, u)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongOp NOK");
  PBErrCatch(PBMathErr);
if (!VecIsEqual(&v2, &u2)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecLongOp NOK");
  PBErrCatch(PBMathErr);
if (!VecIsEqual(&v3, &u3)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "_VecLongOp NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v4, &u4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongOp NOK");
   PBErrCatch(PBMathErr);
 }
 VecFree(&v);
 VecFree(&w);
 VecFree(&u);
 printf("UnitTestVecLongOp OK\n");
void UnitTestVecLongShiftStep() {
 VecLong3D v = VecLongCreateStatic3D();
 VecLong3D from = VecLongCreateStatic3D();
 VecLong3D to = VecLongCreateStatic3D();
 VecSet(&from, 0, 0);
 VecSet(&from, 1, 1);
 VecSet(&from, 2, 2);
  VecSet(&to, 0, 3);
 VecSet(&to, 1, 4);
  VecSet(&to, 2, 5);
  VecCopy(&v, &from);
  long check[81] = {
    0, 1, 2, 0, 1, 3, 0, 1, 4,
   0, 2, 2, 0, 2, 3, 0, 2, 4,
   0, 3, 2, 0, 3, 3, 0, 3, 4,
   1, 1, 2, 1, 1, 3, 1, 1, 4,
   1, 2, 2, 1, 2, 3, 1, 2, 4,
   1, 3, 2, 1, 3, 3, 1, 3, 4,
   2, 1, 2, 2, 1, 3, 2, 1, 4,
   2, 2, 2, 2, 3, 2, 2, 4,
    2, 3, 2, 2, 3, 3, 2, 3, 4
   }:
 int iCheck = 0;
 do {
    for (int i = 0; i < 3; ++i) {
      if (ISEQUALF(check[iCheck], VecGet(&v, i)) == false) {
       PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecShiftStep NOK");
        PBErrCatch(PBMathErr);
     }
     ++iCheck;
 } while(VecShiftStep(&v, &from, &to));
 printf("UnitTestVecLongShiftStep OK\n");
void UnitTestVecLongGetMinMax() {
 VecLong3D v = VecLongCreateStatic3D();
 VecSet(&v, 0, 2); VecSet(&v, 1, 4); VecSet(&v, 2, 3);
 long val = VecGetMaxVal(&v);
 if (val != 4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
   PBErrCatch(PBMathErr);
 if (VecGetIMaxVal(&v) != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetIMaxVal NOK");
```

```
PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinVal(&v);
 if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, -4); VecSet(&v, 2, 3);
 val = VecGetMaxValAbs(&v);
 if (val != -4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, -2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinValAbs(&v);
 if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecLongGetMinMax OK\n");
void UnitTestVecLongHadamardProd() {
 VecLong* u = VecLongCreate(3);
 for (int i = 3; i--;)
   VecSet(u, i, i + 2);
 VecLong* uprod = VecGetHadamardProd(u, u);
 VecHadamardProd(u, u);
 long checku[3] = \{4, 9, 16\};
 for (int i = 3; i--;)
   if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
   }
 if (VecIsEqual(uprod, u) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&uprod);
 VecFree(&u);
 VecLong2D v = VecLongCreateStatic2D();
 for (int i = 2; i--;)
   VecSet(\&v, i, i + 2);
 VecLong2D vprod = VecGetHadamardProd(&v, &v);
 VecHadamardProd(&v, &v);
 long checkv[2] = {4, 9};
 for (int i = 2; i--;)
   if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&vprod, &v) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
```

```
VecLong3D w = VecLongCreateStatic3D();
  for (int i = 3; i--;)
    VecSet(&w, i, i + 2);
  VecLong3D wprod = VecGetHadamardProd(&w, &w);
  VecHadamardProd(&w, &w);
  long checkw[3] = \{4, 9, 16\};
  for (int i = 3; i--;)
    if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
      PBErrCatch(PBMathErr);
  if (VecIsEqual(&wprod, &w) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
    PBErrCatch(PBMathErr);
  VecLong4D x = VecLongCreateStatic4D();
  for (int i = 4; i--;)
    VecSet(&x, i, i + 2);
  VecLong4D xprod = VecGetHadamardProd(&x, &x);
  VecHadamardProd(&x, &x);
  long checkx[4] = \{4, 9, 16, 25\};
  for (int i = 4; i--;)
    if (ISEQUALF(VecGet(&xprod, i), checkx[i]) == false) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
      PBErrCatch(PBMathErr);
  if (VecIsEqual(&xprod, &x) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
    PBErrCatch(PBMathErr);
printf("UnitTestVecLongHadamardProd OK\n");
}
void UnitTestVecLong() {
  UnitTestVecLongCreateFree();
  UnitTestVecLongClone();
  UnitTestVecLongLoadSave();
  UnitTestVecLongGetSetDim();
  UnitTestVecLongStep();
  UnitTestVecLongHamiltonDist();
  UnitTestVecLongIsEqual();
  UnitTestVecLongDotProd();
  UnitTestVecLongCopy();
  UnitTestSpeedVecLong();
  UnitTestVecLongOp();
  UnitTestVecLongShiftStep();
  UnitTestVecLongGetMinMax();
  UnitTestVecLongHadamardProd();
  printf("UnitTestVecLong OK\n");
void UnitTestVecFloatCreateFree() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  VecPrintln(v, stdout);
  VecPrintln(&v2, stdout);
```

```
VecPrintln(&v3, stdout);
  _VecFloatFree(&v);
  if (v != NULL) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecFloat is not null after _VecFloatFree");
   PBErrCatch(PBMathErr);
 printf("VecFloatCreateFree OK\n");
void UnitTestVecFloatClone() {
 VecFloat* v = VecFloatCreate(5);
 for (int i = 5; i--;) VecSet(v, i, i + 1);
  VecFloat* w = VecClone(v);
 if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatClone NOK");
   PBErrCatch(PBMathErr);
  _VecFloatFree(&v);
  _VecFloatFree(&w);
 printf("_VecFloatClone OK\n");
void UnitTestVecFloatLoadSave() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 FILE* f = fopen("./UnitTestVecFloatLoadSave.txt", "w");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecFloatLoadSave.txt for writing");
   PBErrCatch(PBMathErr);
 bool compact = false;
  if (!VecSave(v, f, compact)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecSave(&v2, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
  if (!VecSave(&v3, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFloat* w = VecFloatCreate(2);
  f = fopen("./UnitTestVecFloatLoadSave.txt", "r");
  if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecFloatLoadSave.txt for reading");
    PBErrCatch(PBMathErr);
```

```
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
    PBErrCatch(PBMathErr);
  if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
    PBErrCatch(PBMathErr);
  if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
    PBErrCatch(PBMathErr);
  if (memcmp(&v2, w, sizeof(VecFloat) + sizeof(float) * 2) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
   PBErrCatch(PBMathErr);
  }
  if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(&v3, w, sizeof(VecFloat) + sizeof(float) * 3) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
    PBErrCatch(PBMathErr);
  }
  fclose(f);
  VecFree(&v);
  VecFree(&w);
  int ret = system("cat ./UnitTestVecFloatLoadSave.txt");
  printf("_VecFloatLoadSave OK\n");
  ret = ret;
void UnitTestVecFloatGetSetDim() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  if (VecGetDim(v) != 5) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGetDim NOK");
   PBErrCatch(PBMathErr);
  for (int i = 5; i--;) VecSet(v, i, (float)(i + 1));
  for (int i = 2; i--;) VecSet(&v2, i, (float)(i + 1));
  for (int i = 3; i--;) VecSet(&v3, i, (float)(i + 1));
  for (int i = 5; i--;)
    if (!ISEQUALF(v->_val[i], (float)(i + 1))) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
      PBErrCatch(PBMathErr);
  for (int i = 2; i--;)
    if (!ISEQUALF(v2._val[i], (float)(i + 1))) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
      PBErrCatch(PBMathErr);
```

```
}
for (int i = 3; i--;)
  if (!ISEQUALF(v3._val[i], (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
   PBErrCatch(PBMathErr);
 7
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(v, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 5; i--;) VecSetAdd(v, i, (float)(i + 1));
for (int i = 2; i--;) VecSetAdd(&v2, i, (float)(i + 1));
for (int i = 3; i--;) VecSetAdd(&v3, i, (float)(i + 1));
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(v, i), 2.0 * (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&v2, i), 2.0 * (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (!ISEQUALF(VecGet(&v3, i), 2.0 * (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
   PBErrCatch(PBMathErr);
 }
VecSetNull(v);
VecSetNull(&v2);
VecSetNull(&v3);
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(v, i), 0.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&v2, i), 0.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
```

```
if (!ISEQUALF(VecGet(&v3, i), 0.0)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
     PBErrCatch(PBMathErr);
  VecSetAll(v, 1.0);
  VecSetAll(&v2, 1.0);
  VecSetAll(&v3, 1.0);
  for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), 1.0)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
     PBErrCatch(PBMathErr);
 for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), 1.0)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
     PBErrCatch(PBMathErr);
 for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), 1.0)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
     PBErrCatch(PBMathErr);
 VecFree(&v);
 printf("_VecFloatGetSetDim OK\n");
void UnitTestVecFloatCopy() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
  VecFloat3D w3 = VecFloatCreateStatic3D();
  VecCopy(w, v);
 VecCopy(&w2, &v2);
  VecCopy(&w3, &v3);
  if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 }
 if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecFloatCopy OK\n");
```

```
void UnitTestVecFloatNorm() {
  VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  if (!ISEQUALF(VecNorm(v), 7.416198)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecNorm(&v2), 2.236068)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(&v3), 3.741657)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
    PBErrCatch(PBMathErr);
 VecNormalise(v);
  VecNormalise(&v2);
  VecNormalise(&v3);
  if (!ISEQUALF(VecNorm(v), 1.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(&v2), 1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
    PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecNorm(&v3), 1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 printf("UnitTestVecFloatNorm OK\n");
void UnitTestVecFloatDist() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 VecFloat* w = VecFloatCreate(5);
  VecFloat2D w2 = VecFloatCreateStatic2D();
  VecFloat3D w3 = VecFloatCreateStatic3D();
  float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
for (int i = 2; i--;) VecSet(&v2, i, b[i]);
  for (int i = 3; i--;) VecSet(&v3, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
  for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1.5);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
  if (!ISEQUALF(VecDist(v, w), 7.158911)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
```

```
PBErrCatch(PBMathErr);
 }
 if (!ISEQUALF(VecDist(&v2, &w2), 2.549510)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecDist(&v3, &w3), 3.840573)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecHamiltonDist(v, w), 13.5)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecHamiltonDist(&v2, &w2), 3.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecHamiltonDist(&v3, &w3), 5.5)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(v, w), 13.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(&v2, &w2), 2.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(&v3, &w3), 5.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w):
 printf("UnitTestVecFloatDist OK\n");
void UnitTestVecFloatIsEqual() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
 if (VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
```

```
if (VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
  if (VecIsEqual(&v3, &w3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
  for (int i = 5; i--;) VecSet(w, i, i + 1);
  for (int i = 2; i--;) VecSet(&w2, i, i + 1);
for (int i = 3; i--;) VecSet(&w3, i, i + 1);
  if (!VecIsEqual(v, w)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
  }
  if (!VecIsEqual(&v3, &w3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecFloatIsEqual OK\n");
void UnitTestVecFloatScale() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  float a = 0.1;
  VecFloat* w = VecGetScale(v, a);
  VecFloat2D w2 = VecGetScale(&v2, a);
  VecFloat3D w3 = VecGetScale(&v3, a);
  VecScale(v, a);
  VecScale(&v2, a);
  VecScale(&v3, a);
  for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(w, i), (float)(i + 1) * a)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
      PBErrCatch(PBMathErr);
    }
  for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&w2, i), (float)(i + 1) * a)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
      PBErrCatch(PBMathErr);
  for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&w3, i), (float)(i + 1) * a)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
     PBErrCatch(PBMathErr);
 for (int i = 5; i--;)
   if (!ISEQUALF(VecGet(v, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
 for (int i = 2; i--;)
   if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
 for (int i = 3; i--;)
   if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
   }
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecFloatScale OK\n");
void UnitTestVecFloatOp() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 float a[2] = \{-0.1, 2.0\};
 float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 0.5);
 for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 0.5);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 0.5);
 VecFloat* u = VecGetOp(v, a[0], w, a[1]);
 VecFloat2D u2 = VecGet0p(&v2, a[0], &w2, a[1]);
 VecFloat3D u3 = VecGet0p(&v3, a[0], &w3, a[1]);
 float checku[5] = \{5.2,3.1,1.0,-1.1,-3.2\};
 float checku2[2] = \{-0.8, -2.9\};
 float checku3[3] = \{1.2,-0.9,-3.0\};
 for (int i = 5; i--;)
   if (!ISEQUALF(VecGet(u, i), checku[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
 for (int i = 2; i--;)
   if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
```

```
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
  VecOp(v, a[0], w, a[1]);
  VecOp(&v2, a[0], &w2, a[1]);
  VecOp(&v3, a[0], &w3, a[1]);
  if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &u2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &u3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 VecFree(&u);
 printf("UnitTestVecFloatOp OK\n");
void UnitTestVecFloatDotProd() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
  float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
  for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1.5);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
  float prod = VecDotProd(v, w);
  if (!ISEQUALF(prod, -10.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v2, &w2);
 if (!ISEQUALF(prod, -0.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v3, &w3);
  if (!ISEQUALF(prod, -3.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
   PBErrCatch(PBMathErr);
```

```
VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecFloatDotProd OK\n");
void UnitTestVecFloatCrossProd() {
  VecFloat* v = VecFloatCreate(3);
  VecFloat3D v3 = VecFloatCreateStatic3D();
  VecFloat* w = VecFloatCreate(3);
  VecFloat3D w3 = VecFloatCreateStatic3D();
  float a[3] = \{3.0, -3.0, 1.0\};
  float b[3] = \{4.0, 9.0, 2.0\};
  float c[3] = \{-15.0, -2.0, 39.0\};
  for (int i = 3; i--;) VecSet(v, i, a[i]);
  for (int i = 3; i--;) VecSet(&v3, i, a[i]);
  for (int i = 3; i--;) VecSet(w, i, b[i]);
  for (int i = 3; i--;) VecSet(&w3, i, b[i]);
  VecFloat* prod = VecCrossProd(v, w);
  for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(prod, i), c[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatCrossProd NOK");
      PBErrCatch(PBMathErr);
  VecFloat3D prod3 = VecCrossProd(&v3, &w3);
  for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&prod3, i), c[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecFloatCrossProd3D NOK");
      PBErrCatch(PBMathErr);
    }
  VecFree(&v);
  VecFree(&w);
  VecFree(&prod);
 printf("UnitTestVecFloatCrossProd OK\n");
void UnitTestVecFloatRotAngleTo() {
  VecFloat* v = VecFloatCreate(2);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat* w = VecFloatCreate(2);
  VecFloat2D w2 = VecFloatCreateStatic2D();
  VecSet(v, 0, 1.0);
  VecSet(&v2, 0, 1.0);
  VecSet(w, 0, 1.0);
  VecSet(&w2, 0, 1.0);
  float a = 0.0;
  float da = PBMATH_TWOPI_DIV_360;
  for (int i = 360; i--;) {
    VecRot(v, da);
    VecNormalise(v);
    VecRot(&v2. da):
    VecNormalise(&v2);
    a += da;
    if (ISEQUALF(a, PBMATH_PI)) {
      a = -PBMATH_PI;
      if (!ISEQUALF(fabs(VecAngleTo(w, v)), fabs(a))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
      if (!ISEQUALF(fabs(VecAngleTo(&w2, &v2)), fabs(a))) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
    } else {
      if (!ISEQUALF(VecAngleTo(w, v), a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
      if (!ISEQUALF(VecAngleTo(&w2, &v2), a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
      }
   }
  VecSet(v, 0, 1.0);
  VecSet(v, 1, 0.0);
  VecRot(v, PBMATH_QUARTERPI);
  VecFloatPrint(v,stdout,6);printf("\n");
  if (!ISEQUALF(VecGet(v, 0), 0.707107) ||
  !ISEQUALF(VecGet(v, 1), 0.707107)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatRot NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v):
  VecFree(&w);
 printf("UnitTestVecFloatAngleTo OK\n");
void UnitTestVecFloatToShort() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  VecShort* w = VecFloatToShort(v);
  VecShort2D w2 = VecFloatToShort2D(&v2);
  VecShort3D w3 = VecFloatToShort3D(&v3);
  VecPrintln(w, stdout);
  VecPrintln(&w2, stdout);
  VecPrintln(&w3, stdout);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecFloatToShort OK\n");
void UnitTestSpeedVecFloat() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  int nbTest = 100000;
  srandom(RANDOMSEED);
  int i = nbTest;
  clock_t clockBefore = clock();
  for (; i--;) {
    int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
    float val = 1.0;
```

```
VecSet(v, j, val);
    float valb = VecGet(v, j);
   valb = valb;
 }
 clock_t clockAfter = clock();
 double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 float* array = malloc(sizeof(float) * 5);
 for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
   float val = 1.0;
   array[j] = val;
   float valb = array[j];
   valb = valb;
 }
 clockAfter = clock();
 double timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecFloat: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
    float val = 1.0;
    VecSet(&v2, j, val);
   float valb = VecGet(&v2, j);
   valb = valb;
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 float array2[2];
 for (; i--;) {
    int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
   float val = 1.0:
   array2[j] = val;
   float valb = array2[j];
   valb = valb;
 }
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecFloat2D: \%fms, array: \%fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
```

```
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
    PBErrCatch(PBMathErr);
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
    float val = 1.0;
    VecSet(&v3, j, val);
    float valb = VecGet(&v3, j);
    valb = valb;
  }
  clockAfter = clock();
  timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  float array3[3];
  for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
    float val = 1.0;
    array3[j] = val;
    float valb = array3[j];
   valb = valb;
  clockAfter = clock();
  timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("VecFloat3D: \%fms, array: \%fms \n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
   PBErrCatch(PBMathErr);
  VecFree(&v);
  free(array);
 printf("UnitTestSpeedVecFloat OK\n");
void UnitTestVecFloatRotAxis() {
  VecFloat3D v = VecFloatCreateStatic3D();
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 0.0); VecSet(&v, 2, 1.0);
  VecFloat3D axis = VecFloatCreateStatic3D();
  VecSet(&axis, 0, 1.0); VecSet(&axis, 1, 1.0); VecSet(&axis, 2, 1.0);
  VecNormalise(&axis);
  float theta = PBMATH_PI;
  VecRotAxis(&v, &axis, theta);
  if (!ISEQUALF(VecGet(&v, 0), 0.333333) ||
    !ISEQUALF(VecGet(&v, 1), 1.333333) ||
!ISEQUALF(VecGet(&v, 2), 0.333333)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "VecRotAxis NOK");
    PBErrCatch(PBMathErr);
  theta = PBMATH_HALFPI;
  VecRotAxis(&v, &axis, theta);
  if (!ISEQUALF(VecGet(&v, 0), 0.089316) ||
    !ISEQUALF(VecGet(&v, 1), 0.666666) ||
    !ISEQUALF(VecGet(&v, 2), 1.244017)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotAxis NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotX(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), 1.0) ||
    !ISEQUALF(VecGet(&v, 1), -1.0) ||
    !ISEQUALF(VecGet(&v, 2), -1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotX NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotY(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
    !ISEQUALF(VecGet(&v, 1), 1.0) ||
!ISEQUALF(VecGet(&v, 2), -1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotY NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotZ(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
    !ISEQUALF(VecGet(&v, 1), -1.0) ||
    !ISEQUALF(VecGet(&v, 2), 1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotZ NOK");
    PBErrCatch(PBMathErr);
printf("UnitTestVecFloatRotAxis OK\n");
}
void UnitTestVecFloatGetMinMax() {
  VecFloat2D v = VecFloatCreateStatic2D();
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 2.0);
  float val = VecGetMaxVal(&v);
  if (ISEQUALF(val, 2.0) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
    PBErrCatch(PBMathErr);
  if (VecGetIMaxVal(&v) != 1) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetIMaxVal NOK");
    PBErrCatch(PBMathErr);
  val = VecGetMinVal(&v);
  if (ISEQUALF(val, 1.0) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 1.0); VecSet(&v, 1, -2.0);
  val = VecGetMaxValAbs(&v);
  if (ISEQUALF(val, -2.0) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
   PBErrCatch(PBMathErr);
 val = VecGetMinValAbs(&v);
 if (ISEQUALF(val, 1.0) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecFloatGetMinMax OK\n");
void UnitTestVecFloatGetNewDim() {
 VecFloat* v = VecFloatCreate(3);
 for (int i = 3; i--;)
   VecSet(v, i, (float)i);
  VecFloat* u = VecGetNewDim(v, 2);
  if (VecGetDim(u) != 2 ||
    ISEQUALF(VecGet(u, 0), 0.0) == false ||
    ISEQUALF(VecGet(u, 1), 1.0) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetNewDim NOK");
   PBErrCatch(PBMathErr);
 VecFloat* w = VecGetNewDim(v, 4);
 if (VecGetDim(w) != 4 ||
    ISEQUALF(VecGet(w, 1), 1.0) == false ||
    ISEQUALF(VecGet(w, 2), 2.0) == false | |
    ISEQUALF(VecGet(w, 3), 0.0) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetNewDim NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&u);
 VecFree(&w);
 printf("UnitTestVecFloatGetNewDim OK\n");
void UnitTestVecFloatHadamardProd() {
 VecFloat* u = VecFloatCreate(3);
 for (int i = 3; i--;)
    VecSet(u, i, (float)i + 2.0);
  VecFloat* uprod = VecGetHadamardProd(u, u);
 VecHadamardProd(u, u);
  float checku[3] = \{4.0, 9.0, 16.0\};
 for (int i = 3; i--;)
    if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
  if (VecIsEqual(uprod, u) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&uprod);
 VecFree(&u);
 VecFloat2D v = VecFloatCreateStatic2D();
 for (int i = 2; i--;)
   VecSet(&v, i, (float)i + 2.0);
 VecFloat2D vprod = VecGetHadamardProd(&v, &v);
 VecHadamardProd(&v, &v);
 float checkv[2] = \{4.0, 9.0\};
 for (int i = 2; i--;)
   if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&vprod, &v) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 VecFloat3D w = VecFloatCreateStatic3D();
 for (int i = 3; i--;)
   VecSet(&w, i, (float)i + 2.0);
 VecFloat3D wprod = VecGetHadamardProd(&w, &w);
 VecHadamardProd(&w, &w);
 float checkw[3] = {4.0, 9.0, 16.0};
 for (int i = 3; i--;)
   if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
     PBErrCatch(PBMathErr);
 if (VecIsEqual(&wprod, &w) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecFloatHadamardProd OK\n");
void UnitTestVecFloat() {
 UnitTestVecFloatCreateFree();
 UnitTestVecFloatClone();
 UnitTestVecFloatLoadSave();
 UnitTestVecFloatGetSetDim();
 UnitTestVecFloatCopy();
 UnitTestVecFloatNorm();
 UnitTestVecFloatDist();
 UnitTestVecFloatIsEqual();
 UnitTestVecFloatScale();
 UnitTestVecFloatOp();
 UnitTestVecFloatDotProd();
 UnitTestVecFloatCrossProd();
 UnitTestVecFloatRotAngleTo();
 UnitTestVecFloatToShort();
 UnitTestVecFloatGetMinMax();
 UnitTestVecFloatRotAxis();
 UnitTestVecFloatGetNewDim();
 UnitTestVecFloatHadamardProd();
 UnitTestSpeedVecFloat();
```

```
printf("UnitTestVecFloat OK\n");
void UnitTestMatFloatCreateFree() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  for (int i = VecGet(&dim, 0) * VecGet(&dim, 1);i--;) {
    if (!ISEQUALF(mat->_val[i], 0.0)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatCreateFree NOK");
      PBErrCatch(PBMathErr);
    }
  }
  MatFree(&mat);
  if (mat != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "mat is not null after MatFree");
    PBErrCatch(PBMathErr);
printf("UnitTestMatFloatCreateFree OK\n");
}
void UnitTestMatFloatGetSetDim() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  if (!VecIsEqual(&(mat->_dim), &dim)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(MatDim(mat), &dim)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
    PBErrCatch(PBMathErr);
  if (MatGetNbRow(mat) != 3) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetNbRow NOK");
    PBErrCatch(PBMathErr);
  if (MatGetNbCol(mat) != 2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetNbCol NOK");
    PBErrCatch(PBMathErr);
  VecShort2D i = VecShortCreateStatic2D();
  float v = 1.0;
  do {
    MatSet(mat, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
  v = 1.0;
  for (int j = 0; j < VecGet(\&dim, 0); ++j) {
    for (int k = 0; k < VecGet(\&dim, 1); ++k) {
      if (!ISEQUALF(mat->_val[k * VecGet(&dim, 0) + j], v)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
        PBErrCatch(PBMathErr);
```

```
v += 1.0;
  VecSetNull(&i);
  v = 1.0;
  do {
    float w = MatGet(mat, &i);
    if (!ISEQUALF(v, w)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
      PBErrCatch(PBMathErr);
    v += 1.0;
  } while(VecStep(&i, &dim));
  MatFree(&mat);
 printf("UnitTestMatFloatGetSetDim OK\n");
void UnitTestMatFloatCloneIsEqual() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v = 1.0;
  do {
    MatSet(mat, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
  MatFloat* clone = MatClone(mat);
  if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
    PBErrCatch(PBMathErr);
  VecSetNull(&i);
  do {
    if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
      PBErrCatch(PBMathErr);
  } while(VecStep(&i, &dim));
if (MatIsEqual(mat, clone) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK1");
    PBErrCatch(PBMathErr);
  VecSet(&i, 0, 0); VecSet(&i, 1, 0);
  MatSet(clone, &i, -1.0);
  if (MatIsEqual(mat, clone) == true) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK2");
    PBErrCatch(PBMathErr);
  MatFree(&mat);
  MatFree(&clone);
  printf("UnitTestMatFloatCloneIsEqual OK\n");
void UnitTestMatFloatLoadSave() {
```

```
VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do ſ
   MatSet(mat, &i, v);
   v += 1.0;
 } while(VecStep(&i, &dim));
 FILE* f = fopen("./UnitTestMatFloatLoadSave.txt", "w");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
   sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestMatFloatLoadSave.txt for writing");
   PBErrCatch(PBMathErr);
 bool compact = false;
 if (!MatSave(mat, f, compact)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_MatFloatSave NOK");
   PBErrCatch(PBMathErr);
 }
 fclose(f);
 MatFloat* clone = MatFloatCreate(&dim);
 f = fopen("./UnitTestMatFloatLoadSave.txt", "r");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
   sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestMatFloatLoadSave.txt for reading");
   PBErrCatch(PBMathErr);
 if (!MatLoad(&clone, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_MatFloatLoad NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
   PBErrCatch(PBMathErr);
 VecSetNull(&i);
 do {
   if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
     PBErrCatch(PBMathErr);
 } while(VecStep(&i, &dim));
 fclose(f);
 MatFree(&mat):
 MatFree(&clone);
 int ret = system("cat ./UnitTestMatFloatLoadSave.txt");
 ret = ret:
 printf("UnitTestMatFloatLoadSave OK\n");
void UnitTestMatFloatTransposeScale() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
```

```
MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v[6] = \{3.0, 2.0, 1.0, 2.0, -2.0, 1.0\};
  int j = 0;
  do {
   MatSet(mat, &i, v[j]);
   ++j;
  } while(VecStep(&i, &dim));
  MatFloat* trans = MatGetTranspose(mat);
  float w[6] = \{3.0, 2.0, 2.0, -2.0, 1.0, 1.0\};
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 2);
  VecSetNull(&i);
  j = 0;
  do {
    if (!ISEQUALF(MatGet(trans, &i), w[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatTranspose NOK");
      PBErrCatch(PBMathErr);
   }
    ++j;
  } while(VecStep(&i, &dim));
  MatScale(mat, 2.0);
  j = 0;
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  VecSetNull(&i);
  float u[6] = \{6.0, 4.0, 2.0, 4.0, -4.0, 2.0\};
  do {
    if (!ISEQUALF(MatGet(mat, &i), u[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "MatScale NOK");
      PBErrCatch(PBMathErr);
    }
    ++j;
  } while(VecStep(&i, &dim));
  MatFree(&mat);
  MatFree(&trans);
 printf("UnitTestMatFloatTransposeScale OK\n");
}
void UnitTestMatFloatInv() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v[9] = \{3.0, 2.0, 0.0, 0.0, 0.0, 1.0, 2.0, -2.0, 1.0\};
  int j = 0;
  do {
    MatSet(mat, &i, v[j]);
    ++j;
  } while(VecStep(&i, &dim));
  MatFloat* inv = MatGetInv(mat);
  float w[9] = \{0.2, -0.2, 0.2, 0.2, 0.3, -0.3, 0.0, 1.0, 0.0\};
  VecSetNull(&i);
  j = 0;
  do {
    if (!ISEQUALF(MatGet(inv, &i), w[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (1)");
      PBErrCatch(PBMathErr);
```

```
++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);
VecSet(&dim, 0, 2);
VecSet(&dim, 1, 2);
mat = MatFloatCreate(&dim);
float vb[4] = \{4.0, 2.0, 7.0, 6.0\};
VecSetNull(&i);
j = 0;
do {
 MatSet(mat, &i, vb[j]);
 ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
float wb[4] = \{0.6, -0.2, -0.7, 0.4\};
VecSetNull(&i);
j = 0;
do {
  if (!ISEQUALF(MatGet(inv, &i), wb[j])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (2)");
    PBErrCatch(PBMathErr);
 ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);
VecSet(&dim, 0, 4);
VecSet(&dim, 1, 4);
mat = MatFloatCreate(&dim);
float vc[16] = \{4, 0, 0, 0, 0, 1, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1\};
VecSetNull(&i);
j = 0;
do {
 MatSet(mat, &i, vc[j]);
  ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv == NULL) {
 PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (3)");
 PBErrCatch(PBMathErr);
float wc[16] = \{0.25, 0, 0, 0, 0, 1, -1, 0, 0, 0, 0.5, 0, -0.25, 0, 0, 1\};
VecSetNull(&i);
j = 0;
do {
 if (!ISEQUALF(MatGet(inv, &i), wc[j])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (4)");
    PBErrCatch(PBMathErr);
  }
 ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);
mat = MatFloatCreate(&dim);
```

```
float vd[16] = {4, 0, 0, 0, 0, 0, 2, 0, 0, 1, 2, 0, 1, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
  MatSet(mat, &i, vd[j]);
  ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv == NULL) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (3)");
 PBErrCatch(PBMathErr);
float wd[16] = \{0.25, 0, 0, 0, 0, -1, 1, 0, 0, 0.5, 0, 0, -0.25, 0, 0, 1\};
VecSetNull(&i);
j = 0;
do {
  if (!ISEQUALF(MatGet(inv, &i), wd[j])) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (5)");
    PBErrCatch(PBMathErr);
  }
  ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);
mat = MatFloatCreate(&dim);
float ve[16] = \{4, 0, 0, 0, 0, 0, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1\};
VecSetNull(&i);
j = 0;
do {
 MatSet(mat, &i, ve[j]);
  ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv != NULL) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (6)");
 PBErrCatch(PBMathErr);
MatFree(&mat);
mat = MatFloatCreate(&dim);
float vf[16] = {0, 1, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1, 4, 0, 0, 0};
VecSetNull(&i);
j = 0;
do {
 MatSet(mat, &i, vf[j]);
  ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv != NULL) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (7)");
 PBErrCatch(PBMathErr);
/* TODO
if (inv == NULL) {
 PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (7)");
  PBErrCatch(PBMathErr);
```

```
float wf[16] = \{0, 0, 0, 0.25, 1, -1, 0, 0, 0, 0.5, 0, 0, 0, 1, -0.25\};
 VecSetNull(&i);
 j = 0;
 do {
   if (!ISEQUALF(MatGet(inv, &i), wf[j])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (8)");
     PBErrCatch(PBMathErr);
   }
   ++j;
 } while(VecStep(&i, &dim));
 MatFree(&inv);
 MatFree(&mat);
 mat = MatFloatCreate(&dim);
 float vg[16] = \{0, 1, 2, 0, 0, 0, 2, 0, 4, 0, 0, 0, 1, 0, 0, 1\};
  VecSetNull(&i);
 j = 0;
 do {
   MatSet(mat, &i, vg[j]);
   ++j;
 } while(VecStep(&i, &dim));
 inv = MatGetInv(mat);
 if (inv != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (9)");
   PBErrCatch(PBMathErr);
 /* TODO
 if (inv == NULL) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (9)");
   PBErrCatch(PBMathErr);
 float wg[16] = \{0, 0, 0.25, 0, 1, -1, 0, 0, 0, 0.5, 0, 0, 0, 0, -0.25, 1\};
 VecSetNull(&i);
 j = 0;
 do {
   if (!ISEQUALF(MatGet(inv, &i), wg[j])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (10)");
     PBErrCatch(PBMathErr);
   ++j;
 } while(VecStep(&i, &dim));
 MatFree(&inv);
 */
 MatFree(&mat);
 printf("UnitTestMatFloatInv OK\n");
void UnitTestMatFloatProdVecFloat() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
```

```
MatSet(mat, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
  VecFloat2D u = VecFloatCreateStatic2D();
  for (int j = 2; j--;)
  VecSet(&u, j, (float)j + 1.0);
VecFloat* w = MatGetProdVec(mat, &u);
  float b[3] = \{9.0, 12.0, 15.0\};
  for (int j = 3; j--;) {
    if (!ISEQUALF(VecGet(w, j), b[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatProdVecFloat NOK");
      PBErrCatch(PBMathErr);
  }
  MatFree(&mat);
  VecFree(&w);
 printf("UnitTestMatFloatProdVecFloat OK\n");
void UnitTestMatFloatProdMatFloat() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 2);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v = 1.0;
  do {
   MatSet(mat, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  MatFloat* matb = MatFloatCreate(&dim);
  VecSetNull(&i);
  v = 1.0;
  do {
   MatSet(matb, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
  MatFloat* matc = MatGetProdMat(mat, matb);
  float w[4] = \{22.0, 28.0, 49.0, 64.0\};
  VecSetNull(&i);
  int j = 0;
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 2);
  if (!VecIsEqual(&dim, &(matc->_dim))) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
    PBErrCatch(PBMathErr);
  do {
    if (!ISEQUALF(MatGet(matc, &i), w[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
      PBErrCatch(PBMathErr);
    ++j;
  } while(VecStep(&i, &dim));
  MatFree(&mat);
  MatFree(&matb):
  MatFree(&matc);
```

```
printf("UnitTestMatFloatProdMatFloat OK\n");
void UnitTestMatFloatProdVecVecTranspose() {
 VecFloat2D v = VecFloatCreateStatic2D();
  VecFloat3D w = VecFloatCreateStatic3D();
 VecSet(&v, 0, 2.0);
 VecSet(&v, 1, 3.0);
 VecSet(&w, 0, 4.0);
 VecSet(&w, 1, 5.0);
  VecSet(&w, 2, 6.0);
 MatFloat* mat = MatGetProdVecVecTranspose(&v, &w);
  VecShort2D pos = VecShortCreateStatic2D();
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 2);
 float check[6] = {8.0, 12.0, 10.0, 15.0, 12.0, 18.0};
 int i = 0;
  do {
   if (!ISEQUALF(MatGet(mat, &pos), check[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "MatGetProdVecVecTranspose NOK");
     PBErrCatch(PBMathErr);
   ++i;
 } while (VecStep(&pos, &dim));
 MatFree(&mat);
 printf("UnitTestMatFloatProdVecVecTranspose OK\n");
void UnitTestMatFloatGetEigenValues() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 3);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D pos = VecShortCreateStatic2D();
  float check[3][3] = {
    { 2.92, 0.86, -1.15},
    { 0.86, 6.51, 3.32},
   {-1.15, 3.32, 4.57}
 };
 do {
   MatSet(mat, &pos, check[VecGet(&pos, 1)][VecGet(&pos, 0)]);
  } while (VecStep(&pos, &dim));
  printf("mat:\n"); MatPrintln(mat, stdout);
  GSetVecFloat set = MatGetEigenValues(mat);
  printf("Eigen values: ");
  VecPrintln(GSetGet(&set, 0), stdout);
  VecFloat3D checkValues = VecFloatCreateStatic3D();
  VecSet(&checkValues, 0, 8.998802);
  VecSet(&checkValues, 1, 3.996595);
  VecSet(&checkValues, 2, 1.004607);
  if (!VecIsEqual(GSetGet(&set, 0), &checkValues)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
   PBErrCatch(PBMathErr);
  printf("Eigen vector 1: ");
  VecPrintln(GSetGet(&set, 1), stdout);
 printf("Eigen vector 2: ");
  VecPrintln(GSetGet(&set, 2), stdout);
 printf("Eigen vector 3: ");
```

```
VecPrintln(GSetGet(&set, 3), stdout);
  VecFloat3D checkVecA = VecFloatCreateStatic3D();
  VecSet(&checkVecA, 0, 0.000290);
 VecSet(&checkVecA, 1, -0.800102);
  VecSet(&checkVecA, 2, -0.599864);
  if (!VecIsEqual(GSetGet(&set, 1), &checkVecA)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
   PBErrCatch(PBMathErr);
 VecFloat3D checkVecB = VecFloatCreateStatic3D();
  VecSet(&checkVecB, 0, 0.800110);
 VecSet(&checkVecB, 1, 0.360017);
  VecSet(&checkVecB, 2, -0.479806);
  if (!VecIsEqual(GSetGet(&set, 2), &checkVecB)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
   PBErrCatch(PBMathErr);
 VecFloat3D checkVecC = VecFloatCreateStatic3D();
  VecSet(&checkVecC, 0, 0.599855);
 VecSet(&checkVecC, 1, -0.479817);
VecSet(&checkVecC, 2, 0.640273);
  if (!VecIsEqual(GSetGet(&set, 3), &checkVecC)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
   PBErrCatch(PBMathErr);
 }
 do {
   VecFloat* v = GSetPop(&set);
    VecFree(&v);
  } while (GSetNbElem(&set) > 0);
 MatFree(&mat);
 printf("UnitTestMatFloatGetEigenValues OK\n");
void UnitTestSpeedMatFloat() {
  VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 3);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 int nbTest = 100000;
  srandom(RANDOMSEED);
 int i = nbTest;
  clock_t clockBefore = clock();
  VecShort2D j = VecShortCreateStatic2D();
 for (; i--;) {
   float val = 1.0;
   MatSet(mat, &j, val);
    float valb = MatGet(mat, &j);
    valb = valb;
    VecStep(&j, &dim);
 }
 clock_t clockAfter = clock();
  double timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
  clockBefore = clock();
  float* array = malloc(sizeof(float) * 9);
  short *ptr = j._val;
 for (; i--;) {
```

```
float val = 1.0;
    int k = ptr[1] * 3 + ptr[0];
    array[k] = val;
    float valb = array[k];
    valb = valb;
   VecStep(&j, &dim);
  clockAfter = clock();
  double timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("MatFloat: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedMatFloat NOK");
    PBErrCatch(PBMathErr);
  MatFree(&mat);
  free(array);
 printf("UnitTestSpeedMatFloat OK\n");
void UnitTestMatFloatGetQR() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 4);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D pos = VecShortCreateStatic2D();
  float val[4][3] = {
      \{-1.0, -1.0, 1.0\},\
      { 1.0, 3.0, 3.0},
{-1.0, -1.0, 5.0},
{ 1.0, 3.0, 7.0}
    };
  do {
   MatSet(mat, &pos, val[VecGet(&pos, 1)][VecGet(&pos, 0)]);
  } while (VecStep(&pos, &dim));
  QRDecomp qr = MatGetQR(mat);
  MatFloat* QR = MatGetProdMat(qr._Q, qr._R);
  printf("mat:\n");
  MatPrintln(mat, stdout);
  printf("Q:\n");
  MatPrintln(qr._Q, stdout);
  printf("R:\n");
  MatPrintln(qr._R, stdout);
  printf("QR:\n");
  MatPrintln(QR, stdout);
  MatFloat* Q = MatFloatCreate(&dim);
  VecSetNull(&pos);
  float checkQ[4][3] = {
      {-0.5, -0.5, 0.5},
{ 0.5, -0.5, 0.5},
{-0.5, -0.5, -0.5},
      { 0.5, -0.5, -0.5}
   };
  do {
    MatSet(Q, &pos, checkQ[VecGet(&pos, 1)][VecGet(&pos, 0)]);
```

```
} while (VecStep(&pos, &dim));
  VecSet(&dim, 1, 3);
  MatFloat* R = MatFloatCreate(&dim);
  VecSetNull(&pos);
  float checkR[3][3] = {
      {2.0, 4.0, 2.0},
{0.0, -2.0, -8.0},
      \{0.0, 0.0, -4.0\}
   };
  do {
    MatSet(R, &pos, checkR[VecGet(&pos, 1)][VecGet(&pos, 0)]);
  } while (VecStep(&pos, &dim));
  if (!MatIsEqual(Q, qr._Q) || !MatIsEqual(R, qr._R) ||
    !MatIsEqual(QR, mat)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetQR NOK");
    PBErrCatch(PBMathErr);
  MatFree(&mat);
  MatFree(&Q):
  MatFree(&R);
  MatFree(&QR);
  QRDecompFreeStatic(&qr);
 printf("UnitTestMatFloatGetQR OK\n");
void UnitTestMatFloat() {
  UnitTestMatFloatCreateFree();
  UnitTestMatFloatGetSetDim():
  UnitTestMatFloatCloneIsEqual();
  UnitTestMatFloatLoadSave();
  UnitTestMatFloatInv();
  UnitTestMatFloatTransposeScale();
  UnitTestMatFloatProdVecFloat();
  UnitTestMatFloatProdMatFloat();
  UnitTestMatFloatGetQR();
  UnitTestMatFloatProdVecVecTranspose();
  UnitTestMatFloatGetEigenValues();
  UnitTestSpeedMatFloat();
 printf("UnitTestMatFloat OK\n");
void UnitTestSysLinEq() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  float a[9] = {2.0, 2.0, 6.0, 1.0, 6.0, 8.0, 3.0, 8.0, 18.0};
  VecShort2D index = VecShortCreateStatic2D();
  int j = 0;
  do {
    MatSet(mat, &index, a[j]);
    ++j;
  } while(VecStep(&index, &dim));
  VecFloat3D v = VecFloatCreateStatic3D();
  float b[3] = \{1.0, 3.0, 5.0\};
  for (int i = 3; i--;)
    VecSet(&v, i, b[i]);
  SysLinEq* sys = SysLinEqCreate(mat, &v);
  VecFloat* res = SysLinEqSolve(sys);
  float c[3] = \{0.3, 0.4, 0\};
  for (int i = 3; i--;) {
```

```
if (!ISEQUALF(c[i], VecGet(res, i))) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
     PBErrCatch(PBMathErr);
 float ab[9] = \{3.0, 2.0, -1.0, 2.0, -2.0, 0.5, -1.0, 4.0, -1.0\};
 VecSetNull(&index);
  j = 0;
 do {
   MatSet(mat, &index, ab[j]);
  } while(VecStep(&index, &dim));
 SysLinEqSetM(sys, mat);
  float bb[3] = \{1.0, -2.0, 0.0\};
  for (int i = 3; i--;)
   VecSet(&v, i, bb[i]);
  SysLinEqSetV(sys, &v);
  VecFree(&res);
 res = SysLinEqSolve(sys);
  float cb[3] = \{1.0, -2.0, -2.0\};
 for (int i = 3; i--;) {
    if (!ISEQUALF(cb[i], VecGet(res, i))) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
     PBErrCatch(PBMathErr);
   }
 }
 VecFree(&res);
 SysLinEqFree(&sys);
  if (sys != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "sys is not null after free");
   PBErrCatch(PBMathErr);
 MatFree(&mat):
 printf("UnitTestSysLinEq OK\n");
void UnitTestGauss() {
 srandom(RANDOMSEED);
 float mean = 1.0;
 float sigma = 0.5;
 Gauss *gauss = GaussCreate(mean, sigma);
  if (!ISEQUALF(gauss->_mean, mean) ||
    !ISEQUALF(gauss->_sigma, sigma)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussCreate NOK");
   PBErrCatch(PBMathErr);
  float a[22] = {0.000268, 0.001224, 0.004768, 0.015831, 0.044789,
    0.107982, 0.221842, 0.388372, 0.579383, 0.736540, 0.797885,
    0.736540,\ 0.579383,\ 0.388372,\ 0.221842,\ 0.107982,\ 0.044789,
   0.015831, 0.004768, 0.001224, 0.000268};
  for (int i = -5; i<= 15; ++i) {
    if (!ISEQUALF(GaussGet(gauss, (float)i * 0.2), a[i + 5])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestGaussGet NOK");
      PBErrCatch(PBMathErr);
 }
 int nbsample = 1000000;
```

```
double sum = 0.0;
  double sumsquare = 0.0;
  for (int i = nbsample; i--;) {
   float v = GaussRnd(gauss);
    sum += v;
   sumsquare += fsquare(v);
  double avg = sum / (double)nbsample;
  double sig = sqrtf(sumsquare / (double)nbsample - fsquare(avg));
  if (fabs(avg - mean) > 0.001 \mid \mid
    fabs(sig - sigma) > 0.001) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussRnd NOK");
    PBErrCatch(PBMathErr);
  GaussFree(&gauss);
  if (gauss != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "gauss is not null after free");
    PBErrCatch(PBMathErr);
  }
 printf("UnitTestGauss OK\n");
void UnitTestSmoother() {
  float smooth[11] = {0.0, 0.028, 0.104, 0.216, 0.352, 0.5, 0.648,
    0.784, 0.896, 0.972, 1.0};
  float smoother[11] = {0.0, 0.00856, 0.05792, 0.16308, 0.31744, 0.5,
    0.68256, 0.83692, 0.94208, 0.99144, 1.0};
  for (int i = 0; i <= 10; ++i) {
    if (!ISEQUALF(SmoothStep((float)i * 0.1), smooth[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestSmooth NOK");
      PBErrCatch(PBMathErr);
    if (!ISEQUALF(SmootherStep((float)i * 0.1), smoother[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestSmoother NOK");
      PBErrCatch(PBMathErr);
 printf("UnitTestSmoother OK\n");
void UnitTestConv() {
  float rad[5] = {0.0, PBMATH_TWOPI, PBMATH_PI, PBMATH_HALFPI, 3.0 * PBMATH_HALFPI};
  float deg[5] = {0.0, 360.0, 180.0, 90.0, 270.0};
  for (int i = 5; i--;) {
    if (!ISEQUALF(ConvRad2Deg(rad[i]), deg[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestConvRad2Deg NOK");
      PBErrCatch(PBMathErr);
    }
    if (!ISEQUALF(ConvDeg2Rad(deg[i]), rad[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestConvDeg2Rad NOK");
      PBErrCatch(PBMathErr);
   }
printf("UnitTestConv OK\n");
}
```

```
void UnitTestThueMorseSeq() {
  long seq_2[16] = \{0,1,1,0,1,0,0,1,1,0,0,1,0,1,1,0\};
  long seq_3[27] = \{0,1,2,1,2,0,2,0,1,1,2,0,2,0,1,0,
   1,2,2,0,1,0,1,2,1,2,0};
  long seq_4[64] = \{0,1,2,3,1,2,3,0,2,3,0,1,3,0,1,2,
    1,2,3,0,2,3,0,1,3,0,1,2,0,1,2,3,2,3,0,1,3,0,1,2,
    0,1,2,3,1,2,3,0,3,0,1,2,0,1,2,3,1,2,3,0,2,3,0,1;
  for (long iElem = 0; iElem < 16; ++iElem) {</pre>
    long thuemorse = ThueMorseSeqGetNthElem(iElem, 2);
    if (thuemorse != seq_2[iElem]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "ThueMorseSeqGetNthElem NOK (%ld,2)",
        iElem):
      PBErrCatch(PBMathErr);
   }
  }
  for (long iElem = 0; iElem < 27; ++iElem) {</pre>
    long thuemorse = ThueMorseSeqGetNthElem(iElem, 3);
    if (thuemorse != seq_3[iElem]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      {\tt sprintf(PBMathErr->\_msg,\ "ThueMorseSeqGetNthElem\ NOK\ (\%ld,3)",}
        iElem);
      PBErrCatch(PBMathErr);
    }
  for (long iElem = 0; iElem < 64; ++iElem) {
    long thuemorse = ThueMorseSeqGetNthElem(iElem, 4);
    if (thuemorse != seq_4[iElem]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "ThueMorseSeqGetNthElem NOK (%ld,4)",
        iElem);
      PBErrCatch(PBMathErr);
 printf("UnitTestThueMorseSeq OK\n");
void UnitTestGetAreaTriangleHero() {
  double area = GetAreaTriangleHero(5.0, 29.0, 30.0);
  if (!ISEQUALF(area, 72.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetAreaTriangleHero NOK (%f)",
      area);
    PBErrCatch(PBMathErr);
 printf("UnitTestGetAreaTriangleHero OK\n");
void UnitTestGetFibonacciSeq() {
  unsigned long* seq = GetFibonacciSeq(14);
  if (
    seq[0] != 1 ||
    seq[1] != 1 ||
    seq[2] != 2 ||
    seq[3] != 3 ||
    seq[4] != 5 ||
    seq[5] != 8 ||
    seq[6] != 13 ||
    seq[7] != 21 ||
    seq[8] != 34 ||
    seq[9] != 55 ||
```

```
seq[10] != 89 ||
    seq[11] != 144 ||
    seq[12] != 233 ||
    seq[13] != 377) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetFibonacciSeq NOK");
   PBErrCatch(PBMathErr);
  free(seq);
 printf("UnitTestGetFibonacciSeq OK\n");
void UnitTestGetFibonacciLattice() {
  unsigned long nbPoints = 0;
  float* latticeGrid =
    {\tt GetFibonacciGridLattice} (
     &nbPoints);
  if (nbPoints != 5) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetFibonacciGridLattice NOK");
    PBErrCatch(PBMathErr);
  float checkGrid[10] =
    {
     0.000000, 0.000000, 0.200000, 0.600000,
      0.400000, 0.200000,
      0.600000, 0.800000,
      0.800000, 0.400000
   };
  for (int i = 0; i < 10; ++i) {
    if (!ISEQUALF(latticeGrid[i], checkGrid[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "GetFibonacciGridLattice NOK");
      PBErrCatch(PBMathErr);
   }
  }
  free(latticeGrid);
  nbPoints = 0;
  float* latticePolar =
    {\tt GetFibonacciPolarLattice} (
      5,
     &nbPoints);
  if (nbPoints != 5) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetFibonacciPolarLattice NOK");
    PBErrCatch(PBMathErr);
  float checkPolar[10] =
    {
      0.000000, 0.000000,
      0.447214, 3.769911,
      0.632456, 1.256637,
      0.774597, 5.026548,
      0.894427, 2.513275
    };
  for (int i = 0; i < 10; ++i) {
    if (!ISEQUALF(latticePolar[i], checkPolar[i])) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "GetFibonacciPolarLattice NOK");
      PBErrCatch(PBMathErr);
  free(latticePolar);
  printf("UnitTestGetFibonacciLattice OK\n");
void UnitTestGetGCD() {
  unsigned int gcd = GetGCD(4, 6);
  if (gcd != 2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetGCD NOK");
   PBErrCatch(PBMathErr);
  gcd = GetGCD(6, 4);
  if (gcd != 2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetGCD NOK");
    PBErrCatch(PBMathErr);
  gcd = GetGCD(10, 6);
  if (gcd != 2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "GetGCD NOK");
    PBErrCatch(PBMathErr);
 printf("UnitTestGetGCD OK\n");
void UnitTestBasicFunctions() {
  UnitTestConv();
  UnitTestPowi();
  UnitTestFastPow();
  UnitTestSpeedFastPow();
  UnitTestFSquare();
  UnitTestConv();
  UnitTestThueMorseSeq();
  UnitTestGetAreaTriangleHero();
  UnitTestGetFibonacciSeq();
  UnitTestGetFibonacciLattice();
  UnitTestGetGCD();
 printf("UnitTestBasicFunctions OK\n");
void UnitTestRatio() {
  Ratio ratio = RatioCreateStatic(1, 2, 3);
  if (
    ratio._base != 1 ||
    ratio._numerator != 2 ||
    ratio._denominator != 3) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "RatioCreateStatic NOK");
   PBErrCatch(PBMathErr);
  if (RatioGetBase(&ratio) != 1) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioGetBase NOK");
  PBErrCatch(PBMathErr);
if (RatioGetNumerator(&ratio) != 2) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioGetNumerator NOK");
  PBErrCatch(PBMathErr);
if (RatioGetDenominator(&ratio) != 3) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioGetDenominator NOK");
 PBErrCatch(PBMathErr);
if (!ISEQUALF(RatioToFloat(&ratio), 1.666666)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioToFloat NOK");
 PBErrCatch(PBMathErr);
RatioSetBase(&ratio, 4);
if (RatioGetBase(&ratio) != 4) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioSetBase NOK");
 PBErrCatch(PBMathErr);
RatioSetNumerator(&ratio, 5);
if (RatioGetNumerator(&ratio) != 5) {
 PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioSetNumerator NOK");
 PBErrCatch(PBMathErr);
RatioSetDenominator(&ratio, 6);
if (RatioGetDenominator(&ratio) != 6) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioSetDenominator NOK");
 PBErrCatch(PBMathErr);
Ratio ratiob = RatioCreateStatic(0, 10, 6);
RatioPrint(&ratiob, stdout);
printf(" -> ");
RatioReduce(&ratiob);
RatioPrintln(&ratiob, stdout);
if (
 ratiob._base != 1 ||
 ratiob._numerator != 2 ||
  ratiob._denominator != 3) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioReduce NOK");
 PBErrCatch(PBMathErr);
Ratio ratioc = RatioFromFloat(1.666666);
printf("1.666666=");
RatioPrintln(&ratioc, stdout);
if (
 ratioc._base != 1 ||
  ratioc._numerator != 2 ||
  ratioc._denominator != 3 ||
  !ISEQUALF(RatioToFloat(&ratioc), 1.666666)) {
  PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "RatioFromFloat NOK");
 PBErrCatch(PBMathErr);
```

```
ratioc = RatioFromFloat(PBMATH_PI);
  printf("PI=");
  RatioPrintln(&ratioc, stdout);
  if (
    ratioc._base != 3 ||
    ratioc._numerator != 16 ||
    ratioc._denominator != 113 ||
    !ISEQUALF(RatioToFloat(&ratioc), PBMATH_PI)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "RatioFromFloat NOK");
    PBErrCatch(PBMathErr);
printf("UnitTestRatio OK\n");
}
void UnitTestLSLR() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v[6] = \{1.0, 1.0, 1.0, 1.0, 2.0, 3.0\};
  int j = 0;
  do {
    MatSet(mat, &i, v[j]);
    ++j;
  } while(VecStep(&i, &dim));
  LeastSquareLinReg lslr = LeastSquareLinRegCreateStatic(mat);
  VecFloat* Y = VecFloatCreate(3);
  VecSet(Y, 0, 3.0);
  VecSet(Y, 1, 5.0);
  VecSet(Y, 2, 7.0);
  VecFloat* beta = LSLRSolve(&lslr, Y);
  VecFloat* check = VecFloatCreate(2);
  VecSet(check, 0, 1.0);
  VecSet(check, 1, 2.0);
  if (
    VecIsEqual(beta, check) == false ||
    !ISEQUALF(LSLRGetBias(&lslr), 0.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "LSLRSolve NOK (1)");
    PBErrCatch(PBMathErr);
  VecFree(&beta);
  VecSet(Y, 0, 2.75);
  VecSet(Y, 1, 5.25);
  VecSet(Y, 2, 6.75);
  beta = LSLRSolve(&lslr, Y);
  VecSet(check, 0, 0.916666);
  VecSet(check, 1, 2.0);
  if (
    VecIsEqual(beta, check) == false ||
    !ISEQUALF(LSLRGetBias(&lslr), 0.408248)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "LSLRSolve NOK (2)");
    PBErrCatch(PBMathErr);
  VecFree(&beta);
  VecFree(&check);
  VecFree(&Y);
```

```
MatFree(&mat);
 LeastSquareLinRegFreeStatic(&lslr);
 printf("UnitTestLSLR OK\n");
void UnitTestAll() {
 UnitTestVecShort();
  UnitTestVecLong();
 UnitTestVecFloat();
 UnitTestMatFloat();
  UnitTestSysLinEq();
  UnitTestGauss();
 UnitTestSmoother();
  UnitTestBasicFunctions();
 UnitTestRatio();
 UnitTestLSLR();
 printf("UnitTestAll OK\n");
int main() {
 UnitTestAll();
  // Return success code
 return 0;
```

6 Unit tests output

```
{
   "_dim":"5",
   "_val":["1","2","3","4","5"]
}
{
   "_dim":"2",
   "_val":["1","2","3"]
}
{
   "_dim":"4",
   "_val":["1","2","3","4","5"]
}
{
   "_dim":"5",
   "_val":["1","2","3","4","5"]
}
{
   "_dim":"2",
   "_val":["1","2","3"]
}
{
   "_dim":"2",
   "_val":["1","2","3"]
}
{
   "_dim":"3",
   "_val":["1","2","3"]
}
{
   "_dim":"4",
   "_val":["1","2","3","4"]
```

```
"_dim":"5",
  "_val":["1.000000","2.000000","3.000000","4.000000","5.000000"]
  "_dim":"2",
  "_val":["1.000000","2.000000"]
}
  "_dim":"3",
  "_val":["1.000000","2.000000","3.000000"]
}
{
  "_nbRow":"2",
  "_nbCol":"3",
  "_val":["1.000000","2.000000","3.000000","4.000000","5.000000","6.000000"]
}
<0,0,0,0,0>
<0,0>
<0,0,0>
<0,0,0,0>
VecShortCreateFree OK
_VecShortClone OK
_VecShortLoadSave OK
_VecShortGetSetDim OK
UnitTestVecShortStep OK
UnitTestVecShortHamiltonDist OK
{\tt UnitTestVecShortIsEqual\ OK}
UnitTestVecShortDotProd OK
UnitTestVecShortCopy OK
VecShort: 0.000058ms, array: 0.000014ms
VecShort2D: 0.000007ms, array: 0.000006ms
VecShort3D: 0.000006ms, array: 0.000007ms
VecShort4D: 0.000006ms, array: 0.000006ms
UnitTestSpeedVecShort OK
<1.000,2.000,3.000,4.000,5.000>
<1.000,2.000>
<1.000,2.000,3.000>
UnitTestVecShortToFloat OK
<1.000,2.000,3.000,4.000,5.000>
<1.000,2.000>
<1.000,2.000,3.000>
UnitTestVecLongToFloat OK
UnitTestVecShortOp OK
UnitTestVecShortShiftStep OK
UnitTestVecShortGetMinMax OK
UnitTestVecShortHadamardProd OK
UnitTestVecShort OK
<0,0,0,0,0>
<0,0>
<0,0,0>
<0,0,0,0>
VecLongCreateFree OK
_VecLongClone OK
_VecLongLoadSave OK
_VecLongGetSetDim OK
UnitTestVecLongStep OK
UnitTestVecLongHamiltonDist OK
UnitTestVecLongIsEqual OK
UnitTestVecLongDotProd OK
UnitTestVecLongCopy OK
```

```
VecLong: 0.000014ms, array: 0.000014ms
VecLong2D: 0.000006ms, array: 0.000006ms
VecLong3D: 0.000006ms, array: 0.000006ms
VecLong4D: 0.000006ms, array: 0.000007ms
UnitTestSpeedVecLong OK
UnitTestVecLongOp OK
UnitTestVecLongShiftStep OK
UnitTestVecLongGetMinMax OK
UnitTestVecLongHadamardProd OK
{\tt UnitTestVecLong\ OK}
<0.000,0.000,0.000,0.000,0.000>
<0.000,0.000>
<0.000,0.000,0.000>
VecFloatCreateFree OK
_VecFloatClone OK
_VecFloatLoadSave OK
_VecFloatGetSetDim OK
{\tt UnitTestVecFloatCopy\ OK}
UnitTestVecFloatNorm OK
UnitTestVecFloatDist OK
UnitTestVecFloatIsEqual OK
UnitTestVecFloatScale OK
UnitTestVecFloatOp OK
{\tt UnitTestVecFloatDotProd\ OK}
UnitTestVecFloatCrossProd OK
<0.707107,0.707107>
UnitTestVecFloatAngleTo OK
<1,2,3,4,5>
<1.2>
<1,2,3>
UnitTestVecFloatToShort OK
UnitTestVecFloatGetMinMax OK
UnitTestVecFloatRotAxis OK
{\tt UnitTestVecFloatGetNewDim\ OK}
UnitTestVecFloatHadamardProd OK
VecFloat: 0.000016ms, array: 0.000015ms
VecFloat2D: 0.000006ms, array: 0.000006ms
VecFloat3D: 0.000006ms, array: 0.000006ms
{\tt UnitTestSpeedVecFloat\ OK}
UnitTestVecFloat OK
UnitTestMatFloatCreateFree OK
UnitTestMatFloatGetSetDim OK
UnitTestMatFloatCloneIsEqual OK
UnitTestMatFloatLoadSave OK
UnitTestMatFloatInv OK
UnitTestMatFloatTransposeScale OK
UnitTestMatFloatProdVecFloat OK
UnitTestMatFloatProdMatFloat OK
mat:
[-1.000, -1.000, 1.000
1.000, 3.000, 3.000
 -1.000, -1.000, 5.000
1.000, 3.000, 7.000]
Q:
[-0.500, -0.500, 0.500
  0.500, -0.500, 0.500
 -0.500, -0.500, -0.500
0.500, -0.500, -0.500]
R:
[ 2.000, 4.000, 2.000
-0.000, -2.000, -8.000
  0.000, -0.000, -4.000]
```

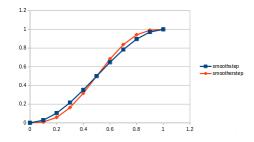
```
QR:
[-1.000, -1.000, 1.000
1.000, 3.000, 3.000
-1.000, -1.000, 5.000
1.000, 3.000, 7.000]
UnitTestMatFloatGetQR OK
{\tt UnitTestMatFloatProdVecVecTranspose\ OK}
[ 2.920, 0.860, -1.150
0.860, 6.510, 3.320
 -1.150, 3.320, 4.570]
Eigen values: <8.999,3.997,1.005>
Eigen vector 1: <0.000,-0.800,-0.600>
Eigen vector 2: <0.800,0.360,-0.480>
Eigen vector 3: <0.600,-0.480,0.640>
UnitTestMatFloatGetEigenValues OK
MatFloat: 0.000003ms, array: 0.000002ms
{\tt UnitTestSpeedMatFloat\ OK}
UnitTestMatFloat OK
UnitTestSysLinEq OK
{\tt UnitTestGauss\ OK}
UnitTestSmoother OK
UnitTestConv OK
powi OK
average error: 0.000000 < 0.000010, max error: 0.000000 < 0.000100
fastpow OK
fastpow: 0.000014ms, pow: 0.000058ms
speed fastpow OK
fsquare OK
UnitTestConv OK
{\tt UnitTestThueMorseSeq\ OK}
{\tt UnitTestGetAreaTriangleHero} \ {\tt OK}
{\tt UnitTestGetFibonacciSeq\ OK}
{\tt UnitTestGetFibonacciLattice\ OK}
UnitTestGetGCD OK
UnitTestBasicFunctions OK
0+10/6 -> 1+2/3
1.666666=1+2/3
PI=3+16/113
UnitTestRatio OK
UnitTestLSLR OK
UnitTestAll OK
```

7 Examples

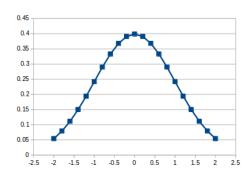
UnitTestVecShortLoadSave.txt:

```
{
    "_dim":"5",
    "_val":["1","2","3","4","5"]
}
{
    "_dim":"2",
    "_val":["1","2"]
}
{
    "_dim":"3",
    "_val":["1","2","3"]
```

```
}
  "_dim":"4",
"_val":["1","2","3","4"]
    Unit Test Vec Long Load Save.txt:\\
  "_dim":"5",
"_val":["1","2","3","4","5"]
}
  "_dim":"2",
"_val":["1","2"]
  "_dim":"3",
"_val":["1","2","3"]
}
  "_dim":"4",
"_val":["1","2","3","4"]
    UnitTestVecFloatLoadSave.txt:\\
  "_dim":"5",
  "_val":["1.000000","2.000000","3.000000","4.000000","5.000000"]
  "_dim":"2",
  "_val":["1.000000","2.000000"]
}
  "_dim":"3",
  "_val":["1.000000","2.000000","3.000000"]
    matfloat.txt:
3 2
0.500000 2.000000 0.000000
2.000000 0.000000 1.000000
    smoother functions:
```



gauss function (mean:0.0, sigma:1.0):



gauss rand function (mean:1.0, sigma:0.5):

