# PBMath

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## Introduction

PBMath is a C library providing mathematical structures and functions.

The VecFloat structure and its functions can be used to manipulate vectors of float values.

The VecShort structure and its functions can be used to manipulate vectors of short values.

The MatFloat structure and its functions can be used to manipulate matrices of float values.

The **Gauss** structure and its functions can be used to get values of the Gauss function and random values distributed accordingly with a Gauss distribution.

The Smoother functions can be used to get values of the SmoothStep and SmootherStep functions.

The EqLinSys structure and its functions can be used to solve systems of linear equation.

It uses the PBErr library.

#### 1 Definitions

#### 1.1 Vector

#### 1.1.1 Distance between two vectors

For VecShort:

$$Dist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$

$$HamiltonDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$

$$PixelDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_{i} - w_{i}|$$
(1)

For VecFloat:

$$Dist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} (v_i - w_i)^2$$

$$HamiltonDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |v_i - w_i|$$

$$PixelDist(\overrightarrow{v}, \overrightarrow{w}) = \sum_{i} |\lfloor v_i \rfloor - \lfloor w_i \rfloor|$$
(2)

#### 1.1.2 Angle between two vectors

The problem is as follow: given two vectors  $\vec{V}$  and  $\vec{W}$  not null, how to calculate the angle  $\theta$  from  $\vec{V}$  to  $\vec{W}$ .

Let's call M the rotation matrix:  $M\vec{V} = \vec{W}$ , and the components of M as follow:

$$M = \begin{bmatrix} Ma & Mb \\ Mc & Md \end{bmatrix} = \begin{bmatrix} cos(\theta) & -sin(\theta) \\ sin(\theta) & cos(\theta) \end{bmatrix}$$
(3)

Then,  $M\vec{V} = \vec{W}$  can be written has

$$\begin{cases}
W_x = M_a V_x + M_b V_y \\
W_y = M_c V_x + M_d V_y
\end{cases}$$
(4)

Equivalent to

$$\begin{cases}
W_x = M_a V_x + M_b V_y \\
W_y = -M_b V_x + M_a V_y
\end{cases}$$
(5)

where  $M_a = cos(\theta)$  and  $M_b = -sin(\theta)$ .

If  $Vx \neq 0.0$ , we can write

$$\begin{cases}
M_b = \frac{M_a V_y - W_y}{V_x} \\
M_a = \frac{W_x + W_y V_y / V_x}{V_x + V_y^2 / V_x}
\end{cases}$$
(6)

Or, if Vx = 0.0, we can write

$$\begin{cases}
Ma = \frac{W_y + M_b V_x}{V_y} \\
Mb = \frac{W_x - W_y V_x / V_y}{V_y + V_x^2 / V_y}
\end{cases}$$
(7)

Then we have  $\theta = \pm \cos^{-1}(M_a)$  where the sign can be determined by verifying that the sign of  $sin(\theta)$  matches the sign of  $-M_b$ : if  $sin(cos^{-1}(M_a))*M_b > 0.0$  then multiply  $\theta = -cos^{-1}(M_a)$  else  $\theta = cos^{-1}(M_a)$ .

#### 1.1.3 Rotation

Rotation if a vector is only defined in 2D and 3D. In 2D, for a right-handed rotation of angle  $\theta$  the rotation matrix is equal to:

$$R = \begin{bmatrix} cos(\theta) & -sin(\theta) \\ sin(\theta) & cos(\theta) \end{bmatrix}$$
 (8)

In 3D, for a right-handed rotation of angle  $\theta$  around axis  $\overrightarrow{u}$  the rotation is equal to (to shorten notation  $\theta$  is not written in the matrix below):

$$R = \begin{bmatrix} \cos + u_x^2 (1 - \cos) & u_x u_y (1 - \cos) - u_z \sin & u_x u_z (1 - \cos) + u_y \sin \\ u_x u_y (1 - \cos) + u_z \sin & \cos + u_y^2 (1 - \cos) & u_y u_z (1 - \cos) - u_x \sin \\ u_x u_z (1 - \cos) - u_y \sin & u_y u_z (1 - \cos) + u_x \sin & \cos + u_z^2 (1 - \cos) \end{bmatrix}$$
(9)

#### 1.2 Matrix

#### 1.2.1 Inverse matrix

The inverse of a matrix is only implemented for square matrices less than 3x3. It is computed directly, based on the determinant and the adjoint matrix.

For a 2x2 matrix M:

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} M_3 & -M_2 \\ -M_1 & M_0 \end{bmatrix}$$
 (10)

where

$$M = \begin{bmatrix} M_0 & M_2 \\ M_1 & M_3 \end{bmatrix} \tag{11}$$

and

$$det = M_0 M_3 - M_1 M_2 (12)$$

For a 3x3 matrix M:

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} (M_4 M_8 - M_5 M_7) & -(M_3 M_8 - M_5 M_6) & (M_3 M_7 - M_4 M_6) \\ -(M_1 M_8 - M_2 M_7) & (M_0 M_8 - M_2 M_6) & -(M_0 M_7 - M_1 M_6) \\ (M_1 M_5 - M_2 M_4) & -(M_0 M_5 - M_2 M_3) & (M_0 M_4 - M_1 M_3) \end{bmatrix}$$

$$(13)$$

where

$$M = \begin{bmatrix} M_0 & M_3 & M_6 \\ M_1 & M_4 & M_7 \\ M_2 & M_5 & M_8 \end{bmatrix}$$
 (14)

and

$$det = M_0(M_4M_8 - M_5M_7) - M_3(M_1M_8 - M_2M_7) + M_6(M_1M_5 - M_2M_4)$$
(15)

### 2 Interface

```
// ====== PBMATH.H =======
#ifndef PBMATH_H
#define PBMATH_H
// ========= Include =========
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <stdbool.h>
#include "pberr.h"
// ====== Define ========
#define PBMATH_EPSILON 0.00001
#define PBMATH_TWOPI 6.283185307
#define PBMATH_TWOPI_DIV_360 0.01745329252
#define PBMATH_PI 3.141592654
#define PBMATH_HALFPI 1.570796327
#define PBMATH_QUARTERPI 0.7853981634
#define PBMATH_SQRTTWO 1.414213562
{\tt \#define\ PBMATH\_SQRTONEHALF\ 0.707106781}
#ifndef MAX
 #define MAX(a,b) ((a)>(b)?(a):(b))
#endif
#ifndef MIN
 #define MIN(a,b) ((a)<(b)?(a):(b))
#define ISEQUALF(a,b) (fabs((a)-(b))<PBMATH_EPSILON)</pre>
#define SHORT(a) ((short)(round(a)))
#define INT(a) ((int)(round(a)))
#define rnd() (float)(rand())/(float)(RAND_MAX)
// ======== Polymorphism =========
#define VecClone(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatClone, \
 VecShort*: _VecShortClone, \
 default: PBErrInvalidPolymorphism)(Vec)
#define VecLoad(VecRef, Stream) _Generic(VecRef, \
  VecFloat**: _VecFloatLoad, \
 VecShort**: _VecShortLoad, \
 default: PBErrInvalidPolymorphism)(VecRef, Stream)
#define VecSave(Vec, Stream) _Generic(Vec, \
 VecFloat*: _VecFloatSave, \
 VecFloat2D*: _VecFloatSave, \
VecFloat3D*: _VecFloatSave, \
 VecShort*: _VecShortSave, \
 {\tt VecShort2D*: \_VecShortSave, \ } \\
 {\tt VecShort3D*: \_VecShortSave, \ } \\
  VecShort4D*: _VecShortSave, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
      VecFloat2D*: (VecFloat*)(Vec), \
     VecFloat3D*: (VecFloat*)(Vec), \
```

```
VecShort2D*: (VecShort*)(Vec), \
     VecShort3D*: (VecShort*)(Vec), \
     VecShort4D*: (VecShort*)(Vec), \
     default: Vec), \
   Stream)
#define VecFree(VecRef) _Generic(VecRef, \
 VecFloat**: _VecFloatFree, \
 VecShort**: _VecShortFree, \
 default: PBErrInvalidPolymorphism)(VecRef)
#define VecPrint(Vec, Stream) _Generic(Vec, \
 VecFloat*: _VecFloatPrintDef, \
 VecFloat2D*: _VecFloatPrintDef, \
 VecFloat3D*: _VecFloatPrintDef, \
 VecShort*: _VecShortPrint, \
 VecShort2D*: _VecShortPrint, \
 VecShort3D*: _VecShortPrint, \
 VecShort4D*: _VecShortPrint, \
 default: PBErrInvalidPolymorphism)( \
   _Generic(Vec, \
     VecFloat2D*: (VecFloat*)(Vec), \
     VecFloat3D*: (VecFloat*)(Vec), \
     VecShort2D*: (VecShort*)(Vec), \
     VecShort3D*: (VecShort*)(Vec), \
     VecShort4D*: (VecShort*)(Vec), \
     default: Vec), \
   Stream)
#define VecGet(Vec, Index) _Generic(Vec, \
 VecFloat*: _VecFloatGet, \
 VecFloat2D*: _VecFloatGet2D, \
 VecFloat3D*: _VecFloatGet3D, \
 VecShort*: _VecShortGet, \
 VecShort2D*: _VecShortGet2D, \
 {\tt VecShort3D*: \_VecShortGet3D, \ } \\
 VecShort4D*: _VecShortGet4D, \
 default: PBErrInvalidPolymorphism)(Vec, Index)
#define VecSet(Vec, Index, Val) _Generic(Vec, \
 VecFloat*: _VecFloatSet, \
 VecFloat2D*: _VecFloatSet2D, \
 VecFloat3D*: _VecFloatSet3D, \
 VecShort*: _VecShortSet, \
 VecShort2D*: _VecShortSet2D, \
 VecShort3D*: _VecShortSet3D, \
 VecShort4D*: _VecShortSet4D, \
 default: PBErrInvalidPolymorphism)(Vec, Index, Val)
#define VecSetNull(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatSetNull, \
 VecFloat2D*: _VecFloatSetNull, \
 VecFloat3D*: _VecFloatSetNull, \
 VecShort*: _VecShortSetNull, \
 VecShort2D*: _VecShortSetNull, \
 VecShort3D*: _VecShortSetNull, \
 VecShort4D*: _VecShortSetNull, \
 default: PBErrInvalidPolymorphism)( \
   _Generic(Vec, \
     VecFloat2D*: (VecFloat*)(Vec), \
     VecFloat3D*: (VecFloat*)(Vec), \
     VecShort2D*: (VecShort*)(Vec), \
```

```
VecShort3D*: (VecShort*)(Vec), \
      VecShort4D*: (VecShort*)(Vec), \
      default: Vec))
#define VecCopy(VecDest, VecSrc) _Generic(VecDest, \
  VecFloat*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat2D*: _VecFloatCopy, \
    VecFloat3D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecFloat2D*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat2D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecFloat3D*: _Generic(VecSrc, \
    VecFloat*: _VecFloatCopy, \
    VecFloat3D*: _VecFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort2D*: _VecShortCopy, \
   VecShort3D*: _VecShortCopy, \
VecShort4D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort2D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort2D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort3D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort3D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  VecShort4D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort4D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)( \
    _Generic(VecDest, \
      VecFloat2D*: (VecFloat*)(VecDest), \
      VecFloat3D*: (VecFloat*)(VecDest), \
      VecShort2D*: (VecShort*)(VecDest), \
      VecShort3D*: (VecShort*)(VecDest), \
      VecShort4D*: (VecShort*)(VecDest), \
     default: VecDest), \
    _Generic(VecSrc, \
      VecFloat2D*: (VecFloat*)(VecSrc), \
      VecFloat3D*: (VecFloat*)(VecSrc), \
      VecShort2D*: (VecShort*)(VecSrc), \
      VecShort3D*: (VecShort*)(VecSrc), \
      VecShort4D*: (VecShort*)(VecSrc), \
      default: VecSrc))
#define VecGetDim(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatGetDim, \
 {\tt VecFloat2D*: \_VecFloatGetDim, \ } \\
 VecFloat3D*: _VecFloatGetDim, \
  VecShort*: _VecShortGetDim, \
  VecShort2D*: _VecShortGetDim, \
  VecShort3D*: _VecShortGetDim, \
  VecShort4D*: _VecShortGetDim, \
  default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
```

```
VecFloat*: Vec, \
      VecFloat2D*: (VecFloat*)(Vec), \
      VecFloat3D*: (VecFloat*)(Vec), \
      VecShort*: Vec, \
      VecShort2D*: (VecShort*)(Vec), \
      VecShort3D*: (VecShort*)(Vec), \
      VecShort4D*: (VecShort*)(Vec), \
      default: Vec))
#define VecNorm(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatNorm, \
 VecFloat2D*: _VecFloatNorm2D, \
VecFloat3D*: _VecFloatNorm3D, \
 default: PBErrInvalidPolymorphism)(Vec)
#define VecNormalise(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatNormalise, \
 VecFloat2D*: _VecFloatNormalise2D, \
 VecFloat3D*: _VecFloatNormalise3D, \
 default: PBErrInvalidPolymorphism)(Vec)
#define VecDist(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatDist, \
    default: PBErrInvalidPolymorphism), \
  VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatDist2D, \
    default: PBErrInvalidPolymorphism), \
  VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatDist3D, \
    default: PBErrInvalidPolymorphism), \
  VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHamiltonDist,\
    default: PBErrInvalidPolymorphism), \
  VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErrInvalidPolymorphism), \
  VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErrInvalidPolymorphism), \
  VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecHamiltonDist(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatHamiltonDist, \
    default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatHamiltonDist2D, \
    default: PBErrInvalidPolymorphism), \
  VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatHamiltonDist3D, \
    default: PBErrInvalidPolymorphism), \
  VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHamiltonDist,\
    default: PBErrInvalidPolymorphism), \
  VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErrInvalidPolymorphism), \
  VecShort3D*: _Generic(VecB, \
```

```
VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecPixelDist(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatPixelDist, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatPixelDist2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatPixelDist3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortHamiltonDist,\
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortHamiltonDist2D,\
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortHamiltonDist3D,\
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortHamiltonDist4D,\
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (VecA, VecB)
#define VecIsEqual(VecA, VecB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatIsEqual, \
   VecFloat2D*: _VecFloatIsEqual, \
   VecFloat3D*: _VecFloatIsEqual, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat*: _VecFloatIsEqual, \
   VecFloat2D*: _VecFloatIsEqual, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat*: _VecFloatIsEqual,
   VecFloat3D*: _VecFloatIsEqual, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortIsEqual,\
   VecShort2D*: _VecShortIsEqual,\
   VecShort3D*: _VecShortIsEqual,\
   VecShort4D*: _VecShortIsEqual,\
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort*: _VecShortIsEqual,\
   VecShort1sEqual,\
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort*: _VecShortIsEqual,\
   VecShort3D*: _VecShortIsEqual,\
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort*: _VecShortIsEqual,\
   VecShort4D*: _VecShortIsEqual,\
```

```
default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)( \
   _Generic(VecA,
     VecFloat2D*: (VecFloat*)(VecA), \
     VecFloat3D*: (VecFloat*)(VecA), \
     VecShort2D*: (VecShort*)(VecA), \
     VecShort3D*: (VecShort*)(VecA), \
     VecShort4D*: (VecShort*)(VecA), \
     default: VecA), \
   _Generic(VecB, \
     VecFloat2D*: (VecFloat*)(VecB), \
     VecFloat3D*: (VecFloat*)(VecB), \
     VecShort2D*: (VecShort*)(VecB), \
     VecShort3D*: (VecShort*)(VecB), \
     VecShort4D*: (VecShort*)(VecB), \
     default: VecB))
#define VecOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
  VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatOp, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloat0p2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloat0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: _Generic(VecB, \
   VecShort*: _VecShortOp, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShort0p2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShort0p3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShort0p4D, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)(VecA, CoeffA, VecB, CoeffB)
#define VecGetOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
 VecFloat*: _Generic(VecB, \
   VecFloat*: _VecFloatGetOp, \
   default: PBErrInvalidPolymorphism), \
 VecFloat2D*: _Generic(VecB, \
   VecFloat2D*: _VecFloatGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 VecFloat3D*: _Generic(VecB, \
   VecFloat3D*: _VecFloatGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort*: Generic(VecB. \
   VecShort*: _VecShortGetOp, \
   default: PBErrInvalidPolymorphism), \
 VecShort2D*: _Generic(VecB, \
   VecShort2D*: _VecShortGetOp2D, \
   default: PBErrInvalidPolymorphism), \
 VecShort3D*: _Generic(VecB, \
   VecShort3D*: _VecShortGetOp3D, \
   default: PBErrInvalidPolymorphism), \
 VecShort4D*: _Generic(VecB, \
   VecShort4D*: _VecShortGetOp4D, \
```

```
default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)(VecA, CoeffA, VecB, CoeffB)
#define VecScale(Vec, Scale) _Generic(Vec, \
  VecFloat*: _VecFloatScale, \
  VecFloat2D*: _VecFloatScale2D, \
VecFloat3D*: _VecFloatScale3D, \
  default: PBErrInvalidPolymorphism)(Vec, Scale)
#define VecGetScale(Vec, Scale) _Generic(Vec, \
  VecFloat*: _VecFloatGetScale, \
  VecFloat2D*: _VecFloatGetScale2D, \
VecFloat3D*: _VecFloatGetScale3D, \
  default: PBErrInvalidPolymorphism)(Vec, Scale)
#define VecRot(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRot2D, \
  VecFloat2D*: _VecFloatRot2D, \
  default: PBErrInvalidPolymorphism)((VecFloat2D*)(Vec), Theta)
#define VecGetRot(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRot2D, \
  VecFloat2D*: _VecFloatGetRot2D, \
  default: PBErrInvalidPolymorphism)((VecFloat2D*)(Vec), Theta)
#define VecRotAxis(Vec, Axis, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRotAxis, \
  VecFloat3D*: _VecFloatRotAxis, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), \
    (VecFloat3D*)(Axis), Theta)
#define VecGetRotAxis(Vec, Axis, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRotAxis, \
  VecFloat3D*: _VecFloatGetRotAxis, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), \
    (VecFloat3D*)(Axis), Theta)
#define VecRotX(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRotX, \
  VecFloat3D*: _VecFloatRotX, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecGetRotX(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRotX, \
  VecFloat3D*: VecFloatGetRotX. \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecRotY(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRotY, \
  VecFloat3D*: _VecFloatRotY, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecGetRotY(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRotY, \
  VecFloat3D*: _VecFloatGetRotY, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecRotZ(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatRotZ, \
  VecFloat3D*: _VecFloatRotZ, \
  default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
```

```
#define VecGetRotZ(Vec, Theta) _Generic(Vec, \
  VecFloat*: _VecFloatGetRotZ, \
  VecFloat3D*: _VecFloatGetRotZ, \
 default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)
#define VecDotProd(VecA, VecB) _Generic(VecA, \
  VecShort*: _VecShortDotProd,\
  VecShort2D*: _VecShortDotProd2D,\
  VecShort3D*: _VecShortDotProd3D,\
 VecShort4D*: _VecShortDotProd4D,\
 VecFloat*: _VecFloatDotProd, \
 VecFloat2D*: _VecFloatDotProd2D, \
VecFloat3D*: _VecFloatDotProd3D, \
 default: PBErrInvalidPolymorphism) (VecA, VecB) \
#define VecAngleTo(VecFrom, VecTo) _Generic(VecFrom, \
 VecFloat*: _VecFloatAngleTo2D, \
 VecFloat2D*: _VecFloatAngleTo2D, \
  default: PBErrInvalidPolymorphism)((VecFloat2D*)(VecFrom), \
    (VecFloat2D*)(VecTo))
#define VecStep(Vec, VecBound) _Generic(Vec, \
 VecShort*: _VecShortStep, \
  VecShort2D*: _VecShortStep, \
 VecShort3D*: _VecShortStep, \
VecShort4D*: _VecShortStep, \
  default: PBErrInvalidPolymorphism)((VecShort*)(Vec), \
    (VecShort*)(VecBound))
#define VecPStep(Vec, VecBound) _Generic(Vec, \
  VecShort*: _VecShortPStep, \
  VecShort2D*: _VecShortPStep, \
  VecShort3D*: _VecShortPStep, \
  VecShort4D*: _VecShortPStep, \
  default: PBErrInvalidPolymorphism)((VecShort*)(Vec), \
    (VecShort*)(VecBound))
#define VecShiftStep(Vec, VecFrom, VecTo) _Generic(Vec, \
  VecShort*: _VecShortShiftStep, \
  VecShort2D*: _VecShortShiftStep, \
  VecShort3D*: _VecShortShiftStep, \
 VecShort4D*: _VecShortShiftStep, \
  default: PBErrInvalidPolymorphism)((VecShort*)(Vec), \
    (VecShort*)(VecFrom), (VecShort*)(VecTo))
#define VecGetMaxVal(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMaxVal, \
  VecFloat2D*: _VecFloatGetMaxVal, \
 VecFloat3D*: _VecFloatGetMaxVal, \
  VecShort*: _VecShortGetMaxVal, \
  VecShort2D*: _VecShortGetMaxVal, \
  VecShort3D*: _VecShortGetMaxVal, \
  VecShort4D*: _VecShortGetMaxVal, \
  default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (VecFloat*)(Vec), \
    VecFloat3D*: (VecFloat*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    default: Vec))
#define VecGetMinVal(Vec) _Generic(Vec, \
```

```
VecFloat*: _VecFloatGetMinVal, \
  VecFloat2D*: _VecFloatGetMinVal, \
  VecFloat3D*: _VecFloatGetMinVal, \
  VecShort*: _VecShortGetMinVal, \
  VecShort2D*: _VecShortGetMinVal, \
 VecShort3D*: _VecShortGetMinVal, \
VecShort4D*: _VecShortGetMinVal, \
  default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (VecFloat*)(Vec), \
    VecFloat3D*: (VecFloat*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    default: Vec))
#define VecGetMaxValAbs(Vec) _Generic(Vec, \
 VecFloat*: _VecFloatGetMaxValAbs, \
  VecFloat2D*: _VecFloatGetMaxValAbs, \
  VecFloat3D*: _VecFloatGetMaxValAbs, \
  VecShort*: _VecShortGetMaxValAbs, \
  VecShort2D*: _VecShortGetMaxValAbs, \
 VecShort3D*: _VecShortGetMaxValAbs, \
VecShort4D*: _VecShortGetMaxValAbs, \
  default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (VecFloat*)(Vec), \
    VecFloat3D*: (VecFloat*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    default: Vec))
#define VecGetMinValAbs(Vec) _Generic(Vec, \
  VecFloat*: _VecFloatGetMinValAbs, \
  VecFloat2D*: _VecFloatGetMinValAbs, \
  VecFloat3D*: _VecFloatGetMinValAbs, \
  VecShort*: _VecShortGetMinValAbs, \
  VecShort2D*: _VecShortGetMinValAbs, \
 VecShort3D*: _VecShortGetMinValAbs, \
VecShort4D*: _VecShortGetMinValAbs, \
  default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (VecFloat*)(Vec), \
    VecFloat3D*: (VecFloat*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    default: Vec))
#define VecStepDelta(Vec, VecBound, Delta) _Generic(Vec, \
 VecFloat*: _VecFloatStepDelta, \
  VecFloat2D*: _VecFloatStepDelta, \
  VecFloat3D*: _VecFloatStepDelta, \
  default: PBErrInvalidPolymorphism)((VecFloat*)(Vec), \
    (VecFloat*)(VecBound), (VecFloat*)(Delta))
#define VecShiftStepDelta(Vec, VecFrom, VecTo, Delta) _Generic(Vec, \
 VecFloat*: _VecFloatShiftStepDelta, \
  VecFloat2D*: _VecFloatShiftStepDelta, \
 {\tt VecFloat3D*: \_VecFloatShiftStepDelta, \ } \\
  default: PBErrInvalidPolymorphism)((VecFloat*)(Vec), \
    (VecFloat*)(VecFrom), (VecFloat*)(VecTo), (VecFloat*)(Delta))
#define MatClone(Mat) _Generic(Mat, \
```

```
MatFloat*: _MatFloatClone, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatLoad(MatRef, Stream) _Generic(MatRef, \
 MatFloat**: _MatFloatLoad, \
  default: PBErrInvalidPolymorphism) (MatRef, Stream)
#define MatSave(Mat, Stream) _Generic(Mat, \
 MatFloat*: _MatFloatSave, \
 default: PBErrInvalidPolymorphism)(Mat, Stream)
#define MatFree(MatRef) _Generic(MatRef, \
 MatFloat**: _MatFloatFree, \
 default: PBErrInvalidPolymorphism)(MatRef)
#define MatPrintln(Mat, Stream) _Generic(Mat, \
 MatFloat*: _MatFloatPrintlnDef, \
  default: PBErrInvalidPolymorphism)(Mat, Stream)
#define MatGet(Mat, VecIndex) _Generic(Mat, \
 MatFloat*: _MatFloatGet, \
 default: PBErrInvalidPolymorphism)(Mat, VecIndex)
#define MatSet(Mat, VecIndex, Val) _Generic(Mat, \
 MatFloat*: _MatFloatSet, \
  default: PBErrInvalidPolymorphism)(Mat, VecIndex, Val)
\verb|#define MatCopy(MatDest, MatSrc) _Generic(MatDest, \\ \\ \\ \\ \\
 MatFloat*: _Generic (MatSrc, \
   MatFloat*: _MatFloatCopy, \
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)(MatDest, MatSrc)
#define MatDim(Mat) _Generic(Mat, \
  MatFloat*: _MatFloatDim, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatGetDim(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatGetDim, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatInv(Mat) _Generic(Mat, \
 MatFloat*: _MatFloatInv, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatGetProdMat(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatGetProdMatFloat, \
    default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (MatA, MatB)
#define MatGetProdVec(Mat, Vec) _Generic(Mat, \
 MatFloat*: _Generic(Vec, \
    VecFloat*: _MatFloatGetProdVecFloat, \
    VecFloat2D*: _MatFloatGetProdVecFloat, \
    VecFloat3D*: _MatFloatGetProdVecFloat, \
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))
#define MatAdd(MatA, MatB) _Generic(MatA, \
 MatFloat*: _Generic(MatB, \
   MatFloat*: _MatFloatAdd, \
```

```
default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)(MatA, MatB)
#define MatGetAdd(MatA, MatB) _Generic(MatA, \
  MatFloat*: _Generic(MatB, \
    MatFloat*: _MatFloatGetAdd, \
    {\tt default:\ PBErrInvalidPolymorphism),\ } \setminus
  default: PBErrInvalidPolymorphism)(MatA, MatB)
#define MatSetIdentity(Mat) _Generic(Mat, \
  MatFloat*: _MatFloatSetIdentity, \
  default: PBErrInvalidPolymorphism)(Mat)
#define MatIsEqual(MatA, MatB) _Generic(MatA, \
  MatFloat*: _Generic(MatB, \
    MatFloat*: _MatFloatIsEqual, \
    default: PBErrInvalidPolymorphism), \
  default: PBErrInvalidPolymorphism)(MatA, MatB)
#define SysLinEqCreate(Mat, Vec) _Generic(Vec, \
  VecFloat*: _SLECreate, \
  VecFloat2D*: _SLECreate, \
VecFloat3D*: _SLECreate, \
  default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))
#define SysLinEqSetV(Sys, Vec) _Generic(Vec, \
  VecFloat*: _SLESetV, \
  VecFloat2D*: _SLESetV, \
VecFloat3D*: _SLESetV, \
  default: PBErrInvalidPolymorphism)(Sys, (VecFloat*)(Vec))
// ----- VecShort
// ====== Data structure =========
// Vector of short values
typedef struct VecShort {
  // Dimension
  int _dim;
  // Values
  short _val[0];
} VecShort;
typedef struct VecShort2D {
  // Dimension
  int _dim;
  // Values
  short _val[2];
} VecShort2D;
typedef struct VecShort3D {
  // Dimension
  int _dim;
  // Values
  short _val[3];
} VecShort3D;
typedef struct VecShort4D {
  // Dimension
  int _dim;
  // Values
  short _val[4];
```

```
} VecShort4D;
// ========= Functions declaration =========
// Create a new VecShort of dimension 'dim'
// Values are initalized to 0.0
VecShort* VecShortCreate(int dim);
// Static constructors for VecShort
#if BUILDMODE != 0
inline
#endif
VecShort2D VecShortCreateStatic2D();
#if BUILDMODE != 0
inline
#endif
VecShort3D VecShortCreateStatic3D();
#if BUILDMODE != 0
#endif
VecShort4D VecShortCreateStatic4D();
// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(VecShort* that);
// Load the VecShort from the stream
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* stream);
// Save the VecShort to the stream
// Return true in case of success, else false
bool _VecShortSave(VecShort* that, FILE* stream);
// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that);
// Print the VecShort on 'stream'
void _VecShortPrint(VecShort* that, FILE* stream);
// Return the i-th value of the VecShort
#if BUILDMODE != 0
inline
#endif
short _VecShortGet(VecShort* that, int i);
#if BUILDMODE != 0
inline
#endif
short _VecShortGet2D(VecShort2D* that, int i);
#if BUILDMODE != 0
inline
#endif
short _VecShortGet3D(VecShort3D* that, int i);
#if BUILDMODE != 0
inline
#endif
short _VecShortGet4D(VecShort4D* that, int i);
// Set the i-th value of the VecShort to v
#if BUILDMODE != 0
```

```
inline
#endif
void _VecShortSet(VecShort* that, int i, short v);
#if BUILDMODE != 0
inline
#endif
void _VecShortSet2D(VecShort2D* that, int i, short v);
#if BUILDMODE != 0
inline
#endif
void _VecShortSet3D(VecShort3D* that, int i, short v);
#if BUILDMODE != 0
inline
#endif
void _VecShortSet4D(VecShort4D* that, int i, short v);
// Return the dimension of the VecShort
// Return 0 if arguments are invalid
#if BUILDMODE != 0
inline
#endif
int _VecShortGetDim(VecShort* that);
// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist(VecShort* that, VecShort* tho);
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist2D(VecShort2D* that, VecShort2D* tho);
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist3D(VecShort3D* that, VecShort3D* tho);
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist4D(VecShort4D* that, VecShort4D* tho);
// Return true if the VecShort 'that' is equal to 'tho', else false
#if BUILDMODE != 0
inline
#endif
bool _VecShortIsEqual(VecShort* that, VecShort* tho);
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
inline
#endif
void _VecShortCopy(VecShort* that, VecShort* w);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd(VecShort* that, VecShort* tho);
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd2D(VecShort2D* that, VecShort2D* tho);
```

```
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd3D(VecShort3D* that, VecShort3D* tho);
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd4D(VecShort4D* that, VecShort4D* tho);
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
inline
#endif
void _VecShortSetNull(VecShort* that);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* that, VecShort* bound);
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''', values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* that, VecShort* bound);
// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* that, VecShort* from, VecShort* to);
// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
inline
#endif
void _VecShortOp(VecShort* that, short a, VecShort* tho, short b);
#if BUILDMODE != 0
inline
#endif
void _VecShortOp2D(VecShort2D* that, short a, VecShort2D* tho, short b);
#if BUILDMODE != 0
inline
#endif
void _VecShortOp3D(VecShort3D* that, short a, VecShort3D* tho, short b);
#if BUILDMODE != 0
inline
```

```
#endif
void _VecShortOp4D(VecShort4D* that, short a, VecShort4D* tho, short b);
// Return a VecShort equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
inline
#endif
VecShort* _VecShortGetOp(VecShort* that, short a,
  VecShort* tho, short b);
#if BUTLDMODE != 0
inline
#endif
VecShort2D _VecShortGetOp2D(VecShort2D* that, short a,
 VecShort2D* tho, short b);
#if BUILDMODE != 0
inline
#endif
VecShort3D* tho, short b);
#if BUILDMODE != 0
inline
#endif
VecShort4D _VecShortGetOp4D(VecShort4D* that, short a,
  VecShort4D* tho, short b);
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMaxVal(VecShort* that);
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMinVal(VecShort* that);
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMaxValAbs(VecShort* that);
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMinValAbs(VecShort* that);
// ----- VecFloat
// ========= Data structure ==========
// Vector of float values
typedef struct VecFloat {
 // Dimension
  int _dim;
```

```
// Values
  float _val[0];
} VecFloat;
typedef struct VecFloat2D {
  // Dimension
  int _dim;
  // Values
  float _val[2];
} VecFloat2D;
typedef struct VecFloat3D {
  // Dimension
  int _dim;
  // Values
  float _val[3];
} VecFloat3D;
// ======== Functions declaration ==========
// Create a new VecFloat of dimension 'dim'
// Values are initalized to 0.0
VecFloat* VecFloatCreate(int dim);
// Static constructors for VecFloat
#if BUILDMODE != 0
inline
#endif
VecFloat2D VecFloatCreateStatic2D();
#if BUILDMODE != 0
inline
#endif
VecFloat3D VecFloatCreateStatic3D();
// Clone the VecFloat
VecFloat* _VecFloatClone(VecFloat* that);
// Load the VecFloat from the stream
// If the VecFloat is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecFloatLoad(VecFloat** that, FILE* stream);
// Save the VecFloat to the stream
// Return true in case of success, else false
bool _VecFloatSave(VecFloat* that, FILE* stream);
// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that);
// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(VecFloat* that, FILE* stream, unsigned int prec);
inline void _VecFloatPrintDef(VecFloat* that, FILE* stream) {
 VecFloatPrint(that, stream, 3);
// Return the 'i'-th value of the VecFloat
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet(VecFloat* that, int i);
```

```
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet2D(VecFloat2D* that, int i);
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet3D(VecFloat3D* that, int i);
// Set the 'i'-th value of the VecFloat to 'v'
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet(VecFloat* that, int i, float v);
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet2D(VecFloat2D* that, int i, float v);
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet3D(VecFloat3D* that, int i, float v);
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
inline
#endif
void _VecFloatSetNull(VecFloat* that);
#if BUILDMODE != 0
inline
#endif
void _VecFloatSetNull2D(VecFloat2D* that);
#if BUILDMODE != 0
inline
#endif
void _VecFloatSetNull3D(VecFloat3D* that);
// Return the dimension of the VecFloat
// Return 0 if arguments are invalid
#if BUILDMODE != 0
inline
#endif
int _VecFloatGetDim(VecFloat* that);
// Copy the values of 'w' in 'that' (must have same dimensions)
// Do nothing if arguments are invalid
#if BUILDMODE != 0
inline
#endif
void _VecFloatCopy(VecFloat* that, VecFloat* w);
// Return the norm of the VecFloat
// Return 0.0 if arguments are invalid
#if BUILDMODE != 0
inline
#endif
float _VecFloatNorm(VecFloat* that);
#if BUILDMODE != 0
inline
#endif
float _VecFloatNorm2D(VecFloat2D* that);
#if BUILDMODE != 0
```

```
inline
#endif
float _VecFloatNorm3D(VecFloat3D* that);
// Normalise the VecFloat
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise(VecFloat* that);
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise2D(VecFloat2D* that);
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise3D(VecFloat3D* that);
// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist(VecFloat* that, VecFloat* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist2D(VecFloat2D* that, VecFloat2D* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist3D(VecFloat3D* that, VecFloat3D* tho);
// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist(VecFloat* that, VecFloat* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist2D(VecFloat2D* that, VecFloat2D* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist3D(VecFloat3D* that, VecFloat3D* tho);
// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatPixelDist(VecFloat* that, VecFloat* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatPixelDist2D(VecFloat2D* that, VecFloat2D* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatPixelDist3D(VecFloat3D* that, VecFloat3D* tho);
// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
```

```
inline
#endif
bool _VecFloatIsEqual(VecFloat* that, VecFloat* tho);
// Calculate (that * a) and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatScale(VecFloat* that, float a);
#if BUILDMODE != 0
inline
#endif
void _VecFloatScale2D(VecFloat2D* that, float a);
#if BUILDMODE != 0
inline
#endif
void _VecFloatScale3D(VecFloat3D* that, float a);
// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0
inline
#endif
VecFloat* _VecFloatGetScale(VecFloat* that, float a);
#if BUILDMODE != 0
inline
#endif
VecFloat2D _VecFloatGetScale2D(VecFloat2D* that, float a);
#if BUILDMODE != 0
inline
#endif
VecFloat3D _VecFloatGetScale3D(VecFloat3D* that, float a);
// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatOp(VecFloat* that, float a, VecFloat* tho, float b);
#if BUILDMODE != 0
inline
#endif
void _VecFloatOp2D(VecFloat2D* that, float a, VecFloat2D* tho, float b);
#if BUILDMODE != 0
inline
#endif
void _VecFloatOp3D(VecFloat3D* that, float a, VecFloat3D* tho, float b);
// Return a VecFloat equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
inline
#endif
VecFloat* _VecFloatGetOp(VecFloat* that, float a,
  VecFloat* tho, float b);
#if BUILDMODE != 0
inline
#endif
VecFloat2D _VecFloatGetOp2D(VecFloat2D* that, float a,
  VecFloat2D* tho, float b);
```

```
#if BUILDMODE != 0
inline
#endif
VecFloat3D _VecFloatGet0p3D(VecFloat3D* that, float a,
    VecFloat3D* tho, float b);
// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRot2D(VecFloat2D* that, float theta);
// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
inline
#endif
VecFloat2D _VecFloatGetRot2D(VecFloat2D* that, float theta);
// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotAxis(VecFloat3D* that, VecFloat3D* axis, float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
\label{thm:local_vecFloat} \begin{tabular}{ll} VecFloatGetRotAxis(VecFloat3D* that, VecFloat3D* axis, VecFloat3D* that, VecFloat3D* that
   float theta);
// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotX(VecFloat3D* that, float theta);
// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotY(VecFloat3D* that, float theta);
// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotZ(VecFloat3D* that, float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(VecFloat3D* that, float theta);
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(VecFloat3D* that, float theta);
```

```
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
VecFloat3D _VecFloatGetRotZ(VecFloat3D* that, float theta);
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd(VecFloat* that, VecFloat* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd2D(VecFloat2D* that, VecFloat2D* tho);
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd3D(VecFloat3D* that, VecFloat3D* tho);
// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
float _VecFloatAngleTo2D(VecFloat2D* that, VecFloat2D* tho);
// Return the conversion of VecFloat 'that' to a VecShort using round()
#if BUILDMODE != 0
inline
#endif
VecShort* VecFloatToShort(VecFloat* that);
#if BUILDMODE != 0
inline
#endif
VecShort2D VecFloatToShort2D(VecFloat2D* that);
#if BUILDMODE != 0
inline
#endif
VecShort3D VecFloatToShort3D(VecFloat3D* that);
// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
inline
#endif
VecFloat* VecShortToFloat(VecShort* that);
#if BUILDMODE != 0
inline
#endif
VecFloat2D VecShortToFloat2D(VecShort2D* that);
#if BUILDMODE != 0
inline
#endif
VecFloat3D VecShortToFloat3D(VecShort3D* that);
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMaxVal(VecFloat* that);
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
```

```
float _VecFloatGetMinVal(VecFloat* that);
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMaxValAbs(VecFloat* that);
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMinValAbs(VecFloat* that);
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper</pre>
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* that, VecFloat* bound,
  VecFloat* delta);
// Step the values of the vector incrementally by delta
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])
// 'that' must be initialised to 'from' before the first call of this
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* that, VecFloat* from,
  VecFloat* to, VecFloat* delta);
// ----- MatFloat
// ====== Data structure =========
// Vector of float values
typedef struct MatFloat {
  // Dimension
  VecShort2D _dim;
  // Values (memorized by columns)
  float _val[0];
} MatFloat;
// ====== Functions declaration =========
// Create a new MatFloat of dimension 'dim' (nbCol, nbLine)
// Values are initalized to 0.0
MatFloat* MatFloatCreate(VecShort2D* dim);
// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
inline
#endif
```

```
void _MatFloatSetIdentity(MatFloat* that);
// Clone the MatFloat
MatFloat* _MatFloatClone(MatFloat* that);
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
inline
#endif
void _MatFloatCopy(MatFloat* that, MatFloat* w);
// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream);
// Save the MatFloat to the stream
\ensuremath{//} Return true upon success, else false
bool _MatFloatSave(MatFloat* that, FILE* stream);
// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that);
// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* that, FILE* stream, unsigned int prec);
inline void _MatFloatPrintlnDef(MatFloat* that, FILE* stream) {
 MatFloatPrintln(that, stream, 3);
// Return the value at index (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
inline
#endif
float _MatFloatGet(MatFloat* that, VecShort2D* index);
// Set the value at index (col, line) of the MatFloat to 'v'
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
inline
#endif
void _MatFloatSet(MatFloat* that, VecShort2D* index, float v);
// Return the dimension of the MatFloat
#if BUILDMODE != 0
inline
#endif
VecShort2D* _MatFloatDim(MatFloat* that);
// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
inline
#endif
VecShort2D _MatFloatGetDim(MatFloat* that);
// Return the inverse matrix of 'that'
// The matrix must be a square matrix
MatFloat* _MatFloatInv(MatFloat* that);
// Return the product of matrix 'that' and vector 'v'
```

```
// Number of columns of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(MatFloat* that, VecFloat* v);
// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(MatFloat* that, MatFloat* tho);
// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
inline
#endif
MatFloat* _MatFloatGetAdd(MatFloat* that, MatFloat* tho);
// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
inline
#endif
void _MatFloatAdd(MatFloat* that, MatFloat* tho);
// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* that, MatFloat* tho);
// ---- Gauss
// ======== Define ========
// ========= Data structure =========
// Vector of float values
typedef struct Gauss {
  // Mean
  float _mean;
  // Sigma
 float _sigma;
} Gauss;
// ====== Functions declaration =========
// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(float mean, float sigma);
Gauss GaussCreateStatic(float mean, float sigma);
// Free the memory used by a Gauss
// Do nothing if arguments are invalid
void GaussFree(Gauss **that);
// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
inline
#endif
float GaussGet(Gauss *that, float x);
// Return a random value according to the Gauss 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
inline
#endif
float GaussRnd(Gauss *that);
```

```
// ----- Smoother
 // ======== Define ========
 // ====== Data structure =======
 // ========= Functions declaration ==========
 // Return the order 1 smooth value of 'x'
 // if x < 0.0 return 0.0
 // if x > 1.0 return 1.0
#if BUILDMODE != 0
 inline
#endif
float SmoothStep(float x);
 // Return the order 2 smooth value of 'x'
 // if x < 0.0 return 0.0
 // if x > 1.0 return 1.0
#if BUILDMODE != 0
inline
#endif
float SmootherStep(float x);
 // ----- Conversion functions
 // ======== Functions declaration ==========
 // Convert radians to degrees
inline float ConvRad2Deg(float rad) {
       return rad / PBMATH_TWOPI_DIV_360;
 // Convert degrees to radians
 inline float ConvDeg2Rad(float deg) {
return PBMATH_TWOPI_DIV_360 * deg;
// ----- SysLinEq
 // ========= Data structure ==========
// Linear system of equalities
typedef struct SysLinEq {
        // Matrix
       MatFloat* _M;
        // Inverse of the matrix % \left( 1\right) =\left( 1\right) \left( 1\right) 
       MatFloat* _Minv;
        // Vector
        VecFloat* _V;
 } SysLinEq;
 // ====== Functions declaration =========
// Create a new SysLinEq with matrix 'm' and vector 'v'
 // The dimension of 'v' must be equal to the number of column of 'm'
 // If 'v' is null the vector null is used instead
 // The matrix 'm' must be a square matrix
 // Return NULL if we couldn't create the SysLinEq
SysLinEq* _SLECreate(MatFloat* m, VecFloat* v);
// Free the memory used by the SysLinEq
```

```
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that);
// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(SysLinEq* that);
// Solve the SysLinEq _M.x = _V
// Return the solution vector, or null if there is no solution or the
// arguments are invalid
#if BUILDMODE != 0
inline
#endif
VecFloat* SysLinEqSolve(SysLinEq* that);
// Set the matrix of the SysLinEq to a clone of 'm'
\ensuremath{//} Do nothing if arguments are invalid
#if BUILDMODE != 0
inline
#endif
void SysLinEqSetM(SysLinEq* that, MatFloat* m);
// Set the vector of the SysLinEq to a clone of 'v'
\ensuremath{//} Do nothing if arguments are invalid
#if BUILDMODE != 0
inline
#endif
void _SLESetV(SysLinEq* that, VecFloat* v);
// ----- Usefull basic functions
// ======= Functions declaration =========
// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/
// does-pow-work-for-int-data-type-in-c
#if BUILDMODE != 0
inline
#endif
int powi(int base, int exp);
// Compute a^n, faster than std::pow for n<~100
inline float fastpow(float a, int n) {
  double ret = 1.0;
 for (; n--;) ret *= (double)a;
 return (float)ret;
// Compute a^2
inline float fsquare(float a) {
 return a * a;
}
// ========= Inliner ========
#if BUILDMODE != 0
#include "pbmath-inline.c"
#endif
```

#endif

#### 3 Code

### 3.1 pbmath.c

```
// ======= PBMATH.C ========
// ========= Include ========
#include "pbmath.h"
#if BUILDMODE == 0
#include "pbmath-inline.c"
#endif
// ----- VecShort
// ======= Functions implementation =========
// Create a new Vec of dimension 'dim'
// Values are initalized to 0.0
VecShort* VecShortCreate(int dim) {
#if BUILDMODE == 0
  if (dim <= 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "invalid 'dim' (%d)", dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Allocate memory
  VecShort* that = PBErrMalloc(PBMathErr,
    sizeof(VecShort) + sizeof(short) * dim);
  // Set the default values
  that->_dim = dim;
  for (int i = dim; i--;)
    that \rightarrow val[i] = 0;
  // Return the new VecShort
 return that;
// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 7
#endif
  // Create a clone
  VecShort* clone = VecShortCreate(that->_dim);
  // Copy the values
  memcpy(clone, that, sizeof(VecShort) + sizeof(short) * that->_dim);
  // Return the clone
 return clone;
// Load the VecShort from the stream \,
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* stream) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
 \ensuremath{//} If 'that' is already allocated
 if (*that != NULL)
   // Free memory
    _VecShortFree(that);
  ^{-} Read the number of dimension
 int dim;
 int ret = fscanf(stream, "%d", &dim);
  // If we coudln't fscanf
 if (ret == EOF)
   return false;
  // Check the dimension
 if (dim <= 0)
   return false;
  // Allocate memory
 *that = VecShortCreate(dim);
  // Read the values
 for (int i = 0; i < dim; ++i) {
   ret = fscanf(stream, "%hi", (*that)->_val + i);
   // If we coudln't fscanf
   if (ret == EOF)
     return false;
 // Return success code
 return true;
// Save the VecShort to the stream
// Return true in case of success, else false
bool _VecShortSave(VecShort* that, FILE* stream) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (stream == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
 // Save the dimension
 int ret = fprintf(stream, "%d ", that->_dim);
 // If we coudln't fprintf
 if (ret < 0)
   return false;
  // Save the values
 for (int i = 0; i < that->_dim; ++i) {
   ret = fprintf(stream, "%hi ", that->_val[i]);
    // If we coudln't fprintf
   if (ret < 0)
```

```
return false;
  }
  fprintf(stream, "\n");
  // If we coudln't fprintf
  if (ret < 0)
    return false;
  // Return success code
  return true;
// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that) {
  // Check argument
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  free(*that);
  *that = NULL;
// Print the VecShort on 'stream' with 'prec' digit precision
void _VecShortPrint(VecShort* that, FILE* stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Print the values
  fprintf(stream, "<");</pre>
  for (int i = 0; i < that->_dim; ++i) {
    fprintf(stream, "%hi", that->_val[i]);
    if (i < that->_dim - 1)
      fprintf(stream, ",");
 fprintf(stream, ">");
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* that, VecShort* bound) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (bound == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
```

```
PBErrCatch(PBMathErr);
 }
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
 bool ret = true;
 // Declare a variable to memorise the dimension currently increasing
 int iDim = that->_dim - 1;
  // Declare a flag for the loop condition
 bool flag = true;
  // Increment
 do {
   ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
      --iDim:
   } else {
     flag = false;
 } while (iDim >= 0 && flag == true);
  if (iDim == -1)
   ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* that, VecShort* bound) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
     that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 int iDim = 0;
 // Declare a flag for the loop condition
```

```
bool flag = true;
  // Increment
  do {
   ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
     that->_val[iDim] = 0;
     ++iDim:
   } else {
     flag = false;
 } while (iDim < that->_dim && flag == true);
  if (iDim == that->_dim)
   ret = false;
 // Return the flag
 return ret;
// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])</pre>
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* that, VecShort* from, VecShort* to) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (from == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'from' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != from->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg, "'from' dimensions don't match (\%d==\%d)",}
     that->_dim, from->_dim);
   PBErrCatch(PBMathErr);
 if (to == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'to' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != to->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'to' dimensions don't match (%d==%d)",
     that->_dim, to->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 int iDim = that->_dim - 1;
 // Declare a flag for the loop condition
```

```
bool flag = true;
  // Increment
  do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= to->_val[iDim]) {
     that->_val[iDim] = from->_val[iDim];
     --iDim;
    } else {
     flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
  return ret;
// ----- VecFloat
// ====== Functions implementation =========
// Create a new Vec of dimension 'dim'
// Values are initalized to 0.0
VecFloat* VecFloatCreate(int dim) {
#if BUILDMODE == 0
  if (dim <= 0) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "invalid 'dim' (%d)", dim);
    PBErrCatch(PBMathErr);
#endif
  // Allocate memory
  VecFloat* that = PBErrMalloc(PBMathErr,
    sizeof(VecFloat) + sizeof(float) * dim);
  // Set the default values
  that->_dim = dim;
  for (int i = dim; i--;)
    that->_val[i] = 0.0;
  // Return the new VecFloat
 return that;
// Clone the VecFloat
VecFloat* _VecFloatClone(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Create a clone
  VecFloat* clone = VecFloatCreate(that->_dim);
  // Clone the properties
 memcpy(clone, that, sizeof(VecFloat) + sizeof(float) * that->_dim);
  // Return the clone
 return clone;
}
// Load the VecFloat from the stream
// If the VecFloat is already allocated, it is freed before loading
bool _VecFloatLoad(VecFloat** that, FILE* stream) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // If 'that' is already allocated
  if (*that != NULL) {
   // Free memory
    _VecFloatFree(that);
  // Read the number of dimension
  int ret = fscanf(stream, "%d", &dim);
  // If we coudln't fscanf
  if (ret == EOF)
   return false;
  // Check the dimension
  if (dim <= 0)
    return false;
  // Allocate memory
  *that = VecFloatCreate(dim);
  // Read the values
  for (int i = 0; i < dim; ++i) {
    ret = fscanf(stream, "%f", (*that)->_val + i);
    // If we coudln't fscanf
    if (ret == EOF)
      return false;
  // Return success code
  return true;
// Save the VecFloat to the stream
// Return true in case of success, else false
bool _VecFloatSave(VecFloat* that, FILE* stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Save the dimension
  int ret = fprintf(stream, "%d ", that->_dim);
  // If we coudln't fprintf
  if (ret < 0)
   return false;
  // Save the values
  for (int i = 0; i < that->_dim; ++i) {
    ret = fprintf(stream, "%f ", that->_val[i]);
```

```
// If we coudln't fprintf
    if (ret < 0)
      return false;
  fprintf(stream, "\n");
  // If we coudln't fprintf
  if (ret < 0)
    return false;
  // Return success code
  return true;
// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that) {
  // Check argument
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  free(*that):
  *that = NULL;
// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(VecFloat* that, FILE* stream, unsigned int prec) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the format string
  char format[100] = {'\0'};
  sprintf(format, "%%.%df", prec);
  // Print the values
  fprintf(stream, "<");</pre>
  for (int i = 0; i < that->_dim; ++i) {
    fprintf(stream, format, that->_val[i]);
    if (i < that->_dim - 1)
      fprintf(stream, ",");
 fprintf(stream, ">");
// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
{\tt float \_VecFloatAngleTo2D(VecFloat2D*\ that,\ VecFloat2D*\ tho)\ \{}
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(that), 1.0)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'that' is not a normed vector");
    PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(tho), 1.0)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'tho' is not a normed vector");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float theta = 0.0;
  // Calculate the angle
  VecFloat2D m = VecFloatCreateStatic2D();
  if (fabs(VecGet(that, 0)) > fabs(VecGet(that, 1))) {
    VecSet(&m, 0,
      (VecGet(tho, 0) + VecGet(tho, 1) * VecGet(that, 1) /
      VecGet(that, 0)) /
      (VecGet(that, 0) + fsquare(VecGet(that, 1)) / VecGet(that, 0)));
    VecSet(&m, 1,
      (VecGet(&m, 0) * VecGet(that, 1) - VecGet(tho, 1)) /
      VecGet(that, 0));
  } else {
    VecSet(&m, 1,
      (VecGet(tho, 0) - VecGet(tho, 1) * VecGet(that, 0) /
      VecGet(that, 1)) /
      (VecGet(that, 1) + fsquare(VecGet(that, 0)) / VecGet(that, 1)));
    VecSet(&m, 0,
      ({\tt VecGet(tho, 1) + VecGet(\&m, 1) * VecGet(that, 0))} \ / \\
      VecGet(that, 1));
  // Due to numerical imprecision m[0] may be slightly out of [-1,1]
  // which makes acos return NaN, prevent this
  if (VecGet(\&m, 0) < -1.0)
    theta = PBMATH_PI;
  else if (VecGet(\&m, 0) > 1.0)
    theta = 0.0;
    theta = acos(VecGet(&m, 0));
  if (\sin(\text{theta}) * \text{VecGet}(\&m, 1) > 0.0)
    theta *= -1.0;
  // Return the result
  return theta;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
VecFloat3D _VecFloatGetRotAxis(VecFloat3D* that, VecFloat3D* axis,
  float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (axis == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
   sprintf(PBMathErr->_msg, "'axis' is null");
   PBErrCatch(PBMathErr);
 if (VecGetDim(that) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
   sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
     VecGetDim(that));
   PBErrCatch(PBMathErr);
 if (VecGetDim(axis) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
   sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%d=3)",
     VecGetDim(axis));
   PBErrCatch(PBMathErr);
 if (ISEQUALF(VecNorm(axis), 1.0) == false) {
   PBMathErr->_type = PBErrTypeInvalidArg;
   sprintf(PBMathErr->_msg, "'axis' is not normalized");
   PBErrCatch(PBMathErr);
#endif
 \//\ {\mbox{Declare variable for optimisation}}
 float cosTheta = cos(theta);
 float sinTheta = sin(theta);
 // Create the rotation matrix
 VecShort2D d = VecShortCreateStatic2D();
 VecSet(&d, 0, 3); VecSet(&d, 1, 3);
 MatFloat* rot = MatFloatCreate(&d);
 VecSet(&d, 0, 0); VecSet(&d, 1, 0);
 float v = cosTheta + fastpow(VecGet(axis, 0), 2) * (1.0 - cosTheta);
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 0);
 v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) -
   VecGet(axis, 2) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 0);
 v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) +
   VecGet(axis, 1) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 1);
 v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) +
   VecGet(axis, 2) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 1);
 v = cosTheta + fastpow(VecGet(axis, 1), 2) * (1.0 - cosTheta);
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 1);
 v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) -
   VecGet(axis, 0) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 0); VecSet(&d, 1, 2);
 v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) -
   VecGet(axis, 1) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 1); VecSet(&d, 1, 2);
 v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) +
   VecGet(axis, 0) * sinTheta;
 MatSet(rot, &d, v);
 VecSet(&d, 0, 2); VecSet(&d, 1, 2);
 v = cosTheta + fastpow(VecGet(axis, 2), 2) * (1.0 - cosTheta);
```

```
MatSet(rot, &d, v);
  // Calculate the result vector
  VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = *(VecFloat3D*)w;
  // Free memory
  VecFree(&w);
 MatFree(&rot):
  // Return the result
 return res;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
   PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare variable for optimisation
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  \ensuremath{//} Create the rotation matrix
  VecShort2D d = VecShortCreateStatic2D();
  VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = 1.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 1);
  v = 0.0:
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 1);
  v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = -sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 2);
  v = sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 2);
  v = cosTheta;
  MatSet(rot, &d, v);
  // Calculate the result vector
```

```
VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = *(VecFloat3D*)w;
  // Free memory
  VecFree(&w);
  MatFree(&rot);
  // Return the result
 return res;
}
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Declare variable for optimisation
  float cosTheta = cos(theta);
  float sinTheta = sin(theta):
  // Create the rotation matrix
  VecShort2D d = VecShortCreateStatic2D();
  VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 0);
  v = sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 1);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 1);
  v = 1.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 2);
  v = -sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 2);
  v = cosTheta;
  MatSet(rot, &d, v);
  // Calculate the result vector
  VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = *(VecFloat3D*)w;
```

```
// Free memory
  VecFree(&w);
  MatFree(&rot);
  // Return the result
 return res;
// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Z
VecFloat3D _VecFloatGetRotZ(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
     VecGetDim(that)):
   PBErrCatch(PBMathErr);
#endif
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  // Create the rotation matrix
  VecShort2D d = VecShortCreateStatic2D();
  VecSet(&d, 0, 3); VecSet(&d, 1, 3);
  MatFloat* rot = MatFloatCreate(&d);
  VecSet(&d, 0, 0); VecSet(&d, 1, 0);
  float v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 0);
  v = -sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 0);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 1);
  v = sinTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 1);
  v = cosTheta;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 1);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 0); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 1); VecSet(&d, 1, 2);
  v = 0.0;
  MatSet(rot, &d, v);
  VecSet(&d, 0, 2); VecSet(&d, 1, 2);
  v = 1.0;
  MatSet(rot, &d, v);
  // Calculate the result vector
  VecFloat* w = MatGetProdVec(rot, that);
  VecFloat3D res = *(VecFloat3D*)w;
  // Free memory
  VecFree(&w);
```

```
MatFree(&rot);
  // Return the result
 return res;
// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* that, VecFloat* bound,
 VecFloat* delta) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (bound == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'bound' is null");
   PBErrCatch(PBMathErr);
 if (delta == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != bound->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'bound' 's dimensions don't match (d=d)",
      that->_dim, bound->_dim);
   PBErrCatch(PBMathErr);
  if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'delta' 's dimensions don't match (%d==%d)",
      that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
#endif
 // Declare a variable for the returned flag
 bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 int iDim = that->_dim - 1;
  // Declare a flag for the loop condition
  bool flag = true;
 // Increment
 do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > bound->_val[iDim] + PBMATH_EPSILON) {
     that->_val[iDim] = 0;
      --iDim;
   } else {
     flag = false;
 } while (iDim >= 0 && flag == true);
  if (iDim == -1)
```

```
ret = false;
  // Return the flag
 return ret;
// Step the values of the vector incrementally by delta
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])
// 'that' must be initialised to 'from' before the first call of this
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* that, VecFloat* from,
 VecFloat* to, VecFloat* delta) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
  if (from == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'from' is null");
   PBErrCatch(PBMathErr);
 if (that->_dim != from->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'from' dimensions don't match (%d==%d)",
     that->_dim, from->_dim);
   PBErrCatch(PBMathErr);
  if (to == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'to' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != to->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'to' dimensions don't match (%d==%d)",
     that->_dim, to->_dim);
   PBErrCatch(PBMathErr);
  if (delta == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'delta' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != delta->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'delta' dimensions don't match (%d==%d)",
      that->_dim, delta->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
 int iDim = that->_dim - 1;
 // Declare a flag for the loop condition
```

```
bool flag = true;
  // Increment
  do {
   that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > to->_val[iDim] + PBMATH_EPSILON) {
     that->_val[iDim] = from->_val[iDim];
     --iDim:
   } else {
     flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
   ret = false;
  // Return the flag
 return ret;
// ----- MatFloat
// ====== Define ========
// ====== Functions implementation =========
// Create a new MatFloat of dimension 'dim' (nbcol, nbline)
// Values are initalized to 0.0
MatFloat* MatFloatCreate(VecShort2D* dim) {
#if BUILDMODE == 0
  if (dim == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'dim' is null");
   PBErrCatch(PBMathErr);
#endif
  // Allocate memory
  int d = VecGet(dim, 0) * VecGet(dim, 1);
  MatFloat* that = PBErrMalloc(PBMathErr, sizeof(MatFloat) +
   sizeof(float) * d);
  // Set the dimension
  that->_dim = *dim;
  // Set the default values
  for (int i = d; i--;)
   that->_val[i] = 0.0;
  // Return the new MatFloat
 return that;
// Clone the MatFloat
MatFloat* _MatFloatClone(MatFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create a clone
  MatFloat* clone = MatFloatCreate(&(that->_dim));
  // Copy the values
  int d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
  for (int i = d; i--;)
   clone->_val[i] = that->_val[i];
  // Return the clone
```

```
return clone;
}
// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // If 'that' is already allocated
  if (*that != NULL)
    // Free memory
    _MatFloatFree(that);
  // Read the number of dimension
  VecShort2D dim = VecShortCreateStatic2D();
  int ret = fscanf(stream, "%hi %hi", dim._val , dim._val + 1);
  // If we coudln't fscanf
  if (ret == EOF)
    return false;
  if (VecGet(&dim, 0) <= 0 || VecGet(&dim, 1) <= 0)
    return false;
  // Allocate memory
  *that = MatFloatCreate(&dim);
  // Read the values
  VecShort2D index = VecShortCreateStatic2D();
  do {
    float v;
    ret = fscanf(stream, "%f", &v);
    // If we coudln't fscanf
    if (ret == EOF)
     return false;
    MatSet(*that, &index, v);
  } while (VecPStep(&index, &dim));
  // Return success code
 return true;
}
// Save the MatFloat to the stream
// Return true upon success, else false
bool _MatFloatSave(MatFloat* that, FILE* stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
    PBErrCatch(PBMathErr);
 }
#endif
```

```
// Save the dimension
  int ret = fprintf(stream, "%hi %hi\n",
    VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
  if (ret < 0)
    return false;
  // Save the values
  VecShort2D index = VecShortCreateStatic2D();
    ret = fprintf(stream, "%f ", MatGet(that, &index));
    // If we coudln't fprintf
    if (ret < 0)
      return false;
    if (VecGet(\&index, 0) == VecGet(\&(that->_dim), 0) - 1) {
      ret = fprintf(stream, "\n");
      // If we coudln't fprintf
      if (ret < 0)
       return false;
    }
  } while (VecPStep(&index, &(that->_dim)));
  // Return success code
 return true;
// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that) {
  // Check argument
  if (that == NULL || *that == NULL)
    return;
  // Free memory
  free(*that);
  *that = NULL;
// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* that, FILE* stream, unsigned int prec) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (stream == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'stream' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the format string
  char format[100] = {'\0'};
  sprintf(format, "%%.%df", prec);
  // Print the values
  fprintf(stream, "[");
  VecShort2D index = VecShortCreateStatic2D();
    if (VecGet(&index, 1) != 0 || VecGet(&index, 0) != 0)
  fprintf(stream, " ");
    fprintf(stream, format, MatGet(that, &index));
    if (VecGet(&index, 0) < VecGet(&(that->_dim), 0) - 1)
      fprintf(stream, ",");
    if (VecGet(\&index, 0) == VecGet(\&(that->_dim), 0) - 1) {
```

```
if (VecGet(&index, 1) == VecGet(&(that->_dim), 1) - 1)
        fprintf(stream, "]");
      fprintf(stream, "\n");
 } while (VecPStep(&index, &(that->_dim)));
// Return the inverse matrix of 'that'
// The matrix must be a square matrix
MatFloat* _MatFloatInv(MatFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGet(&(that->_dim), 0) != VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "the matrix is not square (%dx%d)",
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  if (VecGet(\&(that->_dim), 0) > 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "_MatFloatInv is defined only for matrix of dim <= 3x3 (%dx%d)",
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
   PBErrCatch(PBMathErr);
 1
#endif
  // Allocate memory for the result
  MatFloat* res = MatFloatCreate(&(that->_dim));
  // If the matrix is of dimension 1x1
  if (VecGet(&(that->_dim), 0) == 1) {
#if BUILDMODE == 0
    if (that->_val[0] < PBMATH_EPSILON) {</pre>
      PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "the matrix is not inversible");
      PBErrCatch(PBMathErr);
   }
#endif
    res->_val[0] = 1.0 / that->_val[0];
  // If the matrix is of dimension 2x2
  } else if (VecGet(&(that->_dim), 0) == 2) {
    float det = that->_val[0] * that->_val[3] -
      that->_val[2] * that->_val[1];
#if BUILDMODE == 0
    if (ISEQUALF(det, 0.0)) {
      PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "the matrix is not inversible");
      PBErrCatch(PBMathErr);
#endif
    res->_val[0] = that->_val[3] / det;
    res->_val[1] = -1.0 * that->_val[1] / det;
    res->_val[2] = -1.0 * that->_val[2] / det;
    res->_val[3] = that->_val[0] / det;
  // Else, the matrix dimension is 3x3
  } else if (VecGet(\&(that->_dim), 0) == 3) {
    float det =
      that->_val[0] *
        (that->_val[4] * that->_val[8] -
```

```
that->_val[5] * that->_val[7]) -
      that->_val[3] *
        (that->_val[1] * that->_val[8] -
        that->_val[2] * that->_val[7]) +
      that->_val[6] *
        (that->_val[1] * that->_val[5] -
        that->_val[2] * that->_val[4]);
#if BUILDMODE == 0
    if (ISEQUALF(det, 0.0)) {
     PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "the matrix is not inversible");
     PBErrCatch(PBMathErr);
#endif
   res->_val[0] = (that->_val[4] * that->_val[8] -
       that->_val[5] * that->_val[7]) / det;
    res->_val[1] = -(that->_val[1] * that->_val[8] -
       that->_val[2] * that->_val[7]) / det;
    res->_val[2] = (that->_val[1] * that->_val[5] -
       that->_val[2] * that->_val[4]) / det;
    res->_val[3] = -(that->_val[3] * that->_val[8] -
       that->_val[5] * that->_val[6]) / det;
    res->_val[4] = (that->_val[0] * that->_val[8] -
        that->_val[2] * that->_val[6]) / det;
    res->_val[5] = -(that->_val[0] * that->_val[5] -
        that->_val[2] * that->_val[3]) / det;
    res->_val[6] = (that->_val[3] * that->_val[7] -
       that->_val[4] * that->_val[6]) / det;
    res->_val[7] = -(that->_val[0] * that->_val[7] -
       that->_val[1] * that->_val[6]) / det;
    res->_val[8] = (that->_val[0] * that->_val[4] -
        that->_val[1] * that->_val[3]) / det;
  // Return the result
 return res;
// Return the product of matrix 'that' and vector 'v'
// Number of colum of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(MatFloat* that, VecFloat* v) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (v == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'v' is null");
   PBErrCatch(PBMathErr);
 if (VecGet(&(that->_dim), 0) != VecGetDim(v)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "the matrix and vector have incompatible dimensions (d=-d)",
     VecGet(&(that->_dim), 0), VecGetDim(v));
   PBErrCatch(PBMathErr);
 7
#endif
  // Declare a variable to memorize the index in the matrix
 VecShort2D i = VecShortCreateStatic2D();
 // Allocate memory for the solution
```

```
VecFloat* ret = VecFloatCreate(VecGet(&(that->_dim), 1));
  // If we could allocate memory
  if (ret != NULL)
   for (VecSet(&i, 0, 0); VecGet(&i, 0) < VecGet(&(that->_dim), 0);
      VecSet(&i, 0, VecGet(&i, 0) + 1))
      for (VecSet(\&i, 1, 0); VecGet(\&i, 1) < VecGet(\&(that->_dim), 1);
        VecSet(&i, 1, VecGet(&i, 1) + 1))
        VecSet(ret, VecGet(&i, 1), VecGet(ret,
          VecGet(&i, 1)) + VecGet(v, VecGet(&i, 0)) * MatGet(that, &i));
  // Return the result
 return ret;
// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(MatFloat* that, MatFloat* tho) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 if (VecGet(\&(that->_dim), 0) != VecGet(\&(tho->_dim), 1)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "the matrices have incompatible dimensions (d=d=d)",
     VecGet(\&(that->_dim), 0), VecGet(\&(tho->_dim), 1));
   PBErrCatch(PBMathErr);
 7
#endif
 \ensuremath{//} Declare 3 variables to memorize the index in the matrix
 VecShort2D i = VecShortCreateStatic2D();
  VecShort2D j = VecShortCreateStatic2D();
 VecShort2D k = VecShortCreateStatic2D();
  // Allocate memory for the solution
  VecSet(&i, 0, VecGet(&(tho->_dim), 0));
 VecSet(&i, 1, VecGet(&(that->_dim), 1));
  MatFloat* ret = MatFloatCreate(&i);
  for (VecSet(&i, 0, 0); VecGet(&i, 0) < VecGet(&(tho->_dim), 0);
    VecSet(&i, 0, VecGet(&i, 0) + 1))
    for (VecSet(&i, 1, 0); VecGet(&i, 1) < VecGet(&(that->_dim), 1);
      VecSet(&i, 1, VecGet(&i, 1) + 1))
      for (VecSet(&j, 0, 0), VecSet(&j, 1, VecGet(&i, 1)),
        VecSet(&k, 0, VecGet(&i, 0)), VecSet(&k, 1, 0);
        VecGet(&j, 0) < VecGet(&(that->_dim), 0);
        VecSet(\&j, 0, VecGet(\&j, 0) + 1),
        VecSet(&k, 1, VecGet(&k, 1) + 1)) {
        MatSet(ret, &i, MatGet(ret, &i) +
          MatGet(that, &j) * MatGet(tho, &k));
  // Return the result
 return ret;
// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* that, MatFloat* tho) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  7
#endif
  if (!VecIsEqual(&(that->_dim), &(tho->_dim)))
   return false;
  VecShort2D v = VecShortCreateStatic2D();
  do {
   if (!ISEQUALF(MatGet(that, &v), MatGet(tho, &v)))
     return false;
  } while (VecStep(&v, &(that->_dim)));
 return true;
// ----- Gauss
// ======== Define ========
// ====== Functions implementation =========
// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(float mean, float sigma) {
  // Allocate memory
  Gauss *that = PBErrMalloc(PBMathErr, sizeof(Gauss));
  // Set properties
  that->_mean = mean;
  that->_sigma = sigma;
  // Return the new Gauss
 return that;
Gauss GaussCreateStatic(float mean, float sigma) {
  // Allocate memory
  Gauss that = {._mean = mean, ._sigma = sigma};
  // Return the new Gauss
 return that;
// Free the memory used by a Gauss
// Do nothing if arguments are invalid
void GaussFree(Gauss **that) {
 // Check argument
  if (that == NULL || *that == NULL)
   return;
  // Free memory
  free(*that);
  *that = NULL;
// ----- SysLinEq
// ======= Functions implementation ==========
// Create a new SysLinEq with matrix 'm' and vector 'v'
// The dimension of 'v' must be equal to the number of column of 'm'
```

```
// If 'v' is null the vector null is used instead
// The matrix 'm' must be a square matrix
// Return NULL if we couldn't create the SysLinEq
SysLinEq* _SLECreate(MatFloat* m, VecFloat* v) {
#if BUILDMODE == 0
 if (m == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'m' is null");
   PBErrCatch(PBMathErr);
 if (VecGet(\&(m->_dim), 0) != VecGet(\&(m->_dim), 1)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "the matrix is not square (%dx%d)",
      VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1));
   PBErrCatch(PBMathErr);
 if (v != NULL) {
    if (VecGet(\&(m->_dim), 0) != VecGetDim(v)) {
     PBMathErr->_type = PBErrTypeInvalidArg;
      sprintf(PBMathErr->_msg,
        "the matrix and vector have incompatible dimensions (%d==%d)",
        VecGet(&(m->_dim), 0), VecGetDim(v));
     PBErrCatch(PBMathErr);
 }
#endif
  // Allocate memory
 SysLinEq* that = PBErrMalloc(PBMathErr, sizeof(SysLinEq));
 that->_M = MatClone(m);
  that->_Minv = MatInv(that->_M);
 if (v != NULL)
    that->_V = VecClone(v);
    that->_V = VecFloatCreate(VecGet(&(m->_dim), 0));
  if (that->_M == NULL || that->_V == NULL || that->_Minv == NULL) {
#if BUILDMODE == 0
    if (that->_M == NULL) {
     PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't create the matrix");
     PBErrCatch(PBMathErr);
    if (that->_Minv == NULL) {
     PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
     PBErrCatch(PBMathErr);
    if (that->_V == NULL) {
     PBMathErr->_type = PBErrTypeOther;
      sprintf(PBMathErr->_msg, "couldn't create the vector");
     PBErrCatch(PBMathErr);
#endif
   SysLinEqFree(&that);
 // Return the new SysLinEq
 return that;
// Free the memory used by the SysLinEq
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that) {
 // Check arguments
```

```
if (that == NULL || *that == NULL)
    return;
  // Free memory
  MatFree(&((*that)->_M));
  MatFree(&((*that)->_Minv));
  VecFree(&((*that)->_V));
  free(*that);
  *that = NULL;
// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(SysLinEq* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable for the result
  SysLinEq* ret = PBErrMalloc(PBMathErr, sizeof(SysLinEq));
  ret->_M = MatClone(that->_M);
  ret->_Minv = MatClone(that->_Minv);
  ret->_V = VecClone(that->_V);
  if (ret->_M == NULL \mid \mid ret->_V == NULL \mid \mid ret->_Minv == NULL)
    SysLinEqFree(&ret);
  // Return the new SysLinEq
  return ret;
```

## 3.2 pbmath-inline.c

```
// ======= PBMATH_INLINE.C ========
// ======= Functions implementation ==========
// Static constructors for VecShort
#if BUILDMODE != 0
inline
#endif
VecShort2D VecShortCreateStatic2D() {
  VecShort2D v = \{.\_val = \{0, 0\}, .\_dim = 2\};
}
#if BUILDMODE != 0
inline
#endif
VecShort3D VecShortCreateStatic3D() {
  VecShort3D v = \{.\_val = \{0, 0, 0\}, .\_dim = 3\};
 return v;
#if BUILDMODE != 0
inline
#endif
VecShort4D VecShortCreateStatic4D() {
```

```
VecShort4D v = \{.\_val = \{0, 0, 0, 0\}, .\_dim = 4\};
// Return the i-th value of the VecShort
#if BUILDMODE != 0
inline
#endif
short _VecShortGet(VecShort* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    \label{eq:sprintf} $$\operatorname{PBMathErr->_msg, "'i' is invalid (0<=\%d<\%d)", i, }
      that->_dim);
   PBErrCatch(PBMathErr);
  }
#endif
 return ((short*)(((void*)that) + sizeof(int)))[i];
#if BUILDMODE != 0
inline
#endif
short _VecShortGet2D(VecShort2D* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  7
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%d<2)", i);\\
   PBErrCatch(PBMathErr);
 }
#endif
 return that->_val[i];
#if BUILDMODE != 0
inline
#endif
short _VecShortGet3D(VecShort3D* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<3)", i);</pre>
    PBErrCatch(PBMathErr);
#endif
  return that->_val[i];
#if BUILDMODE != 0
inline
```

```
short _VecShortGet4D(VecShort4D* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 4) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%d<4)", i);\\
    PBErrCatch(PBMathErr);
#endif
 return that->_val[i];
// Set the i-th value of the VecShort to v
#if BUILDMODE != 0
inline
#endif
void _VecShortSet(VecShort* that, int i, short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<%d)", i,
      that->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  ((short*)(((void*)that) + sizeof(int)))[i] = v;
#if BUILDMODE != 0
inline
#endif
void _VecShortSet2D(VecShort2D* that, int i, short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%d<2)", i);\\
   PBErrCatch(PBMathErr);
#endif
 that->_val[i] = v;
#if BUILDMODE != 0
inline
#endif
void _VecShortSet3D(VecShort3D* that, int i, short v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<3)", i);</pre>
    PBErrCatch(PBMathErr);
  }
#endif
 that->_val[i] = v;
#if BUILDMODE != 0
inline
#endif
\label{lem:void_VecShortSet4D(VecShort4D* that, int i, short v) {} \\
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 | | i >= 4) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->\_msg, "'i' is invalid (0<=\%d<4)", i);\\
   PBErrCatch(PBMathErr);
#endif
 that->_val[i] = v;
// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
inline
#endif
void _VecShortSetNull(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Set values
  for (int iDim = that->_dim; iDim--;)
    that->_val[iDim] = 0;
// Return the dimension of the VecShort
#if BUILDMODE != 0
inline
#endif
int _VecShortGetDim(VecShort* that) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 7
#endif
 return that->_dim;
// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
```

```
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist(VecShort* that, VecShort* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    \label{lem:constraint} sprintf(PBMathErr->\_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Declare a variable to calculate the distance
  short ret = 0;
  for (int iDim = VecGetDim(that); iDim--;)
    ret += abs(VecGet(that, iDim) - VecGet(tho, iDim));
  // Return the distance
  return ret;
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist2D(VecShort2D* that, VecShort2D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
  abs(VecGet(that, 1) - VecGet(tho, 1));
#if BUILDMODE != 0
inline
#endif
short _VecShortHamiltonDist3D(VecShort3D* that, VecShort3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
```

```
PBErrCatch(PBMathErr);
  }
#endif
 // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
   abs(VecGet(that, 1) - VecGet(tho, 1)) +
abs(VecGet(that, 2) - VecGet(tho, 2));
#if BUILDMODE != 0
inline
#endif
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Return the distance
  return abs(VecGet(that, 0) - VecGet(tho, 0)) +
    abs(VecGet(that, 1) - VecGet(tho, 1)) +
    abs(VecGet(that, 2) - VecGet(tho, 2)) +
    abs(VecGet(that, 3) - VecGet(tho, 3));
}
// Return true if the VecShort 'that' is equal to 'tho', else false
#if BUILDMODE != 0
inline
#endif
bool _VecShortIsEqual(VecShort* that, VecShort* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    \label{lem:constraint} sprintf(PBMathErr->\_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  return
    (memcmp(that->_val, tho->_val, sizeof(short) * that->_dim) == 0);
// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
inline
#endif
```

```
void _VecShortCopy(VecShort* that, VecShort* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Copy the values
  {\tt memcpy(that->\_val,\ tho->\_val,\ sizeof(short)\ *\ that->\_dim);}
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd(VecShort* that, VecShort* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "dimensions\ \bar{d}on't\ match\ (\%d==\%d)",}
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} Declare a variable ot memorise the result
  short res = 0;
  // For each component
  for (int iDim = that->_dim; iDim--;)
    // Calculate the product
    res += VecGet(that, iDim) * VecGet(tho, iDim);
  // Return the result
  return res;
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd2D(VecShort2D* that, VecShort2D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1);
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd3D(VecShort3D* that, VecShort3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2);
#if BUILDMODE != 0
inline
#endif
short _VecShortDotProd4D(VecShort4D* that, VecShort4D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  return VecGet(that, 0) * VecGet(tho, 0) +
    VecGet(that, 1) * VecGet(tho, 1) +
    VecGet(that, 2) * VecGet(tho, 2) +
    VecGet(that, 3) * VecGet(tho, 3);
}
// Static constructors for VecFloat
#if BUILDMODE != 0
inline
#endif
VecFloat2D VecFloatCreateStatic2D() {
 VecFloat2D v = {._val = {0.0, 0.0}, ._dim = 2};
 return v;
}
```

```
#if BUILDMODE != 0
inline
VecFloat3D VecFloatCreateStatic3D() {
  VecFloat3D v = {.\_val = {0.0, 0.0, 0.0}, .\_dim = 3};
 return v;
// Return the i-th value of the VecFloat
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet(VecFloat* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'i' is invalid (0<=%d<%d)", i, that->_dim);
    PBErrCatch(PBMathErr);
#endif
  // Return the value
 return that->_val[i];
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet2D(VecFloat2D* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<2)", i);</pre>
    PBErrCatch(PBMathErr);
#endif
 // Return the value
 return that->_val[i];
#if BUILDMODE != 0
inline
#endif
float _VecFloatGet3D(VecFloat3D* that, int i) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<3)", i);
    PBErrCatch(PBMathErr);
```

```
}
#endif
  // Return the value
  return that->_val[i];
// Set the i-th value of the VecFloat to \boldsymbol{v}
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet(VecFloat* that, int i, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 || i >= that->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'i' is invalid (0<=%d<%d)", i, that->_dim);
    PBErrCatch(PBMathErr);
 }
#endif
  // Set the value
  that->_val[i] = v;
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet2D(VecFloat2D* that, int i, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<2)", i);</pre>
    PBErrCatch(PBMathErr);
#endif
  // Set the value
  that->_val[i] = v;
#if BUILDMODE != 0
inline
#endif
void _VecFloatSet3D(VecFloat3D* that, int i, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (i < 0 \mid | i >= 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%d<3)", i);</pre>
    PBErrCatch(PBMathErr);
  }
#endif
```

```
// Set the value
  that->_val[i] = v;
// Set all values of the vector 'that' to 0.0
#if BUILDMODE != 0
inline
#endif
void _VecFloatSetNull(VecFloat* that) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Set values
  for (int iDim = that->_dim; iDim--;)
    that->_val[iDim] = 0.0;
#if BUILDMODE != 0
inline
#endif
void _VecFloatSetNull2D(VecFloat2D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Set values
  that->_val[0] = 0.0;
  that->_val[1] = 0.0;
#if BUILDMODE != 0
inline
void _VecFloatSetNull3D(VecFloat3D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Set values
  that->_val[0] = 0.0;
  that->_val[1] = 0.0;
 that->_val[2] = 0.0;
// Return the dimension of the VecFloat
#if BUILDMODE != 0
inline
#endif
int _VecFloatGetDim(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
}
#endif
 return that->_dim;
// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatCopy(VecFloat* that, VecFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Copy the values
 memcpy(that->_val, tho->_val, sizeof(float) * that->_dim);
// Return the norm of the VecFloat
#if BUILDMODE != 0
inline
#endif
float _VecFloatNorm(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} Declare a variable to calculate the norm
  float ret = 0.0;
  // Calculate the norm
  for (int iDim = that->_dim; iDim--;)
   ret += fsquare(VecGet(that, iDim));
  ret = sqrt(ret);
  // Return the result
 return ret;
}
#if BUILDMODE != 0
inline
#endif
float _VecFloatNorm2D(VecFloat2D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
}
#endif
  // Return the result
 return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)));
#if BUILDMODE != 0
inline
#endif
float _VecFloatNorm3D(VecFloat3D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Return the result
  return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)) +
    fsquare(VecGet(that, 2)));
// Normalise the VecFloat
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Normalise
  float norm = VecNorm(that);
  for (int iDim = that->_dim; iDim--;)
    VecSet(that, iDim, VecGet(that, iDim) / norm);
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise2D(VecFloat2D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Normalise
  float norm = _VecFloatNorm2D(that);
  VecSet(that, 0, VecGet(that, 0) / norm);
  VecSet(that, 1, VecGet(that, 1) / norm);
#if BUILDMODE != 0
inline
#endif
void _VecFloatNormalise3D(VecFloat3D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Normalise
  float norm = _VecFloatNorm3D(that);
  VecSet(that, 0, VecGet(that, 0) / norm);
  VecSet(that, 1, VecGet(that, 1) / norm);
  VecSet(that, 2, VecGet(that, 2) / norm);
// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist(VecFloat* that, VecFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (int iDim = that->_dim; iDim--;)
   ret += fsquare(VecGet(that, iDim) - VecGet(tho, iDim));
  ret = sqrt(ret);
  // Return the distance
 return ret;
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist2D(VecFloat2D* that, VecFloat2D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
    fsquare(VecGet(that, 1) - VecGet(tho, 1)));
```

```
#if BUILDMODE != 0
inline
#endif
float _VecFloatDist3D(VecFloat3D* that, VecFloat3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
    fsquare(VecGet(that, 1) - VecGet(tho, 1)) +
fsquare(VecGet(that, 2) - VecGet(tho, 2)));
// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist(VecFloat* that, VecFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (int iDim = that->_dim; iDim--;)
   ret += fabs(VecGet(that, iDim) - VecGet(tho, iDim));
  // Return the distance
 return ret;
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist2D(VecFloat2D* that, VecFloat2D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Return the distance
  return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
   fabs(VecGet(that, 1) - VecGet(tho, 1));
#if BUILDMODE != 0
inline
#endif
float _VecFloatHamiltonDist3D(VecFloat3D* that, VecFloat3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
  fabs(VecGet(that, 1) - VecGet(tho, 1)) +
    fabs(VecGet(that, 2) - VecGet(tho, 2));
// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatPixelDist(VecFloat* that, VecFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to calculate the distance
  float ret = 0.0;
  for (int iDim = that->_dim; iDim--;)
    ret += fabs(floor(VecGet(that, iDim)) - floor(VecGet(tho, iDim)));
  // Return the distance
  return ret;
```

```
#if BUILDMODE != 0
inline
#endif
{\tt float \_VecFloatPixelDist2D(VecFloat2D*\ that,\ VecFloat2D*\ tho)\ \{}
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the distance
  return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) +
    fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1)));
#if BUILDMODE != 0
inline
#endif
float _VecFloatPixelDist3D(VecFloat3D* that, VecFloat3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  // Return the distance
  return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) +
    fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1))) +
    fabs(floor(VecGet(that, 2)) - floor(VecGet(tho, 2)));
// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
inline
#endif
bool _VecFloatIsEqual(VecFloat* that, VecFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
```

```
PBErrCatch(PBMathErr);
  }
#endif
  // For each component
  for (int iDim = that->_dim; iDim--;)
    // If the values of this components are different
    if (!ISEQUALF(VecGet(that, iDim), VecGet(tho, iDim)))
      // Return false
      return false;
  // Return true
 return true;
// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloat0p(VecFloat* that, float a, VecFloat* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
#endif
  for (int iDim = that->_dim; iDim--;)
    VecSet(that, iDim,
      a * VecGet(that, iDim) + b * VecGet(tho, iDim));
#if BUILDMODE != 0
inline
#endif
void _VecFloatOp2D(VecFloat2D* that, float a, VecFloat2D* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
#if BUILDMODE != 0
inline
#endif
```

```
void _VecFloatOp3D(VecFloat3D* that, float a, VecFloat3D* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
// Return a VecFloat equal to (that * a + tho * b)
#if BUILDMODE != 0
inline
#endif
VecFloat* _VecFloatGetOp(VecFloat* that, float a,
  VecFloat* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  VecFloat* res = VecFloatCreate(that->_dim);
  for (int iDim = that->_dim; iDim--;)
    VecSet(res. iDim.
     a * VecGet(that, iDim) + b * VecGet(tho, iDim));
 return res;
#if BUILDMODE != 0
inline
VecFloat2D _VecFloatGetOp2D(VecFloat2D* that, float a,
  VecFloat2D* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
```

```
PBErrCatch(PBMathErr);
  }
#endif
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
 return res;
}
#if BUILDMODE != 0
{\tt inline}
VecFloat3D _VecFloatGetOp3D(VecFloat3D* that, float a,
  VecFloat3D* tho, float b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
 return res;
// Calculate (that * a) and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatScale(VecFloat* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  for (int iDim = that->_dim; iDim--;)
    VecSet(that, iDim, a * VecGet(that, iDim));
#if BUILDMODE != 0
inline
#endif
void _VecFloatScale2D(VecFloat2D* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  VecSet(that, 0, a * VecGet(that, 0));
  VecSet(that, 1, a * VecGet(that, 1));
#if BUILDMODE != 0
```

```
inline
#endif
void _VecFloatScale3D(VecFloat3D* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  VecSet(that, 0, a * VecGet(that, 0));
  VecSet(that, 1, a * VecGet(that, 1));
  VecSet(that, 2, a * VecGet(that, 2));
// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0
inline
#endif
VecFloat* _VecFloatGetScale(VecFloat* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  VecFloat* res = VecFloatCreate(that->_dim);
  for (int iDim = that->_dim; iDim--;)
   VecSet(res, iDim, a * VecGet(that, iDim));
 return res;
#if BUILDMODE != 0
inline
#endif
VecFloat2D _VecFloatGetScale2D(VecFloat2D* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, a * VecGet(that, 0));
  VecSet(&res, 1, a * VecGet(that, 1));
 return res;
#if BUILDMODE != 0
inline
#endif
VecFloat3D _VecFloatGetScale3D(VecFloat3D* that, float a) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 7
#endif
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, a * VecGet(that, 0));
  VecSet(&res, 1, a * VecGet(that, 1));
```

```
VecSet(&res, 2, a * VecGet(that, 2));
  return res;
// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRot2D(VecFloat2D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    \label{lem:sprintf} sprintf(PBMathErr->\_msg, \ "'that' \ 's \ dimension is invalid \ (\%d=2)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  }
#endif
 *that = _VecFloatGetRot2D(that, theta);
// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
inline
#endif
VecFloat2D _VecFloatGetRot2D(VecFloat2D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=2)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  VecFloat2D res = VecFloatCreateStatic2D();
  // Declare variable for optimization
  float cosTheta = cos(theta);
  float sinTheta = sin(theta);
  // Calculate the rotation
  VecSet(&res, 0,
    cosTheta * VecGet(that, 0) - sinTheta * VecGet(that, 1));
  VecSet(&res, 1,
    sinTheta * VecGet(that, 0) + cosTheta * VecGet(that, 1));
  // Return the result
 return res;
// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd(VecFloat* that, VecFloat* tho) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float res = 0.0:
  // Calculate
  for (int iDim = that->_dim; iDim--;)
   res += that->_val[iDim] * tho->_val[iDim];
  // Return the result
 return res;
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd2D(VecFloat2D* that, VecFloat2D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
 return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1];
#if BUILDMODE != 0
inline
#endif
float _VecFloatDotProd3D(VecFloat3D* that, VecFloat3D* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1] +
    that->_val[2] * tho->_val[2];
```

```
// Return the conversion of VecFloat 'that' to a VecShort using round()
#if BUILDMODE != 0
inline
#endif
VecShort* VecFloatToShort(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Create the result
  VecShort* res = VecShortCreate(that->_dim);
  for (int iDim = that->_dim; iDim--;)
    VecSet(res, iDim, SHORT(VecGet(that, iDim)));
  // Return the result
 return res;
}
#if BUILDMODE != 0
inline
#endif
VecShort2D VecFloatToShort2D(VecFloat2D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecShort2D res = VecShortCreateStatic2D();
  VecSet(&res, 0, SHORT(VecGet(that, 0)));
  VecSet(&res, 1, SHORT(VecGet(that, 1)));
  // Return the result
 return res;
#if BUILDMODE != 0
inline
#endif
VecShort3D VecFloatToShort3D(VecFloat3D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Create the result
  VecShort3D res = VecShortCreateStatic3D();
  VecSet(&res, 0, SHORT(VecGet(that, 0)));
  VecSet(&res, 1, SHORT(VecGet(that, 1)));
  VecSet(&res, 2, SHORT(VecGet(that, 2)));
  // Return the result
 return res;
// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
inline
```

```
#endif
VecFloat* VecShortToFloat(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecFloat* res = VecFloatCreate(that->_dim);
  for (int iDim = that->_dim; iDim--;)
    VecSet(res, iDim, (float)VecGet(that, iDim));
  // Return the result
  return res;
#if BUILDMODE != 0
inline
#endif
VecFloat2D VecShortToFloat2D(VecShort2D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Create the result
  VecFloat2D res = VecFloatCreateStatic2D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
  // Return the result
 return res;
}
#if BUILDMODE != 0
inline
#endif
VecFloat3D VecShortToFloat3D(VecShort3D* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Create the result
  VecFloat3D res = VecFloatCreateStatic3D();
  VecSet(&res, 0, (float)VecGet(that, 0));
  VecSet(&res, 1, (float)VecGet(that, 1));
  VecSet(&res, 2, (float)VecGet(that, 2));
  // Return the result
 return res;
}
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMaxVal(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float max = VecGet(that, 0);
  // Search for the maximum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   max = MAX(max, VecGet(that, i));
  // Return the result
 return max;
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMinVal(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable to memorize the result
  float min = VecGet(that, 0);
  // Search for the minimum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   min = MIN(min, VecGet(that, i));
  // Return the result
 return min;
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMaxValAbs(VecFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Declare a variable to memorize the result
 float max = fabs(VecGet(that, 0));
  // Search for the maximum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   max = (fabs(max) > fabs(VecGet(that, i)) ? max : VecGet(that, i));
  // Return the result
 return max;
// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
float _VecFloatGetMinValAbs(VecFloat* that) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  float min = fabs(VecGet(that, 0));
  // Search for the minimum value
  for (int i = VecGetDim(that); i-- && i != 0;)
    min = (fabs(min) < fabs(VecGet(that, i)) ? min : VecGet(that, i));</pre>
  // Return the result
 return min;
}
// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
inline
#endif
void _MatFloatSetIdentity(MatFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(\&(that->_dim), 0) != VecGet(\&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(PBMathErr->\_msg,\ "the\ matrix\ is\ not\ square\ (\%dx\%d)",}
      VecGet(\&(that->_dim), 0), VecGet(\&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  7
#endif
  // Set the values
  VecShort2D i = VecShortCreateStatic2D();
    if (VecGet(&i, 0) == VecGet(&i, 1))
      MatSet(that, &i, 1.0);
      MatSet(that, &i, 0.0);
 } while (VecStep(&i, &(that->_dim)));
// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
inline
#endif
MatFloat* _MatFloatGetAdd(MatFloat* that, MatFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
```

```
if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' and 'tho' have different dimensions");
    PBErrCatch(PBMathErr);
  }
#endif
  // Declare a variable for the result
  MatFloat* res = MatFloatCreate(MatDim(that));
  // Add each values
  VecShort2D i = VecShortCreateStatic2D();
    MatSet(res, &i, MatGet(that, &i) + MatGet(tho, &i));
  } while (VecStep(&i, MatDim(that)));
  // Return the result
 return res;
// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
inline
#endif
void _MatFloatAdd(MatFloat* that, MatFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' and 'tho' have different dimensions");
    PBErrCatch(PBMathErr);
#endif
  // Add each values
  VecShort2D i = VecShortCreateStatic2D();
  do {
    MatSet(that, &i, MatGet(that, &i) + MatGet(tho, &i));
 } while (VecStep(&i, MatDim(that)));
// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
inline
#endif
void _MatFloatCopy(MatFloat* that, MatFloat* tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
```

```
sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&(that->_dim), &(tho->_dim))) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'that' and 'tho' have different dimensions (\dx\d==\dx\d)",
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1),
      VecGet(\&(tho->_dim), 0), VecGet(\&(tho->_dim), 1));
    PBErrCatch(PBMathErr);
  }
#endif
  // Copy the matrix values
  int d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
 memcpy(that->_val, tho->_val, d * sizeof(float));
// Return the value at index 'i' (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
inline
#endif
float _MatFloatGet(MatFloat* that, VecShort2D* index) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (index == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'index' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(index, 0) < 0 ||</pre>
    VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
    VecGet(index, 1) < 0 | |
    VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'index' is invalid (0,0 \le d,d < d,d)",
      VecGet(index, 0), VecGet(index, 1),
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
#endif
  // Return the value
  return that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
    VecGet(index, 0)];
// Set the value at index 'i' (col, line) of the MatFloat to 'v'
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
inline
#endif
void _MatFloatSet(MatFloat* that, VecShort2D* index, float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
```

```
if (index == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'index' is null");
    PBErrCatch(PBMathErr);
  if (VecGet(index, 0) < 0 \mid |
    VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
    VecGet(index, 1) < 0 ||</pre>
    VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
      "'index' is invalid (0,0 <= d,d < d,d",
      VecGet(index, 0), VecGet(index, 1),
      VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
  }
#endif
  // Set the value
  that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
    VecGet(index, 0)] = v;
// Return the dimension of the MatFloat
#if BUILDMODE != 0
inline
#endif
VecShort2D* _MatFloatDim(MatFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  \ensuremath{//} Return the dimension
  return &(that->_dim);
// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
inline
#endif
VecShort2D _MatFloatGetDim(MatFloat* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  // Return the dimension
  return that->_dim;
// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
inline
#endif
float GaussGet(Gauss *that, float x) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  // Calculate the value
  float a = 1.0 / (that->_sigma * sqrt(2.0 * PBMATH_PI));
  float ret = a * exp(-1.0 * fsquare(x - that->_mean) /
    (2.0 * fsquare(that->_sigma)));
  // Return the value
 return ret;
// Return a random value (in ]0.0, 1.0[)according to the
// Gauss distribution 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
inline
#endif
float GaussRnd(Gauss *that) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare variable for calcul
  float v1,v2,s;
  // Calculate the value
  do {
   v1 = (rnd() - 0.5) * 2.0;
   v2 = (rnd() - 0.5) * 2.0;
    s = v1 * v1 + v2 * v2;
  } while (s >= 1.0);
  // Return the value
  float ret = 0.0;
  if (s > PBMATH_EPSILON)
    ret = v1 * sqrt(-2.0 * log(s) / s);
 return ret * that->_sigma + that->_mean;
// Return the order 1 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
inline
#endif
float SmoothStep(float x) {
  if (x > 0.0)
    if (x < 1.0)
     return x * x * (3.0 - 2.0 * x);
    else
     return 1.0;
  else
    return 0.0;
// Return the order 2 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
```

```
inline
#endif
float SmootherStep(float x) {
  if (x > 0.0)
    if (x < 1.0)
    return x * x * x * (x * (x * 6.0 - 15.0) + 10.0);
    else
      return 1.0;
  else
    return 0.0;
// Solve the SysLinEq _M.x = _V
// Return the solution vector, or null if there is no solution or the
// arguments are invalid
#if BUILDMODE != 0
inline
#endif
VecFloat* SysLinEqSolve(SysLinEq* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the solution
  VecFloat* ret = NULL;
  // Calculate the solution
  ret = MatGetProdVec(that->_Minv, that->_V);
  // Return the solution vector
 return ret;
// Set the matrix of the SysLinEq to a copy of 'm'
// 'm' must have same dimensions has the current matrix
// Do nothing if arguments are invalid
#if BUILDMODE != 0
inline
#endif
void SysLinEqSetM(SysLinEq* that, MatFloat* m) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (m == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'m' is null");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&(m->_dim), &(that->_M->_dim))) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'m' has invalid dimension (%dx%d==%dx%d)",
      VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1),
      VecGet(&(that->_M->_dim), 0), VecGet(&(that->_M->_dim), 1));
    PBErrCatch(PBMathErr);
#endif
  // Update the matrix values
  MatCopy(that->_M, m);
```

```
// Update the inverse matrix
 MatFree(&(that->_Minv));
 that->_Minv = MatInv(that->_M);
#if BUILDMODE == 0
  if (that->_Minv == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
   PBErrCatch(PBMathErr);
#endif
// Set the vector of the SysLinEq to a copy of 'v'
// 'v' must have same dimensions has the current vector
\ensuremath{//} Do nothing if arguments are invalid
#if BUILDMODE != 0
inline
#endif
void _SLESetV(SysLinEq* that, VecFloat* v) {
#if BUILDMODE == 0
 if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 if (v == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'v' is null");
   PBErrCatch(PBMathErr);
 if (VecGetDim(v) != VecGetDim(that->_V)) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'v' has invalid dimension (%d==%d)",
     VecGetDim(v), VecGetDim(that->_V));
   PBErrCatch(PBMathErr);
 }
#endif
  // Update the vector values
 VecCopy(that->_V, v);
// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/
// does-pow-work-for-int-data-type-in-c
#if BUILDMODE != 0
inline
#endif
int powi(int base, int exp) {
 // Declare a variable to memorize the result and init to 1
 int res = 1;
 // Loop on exponent
 while (exp) {
   // Do some magic trick
   if (exp & 1)
     res *= base;
   exp /= 2;
   base *= base;
 // Return the result
 return res;
```

```
// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecShortOp(VecShort* that, short a, VecShort* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
   PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
     that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
 }
#endif
  for (int iDim = that->_dim; iDim--;)
   VecSet(that, iDim,
     a * VecGet(that, iDim) + b * VecGet(tho, iDim));
#if BUILDMODE != 0
inline
#endif
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
  }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
#if BUILDMODE != 0
inline
#endif
void _VecShortOp3D(VecShort3D* that, short a, VecShort3D* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
   PBErrCatch(PBMathErr);
```

```
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
#if BUILDMODE != 0
inline
#endif
void _VecShortOp4D(VecShort4D* that, short a, VecShort4D* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
 }
#endif
  VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  VecSet(that, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
// Return a VecShort equal to (that * a + tho * b)
#if BUILDMODE != 0
inline
#endif
VecShort* _VecShortGetOp(VecShort* that, short a,
  VecShort* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%d==%d)",
      that->_dim, tho->_dim);
   PBErrCatch(PBMathErr);
  7
#endif
  VecShort* res = VecShortCreate(that->_dim);
  for (int iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
     a * VecGet(that, iDim) + b * VecGet(tho, iDim));
 return res;
#if BUILDMODE != 0
inline
#endif
VecShort2D _VecShortGetOp2D(VecShort2D* that, short a,
  VecShort2D* tho, short b) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecShort2D res = VecShortCreateStatic2D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  return res;
#if BUILDMODE != 0
#endif
VecShort3D _VecShortGetOp3D(VecShort3D* that, short a,
  VecShort3D* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
#endif
  VecShort3D res = VecShortCreateStatic3D();
  \label{lem:vecSet(lambdares)} $\operatorname{VecSet}(\operatorname{lamb}, \ 0, \ a \ * \ \operatorname{VecGet}(\operatorname{that}, \ 0) \ + \ b \ * \ \operatorname{VecGet}(\operatorname{tho}, \ 0)); $$
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
  VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  return res;
}
#if BUILDMODE != 0
inline
VecShort4D _VecShortGetOp4D(VecShort4D* that, short a,
  VecShort4D* tho, short b) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (tho == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
  }
#endif
  VecShort4D res = VecShortCreateStatic4D();
  VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
  VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
  VecSet(&res, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
```

```
return res;
}
// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMaxVal(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short max = VecGet(that, 0);
  // Search for the maximum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   max = MAX(max, VecGet(that, i));
  // Return the result
 return max;
// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMinVal(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  \ensuremath{//} Declare a variable to memorize the result
  short min = VecGet(that, 0);
  // Search for the minimum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   min = MIN(min, VecGet(that, i));
  \ensuremath{//} Return the result
 return min;
// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMaxValAbs(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short max = abs(VecGet(that, 0));
  // Search for the maximum value
  for (int i = VecGetDim(that); i-- && i != 0;)
```

```
max = (abs(max) > abs(VecGet(that, i)) ? max : VecGet(that, i));
  // Return the result
 return max;
// Get the min value (in absolute value) in components of the vector 'that'
#if BUILDMODE != 0
inline
#endif
short _VecShortGetMinValAbs(VecShort* that) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
#endif
  // Declare a variable to memorize the result
  short min = abs(VecGet(that, 0));
  // Search for the minimum value
  for (int i = VecGetDim(that); i-- && i != 0;)
   min = (abs(min) < abs(VecGet(that, i)) ? min : VecGet(that, i));</pre>
  // Return the result
 return min;
// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotAxis(VecFloat3D* that, VecFloat3D* axis, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  }
  if (axis == NULL) {
   PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'axis' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
      VecGetDim(that));
   PBErrCatch(PBMathErr);
  if (VecGetDim(axis) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%d=3)",
      VecGetDim(axis));
   PBErrCatch(PBMathErr);
  if (ISEQUALF(VecNorm(axis), 1.0) == false) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'axis' is not normalized");
    PBErrCatch(PBMathErr);
```

```
#endif
 *that = _VecFloatGetRotAxis(that, axis, theta);
// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotX(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
      VecGetDim(that)):
   PBErrCatch(PBMathErr);
#endif
  *that = _VecFloatGetRotX(that, theta);
// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotY(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%d=3)",
      VecGetDim(that));
    PBErrCatch(PBMathErr);
  }
#endif
  *that = _VecFloatGetRotY(that, theta);
}
// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
inline
#endif
void _VecFloatRotZ(VecFloat3D* that, float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (VecGetDim(that) != 3) {
    PBMathErr->_type = PBErrTypeInvalidArg;
```

## 4 Makefile

```
#directory
PBERRDIR=../PBErr
# Build mode
# 0: development (max safety, no optimisation)
# 1: release (min safety, optimisation)
# 2: fast and furious (no safety, optimisation)
BUILDMODE=1
include $(PBERRDIR)/Makefile.inc
INCPATH=-I./ -I$(PBERRDIR)/
BUILDOPTIONS=$(BUILDPARAM) $(INCPATH)
# compiler
COMPILER=gcc
#rules
all : main
main: main.o pberr.o pbmath.o Makefile
$(COMPILER) main.o pberr.o pbmath.o $(LINKOPTIONS) -o main
main.o : main.c $(PBERRDIR)/pberr.h pbmath.h pbmath-inline.c Makefile
$(COMPILER) $(BUILDOPTIONS) -c main.c
pbmath.o : pbmath.c pbmath.h pbmath-inline.c Makefile
$(COMPILER) $(BUILDOPTIONS) -c pbmath.c
pberr.o : $(PBERRDIR)/pberr.c $(PBERRDIR)/pberr.h Makefile
$(COMPILER) $(BUILDOPTIONS) -c $(PBERRDIR)/pberr.c
clean :
rm -rf *.o main
valgrind :
valgrind -v --track-origins=yes --leak-check=full --gen-suppressions=yes --show-leak-kinds=all ./main
main > unitTest.txt; diff unitTest.txt unitTestRef.txt
```

## 5 Unit tests

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
```

```
#include <string.h>
#include <time.h>
#include <unistd.h>
#include <sys/time.h>
#include "pberr.h"
#include "pbmath.h"
#define RANDOMSEED 0
void UnitTestPowi() {
 int a;
  int n;
  for (n = 1; n \le 5; ++n) {
    for (a = 0; a <= 10; ++a) {
      int b = powi(a, n);
      int c = 1;
      int m = n;
      for (; m--;) c *= a;
      if (b != c) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg,
          "powi(%d, %d) = %d , %d^%d = %d",
          a, n, b, a, n, c);
        PBErrCatch(PBMathErr);
   }
printf("powi OK\n");
}
void UnitTestFastPow() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  float sumErr = 0.0;
  float maxErr = 0.0;
  int i = nbTest;
  for (; i--;) {
    float a = (rnd() - 0.5) * 1000.0;
    int n = INT(rnd() * 5.0);
    float b = fastpow(a, n);
    float c = pow(a, n);
    float err = fabs(b - c);
    sumErr += err;
    if (maxErr < err)</pre>
      maxErr = err;
  float avgErr = sumErr / (float)nbTest;
  printf("average error: %f < %f, max error: %f < %f \n",
   avgErr, PBMATH_EPSILON, maxErr, PBMATH_EPSILON * 10.0);
  if (avgErr >= PBMATH_EPSILON ||
    maxErr >= PBMATH_EPSILON * 10.0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "fastpow NOK");
    PBErrCatch(PBMathErr);
printf("fastpow OK\n");
}
void UnitTestSpeedFastPow() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  int i = nbTest;
```

```
clock_t clockBefore = clock();
  for (; i--;) {
    float a = (rnd() - 0.5) * 1000.0;
    int n = INT(rnd() * 5.0);
    float b = fastpow(a, n);
   b = b;
  clock_t clockAfter = clock();
  double timeFastpow = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
  clockBefore = clock();
  for (; i--;) {
    float a = (rnd() - 0.5) * 1000.0;
int n = INT(rnd() * 5.0);
    float c = pow(a, n);
   c = c;
  clockAfter = clock();
  double timePow = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
  printf("fastpow: %fms, pow: %fms\n",
    timeFastpow / (float)nbTest, timePow / (float)nbTest);
  if (timeFastpow >= timePow) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    PBMathErr->_fatal = false;
    sprintf(PBMathErr->_msg, "speed fastpow NOK");
    PBErrCatch(PBMathErr);
printf("speed fastpow OK\n");
}
void UnitTestFSquare() {
  srandom(RANDOMSEED);
  int nbTest = 1000;
  for (; nbTest--;) {
    float a = (rnd() - 0.5) * 2000.0;
    float b = fsquare(a);
    float c = a * a;
    if (!ISEQUALF(b, c)) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      PBMathErr->_fatal = false;
      sprintf(PBMathErr->_msg,
        "fsquare(%f) = %f , %f*%f = %f",
        a, b, a, a, c);
      PBErrCatch(PBMathErr);
printf("fsquare OK\n");
}
void UnitTestVecShortCreateFree() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecPrint(v, stdout);printf("\n");
  VecPrint(&v2, stdout);printf("\n");
  VecPrint(&v3, stdout);printf("\n");
  VecPrint(&v4, stdout);printf("\n");
  VecFree(&v);
```

```
if (v != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecShort is not null after VecFree");
   PBErrCatch(PBMathErr);
 printf("VecShortCreateFree OK\n");
void UnitTestVecShortClone() {
 VecShort* v = VecShortCreate(5);
  for (int i = 5; i--;) VecSet(v, i, i + 1);
 VecShort* w = VecClone(v);
  if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortClone NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("_VecShortClone OK\n");
void UnitTestVecShortLoadSave() {
 VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 FILE* f = fopen("./UnitTestVecShortLoadSave.txt", "w");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecShortLoadSave.txt for writing");
   PBErrCatch(PBMathErr);
 if (!VecSave(v, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecSave(&v2, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecSave(&v3, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
   PBErrCatch(PBMathErr);
 }
 if (!VecSave(&v4, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSave NOK");
   PBErrCatch(PBMathErr);
 VecShort* w = VecShortCreate(2);
 f = fopen("./UnitTestVecShortLoadSave.txt", "r");
  if (f == NULL) {
```

```
PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecShortLoadSave.txt for reading");
   PBErrCatch(PBMathErr);
  if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(&v2, w, sizeof(VecShort) + sizeof(short) * 2) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
  if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(\&v3, w, sizeof(VecShort) + sizeof(short) * 3) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
   PBErrCatch(PBMathErr);
  if (memcmp(&v4, w, sizeof(VecShort) + sizeof(short) * 4) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFree(&v);
 VecFree(&w);
 int ret = system("cat ./UnitTestVecShortLoadSave.txt");
 printf("_VecShortLoadSave OK\n");
 ret = system("rm ./UnitTestVecShortLoadSave.txt");
 ret = ret;
void UnitTestVecShortGetSetDim() {
 VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
 if (VecGetDim(v) != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGetDim NOK");
```

}

```
PBErrCatch(PBMathErr);
}
for (int i = 5; i--;) VecSet(v, i, i + 1);
for (int i = 2; i--;) VecSet(&v2, i, i + 1);
for (int i = 3; i--;) VecSet(&v3, i, i + 1);
for (int i = 4; i--;) VecSet(&v4, i, i + 1);
for (int i = 5; i--;)
  if (v->_val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (v2._val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (v3._val[i] != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 4; i--;)
  if (v4._val[i] != i + 1) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortSet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 5; i--;)
  if (VecGet(v, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (VecGet(&v2, i) != i + 1) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (VecGet(&v3, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 4; i--;)
  if (VecGet(&v4, i) != i + 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
   PBErrCatch(PBMathErr);
VecSetNull(v);
VecSetNull(&v2);
VecSetNull(&v3);
VecSetNull(&v4);
for (int i = 5; i--;)
 if (VecGet(v, i) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortGet NOK");
```

```
PBErrCatch(PBMathErr);
    }
  for (int i = 2; i--;)
    if (VecGet(&v2, i) != 0) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGet NOK");
      PBErrCatch(PBMathErr);
    }
  for (int i = 3; i--;)
    if (VecGet(&v3, i) != 0) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGet NOK");
      PBErrCatch(PBMathErr);
  for (int i = 4; i--;)
    if (VecGet(&v4, i) != 0) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGet NOK");
      PBErrCatch(PBMathErr);
  VecFree(&v);
 printf("_VecShortGetSetDim OK\n");
void UnitTestVecShortStep() {
  VecShort* v = VecShortCreate(5);
  VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecShort* bv = VecShortCreate(5);
  VecShort2D bv2 = VecShortCreateStatic2D();
  VecShort3D bv3 = VecShortCreateStatic3D();
  VecShort4D bv4 = VecShortCreateStatic4D();
  short b[5] = \{2, 3, 4, 5, 6\};
  for (int i = 5; i--;) VecSet(bv, i, b[i]);
  for (int i = 2; i--;) VecSet(&bv2, i, b[i]);
  for (int i = 3; i--;) VecSet(&bv3, i, b[i]);
  for (int i = 4; i--;) VecSet(&bv4, i, b[i]);
  int acheck[2 * 3 * 4 * 5 * 6];
  for (int i = 0; i < 2 * 3 * 4 * 5 * 6; ++i)
   acheck[i] = i;
  int iCheck = 0;
  do {
    int a = VecGet(v, 0);
    for (int i = 1; i < VecGetDim(v); ++i)</pre>
      a = a * b[i] + VecGet(v, i);
    if (a != acheck[iCheck]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortStep NOK");
      PBErrCatch(PBMathErr);
    ++iCheck;
  } while (VecStep(v, bv));
  iCheck = 0;
  do {
    int a = VecGet(&v2, 0);
    for (int i = 1; i < 2; ++i)
      a = a * b[i] + VecGet(&v2, i);
    if (a != acheck[iCheck]) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortStep NOK");
      PBErrCatch(PBMathErr);
```

```
++iCheck;
} while (VecStep(&v2, &bv2));
iCheck = 0;
do {
  int a = VecGet(&v3, 0);
 for (int i = 1; i < 3; ++i)
   a = a * b[i] + VecGet(&v3, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecStep(&v3, &bv3));
iCheck = 0;
do {
 int a = VecGet(&v4, 0);
  for (int i = 1; i < 4; ++i)
   a = a * b[i] + VecGet(&v4, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecStep(&v4, &bv4));
iCheck = 0;
do {
 int a = VecGet(v, VecGetDim(v) - 1);
 for (int i = VecGetDim(v) - 2; i >= 0; --i)
   a = a * b[i] + VecGet(v, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecPStep(v, bv));
iCheck = 0;
do {
 int a = VecGet(&v2, 1);
  a = a * b[0] + VecGet(&v2, 0);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
 ++iCheck;
} while (VecPStep(&v2, &bv2));
iCheck = 0;
do {
 int a = VecGet(&v3, 2);
  for (int i = 1; i >= 0; --i)
   a = a * b[i] + VecGet(&v3, i);
  if (a != acheck[iCheck]) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
   PBErrCatch(PBMathErr);
 }
  ++iCheck;
} while (VecPStep(&v3, &bv3));
```

```
iCheck = 0;
  do {
   int a = VecGet(&v4, 3);
    for (int i = 2; i >= 0; --i)
     a = a * b[i] + VecGet(&v4, i);
    if (a != acheck[iCheck]) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
     PBErrCatch(PBMathErr);
   ++iCheck;
 } while (VecPStep(&v4, &bv4));
 VecFree(&v);
 VecFree(&bv);
 printf("UnitTestVecShortStep OK\n");
void UnitTestVecShortHamiltonDist() {
  VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
 VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
 VecShort4D w4 = VecShortCreateStatic4D();
  short b[5] = \{-2, -1, 0, 1, 2\};
  for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 4; i--;) VecSet(&v4, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
 for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
  for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
  short dist = VecHamiltonDist(v, w);
  if (dist != 13) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v2, &w2);
  if (dist != 2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 dist = VecHamiltonDist(&v3, &w3);
 if (dist != 5) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 }
 dist = VecHamiltonDist(&v4, &w4);
 if (dist != 8) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortHamiltonDist OK\n");
```

```
void UnitTestVecShortIsEqual() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 VecShort* w = VecShortCreate(5);
 VecShort2D w2 = VecShortCreateStatic2D();
 VecShort3D w3 = VecShortCreateStatic3D();
 VecShort4D w4 = VecShortCreateStatic4D();
 if (VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 for (int i = 5; i--;) VecSet(w, i, i + 1);
 for (int i = 2; i--;) VecSet(\&w2, i, i + 1);
 for (int i = 3; i--;) VecSet(&w3, i, i + 1);
 for (int i = 4; i--;) VecSet(&w4, i, i + 1);
 if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortIsEqual OK\n");
```

```
void UnitTestVecShortCopy() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
  VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  for (int i = 4; i--;) VecSet(&v4, i, i + 1);
  VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  VecCopy(w, v);
  VecCopy(&w2, &v2);
  VecCopy(&w3, &v3);
  VecCopy(&w4, &v4);
  if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v4, &w4)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecShortCopy OK\n");
void UnitTestVecShortDotProd() {
  VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
  VecShort4D v4 = VecShortCreateStatic4D();
  VecShort* w = VecShortCreate(5);
  VecShort2D w2 = VecShortCreateStatic2D();
  VecShort3D w3 = VecShortCreateStatic3D();
  VecShort4D w4 = VecShortCreateStatic4D();
  short b[5] = \{-2, -1, 0, 1, 2\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 4; i--;) VecSet(&v4, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
  for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
  for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
```

```
short prod = VecDotProd(v, w);
 if (prod != -10) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v2, &w2);
 if (prod != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 prod = VecDotProd(&v3, &w3);
 if (prod != -2) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 }
 prod = VecDotProd(&v4, &w4);
 if (prod != -6) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortDotProd OK\n");
void UnitTestSpeedVecShort() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 int nbTest = 100000;
 srandom(RANDOMSEED);
 int i = nbTest;
 clock_t clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
   short val = 1;
   VecSet(v, j, val);
   short valb = VecGet(v, j);
   valb = valb;
 clock_t clockAfter = clock();
 double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 short* array = malloc(sizeof(short) * 5);
 for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
   short val = 1;
   array[j] = val;
   short valb = array[j];
   valb = valb;
 clockAfter = clock();
 double timeRef = ((double)(clockAfter - clockBefore)) /
```

```
CLOCKS_PER_SEC * 1000.0;
 printf("VecShort: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
 if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
  for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
    short val = 1;
   VecSet(&v2, j, val);
short valb = VecGet(&v2, j);
   valb = valb;
 clockAfter = clock();
  timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
 clockBefore = clock();
 short array2[2];
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
    short val = 1;
   array2[j] = val;
   short valb = array2[j];
   valb = valb;
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecShort2D: \%fms, array: \%fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
 if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest:
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
    short val = 1;
    VecSet(&v3, j, val);
   short valb = VecGet(&v3, j);
   valb = valb;
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
```

```
CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
 clockBefore = clock();
  short array3[3];
  for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
    short val = 1;
   array3[j] = val;
    short valb = array3[j];
   valb = valb;
 }
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  printf("VecShort3D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
    short val = 1;
   VecSet(&v4, j, val);
   short valb = VecGet(&v4, j);
   valb = valb;
 clockAfter = clock();
  timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
  short array4[4];
  for (; i--;) {
   int j = INT(rnd() * (3.0 - PBMATH_EPSILON));
   short val = 1;
   array4[j] = val;
    short valb = array4[j];
   valb = valb;
 7
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecShort4D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
    PBErrCatch(PBMathErr);
```

```
}
 VecFree(&v);
 free(array);
 printf("UnitTestSpeedVecShort OK\n");
void UnitTestVecShortToFloat() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 for (int i = 4; i--;) VecSet(&v4, i, i + 1);
 VecFloat* w = VecShortToFloat(v);
 VecFloat2D w2 = VecShortToFloat2D(&v2);
 VecFloat3D w3 = VecShortToFloat3D(&v3);
 VecPrint(w, stdout); printf("\n");
 VecPrint(&w2, stdout); printf("\n");
 VecPrint(&w3, stdout); printf("\n");
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecShortToFloat OK\n");
void UnitTestVecShortOp() {
 VecShort* v = VecShortCreate(5);
 VecShort2D v2 = VecShortCreateStatic2D();
 VecShort3D v3 = VecShortCreateStatic3D();
 VecShort4D v4 = VecShortCreateStatic4D();
 VecShort* w = VecShortCreate(5);
 VecShort2D w2 = VecShortCreateStatic2D();
 VecShort3D w3 = VecShortCreateStatic3D();
 VecShort4D w4 = VecShortCreateStatic4D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 short a[2] = \{-1, 2\};
 short b[5] = \{-2, -1, 0, 1, 2\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 4; i--;) VecSet(&v4, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
 for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
 for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
 VecShort* u = VecGetOp(v, a[0], w, a[1]);
 VecShort2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
 VecShort3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
 VecShort4D u4 = VecGetOp(&v4, a[0], &w4, a[1]);
 short checku[5] = \{8,5,2,-1,-4\};
 short checku2[2] = \{2,-1\};
 short checku3[3] = \{4,1,-2\};
 short checku4[4] = \{6,3,0,-3\};
 for (int i = 5; i--;)
   if (!ISEQUALF(VecGet(u, i), checku[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
     PBErrCatch(PBMathErr);
```

```
}
  for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
     PBErrCatch(PBMathErr);
   }
  for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
     PBErrCatch(PBMathErr);
 for (int i = 4; i--;)
    if (!ISEQUALF(VecGet(&u4, i), checku4[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
     PBErrCatch(PBMathErr);
  VecOp(v, a[0], w, a[1]);
  VecOp(&v2, a[0], &w2, a[1]);
 VecOp(&v3, a[0], &w3, a[1]);
VecOp(&v4, a[0], &w4, a[1]);
  if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v2, &u2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
   PBErrCatch(PBMathErr);
  if (!VecIsEqual(&v3, &u3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v4, &u4)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w):
  VecFree(&u);
 printf("UnitTestVecShortOp\ OK\n");\\
void UnitTestVecShortShiftStep() {
  VecShort3D v = VecShortCreateStatic3D();
  VecShort3D from = VecShortCreateStatic3D();
  VecShort3D to = VecShortCreateStatic3D();
  VecSet(&from, 0, 0);
 VecSet(&from, 1, 1);
 VecSet(&from, 2, 2);
  VecSet(&to, 0, 3);
  VecSet(&to, 1, 4);
  VecSet(&to, 2, 5);
  VecCopy(&v, &from);
  short check[81] = {
    0, 1, 2, 0, 1, 3, 0, 1, 4,
```

```
0, 2, 2, 0, 2, 3, 0, 2, 4,
   0, 3, 2, 0, 3, 3, 0, 3, 4,
    1, 1, 2, 1, 1, 3, 1, 1, 4,
   1, 2, 2, 1, 2, 3, 1, 2, 4,
   1, 3, 2, 1, 3, 3, 1, 3, 4,
    2, 1, 2, 2, 1, 3, 2, 1, 4,
    2, 2, 2, 2, 2, 3, 2, 2, 4,
    2, 3, 2, 2, 3, 3, 2, 3, 4
   };
  int iCheck = 0;
 do {
    for (int i = 0; i < 3; ++i) {
      if (ISEQUALF(check[iCheck], VecGet(&v, i)) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecShiftStep NOK");
       PBErrCatch(PBMathErr);
     ++iCheck;
 } while(VecShiftStep(&v, &from, &to));
 printf("UnitTestVecShortShiftStep OK\n");
void UnitTestVecShortGetMinMax() {
 VecShort3D v = VecShortCreateStatic3D();
 VecSet(&v, 0, 2); VecSet(&v, 1, 4); VecSet(&v, 2, 3);
  short val = VecGetMaxVal(&v);
 if (val != 4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinVal(&v);
  if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 2); VecSet(&v, 1, -4); VecSet(&v, 2, 3);
 val = VecGetMaxValAbs(&v);
  if (val != -4) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, -2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
 val = VecGetMinValAbs(&v);
 if (val != 1) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecShortGetMinMax OK\n");
void UnitTestVecShort() {
 UnitTestVecShortCreateFree();
 UnitTestVecShortClone();
 UnitTestVecShortLoadSave();
 UnitTestVecShortGetSetDim();
 UnitTestVecShortStep();
```

```
UnitTestVecShortHamiltonDist();
 UnitTestVecShortIsEqual();
  UnitTestVecShortDotProd();
 UnitTestVecShortCopy();
 UnitTestSpeedVecShort();
 UnitTestVecShortToFloat();
 UnitTestVecShortOp();
 UnitTestVecShortShiftStep();
 UnitTestVecShortGetMinMax();
 printf("UnitTestVecShort OK\n");
void UnitTestVecFloatCreateFree() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 VecPrint(v, stdout);printf("\n");
 VecPrint(&v2, stdout);printf("\n");
  VecPrint(&v3, stdout);printf("\n");
  VecFloatFree(&v);
  if (v != NULL) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecFloat is not null after _VecFloatFree");
   PBErrCatch(PBMathErr);
 printf("VecFloatCreateFree OK\n");
void UnitTestVecFloatClone() {
 VecFloat* v = VecFloatCreate(5);
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 VecFloat* w = VecClone(v);
 if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatClone NOK");
   PBErrCatch(PBMathErr);
  _VecFloatFree(&v);
  _VecFloatFree(&w);
 printf("_VecFloatClone OK\n");
void UnitTestVecFloatLoadSave() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 FILE* f = fopen("./UnitTestVecFloatLoadSave.txt", "w");
  if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecFloatLoadSave.txt for writing");
   PBErrCatch(PBMathErr);
 }
  if (!VecSave(v, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecSave(&v2, f)) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecSave(&v3, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFloat* w = VecFloatCreate(2);
 f = fopen("./UnitTestVecFloatLoadSave.txt", "r");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
   sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestVecFloatLoadSave.txt for reading");
   PBErrCatch(PBMathErr);
 }
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(\&v2, w, sizeof(VecFloat) + sizeof(float) * 2) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
   PBErrCatch(PBMathErr);
 if (!VecLoad(&w, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
   PBErrCatch(PBMathErr);
 if (memcmp(\&v3, w, sizeof(VecFloat) + sizeof(float) * 3) != 0) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 VecFree(&v);
 int ret = system("cat ./UnitTestVecFloatLoadSave.txt");
 printf("_VecFloatLoadSave OK\n");
 ret = system("rm ./UnitTestVecFloatLoadSave.txt");
 ret = ret;
void UnitTestVecFloatGetSetDim() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 if (VecGetDim(v) != 5) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
  sprintf(PBMathErr->_msg, "_VecFloatGetDim NOK");
  PBErrCatch(PBMathErr);
for (int i = 5; i--;) VecSet(v, i, (float)(i + 1));
for (int i = 2; i--;) VecSet(\&v2, i, (float)(i + 1));
for (int i = 3; i--;) VecSet(&v3, i, (float)(i + 1));
for (int i = 5; i--;)
 if (!ISEQUALF(v->_val[i], (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(v2._val[i], (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 3; i--;)
  if (!ISEQUALF(v3._val[i], (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
   PBErrCatch(PBMathErr);
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(v, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
 }
for (int i = 3; i--;)
  if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
VecSetNull(v);
VecSetNull(&v2):
VecSetNull(&v3);
for (int i = 5; i--;)
  if (!ISEQUALF(VecGet(v, i), 0.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
for (int i = 2; i--;)
  if (!ISEQUALF(VecGet(&v2, i), 0.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
   PBErrCatch(PBMathErr);
 7
for (int i = 3; i--;)
  if (!ISEQUALF(VecGet(&v3, i), 0.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
```

```
PBErrCatch(PBMathErr);
   }
 VecFree(&v);
 printf("\_VecFloatGetSetDim OK\n");
void UnitTestVecFloatCopy() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
 VecCopy(w, v);
 VecCopy(&w2, &v2);
 VecCopy(&w3, &v3);
 if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w):
 printf("UnitTestVecFloatCopy OK\n");
void UnitTestVecFloatNorm() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 if (!ISEQUALF(VecNorm(v), 7.416198)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecNorm(&v2), 2.236068)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecNorm(&v3), 3.741657)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
   PBErrCatch(PBMathErr);
 VecNormalise(v);
```

```
VecNormalise(&v2);
  VecNormalise(&v3);
  if (!ISEQUALF(VecNorm(v), 1.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(&v2), 1.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
    PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecNorm(&v3), 1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 printf("UnitTestVecFloatNorm OK\n");
void UnitTestVecFloatDist() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
 VecFloat* w = VecFloatCreate(5);
  VecFloat2D w2 = VecFloatCreateStatic2D();
  VecFloat3D w3 = VecFloatCreateStatic3D();
  float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
  for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
  for (int i = 2; i--;) VecSet(\&w2, i, b[1 - i] + 1.5);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
  if (!ISEQUALF(VecDist(v, w), 7.158911)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecDist(&v2, &w2), 2.549510)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecDist(&v3, &w3), 3.840573)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecHamiltonDist(v, w), 13.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
   PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecHamiltonDist(&v2, &w2), 3.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
    PBErrCatch(PBMathErr);
  if (!ISEQUALF(VecHamiltonDist(&v3, &w3), 5.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(v, w), 13.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(&v2, &w2), 2.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 if (!ISEQUALF(VecPixelDist(&v3, &w3), 5.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w):
 printf("UnitTestVecFloatDist OK\n");
void UnitTestVecFloatIsEqual() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
 if (VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (VecIsEqual(&v3, &w3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
 for (int i = 5; i--;) VecSet(w, i, i + 1);
 for (int i = 2; i--;) VecSet(&w2, i, i + 1);
 for (int i = 3; i--;) VecSet(&w3, i, i + 1);
 if (!VecIsEqual(v, w)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &w2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &w3)) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
    PBErrCatch(PBMathErr);
 VecFree(&v);
 VecFree(&w);
 printf("UnitTestVecFloatIsEqual OK\n");
void UnitTestVecFloatScale() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 float a = 0.1;
 VecFloat* w = VecGetScale(v, a);
  VecFloat2D w2 = VecGetScale(&v2, a);
  VecFloat3D w3 = VecGetScale(&v3, a);
  VecScale(v, a);
  VecScale(&v2, a);
 VecScale(&v3, a);
  for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(w, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
     PBErrCatch(PBMathErr);
 for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(\&w2, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
     PBErrCatch(PBMathErr);
 for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&w3, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
     PBErrCatch(PBMathErr);
  for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
   }
  for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
   }
 for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1) * a)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
     PBErrCatch(PBMathErr);
   }
  VecFree(&v);
  VecFree(&w);
  printf("UnitTestVecFloatScale OK\n");
```

```
void UnitTestVecFloatOp() {
 VecFloat* v = VecFloatCreate(5);
 VecFloat2D v2 = VecFloatCreateStatic2D();
 VecFloat3D v3 = VecFloatCreateStatic3D();
 VecFloat* w = VecFloatCreate(5);
 VecFloat2D w2 = VecFloatCreateStatic2D();
 VecFloat3D w3 = VecFloatCreateStatic3D();
 for (int i = 5; i--;) VecSet(v, i, i + 1);
 for (int i = 2; i--;) VecSet(&v2, i, i + 1);
 for (int i = 3; i--;) VecSet(&v3, i, i + 1);
 float a[2] = \{-0.1, 2.0\};
 float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
 for (int i = 5; i--;) VecSet(v, i, b[i]);
 for (int i = 2; i--;) VecSet(&v2, i, b[i]);
 for (int i = 3; i--;) VecSet(&v3, i, b[i]);
 for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 0.5);
 for (int i = 2; i--;) VecSet(\&w2, i, b[1 - i] + 0.5);
 for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 0.5);
 VecFloat* u = VecGetOp(v, a[0], w, a[1]);
 VecFloat2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
 VecFloat3D u3 = VecGet0p(&v3, a[0], &w3, a[1]);
 float checku[5] = \{5.2,3.1,1.0,-1.1,-3.2\};
 float checku2[2] = \{-0.8, -2.9\};
 float checku3[3] = \{1.2,-0.9,-3.0\};
 for (int i = 5; i--;)
   if (!ISEQUALF(VecGet(u, i), checku[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
 for (int i = 2; i--;)
   if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
 for (int i = 3; i--;)
   if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
     PBErrCatch(PBMathErr);
 VecOp(v, a[0], w, a[1]);
 VecOp(&v2, a[0], &w2, a[1]);
 VecOp(&v3, a[0], &w3, a[1]);
 if (!VecIsEqual(v, u)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v2, &u2)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(&v3, &u3)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
   sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
   PBErrCatch(PBMathErr);
```

```
VecFree(&v);
  VecFree(&w);
  VecFree(&u);
  printf("UnitTestVecFloatOp OK\n");
void UnitTestVecFloatDotProd() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  VecFloat* w = VecFloatCreate(5);
  VecFloat2D w2 = VecFloatCreateStatic2D();
  VecFloat3D w3 = VecFloatCreateStatic3D();
  float b[5] = \{-2.0, -1.0, 0.0, 1.0, 2.0\};
  for (int i = 5; i--;) VecSet(v, i, b[i]);
  for (int i = 2; i--;) VecSet(&v2, i, b[i]);
  for (int i = 3; i--;) VecSet(&v3, i, b[i]);
  for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
  for (int i = 2; i--;) VecSet(\&w2, i, b[1 - i] + 1.5);
  for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
  float prod = VecDotProd(v, w);
  if (!ISEQUALF(prod, -10.0)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
  prod = VecDotProd(&v2, &w2);
  if (!ISEQUALF(prod, -0.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
  prod = VecDotProd(&v3, &w3);
  if (!ISEQUALF(prod, -3.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecFloatDotProd OK\n");
void UnitTestVecFloatRotAngleTo() {
  VecFloat* v = VecFloatCreate(2):
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat* w = VecFloatCreate(2);
  VecFloat2D w2 = VecFloatCreateStatic2D();
  VecSet(v, 0, 1.0);
  VecSet(&v2, 0, 1.0);
  VecSet(w, 0, 1.0);
  VecSet(&w2, 0, 1.0);
  float a = 0.0;
  float da = PBMATH_TWOPI_DIV_360;
  for (int i = 360; i--;) {
    VecRot(v, da);
    VecNormalise(v);
    VecRot(&v2, da);
    VecNormalise(&v2);
    a += da;
    if (ISEQUALF(a, PBMATH_PI)) {
      a = -PBMATH_PI;
```

```
if (!ISEQUALF(fabs(VecAngleTo(w, v)), fabs(a))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
      if (!ISEQUALF(fabs(VecAngleTo(&w2, &v2)), fabs(a))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
    } else {
      if (!ISEQUALF(VecAngleTo(w, v), a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
      if (!ISEQUALF(VecAngleTo(&w2, &v2), a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
        PBErrCatch(PBMathErr);
   }
  }
  VecSet(v, 0, 1.0);
  VecSet(v, 1, 0.0);
VecRot(v, PBMATH_QUARTERPI);
  if (!ISEQUALF(VecGet(v, 0), 0.70711) ||
    ! ISEQUALF(VecGet(v, 1), 0.70711)) \ \{
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatRot NOK");
    PBErrCatch(PBMathErr);
  VecFree(&v);
  VecFree(&w);
 printf("UnitTestVecFloatAngleTo OK\n");
void UnitTestVecFloatToShort() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  for (int i = 5; i--;) VecSet(v, i, i + 1);
  for (int i = 2; i--;) VecSet(&v2, i, i + 1);
  for (int i = 3; i--;) VecSet(&v3, i, i + 1);
  VecShort* w = VecFloatToShort(v);
  VecShort2D w2 = VecFloatToShort2D(&v2);
  VecShort3D w3 = VecFloatToShort3D(&v3);
  VecPrint(w, stdout); printf("\n");
  VecPrint(&w2, stdout); printf("\n");
  \label{lem:vecPrint(&w3, stdout); printf("\n");} VecPrint(\&w3, stdout); printf("\n");
  VecFree(&v);
  VecFree(&w):
  printf("UnitTestVecFloatToShort OK\n");
void UnitTestSpeedVecFloat() {
  VecFloat* v = VecFloatCreate(5);
  VecFloat2D v2 = VecFloatCreateStatic2D();
  VecFloat3D v3 = VecFloatCreateStatic3D();
  int nbTest = 100000;
  srandom(RANDOMSEED);
```

```
int i = nbTest;
  clock_t clockBefore = clock();
  for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
    float val = 1.0;
   VecSet(v, j, val);
float valb = VecGet(v, j);
    valb = valb;
 }
 clock_t clockAfter = clock();
 double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
  float* array = malloc(sizeof(float) * 5);
 for (; i--;) {
   int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
    float val = 1.0;
   array[j] = val;
   float valb = array[j];
   valb = valb;
 }
 clockAfter = clock();
 double timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecFloat: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
 if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
    float val = 1.0;
   VecSet(&v2, j, val);
float valb = VecGet(&v2, j);
   valb = valb;
 }
  clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
 i = nbTest;
 clockBefore = clock();
 float array2[2];
 for (; i--;) {
   int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
   float val = 1.0;
   array2[j] = val;
    float valb = array2[j];
   valb = valb;
 clockAfter = clock();
```

```
timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecFloat2D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
   PBErrCatch(PBMathErr);
 srandom(RANDOMSEED);
 i = nbTest;
  clockBefore = clock();
 for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
    float val = 1.0;
    VecSet(&v3, j, val);
    float valb = VecGet(&v3, j);
   valb = valb;
 }
 clockAfter = clock();
 timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  srandom(RANDOMSEED);
  i = nbTest;
 clockBefore = clock();
 float array3[3];
 for (; i--;) {
   int j = INT(rnd() * (2.0 - PBMATH_EPSILON));
   float val = 1.0;
    array3[j] = val;
    float valb = array3[j];
   valb = valb;
 }
 clockAfter = clock();
 timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 printf("VecFloat3D: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
  if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
   PBErrCatch(PBMathErr);
 VecFree(&v);
 free(array):
 printf("UnitTestSpeedVecFloat OK\n");
void UnitTestVecFloatRotAxis() {
 VecFloat3D v = VecFloatCreateStatic3D();
 VecSet(&v, 0, 1.0); VecSet(&v, 1, 0.0); VecSet(&v, 2, 1.0);
 VecFloat3D axis = VecFloatCreateStatic3D();
 VecSet(&axis, 0, 1.0); VecSet(&axis, 1, 1.0); VecSet(&axis, 2, 1.0);
 VecNormalise(&axis);
 float theta = PBMATH_PI;
```

```
VecRotAxis(&v, &axis, theta);
  if (!ISEQUALF(VecGet(&v, 0), 0.333333) ||
    !ISEQUALF(VecGet(&v, 1), 1.333333) ||
    !ISEQUALF(VecGet(&v, 2), 0.333333)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotAxis NOK");
    PBErrCatch(PBMathErr);
  theta = PBMATH_HALFPI;
  VecRotAxis(&v, &axis, theta);
  if (!ISEQUALF(VecGet(&v, 0), 0.089316) ||
    !ISEQUALF(VecGet(&v, 1), 0.666666) ||
!ISEQUALF(VecGet(&v, 2), 1.244017)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotAxis NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotX(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), 1.0) |
    !ISEQUALF(VecGet(&v, 1), -1.0) ||
    !ISEQUALF(VecGet(&v, 2), -1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotX NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotY(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
     !ISEQUALF(VecGet(&v, 1), 1.0) ||
    !ISEQUALF(VecGet(&v, 2), -1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecRotY NOK");
    PBErrCatch(PBMathErr);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
  theta = PBMATH_PI;
  VecRotZ(&v, theta);
  if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
    !ISEQUALF(VecGet(&v, 1), -1.0) ||
    !ISEQUALF(VecGet(&v, 2), 1.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
sprintf(PBMathErr->_msg, "VecRotZ NOK");
    PBErrCatch(PBMathErr);
printf("UnitTestVecFloatRotAxis OK\n");
}
void UnitTestVecFloatGetMinMax() {
  VecFloat2D v = VecFloatCreateStatic2D();
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 2.0);
  float val = VecGetMaxVal(&v);
  if (ISEQUALF(val, 2.0) == false) {}
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
    PBErrCatch(PBMathErr);
  val = VecGetMinVal(&v);
  if (ISEQUALF(val, 1.0) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
   PBErrCatch(PBMathErr);
 VecSet(&v, 0, 1.0); VecSet(&v, 1, -2.0);
  val = VecGetMaxValAbs(&v);
  if (ISEQUALF(val, -2.0) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
   PBErrCatch(PBMathErr);
 val = VecGetMinValAbs(&v);
 if (ISEQUALF(val, 1.0) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
   PBErrCatch(PBMathErr);
 printf("UnitTestVecFloatGetMinMax OK\n");
void UnitTestVecFloat() {
 UnitTestVecFloatCreateFree();
 UnitTestVecFloatClone();
 UnitTestVecFloatLoadSave();
 UnitTestVecFloatGetSetDim();
 UnitTestVecFloatCopy();
 UnitTestVecFloatNorm();
  UnitTestVecFloatDist();
 UnitTestVecFloatIsEqual();
 UnitTestVecFloatScale();
 UnitTestVecFloatOp();
 UnitTestVecFloatDotProd();
 UnitTestVecFloatRotAngleTo();
 UnitTestVecFloatToShort();
 UnitTestVecFloatGetMinMax();
 UnitTestVecFloatRotAxis();
 UnitTestSpeedVecFloat();
 printf("UnitTestVecFloat OK\n");
void UnitTestMatFloatCreateFree() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 for (int i = VecGet(&dim, 0) * VecGet(&dim, 1);i--;) {
    if (!ISEQUALF(mat->_val[i], 0.0)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatCreateFree NOK");
     PBErrCatch(PBMathErr);
   }
 MatFree(&mat);
  if (mat != NULL) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "mat is not null after MatFree");
   PBErrCatch(PBMathErr);
 printf("UnitTestMatFloatCreateFree OK\n");
void UnitTestMatFloatGetSetDim() {
 VecShort2D dim = VecShortCreateStatic2D();
```

```
VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
 if (!VecIsEqual(&(mat->_dim), &dim)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
   PBErrCatch(PBMathErr);
 if (!VecIsEqual(MatDim(mat), &dim)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
   PBErrCatch(PBMathErr);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
   MatSet(mat, &i, v);
    v += 1.0;
 } while(VecStep(&i, &dim));
  v = 1.0:
 for (int j = 0; j < VecGet(\&dim, 0); ++j) {
   for (int k = 0; k < VecGet(\&dim, 1); ++k) {
     if (!ISEQUALF(mat->_val[k * VecGet(&dim, 0) + j], v)) {
       PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
       PBErrCatch(PBMathErr);
     }
     v += 1.0;
   }
 VecSetNull(&i);
 v = 1.0;
 do {
   float w = MatGet(mat, &i);
    if (!ISEQUALF(v, w)) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
     PBErrCatch(PBMathErr);
   }
    v += 1.0;
 } while(VecStep(&i, &dim));
 MatFree(&mat);
 printf("UnitTestMatFloatGetSetDim OK\n");
void UnitTestMatFloatCloneIsEqual() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
   MatSet(mat, &i, v);
   v += 1.0;
  } while(VecStep(&i, &dim));
 MatFloat* clone = MatClone(mat);
  if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
   PBErrCatch(PBMathErr);
```

```
VecSetNull(&i);
  do {
    if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
     PBErrCatch(PBMathErr);
  } while(VecStep(&i, &dim));
  if (MatIsEqual(mat, clone) == false) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK1");
   PBErrCatch(PBMathErr);
 VecSet(&i, 0, 0); VecSet(&i, 1, 0);
 MatSet(clone, &i, -1.0);
  if (MatIsEqual(mat, clone) == true) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK2");
   PBErrCatch(PBMathErr);
 MatFree(&mat);
 MatFree(&clone);
 printf("UnitTestMatFloatCloneIsEqual OK\n");
void UnitTestMatFloatLoadSave() {
  VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
   MatSet(mat, &i, v);
    v += 1.0;
  } while(VecStep(&i, &dim));
 FILE* f = fopen("./UnitTestMatFloatLoadSave.txt", "w");
  if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestMatFloatLoadSave.txt for writing");
   PBErrCatch(PBMathErr);
 if (!MatSave(mat, f)) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_MatFloatSave NOK");
   PBErrCatch(PBMathErr);
 fclose(f);
 MatFloat* clone = MatFloatCreate(&dim);
  f = fopen("./UnitTestMatFloatLoadSave.txt", "r");
 if (f == NULL) {
   PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
      "Can't open ./UnitTestMatFloatLoadSave.txt for reading");
   PBErrCatch(PBMathErr);
  if (!MatLoad(&clone, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_MatFloatLoad NOK");
   PBErrCatch(PBMathErr);
```

```
if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
    PBErrCatch(PBMathErr);
  }
  VecSetNull(&i);
  do {
    if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
      PBErrCatch(PBMathErr);
  } while(VecStep(&i, &dim));
  fclose(f);
  MatFree(&mat);
  MatFree(&clone);
  int ret = system("cat ./UnitTestMatFloatLoadSave.txt");
  ret = system("rm ./UnitTestMatFloatLoadSave.txt");
 printf("UnitTestMatFloatLoadSave OK\n");
}
void UnitTestMatFloatInv() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  VecShort2D i = VecShortCreateStatic2D();
  float v[9] = \{3.0, 2.0, 0.0, 0.0, 0.0, 1.0, 2.0, -2.0, 1.0\};
  int j = 0;
  do {
    MatSet(mat, &i, v[j]);
   ++j;
  } while(VecStep(&i, &dim));
  MatFloat* inv = MatInv(mat);
  float w[9] = \{0.2, -0.2, 0.2, 0.2, 0.3, -0.3, 0.0, 1.0, 0.0\};
  VecSetNull(&i);
  j = 0;
  do {
    if (!ISEQUALF(MatGet(inv, &i), w[j])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK");
      PBErrCatch(PBMathErr);
    }
    ++j;
  } while(VecStep(&i, &dim));
  MatFree(&mat);
  MatFree(&inv);
  VecSet(&dim, 0, 2);
  VecSet(&dim, 1, 2);
  mat = MatFloatCreate(&dim);
  float vb[4] = \{4.0, 2.0, 7.0, 6.0\};
  VecSetNull(&i);
  j = 0;
  do {
    MatSet(mat, &i, vb[j]);
    ++j;
  } while(VecStep(&i, &dim));
  inv = MatInv(mat);
  float wb[4] = \{0.6, -0.2, -0.7, 0.4\};
  VecSetNull(&i);
  j = 0;
```

```
do {
   if (!ISEQUALF(MatGet(inv, &i), wb[j])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK");
     PBErrCatch(PBMathErr);
   }
   ++j;
 } while(VecStep(&i, &dim));
 MatFree(&mat);
 MatFree(&inv);
 printf("UnitTestMatFloatInv OK\n");
void UnitTestMatFloatProdVecFloat() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
   MatSet(mat, &i, v);
   v += 1.0;
 } while(VecStep(&i, &dim));
  VecFloat2D u = VecFloatCreateStatic2D();
  for (int j = 2; j--;)
    VecSet(&u, j, (float)j + 1.0);
  VecFloat* w = MatGetProdVec(mat, &u);
 float b[3] = \{9.0, 12.0, 15.0\};
 for (int j = 3; j--;) {
    if (!ISEQUALF(VecGet(w, j), b[j])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "UnitTestMatFloatProdVecFloat NOK");
     PBErrCatch(PBMathErr);
 MatFree(&mat);
 VecFree(&w);
 printf("UnitTestMatFloatProdVecFloat OK\n");
void UnitTestMatFloatProdMatFloat() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 3);
 VecSet(&dim, 1, 2);
 MatFloat* mat = MatFloatCreate(&dim);
 VecShort2D i = VecShortCreateStatic2D();
 float v = 1.0;
 do {
   MatSet(mat, &i, v);
   v += 1.0;
  } while(VecStep(&i, &dim));
  VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 3);
 MatFloat* matb = MatFloatCreate(&dim);
 VecSetNull(&i);
 v = 1.0;
 do {
   MatSet(matb, &i, v);
   v += 1.0;
 } while(VecStep(&i, &dim));
 MatFloat* matc = MatGetProdMat(mat, matb);
```

```
float w[4] = \{22.0, 28.0, 49.0, 64.0\};
 VecSetNull(&i);
  int j = 0;
 VecSet(&dim, 0, 2);
 VecSet(&dim, 1, 2);
  if (!VecIsEqual(&dim, &(matc->_dim))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
   PBErrCatch(PBMathErr);
 do {
   if (!ISEQUALF(MatGet(matc, &i), w[j])) {
     PBMathErr->_type = PBErrTypeUnitTestFailed;
     sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
     PBErrCatch(PBMathErr);
   }
   ++j;
 } while(VecStep(&i, &dim));
 MatFree(&mat);
 MatFree(&matb):
 MatFree(&matc);
 printf("UnitTestMatFloatProdMatFloat OK\n");
void UnitTestSpeedMatFloat() {
 VecShort2D dim = VecShortCreateStatic2D();
 VecSet(&dim, 0, 3);
 VecSet(&dim, 1, 3);
 MatFloat* mat = MatFloatCreate(&dim);
 int nbTest = 100000;
 srandom(RANDOMSEED);
 int i = nbTest;
 clock_t clockBefore = clock();
 VecShort2D j = VecShortCreateStatic2D();
 for (; i--;) {
   float val = 1.0;
   MatSet(mat, &j, val);
   float valb = MatGet(mat, &j);
   valb = valb;
   VecStep(&j, &dim);
 clock_t clockAfter = clock();
  double timeV = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
 srandom(RANDOMSEED):
  i = nbTest;
 clockBefore = clock();
 float* array = malloc(sizeof(float) * 9);
 short *ptr = j._val;
 for (; i--;) {
   float val = 1.0;
   int k = ptr[1] * 3 + ptr[0];
   array[k] = val;
   float valb = array[k];
   valb = valb;
   VecStep(&j, &dim);
  clockAfter = clock();
  double timeRef = ((double)(clockAfter - clockBefore)) /
   CLOCKS_PER_SEC * 1000.0;
  printf("MatFloat: %fms, array: %fms\n",
   timeV / (float)nbTest, timeRef / (float)nbTest);
```

```
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
   PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedMatFloat NOK");
    PBErrCatch(PBMathErr);
  MatFree(&mat);
  free(array);
 printf("UnitTestSpeedMatFloat OK\n");
void UnitTestMatFloat() {
  UnitTestMatFloatCreateFree();
  UnitTestMatFloatGetSetDim();
  UnitTestMatFloatCloneIsEqual();
  UnitTestMatFloatLoadSave();
  UnitTestMatFloatInv();
  UnitTestMatFloatProdVecFloat():
  UnitTestMatFloatProdMatFloat();
  UnitTestSpeedMatFloat();
 printf("UnitTestMatFloat OK\n");
void UnitTestSysLinEq() {
  VecShort2D dim = VecShortCreateStatic2D();
  VecSet(&dim, 0, 3);
  VecSet(&dim, 1, 3);
  MatFloat* mat = MatFloatCreate(&dim);
  float a[9] = \{2.0, 2.0, 6.0, 1.0, 6.0, 8.0, 3.0, 8.0, 18.0\};
  VecShort2D index = VecShortCreateStatic2D();
  int j = 0;
  do {
   MatSet(mat, &index, a[j]);
    ++j;
  } while(VecStep(&index, &dim));
  VecFloat3D v = VecFloatCreateStatic3D();
  float b[3] = \{1.0, 3.0, 5.0\};
  for (int i = 3; i--;)
   VecSet(&v, i, b[i]);
  SysLinEq* sys = SysLinEqCreate(mat, &v);
  VecFloat* res = SysLinEqSolve(sys);
  float c[3] = {0.3, 0.4, 0};
  for (int i = 3; i--;) {
    if (!ISEQUALF(c[i], VecGet(res, i))) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
      PBErrCatch(PBMathErr);
  float ab[9] = \{3.0, 2.0, -1.0, 2.0, -2.0, 0.5, -1.0, 4.0, -1.0\};
  VecSetNull(&index);
  j = 0;
  do {
    MatSet(mat, &index, ab[j]);
    ++j;
  } while(VecStep(&index, &dim));
  SysLinEqSetM(sys, mat);
  float bb[3] = \{1.0, -2.0, 0.0\};
  for (int i = 3; i--;)
    VecSet(&v, i, bb[i]);
```

```
SysLinEqSetV(sys, &v);
  VecFree(&res);
  res = SysLinEqSolve(sys);
  float cb[3] = \{1.0, -2.0, -2.0\};
  for (int i = 3; i--;) {
    if (!ISEQUALF(cb[i], VecGet(res, i))) {
   PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
      PBErrCatch(PBMathErr);
   }
  }
  VecFree(&res);
  SysLinEqFree(&sys);
  if (sys != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "sys is not null after free");
    PBErrCatch(PBMathErr);
  MatFree(&mat);
 printf("UnitTestSysLinEq OK\n");
void UnitTestGauss() {
  srandom(RANDOMSEED);
  float mean = 1.0;
  float sigma = 0.5;
  Gauss *gauss = GaussCreate(mean, sigma);
  if (!ISEQUALF(gauss->_mean, mean) ||
    !ISEQUALF(gauss->_sigma, sigma)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussCreate NOK");
   PBErrCatch(PBMathErr);
  float a[22] = {0.000268, 0.001224, 0.004768, 0.015831, 0.044789,
    0.107982, 0.221842, 0.388372, 0.579383, 0.736540, 0.797885,
    0.736540, 0.579383, 0.388372, 0.221842, 0.107982, 0.044789,
    0.015831, 0.004768, 0.001224, 0.000268};
  for (int i = -5; i \le 15; ++i) {
    if (!ISEQUALF(GaussGet(gauss, (float)i * 0.2), a[i + 5])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestGaussGet NOK");
      PBErrCatch(PBMathErr);
  }
  int nbsample = 1000000;
  double sum = 0.0;
  double sumsquare = 0.0;
  for (int i = nbsample; i--;) {
   float v = GaussRnd(gauss);
    sum += v;
    sumsquare += fsquare(v);
  double avg = sum / (double)nbsample;
  double sig = sqrtf(sumsquare / (double)nbsample - fsquare(avg));
  if (fabs(avg - mean) > 0.001 | |
    fabs(sig - sigma) > 0.001) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussRnd NOK");
    PBErrCatch(PBMathErr);
  GaussFree(&gauss);
  if (gauss != NULL) {
```

```
PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "gauss is not null after free");
    PBErrCatch(PBMathErr);
 printf("UnitTestGauss OK\n");
void UnitTestSmoother() {
  float smooth[11] = {0.0, 0.028, 0.104, 0.216, 0.352, 0.5, 0.648,
    0.784, 0.896, 0.972, 1.0};
  float smoother[11] = {0.0, 0.00856, 0.05792, 0.16308, 0.31744, 0.5,
    0.68256, 0.83692, 0.94208, 0.99144, 1.0};
  for (int i = 0; i <= 10; ++i) {
    if (!ISEQUALF(SmoothStep((float)i * 0.1), smooth[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestSmooth NOK");
      PBErrCatch(PBMathErr);
    if (!ISEQUALF(SmootherStep((float)i * 0.1), smoother[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestSmoother NOK");
      PBErrCatch(PBMathErr);
    }
  }
 printf("UnitTestSmoother OK\n");
void UnitTestConv() {
  float rad[5] = {0.0, PBMATH_TWOPI, PBMATH_PI, PBMATH_HALFPI, 3.0 * PBMATH_HALFPI};
  float deg[5] = \{0.0, 360.0, 180.0, 90.0, 270.0\};
  for (int i = 5; i--;) {
    if (!ISEQUALF(ConvRad2Deg(rad[i]), deg[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestConvRad2Deg NOK");
      PBErrCatch(PBMathErr);
    if (!ISEQUALF(ConvDeg2Rad(deg[i]), rad[i])) {
      PBMathErr->_type = PBErrTypeUnitTestFailed;
      sprintf(PBMathErr->_msg, "UnitTestConvDeg2Rad NOK");
      PBErrCatch(PBMathErr);
printf("UnitTestConv OK\n");
}
void UnitTestBasicFunctions() {
  UnitTestConv();
  UnitTestPowi();
  UnitTestFastPow();
  UnitTestSpeedFastPow();
  UnitTestFSquare();
  UnitTestConv();
  printf("UnitTestBasicFunctions OK\n");
void UnitTestAll() {
  UnitTestVecShort();
  UnitTestVecFloat();
  UnitTestMatFloat();
  UnitTestSysLinEq();
  UnitTestGauss();
  UnitTestSmoother();
```

```
UnitTestBasicFunctions();
printf("UnitTestAll OK\n");
}
int main() {
  UnitTestAll();
  // Return success code
  return 0;
}
```

# 6 Unit tests output

```
5 1 2 3 4 5
2 1 2
3 1 2 3
4 1 2 3 4
5 1.000000 2.000000 3.000000 4.000000 5.000000
2 1.000000 2.000000
3 1.000000 2.000000 3.000000
1.000000 4.000000
2.000000 5.000000
3.000000 6.000000
<0,0,0,0,0>
<0,0>
<0,0,0>
<0,0,0,0>
VecShortCreateFree OK
_VecShortClone OK
_VecShortLoadSave OK
_VecShortGetSetDim OK
UnitTestVecShortStep OK
UnitTestVecShortHamiltonDist OK
UnitTestVecShortIsEqual OK
UnitTestVecShortDotProd OK
UnitTestVecShortCopy OK
VecShort: 0.000031ms, array: 0.000033ms
VecShort2D: 0.000014ms, array: 0.000014ms
VecShort3D: 0.000014ms, array: 0.000014ms
VecShort4D: 0.000012ms, array: 0.000013ms
UnitTestSpeedVecShort OK
<1.000,2.000,3.000,4.000,5.000>
<1.000,2.000>
<1.000,2.000,3.000>
UnitTestVecShortToFloat OK
UnitTestVecShortOp OK
UnitTestVecShortShiftStep OK
{\tt UnitTestVecShortGetMinMax\ OK}
UnitTestVecShort OK
<0.000,0.000,0.000,0.000,0.000>
<0.000,0.000>
<0.000,0.000,0.000>
VecFloatCreateFree OK
_VecFloatClone OK
_VecFloatLoadSave OK
_{	t VecFloatGetSetDim\ OK}
UnitTestVecFloatCopy OK
UnitTestVecFloatNorm OK
```

```
UnitTestVecFloatDist OK
{\tt UnitTestVecFloatIsEqual\ OK}
UnitTestVecFloatScale OK
UnitTestVecFloatOp OK
{\tt UnitTestVecFloatDotProd\ OK}
UnitTestVecFloatAngleTo OK
<1,2,3,4,5>
<1,2>
<1,2,3>
{\tt UnitTestVecFloatToShort\ OK}
UnitTestVecFloatGetMinMax OK
UnitTestVecFloatRotAxis OK
VecFloat: 0.000029ms, array: 0.000029ms
VecFloat2D: 0.000016ms, array: 0.000014ms
VecFloat3D: 0.000013ms, array: 0.000013ms
UnitTestSpeedVecFloat OK
UnitTestVecFloat OK
UnitTestMatFloatCreateFree OK
UnitTestMatFloatGetSetDim OK
UnitTestMatFloatCloneIsEqual OK
UnitTestMatFloatLoadSave OK
UnitTestMatFloatInv OK
UnitTestMatFloatProdVecFloat OK
{\tt UnitTestMatFloatProdMatFloat\ OK}
MatFloat: 0.000006ms, array: 0.000006ms
{\tt UnitTestSpeedMatFloat\ OK}
UnitTestMatFloat OK
UnitTestSysLinEq OK
{\tt UnitTestGauss} \ {\tt OK}
UnitTestSmoother OK
UnitTestConv OK
powi OK
average error: 0.000000 < 0.000010, max error: 0.000000 < 0.000100
fastpow OK
fastpow: 0.000024ms, pow: 0.000075ms
speed fastpow OK
fsquare OK
UnitTestConv OK
UnitTestBasicFunctions OK
UnitTestAll OK
```

## 7 Examples

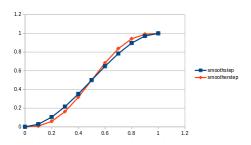
```
vecshort.txt:

3 0 1 0
    vecfloat.txt:

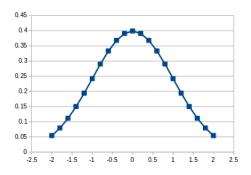
3 0.000000 1.000000 0.000000
    matfloat.txt:

3 2
    0.500000 2.000000 0.000000
2.000000 0.000000 1.000000
```

#### smoother functions:



## gauss function (mean:0.0, sigma:1.0):



## gauss rand function (mean:1.0, sigma:0.5):

