

# PBMath

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## Introduction

PBMath is a C library providing mathematical structures and functions.

The **VecFloat** structure and its functions can be used to manipulate vectors of float values.

The **VecShort** structure and its functions can be used to manipulate vectors of short values.

The **MatFloat** structure and its functions can be used to manipulate matrices of float values.

The **Gauss** structure and its functions can be used to get values of the Gauss function and random values distributed accordingly with a Gauss distribution.

The **Smoother** functions can be used to get values of the SmoothStep and SmootherStep functions.

The **EqLinSys** structure and its functions can be used to solve systems of linear equation.

The **Ratio** structure and its functions can be used to manipulate rationals.

It uses the **PBErr** library.

# 1 Definitions

## 1.1 Vector

### 1.1.1 Distance between two vectors

For **VecShort**:

$$\begin{aligned} Dist(\vec{v}, \vec{w}) &= \sum_i |v_i - w_i| \\ HamiltonDist(\vec{v}, \vec{w}) &= \sum_i |v_i - w_i| \\ PixelDist(\vec{v}, \vec{w}) &= \sum_i |v_i - w_i| \end{aligned} \tag{1}$$

For **VecFloat**:

$$\begin{aligned} Dist(\vec{v}, \vec{w}) &= \sum_i (v_i - w_i)^2 \\ HamiltonDist(\vec{v}, \vec{w}) &= \sum_i |v_i - w_i| \\ PixelDist(\vec{v}, \vec{w}) &= \sum_i |\lfloor v_i \rfloor - \lfloor w_i \rfloor| \end{aligned} \tag{2}$$

### 1.1.2 Angle between two vectors

The problem is as follow: given two vectors  $\vec{V}$  and  $\vec{W}$  not null, how to calculate the angle  $\theta$  from  $\vec{V}$  to  $\vec{W}$ .

Let's call  $M$  the rotation matrix:  $M\vec{V} = \vec{W}$ , and the components of  $M$  as follow:

$$M = \begin{bmatrix} Ma & Mb \\ Mc & Md \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \quad (3)$$

Then,  $M\vec{V} = \vec{W}$  can be written has

$$\begin{cases} W_x = M_a V_x + M_b V_y \\ W_y = M_c V_x + M_d V_y \end{cases} \quad (4)$$

Equivalent to

$$\begin{cases} W_x = M_a V_x + M_b V_y \\ W_y = -M_b V_x + M_a V_y \end{cases} \quad (5)$$

where  $M_a = \cos(\theta)$  and  $M_b = -\sin(\theta)$ .

If  $V_x \neq 0.0$ , we can write

$$\begin{cases} M_b = \frac{M_a V_y - W_y}{V_x} \\ M_a = \frac{W_x + W_y V_y / V_x}{V_x + V_y^2 / V_x} \end{cases} \quad (6)$$

Or, if  $V_x = 0.0$ , we can write

$$\begin{cases} Ma = \frac{W_y + M_b V_x}{V_y} \\ Mb = \frac{W_x - W_y V_x / V_y}{V_y + V_x^2 / V_y} \end{cases} \quad (7)$$

Then we have  $\theta = \pm \cos^{-1}(M_a)$  where the sign can be determined by verifying that the sign of  $\sin(\theta)$  matches the sign of  $-M_b$ : if  $\sin(\cos^{-1}(M_a)) * M_b > 0.0$  then multiply  $\theta = -\cos^{-1}(M_a)$  else  $\theta = \cos^{-1}(M_a)$ .

### 1.1.3 Rotation

Rotation if a vector is only defined in 2D and 3D. In 2D, for a right-handed rotation of angle  $\theta$  the rotation matrix is equal to:

$$R = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \quad (8)$$

In 3D, for a right-handed rotation of angle  $\theta$  around axis  $\vec{u}$  the rotation is equal to (to shorten notation  $\theta$  is not written in the matrix below):

$$R = \begin{bmatrix} \cos + u_x^2(1 - \cos) & u_x u_y(1 - \cos) - u_z \sin & u_x u_z(1 - \cos) + u_y \sin \\ u_x u_y(1 - \cos) + u_z \sin & \cos + u_y^2(1 - \cos) & u_y u_z(1 - \cos) - u_x \sin \\ u_x u_z(1 - \cos) - u_y \sin & u_y u_z(1 - \cos) + u_x \sin & \cos + u_z^2(1 - \cos) \end{bmatrix} \quad (9)$$

## 1.2 Matrix

### 1.2.1 Inverse matrix

The inverse of a matrix is only implemented for square matrices less than 3x3. It is computed directly, based on the determinant and the adjoint matrix.

For a 2x2 matrix  $M$ :

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} M_3 & -M_2 \\ -M_1 & M_0 \end{bmatrix} \quad (10)$$

where

$$M = \begin{bmatrix} M_0 & M_2 \\ M_1 & M_3 \end{bmatrix} \quad (11)$$

and

$$\det = M_0 M_3 - M_1 M_2 \quad (12)$$

For a 3x3 matrix  $M$ :

$$M^{-1} = \frac{1}{\det} \begin{bmatrix} (M_4 M_8 - M_5 M_7) & -(M_3 M_8 - M_5 M_6) & (M_3 M_7 - M_4 M_6) \\ -(M_1 M_8 - M_2 M_7) & (M_0 M_8 - M_2 M_6) & -(M_0 M_7 - M_1 M_6) \\ (M_1 M_5 - M_2 M_4) & -(M_0 M_5 - M_2 M_3) & (M_0 M_4 - M_1 M_3) \end{bmatrix} \quad (13)$$

where

$$M = \begin{bmatrix} M_0 & M_3 & M_6 \\ M_1 & M_4 & M_7 \\ M_2 & M_5 & M_8 \end{bmatrix} \quad (14)$$

and

$$\det = M_0(M_4 M_8 - M_5 M_7) - M_3(M_1 M_8 - M_2 M_7) + M_6(M_1 M_5 - M_2 M_4) \quad (15)$$

### 1.2.2 QR factorization

The QR factorization is performed using the Householder algorithm:

```
Compute Q and R such as  $A = QR$ 
A[i][j] <=> value of matrix A at the i-th column and j-th row
Must have nbCol(A) <= nbRow(A)

QQtilde := matrix identity of dimensions (nbRow(A) columns, nbRow(A) rows)
for k := 0 to nbCol(A):

    w := vector null of dimension (nbRow(A) - k)
    for i := 0 to dim(w)
        w[i] := A[k][k + i]

    sign := if w[0] >= 0.0 then 1.0 else -1.0
    w[0] := w[0] + sign * norm(w)

    v = w / nom(w)

    H := matrix identity of dimensions (dim(v) columns, dim(v) rows)
    vvt := v * transpose(v)
    H := H - 2.0 * vvt

    reflector := matrix identity of dimensions (nbRow(A) columns, nbRow(A) rows)
    for i := 0 to nbCol(H)
        for j := 0 to nbRow(H)
            reflector[i + k][j + k] := H[i][j]

    A := reflector * A

    QQtilde := QQtilde * reflector

R := matrix of dimensions (nbCol(A) columns, nbCol(A) rows)
for i := 0 to nbCol(A)
    for j := 0 to nbCol(A)
        R[i][j] := A[i][j]

Q := matrix of dimensions (nbCol(A) columns, nbRow(A) rows)
for i := 0 to nbCol(A)
    for j := 0 to nbRow(A)
        Q[i][j] := QQtilde[i][j]
```

Example of execution step by step:

```
A:
[-1.000, -1.000,  1.000
  1.000,  3.000,  3.000
 -1.000, -1.000,  5.000
  1.000,  3.000,  7.000]

k: 0
----
w: <-3.000,1.000,-1.000,1.000>
v: <-0.866,0.289,-0.289,0.289>
vvt:
[ 0.750, -0.250,  0.250, -0.250
```

```

-0.250, 0.083, -0.083, 0.083
0.250, -0.083, 0.083, -0.083
-0.250, 0.083, -0.083, 0.083]
H:
[-0.500, 0.500, -0.500, 0.500
0.500, 0.833, 0.167, -0.167
-0.500, 0.167, 0.833, 0.167
0.500, -0.167, 0.167, 0.833]
reflector:
[-0.500, 0.500, -0.500, 0.500
0.500, 0.833, 0.167, -0.167
-0.500, 0.167, 0.833, 0.167
0.500, -0.167, 0.167, 0.833]
reflector.A:
[ 2.000, 4.000, 2.000
0.000, 1.333, 2.667
-0.000, 0.667, 5.333
0.000, 1.333, 6.667]
QQtilde:
[-0.500, 0.500, -0.500, 0.500
0.500, 0.833, 0.167, -0.167
-0.500, 0.167, 0.833, 0.167
0.500, -0.167, 0.167, 0.833]

k: 1
----
w: <3.333,0.667,1.333>
v: <0.913,0.183,0.365>
vvt:
[ 0.833, 0.167, 0.333
0.167, 0.033, 0.067
0.333, 0.067, 0.133]
H:
[-0.667, -0.333, -0.667
-0.333, 0.933, -0.133
-0.667, -0.133, 0.733]
reflector:
[ 1.000, 0.000, 0.000, 0.000
0.000, -0.667, -0.333, -0.667
0.000, -0.333, 0.933, -0.133
0.000, -0.667, -0.133, 0.733]
reflector.A:
[ 2.000, 4.000, 2.000
-0.000, -2.000, -8.000
-0.000, 0.000, 3.200
0.000, -0.000, 2.400]
QQtilde:
[-0.500, -0.500, -0.700, 0.100
0.500, -0.500, -0.100, -0.700
-0.500, -0.500, 0.700, -0.100
0.500, -0.500, 0.100, 0.700]

k: 2
----
w: <7.200,2.400>
v: <0.949,0.316>
vvt:
[ 0.900, 0.300
0.300, 0.100]
H:
[-0.800, -0.600
-0.600, 0.800]

```

```

reflector:
[ 1.000,  0.000,  0.000,  0.000
  0.000,  1.000,  0.000,  0.000
  0.000,  0.000, -0.800, -0.600
  0.000,  0.000, -0.600,  0.800]
reflector.A:
[ 2.000,  4.000,  2.000
 -0.000, -2.000, -8.000
  0.000, -0.000, -4.000
  0.000, -0.000, -0.000]
QQtilde:
[-0.500, -0.500,  0.500,  0.500
  0.500, -0.500,  0.500, -0.500
 -0.500, -0.500, -0.500, -0.500
  0.500, -0.500, -0.500,  0.500]

Q:
[-0.500, -0.500,  0.500
  0.500, -0.500,  0.500
 -0.500, -0.500, -0.500
  0.500, -0.500, -0.500]

R:
[ 2.000,  4.000,  2.000
 -0.000, -2.000, -8.000
  0.000, -0.000, -4.000]

QR:
[-1.000, -1.000,  1.000
  1.000,  3.000,  3.000
 -1.000, -1.000,  5.000
  1.000,  3.000,  7.000]

```

### 1.2.3 Eigen values and vectors

The Eigen values and vectors are obtained using the QR algorithm:

```

Compute Eigen values and vectors of A
A[i][j] <=> value of matrix A at the i-th column and j-th row
Must have nbCol(A) = nbRow(A)

err := 1.0
M := matrix identity of dimensions(nbCol(A) columns, nbRow(A) rows)
loop until err < epsilon
  Q,R := QRDecomposition(A)
  A := R * Q
  M := M * Q
  err := max(abs(non diagonal values of A))
for i := 0 to NbCol(A)
  eigenValue[i] := A[i][i]
  for j := 0 to nbRow(A)
    eigenVector_i[j] := M[i][j]

```

Example of execution step by step:

```

A:
[ 2.920000,  0.860000, -1.150000
  0.860000,  6.510000,  3.320000

```

```

-1.150000, 3.320000, 4.570000]
k: 0
----
A:
[ 3.893980, 0.051622, -0.542073
 0.051622, 8.916388, 0.802225
-0.542073, 0.802225, 1.189634]
M:
[-0.897358, 0.044696, -0.439034
-0.264290, -0.851147, 0.453541
 0.353411, -0.523021, -0.775596]
k: 1
----
A:
[ 3.989910, -0.007497, -0.141512
-0.007497, 8.997707, 0.092890
-0.141512, 0.092890, 1.012387]
M:
[ 0.827596, -0.005324, 0.561300
 0.335447, 0.806451, -0.486943
-0.450068, 0.591278, 0.669201]
k: 2
----
A:
[ 3.996253, -0.020544, -0.035648
-0.020544, 8.998704, 0.010273
-0.035648, 0.010273, 1.005045]
M:
[-0.807189, -0.002264, -0.590289
-0.350981, -0.802184, 0.483025
 0.474614, -0.597072, -0.646720]
k: 3
----
A:
[ 3.996995, -0.046356, -0.008962
-0.046356, 8.998370, 0.001080
-0.008962, 0.001080, 1.004634]
M:
[ 0.801869, 0.007056, 0.597458
 0.351147, 0.803462, -0.480776
-0.483427, 0.595315, 0.641793]
k: 4
----
A:
[ 3.998767, -0.104343, -0.002252
-0.104343, 8.996623, 0.000083
-0.002252, 0.000083, 1.004609]
M:
[-0.800392, -0.016405, -0.599253
-0.342883, -0.807440, 0.480075
 0.491736, -0.589721, -0.640644]
k: 5
----
A:
[ 4.007611, -0.234525, -0.000566
-0.234525, 8.987781, -0.000012
-0.000566, -0.000012, 1.004607]
M:
[ 0.799354, 0.037270, 0.599703
 0.321974, 0.816115, -0.479884
-0.507312, 0.576686, 0.640365]
k: 6

```



```

----
A:
[ 4.051963, -0.523369, -0.000142
 -0.523369,  8.943428, -0.000013
 -0.000142, -0.000013,  1.004607]
M:
[-0.795727, -0.083897, -0.599817
 -0.273814, -0.833538,  0.479834
  0.540226, -0.546055, -0.640296]
k: 7
----
A:
[ 4.265212, -1.127628, -0.000035
 -1.127628,  8.730177, -0.000008
 -0.000035, -0.000008,  1.004607]
M:
[ 0.778403,  0.185133,  0.599845
  0.164799,  0.861750, -0.479822
 -0.605747,  0.472348,  0.640279]
k: 8
----
A:
[ 5.114194, -2.083614, -0.000008
 -2.083614,  7.881196, -0.000004
 -0.000008, -0.000004,  1.004607]
M:
[-0.705223, -0.377938, -0.599852
  0.060932, -0.875249,  0.479818
  0.706362, -0.301829, -0.640275]
k: 9
----
A:
[ 6.964207, -2.457212, -0.000001
 -2.457211,  6.031182, -0.000002
 -0.000001, -0.000002,  1.004607]
M:
[ 0.510500,  0.616088,  0.599854
 -0.386664,  0.787570, -0.479818
 -0.768037,  0.013005,  0.640274]
k: 10
----
A:
[ 8.402923, -1.620381, -0.000000
 -1.620380,  4.592468, -0.000001
 -0.000000, -0.000001,  1.004607]
M:
[-0.276422, -0.750843, -0.599854
  0.626681, -0.614041,  0.479817
  0.728603,  0.243285, -0.640273]
k: 11
----
A:
[ 8.868839, -0.795746,  0.000000
 -0.795745,  4.126554, -0.000000
 -0.000000, -0.000000,  1.004607]
M:
[ 0.129251,  0.789600,  0.599855
 -0.731611,  0.484273, -0.479817
 -0.669357, -0.376843,  0.640273]
k: 12
----
A:

```

```

[ 8.972622, -0.360938, 0.000000
 -0.360938, 4.022771, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[-0.058172, -0.797991, -0.599855
 0.771961, -0.416956, 0.479817
 0.633003, 0.435152, -0.640273]
k: 13
----
A:
[ 8.993616, -0.160978, 0.000000
 -0.160978, 4.001777, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.026050, 0.799685, 0.599855
 -0.788096, 0.385590, -0.479817
 -0.615001, -0.460244, 0.640273]
k: 14
----
A:
[ 8.997777, -0.071554, 0.000000
 -0.071554, 3.997614, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[-0.011735, -0.800023, -0.599855
 0.794871, -0.371425, 0.479817
 0.606666, 0.471176, -0.640273]
k: 15
----
A:
[ 8.998597, -0.031784, 0.000000
 -0.031784, 3.996793, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.005373, 0.800091, 0.599855
 -0.797799, 0.365092, -0.479817
 -0.602899, -0.475986, 0.640273]
k: 16
----
A:
[ 8.998760, -0.014117, 0.000000
 -0.014117, 3.996630, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[-0.002547, -0.800105, -0.599855
 0.799084, -0.362272, 0.479817
 0.601215, 0.478112, -0.640273]
k: 17
----
A:
[ 8.998793, -0.006270, 0.000000
 -0.006270, 3.996598, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.001291, 0.800108, 0.599855
 -0.799651, 0.361018, -0.479817
 -0.600464, -0.479055, 0.640273]
k: 18
----
A:
[ 8.998798, -0.002785, 0.000000
 -0.002784, 3.996592, -0.000000

```

```

-0.000000, -0.000000, 1.004607]
M:
[-0.000734, -0.800108, -0.599855
 0.799902, -0.360460, 0.479817
 0.600130, 0.479473, -0.640273]
k: 19
----
A:
[ 8.998800, -0.001237, 0.000000
 -0.001237, 3.996591, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.000486, 0.800109, 0.599855
 -0.800014, 0.360213, -0.479817
 -0.599982, -0.479659, 0.640273]
k: 20
----
A:
[ 8.998800, -0.000550, 0.000000
 -0.000549, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[-0.000376, -0.800109, -0.599855
 0.800063, -0.360103, 0.479817
 0.599916, 0.479741, -0.640273]
k: 21
----
A:
[ 8.998800, -0.000244, 0.000000
 -0.000244, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.000328, 0.800109, 0.599855
 -0.800085, 0.360054, -0.479817
 -0.599886, -0.479778, 0.640273]
k: 22
----
A:
[ 8.998800, -0.000109, 0.000000
 -0.000108, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[-0.000306, -0.800109, -0.599855
 0.800095, -0.360032, 0.479817
 0.599873, 0.479794, -0.640273]
k: 23
----
A:
[ 8.998800, -0.000048, 0.000000
 -0.000048, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.000296, 0.800109, 0.599855
 -0.800099, 0.360023, -0.479817
 -0.599868, -0.479801, 0.640273]
k: 24
----
A:
[ 8.998800, -0.000022, 0.000000
 -0.000021, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:

```

```

[-0.000292, -0.800109, -0.599855
 0.800101, -0.360019, 0.479817
 0.599865, 0.479804, -0.640273]
k: 25
----
A:
[ 8.998800, -0.000010, 0.000000
 -0.000009, 3.996590, -0.000000
 -0.000000, -0.000000, 1.004607]
M:
[ 0.000290, 0.800109, 0.599855
 -0.800102, 0.360017, -0.479817
 -0.599864, -0.479806, 0.640273]
Eigen values: <8.999,3.997,1.005>
Eigen vector 1: <0.000,-0.800,-0.600>
Eigen vector 2: <0.800,0.360,-0.480>
Eigen vector 3: <0.600,-0.480,0.640>

```

## 2 Interface

```

// ===== PBMATH.H =====

#ifndef PBMATH_H
#define PBMATH_H

// ===== Include =====

#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <stdbool.h>
#include <stddef.h>
#include <float.h>
#include "pberr.h"
#include "pbjson.h"

// ===== Define =====

#define PBMATH_EPSILON 0.00001
#define PBMATH_TWOPI 6.283185307
#define PBMATH_TWOPI_DIV_360 0.01745329252
#define PBMATH_PI 3.141592654
#define PBMATH_HALFPPI 1.570796327
#define PBMATH_QUARTERPI 0.7853981634
#define PBMATH_SQRTTWO 1.414213562
#define PBMATH_SQRTONEHALF 0.707106781
#ifndef MAX
#define MAX(a,b) ((a)>(b)?(a):(b))
#endif
#ifndef MIN
#define MIN(a,b) ((a)<(b)?(a):(b))
#endif
#define ISEQUALF(a,b) (fabs((a)-(b))<PBMATH_EPSILON)
#define SHORT(a) ((short)(round(a)))
#define INT(a) ((int)(round(a)))
#define rnd() (float)(rand()/(float)(RAND_MAX))

// ----- VecLong

```

```

// ===== Data structure =====

// Vector of long values
typedef struct VecLong {
    // Dimension
    long _dim;
    // Values
    long _val[0];
} VecLong;

typedef struct VecLong2D {
    // Dimension
    long _dim;
    // Values
    long _val[2];
} VecLong2D;

typedef struct VecLong3D {
    // Dimension
    long _dim;
    // Values
    long _val[3];
} VecLong3D;

typedef struct VecLong4D {
    // Dimension
    long _dim;
    // Values
    long _val[4];
} VecLong4D;

// ===== Functions declaration =====

// Create a new VecLong of dimension 'dim'
// Values are initialized to 0.0
VecLong* VecLongCreate(const long dim);

// Static constructors for VecLong
#if BUILDMODE != 0
static inline
#endif
VecLong2D VecLongCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
VecLong3D VecLongCreateStatic3D();
#if BUILDMODE != 0
static inline
#endif
VecLong4D VecLongCreateStatic4D();

// Clone the VecLong
// Return NULL if we couldn't clone the VecLong
VecLong* _VecLongClone(const VecLong* const that);

// Function which return the JSON encoding of 'that'
JSONNode* _VecLongEncodeAsJSON(const VecLong* const that);

// Function which decode from JSON encoding 'json' to 'that'
bool _VecLongDecodeAsJSON(VecLong** that, const JSONNode* const json);

```

```

// Load the VecLong from the stream
// If the VecLong is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecLongLoad(VecLong** that, FILE* const stream);

// Save the VecLong to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecLongSave(const VecLong* const that,
    FILE* const stream, const bool compact);

// Free the memory used by a VecLong
// Do nothing if arguments are invalid
void _VecLongFree(VecLong** that);

// Print the VecLong on 'stream'
void _VecLongPrint(const VecLong* const that,
    FILE* const stream);

// Return the i-th value of the VecLong
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet(const VecLong* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet2D(const VecLong2D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet3D(const VecLong3D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
long _VecLongGet4D(const VecLong4D* const that, const long i);

// Set the i-th value of the VecLong to v
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet(VecLong* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet2D(VecLong2D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet3D(VecLong3D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet4D(VecLong4D* const that, const long i, const long v);

// Set the i-th value of the VecLong to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd(VecLong* const that, const long i, const long v);
#if BUILDMODE != 0

```

```

static inline
#endif
void _VecLongSetAdd2D(VecLong2D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd3D(VecLong3D* const that, const long i, const long v);
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd4D(VecLong4D* const that, const long i, const long v);

// Return the dimension of the VecLong
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetDim(const VecLong* const that);

// Return the Hamiltonian distance between the VecLong 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist(const VecLong* const that, const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist2D(const VecLong2D* const that, const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist3D(const VecLong3D* const that, const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist4D(const VecLong4D* const that, const VecLong4D* const tho);

// Return true if the VecLong 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecLongIsEqual(const VecLong* const that,
    const VecLong* const tho);

// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _VecLongCopy(VecLong* const that, const VecLong* const w);

// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd(const VecLong* const that,
    const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd2D(const VecLong2D* const that,
    const VecLong2D* const tho);
#if BUILDMODE != 0

```

```

static inline
#endif
long _VecLongDotProd3D(const VecLong3D* const that,
    const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd4D(const VecLong4D* const that,
    const VecLong4D* const tho);

// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetNull(VecLong* const that);

// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAll(VecLong* const that, long v);

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStep(VecLong* const that, const VecLong* const bound);

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStep(VecLong* const that, const VecLong* const bound);

// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecLongShiftStep(VecLong* const that,
    const VecLong* const from, const VecLong* const to);

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStepDelta(VecLong* const that,
    const VecLong* const bound, const VecLong* const delta);

```



```

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStepDelta(VecLong* const that,
    const VecLong* const bound, const VecLong* const delta);

// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp(VecLong* const that, const long a,
    const VecLong* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp2D(VecLong2D* const that, const long a,
    const VecLong2D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp3D(VecLong3D* const that, const long a,
    const VecLong3D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp4D(VecLong4D* const that, const long a,
    const VecLong4D* const tho, const long b);

// Return a VecLong equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetOp(const VecLong* const that, const long a,
    const VecLong* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetOp2D(const VecLong2D* const that, const long a,
    const VecLong2D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetOp3D(const VecLong3D* const that, const long a,
    const VecLong3D* const tho, const long b);
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetOp4D(const VecLong4D* const that, const long a,
    const VecLong4D* const tho, const long b);

// Calculate the Hadamard product of that by tho and store the
// result in 'that'

```

```

// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd(VecLong* const that,
    const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd2D(VecLong2D* const that,
    const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd3D(VecLong3D* const that,
    const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd4D(VecLong4D* const that,
    const VecLong4D* const tho);

// Return a VecLong equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetHadamardProd(const VecLong* const that,
    const VecLong* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetHadamardProd2D(const VecLong2D* const that,
    const VecLong2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetHadamardProd3D(const VecLong3D* const that,
    const VecLong3D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetHadamardProd4D(const VecLong4D* const that,
    const VecLong4D* const tho);

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxVal(const VecLong* const that);

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinVal(const VecLong* const that);

// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline

```

```

#endif
long _VecLongGetMaxValAbs(const VecLong* const that);

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinValAbs(const VecLong* const that);

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetIMaxVal(const VecLong* const that);

// Return a new VecLong as a copy of the VecLong 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0
// If it is shrunk, values are discarded from the end of the vector
VecLong* _VecLongGetNewDim(const VecLong* const that, const long dim);

// ----- VecShort

// ===== Data structure =====

// Vector of short values
typedef struct VecShort {
    // Dimension
    long _dim;
    // Values
    short _val[0];
} VecShort;

typedef struct VecShort2D {
    // Dimension
    long _dim;
    // Values
    short _val[2];
} VecShort2D;

typedef struct VecShort3D {
    // Dimension
    long _dim;
    // Values
    short _val[3];
} VecShort3D;

typedef struct VecShort4D {
    // Dimension
    long _dim;
    // Values
    short _val[4];
} VecShort4D;

// ===== Functions declaration =====

// Create a new VecShort of dimension 'dim'
// Values are initialized to 0.0
VecShort* VecShortCreate(const long dim);

// Static constructors for VecShort

```

```

#if BUILDMODE != 0
static inline
#endif
VecShort2D VecShortCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecShortCreateStatic3D();
#if BUILDMODE != 0
static inline
#endif
VecShort4D VecShortCreateStatic4D();

// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(const VecShort* const that);

// Function which return the JSON encoding of 'that'
JSONNode* _VecShortEncodeAsJSON(const VecShort* const that);

// Function which decode from JSON encoding 'json' to 'that'
bool _VecShortDecodeAsJSON(VecShort** that, const JSONNode* const json);

// Load the VecShort from the stream
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* const stream);

// Save the VecShort to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecShortSave(const VecShort* const that,
    FILE* const stream, const bool compact);

// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that);

// Print the VecShort on 'stream'
void _VecShortPrint(const VecShort* const that,
    FILE* const stream);

// Return the i-th value of the VecShort
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet(const VecShort* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet2D(const VecShort2D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet3D(const VecShort3D* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet4D(const VecShort4D* const that, const long i);

// Set the i-th value of the VecShort to v

```

```

#if BUILDMODE != 0
static inline
#endif
void _VecShortSet(VecShort* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet2D(VecShort2D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet3D(VecShort3D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet4D(VecShort4D* const that, const long i, const short v);

// Set the i-th value of the VecShort to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd(VecShort* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd2D(VecShort2D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd3D(VecShort3D* const that, const long i, const short v);
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd4D(VecShort4D* const that, const long i, const short v);

// Return the dimension of the VecShort
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetDim(const VecShort* const that);

// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist(const VecShort* const that, const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist2D(const VecShort2D* const that, const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist3D(const VecShort3D* const that, const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist4D(const VecShort4D* const that, const VecShort4D* const tho);

// Return true if the VecShort 'that' is equal to 'tho', else false
#if BUILDMODE != 0

```

```

static inline
#endif
bool _VecShortIsEqual(const VecShort* const that,
    const VecShort* const tho);

// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _VecShortCopy(VecShort* const that, const VecShort* const w);

// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd(const VecShort* const that,
    const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd2D(const VecShort2D* const that,
    const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd3D(const VecShort3D* const that,
    const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd4D(const VecShort4D* const that,
    const VecShort4D* const tho);

// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetNull(VecShort* const that);

// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAll(VecShort* const that, short v);

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* const that, const VecShort* const bound);

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* const that, const VecShort* const bound);

```

```

// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* const that,
    const VecShort* const from, const VecShort* const to);

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStepDelta(VecShort* const that,
    const VecShort* const bound, const VecShort* const delta);

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStepDelta(VecShort* const that,
    const VecShort* const bound, const VecShort* const delta);

// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp(VecShort* const that, const short a,
    const VecShort* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp2D(VecShort2D* const that, const short a,
    const VecShort2D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp3D(VecShort3D* const that, const short a,
    const VecShort3D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp4D(VecShort4D* const that, const short a,
    const VecShort4D* const tho, const short b);

// Return a VecShort equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'

```

```

#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetOp(const VecShort* const that, const short a,
    const VecShort* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetOp2D(const VecShort2D* const that, const short a,
    const VecShort2D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetOp3D(const VecShort3D* const that, const short a,
    const VecShort3D* const tho, const short b);
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetOp4D(const VecShort4D* const that, const short a,
    const VecShort4D* const tho, const short b);

// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd(VecShort* const that,
    const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd2D(VecShort2D* const that,
    const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd3D(VecShort3D* const that,
    const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd4D(VecShort4D* const that,
    const VecShort4D* const tho);

// Return a VecShort equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetHadamardProd(const VecShort* const that,
    const VecShort* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetHadamardProd2D(const VecShort2D* const that,
    const VecShort2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetHadamardProd3D(const VecShort3D* const that,

```



```

    const VecShort3D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetHadamardProd4D(const VecShort4D* const that,
    const VecShort4D* const tho);

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxVal(const VecShort* const that);

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinVal(const VecShort* const that);

// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxValAbs(const VecShort* const that);

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinValAbs(const VecShort* const that);

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetIMaxVal(const VecShort* const that);

// ----- VecFloat

// ===== Data structure =====

// Vector of float values
typedef struct VecFloat {
    // Dimension
    long _dim;
    // Values
    float _val[0];
} VecFloat;

typedef struct VecFloat2D {
    // Dimension
    long _dim;
    // Values
    float _val[2];
} VecFloat2D;

typedef struct VecFloat3D {
    // Dimension
    long _dim;
    // Values

```

```

    float _val[3];
} VecFloat3D;

// ===== Functions declaration =====

// Create a new VecFloat of dimension 'dim'
// Values are initialized to 0.0
VecFloat* VecFloatCreate(const long dim);

// Static constructors for VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecFloatCreateStatic2D();
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecFloatCreateStatic3D();

// Clone the VecFloat
VecFloat* _VecFloatClone(const VecFloat* const that);

// Function which return the JSON encoding of 'that'
JSONNode* _VecFloatEncodeAsJSON(const VecFloat* const that);

// Function which decode from JSON encoding 'json' to 'that'
bool _VecFloatDecodeAsJSON(VecFloat** that, const JSONNode* const json);

// Load the VecFloat from the stream
// If the VecFloat is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecFloatLoad(VecFloat** that, FILE* const stream);

// Save the VecFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecFloatSave(const VecFloat* const that,
    FILE* const stream, const bool compact);

// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that);

// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(const VecFloat* const that, FILE* const stream,
    const unsigned int prec);
static inline void _VecFloatPrintDef(const VecFloat* const that,
    FILE* const stream) {
    VecFloatPrint(that, stream, 3);
}

// Return the 'i'-th value of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet(const VecFloat* const that, const long i);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet2D(const VecFloat2D* const that, const long i);

```

```

#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet3D(const VecFloat3D* const that, const long i);

// Set the 'i'-th value of the VecFloat to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet(VecFloat* const that, const long i, const float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet2D(VecFloat2D* const that, const long i, const float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet3D(VecFloat3D* const that, const long i, const float v);

// Set the 'i'-th value of the VecFloat to 'v' plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd(VecFloat* const that, const long i, const float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd2D(VecFloat2D* const that, const long i,
    const float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd3D(VecFloat3D* const that, const long i,
    const float v);

// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull(VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull2D(VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull3D(VecFloat3D* const that);

// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll(VecFloat* const that, float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll2D(VecFloat2D* const that, float v);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll3D(VecFloat3D* const that, float v);

```

```

// Return the dimension of the VecFloat
// Return 0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetDim(const VecFloat* const that);

// Return a new VecFloat as a copy of the VecFloat 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0.0
// If it is shrunk, values are discarded from the end of the vector
VecFloat* _VecFloatGetNewDim(const VecFloat* const that, const long dim);

// Copy the values of 'w' in 'that' (must have same dimensions)
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void _VecFloatCopy(VecFloat* const that, const VecFloat* const w);

// Return the norm of the VecFloat
// Return 0.0 if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm(const VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm2D(const VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm3D(const VecFloat3D* const that);

// Normalise the VecFloat
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise(VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise2D(VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise3D(VecFloat3D* const that);

// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0

```

```

static inline
#endif
float _VecFloatDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecFloatIsEqual(const VecFloat* const that,
    const VecFloat* const tho);

// Calculate (that * a) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale(VecFloat* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale2D(VecFloat2D* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatScale3D(VecFloat3D* const that, const float a);

// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0

```

```

static inline
#endif
VecFloat* _VecFloatGetScale(const VecFloat* const that, const float a);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetScale2D(const VecFloat2D* const that,
    const float a);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetScale3D(const VecFloat3D* const that,
    const float a);

// Calculate (that * a + tho * b) and store the result in 'that'
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp(VecFloat* const that, const float a,
    const VecFloat* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp2D(VecFloat2D* const that, const float a,
    const VecFloat2D* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp3D(VecFloat3D* const that, const float a,
    const VecFloat3D* const tho, const float b);

// Return a VecFloat equal to (that * a + tho * b)
// Return NULL if arguments are invalid
// 'tho' can be null, in which case it is consider to be the null vector
// If 'tho' is not null it must be of same dimension as 'that'
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetOp(const VecFloat* const that, const float a,
    const VecFloat* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetOp2D(const VecFloat2D* const that, const float a,
    const VecFloat2D* const tho, const float b);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetOp3D(const VecFloat3D* const that, const float a,
    const VecFloat3D* const tho, const float b);

// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd(VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0

```

```

static inline
#endif
void _VecFloatHadamardProd2D(VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd3D(VecFloat3D* const that,
    const VecFloat3D* const tho);

// Return a VecFloat equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetHadamardProd(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetHadamardProd2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetHadamardProd3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRot2D(VecFloat2D* const that, const float theta);

// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetRot2D(const VecFloat2D* const that,
    const float theta);

// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotAxis(VecFloat3D* const that,
    const VecFloat3D* const axis, const float theta);

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
VecFloat3D _VecFloatGetRotAxis(const VecFloat3D* const that,
    const VecFloat3D* const axis, const float theta);

// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0

```

```

static inline
#endif
void _VecFloatRotX(VecFloat3D* const that, const float theta);

// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotY(VecFloat3D* const that, const float theta);

// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotZ(VecFloat3D* const that, const float theta);

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(const VecFloat3D* const that,
    const float theta);

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(const VecFloat3D* const that,
    const float theta);

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Z
VecFloat3D _VecFloatGetRotZ(const VecFloat3D* const that,
    const float theta);

// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

// Return the cross product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetCrossProd(const VecFloat* const that,
    const VecFloat* const tho);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetCrossProd3D(const VecFloat3D* const that,
    const VecFloat3D* const tho);

```



```

// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
float _VecFloatAngleTo2D(const VecFloat2D* const that,
    const VecFloat2D* const tho);

// Return the conversion of VecFloat 'that' to a VecShort using round()
#if BUILDMODE != 0
static inline
#endif
VecShort* VecFloatToShort(const VecFloat* const that);
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecFloatToShort2D(const VecFloat2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecFloatToShort3D(const VecFloat3D* const that);

// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecShortToFloat(const VecShort* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecShortToFloat2D(const VecShort2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecShortToFloat3D(const VecShort3D* const that);

// Return the conversion of VecLong 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecLongToFloat(const VecLong* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecLongToFloat2D(const VecLong2D* const that);
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecLongToFloat3D(const VecLong3D* const that);

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxVal(const VecFloat* const that);

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinVal(const VecFloat* const that);

// Get the max value (in absolute value) in components of the
// vector 'that'

```

```

#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxValAbs(const VecFloat* const that);

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinValAbs(const VecFloat* const that);

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* const that,
    const VecFloat* const bound, const VecFloat* const delta);

// Step the values of the vector incrementally by delta
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* const that,
    const VecFloat* const from, const VecFloat* const to,
    const VecFloat* const delta);

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetIMaxVal(const VecFloat* const that);

// Return a set of two vectors containing the bounds of the vectors in
// the GSet 'that'
// The set must have at least one element
// The returned set is ordered as follow: (boundMin, boundMax)
GSetVecFloat _GSetVecFloatGetBounds(const GSetVecFloat* const that);

// ----- MatFloat

// ===== Data structure =====

// Vector of float values
typedef struct MatFloat {
    // Dimension (nbCol, nbLine)
    const VecShort2D _dim;
    // Values (memorized by lines)
    float _val[0];
} MatFloat;

// Simple pod to hold the result of a QR decomposition
typedef struct QRDecomp {

```

```

    MatFloat* _Q;
    MatFloat* _R;
} QRDecomp;

// ===== Functions declaration =====

// Free memory used by the QRDecomp 'that'
#if BUILDMODE != 0
static inline
#endif
void QRDecompFreeStatic(QRDecomp* const that);

// Create a new MatFloat of dimension 'dim' (nbCol, nbLine)
// Values are initialized to 0.0
MatFloat* MatFloatCreate(const VecShort2D* const dim);

// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSetIdentity(MatFloat* const that);

// Clone the MatFloat
MatFloat* _MatFloatClone(const MatFloat* const that);

// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _MatFloatCopy(MatFloat* const that, const MatFloat* const tho);

// Function which return the JSON encoding of 'that'
JSONNode* _MatFloatEncodeAsJSON(MatFloat* const that);

// Function which decode from JSON encoding 'json' to 'that'
bool _MatFloatDecodeAsJSON(MatFloat** that, JSONNode* json);

// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream);

// Save the MatFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true upon success, else false
bool _MatFloatSave(MatFloat* const that, FILE* stream, bool compact);

// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that);

// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* const that, FILE* stream, unsigned int prec);
static inline void _MatFloatPrintlnDef(MatFloat* const that, FILE* stream) {
    MatFloatPrintln(that, stream, 3);
}

// Return the value at index (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col

```

```

#if BUILDMODE != 0
static inline
#endif
float _MatFloatGet(const MatFloat* const that,
    VecShort2D* index);

// Set the value at index (col, line) of the MatFloat to 'v'
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSet(MatFloat* const that, VecShort2D* index, float v);

// Return the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
const VecShort2D* _MatFloatDim(const MatFloat* const that);

// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
VecShort2D _MatFloatGetDim(const MatFloat* const that);

// Return the number of rows of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbRow(const MatFloat* const that);

// Return the number of columns of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbCol(const MatFloat* const that);

// Return the inverse matrix of 'that'
// The matrix must be a square matrix
// Return NULL if the matrix is not invertible, or in some case when
// the matrix's diagonal contains null values and the matrix's size
// is greater than 3
MatFloat* _MatFloatGetInv(const MatFloat* const that);

// Return the product of matrix 'that' and vector 'v'
// Number of columns of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(
    const MatFloat* const that, const VecFloat* v);

// Return the product of vector 'v' and transpose of vector 'w'
MatFloat* _MatFloatGetProdVecVecTransposeFloat(
    const VecFloat* const v,
    const VecFloat* const w);

// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(const MatFloat* const that, const MatFloat* tho);

// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline

```

```

#endif
MatFloat* _MatFloatGetAdd(MatFloat* const that, MatFloat* tho);

// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
void _MatFloatAdd(MatFloat* const that, MatFloat* tho);

// Multiply the matrix 'that' by 'a'
#if BUILDMODE != 0
static inline
#endif
void _MatFloatScale(MatFloat* const that, const float a);

// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* const that, MatFloat* tho);

// Calculate the Eigen values and vectors of the MatFloat 'that'
// Return a set of VecFloat. The first VecFloat of the set contains
// the Eigen values, with values sorted from biggest to
// smallest (in absolute value). The following VecFloat are the
// respectiev Eigen vectors
// 'that' must be a 2D square matrix
// Return the identity if the QR decompostion fails
// http://madrury.github.io/jekyll/update/statistics/2017/10/04/qr-algorithm.html
// TODO: should be improved with the Hessenberg QR method
// https://www.math.kth.se/na/SF2524/matber15/qrmeth.pdf
GSetVecFloat _MatFloatGetEigenValues(const MatFloat* const that);

// Calculate the QR decomposition of the MatFloat 'that' using the
// Householder algorithm
// Return {NULL, NULL} if the MatFloat couldn't be decomposed
// http://www.seas.ucla.edu/~vandenbe/133A/lectures/qr.pdf
QRDecomp _MatFloatGetQR(const MatFloat* const that);

// Calculate the transposed of the MatFloat 'that'
MatFloat* _MatFloatGetTranspose(const MatFloat* const that);

// ----- Gauss

// ===== Define =====

// ===== Data structure =====

// Should be vector of float values
typedef struct Gauss {
    // Mean
    float _mean;
    // Sigma
    float _sigma;
} Gauss;

// ===== Functions declaration =====

// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(const float mean, const float sigma);
Gauss GaussCreateStatic(const float mean, const float sigma);

// Free the memory used by a Gauss

```

```

// Do nothing if arguments are invalid
void GaussFree(Gauss** that);

// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
static inline
#endif
float GaussGet(const Gauss* const that, const float x);

// Return a random value according to the Gauss 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
static inline
#endif
float GaussRnd(Gauss* const that);

// ----- Smoother

// ===== Define =====

// ===== Data structure =====

// ===== Functions declaration =====

// Return the order 1 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmoothStep(const float x);

// Return the order 2 smooth value of 'x'
// if x < 0.0 return 0.0
// if x > 1.0 return 1.0
#if BUILDMODE != 0
static inline
#endif
float SmootherStep(const float x);

// ----- Conversion functions

// ===== Functions declaration =====

// Convert radians to degrees
static inline float ConvRad2Deg(const float rad) {
    return rad / PBMath_TWOPI_DIV_360;
}

// Convert degrees to radians
static inline float ConvDeg2Rad(const float deg) {
    return PBMath_TWOPI_DIV_360 * deg;
}

// ----- SysLinEq

// ===== Data structure =====

// Linear system of equalities
typedef struct SysLinEq {
    // Matrix
    MatFloat* _M;

```

```

    // Inverse of the matrix
    MatFloat* _Minv;
    // Vector
    VecFloat* _V;
} SysLinEq;

// ===== Functions declaration =====

// Create a new SysLinEq with matrix 'm' and vector 'v'
// The dimension of 'v' must be equal to the number of column of 'm'
// If 'v' is null the vector null is used instead
// The matrix 'm' must be a square matrix
// Return NULL if we couldn't create the SysLinEq
SysLinEq* _SLECreate(const MatFloat* const m, const VecFloat* const v);

// Free the memory used by the SysLinEq
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that);

// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(const SysLinEq* const that);

// Solve the SysLinEq  $M \cdot x = V$ 
// Return the solution vector, or null if there is no solution or the
// arguments are invalid
#if BUILDMODE != 0
static inline
#endif
VecFloat* SysLinEqSolve(const SysLinEq* const that);

// Set the matrix of the SysLinEq to a clone of 'm'
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void SysLinEqSetM(SysLinEq* const that, const MatFloat* const m);

// Set the vector of the SysLinEq to a clone of 'v'
// Do nothing if arguments are invalid
#if BUILDMODE != 0
static inline
#endif
void _SLESetV(SysLinEq* const that, const VecFloat* const v);

// ----- Ratio

// ===== Data structure =====

// Linear system of equalities
typedef struct Ratio {

    // Components
    long _base;
    unsigned int _numerator;
    unsigned int _denominator;

} Ratio;

// ===== Functions declaration =====

// Create a new static Ratio

```

```

Ratio RatioCreateStatic(long b, unsigned int n, unsigned int d);

// Convert the float 'v' into the nearest Ratio using the Farey's algorithm
// given the precision 'prec'
Ratio RatioFromFloatPrec(float v, float prec);
#define RatioFromFloat(v) RatioFromFloatPrec((v), PBMATH_EPSILON)

// Convert the Ratio 'that' into a float
float RatioToFloat(const Ratio* that);

// Reduce the fractional part of the Ratio 'that' and update the base such as
// numerator < denominator
void RatioReduce(Ratio* that);

// Get the base of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
long RatioGetBase(const Ratio* that);

// Get the numerator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetNumerator(const Ratio* that);

// Get the denominator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetDenominator(const Ratio* that);

// Set the base of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetBase(Ratio* that, long v);

// Set the numerator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetNumerator(Ratio* that, unsigned int v);

// Set the denominator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetDenominator(Ratio* that, unsigned int v);

// Print the Ratio on 'stream' as a+b/c
void RatioPrint(const Ratio* that, FILE* stream);
#define RatioPrintln(R, S) do{RatioPrint(R,S);fprintf(S,"\n");}while(0)

// ----- LeastSquareLinReg

// ===== Data structure =====

// Linear system of equalities
typedef struct LeastSquareLinReg {

    // Component

```



```

    const MatFloat* X;

    // Matrix for computation
    MatFloat* Xp;

    // Bias of the last computed solution
    float bias;

} LeastSquareLinReg;

// ===== Functions declaration =====

// Create a new static LeastSquareLinReg
LeastSquareLinReg LeastSquareLinRegCreateStatic(MatFloat* X);

// Free the static LeastSquareLinReg 'that'
void LeastSquareLinRegFreeStatic(LeastSquareLinReg* that);

// Compute the solution of the LeastSquareLinReg 'that' for 'Y'
VecFloat* LSLRSolve(LeastSquareLinReg* that, const VecFloat* Y);

// Set the bias of the LeastSquareLinReg 'that' to 'X'
#ifdef BUILDMODE != 0
static inline
#endif
void LSLRSetComp(LeastSquareLinReg* that, const MatFloat* X);

// Get the bias of the last computed solution of the LeastSquareLinReg 'that'
#ifdef BUILDMODE != 0
static inline
#endif
float LSLRGetBias(const LeastSquareLinReg* that);

// Return true if the LeastSquareLinReg 'that' is solvable
#ifdef BUILDMODE != 0
static inline
#endif
bool LSLRIsSolvable(const LeastSquareLinReg* that);

// ----- Usefull basic functions

// ===== Functions declaration =====

// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/does-pow-work-for-int-data-type-in-c
// does-pow-work-for-int-data-type-in-c
#ifdef BUILDMODE != 0
static inline
#endif
int powi(const int base, const int exp);

// Compute a^n, faster than std::pow for n<~100
static inline float fastpow(const float a, const int n) {
    double ret = 1.0;
    double b = a;
    for (int i = n; i--;) ret *= b;
    return (float)ret;
}

// Compute a^2
static inline float fsquare(const float a) {

```

```

    return a * a;
}

// Compute the 'iElem'-th element of the 'base'-ary version of the
// Thue-Morse sequence
// 'iElem' >= 0
// 'base' >= 2
long ThueMorseSeqGetNthElem(long iElem, long base);

// Compute the area of a triangle knowing its 3 sides length 'a', 'b', 'c'
// using the Hero's formula
double GetAreaTriangleHero(
    const double a,
    const double b,
    const double c);

// Return the Fibonacci sequence up to the 'n'-th element in a dynamically
// allocated array of unsigned long
unsigned long* GetFibonacciSeq(unsigned int n);

// Return the Fibonacci grid lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [0,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciGridLattice(
    unsigned int n,
    unsigned long* nbPoints);

// Return the Fibonacci polar lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [-1,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciPolarLattice(
    unsigned int n,
    unsigned long* nbPoints);

// Return the greatest common divisor using the Stein's algorithm
// https://en.wikipedia.org/wiki/Binary_GCD_algorithm
unsigned int GetGCD(unsigned int u, unsigned int v);

// ===== Polymorphism =====

#define VecClone(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatClone, \
    VecShort*: _VecShortClone, \
    VecLong*: _VecLongClone, \
    const VecFloat*: _VecFloatClone, \
    const VecShort*: _VecShortClone, \
    const VecLong*: _VecLongClone, \
    default: PBErrInvalidPolymorphism)(Vec)

#define VecEncodeAsJSON(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatEncodeAsJSON, \
    VecShort*: _VecShortEncodeAsJSON, \
    VecLong*: _VecLongEncodeAsJSON, \
    const VecFloat*: _VecFloatEncodeAsJSON, \
    const VecShort*: _VecShortEncodeAsJSON, \
    const VecLong*: _VecLongEncodeAsJSON, \
    default: PBErrInvalidPolymorphism)(Vec)

#define VecDecodeAsJSON(VecRef, Json) _Generic(VecRef, \
    VecFloat*: _VecFloatDecodeAsJSON, \
    VecShort*: _VecShortDecodeAsJSON, \
    VecLong*: _VecLongDecodeAsJSON, \
    const VecFloat*: _VecFloatDecodeAsJSON, \
    const VecShort*: _VecShortDecodeAsJSON, \
    const VecLong*: _VecLongDecodeAsJSON, \
    default: PBErrInvalidPolymorphism)(VecRef, Json)

```

```

    default: PBErrInvalidPolymorphism)(VecRef, Json)

#define VecLoad(VecRef, Stream) _Generic(VecRef, \
    VecFloat*: _VecFloatLoad, \
    VecShort*: _VecShortLoad, \
    VecLong*: _VecLongLoad, \
    default: PBErrInvalidPolymorphism)(VecRef, Stream)

#define VecSave(Vec, Stream, Compact) _Generic(Vec, \
    VecFloat*: _VecFloatSave, \
    VecFloat2D*: _VecFloatSave, \
    VecFloat3D*: _VecFloatSave, \
    VecShort*: _VecShortSave, \
    VecShort2D*: _VecShortSave, \
    VecShort3D*: _VecShortSave, \
    VecShort4D*: _VecShortSave, \
    VecLong*: _VecLongSave, \
    VecLong2D*: _VecLongSave, \
    VecLong3D*: _VecLongSave, \
    VecLong4D*: _VecLongSave, \
    const VecFloat*: _VecFloatSave, \
    const VecFloat2D*: _VecFloatSave, \
    const VecFloat3D*: _VecFloatSave, \
    const VecShort*: _VecShortSave, \
    const VecShort2D*: _VecShortSave, \
    const VecShort3D*: _VecShortSave, \
    const VecShort4D*: _VecShortSave, \
    const VecLong*: _VecLongSave, \
    const VecLong2D*: _VecLongSave, \
    const VecLong3D*: _VecLongSave, \
    const VecLong4D*: _VecLongSave, \
    default: PBErrInvalidPolymorphism)( \
        _Generic(Vec, \
            VecFloat2D*: (const VecFloat*)(Vec), \
            VecFloat3D*: (const VecFloat*)(Vec), \
            VecShort2D*: (const VecShort*)(Vec), \
            VecShort3D*: (const VecShort*)(Vec), \
            VecShort4D*: (const VecShort*)(Vec), \
            VecLong2D*: (const VecLong*)(Vec), \
            VecLong3D*: (const VecLong*)(Vec), \
            VecLong4D*: (const VecLong*)(Vec), \
            const VecFloat2D*: (const VecFloat*)(Vec), \
            const VecFloat3D*: (const VecFloat*)(Vec), \
            const VecShort2D*: (const VecShort*)(Vec), \
            const VecShort3D*: (const VecShort*)(Vec), \
            const VecShort4D*: (const VecShort*)(Vec), \
            const VecLong2D*: (const VecLong*)(Vec), \
            const VecLong3D*: (const VecLong*)(Vec), \
            const VecLong4D*: (const VecLong*)(Vec), \
            default: Vec), \
        Stream, Compact)

#define VecFree(VecRef) _Generic(VecRef, \
    VecFloat*: _VecFloatFree, \
    VecShort*: _VecShortFree, \
    VecLong*: _VecLongFree, \
    default: PBErrInvalidPolymorphism)(VecRef)

#define VecPrint(Vec, Stream) _Generic(Vec, \
    VecFloat*: _VecFloatPrintDef, \
    VecFloat2D*: _VecFloatPrintDef, \
    VecFloat3D*: _VecFloatPrintDef, \

```

```

VecShort*: _VecShortPrint, \
VecShort2D*: _VecShortPrint, \
VecShort3D*: _VecShortPrint, \
VecShort4D*: _VecShortPrint, \
VecLong*: _VecLongPrint, \
VecLong2D*: _VecLongPrint, \
VecLong3D*: _VecLongPrint, \
VecLong4D*: _VecLongPrint, \
const VecFloat*: _VecFloatPrintDef, \
const VecFloat2D*: _VecFloatPrintDef, \
const VecFloat3D*: _VecFloatPrintDef, \
const VecShort*: _VecShortPrint, \
const VecShort2D*: _VecShortPrint, \
const VecShort3D*: _VecShortPrint, \
const VecShort4D*: _VecShortPrint, \
const VecLong*: _VecLongPrint, \
const VecLong2D*: _VecLongPrint, \
const VecLong3D*: _VecLongPrint, \
const VecLong4D*: _VecLongPrint, \
default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
        VecFloat2D*: (const VecFloat*)(Vec), \
        VecFloat3D*: (const VecFloat*)(Vec), \
        VecShort2D*: (const VecShort*)(Vec), \
        VecShort3D*: (const VecShort*)(Vec), \
        VecShort4D*: (const VecShort*)(Vec), \
        VecLong2D*: (const VecLong*)(Vec), \
        VecLong3D*: (const VecLong*)(Vec), \
        VecLong4D*: (const VecLong*)(Vec), \
        const VecFloat2D*: (const VecFloat*)(Vec), \
        const VecFloat3D*: (const VecFloat*)(Vec), \
        const VecShort2D*: (const VecShort*)(Vec), \
        const VecShort3D*: (const VecShort*)(Vec), \
        const VecShort4D*: (const VecShort*)(Vec), \
        const VecLong2D*: (const VecLong*)(Vec), \
        const VecLong3D*: (const VecLong*)(Vec), \
        const VecLong4D*: (const VecLong*)(Vec), \
        default: Vec), \
    Stream)

#define VecPrintln(V, S) do {VecPrint(V, S); fprintf(S, "\n");} while(0)

#define VecGet(Vec, Index) _Generic(Vec, \
    VecFloat*: _VecFloatGet, \
    VecFloat2D*: _VecFloatGet2D, \
    VecFloat3D*: _VecFloatGet3D, \
    VecShort*: _VecShortGet, \
    VecShort2D*: _VecShortGet2D, \
    VecShort3D*: _VecShortGet3D, \
    VecShort4D*: _VecShortGet4D, \
    VecLong*: _VecLongGet, \
    VecLong2D*: _VecLongGet2D, \
    VecLong3D*: _VecLongGet3D, \
    VecLong4D*: _VecLongGet4D, \
    const VecFloat*: _VecFloatGet, \
    const VecFloat2D*: _VecFloatGet2D, \
    const VecFloat3D*: _VecFloatGet3D, \
    const VecShort*: _VecShortGet, \
    const VecShort2D*: _VecShortGet2D, \
    const VecShort3D*: _VecShortGet3D, \
    const VecShort4D*: _VecShortGet4D, \
    const VecLong*: _VecLongGet, \

```

```

const VecLong2D*: _VecLongGet2D, \
const VecLong3D*: _VecLongGet3D, \
const VecLong4D*: _VecLongGet4D, \
default: PBErrInvalidPolymorphism)(Vec, Index)

#define VecSet(Vec, Index, Val) _Generic(Vec, \
    VecFloat*: _VecFloatSet, \
    VecFloat2D*: _VecFloatSet2D, \
    VecFloat3D*: _VecFloatSet3D, \
    VecShort*: _VecShortSet, \
    VecShort2D*: _VecShortSet2D, \
    VecShort3D*: _VecShortSet3D, \
    VecShort4D*: _VecShortSet4D, \
    VecLong*: _VecLongSet, \
    VecLong2D*: _VecLongSet2D, \
    VecLong3D*: _VecLongSet3D, \
    VecLong4D*: _VecLongSet4D, \
    default: PBErrInvalidPolymorphism)(Vec, Index, Val)

#define VecSetAdd(Vec, Index, Val) _Generic(Vec, \
    VecFloat*: _VecFloatSetAdd, \
    VecFloat2D*: _VecFloatSetAdd2D, \
    VecFloat3D*: _VecFloatSetAdd3D, \
    VecShort*: _VecShortSetAdd, \
    VecShort2D*: _VecShortSetAdd2D, \
    VecShort3D*: _VecShortSetAdd3D, \
    VecShort4D*: _VecShortSetAdd4D, \
    VecLong*: _VecLongSetAdd, \
    VecLong2D*: _VecLongSetAdd2D, \
    VecLong3D*: _VecLongSetAdd3D, \
    VecLong4D*: _VecLongSetAdd4D, \
    default: PBErrInvalidPolymorphism)(Vec, Index, Val)

#define VecSetNull(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatSetNull, \
    VecFloat2D*: _VecFloatSetNull, \
    VecFloat3D*: _VecFloatSetNull, \
    VecShort*: _VecShortSetNull, \
    VecShort2D*: _VecShortSetNull, \
    VecShort3D*: _VecShortSetNull, \
    VecShort4D*: _VecShortSetNull, \
    VecLong*: _VecLongSetNull, \
    VecLong2D*: _VecLongSetNull, \
    VecLong3D*: _VecLongSetNull, \
    VecLong4D*: _VecLongSetNull, \
    default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
        VecFloat2D*: (VecFloat*)(Vec), \
        VecFloat3D*: (VecFloat*)(Vec), \
        VecShort2D*: (VecShort*)(Vec), \
        VecShort3D*: (VecShort*)(Vec), \
        VecShort4D*: (VecShort*)(Vec), \
        VecLong2D*: (VecLong*)(Vec), \
        VecLong3D*: (VecLong*)(Vec), \
        VecLong4D*: (VecLong*)(Vec), \
        default: Vec))

#define VecSetAll(Vec, Val) _Generic(Vec, \
    VecFloat*: _VecFloatSetAll, \
    VecFloat2D*: _VecFloatSetAll, \
    VecFloat3D*: _VecFloatSetAll, \
    VecShort*: _VecShortSetAll, \

```

```

VecShort2D*: _VecShortSetAll, \
VecShort3D*: _VecShortSetAll, \
VecShort4D*: _VecShortSetAll, \
VecLong*: _VecLongSetAll, \
VecLong2D*: _VecLongSetAll, \
VecLong3D*: _VecLongSetAll, \
VecLong4D*: _VecLongSetAll, \
default: PBErriInvalidPolymorphism)( \
    _Generic(Vec, \
        VecFloat2D*: (VecFloat*)(Vec), \
        VecFloat3D*: (VecFloat*)(Vec), \
        VecShort2D*: (VecShort*)(Vec), \
        VecShort3D*: (VecShort*)(Vec), \
        VecShort4D*: (VecShort*)(Vec), \
        VecLong2D*: (VecLong*)(Vec), \
        VecLong3D*: (VecLong*)(Vec), \
        VecLong4D*: (VecLong*)(Vec), \
        default: Vec), Val)

#define VecCopy(VecDest, VecSrc) _Generic(VecDest, \
    VecFloat*: _Generic(VecSrc, \
        VecFloat*: _VecFloatCopy, \
        VecFloat2D*: _VecFloatCopy, \
        VecFloat3D*: _VecFloatCopy, \
        const VecFloat*: _VecFloatCopy, \
        const VecFloat2D*: _VecFloatCopy, \
        const VecFloat3D*: _VecFloatCopy, \
        default: PBErriInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecSrc, \
        VecFloat*: _VecFloatCopy, \
        VecFloat2D*: _VecFloatCopy, \
        const VecFloat*: _VecFloatCopy, \
        const VecFloat2D*: _VecFloatCopy, \
        default: PBErriInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecSrc, \
        VecFloat*: _VecFloatCopy, \
        VecFloat3D*: _VecFloatCopy, \
        const VecFloat*: _VecFloatCopy, \
        const VecFloat3D*: _VecFloatCopy, \
        default: PBErriInvalidPolymorphism), \
    VecShort*: _Generic(VecSrc, \
        VecShort*: _VecShortCopy, \
        VecShort2D*: _VecShortCopy, \
        VecShort3D*: _VecShortCopy, \
        VecShort4D*: _VecShortCopy, \
        const VecShort*: _VecShortCopy, \
        const VecShort2D*: _VecShortCopy, \
        const VecShort3D*: _VecShortCopy, \
        const VecShort4D*: _VecShortCopy, \
        default: PBErriInvalidPolymorphism), \
    VecShort2D*: _Generic(VecSrc, \
        VecShort*: _VecShortCopy, \
        VecShort2D*: _VecShortCopy, \
        const VecShort*: _VecShortCopy, \
        const VecShort2D*: _VecShortCopy, \
        default: PBErriInvalidPolymorphism), \
    VecShort3D*: _Generic(VecSrc, \
        VecShort*: _VecShortCopy, \
        VecShort3D*: _VecShortCopy, \
        const VecShort*: _VecShortCopy, \
        const VecShort3D*: _VecShortCopy, \
        default: PBErriInvalidPolymorphism), \

```

```

VecShort4D*: _Generic(VecSrc, \
    VecShort*: _VecShortCopy, \
    VecShort4D*: _VecShortCopy, \
    const VecShort*: _VecShortCopy, \
    const VecShort4D*: _VecShortCopy, \
    default: PBErrInvalidPolymorphism), \
VecLong*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong2D*: _VecLongCopy, \
    VecLong3D*: _VecLongCopy, \
    VecLong4D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong2D*: _VecLongCopy, \
    const VecLong3D*: _VecLongCopy, \
    const VecLong4D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
VecLong2D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong2D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong2D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
VecLong3D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong3D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong3D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
VecLong4D*: _Generic(VecSrc, \
    VecLong*: _VecLongCopy, \
    VecLong4D*: _VecLongCopy, \
    const VecLong*: _VecLongCopy, \
    const VecLong4D*: _VecLongCopy, \
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)( \
    _Generic(VecDest, \
        VecFloat2D*: (VecFloat*)(VecDest), \
        VecFloat3D*: (VecFloat*)(VecDest), \
        VecShort2D*: (VecShort*)(VecDest), \
        VecShort3D*: (VecShort*)(VecDest), \
        VecShort4D*: (VecShort*)(VecDest), \
        VecLong2D*: (VecLong*)(VecDest), \
        VecLong3D*: (VecLong*)(VecDest), \
        VecLong4D*: (VecLong*)(VecDest), \
        default: VecDest), \
    _Generic(VecSrc, \
        VecFloat2D*: (const VecFloat*)(VecSrc), \
        VecFloat3D*: (const VecFloat*)(VecSrc), \
        VecShort2D*: (const VecShort*)(VecSrc), \
        VecShort3D*: (const VecShort*)(VecSrc), \
        VecShort4D*: (const VecShort*)(VecSrc), \
        VecLong2D*: (const VecLong*)(VecSrc), \
        VecLong3D*: (const VecLong*)(VecSrc), \
        VecLong4D*: (const VecLong*)(VecSrc), \
        const VecFloat2D*: (const VecFloat*)(VecSrc), \
        const VecFloat3D*: (const VecFloat*)(VecSrc), \
        const VecShort2D*: (const VecShort*)(VecSrc), \
        const VecShort3D*: (const VecShort*)(VecSrc), \
        const VecShort4D*: (const VecShort*)(VecSrc), \
        const VecLong2D*: (const VecLong*)(VecSrc), \
        const VecLong3D*: (const VecLong*)(VecSrc), \
        const VecLong4D*: (const VecLong*)(VecSrc), \

```

```

        default: VecSrc))

#define VecGetDim(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatGetDim, \
    VecFloat2D*: _VecFloatGetDim, \
    VecFloat3D*: _VecFloatGetDim, \
    VecShort*: _VecShortGetDim, \
    VecShort2D*: _VecShortGetDim, \
    VecShort3D*: _VecShortGetDim, \
    VecShort4D*: _VecShortGetDim, \
    VecLong*: _VecLongGetDim, \
    VecLong2D*: _VecLongGetDim, \
    VecLong3D*: _VecLongGetDim, \
    VecLong4D*: _VecLongGetDim, \
    const VecFloat*: _VecFloatGetDim, \
    const VecFloat2D*: _VecFloatGetDim, \
    const VecFloat3D*: _VecFloatGetDim, \
    const VecShort*: _VecShortGetDim, \
    const VecShort2D*: _VecShortGetDim, \
    const VecShort3D*: _VecShortGetDim, \
    const VecShort4D*: _VecShortGetDim, \
    const VecLong*: _VecLongGetDim, \
    const VecLong2D*: _VecLongGetDim, \
    const VecLong3D*: _VecLongGetDim, \
    const VecLong4D*: _VecLongGetDim, \
    default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
        VecFloat*: (const VecFloat*)(Vec), \
        VecFloat2D*: (const VecFloat*)(Vec), \
        VecFloat3D*: (const VecFloat*)(Vec), \
        VecShort*: (const VecShort*)(Vec), \
        VecShort2D*: (const VecShort*)(Vec), \
        VecShort3D*: (const VecShort*)(Vec), \
        VecShort4D*: (const VecShort*)(Vec), \
        VecLong*: (const VecLong*)(Vec), \
        VecLong2D*: (const VecLong*)(Vec), \
        VecLong3D*: (const VecLong*)(Vec), \
        VecLong4D*: (const VecLong*)(Vec), \
        const VecFloat2D*: (const VecFloat*)(Vec), \
        const VecFloat3D*: (const VecFloat*)(Vec), \
        const VecShort2D*: (const VecShort*)(Vec), \
        const VecShort3D*: (const VecShort*)(Vec), \
        const VecShort4D*: (const VecShort*)(Vec), \
        const VecLong2D*: (const VecLong*)(Vec), \
        const VecLong3D*: (const VecLong*)(Vec), \
        const VecLong4D*: (const VecLong*)(Vec), \
        default: Vec))

#define VecGetNewDim(Vec, Dim) _Generic(Vec, \
    VecFloat*: _VecFloatGetNewDim, \
    const VecFloat*: _VecFloatGetNewDim, \
    VecLong*: _VecLongGetNewDim, \
    const VecLong*: _VecLongGetNewDim, \
    default: PBErrInvalidPolymorphism)( \
    _Generic(Vec, \
        VecFloat*: Vec, \
        const VecFloat*: Vec, \
        VecLong*: Vec, \
        const VecLong*: Vec, \
        default: Vec), Dim)

#define VecNorm(Vec) _Generic(Vec, \

```



```

VecFloat*: _VecFloatNorm, \
VecFloat2D*: _VecFloatNorm2D, \
VecFloat3D*: _VecFloatNorm3D, \
const VecFloat*: _VecFloatNorm, \
const VecFloat2D*: _VecFloatNorm2D, \
const VecFloat3D*: _VecFloatNorm3D, \
default: PBErrInvalidPolymorphism)(Vec)

#define VecNormalise(Vec) _Generic(Vec, \
VecFloat*: _VecFloatNormalise, \
VecFloat2D*: _VecFloatNormalise2D, \
VecFloat3D*: _VecFloatNormalise3D, \
default: PBErrInvalidPolymorphism)(Vec)

#define VecDist(VecA, VecB) _Generic(VecA, \
VecFloat*: _Generic(VecB, \
VecFloat*: _VecFloatDist, \
const VecFloat*: _VecFloatDist, \
default: PBErrInvalidPolymorphism), \
VecFloat2D*: _Generic(VecB, \
VecFloat2D*: _VecFloatDist2D, \
const VecFloat2D*: _VecFloatDist2D, \
default: PBErrInvalidPolymorphism), \
VecFloat3D*: _Generic(VecB, \
VecFloat3D*: _VecFloatDist3D, \
const VecFloat3D*: _VecFloatDist3D, \
default: PBErrInvalidPolymorphism), \
VecShort*: _Generic(VecB, \
VecShort*: _VecShortHamiltonDist, \
const VecShort*: _VecShortHamiltonDist, \
default: PBErrInvalidPolymorphism), \
VecShort2D*: _Generic(VecB, \
VecShort2D*: _VecShortHamiltonDist2D, \
const VecShort2D*: _VecShortHamiltonDist2D, \
default: PBErrInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
VecShort3D*: _VecShortHamiltonDist3D, \
const VecShort3D*: _VecShortHamiltonDist3D, \
default: PBErrInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
VecShort4D*: _VecShortHamiltonDist4D, \
const VecShort4D*: _VecShortHamiltonDist4D, \
default: PBErrInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
VecLong*: _VecLongHamiltonDist, \
const VecLong*: _VecLongHamiltonDist, \
default: PBErrInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
VecLong2D*: _VecLongHamiltonDist2D, \
const VecLong2D*: _VecLongHamiltonDist2D, \
default: PBErrInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
VecLong3D*: _VecLongHamiltonDist3D, \
const VecLong3D*: _VecLongHamiltonDist3D, \
default: PBErrInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
VecLong4D*: _VecLongHamiltonDist4D, \
const VecLong4D*: _VecLongHamiltonDist4D, \
default: PBErrInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
VecFloat*: _VecFloatDist, \
const VecFloat*: _VecFloatDist, \

```

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        default: PBErInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatDist2D, \
    const VecFloat2D*: _VecFloatDist2D, \
    default: PBErInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatDist3D, \
    const VecFloat3D*: _VecFloatDist3D, \
    default: PBErInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHamiltonDist,\
    const VecShort*: _VecShortHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHamiltonDist2D,\
    const VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    const VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    const VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHamiltonDist,\
    const VecLong*: _VecLongHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHamiltonDist2D,\
    const VecLong2D*: _VecLongHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHamiltonDist3D,\
    const VecLong3D*: _VecLongHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHamiltonDist4D,\
    const VecLong4D*: _VecLongHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
default: PBErInvalidPolymorphism)(VecA, VecB)

#define VecHamiltonDist(VecA, VecB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatHamiltonDist, \
        const VecFloat*: _VecFloatHamiltonDist, \
        default: PBErInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatHamiltonDist2D, \
        const VecFloat2D*: _VecFloatHamiltonDist2D, \
        default: PBErInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat3D*: _VecFloatHamiltonDist3D, \
        const VecFloat3D*: _VecFloatHamiltonDist3D, \
        default: PBErInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortHamiltonDist,\
        const VecShort*: _VecShortHamiltonDist,\
        default: PBErInvalidPolymorphism), \
    VecShort2D*: _Generic(VecB, \
        VecShort2D*: _VecShortHamiltonDist2D,\

```

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    const VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    const VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    const VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHamiltonDist,\
    const VecLong*: _VecLongHamiltonDist,\
    default: PBErInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHamiltonDist2D,\
    const VecLong2D*: _VecLongHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHamiltonDist3D,\
    const VecLong3D*: _VecLongHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHamiltonDist4D,\
    const VecLong4D*: _VecLongHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatHamiltonDist, \
    const VecFloat*: _VecFloatHamiltonDist, \
    default: PBErInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatHamiltonDist2D, \
    const VecFloat2D*: _VecFloatHamiltonDist2D, \
    default: PBErInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatHamiltonDist3D, \
    const VecFloat3D*: _VecFloatHamiltonDist3D, \
    default: PBErInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHamiltonDist,\
    const VecShort*: _VecShortHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHamiltonDist2D,\
    const VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    const VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    const VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHamiltonDist,\
    const VecLong*: _VecLongHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHamiltonDist2D,\
    const VecLong2D*: _VecLongHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \

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const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHamiltonDist3D,\
    const VecLong3D*: _VecLongHamiltonDist3D,\
    default: PBErrInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHamiltonDist4D,\
    const VecLong4D*: _VecLongHamiltonDist4D,\
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)(VecA, VecB)

#define VecPixelDist(VecA, VecB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatPixelDist, \
        const VecFloat*: _VecFloatPixelDist, \
        default: PBErrInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatPixelDist2D, \
        const VecFloat2D*: _VecFloatPixelDist2D, \
        default: PBErrInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat3D*: _VecFloatPixelDist3D, \
        const VecFloat3D*: _VecFloatPixelDist3D, \
        default: PBErrInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortHamiltonDist,\
        const VecShort*: _VecShortHamiltonDist,\
        default: PBErrInvalidPolymorphism), \
    VecShort2D*: _Generic(VecB, \
        VecShort2D*: _VecShortHamiltonDist2D,\
        const VecShort2D*: _VecShortHamiltonDist2D,\
        default: PBErrInvalidPolymorphism), \
    VecShort3D*: _Generic(VecB, \
        VecShort3D*: _VecShortHamiltonDist3D,\
        const VecShort3D*: _VecShortHamiltonDist3D,\
        default: PBErrInvalidPolymorphism), \
    VecShort4D*: _Generic(VecB, \
        VecShort4D*: _VecShortHamiltonDist4D,\
        const VecShort4D*: _VecShortHamiltonDist4D,\
        default: PBErrInvalidPolymorphism), \
    VecLong*: _Generic(VecB, \
        VecLong*: _VecLongHamiltonDist,\
        const VecLong*: _VecLongHamiltonDist,\
        default: PBErrInvalidPolymorphism), \
    VecLong2D*: _Generic(VecB, \
        VecLong2D*: _VecLongHamiltonDist2D,\
        const VecLong2D*: _VecLongHamiltonDist2D,\
        default: PBErrInvalidPolymorphism), \
    VecLong3D*: _Generic(VecB, \
        VecLong3D*: _VecLongHamiltonDist3D,\
        const VecLong3D*: _VecLongHamiltonDist3D,\
        default: PBErrInvalidPolymorphism), \
    VecLong4D*: _Generic(VecB, \
        VecLong4D*: _VecLongHamiltonDist4D,\
        const VecLong4D*: _VecLongHamiltonDist4D,\
        default: PBErrInvalidPolymorphism), \
    const VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatPixelDist, \
        const VecFloat*: _VecFloatPixelDist, \
        default: PBErrInvalidPolymorphism), \
    const VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatPixelDist2D, \
        const VecFloat2D*: _VecFloatPixelDist2D, \

```

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        default: PBErInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatPixelDist3D, \
    const VecFloat3D*: _VecFloatPixelDist3D, \
    default: PBErInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHamiltonDist,\
    const VecShort*: _VecShortHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHamiltonDist2D,\
    const VecShort2D*: _VecShortHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHamiltonDist3D,\
    const VecShort3D*: _VecShortHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHamiltonDist4D,\
    const VecShort4D*: _VecShortHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHamiltonDist,\
    const VecLong*: _VecLongHamiltonDist,\
    default: PBErInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHamiltonDist2D,\
    const VecLong2D*: _VecLongHamiltonDist2D,\
    default: PBErInvalidPolymorphism), \
const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHamiltonDist3D,\
    const VecLong3D*: _VecLongHamiltonDist3D,\
    default: PBErInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHamiltonDist4D,\
    const VecLong4D*: _VecLongHamiltonDist4D,\
    default: PBErInvalidPolymorphism), \
default: PBErInvalidPolymorphism)(VecA, VecB)

#define VecIsEqual(VecA, VecB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatIsEqual, \
        VecFloat2D*: _VecFloatIsEqual, \
        VecFloat3D*: _VecFloatIsEqual, \
        const VecFloat*: _VecFloatIsEqual, \
        const VecFloat2D*: _VecFloatIsEqual, \
        const VecFloat3D*: _VecFloatIsEqual, \
        default: PBErInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat*: _VecFloatIsEqual, \
        VecFloat2D*: _VecFloatIsEqual, \
        const VecFloat*: _VecFloatIsEqual, \
        const VecFloat2D*: _VecFloatIsEqual, \
        default: PBErInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat*: _VecFloatIsEqual, \
        VecFloat3D*: _VecFloatIsEqual, \
        const VecFloat*: _VecFloatIsEqual, \
        const VecFloat3D*: _VecFloatIsEqual, \
        default: PBErInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortIsEqual,\

```

```

VecShort2D*: _VecShortIsEqual, \
VecShort3D*: _VecShortIsEqual, \
VecShort4D*: _VecShortIsEqual, \
const VecShort*: _VecShortIsEqual, \
const VecShort2D*: _VecShortIsEqual, \
const VecShort3D*: _VecShortIsEqual, \
const VecShort4D*: _VecShortIsEqual, \
default: PBErInvalidPolymorphism), \
VecShort2D*: _Generic(VecB, \
VecShort*: _VecShortIsEqual, \
VecShort2D*: _VecShortIsEqual, \
const VecShort*: _VecShortIsEqual, \
const VecShort2D*: _VecShortIsEqual, \
default: PBErInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
VecShort*: _VecShortIsEqual, \
VecShort3D*: _VecShortIsEqual, \
const VecShort*: _VecShortIsEqual, \
const VecShort3D*: _VecShortIsEqual, \
default: PBErInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
VecShort*: _VecShortIsEqual, \
VecShort4D*: _VecShortIsEqual, \
const VecShort*: _VecShortIsEqual, \
const VecShort4D*: _VecShortIsEqual, \
default: PBErInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
VecLong*: _VecLongIsEqual, \
VecLong2D*: _VecLongIsEqual, \
VecLong3D*: _VecLongIsEqual, \
VecLong4D*: _VecLongIsEqual, \
const VecLong*: _VecLongIsEqual, \
const VecLong2D*: _VecLongIsEqual, \
const VecLong3D*: _VecLongIsEqual, \
const VecLong4D*: _VecLongIsEqual, \
default: PBErInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
VecLong*: _VecLongIsEqual, \
VecLong2D*: _VecLongIsEqual, \
const VecLong*: _VecLongIsEqual, \
const VecLong2D*: _VecLongIsEqual, \
default: PBErInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
VecLong*: _VecLongIsEqual, \
VecLong3D*: _VecLongIsEqual, \
const VecLong*: _VecLongIsEqual, \
const VecLong3D*: _VecLongIsEqual, \
default: PBErInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
VecLong*: _VecLongIsEqual, \
VecLong4D*: _VecLongIsEqual, \
const VecLong*: _VecLongIsEqual, \
const VecLong4D*: _VecLongIsEqual, \
default: PBErInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
VecFloat*: _VecFloatIsEqual, \
VecFloat2D*: _VecFloatIsEqual, \
VecFloat3D*: _VecFloatIsEqual, \
const VecFloat*: _VecFloatIsEqual, \
const VecFloat2D*: _VecFloatIsEqual, \
const VecFloat3D*: _VecFloatIsEqual, \
default: PBErInvalidPolymorphism), \

```

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const VecFloat2D*: _Generic(VecB, \
    VecFloat*: _VecFloatIsEqual, \
    VecFloat2D*: _VecFloatIsEqual, \
    const VecFloat*: _VecFloatIsEqual, \
    const VecFloat2D*: _VecFloatIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat*: _VecFloatIsEqual, \
    VecFloat3D*: _VecFloatIsEqual, \
    const VecFloat*: _VecFloatIsEqual, \
    const VecFloat3D*: _VecFloatIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual, \
    VecShort2D*: _VecShortIsEqual, \
    VecShort3D*: _VecShortIsEqual, \
    VecShort4D*: _VecShortIsEqual, \
    const VecShort*: _VecShortIsEqual, \
    const VecShort2D*: _VecShortIsEqual, \
    const VecShort3D*: _VecShortIsEqual, \
    const VecShort4D*: _VecShortIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual, \
    VecShort2D*: _VecShortIsEqual, \
    const VecShort*: _VecShortIsEqual, \
    const VecShort2D*: _VecShortIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual, \
    VecShort3D*: _VecShortIsEqual, \
    const VecShort*: _VecShortIsEqual, \
    const VecShort3D*: _VecShortIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort*: _VecShortIsEqual, \
    VecShort4D*: _VecShortIsEqual, \
    const VecShort*: _VecShortIsEqual, \
    const VecShort4D*: _VecShortIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongIsEqual, \
    VecLong2D*: _VecLongIsEqual, \
    VecLong3D*: _VecLongIsEqual, \
    VecLong4D*: _VecLongIsEqual, \
    const VecLong*: _VecLongIsEqual, \
    const VecLong2D*: _VecLongIsEqual, \
    const VecLong3D*: _VecLongIsEqual, \
    const VecLong4D*: _VecLongIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong*: _VecLongIsEqual, \
    VecLong2D*: _VecLongIsEqual, \
    const VecLong*: _VecLongIsEqual, \
    const VecLong2D*: _VecLongIsEqual, \
    default: PBErInvalidPolymorphism), \
const VecLong3D*: _Generic(VecB, \
    VecLong*: _VecLongIsEqual, \
    VecLong3D*: _VecLongIsEqual, \
    const VecLong*: _VecLongIsEqual, \
    const VecLong3D*: _VecLongIsEqual, \
    default: PBErInvalidPolymorphism), \

```

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const VecLong4D*: _Generic(VecB, \
    VecLong*: _VecLongIsEqual, \
    VecLong4D*: _VecLongIsEqual, \
    const VecLong*: _VecLongIsEqual, \
    const VecLong4D*: _VecLongIsEqual, \
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)( \
    _Generic(VecA, \
        VecFloat2D*: (const VecFloat*)(VecA), \
        VecFloat3D*: (const VecFloat*)(VecA), \
        VecShort2D*: (const VecShort*)(VecA), \
        VecShort3D*: (const VecShort*)(VecA), \
        VecShort4D*: (const VecShort*)(VecA), \
        VecLong2D*: (const VecLong*)(VecA), \
        VecLong3D*: (const VecLong*)(VecA), \
        VecLong4D*: (const VecLong*)(VecA), \
        const VecFloat2D*: (const VecFloat*)(VecA), \
        const VecFloat3D*: (const VecFloat*)(VecA), \
        const VecShort2D*: (const VecShort*)(VecA), \
        const VecShort3D*: (const VecShort*)(VecA), \
        const VecShort4D*: (const VecShort*)(VecA), \
        const VecLong2D*: (const VecLong*)(VecA), \
        const VecLong3D*: (const VecLong*)(VecA), \
        const VecLong4D*: (const VecLong*)(VecA), \
        default: VecA), \
    _Generic(VecB, \
        VecFloat2D*: (const VecFloat*)(VecB), \
        VecFloat3D*: (const VecFloat*)(VecB), \
        VecShort2D*: (const VecShort*)(VecB), \
        VecShort3D*: (const VecShort*)(VecB), \
        VecShort4D*: (const VecShort*)(VecB), \
        VecLong2D*: (const VecLong*)(VecB), \
        VecLong3D*: (const VecLong*)(VecB), \
        VecLong4D*: (const VecLong*)(VecB), \
        const VecFloat2D*: (const VecFloat*)(VecB), \
        const VecFloat3D*: (const VecFloat*)(VecB), \
        const VecShort2D*: (const VecShort*)(VecB), \
        const VecShort3D*: (const VecShort*)(VecB), \
        const VecShort4D*: (const VecShort*)(VecB), \
        const VecLong2D*: (const VecLong*)(VecB), \
        const VecLong3D*: (const VecLong*)(VecB), \
        const VecLong4D*: (const VecLong*)(VecB), \
        default: VecB))

#define VecOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatOp, \
        const VecFloat*: _VecFloatOp, \
        default: PBErrInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatOp2D, \
        const VecFloat2D*: _VecFloatOp2D, \
        default: PBErrInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat3D*: _VecFloatOp3D, \
        const VecFloat3D*: _VecFloatOp3D, \
        default: PBErrInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortOp, \
        const VecShort*: _VecShortOp, \
        default: PBErrInvalidPolymorphism), \
    VecShort2D*: _Generic(VecB, \

```



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    VecShort2D*: _VecShortOp2D, \
    const VecShort2D*: _VecShortOp2D, \
    default: PBErInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortOp3D, \
    const VecShort3D*: _VecShortOp3D, \
    default: PBErInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortOp4D, \
    const VecShort4D*: _VecShortOp4D, \
    default: PBErInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
    VecLong*: _VecLongOp, \
    const VecLong*: _VecLongOp, \
    default: PBErInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongOp2D, \
    const VecLong2D*: _VecLongOp2D, \
    default: PBErInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongOp3D, \
    const VecLong3D*: _VecLongOp3D, \
    default: PBErInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongOp4D, \
    const VecLong4D*: _VecLongOp4D, \
    default: PBErInvalidPolymorphism), \
    default: PBErInvalidPolymorphism)(VecA, CoeffA, VecB, CoeffB)

#define VecGetOp(VecA, CoeffA, VecB, CoeffB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatGetOp, \
        const VecFloat*: _VecFloatGetOp, \
        default: PBErInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatGetOp2D, \
        const VecFloat2D*: _VecFloatGetOp2D, \
        default: PBErInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat3D*: _VecFloatGetOp3D, \
        const VecFloat3D*: _VecFloatGetOp3D, \
        default: PBErInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortGetOp, \
        const VecShort*: _VecShortGetOp, \
        default: PBErInvalidPolymorphism), \
    VecShort2D*: _Generic(VecB, \
        VecShort2D*: _VecShortGetOp2D, \
        const VecShort2D*: _VecShortGetOp2D, \
        default: PBErInvalidPolymorphism), \
    VecShort3D*: _Generic(VecB, \
        VecShort3D*: _VecShortGetOp3D, \
        const VecShort3D*: _VecShortGetOp3D, \
        default: PBErInvalidPolymorphism), \
    VecShort4D*: _Generic(VecB, \
        VecShort4D*: _VecShortGetOp4D, \
        const VecShort4D*: _VecShortGetOp4D, \
        default: PBErInvalidPolymorphism), \
    VecLong*: _Generic(VecB, \
        VecLong*: _VecLongGetOp, \
        const VecLong*: _VecLongGetOp, \
        default: PBErInvalidPolymorphism), \

```

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VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongGetOp2D, \
    const VecLong2D*: _VecLongGetOp2D, \
    default: PBErrInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongGetOp3D, \
    const VecLong3D*: _VecLongGetOp3D, \
    default: PBErrInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongGetOp4D, \
    const VecLong4D*: _VecLongGetOp4D, \
    default: PBErrInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatGetOp, \
    const VecFloat*: _VecFloatGetOp, \
    default: PBErrInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatGetOp2D, \
    const VecFloat2D*: _VecFloatGetOp2D, \
    default: PBErrInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatGetOp3D, \
    const VecFloat3D*: _VecFloatGetOp3D, \
    default: PBErrInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortGetOp, \
    const VecShort*: _VecShortGetOp, \
    default: PBErrInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortGetOp2D, \
    const VecShort2D*: _VecShortGetOp2D, \
    default: PBErrInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortGetOp3D, \
    const VecShort3D*: _VecShortGetOp3D, \
    default: PBErrInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortGetOp4D, \
    const VecShort4D*: _VecShortGetOp4D, \
    default: PBErrInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongGetOp, \
    const VecLong*: _VecLongGetOp, \
    default: PBErrInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongGetOp2D, \
    const VecLong2D*: _VecLongGetOp2D, \
    default: PBErrInvalidPolymorphism), \
const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongGetOp3D, \
    const VecLong3D*: _VecLongGetOp3D, \
    default: PBErrInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongGetOp4D, \
    const VecLong4D*: _VecLongGetOp4D, \
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)(VecA, CoeffA, VecB, CoeffB)

#define VecHadamardProd(VecA, VecB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatHadamardProd, \
        const VecFloat*: _VecFloatHadamardProd, \

```

```

    default: PBErInvalidPolymorphism), \
VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatHadamardProd2D, \
    const VecFloat2D*: _VecFloatHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatHadamardProd3D, \
    const VecFloat3D*: _VecFloatHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
VecShort*: _Generic(VecB, \
    VecShort*: _VecShortHadamardProd, \
    const VecShort*: _VecShortHadamardProd, \
    default: PBErInvalidPolymorphism), \
VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortHadamardProd2D, \
    const VecShort2D*: _VecShortHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortHadamardProd3D, \
    const VecShort3D*: _VecShortHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortHadamardProd4D, \
    const VecShort4D*: _VecShortHadamardProd4D, \
    default: PBErInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
    VecLong*: _VecLongHadamardProd, \
    const VecLong*: _VecLongHadamardProd, \
    default: PBErInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongHadamardProd2D, \
    const VecLong2D*: _VecLongHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongHadamardProd3D, \
    const VecLong3D*: _VecLongHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongHadamardProd4D, \
    const VecLong4D*: _VecLongHadamardProd4D, \
    default: PBErInvalidPolymorphism), \
default: PBErInvalidPolymorphism)(VecA, VecB)

#define VecGetHadamardProd(VecA, VecB) _Generic(VecA, \
    VecFloat*: _Generic(VecB, \
        VecFloat*: _VecFloatGetHadamardProd, \
        const VecFloat*: _VecFloatGetHadamardProd, \
        default: PBErInvalidPolymorphism), \
    VecFloat2D*: _Generic(VecB, \
        VecFloat2D*: _VecFloatGetHadamardProd2D, \
        const VecFloat2D*: _VecFloatGetHadamardProd2D, \
        default: PBErInvalidPolymorphism), \
    VecFloat3D*: _Generic(VecB, \
        VecFloat3D*: _VecFloatGetHadamardProd3D, \
        const VecFloat3D*: _VecFloatGetHadamardProd3D, \
        default: PBErInvalidPolymorphism), \
    VecShort*: _Generic(VecB, \
        VecShort*: _VecShortGetHadamardProd, \
        const VecShort*: _VecShortGetHadamardProd, \
        default: PBErInvalidPolymorphism), \
    VecShort2D*: _Generic(VecB, \
        VecShort2D*: _VecShortGetHadamardProd2D, \

```

```

    const VecShort2D*: _VecShortGetHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortGetHadamardProd3D, \
    const VecShort3D*: _VecShortGetHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortGetHadamardProd4D, \
    const VecShort4D*: _VecShortGetHadamardProd4D, \
    default: PBErInvalidPolymorphism), \
VecLong*: _Generic(VecB, \
    VecLong*: _VecLongGetHadamardProd, \
    const VecLong*: _VecLongGetHadamardProd, \
    default: PBErInvalidPolymorphism), \
VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongGetHadamardProd2D, \
    const VecLong2D*: _VecLongGetHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongGetHadamardProd3D, \
    const VecLong3D*: _VecLongGetHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongGetHadamardProd4D, \
    const VecLong4D*: _VecLongGetHadamardProd4D, \
    default: PBErInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
    VecFloat*: _VecFloatGetHadamardProd, \
    const VecFloat*: _VecFloatGetHadamardProd, \
    default: PBErInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
    VecFloat2D*: _VecFloatGetHadamardProd2D, \
    const VecFloat2D*: _VecFloatGetHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat3D*: _VecFloatGetHadamardProd3D, \
    const VecFloat3D*: _VecFloatGetHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
const VecShort*: _Generic(VecB, \
    VecShort*: _VecShortGetHadamardProd, \
    const VecShort*: _VecShortGetHadamardProd, \
    default: PBErInvalidPolymorphism), \
const VecShort2D*: _Generic(VecB, \
    VecShort2D*: _VecShortGetHadamardProd2D, \
    const VecShort2D*: _VecShortGetHadamardProd2D, \
    default: PBErInvalidPolymorphism), \
const VecShort3D*: _Generic(VecB, \
    VecShort3D*: _VecShortGetHadamardProd3D, \
    const VecShort3D*: _VecShortGetHadamardProd3D, \
    default: PBErInvalidPolymorphism), \
const VecShort4D*: _Generic(VecB, \
    VecShort4D*: _VecShortGetHadamardProd4D, \
    const VecShort4D*: _VecShortGetHadamardProd4D, \
    default: PBErInvalidPolymorphism), \
const VecLong*: _Generic(VecB, \
    VecLong*: _VecLongGetHadamardProd, \
    const VecLong*: _VecLongGetHadamardProd, \
    default: PBErInvalidPolymorphism), \
const VecLong2D*: _Generic(VecB, \
    VecLong2D*: _VecLongGetHadamardProd2D, \
    const VecLong2D*: _VecLongGetHadamardProd2D, \
    default: PBErInvalidPolymorphism), \

```

```

const VecLong3D*: _Generic(VecB, \
    VecLong3D*: _VecLongGetHadamardProd3D, \
    const VecLong3D*: _VecLongGetHadamardProd3D, \
    default: PBErrInvalidPolymorphism), \
const VecLong4D*: _Generic(VecB, \
    VecLong4D*: _VecLongGetHadamardProd4D, \
    const VecLong4D*: _VecLongGetHadamardProd4D, \
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)(VecA, VecB)

#define VecScale(Vec, Scale) _Generic(Vec, \
    VecFloat*: _VecFloatScale, \
    VecFloat2D*: _VecFloatScale2D, \
    VecFloat3D*: _VecFloatScale3D, \
    default: PBErrInvalidPolymorphism)(Vec, Scale)

#define VecGetScale(Vec, Scale) _Generic(Vec, \
    VecFloat*: _VecFloatGetScale, \
    const VecFloat*: _VecFloatGetScale, \
    VecFloat2D*: _VecFloatGetScale2D, \
    const VecFloat2D*: _VecFloatGetScale2D, \
    VecFloat3D*: _VecFloatGetScale3D, \
    const VecFloat3D*: _VecFloatGetScale3D, \
    default: PBErrInvalidPolymorphism)(Vec, Scale)

#define VecRot(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatRot2D, \
    VecFloat2D*: _VecFloatRot2D, \
    default: PBErrInvalidPolymorphism)((VecFloat2D*)(Vec), Theta)

#define VecGetRot(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatGetRot2D, \
    const VecFloat*: _VecFloatGetRot2D, \
    VecFloat2D*: _VecFloatGetRot2D, \
    const VecFloat2D*: _VecFloatGetRot2D, \
    default: PBErrInvalidPolymorphism)((const VecFloat2D*)(Vec), Theta)

#define VecRotAxis(Vec, Axis, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatRotAxis, \
    VecFloat3D*: _VecFloatRotAxis, \
    default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), \
    (VecFloat3D*)(Axis), Theta)

#define VecGetRotAxis(Vec, Axis, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatGetRotAxis, \
    const VecFloat*: _VecFloatGetRotAxis, \
    VecFloat3D*: _VecFloatGetRotAxis, \
    const VecFloat3D*: _VecFloatGetRotAxis, \
    default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), \
    (const VecFloat3D*)(Axis), Theta)

#define VecRotX(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatRotX, \
    VecFloat3D*: _VecFloatRotX, \
    default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)

#define VecGetRotX(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatGetRotX, \
    const VecFloat*: _VecFloatGetRotX, \
    VecFloat3D*: _VecFloatGetRotX, \
    const VecFloat3D*: _VecFloatGetRotX, \
    default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)

```

```

#define VecRotY(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatRotY, \
    VecFloat3D*: _VecFloatRotY, \
    default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)

#define VecGetRotY(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatGetRotY, \
    const VecFloat*: _VecFloatGetRotY, \
    VecFloat3D*: _VecFloatGetRotY, \
    const VecFloat3D*: _VecFloatGetRotY, \
    default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)

#define VecRotZ(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatRotZ, \
    VecFloat3D*: _VecFloatRotZ, \
    default: PBErrInvalidPolymorphism)((VecFloat3D*)(Vec), Theta)

#define VecGetRotZ(Vec, Theta) _Generic(Vec, \
    VecFloat*: _VecFloatGetRotZ, \
    const VecFloat*: _VecFloatGetRotZ, \
    VecFloat3D*: _VecFloatGetRotZ, \
    const VecFloat3D*: _VecFloatGetRotZ, \
    default: PBErrInvalidPolymorphism)((const VecFloat3D*)(Vec), Theta)

#define VecDotProd(VecA, VecB) _Generic(VecA, \
    VecShort*: _VecShortDotProd, \
    const VecShort*: _VecShortDotProd, \
    VecShort2D*: _VecShortDotProd2D, \
    const VecShort2D*: _VecShortDotProd2D, \
    VecShort3D*: _VecShortDotProd3D, \
    const VecShort3D*: _VecShortDotProd3D, \
    VecShort4D*: _VecShortDotProd4D, \
    const VecShort4D*: _VecShortDotProd4D, \
    VecLong*: _VecLongDotProd, \
    const VecLong*: _VecLongDotProd, \
    VecLong2D*: _VecLongDotProd2D, \
    const VecLong2D*: _VecLongDotProd2D, \
    VecLong3D*: _VecLongDotProd3D, \
    const VecLong3D*: _VecLongDotProd3D, \
    VecLong4D*: _VecLongDotProd4D, \
    const VecLong4D*: _VecLongDotProd4D, \
    VecFloat*: _VecFloatDotProd, \
    const VecFloat*: _VecFloatDotProd, \
    VecFloat2D*: _VecFloatDotProd2D, \
    const VecFloat2D*: _VecFloatDotProd2D, \
    VecFloat3D*: _VecFloatDotProd3D, \
    const VecFloat3D*: _VecFloatDotProd3D, \
    default: PBErrInvalidPolymorphism)(VecA, VecB) \

#define VecCrossProd(VecA, VecB) _Generic(VecA, \
    VecFloat*: _VecFloatGetCrossProd, \
    const VecFloat*: _VecFloatGetCrossProd, \
    VecFloat3D*: _VecFloatGetCrossProd3D, \
    const VecFloat3D*: _VecFloatGetCrossProd3D, \
    default: PBErrInvalidPolymorphism)(VecA, VecB) \

#define VecAngleTo(VecFrom, VecTo) _Generic(VecFrom, \
    VecFloat*: _VecFloatAngleTo2D, \
    const VecFloat*: _VecFloatAngleTo2D, \
    VecFloat2D*: _VecFloatAngleTo2D, \
    const VecFloat2D*: _VecFloatAngleTo2D, \

```

```

default: PBErrInvalidPolymorphism)((const VecFloat2D*)(VecFrom), \
    (const VecFloat2D*)(VecTo))

#define VecStep(Vec, VecBound) _Generic(Vec, \
    VecShort*: _VecShortStep, \
    VecShort2D*: _VecShortStep, \
    VecShort3D*: _VecShortStep, \
    VecShort4D*: _VecShortStep, \
    VecLong*: _VecLongStep, \
    VecLong2D*: _VecLongStep, \
    VecLong3D*: _VecLongStep, \
    VecLong4D*: _VecLongStep, \
    default: PBErrInvalidPolymorphism)(_Generic(Vec, \
    VecShort*: (VecShort*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    VecLong*: (VecLong*)(Vec), \
    VecLong2D*: (VecLong*)(Vec), \
    VecLong3D*: (VecLong*)(Vec), \
    VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
    VecShort*: (const VecShort*)(VecBound), \
    VecShort2D*: (const VecShort*)(VecBound), \
    VecShort3D*: (const VecShort*)(VecBound), \
    VecShort4D*: (const VecShort*)(VecBound), \
    const VecShort*: (const VecShort*)(VecBound), \
    const VecShort2D*: (const VecShort*)(VecBound), \
    const VecShort3D*: (const VecShort*)(VecBound), \
    const VecShort4D*: (const VecShort*)(VecBound), \
    VecLong*: (const VecLong*)(VecBound), \
    VecLong2D*: (const VecLong*)(VecBound), \
    VecLong3D*: (const VecLong*)(VecBound), \
    VecLong4D*: (const VecLong*)(VecBound), \
    const VecLong*: (const VecLong*)(VecBound), \
    const VecLong2D*: (const VecLong*)(VecBound), \
    const VecLong3D*: (const VecLong*)(VecBound), \
    const VecLong4D*: (const VecLong*)(VecBound)))

#define VecPStep(Vec, VecBound) _Generic(Vec, \
    VecShort*: _VecShortPStep, \
    VecShort2D*: _VecShortPStep, \
    VecShort3D*: _VecShortPStep, \
    VecShort4D*: _VecShortPStep, \
    VecLong*: _VecLongPStep, \
    VecLong2D*: _VecLongPStep, \
    VecLong3D*: _VecLongPStep, \
    VecLong4D*: _VecLongPStep, \
    default: PBErrInvalidPolymorphism)(_Generic(Vec, \
    VecShort*: (VecShort*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    VecLong*: (VecLong*)(Vec), \
    VecLong2D*: (VecLong*)(Vec), \
    VecLong3D*: (VecLong*)(Vec), \
    VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
    VecShort*: (const VecShort*)(VecBound), \
    VecShort2D*: (const VecShort*)(VecBound), \
    VecShort3D*: (const VecShort*)(VecBound), \
    VecShort4D*: (const VecShort*)(VecBound), \
    const VecShort*: (const VecShort*)(VecBound), \
    const VecShort2D*: (const VecShort*)(VecBound), \

```

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const VecShort3D*: (const VecShort*)(VecBound), \
const VecShort4D*: (const VecShort*)(VecBound), \
VecLong*: (const VecLong*)(VecBound), \
VecLong2D*: (const VecLong*)(VecBound), \
VecLong3D*: (const VecLong*)(VecBound), \
VecLong4D*: (const VecLong*)(VecBound), \
const VecLong*: (const VecLong*)(VecBound), \
const VecLong2D*: (const VecLong*)(VecBound), \
const VecLong3D*: (const VecLong*)(VecBound), \
const VecLong4D*: (const VecLong*)(VecBound)))

#define VecShiftStep(Vec, VecFrom, VecTo) _Generic(Vec, \
VecShort*: _VecShortShiftStep, \
VecShort2D*: _VecShortShiftStep, \
VecShort3D*: _VecShortShiftStep, \
VecShort4D*: _VecShortShiftStep, \
VecLong*: _VecLongShiftStep, \
VecLong2D*: _VecLongShiftStep, \
VecLong3D*: _VecLongShiftStep, \
VecLong4D*: _VecLongShiftStep, \
default: PBErrInvalidPolymorphism)(_Generic(Vec, \
VecShort*: (VecShort*)(Vec), \
VecShort2D*: (VecShort*)(Vec), \
VecShort3D*: (VecShort*)(Vec), \
VecShort4D*: (VecShort*)(Vec), \
VecLong*: (VecLong*)(Vec), \
VecLong2D*: (VecLong*)(Vec), \
VecLong3D*: (VecLong*)(Vec), \
VecLong4D*: (VecLong*)(Vec)), _Generic(VecFrom, \
VecShort*: (const VecShort*)(VecFrom), \
VecShort2D*: (const VecShort*)(VecFrom), \
VecShort3D*: (const VecShort*)(VecFrom), \
VecShort4D*: (const VecShort*)(VecFrom), \
const VecShort*: (const VecShort*)(VecFrom), \
const VecShort2D*: (const VecShort*)(VecFrom), \
const VecShort3D*: (const VecShort*)(VecFrom), \
const VecShort4D*: (const VecShort*)(VecFrom), \
VecLong*: (const VecLong*)(VecFrom), \
VecLong2D*: (const VecLong*)(VecFrom), \
VecLong3D*: (const VecLong*)(VecFrom), \
VecLong4D*: (const VecLong*)(VecFrom), \
const VecLong*: (const VecLong*)(VecFrom), \
const VecLong2D*: (const VecLong*)(VecFrom), \
const VecLong3D*: (const VecLong*)(VecFrom), \
const VecLong4D*: (const VecLong*)(VecFrom)), _Generic(VecTo, \
VecShort*: (const VecShort*)(VecTo), \
VecShort2D*: (const VecShort*)(VecTo), \
VecShort3D*: (const VecShort*)(VecTo), \
VecShort4D*: (const VecShort*)(VecTo), \
const VecShort*: (const VecShort*)(VecTo), \
const VecShort2D*: (const VecShort*)(VecTo), \
const VecShort3D*: (const VecShort*)(VecTo), \
const VecShort4D*: (const VecShort*)(VecTo), \
VecLong*: (const VecLong*)(VecTo), \
VecLong2D*: (const VecLong*)(VecTo), \
VecLong3D*: (const VecLong*)(VecTo), \
VecLong4D*: (const VecLong*)(VecTo), \
const VecLong*: (const VecLong*)(VecTo), \
const VecLong2D*: (const VecLong*)(VecTo), \
const VecLong3D*: (const VecLong*)(VecTo), \
const VecLong4D*: (const VecLong*)(VecTo)))

```



```

#define VecPStepDelta(Vec, VecBound, VecDelta) _Generic(Vec, \
    VecShort*: _VecShortPStepDelta, \
    VecShort2D*: _VecShortPStepDelta, \
    VecShort3D*: _VecShortPStepDelta, \
    VecShort4D*: _VecShortPStepDelta, \
    VecLong*: _VecLongPStepDelta, \
    VecLong2D*: _VecLongPStepDelta, \
    VecLong3D*: _VecLongPStepDelta, \
    VecLong4D*: _VecLongPStepDelta, \
    default: PBErrInvalidPolymorphism)(_Generic(Vec, \
    VecShort*: (VecShort*)(Vec), \
    VecShort2D*: (VecShort*)(Vec), \
    VecShort3D*: (VecShort*)(Vec), \
    VecShort4D*: (VecShort*)(Vec), \
    VecLong*: (VecLong*)(Vec), \
    VecLong2D*: (VecLong*)(Vec), \
    VecLong3D*: (VecLong*)(Vec), \
    VecLong4D*: (VecLong*)(Vec)), _Generic(VecBound, \
    VecShort*: (const VecShort*)(VecBound), \
    VecShort2D*: (const VecShort*)(VecBound), \
    VecShort3D*: (const VecShort*)(VecBound), \
    VecShort4D*: (const VecShort*)(VecBound), \
    const VecShort*: (const VecShort*)(VecBound), \
    const VecShort2D*: (const VecShort*)(VecBound), \
    const VecShort3D*: (const VecShort*)(VecBound), \
    const VecShort4D*: (const VecShort*)(VecBound), \
    VecLong*: (const VecLong*)(VecBound), \
    VecLong2D*: (const VecLong*)(VecBound), \
    VecLong3D*: (const VecLong*)(VecBound), \
    VecLong4D*: (const VecLong*)(VecBound), \
    const VecLong*: (const VecLong*)(VecBound), \
    const VecLong2D*: (const VecLong*)(VecBound), \
    const VecLong3D*: (const VecLong*)(VecBound), \
    const VecLong4D*: (const VecLong*)(VecBound)), _Generic(VecDelta, \
    VecShort*: (const VecShort*)(VecDelta), \
    VecShort2D*: (const VecShort*)(VecDelta), \
    VecShort3D*: (const VecShort*)(VecDelta), \
    VecShort4D*: (const VecShort*)(VecDelta), \
    const VecShort*: (const VecShort*)(VecDelta), \
    const VecShort2D*: (const VecShort*)(VecDelta), \
    const VecShort3D*: (const VecShort*)(VecDelta), \
    const VecShort4D*: (const VecShort*)(VecDelta), \
    VecLong*: (const VecLong*)(VecDelta), \
    VecLong2D*: (const VecLong*)(VecDelta), \
    VecLong3D*: (const VecLong*)(VecDelta), \
    VecLong4D*: (const VecLong*)(VecDelta), \
    const VecLong*: (const VecLong*)(VecDelta), \
    const VecLong2D*: (const VecLong*)(VecDelta), \
    const VecLong3D*: (const VecLong*)(VecDelta), \
    const VecLong4D*: (const VecLong*)(VecDelta)))

#define VecGetMaxVal(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatGetMaxVal, \
    const VecFloat*: _VecFloatGetMaxVal, \
    VecFloat2D*: _VecFloatGetMaxVal, \
    const VecFloat2D*: _VecFloatGetMaxVal, \
    VecFloat3D*: _VecFloatGetMaxVal, \
    const VecFloat3D*: _VecFloatGetMaxVal, \
    VecShort*: _VecShortGetMaxVal, \
    const VecShort*: _VecShortGetMaxVal, \
    VecShort2D*: _VecShortGetMaxVal, \
    const VecShort2D*: _VecShortGetMaxVal, \

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VecShort3D*: _VecShortGetMaxVal, \
const VecShort3D*: _VecShortGetMaxVal, \
VecShort4D*: _VecShortGetMaxVal, \
const VecShort4D*: _VecShortGetMaxVal, \
VecLong*: _VecLongGetMaxVal, \
const VecLong*: _VecLongGetMaxVal, \
VecLong2D*: _VecLongGetMaxVal, \
const VecLong2D*: _VecLongGetMaxVal, \
VecLong3D*: _VecLongGetMaxVal, \
const VecLong3D*: _VecLongGetMaxVal, \
VecLong4D*: _VecLongGetMaxVal, \
const VecLong4D*: _VecLongGetMaxVal, \
default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (const VecFloat*)(Vec), \
    const VecFloat2D*: (const VecFloat*)(Vec), \
    VecFloat3D*: (const VecFloat*)(Vec), \
    const VecFloat3D*: (const VecFloat*)(Vec), \
    VecShort2D*: (const VecShort*)(Vec), \
    const VecShort2D*: (const VecShort*)(Vec), \
    VecShort3D*: (const VecShort*)(Vec), \
    const VecShort3D*: (const VecShort*)(Vec), \
    VecShort4D*: (const VecShort*)(Vec), \
    const VecShort4D*: (const VecShort*)(Vec), \
    VecLong2D*: (const VecLong*)(Vec), \
    const VecLong2D*: (const VecLong*)(Vec), \
    VecLong3D*: (const VecLong*)(Vec), \
    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))

#define VecGetMinVal(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatGetMinVal, \
    const VecFloat*: _VecFloatGetMinVal, \
    VecFloat2D*: _VecFloatGetMinVal, \
    const VecFloat2D*: _VecFloatGetMinVal, \
    VecFloat3D*: _VecFloatGetMinVal, \
    const VecFloat3D*: _VecFloatGetMinVal, \
    VecShort*: _VecShortGetMinVal, \
    const VecShort*: _VecShortGetMinVal, \
    VecShort2D*: _VecShortGetMinVal, \
    const VecShort2D*: _VecShortGetMinVal, \
    VecShort3D*: _VecShortGetMinVal, \
    const VecShort3D*: _VecShortGetMinVal, \
    VecShort4D*: _VecShortGetMinVal, \
    const VecShort4D*: _VecShortGetMinVal, \
    VecLong*: _VecLongGetMinVal, \
    const VecLong*: _VecLongGetMinVal, \
    VecLong2D*: _VecLongGetMinVal, \
    const VecLong2D*: _VecLongGetMinVal, \
    VecLong3D*: _VecLongGetMinVal, \
    const VecLong3D*: _VecLongGetMinVal, \
    VecLong4D*: _VecLongGetMinVal, \
    const VecLong4D*: _VecLongGetMinVal, \
    default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (const VecFloat*)(Vec), \
    const VecFloat2D*: (const VecFloat*)(Vec), \
    VecFloat3D*: (const VecFloat*)(Vec), \
    const VecFloat3D*: (const VecFloat*)(Vec), \
    VecShort2D*: (const VecShort*)(Vec), \
    const VecShort2D*: (const VecShort*)(Vec), \
    VecShort3D*: (const VecShort*)(Vec), \

```

```

    const VecShort3D*: (const VecShort*)(Vec), \
    VecShort4D*: (const VecShort*)(Vec), \
    const VecShort4D*: (const VecShort*)(Vec), \
    VecLong2D*: (const VecLong*)(Vec), \
    const VecLong2D*: (const VecLong*)(Vec), \
    VecLong3D*: (const VecLong*)(Vec), \
    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))

#define VecGetMaxValAbs(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatGetMaxValAbs, \
    const VecFloat*: _VecFloatGetMaxValAbs, \
    VecFloat2D*: _VecFloatGetMaxValAbs, \
    const VecFloat2D*: _VecFloatGetMaxValAbs, \
    VecFloat3D*: _VecFloatGetMaxValAbs, \
    const VecFloat3D*: _VecFloatGetMaxValAbs, \
    VecShort*: _VecShortGetMaxValAbs, \
    const VecShort*: _VecShortGetMaxValAbs, \
    VecShort2D*: _VecShortGetMaxValAbs, \
    const VecShort2D*: _VecShortGetMaxValAbs, \
    VecShort3D*: _VecShortGetMaxValAbs, \
    const VecShort3D*: _VecShortGetMaxValAbs, \
    VecShort4D*: _VecShortGetMaxValAbs, \
    const VecShort4D*: _VecShortGetMaxValAbs, \
    VecLong*: _VecLongGetMaxValAbs, \
    const VecLong*: _VecLongGetMaxValAbs, \
    VecLong2D*: _VecLongGetMaxValAbs, \
    const VecLong2D*: _VecLongGetMaxValAbs, \
    VecLong3D*: _VecLongGetMaxValAbs, \
    const VecLong3D*: _VecLongGetMaxValAbs, \
    VecLong4D*: _VecLongGetMaxValAbs, \
    const VecLong4D*: _VecLongGetMaxValAbs, \
    default: PBErrInvalidPolymorphism) (_Generic(Vec, \
    VecFloat2D*: (const VecFloat*)(Vec), \
    const VecFloat2D*: (const VecFloat*)(Vec), \
    VecFloat3D*: (const VecFloat*)(Vec), \
    const VecFloat3D*: (const VecFloat*)(Vec), \
    VecShort2D*: (const VecShort*)(Vec), \
    const VecShort2D*: (const VecShort*)(Vec), \
    VecShort3D*: (const VecShort*)(Vec), \
    const VecShort3D*: (const VecShort*)(Vec), \
    VecShort4D*: (const VecShort*)(Vec), \
    const VecShort4D*: (const VecShort*)(Vec), \
    VecLong2D*: (const VecLong*)(Vec), \
    const VecLong2D*: (const VecLong*)(Vec), \
    VecLong3D*: (const VecLong*)(Vec), \
    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))

#define VecGetMinValAbs(Vec) _Generic(Vec, \
    VecFloat*: _VecFloatGetMinValAbs, \
    const VecFloat*: _VecFloatGetMinValAbs, \
    VecFloat2D*: _VecFloatGetMinValAbs, \
    const VecFloat2D*: _VecFloatGetMinValAbs, \
    VecFloat3D*: _VecFloatGetMinValAbs, \
    const VecFloat3D*: _VecFloatGetMinValAbs, \
    VecShort*: _VecShortGetMinValAbs, \
    const VecShort*: _VecShortGetMinValAbs, \

```

```

VecShort2D*: _VecShortGetMinValAbs, \
const VecShort2D*: _VecShortGetMinValAbs, \
VecShort3D*: _VecShortGetMinValAbs, \
const VecShort3D*: _VecShortGetMinValAbs, \
VecShort4D*: _VecShortGetMinValAbs, \
const VecShort4D*: _VecShortGetMinValAbs, \
VecLong*: _VecLongGetMinValAbs, \
const VecLong*: _VecLongGetMinValAbs, \
VecLong2D*: _VecLongGetMinValAbs, \
const VecLong2D*: _VecLongGetMinValAbs, \
VecLong3D*: _VecLongGetMinValAbs, \
const VecLong3D*: _VecLongGetMinValAbs, \
VecLong4D*: _VecLongGetMinValAbs, \
const VecLong4D*: _VecLongGetMinValAbs, \
default: PBErrInvalidPolymorphism)(_Generic(Vec, \
    VecFloat2D*: (const VecFloat*)(Vec), \
    const VecFloat2D*: (const VecFloat*)(Vec), \
    VecFloat3D*: (const VecFloat*)(Vec), \
    const VecFloat3D*: (const VecFloat*)(Vec), \
    VecShort2D*: (const VecShort*)(Vec), \
    const VecShort2D*: (const VecShort*)(Vec), \
    VecShort3D*: (const VecShort*)(Vec), \
    const VecShort3D*: (const VecShort*)(Vec), \
    VecShort4D*: (const VecShort*)(Vec), \
    const VecShort4D*: (const VecShort*)(Vec), \
    VecLong2D*: (const VecLong*)(Vec), \
    const VecLong2D*: (const VecLong*)(Vec), \
    VecLong3D*: (const VecLong*)(Vec), \
    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))

#define VecStepDelta(Vec, VecBound, Delta) _Generic(Vec, \
    VecFloat*: _VecFloatStepDelta, \
    VecFloat2D*: _VecFloatStepDelta, \
    VecFloat3D*: _VecFloatStepDelta, \
    VecShort*: _VecShortStepDelta, \
    VecShort2D*: _VecShortStepDelta, \
    VecShort3D*: _VecShortStepDelta, \
    VecShort4D*: _VecShortStepDelta, \
    VecLong*: _VecLongStepDelta, \
    VecLong2D*: _VecLongStepDelta, \
    VecLong3D*: _VecLongStepDelta, \
    VecLong4D*: _VecLongStepDelta, \
    default: PBErrInvalidPolymorphism)(_Generic(Vec, \
        VecFloat*: Vec, \
        VecFloat2D*: (VecFloat*)(Vec), \
        VecFloat3D*: (VecFloat*)(Vec), \
        VecShort*: Vec, \
        VecShort2D*: (VecShort*)(Vec), \
        VecShort3D*: (VecShort*)(Vec), \
        VecShort4D*: (VecShort*)(Vec), \
        VecLong*: Vec, \
        VecLong2D*: (VecLong*)(Vec), \
        VecLong3D*: (VecLong*)(Vec), \
        VecLong4D*: (VecLong*)(Vec)), _Generic(Vec, \
        VecFloat*: VecBound, \
        VecFloat2D*: (VecFloat*)(VecBound), \
        VecFloat3D*: (VecFloat*)(VecBound), \
        VecShort*: VecBound, \
        VecShort2D*: (VecShort*)(VecBound), \

```

```

VecShort3D*: (VecShort*)(VecBound), \
VecShort4D*: (VecShort*)(VecBound), \
VecLong*: VecBound, \
VecLong2D*: (VecLong*)(VecBound), \
VecLong3D*: (VecLong*)(VecBound), \
VecLong4D*: (VecLong*)(VecBound)), _Generic(Vec, \
VecFloat*: Delta, \
VecFloat2D*: (VecFloat*)(Delta), \
VecFloat3D*: (VecFloat*)(Delta), \
VecShort*: Delta, \
VecShort2D*: (VecShort*)(Delta), \
VecShort3D*: (VecShort*)(Delta), \
VecShort4D*: (VecShort*)(Delta), \
VecLong*: Delta, \
VecLong2D*: (VecLong*)(Delta), \
VecLong3D*: (VecLong*)(Delta), \
VecLong4D*: (VecLong*)(Delta)))

#define VecShiftStepDelta(Vec, VecFrom, VecTo, Delta) _Generic(Vec, \
VecFloat*: _VecFloatShiftStepDelta, \
VecFloat2D*: _VecFloatShiftStepDelta, \
VecFloat3D*: _VecFloatShiftStepDelta, \
default: PBErrInvalidPolymorphism)((VecFloat*)(Vec), \
(VecFloat*)(VecFrom), (VecFloat*)(VecTo), (VecFloat*)(Delta))

#define VecGetIMaxVal(Vec) _Generic(Vec, \
VecFloat*: _VecFloatGetIMaxVal, \
const VecFloat*: _VecFloatGetIMaxVal, \
VecFloat2D*: _VecFloatGetIMaxVal, \
const VecFloat2D*: _VecFloatGetIMaxVal, \
VecFloat3D*: _VecFloatGetIMaxVal, \
const VecFloat3D*: _VecFloatGetIMaxVal, \
VecShort*: _VecShortGetIMaxVal, \
const VecShort*: _VecShortGetIMaxVal, \
VecShort2D*: _VecShortGetIMaxVal, \
const VecShort2D*: _VecShortGetIMaxVal, \
VecShort3D*: _VecShortGetIMaxVal, \
const VecShort3D*: _VecShortGetIMaxVal, \
VecShort4D*: _VecShortGetIMaxVal, \
const VecShort4D*: _VecShortGetIMaxVal, \
VecLong*: _VecLongGetIMaxVal, \
const VecLong*: _VecLongGetIMaxVal, \
VecLong2D*: _VecLongGetIMaxVal, \
const VecLong2D*: _VecLongGetIMaxVal, \
VecLong3D*: _VecLongGetIMaxVal, \
const VecLong3D*: _VecLongGetIMaxVal, \
VecLong4D*: _VecLongGetIMaxVal, \
const VecLong4D*: _VecLongGetIMaxVal, \
default: PBErrInvalidPolymorphism) (_Generic(Vec, \
VecFloat2D*: (const VecFloat*)(Vec), \
const VecFloat2D*: (const VecFloat*)(Vec), \
VecFloat3D*: (const VecFloat*)(Vec), \
const VecFloat3D*: (const VecFloat*)(Vec), \
VecShort2D*: (const VecShort*)(Vec), \
const VecShort2D*: (const VecShort*)(Vec), \
VecShort3D*: (const VecShort*)(Vec), \
const VecShort3D*: (const VecShort*)(Vec), \
VecShort4D*: (const VecShort*)(Vec), \
const VecShort4D*: (const VecShort*)(Vec), \
VecLong2D*: (const VecLong*)(Vec), \
const VecLong2D*: (const VecLong*)(Vec), \
VecLong3D*: (const VecLong*)(Vec), \

```

```

    const VecLong3D*: (const VecLong*)(Vec), \
    VecLong4D*: (const VecLong*)(Vec), \
    const VecLong4D*: (const VecLong*)(Vec), \
    default: Vec))

#define MatClone(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatClone, \
    const MatFloat*: _MatFloatClone, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatEncodeAsJSON(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatEncodeAsJSON, \
    const MatFloat*: _MatFloatEncodeAsJSON, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatDecodeAsJSON(MatRef, Json) _Generic(MatRef, \
    MatFloat*: _MatFloatDecodeAsJSON, \
    default: PBErrInvalidPolymorphism)(MatRef, Json)

#define MatLoad(MatRef, Stream) _Generic(MatRef, \
    MatFloat*: _MatFloatLoad, \
    default: PBErrInvalidPolymorphism)(MatRef, Stream)

#define MatSave(Mat, Stream, Compact) _Generic(Mat, \
    MatFloat*: _MatFloatSave, \
    const MatFloat*: _MatFloatSave, \
    default: PBErrInvalidPolymorphism)(Mat, Stream, Compact)

#define MatFree(MatRef) _Generic(MatRef, \
    MatFloat*: _MatFloatFree, \
    default: PBErrInvalidPolymorphism)(MatRef)

#define MatPrintln(Mat, Stream) _Generic(Mat, \
    MatFloat*: _MatFloatPrintlnDef, \
    const MatFloat*: _MatFloatPrintlnDef, \
    default: PBErrInvalidPolymorphism)(Mat, Stream)

#define MatGet(Mat, VecIndex) _Generic(Mat, \
    MatFloat*: _MatFloatGet, \
    const MatFloat*: _MatFloatGet, \
    default: PBErrInvalidPolymorphism)(Mat, VecIndex)

#define MatSet(Mat, VecIndex, Val) _Generic(Mat, \
    MatFloat*: _MatFloatSet, \
    default: PBErrInvalidPolymorphism)(Mat, VecIndex, Val)

#define MatCopy(MatDest, MatSrc) _Generic(MatDest, \
    MatFloat*: _Generic (MatSrc, \
        MatFloat*: _MatFloatCopy, \
        const MatFloat*: _MatFloatCopy, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(MatDest, MatSrc)

#define MatDim(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatDim, \
    const MatFloat*: _MatFloatDim, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetDim(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetDim, \
    const MatFloat*: _MatFloatGetDim, \
    default: PBErrInvalidPolymorphism)(Mat)

```

```

#define MatGetEigenValues(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetEigenValues, \
    const MatFloat*: _MatFloatGetEigenValues, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetQR(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetQR, \
    const MatFloat*: _MatFloatGetQR, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetInv(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetInv, \
    const MatFloat*: _MatFloatGetInv, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetTranspose(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetTranspose, \
    const MatFloat*: _MatFloatGetTranspose, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetNbRow(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetNbRow, \
    const MatFloat*: _MatFloatGetNbRow, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetNbCol(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatGetNbCol, \
    const MatFloat*: _MatFloatGetNbCol, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatGetProdMat(MatA, MatB) _Generic(MatA, \
    MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatGetProdMatFloat, \
        const MatFloat*: _MatFloatGetProdMatFloat, \
        default: PBErrInvalidPolymorphism), \
    const MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatGetProdMatFloat, \
        const MatFloat*: _MatFloatGetProdMatFloat, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(MatA, MatB)

#define MatGetProdVec(Mat, Vec) _Generic(Mat, \
    MatFloat*: _Generic(Vec, \
        VecFloat*: _MatFloatGetProdVecFloat, \
        const VecFloat*: _MatFloatGetProdVecFloat, \
        VecFloat2D*: _MatFloatGetProdVecFloat, \
        const VecFloat2D*: _MatFloatGetProdVecFloat, \
        VecFloat3D*: _MatFloatGetProdVecFloat, \
        const VecFloat3D*: _MatFloatGetProdVecFloat, \
        default: PBErrInvalidPolymorphism), \
    const MatFloat*: _Generic(Vec, \
        VecFloat*: _MatFloatGetProdVecFloat, \
        const VecFloat*: _MatFloatGetProdVecFloat, \
        VecFloat2D*: _MatFloatGetProdVecFloat, \
        const VecFloat2D*: _MatFloatGetProdVecFloat, \
        VecFloat3D*: _MatFloatGetProdVecFloat, \
        const VecFloat3D*: _MatFloatGetProdVecFloat, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))

#define MatGetProdVecVecTranspose(VecA, VecB) _Generic(VecA, \

```

```

VecFloat*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
const VecFloat*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
VecFloat2D*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
const VecFloat2D*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
VecFloat3D*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
const VecFloat3D*: _Generic(VecB, \
    VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat2D*: _MatFloatGetProdVecVecTransposeFloat, \
    VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    const VecFloat3D*: _MatFloatGetProdVecVecTransposeFloat, \
    default: PBErrInvalidPolymorphism), \
default: PBErrInvalidPolymorphism)((VecFloat*)(VecA), \
    (VecFloat*)(VecB))

#define MatAdd(MatA, MatB) _Generic(MatA, \
    MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatAdd, \
        const MatFloat*: _MatFloatAdd, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(MatA, MatB)

#define MatScale(MatA, A) _Generic(MatA, \
    MatFloat*: _MatFloatScale, \
    const MatFloat*: _MatFloatScale, \
    default: PBErrInvalidPolymorphism)(MatA, A)

```



```

#define MatGetAdd(MatA, MatB) _Generic(MatA, \
    MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatGetAdd, \
        const MatFloat*: _MatFloatGetAdd, \
        default: PBErrInvalidPolymorphism), \
    const MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatGetAdd, \
        const MatFloat*: _MatFloatGetAdd, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(MatA, MatB)

#define MatSetIdentity(Mat) _Generic(Mat, \
    MatFloat*: _MatFloatSetIdentity, \
    default: PBErrInvalidPolymorphism)(Mat)

#define MatIsEqual(MatA, MatB) _Generic(MatA, \
    MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatIsEqual, \
        const MatFloat*: _MatFloatIsEqual, \
        default: PBErrInvalidPolymorphism), \
    const MatFloat*: _Generic(MatB, \
        MatFloat*: _MatFloatIsEqual, \
        const MatFloat*: _MatFloatIsEqual, \
        default: PBErrInvalidPolymorphism), \
    default: PBErrInvalidPolymorphism)(MatA, MatB)

#define SysLinEqCreate(Mat, Vec) _Generic(Vec, \
    VecFloat*: _SLECreate, \
    const VecFloat*: _SLECreate, \
    VecFloat2D*: _SLECreate, \
    const VecFloat2D*: _SLECreate, \
    VecFloat3D*: _SLECreate, \
    const VecFloat3D*: _SLECreate, \
    default: PBErrInvalidPolymorphism)(Mat, (VecFloat*)(Vec))

#define SysLinEqSetV(Sys, Vec) _Generic(Vec, \
    VecFloat*: _SLESetV, \
    const VecFloat*: _SLESetV, \
    VecFloat2D*: _SLESetV, \
    const VecFloat2D*: _SLESetV, \
    VecFloat3D*: _SLESetV, \
    const VecFloat3D*: _SLESetV, \
    default: PBErrInvalidPolymorphism)(Sys, (VecFloat*)(Vec))

// ===== static inliner =====

#if BUILDMODE != 0
#include "pbmath-inline.c"
#endif

#endif

```

## 3 Code

### 3.1 pbmath.c

```
// ===== PBMath.C =====

// ===== Include =====

#include "pbmath.h"
#if BUILDMODE == 0
#include "pbmath-inline.c"
#endif

// ----- VecShort

// ===== Functions implementation =====

// Create a new Vec of dimension 'dim'
// Values are initialized to 0.0
VecShort* VecShortCreate(const long dim) {
    #if BUILDMODE == 0
        if (dim <= 0) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Allocate memory
    VecShort* that = PBErrMalloc(PBMathErr,
        offsetof(VecShort, _val) + sizeof(short) * dim);
    // Set the default values
    that->_dim = dim;
    for (long i = dim; i--;)
        that->_val[i] = 0;
    // Return the new VecShort
    return that;
}

// Clone the VecShort
// Return NULL if we couldn't clone the VecShort
VecShort* _VecShortClone(const VecShort* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Create a clone
    VecShort* clone = VecShortCreate(that->_dim);
    // Copy the values
    memcpy(clone, that, sizeof(VecShort) + sizeof(short) * that->_dim);
    // Return the clone
    return clone;
}

// Function which return the JSON encoding of 'that'
JSONNode* _VecShortEncodeAsJSON(const VecShort* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;

```

```

        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
#endif
    // Create the JSON structure
    JSONNode* json = JSONCreate();
    // Declare a buffer to convert value into string
    char val[100];
    // Encode the dimension
    sprintf(val, "%ld", VecGetDim(that));
    JSONAddProp(json, "_dim", val);
    // Encode the values
    JSONArrayVal setVal = JSONArrayValCreateStatic();
    for (long i = 0; i < VecGetDim(that); ++i) {
        sprintf(val, "%d", VecGet(that, i));
        JSONArrayValAdd(&setVal, val);
    }
    JSONAddProp(json, "_val", &setVal);
    // Free memory
    JSONArrayValFlush(&setVal);
    // Return the created JSON
    return json;
}

// Function which decode from JSON encoding 'json' to 'that'
bool _VecShortDecodeAsJSON(VecShort** that, const JSONNode* const json) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (json == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'json' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // If 'that' is already allocated
    if (*that != NULL)
        // Free memory
        _VecShortFree(that);
    // Get the dimension from the JSON
    JSONNode* prop = JSONProperty(json, "_dim");
    if (prop == NULL) {
        return false;
    }
    long dim = atol(JSONLb1Val(prop));
    // If data are invalid
    if (dim < 1)
        return false;
    // Allocate memory
    *that = VecShortCreate(dim);
    // Get the values
    prop = JSONProperty(json, "_val");
    if (prop == NULL) {
        return false;
    }
    for (long i = 0; i < dim; ++i) {
        long val = atol(JSONLabel(JSONValue(prop, i)));
        VecSet(*that, i, val);
    }
}

```

```

    // Return the success code
    return true;
}

// Load the VecShort from the stream
// If the VecShort is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecShortLoad(VecShort** that, FILE* const stream) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (stream == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'stream' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a json to load the encoded data
    JSONNode* json = JSONCreate();
    // Load the whole encoded data
    if (!JSONLoad(json, stream)) {
        return false;
    }
    // Decode the data from the JSON
    if (!VecDecodeAsJSON(that, json)) {
        return false;
    }
    // Free the memory used by the JSON
    JSONFree(&json);
    // Return the success code
    return true;
}

// Save the VecShort to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecShortSave(const VecShort* const that,
    FILE* const stream, const bool compact) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (stream == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'stream' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Get the JSON encoding
    JSONNode* json = VecEncodeAsJSON(that);
    // Save the JSON
    if (!JSONSave(json, stream, compact)) {
        return false;
    }
    // Free memory
    JSONFree(&json);
}

```

```

    // Return success code
    return true;
}

// Free the memory used by a VecShort
// Do nothing if arguments are invalid
void _VecShortFree(VecShort** that) {
    // Check argument
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    free(*that);
    *that = NULL;
}

// Print the VecShort on 'stream' with 'prec' digit precision
void _VecShortPrint(const VecShort* const that,
    FILE* const stream) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (stream == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'stream' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Print the values
    fprintf(stream, "[");
    for (long i = 0; i < that->_dim; ++i) {
        fprintf(stream, "%hi", that->_val[i]);
        if (i < that->_dim - 1)
            fprintf(stream, ",");
    }
    fprintf(stream, "]\n");
}

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStep(VecShort* const that, const VecShort* const bound) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (bound == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'bound' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != bound->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",

```

```

        that->_dim, bound->_dim);
    PBErrCatch(PBMathErr);
}
#endif
// Declare a variable for the returned flag
bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = that->_dim - 1;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
        that->_val[iDim] = 0;
        --iDim;
    } else {
        flag = false;
    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortPStep(VecShort* const that, const VecShort* const bound) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
}
#endif
// Declare a variable for the returned flag
bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = 0;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {

```

```

        that->_val[iDim] = 0;
        ++iDim;
    } else {
        flag = false;
    }
} while (iDim < that->_dim && flag == true);
if (iDim == that->_dim)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecShortShiftStep(VecShort* const that,
    const VecShort* const from, const VecShort* const to) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (from == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'from' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != from->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
            that->_dim, from->_dim);
        PBErrCatch(PBMathErr);
    }
    if (to == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'to' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != to->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
            that->_dim, to->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = that->_dim - 1;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        ++(that->_val[iDim]);

```

```

        if (that->_val[iDim] >= to->_val[iDim]) {
            that->_val[iDim] = from->_val[iDim];
            --iDim;
        } else {
            flag = false;
        }
    } while (iDim >= 0 && flag == true);
    if (iDim == -1)
        ret = false;
    // Return the flag
    return ret;
}

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecShortStepDelta(VecShort* const that,
    const VecShort* const bound, const VecShort* const delta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (delta == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'delta' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != delta->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, delta->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = that->_dim - 1;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        that->_val[iDim] += delta->_val[iDim];
        if (that->_val[iDim] >= bound->_val[iDim]) {
            that->_val[iDim] = 0;

```



```

        --iDim;
    } else {
        flag = false;
    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that's values are all set back to 0)
// Return true else
bool _VecShortPStepDelta(VecShort* const that,
    const VecShort* const bound, const VecShort* const delta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (delta == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'delta' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != delta->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, delta->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = 0;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        that->_val[iDim] += delta->_val[iDim];
        if (that->_val[iDim] >= bound->_val[iDim]) {
            that->_val[iDim] = 0;
            ++iDim;
        } else {

```

```

        flag = false;
    }
} while (iDim < that->_dim && flag == true);
if (iDim == that->_dim)
    ret = false;
// Return the flag
return ret;
}

// ----- VecLong

// ===== Functions implementation =====

// Create a new Vec of dimension 'dim'
// Values are initialized to 0.0
VecLong* VecLongCreate(const long dim) {
#ifdef BUILDMODE == 0
    if (dim <= 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Allocate memory
    VecLong* that = PBErrMalloc(PBMathErr,
        offsetof(VecLong, _val) + sizeof(long) * dim);
    // Set the default values
    that->_dim = dim;
    for (long i = dim; i--;)
        that->_val[i] = 0;
    // Return the new VecLong
    return that;
}

// Clone the VecLong
// Return NULL if we couldn't clone the VecLong
VecLong* _VecLongClone(const VecLong* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create a clone
    VecLong* clone = VecLongCreate(that->_dim);
    // Copy the values
    memcpy(clone, that, sizeof(VecLong) + sizeof(long) * that->_dim);
    // Return the clone
    return clone;
}

// Function which return the JSON encoding of 'that'
JSONNode* _VecLongEncodeAsJSON(const VecLong* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the JSON structure

```

```

JSONNode* json = JSONCreate();
// Declare a buffer to convert value into string
char val[100];
// Encode the dimension
sprintf(val, "%ld", VecGetDim(that));
JSONAddProp(json, "_dim", val);
// Encode the values
JSONArrayVal setVal = JSONArrayValCreateStatic();
for (long i = 0; i < VecGetDim(that); ++i) {
    sprintf(val, "%ld", VecGet(that, i));
    JSONArrayValAdd(&setVal, val);
}
JSONAddProp(json, "_val", &setVal);
// Free memory
JSONArrayValFlush(&setVal);
// Return the created JSON
return json;
}

// Function which decode from JSON encoding 'json' to 'that'
bool _VecLongDecodeAsJSON(VecLong** that, const JSONNode* const json) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (json == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'json' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // If 'that' is already allocated
    if (*that != NULL)
        // Free memory
        _VecLongFree(that);
    // Get the dimension from the JSON
    JSONNode* prop = JSONProperty(json, "_dim");
    if (prop == NULL) {
        return false;
    }
    long dim = atol(JSONLb1Val(prop));
    // If data are invalid
    if (dim < 1)
        return false;
    // Allocate memory
    *that = VecLongCreate(dim);
    // Get the values
    prop = JSONProperty(json, "_val");
    if (prop == NULL) {
        return false;
    }
    for (long i = 0; i < dim; ++i) {
        long val = atol(JSONLabel(JSONValue(prop, i)));
        VecSet(*that, i, val);
    }
    // Return the success code
    return true;
}

// Load the VecLong from the stream

```

```

// If the VecLong is already allocated, it is freed before loading
// Return true in case of success, else false
bool _VecLongLoad(VecLong** that, FILE* const stream) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a json to load the encoded data
    JSONNode* json = JSONCreate();
    // Load the whole encoded data
    if (!JSONLoad(json, stream)) {
        return false;
    }
    // Decode the data from the JSON
    if (!VecDecodeAsJSON(that, json)) {
        return false;
    }
    // Free the memory used by the JSON
    JSONFree(&json);
    // Return the success code
    return true;
}

// Save the VecLong to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecLongSave(const VecLong* const that,
    FILE* const stream, const bool compact) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Get the JSON encoding
    JSONNode* json = VecEncodeAsJSON(that);
    // Save the JSON
    if (!JSONSave(json, stream, compact)) {
        return false;
    }
    // Free memory
    JSONFree(&json);
    // Return success code
    return true;
}

// Free the memory used by a VecLong

```

```

// Do nothing if arguments are invalid
void _VecLongFree(VecLong** that) {
    // Check argument
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    free(*that);
    *that = NULL;
}

// Print the VecLong on 'stream' with 'prec' digit precision
void _VecLongPrint(const VecLong* const that,
    FILE* const stream) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (stream == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'stream' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Print the values
    fprintf(stream, "[");
    for (long i = 0; i < that->_dim; ++i) {
        fprintf(stream, "%ld", that->_val[i]);
        if (i < that->_dim - 1)
            fprintf(stream, ",");
    }
    fprintf(stream, "]\n");
}

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStep(VecLong* const that, const VecLong* const bound) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (bound == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'bound' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != bound->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, bound->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable for the returned flag

```

```

bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = that->_dim - 1;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    ++(that->_val[iDim]);
    if (that->_val[iDim] >= bound->_val[iDim]) {
        that->_val[iDim] = 0;
        --iDim;
    } else {
        flag = false;
    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by 1 from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] < dim[i])
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongPStep(VecLong* const that, const VecLong* const bound) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = 0;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        ++(that->_val[iDim]);
        if (that->_val[iDim] >= bound->_val[iDim]) {
            that->_val[iDim] = 0;
            ++iDim;
        } else {
            flag = false;
        }
    }

```

```

    } while (iDim < that->_dim && flag == true);
    if (iDim == that->_dim)
        ret = false;
    // Return the flag
    return ret;
}

// Step the values of the vector incrementally by 1
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] < to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false if all values of 'that' have reached their upper limit
// (in which case 'that''s values are all set back to from)
// Return true else
bool _VecLongShiftStep(VecLong* const that,
    const VecLong* const from, const VecLong* const to) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (from == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'from' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != from->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
            that->_dim, from->_dim);
        PBErrCatch(PBMathErr);
    }
    if (to == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'to' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != to->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
            that->_dim, to->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = that->_dim - 1;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        ++(that->_val[iDim]);
        if (that->_val[iDim] >= to->_val[iDim]) {
            that->_val[iDim] = from->_val[iDim];
            --iDim;
        } else {
            flag = false;
        }
    } while (iDim > 0 && flag == true);
    return ret;
}

```

```

    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(0,0,1)->(0,0,2)->(0,1,0)->(0,1,1)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0)
// Return true else
bool _VecLongStepDelta(VecLong* const that,
    const VecLong* const bound, const VecLong* const delta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (delta == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'delta' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != delta->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, delta->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the returned flag
    bool ret = true;
    // Declare a variable to memorise the dimension currently increasing
    long iDim = that->_dim - 1;
    // Declare a flag for the loop condition
    bool flag = true;
    // Increment
    do {
        that->_val[iDim] += delta->_val[iDim];
        if (that->_val[iDim] >= bound->_val[iDim]) {
            that->_val[iDim] = 0;
            --iDim;
        } else {
            flag = false;
        }
    }
} while (iDim >= 0 && flag == true);

```



```

    if (iDim == -1)
        ret = false;
    // Return the flag
    return ret;
}

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0,0,0)->(1,0,0)->(2,0,0)->(0,1,0)->(1,1,0)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that's values are all set back to 0)
// Return true else
bool _VecLongPStepDelta(VecLong* const that,
    const VecLong* const bound, const VecLong* const delta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'that' is null");
        PBErrCatch(PBMATHERR);
    }
    if (bound == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'bound' is null");
        PBErrCatch(PBMATHERR);
    }
    if (delta == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'delta' is null");
        PBErrCatch(PBMATHERR);
    }
    if (that->_dim != bound->_dim) {
        PBMATHERR->_type = PBErrTypeInvalidArg;
        sprintf(PBMATHERR->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMATHERR);
    }
    if (that->_dim != delta->_dim) {
        PBMATHERR->_type = PBErrTypeInvalidArg;
        sprintf(PBMATHERR->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, delta->_dim);
        PBErrCatch(PBMATHERR);
    }
}
#endif
// Declare a variable for the returned flag
bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = 0;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] >= bound->_val[iDim]) {
        that->_val[iDim] = 0;
        ++iDim;
    } else {
        flag = false;
    }
} while (iDim < that->_dim && flag == true);
if (iDim == that->_dim)
    ret = false;

```

```

    // Return the flag
    return ret;
}

// Return a new VecLong as a copy of the VecLong 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0
// If it is shrunk, values are discarded from the end of the vector
VecLong* _VecLongGetNewDim(const VecLong* const that, const long dim) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (dim <= 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'dim' is invalid match (%ld>0)", dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // If the new dimension is the same as the current one
    if (dim == VecGetDim(that)) {
        // Return the clone of the vector
        return VecClone(that);
    }
    // Else, the new dimension is actually different
    else {
        // Declare the returned vector
        VecLong* ret = VecLongCreate(dim);
        // Copy the components
        for (long iAxis = MIN(VecGetDim(that), dim); iAxis--;)
            VecSet(ret, iAxis, VecGet(that, iAxis));
        // Return the new vector
        return ret;
    }
}

// ----- VecFloat

// ===== Functions implementation =====

// Create a new Vec of dimension 'dim'
// Values are initialized to 0.0
VecFloat* VecFloatCreate(const long dim) {
#ifdef BUILDMODE == 0
    if (dim <= 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "invalid 'dim' (%ld)", dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Allocate memory
    VecFloat* that = PBErrMalloc(PBMathErr,
        offsetof(VecFloat, _val) + sizeof(float) * dim);
    // Set the default values
    that->_dim = dim;
    for (long i = dim; i--;)
        that->_val[i] = 0.0;
    // Return the new VecFloat
    return that;
}

```

```

// Clone the VecFloat
VecFloat* _VecFloatClone(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create a clone
    VecFloat* clone = VecFloatCreate(that->_dim);
    // Clone the properties
    memcpy(clone, that, sizeof(VecFloat) + sizeof(float) * that->_dim);
    // Return the clone
    return clone;
}

// Function which return the JSON encoding of 'that'
JSONNode* _VecFloatEncodeAsJSON(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the JSON structure
    JSONNode* json = JSONCreate();
    // Declare a buffer to convert value into string
    char val[100];
    // Encode the dimension
    sprintf(val, "%ld", VecGetDim(that));
    JSONAddProp(json, "_dim", val);
    // Encode the values
    JSONArrayVal setVal = JSONArrayValCreateStatic();
    for (long i = 0; i < VecGetDim(that); ++i) {
        sprintf(val, "%f", VecGet(that, i));
        JSONArrayValAdd(&setVal, val);
    }
    JSONAddProp(json, "_val", &setVal);
    // Free memory
    JSONArrayValFlush(&setVal);
    // Return the created JSON
    return json;
}

// Function which decode from JSON encoding 'json' to 'that'
bool _VecFloatDecodeAsJSON(VecFloat** that, const JSONNode* const json) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (json == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'json' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // If 'that' is already allocated
    if (*that != NULL)

```

```

        // Free memory
        _VecFloatFree(that);
    // Get the dimension from the JSON
    JSONNode* prop = JSONProperty(json, "_dim");
    if (prop == NULL) {
        return false;
    }
    long dim = atol(JSONLb1Val(prop));
    // If data are invalid
    if (dim < 1)
        return false;
    // Allocate memory
    *that = VecFloatCreate(dim);
    // Get the values
    prop = JSONProperty(json, "_val");
    if (prop == NULL) {
        return false;
    }
    for (long i = 0; i < dim; ++i) {
        float val = atof(JSONLabel(JSONValue(prop, i)));
        VecSet(*that, i, val);
    }
    // Return the success code
    return true;
}

// Load the VecFloat from the stream
// If the VecFloat is already allocated, it is freed before loading
bool _VecFloatLoad(VecFloat** that, FILE* const stream) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a json to load the encoded data
    JSONNode* json = JSONCreate();
    // Load the whole encoded data
    if (!JSONLoad(json, stream)) {
        return false;
    }
    // Decode the data from the JSON
    if (!VecDecodeAsJSON(that, json)) {
        return false;
    }
    // Free the memory used by the JSON
    JSONFree(&json);
    // Return the success code
    return true;
}

// Save the VecFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true in case of success, else false
bool _VecFloatSave(const VecFloat* const that,

```

```

    FILE* const stream, const bool compact) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Get the JSON encoding
    JSONNode* json = VecEncodeAsJSON(that);
    // Save the JSON
    if (!JSONSave(json, stream, compact)) {
        return false;
    }
    // Free memory
    JSONFree(&json);
    // Return success code
    return true;
}

// Free the memory used by a VecFloat
// Do nothing if arguments are invalid
void _VecFloatFree(VecFloat** that) {
    // Check argument
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    free(*that);
    *that = NULL;
}

// Print the VecFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void VecFloatPrint(const VecFloat* const that, FILE* const stream,
    const unsigned int prec) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the format string
    char format[100] = {'\0'};
    sprintf(format, "%%.%df", prec);
    // Print the values
    fprintf(stream, "[");
    for (long i = 0; i < that->_dim; ++i) {
        fprintf(stream, format, that->_val[i]);
        if (i < that->_dim - 1)
            fprintf(stream, ",");
    }
}

```

```

    fprintf(stream, "]\n");
}

// Return the angle of the rotation making 'that' colinear to 'tho'
// 'that' and 'tho' must be normalised
// Return a value in [-PI,PI]
float _VecFloatAngleTo2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(that), 1.0)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' is not a normed vector");
        PBErrCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(tho), 1.0)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'tho' is not a normed vector");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    float theta = 0.0;
    // Calculate the angle
    VecFloat2D m = VecFloatCreateStatic2D();
    if (fabs(VecGet(that, 0)) > fabs(VecGet(that, 1))) {
        VecSet(&m, 0,
            (VecGet(tho, 0) + VecGet(tho, 1) * VecGet(that, 1) /
            VecGet(that, 0)) /
            (VecGet(that, 0) + fsquare(VecGet(that, 1)) / VecGet(that, 0)));
        VecSet(&m, 1,
            (VecGet(&m, 0) * VecGet(that, 1) - VecGet(tho, 1)) /
            VecGet(that, 0));
    } else {
        VecSet(&m, 1,
            (VecGet(tho, 0) - VecGet(tho, 1) * VecGet(that, 0) /
            VecGet(that, 1)) /
            (VecGet(that, 1) + fsquare(VecGet(that, 0)) / VecGet(that, 1)));
        VecSet(&m, 0,
            (VecGet(tho, 1) + VecGet(&m, 1) * VecGet(that, 0)) /
            VecGet(that, 1));
    }
    // Due to numerical imprecision m[0] may be slightly out of [-1,1]
    // which makes acos return NaN, prevent this
    if (VecGet(&m, 0) < -1.0)
        theta = PBMATH_PI;
    else if (VecGet(&m, 0) > 1.0)
        theta = 0.0;
    else
        theta = acos(VecGet(&m, 0));
    if (sin(theta) * VecGet(&m, 1) > 0.0)
        theta *= -1.0;
    // Return the result

```

```

    return theta;
}

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around 'axis'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
VecFloat3D _VecFloatGetRotAxis(const VecFloat3D* const that,
    const VecFloat3D* const axis, const float theta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (axis == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'axis' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld=3)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(axis) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%ld=3)",
            VecGetDim(axis));
        PBErrCatch(PBMathErr);
    }
    if (ISEQUALF(VecNorm(axis), 1.0) == false) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'axis' is not normalized");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare variable for optimisation
    float cosTheta = cos(theta);
    float sinTheta = sin(theta);
    // Create the rotation matrix
    VecShort2D d = VecShortCreateStatic2D();
    VecSet(&d, 0, 3); VecSet(&d, 1, 3);
    MatFloat* rot = MatFloatCreate(&d);
    VecSet(&d, 0, 0); VecSet(&d, 1, 0);
    float v = cosTheta + fastpow(VecGet(axis, 0), 2) * (1.0 - cosTheta);
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 0);
    v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) -
        VecGet(axis, 2) * sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 0);
    v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) +
        VecGet(axis, 1) * sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 1);
    v = VecGet(axis, 0) * VecGet(axis, 1) * (1.0 - cosTheta) +
        VecGet(axis, 2) * sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 1);
    v = cosTheta + fastpow(VecGet(axis, 1), 2) * (1.0 - cosTheta);

```

```

MatSet(rot, &d, v);
VecSet(&d, 0, 2); VecSet(&d, 1, 1);
v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) -
    VecGet(axis, 0) * sinTheta;
MatSet(rot, &d, v);
VecSet(&d, 0, 0); VecSet(&d, 1, 2);
v = VecGet(axis, 0) * VecGet(axis, 2) * (1.0 - cosTheta) -
    VecGet(axis, 1) * sinTheta;
MatSet(rot, &d, v);
VecSet(&d, 0, 1); VecSet(&d, 1, 2);
v = VecGet(axis, 1) * VecGet(axis, 2) * (1.0 - cosTheta) +
    VecGet(axis, 0) * sinTheta;
MatSet(rot, &d, v);
VecSet(&d, 0, 2); VecSet(&d, 1, 2);
v = cosTheta + fastpow(VecGet(axis, 2), 2) * (1.0 - cosTheta);
MatSet(rot, &d, v);
// Calculate the result vector
VecFloat* w = MatGetProdVec(rot, that);
VecFloat3D res = VecFloatCreateStatic3D();
VecCopy(&res, w);
// Free memory
VecFree(&w);
MatFree(&rot);
// Return the result
return res;
}

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around X
VecFloat3D _VecFloatGetRotX(const VecFloat3D* const that,
    const float theta) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (VecGetDim(that) != 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld=3)",
                VecGetDim(that));
            PBErrCatch(PBMathErr);
        }
    }
    #endif
    // Declare variable for optimisation
    float cosTheta = cos(theta);
    float sinTheta = sin(theta);
    // Create the rotation matrix
    VecShort2D d = VecShortCreateStatic2D();
    VecSet(&d, 0, 3); VecSet(&d, 1, 3);
    MatFloat* rot = MatFloatCreate(&d);
    VecSet(&d, 0, 0); VecSet(&d, 1, 0);
    float v = 1.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 0);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 0);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 1);
    v = 0.0;

```



```

    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 1);
    v = cosTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 1);
    v = -sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 2);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 2);
    v = sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 2);
    v = cosTheta;
    MatSet(rot, &d, v);
    // Calculate the result vector
    VecFloat* w = MatGetProdVec(rot, that);
    VecFloat3D res = VecFloatCreateStatic3D();
    VecCopy(&res, w);
    // Free memory
    VecFree(&w);
    MatFree(&rot);
    // Return the result
    return res;
}

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Y
VecFloat3D _VecFloatGetRotY(const VecFloat3D* const that,
    const float theta) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (VecGetDim(that) != 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld=3)",
                VecGetDim(that));
            PBErrCatch(PBMathErr);
        }
    }
    #endif
    // Declare variable for optimisation
    float cosTheta = cos(theta);
    float sinTheta = sin(theta);
    // Create the rotation matrix
    VecShort2D d = VecShortCreateStatic2D();
    VecSet(&d, 0, 3); VecSet(&d, 1, 3);
    MatFloat* rot = MatFloatCreate(&d);
    VecSet(&d, 0, 0); VecSet(&d, 1, 0);
    float v = cosTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 0);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 0);
    v = sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 1);
    v = 0.0;

```

```

    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 1);
    v = 1.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 1);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 2);
    v = -sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 2);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 2);
    v = cosTheta;
    MatSet(rot, &d, v);
    // Calculate the result vector
    VecFloat* w = MatGetProdVec(rot, that);
    VecFloat3D res = VecFloatCreateStatic3D();
    VecCopy(&res, w);
    // Free memory
    VecFree(&w);
    MatFree(&rot);
    // Return the result
    return res;
}

// Return a VecFloat3D equal to 'that' rotated right-hand by 'theta'
// radians around Z
VecFloat3D _VecFloatGetRotZ(const VecFloat3D* const that,
    const float theta) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (VecGetDim(that) != 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld=3)",
                VecGetDim(that));
            PBErrCatch(PBMathErr);
        }
    }
    #endif
    // Declare variable for optimisation
    float cosTheta = cos(theta);
    float sinTheta = sin(theta);
    // Create the rotation matrix
    VecShort2D d = VecShortCreateStatic2D();
    VecSet(&d, 0, 3); VecSet(&d, 1, 3);
    MatFloat* rot = MatFloatCreate(&d);
    VecSet(&d, 0, 0); VecSet(&d, 1, 0);
    float v = cosTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 0);
    v = -sinTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 0);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 1);
    v = sinTheta;

```

```

    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 1);
    v = cosTheta;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 1);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 0); VecSet(&d, 1, 2);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 1); VecSet(&d, 1, 2);
    v = 0.0;
    MatSet(rot, &d, v);
    VecSet(&d, 0, 2); VecSet(&d, 1, 2);
    v = 1.0;
    MatSet(rot, &d, v);
    // Calculate the result vector
    VecFloat* w = MatGetProdVec(rot, that);
    VecFloat3D res = VecFloatCreateStatic3D();
    VecCopy(&res, w);
    // Free memory
    VecFree(&w);
    MatFree(&rot);
    // Return the result
    return res;
}

// Step the values of the vector incrementally by delta from 0
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The upper limit for each value is given by 'bound' (val[i] <= dim[i])
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to 0.)
// Return true else
bool _VecFloatStepDelta(VecFloat* const that,
    const VecFloat* const bound, const VecFloat* const delta) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (bound == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'bound' is null");
        PBErrCatch(PBMathErr);
    }
    if (delta == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'delta' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != bound->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'bound' 's dimensions don't match (%ld==%ld)",
            that->_dim, bound->_dim);
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != delta->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,

```

```

        "'delta' 's dimensions don't match (%ld==%ld)",
        that->_dim, delta->_dim);
    PBErrCatch(PBMathErr);
}
#endif
// Declare a variable for the returned flag
bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = that->_dim - 1;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > bound->_val[iDim] + PBMath_EPSILON) {
        that->_val[iDim] = 0;
        --iDim;
    } else {
        flag = false;
    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Step the values of the vector incrementally by delta
// in the following order (for example) :
// (0.,0.,0.)->(0.,0.,1.)->(0.,0.,2.)->(0.,1.,0.)->(0.,1.,1.)->...
// The lower limit for each value is given by 'from' (val[i] >= from[i])
// The upper limit for each value is given by 'to' (val[i] <= to[i])
// 'that' must be initialised to 'from' before the first call of this
// function
// Return false after all values of 'that' have reached their upper
// limit (in which case 'that''s values are all set back to from)
// Return true else
bool _VecFloatShiftStepDelta(VecFloat* const that,
    const VecFloat* const from, const VecFloat* const to,
    const VecFloat* const delta) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (from == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'from' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != from->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'from' dimensions don't match (%ld==%ld)",
                that->_dim, from->_dim);
            PBErrCatch(PBMathErr);
        }
        if (to == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'to' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
}

```

```

    if (that->_dim != to->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'to' dimensions don't match (%ld==%ld)",
            that->_dim, to->_dim);
        PBErrCatch(PBMathErr);
    }
    if (delta == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'delta' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != delta->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'delta' dimensions don't match (%ld==%ld)",
            that->_dim, delta->_dim);
        PBErrCatch(PBMathErr);
    }
}
#endif
// Declare a variable for the returned flag
bool ret = true;
// Declare a variable to memorise the dimension currently increasing
long iDim = that->_dim - 1;
// Declare a flag for the loop condition
bool flag = true;
// Increment
do {
    that->_val[iDim] += delta->_val[iDim];
    if (that->_val[iDim] > to->_val[iDim] + PB_MATH_EPSILON) {
        that->_val[iDim] = from->_val[iDim];
        --iDim;
    } else {
        flag = false;
    }
} while (iDim >= 0 && flag == true);
if (iDim == -1)
    ret = false;
// Return the flag
return ret;
}

// Return a new VecFloat as a copy of the VecFloat 'that' with
// dimension changed to 'dim'
// if it is extended, the values of new components are 0.0
// If it is shrunk, values are discarded from the end of the vector
VecFloat* _VecFloatGetNewDim(const VecFloat* const that, const long dim) {
#ifdef BUILD_MODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (dim <= 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'dim' is invalid match (%ld>0)", dim);
        PBErrCatch(PBMathErr);
    }
#endif
// If the new dimension is the same as the current one
if (dim == VecGetDim(that)) {
    // Return the clone of the vector
    return VecClone(that);
}
// Else, the new dimension is actually different

```

```

    } else {
        // Declare the returned vector
        VecFloat* ret = VecFloatCreate(dim);
        // Copy the components
        for (long iAxis = MIN(VecGetDim(that), dim); iAxis--;)
            VecSet(ret, iAxis, VecGet(that, iAxis));
        // Return the new vector
        return ret;
    }
}

// ----- MatFloat

// ===== Define =====

// ===== Functions implementation =====

// Create a new MatFloat of dimension 'dim' (nbc, nbl)
// Values are initialized to 0.0
MatFloat* MatFloatCreate(const VecShort2D* const dim) {
#ifdef BUILDMODE == 0
    if (dim == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'dim' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Allocate memory
    long d = VecGet(dim, 0) * VecGet(dim, 1);
    MatFloat* that = PBErrMalloc(PBMathErr, offsetof(MatFloat, _val) +
        sizeof(float) * d);
    // Set the dimensions
    *(VecShort2D*)&(that->_dim) = *dim;
    // Set the default values
    for (long i = d; i--;)
        that->_val[i] = 0.0;
    // Return the new MatFloat
    return that;
}

// Clone the MatFloat
MatFloat* _MatFloatClone(const MatFloat* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create a clone
    MatFloat* clone = MatFloatCreate(&(that->_dim));
    // Copy the values
    long d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
    for (long i = d; i--;)
        clone->_val[i] = that->_val[i];
    // Return the clone
    return clone;
}

// Function which return the JSON encoding of 'that'
JSONNode* _MatFloatEncodeAsJSON(MatFloat* const that) {
#ifdef BUILDMODE == 0

```

```

    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the JSON structure
    JSONNode* json = JSONCreate();
    // Declare a buffer to convert value into string
    char val[100];
    // Encode the dimensions
    sprintf(val, "%d", VecGet(&(that->_dim), 0));
    JSONAddProp(json, "_nbRow", val);
    sprintf(val, "%d", VecGet(&(that->_dim), 1));
    JSONAddProp(json, "_nbCol", val);
    // Encode the values
    JSONArrayVal setVal = JSONArrayValCreateStatic();
    VecShort2D index = VecShortCreateStatic2D();
    do {
        sprintf(val, "%f", MatGet(that, &index));
        JSONArrayValAdd(&setVal, val);
    } while (VecStep(&index, &(that->_dim)));
    JSONAddProp(json, "_val", &setVal);
    // Free memory
    JSONArrayValFlush(&setVal);
    // Return the created JSON
    return json;
}

// Function which decode from JSON encoding 'json' to 'that'
bool _MatFloatDecodeAsJSON(MatFloat** that, JSONNode* json) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (json == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'json' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // If 'that' is already allocated
    if (*that != NULL)
        // Free memory
        _MatFloatFree(that);
    // Get the dimensions from the JSON
    JSONNode* prop = JSONProperty(json, "_nbRow");
    if (prop == NULL) {
        return false;
    }
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, atoi(JSONLblVal(prop)));
    prop = JSONProperty(json, "_nbCol");
    if (prop == NULL) {
        return false;
    }
    VecSet(&dim, 1, atoi(JSONLblVal(prop)));
    // If data are invalid
    if (VecGet(&dim, 0) < 1 || VecGet(&dim, 1) < 1)
        return false;
}

```

```

    // Allocate memory
    *that = MatFloatCreate(&dim);
    // Get the values
    prop = JSONProperty(json, "_val");
    if (prop == NULL) {
        return false;
    }
    VecShort2D index = VecShortCreateStatic2D();
    int i = 0;
    do {
        MatSet(*that, &index, atof(JSONLabel(JSONValue(prop, i))));
        ++i;
    } while (VecStep(&index, &dim));
    // Return the success code
    return true;
}

// Load the MatFloat from the stream
// If the MatFloat is already allocated, it is freed before loading
// Return true upon success, else false
bool _MatFloatLoad(MatFloat** that, FILE* stream) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a json to load the encoded data
    JSONNode* json = JSONCreate();
    // Load the whole encoded data
    if (!JSONLoad(json, stream)) {
        return false;
    }
    // Decode the data from the JSON
    if (!MatDecodeAsJSON(that, json)) {
        return false;
    }
    // Free the memory used by the JSON
    JSONFree(&json);
    // Return the success code
    return true;
}

// Save the MatFloat to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true upon success, else false
bool _MatFloatSave(MatFloat* const that, FILE* stream, bool compact) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (stream == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
    }
#endif
}

```



```

        sprintf(PBMathErr->_msg, "'stream' is null");
        PBErCatch(PBMathErr);
    }
#endif
    // Get the JSON encoding
    JSONNode* json = MatEncodeAsJSON(that);
    // Save the JSON
    if (!JSONSave(json, stream, compact)) {
        return false;
    }
    // Free memory
    JSONFree(&json);
    // Return success code
    return true;
}

// Free the memory used by a MatFloat
// Do nothing if arguments are invalid
void _MatFloatFree(MatFloat** that) {
    // Check argument
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    free(*that);
    *that = NULL;
}

// Print the MatFloat on 'stream' with 'prec' digit precision
// Do nothing if arguments are invalid
void MatFloatPrintln(MatFloat* const that, FILE* stream, unsigned int prec) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (stream == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'stream' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Create the format string
    char format[100] = {'\0'};
    sprintf(format, "%%. %df", prec);
    // Print the values
    fprintf(stream, "[");
    VecShort2D index = VecShortCreateStatic2D();
    do {
        if (VecGet(&index, 1) != 0 || VecGet(&index, 0) != 0)
            fprintf(stream, " ");
        fprintf(stream, format, MatGet(that, &index));
        if (VecGet(&index, 0) < VecGet(&(that->_dim), 0) - 1)
            fprintf(stream, ",");
        if (VecGet(&index, 0) == VecGet(&(that->_dim), 0) - 1) {
            if (VecGet(&index, 1) == VecGet(&(that->_dim), 1) - 1)
                fprintf(stream, "]");
            fprintf(stream, "\n");
        }
    } while (VecPStep(&index, &(that->_dim)));
}

```

```

// Return the inverse matrix of 'that'
// The matrix must be a square matrix
// Return NULL if the matrix is not invertible, or in some case when
// the matrix's diagonal contains null values and the matrix's size
// is greater than 3
MatFloat* _MatFloatGetInv(const MatFloat* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGet(&(that->_dim), 0) != VecGet(&(that->_dim), 1)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "the matrix is not square (%dx%d)",
            VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
        PBErrCatch(PBMathErr);
    }
#endif
    // Allocate memory for the result
    MatFloat* res = NULL;
    // If the matrix is of dimension 1x1
    if (VecGet(&(that->_dim), 0) == 1) {
        if (fabs(that->_val[0]) > PBMath_EPSILON) {
            // Allocate memory for the result
            res = MatFloatCreate(&(that->_dim));
            res->_val[0] = 1.0 / that->_val[0];
        }
    }
    // If the matrix is of dimension 2x2
    } else if (VecGet(&(that->_dim), 0) == 2) {
        float det = that->_val[0] * that->_val[3] -
            that->_val[2] * that->_val[1];
        if (!ISEQUALF(det, 0.0)) {
            // Allocate memory for the result
            res = MatFloatCreate(&(that->_dim));
            res->_val[0] = that->_val[3] / det;
            res->_val[1] = -1.0 * that->_val[1] / det;
            res->_val[2] = -1.0 * that->_val[2] / det;
            res->_val[3] = that->_val[0] / det;
        }
    }
    // Else, the matrix dimension is 3x3
    } else if (VecGet(&(that->_dim), 0) == 3) {
        float det =
            that->_val[0] *
                (that->_val[4] * that->_val[8] -
                 that->_val[5] * that->_val[7]) -
            that->_val[3] *
                (that->_val[1] * that->_val[8] -
                 that->_val[2] * that->_val[7]) +
            that->_val[6] *
                (that->_val[1] * that->_val[5] -
                 that->_val[2] * that->_val[4]);
        if (!ISEQUALF(det, 0.0)) {
            // Allocate memory for the result
            res = MatFloatCreate(&(that->_dim));
            res->_val[0] = (that->_val[4] * that->_val[8] -
                that->_val[5] * that->_val[7]) / det;
            res->_val[1] = -(that->_val[1] * that->_val[8] -
                that->_val[2] * that->_val[7]) / det;
            res->_val[2] = (that->_val[1] * that->_val[5] -
                that->_val[2] * that->_val[4]) / det;
            res->_val[3] = -(that->_val[3] * that->_val[8] -

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        that->_val[5] * that->_val[6]) / det;
res->_val[4] = (that->_val[0] * that->_val[8] -
        that->_val[2] * that->_val[6]) / det;
res->_val[5] = -(that->_val[0] * that->_val[5] -
        that->_val[2] * that->_val[3]) / det;
res->_val[6] = (that->_val[3] * that->_val[7] -
        that->_val[4] * that->_val[6]) / det;
res->_val[7] = -(that->_val[0] * that->_val[7] -
        that->_val[1] * that->_val[6]) / det;
res->_val[8] = (that->_val[0] * that->_val[4] -
        that->_val[1] * that->_val[3]) / det;
    }
} else {
    // Clone the matrix to be inverted
    res = MatClone(that);
    // Farooq Hamid algorithm (modified to handle some matrix with null
    // values on the diagonal)
    // https://www.researchgate.net/publication/
    // 220337322_An_Efficient_and_Simple_Algorithm_for_Matrix_Inversion
    //float det = 1.0;
    short size = VecGet(&(that->_dim), 0);
    float* mat = res->_val;
    bool flagHasChanged = true;
    short nbRemaining = size;
    bool* hasPivotChanged = PBErrMalloc(PBMathErr, size * sizeof(bool));
    for(short p = 0; p < size; ++p) {
        hasPivotChanged[p] = false;
    }
    while (flagHasChanged == true && nbRemaining > 0) {
        flagHasChanged = false;
        for(short p = 0; p < size; ++p) {
            float pivot = mat[p * size + p];
            if (fabs(pivot) > FLT_MIN && !(hasPivotChanged[p])) {
                flagHasChanged = true;
                --nbRemaining;
                hasPivotChanged[p] = true;
                //det *= pivot;
                for (short i = 0; i < size; ++i) {
                    mat[i * size + p] = -1.0 * mat[i * size + p] / pivot;
                }
                for (short i = 0; i < size; ++i) {
                    if (i != p) {
                        for (short j = 0; j < size; ++j) {
                            if (j != p) {
                                mat[i * size + j] =
                                    mat[i * size + j] + mat[p * size + j] * mat[i * size + p];
                            }
                        }
                    }
                }
                for (short j = 0; j < size; ++j) {
                    mat[p * size + j] = mat[p * size + j] / pivot;
                }
                mat[p * size + p] = 1.0 / pivot;
            }
        }
    }
}
free(hasPivotChanged);
if (nbRemaining > 0) {
    MatFree(&res);
    return NULL;
}
}

```

```

    }
    // Return the result
    return res;
}

// Return the product of matrix 'that' and vector 'v'
// Number of column of 'that' must equal dimension of 'v'
VecFloat* _MatFloatGetProdVecFloat(
    const MatFloat* const that, const VecFloat* v) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (v == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'v' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGet(&(that->_dim), 0) != VecGetDim(v)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "the matrix and vector have incompatible dimensions (%d==%ld)",
            VecGet(&(that->_dim), 0), VecGetDim(v));
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the index in the matrix
    VecShort2D i = VecShortCreateStatic2D();
    // Allocate memory for the solution
    VecFloat* ret = VecFloatCreate(VecGet(&(that->_dim), 1));
    // If we could allocate memory
    if (ret != NULL)
        for (VecSet(&i, 0, 0); VecGet(&i, 0) < VecGet(&(that->_dim), 0); VecSetAdd(&i, 0, 1))
            for (VecSet(&i, 1, 0); VecGet(&i, 1) < VecGet(&(that->_dim), 1); VecSetAdd(&i, 1, 1))
                VecSetAdd(ret, VecGet(&i, 1),
                    VecGet(v, VecGet(&i, 0)) * MatGet(that, &i));
    // Return the result
    return ret;
}

// Return the product of vector 'v' and transpose of vector 'w'
MatFloat* _MatFloatGetProdVecVecTransposeFloat(
    const VecFloat* const v,
    const VecFloat* const w) {
#ifdef BUILDMODE == 0
    if (v == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'v' is null");
        PBErrCatch(PBMathErr);
    }
    if (w == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'w' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the position in the matrix
    VecShort2D pos = VecShortCreateStatic2D();
    // Allocate memory for the solution
    VecShort2D dim = VecShortCreateStatic2D();

```

```

    VecSet(&dim, 0, VecGetDim(w));
    VecSet(&dim, 1, VecGetDim(v));
    MatFloat* ret = MatFloatCreate(&dim);
    // Calculate the result
    do {
        MatSet(ret, &pos,
            VecGet(v, VecGet(&pos, 1)) * VecGet(w, VecGet(&pos, 0)));
    } while(VecStep(&pos, &dim));
    // Return the result
    return ret;
}

// Return the product of matrix 'that' by matrix 'tho'
// Number of columns of 'that' must equal number of line of 'tho'
MatFloat* _MatFloatGetProdMatFloat(const MatFloat* const that, const MatFloat* tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (VecGet(&(that->_dim), 0) != VecGet(&(tho->_dim), 1)) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg,
                "the matrices have incompatible dimensions (%d==%d)",
                VecGet(&(that->_dim), 0), VecGet(&(tho->_dim), 1));
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare 3 variables to memorize the index in the matrix
    VecShort2D i = VecShortCreateStatic2D();
    VecShort2D j = VecShortCreateStatic2D();
    VecShort2D k = VecShortCreateStatic2D();
    // Allocate memory for the solution
    VecSet(&i, 0, VecGet(&(tho->_dim), 0));
    VecSet(&i, 1, VecGet(&(that->_dim), 1));
    MatFloat* ret = MatFloatCreate(&i);
    for (VecSet(&i, 0, 0); VecGet(&i, 0) < VecGet(&(tho->_dim), 0); VecSetAdd(&i, 0, 1))
        for (VecSet(&i, 1, 0); VecGet(&i, 1) < VecGet(&(that->_dim), 1); VecSetAdd(&i, 1, 1))
            for (VecSet(&j, 0, 0), VecSet(&j, 1, VecGet(&i, 1)),
                VecSet(&k, 0, VecGet(&i, 0)), VecSet(&k, 1, 0);
                VecGet(&j, 0) < VecGet(&(that->_dim), 0);
                VecSetAdd(&j, 0, 1),
                VecSetAdd(&k, 1, 1)) {
                MatSet(ret, &i, MatGet(ret, &i) +
                    MatGet(that, &j) * MatGet(tho, &k));
            }
    // Return the result
    return ret;
}

// Return true if 'that' is equal to 'tho', false else
bool _MatFloatIsEqual(MatFloat* const that, MatFloat* tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");

```

```

    PBErCatch(PBMathErr);
}
if (tho == NULL) {
    PBMathErr->_type = PBErTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErCatch(PBMathErr);
}
#endif
if (!VecIsEqual(&(that->_dim), &(tho->_dim)))
    return false;
VecShort2D v = VecShortCreateStatic2D();
do {
    if (!ISEQUALF(MatGet(that, &v), MatGet(tho, &v)))
        return false;
} while (VecStep(&v, &(that->_dim)));
return true;
}

// Calculate the Eigen values and vectors of the MatFloat 'that'
// Return a set of VecFloat. The first VecFloat of the set contains
// the Eigen values, with values sorted from biggest to
// smallest (in absolute value). The following VecFloat are the
// respectiev Eigen vectors
// 'that' must be a 2D square matrix
// Return the identity if the QR decompostion fails
// http://madrury.github.io/jekyll/update/statistics/2017/10/04/qr-algorithm.html
// TODO: should be improved with the Hessenberg QR method
// https://www.math.kth.se/na/SF2524/matber15/qrmethod.pdf
GSetVecFloat _MatFloatGetEigenValues(const MatFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (VecGet(MatDim(that), 0) != VecGet(MatDim(that), 1)) {
        PBMathErr->_type = PBErTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' is not squared");
        PBErCatch(PBMathErr);
    }
#endif
    // Declare the result set
    GSetVecFloat set = GSetVecFloatCreateStatic();
    // Clone the original matrix
    MatFloat* A = MatClone(that);
    // Create a matrix to compute the Eigen vectors
    MatFloat* Q = MatFloatCreate(MatDim(that));
    MatSetIdentity(Q);
    // Apply the QR algorithm
    VecShort2D pos = VecShortCreateStatic2D();
    float err = 0.0;
    do {
        QRDecomp QR = MatGetQR(A);
        if (QR._Q != NULL) {
            MatFloat* RQ = MatGetProdMat(QR._R, QR._Q);
            MatFree(&A);
            A = RQ;
            MatFloat* M = MatGetProdMat(Q, QR._Q);
            MatFree(&Q);
            Q = M;
            err = 0.0;
            do {

```

```

        if (VecGet(&pos, 0) != VecGet(&pos, 1))
            err = MAX(err, fabs(MatGet(A, &pos)));
    } while (VecStep(&pos, MatDim(A)));
    QRDecompFreeStatic(&QR);
} else {
    MatSetIdentity(A);
    MatSetIdentity(Q);
    err = 0.0;
}
} while (err > PBMATH_EPSILON);
// Extract the results
VecFloat* values = VecFloatCreate(MatGetNbCol(that));
GSetPush(&set, values);
for (int i = 0; i < MatGetNbCol(that); ++i) {
    VecSet(&pos, 0, i);
    VecSet(&pos, 1, i);
    VecSet(values, i, MatGet(A, &pos));
    GSetAppend(&set, VecFloatCreate(MatGetNbCol(that)));
}
VecSetNull(&pos);
do {
    VecSet(GSetGet(&set, 1 + VecGet(&pos, 0)), VecGet(&pos, 1),
        MatGet(Q, &pos));
} while (VecStep(&pos, MatDim(Q)));
// Free memory
MatFree(&A);
MatFree(&Q);
// Return the result
return set;
}

// Calculate the QR decomposition of the MatFloat 'that' using the
// Householder algorithm
// Return {NULL, NULL} if the MatFloat couldn't be decomposed
// http://www.seas.ucla.edu/~vandenbe/133A/lectures/qr.pdf
QRDecomp_MatFloatGetQR(const MatFloat* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (MatGetNbCol(that) > MatGetNbRow(that)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'that' must have at least as many rows as columns (%d<=%d)",
            MatGetNbCol(that), MatGetNbRow(that));
        PBErrCatch(PBMathErr);
    }
#endif
}

// Allocate memory for the final R matrix
VecShort2D dimR = VecShortCreateStatic2D();
VecSet(&dimR, 0, MatGetNbCol(that));
VecSet(&dimR, 1, MatGetNbCol(that));
MatFloat* R = MatFloatCreate(&dimR);

// Allocate memory for the final Q matrix
MatFloat* Q = MatFloatCreate(MatDim(that));

// Allocate memory for the QQ~ matrix
VecShort2D dimQQtilde = VecShortCreateStatic2D();

```

```

VecSet(&dimQQtilde, 0, MatGetNbRow(that));
VecSet(&dimQQtilde, 1, MatGetNbRow(that));
MatFloat* QQtilde = MatFloatCreate(&dimQQtilde);
MatSetIdentity(QQtilde);

// Create a clone of that to be overwritten during computation
MatFloat* A = MatClone(that);

// Declare two vectors to access value in the arrays
VecShort2D pos = VecShortCreateStatic2D();
VecShort2D shiftPos = VecShortCreateStatic2D();

// Householder algorithm
for (short k = 0; k < MatGetNbCol(that); ++k) {

    // Calculate w
    VecFloat* w = VecFloatCreate(MatGetNbRow(that) - k);
    VecSet(&pos, 0, k);
    for (short i = 0; i < VecGetDim(w); ++i) {
        VecSet(&pos, 1, k + i);
        VecSet(w, i, MatGet(A, &pos));
    }
    if (ISEQUALF(VecNorm(w), 0.0)) {
        MatFree(&R);
        MatFree(&Q);
        MatFree(&QQtilde);
        MatFree(&A);
        VecFree(&w);
        return (QRDecomp){._Q = NULL, ._R = NULL};
    }
    float sign = (VecGet(w, 0) >= 0.0 ? 1.0 : -1.0);
    VecSet(w, 0, VecGet(w, 0) + sign * VecNorm(w));

    // Calculate v = w / ||w||
    VecFloat* v = VecClone(w);
    VecNormalise(v);

    //
    // I 0
    // Calculate the reflector 0 H where H = I - 2vv^t
    VecShort2D dimH = VecShortCreateStatic2D();
    VecSet(&dimH, 0, VecGetDim(v));
    VecSet(&dimH, 1, VecGetDim(v));
    MatFloat* H = MatFloatCreate(&dimH);
    MatSetIdentity(H);
    MatFloat* vvt = MatGetProdVecVecTranspose(v, v);
    MatScale(vvt, -2.0);
    MatAdd(H, vvt);
    MatFloat* reflector = MatFloatCreate(&dimQQtilde);
    MatSetIdentity(reflector);
    VecSetNull(&pos);
    do {
        VecSet(&shiftPos, 0, VecGet(&pos, 0) + k);
        VecSet(&shiftPos, 1, VecGet(&pos, 1) + k);
        MatSet(reflector, &shiftPos, MatGet(H, &pos));
    } while (VecStep(&pos, &dimH));

    // Update A := reflector . A
    MatFloat* M = MatGetProdMat(reflector, A);
    MatFree(&A);
    A = M;

    // Update QQtilde := QQtilde.reflector

```



```

    M = MatGetProdMat(QQtilde, reflector);
    MatFree(&QQtilde);
    QQtilde = M;

    // Free memory
    MatFree(&reflector);
    MatFree(&H);
    MatFree(&vvt);
    VecFree(&v);
    VecFree(&w);
}

// Extract R from the final A
VecSetNull(&pos);
do {
    MatSet(R, &pos, MatGet(A, &pos));
} while (VecStep(&pos, &dimR));

// Extract Q from the final QQtilde
VecSetNull(&pos);
do {
    MatSet(Q, &pos, MatGet(QQtilde, &pos));
} while (VecStep(&pos, MatDim(that)));

// Create the result QR decomposition
QRDecomp qr = {._Q = Q, ._R = R};

// Free memory
MatFree(&A);
MatFree(&QQtilde);

// Return the decomposition
return qr;
}

// Calculate the transposed of the MatFloat 'that'
MatFloat* _MatFloatGetTranspose(const MatFloat* const that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Allocate memory for the result matrix
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, VecGet(MatDim(that), 1));
    VecSet(&dim, 1, VecGet(MatDim(that), 0));
    MatFloat* res = MatFloatCreate(&dim);
    // Calculate the transposed matrix
    VecShort2D pos = VecShortCreateStatic2D();
    VecShort2D posB = VecShortCreateStatic2D();
    do {
        VecSet(&posB, 0, VecGet(&pos, 1));
        VecSet(&posB, 1, VecGet(&pos, 0));
        MatSet(res, &pos, MatGet(that, &posB));
    } while (VecStep(&pos, &dim));
    // Return the transposed matrix
    return res;
}

```

```

// ----- Gauss

// ===== Define =====

// ===== Functions implementation =====

// Create a new Gauss of mean 'mean' and sigma 'sigma'
// Return NULL if we couldn't create the Gauss
Gauss* GaussCreate(const float mean, const float sigma) {
    // Allocate memory
    Gauss *that = PBErrMalloc(PBMathErr, sizeof(Gauss));
    // Set properties
    that->_mean = mean;
    that->_sigma = sigma;
    // Return the new Gauss
    return that;
}

Gauss GaussCreateStatic(const float mean, const float sigma) {
    // Allocate memory
    Gauss that = {._mean = mean, ._sigma = sigma};
    // Return the new Gauss
    return that;
}

// Free the memory used by a Gauss
// Do nothing if arguments are invalid
void GaussFree(Gauss** that) {
    // Check argument
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    free(*that);
    *that = NULL;
}

// ----- SysLinEq

// ===== Functions implementation =====

// Create a new SysLinEq with matrix 'm' and vector 'v'
// The dimension of 'v' must be equal to the number of column of 'm'
// If 'v' is null the vector null is used instead
// The matrix 'm' must be a square matrix
// Return NULL if we couldn't create the SysLinEq
SysLinEq* _SLECreate(const MatFloat* const m, const VecFloat* const v) {
#ifdef BUILDMODE == 0
    if (m == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'m' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGet(&(m->_dim), 0) != VecGet(&(m->_dim), 1)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "the matrix is not square (%dx%d)",
            VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1));
        PBErrCatch(PBMathErr);
    }
    if (v != NULL) {
        if (VecGet(&(m->_dim), 0) != VecGetDim(v)) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg,
                "the matrix and vector have incompatible dimensions (%d==%ld)",

```

```

        VecGet(&(m->_dim), 0), VecGetDim(v));
    PBErCatch(PBMathErr);
}
}
#endif
// Allocate memory
SysLinEq* that = PBErMalloc(PBMathErr, sizeof(SysLinEq));
that->_M = MatClone(m);
that->_Minv = MatGetInv(that->_M);
if (v != NULL)
    that->_V = VecClone(v);
else
    that->_V = VecFloatCreate(VecGet(&(m->_dim), 0));
if (that->_M == NULL || that->_V == NULL || that->_Minv == NULL) {
#if BUILDMODE == 0
    if (that->_M == NULL) {
        PBMathErr->_type = PBErTypeOther;
        sprintf(PBMathErr->_msg, "couldn't create the matrix");
        PBErCatch(PBMathErr);
    }
    if (that->_Minv == NULL) {
        PBMathErr->_type = PBErTypeOther;
        sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
        PBErCatch(PBMathErr);
    }
    if (that->_V == NULL) {
        PBMathErr->_type = PBErTypeOther;
        sprintf(PBMathErr->_msg, "couldn't create the vector");
        PBErCatch(PBMathErr);
    }
}
#endif
SysLinEqFree(&that);
}
// Return the new SysLinEq
return that;
}

// Free the memory used by the SysLinEq
// Do nothing if arguments are invalid
void SysLinEqFree(SysLinEq** that) {
    // Check arguments
    if (that == NULL || *that == NULL)
        return;
    // Free memory
    MatFree(&((*that)->_M));
    MatFree(&((*that)->_Minv));
    VecFree(&((*that)->_V));
    free(*that);
    *that = NULL;
}

// Clone the SysLinEq 'that'
// Return NULL if we couldn't clone the SysLinEq
SysLinEq* SysLinEqClone(const SysLinEq* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
}
#endif
// Declare a variable for the result

```

```

SysLinEq* ret = PBErrMalloc(PBMathErr, sizeof(SysLinEq));
ret->_M = MatClone(that->_M);
ret->_Minv = MatClone(that->_Minv);
ret->_V = VecClone(that->_V);
if (ret->_M == NULL || ret->_V == NULL || ret->_Minv == NULL)
    SysLinEqFree(&ret);
// Return the new SysLinEq
return ret;
}

// ----- Ratio

// ===== Functions implementation =====

// Create a new static Ratio
Ratio RatioCreateStatic(long b, unsigned int n, unsigned int d) {
#ifdef BUILDMODE == 0
    if (d == 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'d' is invalid (%u > 0)", d);
        PBErrCatch(PBMathErr);
    }
#endif

    // Create the Ratio
    Ratio ratio = {
        ._base = b,
        ._numerator = n,
        ._denominator = d
    };

    // Return the Ratio
    return ratio;
}

// Convert the float 'v' into the nearest Ratio using the Farey's algorithm
// given the precision 'prec'
Ratio RatioFromFloatPrec(float v, float prec) {

    // Create the two bounding Ratio
    Ratio ratioLow = RatioCreateStatic(0, 0, 1);
    Ratio ratioHigh = RatioCreateStatic(0, 1, 1);

    // Create the result ratio
    Ratio ratio = RatioCreateStatic(floor(v), 0, 1);

    // Get the decimals of 'v'
    float dec = v - RatioGetBase(&ratio);

    // Loop until the bounding Ratio reaches the requested precision
    Ratio mediant;
    while(
        RatioToFloat(&ratioHigh) - RatioToFloat(&ratioLow) > prec &&
        fabs(RatioToFloat(&ratioHigh) - dec) > prec &&
        fabs(RatioToFloat(&ratioLow) - dec) > prec) {

        mediant = RatioCreateStatic(0,
            RatioGetNumerator(&ratioLow) + RatioGetNumerator(&ratioHigh),
            RatioGetDenominator(&ratioLow) + RatioGetDenominator(&ratioHigh));

        if (RatioToFloat(&mediant) > dec) {

```

```

        ratioHigh = mediant;

    } else {

        ratioLow = mediant;

    }

}

// Update the fractional part of the result
if (fabs(RatioToFloat(&ratioHigh) - dec) <= prec) {

    RatioSetNumerator(&ratio, RatioGetNumerator(&ratioHigh));
    RatioSetDenominator(&ratio, RatioGetDenominator(&ratioHigh));

} else if (fabs(RatioToFloat(&ratioLow) - dec) <= prec) {

    RatioSetNumerator(&ratio, RatioGetNumerator(&ratioLow));
    RatioSetDenominator(&ratio, RatioGetDenominator(&ratioLow));

} else {

    RatioSetNumerator(&ratio, RatioGetNumerator(&mediant));
    RatioSetDenominator(&ratio, RatioGetDenominator(&mediant));

}

// Reduce the result
RatioReduce(&ratio);

// Return the result
return ratio;

}

// Convert the Ratio 'that' into a float
float RatioToFloat(const Ratio* that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the Ratio converted to float
    return (float)RatioGetBase(that) +
        (float)RatioGetNumerator(that) / (float)RatioGetDenominator(that);
}

// Reduce the fractional part of the Ratio 'that' and update the base such as
// numerator < denominator
void RatioReduce(Ratio* that) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
}

```

```

// If the numerator is greater than the denominator
if (RatioGetNumerator(that) >= RatioGetDenominator(that)) {

    // Update the component to keep the fractional part less than 1.0
    unsigned int delta = RatioGetNumerator(that) / RatioGetDenominator(that);
    RatioSetBase(that, RatioGetBase(that) + delta);
    RatioSetNumerator(that,
        RatioGetNumerator(that) - delta * RatioGetDenominator(that));

}

// Get the GCD of the numerator and denominator
unsigned int div = GetGCD(
    RatioGetNumerator(that), RatioGetDenominator(that));
// Divide the numerator and denominator by the gcd
RatioSetNumerator(that, RatioGetNumerator(that) / div);
RatioSetDenominator(that, RatioGetDenominator(that) / div);

}

// Print the Ratio on 'stream' as a+b/c
void RatioPrint(const Ratio* that, FILE* stream) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'that' is null");
        PBErrCatch(PBMATHERR);
    }
    if (stream == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'stream' is null");
        PBErrCatch(PBMATHERR);
    }
}
#endif

    fprintf(stream, "%ld+%u/%u",
        RatioGetBase(that), RatioGetNumerator(that), RatioGetDenominator(that));

}

// ----- Usefull basic functions

// ===== Functions implementation =====

// Compute the 'iElem'-th element of the 'base'-ary version of the
// Thue-Morse sequence
// 'iElem' >= 0
// 'base' >= 2
long ThueMorseSeqGetNthElem(long iElem, long base) {
#ifdef BUILDMODE == 0
    if (iElem < 0) {
        PBMATHERR->_type = PBErrTypeInvalidArg;
        sprintf(PBMATHERR->_msg, "'iElem' is invalid (%ld>=0)", iElem);
        PBErrCatch(PBMATHERR);
    }
    if (base < 2) {
        PBMATHERR->_type = PBErrTypeInvalidArg;
        sprintf(PBMATHERR->_msg, "'base' is invalid (%ld>=2)", base);
        PBErrCatch(PBMATHERR);
    }
}
#endif
    if (base > iElem) {

```

```

        return iElem;
    } else {
        ldiv_t d = ldiv(iElem, base);
        return (ThueMorseSeqGetNthElem(d.quot, base) + d.rem) % base;
    }
}

// Return a set of two vectors containing the bounds of the vectors in
// the GSet 'that'
// The set must have at least one element
// The returned set is ordered as follow: (boundMin, boundMax)
GSetVecFloat _GSetVecFloatGetBounds(const GSetVecFloat* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (GSetNbElem(that) < 1) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'that' is empty");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Create the set containing the bounds
    GSetVecFloat bounds = GSetVecFloatCreateStatic();
    // Create the two bounds vector, initialised with the first vector of
    // the set
    VecFloat* boundMin = _VecFloatClone(GSetGet(that, 0));
    VecFloat* boundMax = _VecFloatClone(GSetGet(that, 0));
    GSetAppend(&bounds, boundMin);
    GSetAppend(&bounds, boundMax);
    // Get the dimension of the vectors, supposes they are all with same
    // dimension
    long dim = _VecFloatGetDim(boundMin);
    // Loop on the vectors of the set, expect the first one
    GSetIterForward iter = GSetIterForwardCreateStatic(that);
    while (GSetIterStep(&iter)) {
        VecFloat* v = GSetIterGet(&iter);
        // Loop on dimension
        for (int iDim = dim; iDim--;) {
            // Update bounds
            if (_VecFloatGet(boundMin, iDim) > _VecFloatGet(v, iDim))
                _VecFloatSet(boundMin, iDim, _VecFloatGet(v, iDim));
            if (_VecFloatGet(boundMax, iDim) < _VecFloatGet(v, iDim))
                _VecFloatSet(boundMax, iDim, _VecFloatGet(v, iDim));
        }
    }
    // Return the set containing the bounds
    return bounds;
}

// Compute the area of a triangle knowing its 3 sides length 'a', 'b', 'c'
// using the Hero's formula
double GetAreaTriangleHero(
    const double a,
    const double b,
    const double c) {

    double s = 0.5 * (a + b + c);
    double area = sqrt(s * (s - a) * (s - b) * (s - c));
    return area;
}

```

```

}

// Return the Fibonacci sequence up to the 'n'-th element in a dynamically
// allocated array of unsigned long
unsigned long* GetFibonacciSeq(unsigned int n) {

    if (n == 0) {

        return NULL;

    } else {

        unsigned long* seq =
            PBErrMalloc(
                PBMathErr,
                sizeof(unsigned long) * n);
        for (
            unsigned int i = 0;
            i < n && i < 2;
            ++i) {

            seq[i] = 1L;

        }
        for (
            unsigned int i = 2;
            i < n;
            ++i) {

            seq[i] = seq[i - 1] + seq[i - 2];

        }

        return seq;

    }

}

// Return the Fibonacci grid lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [0,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciGridLattice(
    unsigned int n,
    unsigned long* nbPoints) {

#ifdef BUILDMODE == 0

    if (nbPoints == NULL) {

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'nbPoints' is null");
        PBErrCatch(PBMathErr);

    }

#endif

    if (n == 0) {

        *nbPoints = 0;

    }

}

```



```

        return NULL;
    } else {
        // Get the Fibonacci sequence
        unsigned long* seq = GetFibonacciSeq(n);

        // Update the number of points
        *nbPoints = seq[n - 1];

        // Allocate memory for the result
        float* lattice =
            PBErrMalloc(
                PBMathErr,
                sizeof(float) * 2L * (*nbPoints));

        // Generate the lattice points
        for (
            unsigned long iPoint = 0;
            iPoint < *nbPoints;
            ++iPoint) {

            lattice[iPoint * 2L] =
                fmodf(
                    (float)iPoint / (float)seq[n > 1 ? n - 1 : 0],
                    1.0);
            lattice[iPoint * 2L + 1L] =
                fmodf(
                    (float)iPoint * (float)seq[n > 2 ? n - 2 : 0] /
                    (float)seq[n > 1 ? n - 1 : 0],
                    1.0);

        }

        // Free memory
        free(seq);

        // Return the lattice
        return lattice;
    }
}

// Return the Fibonacci polar lattice for the 'n'-th Fibonacci number in a
// dynamically allocated array of pairs of float in [-1,1]
// Stores the nb of points in 'nbPoints'
float* GetFibonacciPolarLattice(
    unsigned int n,
    unsigned long* nbPoints) {
    #if BUILDMODE == 0

        if (nbPoints == NULL) {

            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'nbPoints' is null");
            PBErrCatch(PBMathErr);

        }

    #endif
}

```

```

// Get the grid lattice
float* lattice =
    GetFibonacciGridLattice(
        n,
        nbPoints);

// Convert each points to polar coordinates
for (
    unsigned long iPoint = *nbPoints;
    iPoint--;) {

    lattice[iPoint * 2L] = sqrt(lattice[iPoint * 2L]);
    lattice[iPoint * 2L + 1L] = 2.0 * PBMATH_PI * lattice[iPoint * 2L + 1L];

}

// Return the lattice
return lattice;

}

// Return the greatest common divisor using the Stein's algorithm
// https://en.wikipedia.org/wiki/Binary_GCD_algorithm
unsigned int GetGCD(unsigned int u, unsigned int v) {

    unsigned int shift = 0;
    if (u == 0)
        return v;
    if (v == 0)
        return u;
    while ((u | v) & 1) == 0 {
        ++shift;
        u >>= 1;
        v >>= 1;
    }
    while ((u & 1) == 0)
        u >>= 1;
    do {
        while ((v & 1) == 0)
            v >>= 1;
        if (u > v) {
            unsigned int t = v;
            v = u;
            u = t;
        }
        v -= u;
    } while (v != 0);
    return u << shift;

}

// ----- LeastSquareLinReg

// ===== Functions implementation =====

// Create a new static LeastSquareLinReg
LeastSquareLinReg LeastSquareLinRegCreateStatic(MatFloat* X) {

#if BUILDMODE == 0

    if (X == NULL) {

```

```

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'X' is null");
        PBErrCatch(PBMathErr);
    }

#endif

    // Declare the new LeastSquareLin
    LeastSquareLinReg that;

    // Set the properties
    that.Xp = NULL;
    LSLRSetComp(
        &that,
        X);
    that.bias = 0.0;

    // Return the new LeastSquareLin
    return that;
}

// Free the static LeastSquareLinReg 'that'
void LeastSquareLinRegFreeStatic(LeastSquareLinReg* that) {

    if (that == NULL) {

        return;
    }

    // Free memory
    MatFree(&(that->Xp));
}

// Compute the solution of the LeastSquareLinReg 'that' for 'Y'
VecFloat* LSLRSolve(LeastSquareLinReg* that, const VecFloat* Y) {

#if BUILDMODE == 0

    if (that == NULL) {

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }

    if (that->X == NULL) {

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that->X' is null");
        PBErrCatch(PBMathErr);
    }

    if (that->Xp == NULL) {

        PBMathErr->_type = PBErrTypeNullPointer;

```

```

        sprintf(PBMathErr->_msg, "'that->Xp' is null");
        PBErCatch(PBMathErr);
    }

    if (Y == NULL) {

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'Y' is null");
        PBErCatch(PBMathErr);
    }

#endif

    // Get the result
    VecFloat* beta =
        MatGetProdVec(
            that->Xp,
            Y);

    // Calculate the bias
    VecFloat* Ybeta =
        MatGetProdVec(
            that->X,
            beta);
    VecOp(
        Ybeta,
        1.0,
        Y,
        -1.0);
    that->bias = VecNorm(Ybeta);
    VecFree(&Ybeta);

    // Return the result
    return beta;
}

```

## 3.2 pbmath-inline.c

```

// ===== PBMath_static inline.C =====

// ===== Functions implementation =====

// ----- VecShort

// Static constructors for VecShort
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecShortCreateStatic2D() {
    VecShort2D v = {._val = {0, 0}, ._dim = 2};
    return v;
}
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecShortCreateStatic3D() {
    VecShort3D v = {._val = {0, 0, 0}, ._dim = 3};
}

```

```

    return v;
}
#if BUILDMODE != 0
static inline
#endif
VecShort4D VecShortCreateStatic4D() {
    VecShort4D v = {._val = {0, 0, 0, 0}, ._dim = 4};
    return v;
}

// Return the i-th value of the VecShort
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet(const VecShort* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
            that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    return ((short*)((void*)that) + sizeof(long))[i];
}
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet2D(const VecShort2D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_val[i];
}
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet3D(const VecShort3D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
}

```

```

    }
#endif
    return that->_val[i];
}
#if BUILDMODE != 0
static inline
#endif
short _VecShortGet4D(const VecShort4D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_val[i];
}

// Set the i-th value of the VecShort to v
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet(VecShort* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
            that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    ((short*)((void*)that) + sizeof(long))[i] = v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortSet2D(VecShort2D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] = v;
}
#if BUILDMODE != 0

```

```

static inline
#endif
void _VecShortSet3D(VecShort3D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] = v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecShortSet4D(VecShort4D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] = v;
}

// Set the i-th value of the VecShort to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd(VecShort* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
            that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    ((short*)((void*)that) + sizeof(long))[i] += v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd2D(VecShort2D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {

```

```

    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
}
if (i < 0 || i >= 2) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
    PBErrCatch(PBMathErr);
}
#endif
    that->_val[i] += v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd3D(VecShort3D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAdd4D(VecShort4D* const that, const long i, const short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
}

// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetNull(VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Set values

```



```

    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = 0;
}

// Set all values of the vector 'that' to 'd'
#if BUILDMODE != 0
static inline
#endif
void _VecShortSetAll(VecShort* const that, short v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Set values
    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = v;
}

// Return the dimension of the VecShort
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetDim(const VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_dim;
}

// Return the Hamiltonian distance between the VecShort 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
short _VecShortHamiltonDist(const VecShort* const that, const VecShort* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to calculate the distance
    short ret = 0;
    for (long iDim = VecGetDim(that); iDim--;)
        ret += abs(VecGet(that, iDim) - VecGet(tho, iDim));
}

```

```

        // Return the distance
        return ret;
    }
    #if BUILDMODE != 0
    static inline
    #endif
    short _VecShortHamiltonDist2D(const VecShort2D* const that, const VecShort2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
        // Return the distance
        return abs(VecGet(that, 0) - VecGet(tho, 0)) +
            abs(VecGet(that, 1) - VecGet(tho, 1));
    }
    #if BUILDMODE != 0
    static inline
    #endif
    short _VecShortHamiltonDist3D(const VecShort3D* const that, const VecShort3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
        // Return the distance
        return abs(VecGet(that, 0) - VecGet(tho, 0)) +
            abs(VecGet(that, 1) - VecGet(tho, 1)) +
            abs(VecGet(that, 2) - VecGet(tho, 2));
    }
    #if BUILDMODE != 0
    static inline
    #endif
    short _VecShortHamiltonDist4D(const VecShort4D* const that, const VecShort4D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
        // Return the distance
        return abs(VecGet(that, 0) - VecGet(tho, 0)) +

```

```

        abs(VecGet(that, 1) - VecGet(tho, 1)) +
        abs(VecGet(that, 2) - VecGet(tho, 2)) +
        abs(VecGet(that, 3) - VecGet(tho, 3));
    }

    // Return true if the VecShort 'that' is equal to 'tho', else false
    #if BUILDMODE != 0
    static inline
    #endif
    bool _VecShortIsEqual(const VecShort* const that,
        const VecShort* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
        return
            (memcmp(that->_val, tho->_val, sizeof(short) * that->_dim) == 0);
    }

    // Copy the values of 'tho' in 'that'
    #if BUILDMODE != 0
    static inline
    #endif
    void _VecShortCopy(VecShort* const that, const VecShort* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
        // Copy the values
        memcpy(that->_val, tho->_val, sizeof(short) * that->_dim);
    }

    // Return the dot product of 'that' and 'tho'
    #if BUILDMODE != 0

```

```

static inline
#endif
short _VecShortDotProd(const VecShort* const that,
    const VecShort* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorise the result
    short res = 0;
    // For each component
    for (long iDim = that->_dim; iDim--;)
        // Calculate the product
        res += VecGet(that, iDim) * VecGet(tho, iDim);
    // Return the result
    return res;
}

#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd2D(const VecShort2D* const that,
    const VecShort2D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1);
}

#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd3D(const VecShort3D* const that,
    const VecShort3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
}

```

```

    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1) +
        VecGet(that, 2) * VecGet(tho, 2);
}
#if BUILDMODE != 0
static inline
#endif
short _VecShortDotProd4D(const VecShort4D* const that,
    const VecShort4D* const tho) {
    if (BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    )
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1) +
        VecGet(that, 2) * VecGet(tho, 2) +
        VecGet(that, 3) * VecGet(tho, 3);
}

// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp(VecShort* const that, const short a,
    const VecShort* const tho, const short b) {
    if (BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    )
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim,
            a * VecGet(that, iDim) + b * VecGet(tho, iDim));
}
#if BUILDMODE != 0

```

```

static inline
#endif
void _VecShortOp2D(VecShort2D* const that, const short a,
    const VecShort2D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp3D(VecShort3D* const that, const short a,
    const VecShort3D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortOp4D(VecShort4D* const that, const short a,
    const VecShort4D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    VecSet(that, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
}

```

```

// Return a VecShort equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetOp(const VecShort* const that, const short a,
    const VecShort* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
}
#endif
VecShort* res = VecShortCreate(that->_dim);
for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
        a * VecGet(that, iDim) + b * VecGet(tho, iDim));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetOp2D(const VecShort2D* const that, const short a,
    const VecShort2D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
}
#endif
VecShort2D res = VecShortCreateStatic2D();
VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort3D _VecShortGetOp3D(const VecShort3D* const that, const short a,
    const VecShort3D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");

```

```

        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecShort3D res = VecShortCreateStatic3D();
    VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetOp4D(const VecShort4D* const that, const short a,
    const VecShort4D* const tho, const short b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
}
#endif
    VecShort4D res = VecShortCreateStatic4D();
    VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    VecSet(&res, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
    return res;
}

// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd(VecShort* const that,
    const VecShort* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
}
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
    }
}

```



```

        PBErCatch(PBMathErr);
    }
#endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd2D(VecShort2D* const that,
    const VecShort2D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd3D(VecShort3D* const that,
    const VecShort3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
}
#if BUILDMODE != 0
static inline
#endif
void _VecShortHadamardProd4D(VecShort4D* const that,
    const VecShort4D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif

```

```

    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
    VecSet(that, 3, VecGet(that, 3) * VecGet(tho, 3));
}

// Return a VecShort equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecShort* _VecShortGetHadamardProd(const VecShort* const that,
    const VecShort* const tho) {
    if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
}
#endif
VecShort* res = VecShortCreate(that->_dim);
for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort2D _VecShortGetHadamardProd2D(const VecShort2D* const that,
    const VecShort2D* const tho) {
    if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
}
#endif
VecShort2D res = VecShortCreateStatic2D();
VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
return res;
}
#if BUILDMODE != 0

```

```

static inline
#endif
VecShort3D _VecShortGetHadamardProd3D(const VecShort3D* const that,
    const VecShort3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecShort3D res = VecShortCreateStatic3D();
    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
    return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort4D _VecShortGetHadamardProd4D(const VecShort4D* const that,
    const VecShort4D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecShort4D res = VecShortCreateStatic4D();
    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
    VecSet(&res, 3, VecGet(that, 3) * VecGet(tho, 3));
    return res;
}

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxVal(const VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    short max = VecGet(that, 0);
    // Search for the maximum value

```

```

    for (long i = VecGetDim(that); i-- && i != 0;)
        max = MAX(max, VecGet(that, i));
    // Return the result
    return max;
}

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecShortGetIMaxVal(const VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    long iMax = 0;
    // Declare a variable to memorize the max value
    short max = VecGet(that, iMax);
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;) {
        if (max < VecGet(that, i)) {
            max = VecGet(that, i);
            iMax = i;
        }
    }
    // Return the result
    return iMax;
}

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinVal(const VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    short min = VecGet(that, 0);
    // Search for the minimum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        min = MIN(min, VecGet(that, i));
    // Return the result
    return min;
}

// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMaxValAbs(const VecShort* const that) {
#if BUILDMODE == 0
    if (that == NULL) {

```

```

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    short max = abs(VecGet(that, 0));
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        max = (abs(max) > abs(VecGet(that, i)) ? max : VecGet(that, i));
    // Return the result
    return max;
}

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
short _VecShortGetMinValAbs(const VecShort* const that) {
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
}
#endif
    // Declare a variable to memorize the result
    short min = abs(VecGet(that, 0));
    // Search for the minimum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        min = (abs(min) < abs(VecGet(that, i)) ? min : VecGet(that, i));
    // Return the result
    return min;
}

// ----- VecLong

// Static constructors for VecLong
#if BUILDMODE != 0
static inline
#endif
VecLong2D VecLongCreateStatic2D() {
    VecLong2D v = {._val = {0, 0}, ._dim = 2};
    return v;
}
#if BUILDMODE != 0
static inline
#endif
VecLong3D VecLongCreateStatic3D() {
    VecLong3D v = {._val = {0, 0, 0}, ._dim = 3};
    return v;
}
#if BUILDMODE != 0
static inline
#endif
VecLong4D VecLongCreateStatic4D() {
    VecLong4D v = {._val = {0, 0, 0, 0}, ._dim = 4};
    return v;
}

// Return the i-th value of the VecLong

```

```

#if BUILDMODE != 0
static inline
#endif
long _VecLongGet(const VecLong* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
            that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    return ((long*)((void*)that) + sizeof(long))[i];
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongGet2D(const VecLong2D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_val[i];
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongGet3D(const VecLong3D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_val[i];
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongGet4D(const VecLong4D* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;

```

```

        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErCatch(PBMathErr);
    }
#endif
    return that->_val[i];
}

// Set the i-th value of the VecLong to v
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet(VecLong* const that, const long i, const long v) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (i < 0 || i >= that->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
                that->_dim);
            PBErCatch(PBMathErr);
        }
    #endif
    ((long*)((void*)that) + sizeof(long))[i] = v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecLongSet2D(VecLong2D* const that, const long i, const long v) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (i < 0 || i >= 2) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
            PBErCatch(PBMathErr);
        }
    #endif
    that->_val[i] = v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecLongSet3D(VecLong3D* const that, const long i, const long v) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (i < 0 || i >= 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
        }
    #endif
}

```

```

        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErCatch(PBMathErr);
    }
#endif
    that->_val[i] = v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongSet4D(VecLong4D* const that, const long i, const long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErCatch(PBMathErr);
    }
#endif
    that->_val[i] = v;
}

// Set the i-th value of the VecLong to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd(VecLong* const that, const long i, const long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<%ld)", i,
            that->_dim);
        PBErCatch(PBMathErr);
    }
#endif
    ((long*)((void*)that) + sizeof(long))[i] += v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd2D(VecLong2D* const that, const long i, const long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
}

```



```

}
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd3D(VecLong3D* const that, const long i, const long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAdd4D(VecLong4D* const that, const long i, const long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 4) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<4)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_val[i] += v;
}

// Set all values of the vector 'that' to 0
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetNull(VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Set values
    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = 0;
}

// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecLongSetAll(VecLong* const that, long v) {
#if BUILDMODE == 0
    if (that == NULL) {

```

```

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Set values
    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = v;
}

// Return the dimension of the VecLong
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetDim(const VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_dim;
}

// Return the Hamiltonian distance between the VecLong 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist(const VecLong* const that, const VecLong* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to calculate the distance
    long ret = 0;
    for (long iDim = VecGetDim(that); iDim--;)
        ret += labs(VecGet(that, iDim) - VecGet(tho, iDim));
    // Return the distance
    return ret;
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist2D(const VecLong2D* const that, const VecLong2D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
    }

```

```

        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    // Return the distance
    return labs(VecGet(that, 0) - VecGet(tho, 0)) +
        labs(VecGet(that, 1) - VecGet(tho, 1));
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist3D(const VecLong3D* const that, const VecLong3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Return the distance
    return labs(VecGet(that, 0) - VecGet(tho, 0)) +
        labs(VecGet(that, 1) - VecGet(tho, 1)) +
        labs(VecGet(that, 2) - VecGet(tho, 2));
}

#if BUILDMODE != 0
static inline
#endif
long _VecLongHamiltonDist4D(const VecLong4D* const that, const VecLong4D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Return the distance
    return labs(VecGet(that, 0) - VecGet(tho, 0)) +
        labs(VecGet(that, 1) - VecGet(tho, 1)) +
        labs(VecGet(that, 2) - VecGet(tho, 2)) +
        labs(VecGet(that, 3) - VecGet(tho, 3));
}

// Return true if the VecLong 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecLongIsEqual(const VecLong* const that,
    const VecLong* const tho) {

```

```

#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    return
        (memcmp(that->_val, tho->_val, sizeof(long) * that->_dim) == 0);
}

// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecLongCopy(VecLong* const that, const VecLong* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Copy the values
    memcpy(that->_val, tho->_val, sizeof(long) * that->_dim);
}

// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd(const VecLong* const that,
    const VecLong* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {

```

```

    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
}
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
        that->_dim, tho->_dim);
    PBErrCatch(PBMathErr);
}
#endif
// Declare a variable to memorise the result
long res = 0;
// For each component
for (long iDim = that->_dim; iDim--;)
    // Calculate the product
    res += VecGet(that, iDim) * VecGet(tho, iDim);
// Return the result
return res;
}
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd2D(const VecLong2D* const that,
    const VecLong2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1);
}
#if BUILDMODE != 0
static inline
#endif
long _VecLongDotProd3D(const VecLong3D* const that,
    const VecLong3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1) +
        VecGet(that, 2) * VecGet(tho, 2);
}
#endif
#if BUILDMODE != 0

```

```

static inline
#endif
long _VecLongDotProd4D(const VecLong4D* const that,
    const VecLong4D* const tho) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return VecGet(that, 0) * VecGet(tho, 0) +
        VecGet(that, 1) * VecGet(tho, 1) +
        VecGet(that, 2) * VecGet(tho, 2) +
        VecGet(that, 3) * VecGet(tho, 3);
}

// Calculate (that * a + tho * b) and store the result in 'that'
#ifdef BUILDMODE != 0
static inline
#endif
void _VecLongOp(VecLong* const that, const long a,
    const VecLong* const tho, const long b) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim,
            a * VecGet(that, iDim) + b * VecGet(tho, iDim));
}
#ifdef BUILDMODE != 0
static inline
#endif
void _VecLongOp2D(VecLong2D* const that, const long a,
    const VecLong2D* const tho, const long b) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {

```

```

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp3D(VecLong3D* const that, const long a,
    const VecLong3D* const tho, const long b) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongOp4D(VecLong4D* const that, const long a,
    const VecLong4D* const tho, const long b) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    VecSet(that, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
}

// Return a VecLong equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetOp(const VecLong* const that, const long a,
    const VecLong* const tho, const long b) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");

```

```

    PBErCatch(PBMathErr);
}
if (tho == NULL) {
    PBMathErr->_type = PBErTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErCatch(PBMathErr);
}
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
        that->_dim, tho->_dim);
    PBErCatch(PBMathErr);
}
#endif
VecLong* res = VecLongCreate(that->_dim);
for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
        a * VecGet(that, iDim) + b * VecGet(tho, iDim));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetOp2D(const VecLong2D* const that, const long a,
    const VecLong2D* const tho, const long b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecLong2D res = VecLongCreateStatic2D();
    VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    return res;
}
#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetOp3D(const VecLong3D* const that, const long a,
    const VecLong3D* const tho, const long b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecLong3D res = VecLongCreateStatic3D();
    VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));

```



```

    VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    return res;
}
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetOp4D(const VecLong4D* const that, const long a,
    const VecLong4D* const tho, const long b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'that' is null");
        PBErrCatch(PBMATHERR);
    }
    if (tho == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'tho' is null");
        PBErrCatch(PBMATHERR);
    }
#endif
    VecLong4D res = VecLongCreateStatic4D();
    VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    VecSet(&res, 3, a * VecGet(that, 3) + b * VecGet(tho, 3));
    return res;
}

// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd(VecLong* const that,
    const VecLong* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'that' is null");
        PBErrCatch(PBMATHERR);
    }
    if (tho == NULL) {
        PBMATHERR->_type = PBErrTypeNullPointer;
        sprintf(PBMATHERR->_msg, "'tho' is null");
        PBErrCatch(PBMATHERR);
    }
    if (that->_dim != tho->_dim) {
        PBMATHERR->_type = PBErrTypeInvalidArg;
        sprintf(PBMATHERR->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMATHERR);
    }
#endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd2D(VecLong2D* const that,
    const VecLong2D* const tho) {

```

```

#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd3D(VecLong3D* const that,
    const VecLong3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
}
#if BUILDMODE != 0
static inline
#endif
void _VecLongHadamardProd4D(VecLong4D* const that,
    const VecLong4D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
    VecSet(that, 3, VecGet(that, 3) * VecGet(tho, 3));
}

// Return a VecLong equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension

```

```

#if BUILDMODE != 0
static inline
#endif
VecLong* _VecLongGetHadamardProd(const VecLong* const that,
    const VecLong* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    VecLong* res = VecLongCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecLong2D _VecLongGetHadamardProd2D(const VecLong2D* const that,
    const VecLong2D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecLong2D res = VecLongCreateStatic2D();
    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecLong3D _VecLongGetHadamardProd3D(const VecLong3D* const that,
    const VecLong3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {

```

```

    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErrCatch(PBMathErr);
}
#endif
VecLong3D res = VecLongCreateStatic3D();
VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecLong4D _VecLongGetHadamardProd4D(const VecLong4D* const that,
    const VecLong4D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    VecLong4D res = VecLongCreateStatic4D();
    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
    VecSet(&res, 3, VecGet(that, 3) * VecGet(tho, 3));
    return res;
}

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxVal(const VecLong* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to memorize the result
    long max = VecGet(that, 0);
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        max = MAX(max, VecGet(that, i));
    // Return the result
    return max;
}

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetIMaxVal(const VecLong* const that) {

```

```

#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
// Declare a variable to memorize the result
long iMax = 0;
// Declare a variable to memorize the max value
long max = VecGet(that, iMax);
// Search for the maximum value
for (long i = VecGetDim(that); i-- && i != 0;) {
    if (max < VecGet(that, i)) {
        max = VecGet(that, i);
        iMax = i;
    }
}
// Return the result
return iMax;
}

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinVal(const VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
// Declare a variable to memorize the result
long min = VecGet(that, 0);
// Search for the minimum value
for (long i = VecGetDim(that); i-- && i != 0;)
    min = MIN(min, VecGet(that, i));
// Return the result
return min;
}

// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMaxValAbs(const VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
// Declare a variable to memorize the result
long max = labs(VecGet(that, 0));
// Search for the maximum value
for (long i = VecGetDim(that); i-- && i != 0;)
    max = (labs(max) > labs(VecGet(that, i))) ? max : VecGet(that, i);
// Return the result

```

```

    return max;
}

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecLongGetMinValAbs(const VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    long min = labs(VecGet(that, 0));
    // Search for the minimum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        min = (labs(min) < labs(VecGet(that, i))) ? min : VecGet(that, i);
    // Return the result
    return min;
}

// ----- VecFloat

// Static constructors for VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecFloatCreateStatic2D() {
    VecFloat2D v = {._val = {0.0, 0.0}, ._dim = 2};
    return v;
}
#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecFloatCreateStatic3D() {
    VecFloat3D v = {._val = {0.0, 0.0, 0.0}, ._dim = 3};
    return v;
}

// Return the i-th value of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGet(const VecFloat* const that, const long i) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the value

```

```

    return that->_val[i];
}
#endif BUILDMODE != 0
static inline
#endif
float _VecFloatGet2D(const VecFloat2D* const that, const long i) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the value
    return that->_val[i];
}
#endif BUILDMODE != 0
static inline
#endif
float _VecFloatGet3D(const VecFloat3D* const that, const long i) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the value
    return that->_val[i];
}

// Set the i-th value of the VecFloat to v
#ifdef BUILDMODE != 0
static inline
#endif
void _VecFloatSet(VecFloat* const that, const long i, const float v) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Set the value
    that->_val[i] = v;
}

```

```

#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet2D(VecFloat2D* const that, const long i, const float v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    // Set the value
    that->_val[i] = v;
}

#if BUILDMODE != 0
static inline
#endif
void _VecFloatSet3D(VecFloat3D* const that, const long i, const float v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
        PBErrCatch(PBMathErr);
    }
#endif
    // Set the value
    that->_val[i] = v;
}

// Set the i-th value of the VecFloat to v plus its current value
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd(VecFloat* const that, const long i, const float v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (i < 0 || i >= that->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'i' is invalid (0<=%ld<%ld)", i, that->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Set the value
    that->_val[i] += v;
}

#if BUILDMODE != 0
static inline

```



```

#endif
void _VecFloatSetAdd2D(VecFloat2D* const that, const long i,
    const float v) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (i < 0 || i >= 2) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<2)", i);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Set the value
    that->_val[i] += v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAdd3D(VecFloat3D* const that, const long i,
    const float v) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (i < 0 || i >= 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "'i' is invalid (0<=%ld<3)", i);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Set the value
    that->_val[i] += v;
}

// Set all values of the vector 'that' to 0.0
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull(VecFloat* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Set values
    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = 0.0;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull2D(VecFloat2D* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;

```

```

        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
#endif
    // Set values
    that->_val[0] = 0.0;
    that->_val[1] = 0.0;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetNull3D(VecFloat3D* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Set values
    that->_val[0] = 0.0;
    that->_val[1] = 0.0;
    that->_val[2] = 0.0;
}

// Set all values of the vector 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll(VecFloat* const that, float v) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Set values
    for (long iDim = that->_dim; iDim--;)
        that->_val[iDim] = v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll2D(VecFloat2D* const that, float v) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    // Set values
    that->_val[0] = v;
    that->_val[1] = v;
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatSetAll3D(VecFloat3D* const that, float v) {
    if BUILDMODE == 0
        if (that == NULL) {

```

```

        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Set values
    that->_val[0] = v;
    that->_val[1] = v;
    that->_val[2] = v;
}

// Return the dimension of the VecFloat
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetDim(const VecFloat* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    return that->_dim;
}

// Copy the values of 'tho' in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatCopy(VecFloat* const that, const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Copy the values
    memcpy(that->_val, tho->_val, sizeof(float) * that->_dim);
}

// Return the norm of the VecFloat
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm(const VecFloat* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
        }
    #endif
}

```

```

        PBErrCatch(PBMathErr);
    }
#endif
// Declare a variable to calculate the norm
float ret = 0.0;
// Calculate the norm
for (long iDim = that->_dim; iDim--;)
    ret += fsquare(VecGet(that, iDim));
ret = sqrt(ret);
// Return the result
return ret;
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm2D(const VecFloat2D* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Return the result
    return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)));
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatNorm3D(const VecFloat3D* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Return the result
    return sqrt(fsquare(VecGet(that, 0)) + fsquare(VecGet(that, 1)) +
        fsquare(VecGet(that, 2)));
}

// Normalise the VecFloat
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise(VecFloat* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Normalise
    float norm = VecNorm(that);
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim, VecGet(that, iDim) / norm);
}

#if BUILDMODE != 0
static inline

```

```

#endif
void _VecFloatNormalise2D(VecFloat2D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Normalise
    float norm = _VecFloatNorm2D(that);
    VecSet(that, 0, VecGet(that, 0) / norm);
    VecSet(that, 1, VecGet(that, 1) / norm);
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatNormalise3D(VecFloat3D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Normalise
    float norm = _VecFloatNorm3D(that);
    VecSet(that, 0, VecGet(that, 0) / norm);
    VecSet(that, 1, VecGet(that, 1) / norm);
    VecSet(that, 2, VecGet(that, 2) / norm);
}

// Return the distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist(const VecFloat* const that,
    const VecFloat* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to calculate the distance
    float ret = 0.0;
    for (long iDim = that->_dim; iDim--;)
        ret += fsquare(VecGet(that, iDim) - VecGet(tho, iDim));
    ret = sqrt(ret);
    // Return the distance

```

```

    return ret;
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the distance
    return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
        fsquare(VecGet(that, 1) - VecGet(tho, 1)));
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the distance
    return sqrt(fsquare(VecGet(that, 0) - VecGet(tho, 0)) +
        fsquare(VecGet(that, 1) - VecGet(tho, 1)) +
        fsquare(VecGet(that, 2) - VecGet(tho, 2)));
}

// Return the Hamiltonian distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist(const VecFloat* const that,
    const VecFloat* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
}

```

```

    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to calculate the distance
    float ret = 0.0;
    for (long iDim = that->_dim; iDim--;)
        ret += fabs(VecGet(that, iDim) - VecGet(tho, iDim));
    // Return the distance
    return ret;
}

#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Return the distance
    return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
        fabs(VecGet(that, 1) - VecGet(tho, 1));
}

#if BUILDMODE != 0
static inline
#endif
float _VecFloatHamiltonDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Return the distance
    return fabs(VecGet(that, 0) - VecGet(tho, 0)) +
        fabs(VecGet(that, 1) - VecGet(tho, 1)) +
        fabs(VecGet(that, 2) - VecGet(tho, 2));
}

// Return the Pixel distance between the VecFloat 'that' and 'tho'
#if BUILDMODE != 0
static inline

```

```

#endif
float _VecFloatPixelDist(const VecFloat* const that,
    const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to calculate the distance
    float ret = 0.0;
    for (long iDim = that->_dim; iDim--;)
        ret += fabs(floor(VecGet(that, iDim)) - floor(VecGet(tho, iDim)));
    // Return the distance
    return ret;
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Return the distance
    return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) +
        fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1)));
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatPixelDist3D(const VecFloat3D* const that,
    const VecFloat3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
        }
    #endif

```



```

        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the distance
    return fabs(floor(VecGet(that, 0)) - floor(VecGet(tho, 0))) +
        fabs(floor(VecGet(that, 1)) - floor(VecGet(tho, 1))) +
        fabs(floor(VecGet(that, 2)) - floor(VecGet(tho, 2)));
}

// Return true if the VecFloat 'that' is equal to 'tho', else false
#if BUILDMODE != 0
static inline
#endif
bool _VecFloatIsEqual(const VecFloat* const that,
    const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // For each component
    for (long iDim = that->_dim; iDim--;)
        // If the values of this components are different
        if (!ISEQUALF(VecGet(that, iDim), VecGet(tho, iDim)))
            // Return false
            return false;
    // Return true
    return true;
}

// Calculate (that * a + tho * b) and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp(VecFloat* const that, const float a,
    const VecFloat* const tho, const float b) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {

```

```

        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
#endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim,
            a * VecGet(that, iDim) + b * VecGet(tho, iDim));
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp2D(VecFloat2D* const that, const float a,
    const VecFloat2D* const tho, const float b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatOp3D(VecFloat3D* const that, const float a,
    const VecFloat3D* const tho, const float b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
    VecSet(that, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
    VecSet(that, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
}

// Return a VecFloat equal to (that * a + tho * b)
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetOp(const VecFloat* const that, const float a,
    const VecFloat* const tho, const float b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
    }

```

```

    PBErCatch(PBMathErr);
}
if (tho == NULL) {
    PBMathErr->_type = PBErTypeNullPointer;
    sprintf(PBMathErr->_msg, "'tho' is null");
    PBErCatch(PBMathErr);
}
if (that->_dim != tho->_dim) {
    PBMathErr->_type = PBErTypeInvalidArg;
    sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
        that->_dim, tho->_dim);
    PBErCatch(PBMathErr);
}
}
#endif
VecFloat* res = VecFloatCreate(that->_dim);
for (long iDim = that->_dim; iDim--;)
    VecSet(res, iDim,
        a * VecGet(that, iDim) + b * VecGet(tho, iDim));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetOp2D(const VecFloat2D* const that, const float a,
    const VecFloat2D* const tho, const float b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
}
#endif
VecFloat2D res = VecFloatCreateStatic2D();
VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));
return res;
}
#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetOp3D(const VecFloat3D* const that, const float a,
    const VecFloat3D* const tho, const float b) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
}
#endif
VecFloat3D res = VecFloatCreateStatic3D();
VecSet(&res, 0, a * VecGet(that, 0) + b * VecGet(tho, 0));
VecSet(&res, 1, a * VecGet(that, 1) + b * VecGet(tho, 1));

```

```

    VecSet(&res, 2, a * VecGet(that, 2) + b * VecGet(tho, 2));
    return res;
}

// Calculate the Hadamard product of that by tho and store the
// result in 'that'
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd(VecFloat* const that,
    const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd2D(VecFloat2D* const that,
    const VecFloat2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
}
#if BUILDMODE != 0
static inline
#endif
void _VecFloatHadamardProd3D(VecFloat3D* const that,
    const VecFloat3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");

```

```

        PBErCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(that, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(that, 2, VecGet(that, 2) * VecGet(tho, 2));
}

// Return a VecFloat equal to the hadamard product of 'that' and 'tho'
// Return NULL if arguments are invalid
// 'tho' and 'that' must be of same dimension
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetHadamardProd(const VecFloat* const that,
    const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim) {
            PBMathErr->_type = PBErTypeInvalidArg;
            sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
                that->_dim, tho->_dim);
            PBErCatch(PBMathErr);
        }
    #endif
    VecFloat* res = VecFloatCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, VecGet(that, iDim) * VecGet(tho, iDim));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetHadamardProd2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErCatch(PBMathErr);
        }
    #endif
    VecFloat2D res = VecFloatCreateStatic2D();

```

```

    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    return res;
}
#endif
static inline
#endif
VecFloat3D _VecFloatGetHadamardProd3D(const VecFloat3D* const that,
const VecFloat3D* const tho) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat3D res = VecFloatCreateStatic3D();
    VecSet(&res, 0, VecGet(that, 0) * VecGet(tho, 0));
    VecSet(&res, 1, VecGet(that, 1) * VecGet(tho, 1));
    VecSet(&res, 2, VecGet(that, 2) * VecGet(tho, 2));
    return res;
}

// Calculate (that * a) and store the result in 'that'
#ifdef BUILDMODE != 0
static inline
#endif
void _VecFloatScale(VecFloat* const that, const float a) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    for (long iDim = that->_dim; iDim--;)
        VecSet(that, iDim, a * VecGet(that, iDim));
}
#ifdef BUILDMODE != 0
static inline
#endif
void _VecFloatScale2D(VecFloat2D* const that, const float a) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0));
    VecSet(that, 1, a * VecGet(that, 1));
}
#ifdef BUILDMODE != 0
static inline
#endif
void _VecFloatScale3D(VecFloat3D* const that, const float a) {
#ifdef BUILDMODE == 0

```

```

    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecSet(that, 0, a * VecGet(that, 0));
    VecSet(that, 1, a * VecGet(that, 1));
    VecSet(that, 2, a * VecGet(that, 2));
}

// Return a VecFloat equal to (that * a)
#if BUILDMODE != 0
static inline
#endif
VecFloat* _VecFloatGetScale(const VecFloat* const that, const float a) {
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat* res = VecFloatCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, a * VecGet(that, iDim));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetScale2D(const VecFloat2D* const that,
    const float a) {
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat2D res = VecFloatCreateStatic2D();
    VecSet(&res, 0, a * VecGet(that, 0));
    VecSet(&res, 1, a * VecGet(that, 1));
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat3D _VecFloatGetScale3D(const VecFloat3D* const that,
    const float a) {
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat3D res = VecFloatCreateStatic3D();
    VecSet(&res, 0, a * VecGet(that, 0));
    VecSet(&res, 1, a * VecGet(that, 1));
    VecSet(&res, 2, a * VecGet(that, 2));
    return res;
}

```

```

}

// Rotate CCW 'that' by 'theta' radians and store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRot2D(VecFloat2D* const that, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==2)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
#endif
    *that = _VecFloatGetRot2D(that, theta);
}

// Return a VecFloat2D equal to 'that' rotated CCW by 'theta' radians
#if BUILDMODE != 0
static inline
#endif
VecFloat2D _VecFloatGetRot2D(const VecFloat2D* const that, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 2) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==2)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    VecFloat2D res = VecFloatCreateStatic2D();
    // Declare variable for optimization
    float cosTheta = cos(theta);
    float sinTheta = sin(theta);
    // Calculate the rotation
    VecSet(&res, 0,
        cosTheta * VecGet(that, 0) - sinTheta * VecGet(that, 1));
    VecSet(&res, 1,
        sinTheta * VecGet(that, 0) + cosTheta * VecGet(that, 1));
    // Return the result
    return res;
}

// Return the dot product of 'that' and 'tho'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd(const VecFloat* const that,
    const VecFloat* const tho) {
#if BUILDMODE == 0

```



```

    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (that->_dim != tho->_dim) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "dimensions don't match (%ld==%ld)",
            that->_dim, tho->_dim);
        PBErrCatch(PBMathErr);
    }
}
#endif
// Declare a variable to memorize the result
float res = 0.0;
// Calculate
for (long iDim = that->_dim; iDim--;)
    res += that->_val[iDim] * tho->_val[iDim];
// Return the result
return res;
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd2D(const VecFloat2D* const that,
    const VecFloat2D* const tho) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1];
}
#if BUILDMODE != 0
static inline
#endif
float _VecFloatDotProd3D(const VecFloat3D* const that,
    const VecFloat3D* const tho) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    return that->_val[0] * tho->_val[0] + that->_val[1] * tho->_val[1] +

```

```

        that->_val[2] * tho->_val[2];
    }

    // Return the cross product of 'that' and 'tho'
    #if BUILDMODE != 0
    static inline
    #endif
    VecFloat* _VecFloatGetCrossProd(const VecFloat* const that,
        const VecFloat* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
        if (that->_dim != tho->_dim || tho->_dim != 3) {
            PBMathErr->_type = PBErrTypeInvalidArg;
            sprintf(PBMathErr->_msg, "invalid dimensions (%ld==%ld==3)",
                that->_dim, tho->_dim);
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to memorize the result
    VecFloat* res = VecFloatCreate(3);
    // Calculate
    VecSet(res, 0,
        VecGet(that, 1) * VecGet(tho, 2) -
        VecGet(that, 2) * VecGet(tho, 1));
    VecSet(res, 1, -1.0 *
        (VecGet(that, 0) * VecGet(tho, 2) -
        VecGet(that, 2) * VecGet(tho, 0)));
    VecSet(res, 2,
        VecGet(that, 0) * VecGet(tho, 1) -
        VecGet(that, 1) * VecGet(tho, 0));
    // Return the result
    return res;
}
#endif
static inline
#endif
VecFloat3D _VecFloatGetCrossProd3D(const VecFloat3D* const that,
    const VecFloat3D* const tho) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
        if (tho == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'tho' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to memorize the result
    VecFloat3D res = VecFloatCreateStatic3D();
    // Calculate

```

```

    VecSet(&res, 0,
        VecGet(that, 1) * VecGet(tho, 2) -
        VecGet(that, 2) * VecGet(tho, 1));
    VecSet(&res, 1, -1.0 *
        (VecGet(that, 0) * VecGet(tho, 2) -
        VecGet(that, 2) * VecGet(tho, 0)));
    VecSet(&res, 2,
        VecGet(that, 0) * VecGet(tho, 1) -
        VecGet(that, 1) * VecGet(tho, 0));
    // Return the result
    return res;
}

// Return the conversion of VecFloat 'that' to a VecShort using round()
#if BUILDMODE != 0
static inline
#endif
VecShort* VecFloatToShort(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PMathErr->_type = PErrTypeNullPointer;
        sprintf(PMathErr->_msg, "'that' is null");
        PErrCatch(PMathErr);
    }
#endif
    // Create the result
    VecShort* res = VecShortCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, SHORT(VecGet(that, iDim)));
    // Return the result
    return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort2D VecFloatToShort2D(const VecFloat2D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PMathErr->_type = PErrTypeNullPointer;
        sprintf(PMathErr->_msg, "'that' is null");
        PErrCatch(PMathErr);
    }
#endif
    // Create the result
    VecShort2D res = VecShortCreateStatic2D();
    VecSet(&res, 0, SHORT(VecGet(that, 0)));
    VecSet(&res, 1, SHORT(VecGet(that, 1)));
    // Return the result
    return res;
}
#if BUILDMODE != 0
static inline
#endif
VecShort3D VecFloatToShort3D(const VecFloat3D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PMathErr->_type = PErrTypeNullPointer;
        sprintf(PMathErr->_msg, "'that' is null");
        PErrCatch(PMathErr);
    }
#endif
    // Create the result

```

```

    VecShort3D res = VecShortCreateStatic3D();
    VecSet(&res, 0, SHORT(VecGet(that, 0)));
    VecSet(&res, 1, SHORT(VecGet(that, 1)));
    VecSet(&res, 2, SHORT(VecGet(that, 2)));
    // Return the result
    return res;
}

// Return the conversion of VecShort 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecShortToFloat(const VecShort* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Create the result
    VecFloat* res = VecFloatCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, (float)VecGet(that, iDim));
    // Return the result
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecShortToFloat2D(const VecShort2D* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Create the result
    VecFloat2D res = VecFloatCreateStatic2D();
    VecSet(&res, 0, (float)VecGet(that, 0));
    VecSet(&res, 1, (float)VecGet(that, 1));
    // Return the result
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecShortToFloat3D(const VecShort3D* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Create the result
    VecFloat3D res = VecFloatCreateStatic3D();
    VecSet(&res, 0, (float)VecGet(that, 0));
    VecSet(&res, 1, (float)VecGet(that, 1));
    VecSet(&res, 2, (float)VecGet(that, 2));
    // Return the result

```

```

    return res;
}

// Return the conversion of VecLong 'that' to a VecFloat
#if BUILDMODE != 0
static inline
#endif
VecFloat* VecLongToFloat(const VecLong* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the result
    VecFloat* res = VecFloatCreate(that->_dim);
    for (long iDim = that->_dim; iDim--;)
        VecSet(res, iDim, (float)VecGet(that, iDim));
    // Return the result
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat2D VecLongToFloat2D(const VecLong2D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the result
    VecFloat2D res = VecFloatCreateStatic2D();
    VecSet(&res, 0, (float)VecGet(that, 0));
    VecSet(&res, 1, (float)VecGet(that, 1));
    // Return the result
    return res;
}

#if BUILDMODE != 0
static inline
#endif
VecFloat3D VecLongToFloat3D(const VecLong3D* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Create the result
    VecFloat3D res = VecFloatCreateStatic3D();
    VecSet(&res, 0, (float)VecGet(that, 0));
    VecSet(&res, 1, (float)VecGet(that, 1));
    VecSet(&res, 2, (float)VecGet(that, 2));
    // Return the result
    return res;
}

// Get the max value in components of the vector 'that'
#if BUILDMODE != 0

```

```

static inline
#endif
float _VecFloatGetMaxVal(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    float max = VecGet(that, 0);
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        max = MAX(max, VecGet(that, i));
    // Return the result
    return max;
}

// Get the index of the max value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
long _VecFloatGetIMaxVal(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    long iMax = 0;
    // Declare a variable to memorize the max value
    float max = VecGet(that, iMax);
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;) {
        if (max < VecGet(that, i)) {
            max = VecGet(that, i);
            iMax = i;
        }
    }
    // Return the result
    return iMax;
}

// Get the min value in components of the vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinVal(const VecFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable to memorize the result
    float min = VecGet(that, 0);
    // Search for the minimum value
    for (long i = VecGetDim(that); i-- && i != 0;)

```

```

        min = MIN(min, VecGet(that, i));
    // Return the result
    return min;
}

// Get the max value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMaxValAbs(const VecFloat* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to memorize the result
    float max = fabs(VecGet(that, 0));
    // Search for the maximum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        max = (fabs(max) > fabs(VecGet(that, i)) ? max : VecGet(that, i));
    // Return the result
    return max;
}

// Get the min value (in absolute value) in components of the
// vector 'that'
#if BUILDMODE != 0
static inline
#endif
float _VecFloatGetMinValAbs(const VecFloat* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
    // Declare a variable to memorize the result
    float min = fabs(VecGet(that, 0));
    // Search for the minimum value
    for (long i = VecGetDim(that); i-- && i != 0;)
        min = (fabs(min) < fabs(VecGet(that, i)) ? min : VecGet(that, i));
    // Return the result
    return min;
}

// Set the MatFloat to the identity matrix
// The matrix must be a square matrix
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSetIdentity(MatFloat* const that) {
    if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    if (VecGet(&(that->_dim), 0) != VecGet(&(that->_dim), 1)) {

```

```

        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "the matrix is not square (%dx%d)",
            VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
        PBErrCatch(PBMathErr);
    }
#endif
    // Set the values
    VecShort2D i = VecShortCreateStatic2D();
    do {
        if (VecGet(&i, 0) == VecGet(&i, 1))
            MatSet(that, &i, 1.0);
        else
            MatSet(that, &i, 0.0);
    } while (VecStep(&i, &(that->_dim)));
}

// Return the addition of matrix 'that' with matrix 'tho'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
MatFloat* _MatFloatGetAdd(MatFloat* const that, MatFloat* tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'that' and 'tho' have different dimensions");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare a variable for the result
    MatFloat* res = MatFloatCreate(MatDim(that));
    // Add each values
    VecShort2D i = VecShortCreateStatic2D();
    do {
        MatSet(res, &i, MatGet(that, &i) + MatGet(tho, &i));
    } while (VecStep(&i, MatDim(that)));
    // Return the result
    return res;
}

// Add matrix 'that' with matrix 'tho' and store the result in 'that'
// 'that' and 'tho' must have same dimensions
#if BUILDMODE != 0
static inline
#endif
void _MatFloatAdd(MatFloat* const that, MatFloat* tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }

```



```

    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(MatDim(that), MatDim(tho)) == false) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'that' and 'tho' have different dimensions");
        PBErrCatch(PBMathErr);
    }
}
#endif
// Add each values
VecShort2D i = VecShortCreateStatic2D();
do {
    MatSet(that, &i, MatGet(that, &i) + MatGet(tho, &i));
} while (VecStep(&i, MatDim(that)));
}

// Multiply the matrix 'that' by 'a'
#if BUILDMODE != 0
static inline
#endif
void _MatFloatScale(MatFloat* const that, const float a) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
// Multiply each values
VecShort2D i = VecShortCreateStatic2D();
do {
    MatSet(that, &i, MatGet(that, &i) * a);
} while (VecStep(&i, MatDim(that)));
}

// Copy the values of 'w' in 'that' (must have same dimensions)
#if BUILDMODE != 0
static inline
#endif
void _MatFloatCopy(MatFloat* const that, const MatFloat* const tho) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (tho == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'tho' is null");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&(that->_dim), &(tho->_dim))) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'that' and 'tho' have different dimensions (%dx%d==%dx%d)",
            VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1),
            VecGet(&(tho->_dim), 0), VecGet(&(tho->_dim), 1));
        PBErrCatch(PBMathErr);
    }
}

```

```

    }
#endif
    // Copy the matrix values
    int d = VecGet(&(that->_dim), 0) * VecGet(&(that->_dim), 1);
    memcpy(that->_val, tho->_val, d * sizeof(float));
}

// Return the value at index 'i' (col, line) of the MatFloat
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
float _MatFloatGet(const MatFloat* const that,
    VecShort2D* index) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (index == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'index' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGet(index, 0) < 0 ||
        VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
        VecGet(index, 1) < 0 ||
        VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg,
            "'index' is invalid (0,0 <= %d,%d < %d,%d)",
            VecGet(index, 0), VecGet(index, 1),
            VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the value
    return that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
        VecGet(index, 0)];
}

// Set the value at index 'i' (col, line) of the MatFloat to 'v'
// Index starts at 0, index in matrix = line * nbCol + col
#if BUILDMODE != 0
static inline
#endif
void _MatFloatSet(MatFloat* const that, VecShort2D* index, float v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (index == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'index' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGet(index, 0) < 0 ||
        VecGet(index, 0) >= VecGet(&(that->_dim), 0) ||
        VecGet(index, 1) < 0 ||

```

```

    VecGet(index, 1) >= VecGet(&(that->_dim), 1)) {
    PBMathErr->_type = PBErrTypeInvalidArg;
    sprintf(PBMathErr->_msg,
        "'index' is invalid (0,0 <= %d,%d < %d,%d)",
        VecGet(index, 0), VecGet(index, 1),
        VecGet(&(that->_dim), 0), VecGet(&(that->_dim), 1));
    PBErrCatch(PBMathErr);
    }
#endif
    // Set the value
    that->_val[VecGet(index, 1) * VecGet(&(that->_dim), 0) +
        VecGet(index, 0)] = v;
}

// Return the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
const VecShort2D* _MatFloatDim(const MatFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the dimension
    return &(that->_dim);
}

// Return a VecShort2D containing the dimension of the MatFloat
#if BUILDMODE != 0
static inline
#endif
VecShort2D _MatFloatGetDim(const MatFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the dimension
    return that->_dim;
}

// Return the number of rows of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbRow(const MatFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the nb of rows
    return VecGet(&(that->_dim), 1);
}

```

```

// Return the number of columns of the MatFloat 'that'
#if BUILDMODE != 0
static inline
#endif
short _MatFloatGetNbCol(const MatFloat* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Return the nb of cols
    return VecGet(&(that->_dim), 0);
}

// Return the value of the Gauss 'that' at 'x'
#if BUILDMODE != 0
static inline
#endif
float GaussGet(const Gauss* const that, const float x) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Calculate the value
    float a = 1.0 / (that->_sigma * sqrt(2.0 * PBMath_PI));
    float ret = a * exp(-1.0 * fsquare(x - that->_mean) /
        (2.0 * fsquare(that->_sigma)));
    // Return the value
    return ret;
}

// Return a random value (in ]0.0, 1.0[) according to the
// Gauss distribution 'that'
// random() must have been called before calling this function
#if BUILDMODE != 0
static inline
#endif
float GaussRnd(Gauss* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    // Declare variable for calcul
    float v1, v2, s;
    // Calculate the value
    do {
        v1 = (rnd() - 0.5) * 2.0;
        v2 = (rnd() - 0.5) * 2.0;
        s = v1 * v1 + v2 * v2;
    } while (s >= 1.0);
    // Return the value
    float ret = 0.0;
    if (s > PBMath_EPSILON)

```

```

        ret = v1 * sqrt(-2.0 * log(s) / s);
        return ret * that->_sigma + that->_mean;
    }

    // Return the order 1 smooth value of 'x'
    // if x < 0.0 return 0.0
    // if x > 1.0 return 1.0
    #if BUILDMODE != 0
    static inline
    #endif
    float SmoothStep(const float x) {
        if (x > 0.0)
            if (x < 1.0)
                return x * x * (3.0 - 2.0 * x);
            else
                return 1.0;
        else
            return 0.0;
    }

    // Return the order 2 smooth value of 'x'
    // if x < 0.0 return 0.0
    // if x > 1.0 return 1.0
    #if BUILDMODE != 0
    static inline
    #endif
    float SmootherStep(const float x) {
        if (x > 0.0)
            if (x < 1.0)
                return x * x * x * (x * (x * 6.0 - 15.0) + 10.0);
            else
                return 1.0;
        else
            return 0.0;
    }

    // Solve the SysLinEq _M.x = _V
    // Return the solution vector, or null if there is no solution or the
    // arguments are invalid
    #if BUILDMODE != 0
    static inline
    #endif
    VecFloat* SysLinEqSolve(const SysLinEq* const that) {
    #if BUILDMODE == 0
        if (that == NULL) {
            PBMathErr->_type = PBErrTypeNullPointer;
            sprintf(PBMathErr->_msg, "'that' is null");
            PBErrCatch(PBMathErr);
        }
    #endif
        // Declare a variable to memorize the solution
        VecFloat* ret = NULL;
        // Calculate the solution
        ret = MatGetProdVec(that->_Minv, that->_V);
        // Return the solution vector
        return ret;
    }

    // Set the matrix of the SysLinEq to a copy of 'm'
    // 'm' must have same dimensions has the current matrix
    // Do nothing if arguments are invalid
    #if BUILDMODE != 0

```

```

static inline
#endif
void SysLinEqSetM(SysLinEq* const that, const MatFloat* const m) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (m == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'m' is null");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&(m->_dim), &(that->_M->_dim))) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'m' has invalid dimension (%dx%d==%dx%d)",
            VecGet(&(m->_dim), 0), VecGet(&(m->_dim), 1),
            VecGet(&(that->_M->_dim), 0), VecGet(&(that->_M->_dim), 1));
        PBErrCatch(PBMathErr);
    }
#endif
    // Update the matrix values
    MatCopy(that->_M, m);
    // Update the inverse matrix
    MatFree(&(that->_Minv));
    that->_Minv = MatGetInv(that->_M);
#ifdef BUILDMODE == 0
    if (that->_Minv == NULL) {
        PBMathErr->_type = PBErrTypeOther;
        sprintf(PBMathErr->_msg, "couldn't inverse the matrix");
        PBErrCatch(PBMathErr);
    }
#endif
}

// Set the vector of the SysLinEq to a copy of 'v'
// 'v' must have same dimensions has the current vector
// Do nothing if arguments are invalid
#ifdef BUILDMODE != 0
static inline
#endif
void _SLESetV(SysLinEq* const that, const VecFloat* const v) {
#ifdef BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (v == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'v' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(v) != VecGetDim(that->_V)) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'v' has invalid dimension (%ld==%ld)",
            VecGetDim(v), VecGetDim(that->_V));
        PBErrCatch(PBMathErr);
    }
#endif
    // Update the vector values

```

```

    VecCopy(that->_V, v);
}

// Return x^y when x and y are int
// to avoid numerical imprecision from (pow(double,double)
// From https://stackoverflow.com/questions/29787310/
// does-pow-work-for-int-data-type-in-c
#if BUILDMODE != 0
static inline
#endif
int powi(const int base, const int exp) {
    // Declare a variable to memorize the result and init to 1
    int res = 1;
    // Loop on exponent
    int e = exp;
    int b = base;
    while (e) {
        // Do some magic trick
        if (e & 1)
            res *= b;
        e /= 2;
        b *= b;
    }
    // Return the result
    return res;
}

// Rotate right-hand 'that' by 'theta' radians around 'axis' and
// store the result in 'that'
// 'axis' must be normalized
// https://en.wikipedia.org/wiki/Rotation_matrix
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotAxis(VecFloat3D* const that,
    const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (axis == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'axis' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(axis) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'axis' 's dimension is invalid (%ld==3)",
            VecGetDim(axis));
        PBErrCatch(PBMathErr);
    }
    if (ISEQUALF(VecNorm(axis), 1.0) == false) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'axis' is not normalized");
    }
#endif
}

```

```

        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat3D v = _VecFloatGetRotAxis(that, axis, theta);
    VecCopy(that, &v);
}

// Rotate right-hand 'that' by 'theta' radians around X and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotX(VecFloat3D* const that, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat3D v = _VecFloatGetRotX(that, theta);
    VecCopy(that, &v);
}

// Rotate right-hand 'that' by 'theta' radians around Y and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotY(VecFloat3D* const that, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (VecGetDim(that) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
            VecGetDim(that));
        PBErrCatch(PBMathErr);
    }
#endif
    VecFloat3D v = _VecFloatGetRotY(that, theta);
    VecCopy(that, &v);
}

// Rotate right-hand 'that' by 'theta' radians around Z and
// store the result in 'that'
#if BUILDMODE != 0
static inline
#endif
void _VecFloatRotZ(VecFloat3D* const that, const float theta) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;

```



```

        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
    if (VecGetDim(that) != 3) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'that' 's dimension is invalid (%ld==3)",
            VecGetDim(that));
        PBErCatch(PBMathErr);
    }
#endif
    VecFloat3D v = _VecFloatGetRotZ(that, theta);
    VecCopy(that, &v);
}

// Free memory used by the QRDecomp 'that'
#if BUILDMODE != 0
static inline
#endif
void QRDecompFreeStatic(QRDecomp* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
#endif
    MatFree(&(that->_Q));
    MatFree(&(that->_R));
}

// Get the base of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
long RatioGetBase(const Ratio* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
#endif
    return that->_base;
}

// Get the numerator of the Ratio 'that'
#if BUILDMODE != 0
static inline
#endif
unsigned int RatioGetNumerator(const Ratio* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErCatch(PBMathErr);
    }
#endif
    return that->_numerator;
}

// Get the denominator of the Ratio 'that'
#if BUILDMODE != 0

```

```

static inline
#endif
unsigned int RatioGetDenominator(const Ratio* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return that->_denominator;
}

// Set the base of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetBase(Ratio* that, long v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    that->_base = v;
}

// Set the numerator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetNumerator(Ratio* that, unsigned int v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    that->_numerator = v;
}

// Set the denominator of the Ratio 'that' to 'v'
#if BUILDMODE != 0
static inline
#endif
void RatioSetDenominator(Ratio* that, unsigned int v) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (v == 0) {
        PBMathErr->_type = PBErrTypeInvalidArg;
        sprintf(PBMathErr->_msg, "'v' is invalid (%u > 0)", v);
        PBErrCatch(PBMathErr);
    }
#endif
    that->_denominator = v;
}

```

```

// ----- LeastSquareLinReg

// Set the component of the LeastSquareLinReg 'that' to 'X'
#if BUILDMODE != 0
static inline
#endif
void LSLRSetComp(LeastSquareLinReg* that, const MatFloat* X) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
    if (X == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'X' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    that->X = X;
    if (that->Xp != NULL) {
        MatFree(&(that->Xp));
    }
    MatFloat* transp = MatGetTranspose(that->X);
    MatFloat* A = MatGetProdMat(transp, that->X);
    MatFloat* inv = MatGetInv(A);
    if (inv != NULL) {
        that->Xp = MatGetProdMat(inv, transp);
    }
    MatFree(&transp);
    MatFree(&A);
    MatFree(&inv);
}

// Get the bias of the last computed solution of the LeastSquareLinReg 'that'
#if BUILDMODE != 0
static inline
#endif
float LSLRGetBias(const LeastSquareLinReg* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
    return that->bias;
}

// Return true if the LeastSquareLinReg 'that' is solvable
#if BUILDMODE != 0
static inline
#endif
bool LSLRIsSolvable(const LeastSquareLinReg* that) {
#if BUILDMODE == 0
    if (that == NULL) {
        PBMathErr->_type = PBErrTypeNullPointer;
        sprintf(PBMathErr->_msg, "'that' is null");
        PBErrCatch(PBMathErr);
    }
#endif
}

```

```

    return (that->Xp != NULL);
}

```

## 4 Makefile

```

# Build mode
# 0: development (max safety, no optimisation)
# 1: release (min safety, optimisation)
# 2: fast and furious (no safety, optimisation)
BUILD_MODE?=1

all: pbmake_wget main

# Automatic installation of the repository PBMake in the parent folder
pbmake_wget:
if [ ! -d ../PBMake ]; then wget https://github.com/BayashiPascal/PBMake/archive/master.zip; unzip master.zip; rm -f

# Makefile definitions
MAKEFILE_INC=../PBMake/Makefile.inc
include $(MAKEFILE_INC)

# Rules to make the executable
repo=pbmath
$($(repo)_EXENAME): \
$($(repo)_EXENAME).o \
$($(repo)_EXE_DEP) \
$($(repo)_DEP)
$(COMPILER) 'echo "$($(repo)_EXE_DEP) $($(repo)_EXENAME).o" | tr ' ' '\n' | sort -u' $(LINK_ARG) $($(repo)_LINK_ARG)

$($(repo)_EXENAME).o: \
$($(repo)_DIR)/$($(repo)_EXENAME).c \
$($(repo)_INC_H_EXE) \
$($(repo)_EXE_DEP)
$(COMPILER) $(BUILD_ARG) $($(repo)_BUILD_ARG) 'echo "$($(repo)_INC_DIR)" | tr ' ' '\n' | sort -u' -c $($(repo)_DIR)/

```

## 5 Unit tests

```

#include <stdlib.h>
#include <stdio.h>
#include <time.h>
#include <string.h>
#include <time.h>
#include <unistd.h>
#include <sys/time.h>
#include "pberr.h"
#include "pbmath.h"

#define RANDOMSEED 0

void UnitTestPowi() {
    int a;
    int n;
    for (n = 1; n <= 5; ++n) {
        for (a = 0; a <= 10; ++a) {
            int b = powi(a, n);

```

```

        int c = 1;
        int m = n;
        for (; m--;) c *= a;
        if (b != c) {
            PBMathErr->_type = PErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg,
                "powi(%d, %d) = %d , %d^%d = %d",
                a, n, b, a, n, c);
            PErrCatch(PBMathErr);
        }
    }
}
printf("powi OK\n");
}

void UnitTestFastPow() {
    srandom(RANDOMSEED);
    int nbTest = 1000;
    float sumErr = 0.0;
    float maxErr = 0.0;
    int i = nbTest;
    for (; i--;) {
        float a = (rnd() - 0.5) * 1000.0;
        int n = INT(rnd() * 5.0);
        float b = fastpow(a, n);
        float c = pow(a, n);
        float err = fabs(b - c);
        sumErr += err;
        if (maxErr < err)
            maxErr = err;
    }
    float avgErr = sumErr / (float)nbTest;
    printf("average error: %f < %f, max error: %f < %f\n",
        avgErr, PBMath_EPSILON, maxErr, PBMath_EPSILON * 10.0);
    if (avgErr >= PBMath_EPSILON ||
        maxErr >= PBMath_EPSILON * 10.0) {
        PBMathErr->_type = PErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "fastpow NOK");
        PErrCatch(PBMathErr);
    }
    printf("fastpow OK\n");
}

void UnitTestSpeedFastPow() {
    srandom(RANDOMSEED);
    int nbTest = 1000;
    int i = nbTest;
    clock_t clockBefore = clock();
    for (; i--;) {
        float a = (rnd() - 0.5) * 1000.0;
        int n = INT(rnd() * 5.0);
        float b = fastpow(a, n);
        b = b;
    }
    clock_t clockAfter = clock();
    double timeFastpow = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srandom(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();
    for (; i--;) {
        float a = (rnd() - 0.5) * 1000.0;

```

```

        int n = INT(rnd() * 5.0);
        float c = pow(a, n);
        c = c;
    }
    clockAfter = clock();
    double timePow = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    printf("fastpow: %fms, pow: %fms\n",
        timeFastpow / (float)nbTest, timePow / (float)nbTest);
    if (timeFastpow >= timePow) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        PBMathErr->_fatal = false;
        sprintf(PBMathErr->_msg, "speed fastpow NOK");
        PBErrCatch(PBMathErr);
    }
    printf("speed fastpow OK\n");
}

void UnitTestFSquare() {
    srandom(RANDOMSEED);
    int nbTest = 1000;
    for (; nbTest--;) {
        float a = (rnd() - 0.5) * 2000.0;
        float b = fsquare(a);
        float c = a * a;
        if (!ISEQUALF(b, c)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            PBMathErr->_fatal = false;
            sprintf(PBMathErr->_msg,
                "fsquare(%f) = %f , %f*%f = %f",
                a, b, a, a, c);
            PBErrCatch(PBMathErr);
        }
    }
    printf("fsquare OK\n");
}

void UnitTestVecShortCreateFree() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    VecPrintln(v, stdout);
    VecPrintln(&v2, stdout);
    VecPrintln(&v3, stdout);
    VecPrintln(&v4, stdout);
    VecFree(&v);
    if (v != NULL) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecShort is not null after VecFree");
        PBErrCatch(PBMathErr);
    }
    printf("VecShortCreateFree OK\n");
}

void UnitTestVecShortClone() {
    VecShort* v = VecShortCreate(5);
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    VecShort* w = VecClone(v);
    if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortClone NOK");
    }
}

```

```

        PBErCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("_VecShortClone OK\n");
}

void UnitTestVecShortLoadSave() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    for (long i = 5; i--;) VecSet(v, i, i + 1);
    for (long i = 2; i--;) VecSet(&v2, i, i + 1);
    for (long i = 3; i--;) VecSet(&v3, i, i + 1);
    for (long i = 4; i--;) VecSet(&v4, i, i + 1);
    FILE* f = fopen("./UnitTestVecShortLoadSave.txt", "w");
    if (f == NULL) {
        PBMathErr->_type = PBErTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestVecShortLoadSave.txt for writing");
        PBErCatch(PBMathErr);
    }
    bool compact = false;
    if (!VecSave(v, f, compact)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortSave NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecSave(&v2, f, compact)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortSave NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecSave(&v3, f, compact)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortSave NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecSave(&v4, f, compact)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortSave NOK");
        PBErCatch(PBMathErr);
    }
    fclose(f);
    VecShort* w = VecShortCreate(2);
    f = fopen("./UnitTestVecShortLoadSave.txt", "r");
    if (f == NULL) {
        PBMathErr->_type = PBErTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestVecShortLoadSave.txt for reading");
        PBErCatch(PBMathErr);
    }
    if (!VecLoad(&w, f)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
        PBErCatch(PBMathErr);
    }
    if (memcmp(v, w, sizeof(VecShort) + sizeof(short) * 5) != 0) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
        PBErCatch(PBMathErr);
    }
}

```

```

}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v2, w, sizeof(VecShort) + sizeof(short) * 2) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v3, w, sizeof(VecShort) + sizeof(short) * 3) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v4, w, sizeof(VecShort) + sizeof(short) * 4) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortLoadSave NOK");
    PBErrCatch(PBMathErr);
}
fclose(f);
VecFree(&v);
VecFree(&w);
int ret = system("cat ./UnitTestVecShortLoadSave.txt");
printf("_VecShortLoadSave OK\n");
ret = ret;
}

void UnitTestVecShortGetSetDim() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    if (VecGetDim(v) != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortGetDim NOK");
        PBErrCatch(PBMathErr);
    }
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    for (int i = 5; i--;)
        if (v->_val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (v2._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;

```



```

        sprintf(PBMathErr->_msg, "_VecShortSet NOK");
        PBErCatch(PBMathErr);
    }
    for (int i = 3; i--;)
        if (v3._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (v4._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 5; i--;)
        if (VecGet(v, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortGet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortGet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortGet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortGet NOK");
            PBErCatch(PBMathErr);
        }
    for (int i = 5; i--;) VecSetAdd(v, i, i + 1);
    for (int i = 2; i--;) VecSetAdd(&v2, i, i + 1);
    for (int i = 3; i--;) VecSetAdd(&v3, i, i + 1);
    for (int i = 4; i--;) VecSetAdd(&v4, i, i + 1);
    for (int i = 5; i--;)
        if (VecGet(v, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK1");
            PBErCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK2");
            PBErCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK3");
            PBErCatch(PBMathErr);
        }
    for (int i = 4; i--;)

```

```

        if (VecGet(&v4, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortSetAdd NOK4");
            PBErrCatch(PBMathErr);
        }
    }
    VecSetNull(v);
    VecSetNull(&v2);
    VecSetNull(&v3);
    VecSetNull(&v4);
    for (int i = 5; i--;)
        if (VecGet(v, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortNull NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortNull NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortNull NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortNull NOK");
            PBErrCatch(PBMathErr);
        }
    }
    VecSetAll(v, 1);
    VecSetAll(&v2, 1);
    VecSetAll(&v3, 1);
    VecSetAll(&v4, 1);
    for (int i = 5; i--;)
        if (VecGet(v, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    VecFree(&v);

```

```

    printf("_VecShortGetSetDim OK\n");
}

void UnitTestVecShortStep() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    VecShort* bv = VecShortCreate(5);
    VecShort2D bv2 = VecShortCreateStatic2D();
    VecShort3D bv3 = VecShortCreateStatic3D();
    VecShort4D bv4 = VecShortCreateStatic4D();
    short b[5] = {2, 3, 4, 5, 6};
    for (int i = 5; i--;) VecSet(bv, i, b[i]);
    for (int i = 2; i--;) VecSet(&bv2, i, b[i]);
    for (int i = 3; i--;) VecSet(&bv3, i, b[i]);
    for (int i = 4; i--;) VecSet(&bv4, i, b[i]);
    int acheck[2 * 3 * 4 * 5 * 6];
    for (int i = 0; i < 2 * 3 * 4 * 5 * 6; ++i)
        acheck[i] = i;
    int iCheck = 0;
    do {
        int a = VecGet(v, 0);
        for (int i = 1; i < VecGetDim(v); ++i)
            a = a * b[i] + VecGet(v, i);
        if (a != acheck[iCheck]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortStep NOK");
            PBErrCatch(PBMathErr);
        }
        ++iCheck;
    } while (VecStep(v, bv));
    iCheck = 0;
    do {
        int a = VecGet(&v2, 0);
        for (int i = 1; i < 2; ++i)
            a = a * b[i] + VecGet(&v2, i);
        if (a != acheck[iCheck]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortStep NOK");
            PBErrCatch(PBMathErr);
        }
        ++iCheck;
    } while (VecStep(&v2, &bv2));
    iCheck = 0;
    do {
        int a = VecGet(&v3, 0);
        for (int i = 1; i < 3; ++i)
            a = a * b[i] + VecGet(&v3, i);
        if (a != acheck[iCheck]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecShortStep NOK");
            PBErrCatch(PBMathErr);
        }
        ++iCheck;
    } while (VecStep(&v3, &bv3));
    iCheck = 0;
    do {
        int a = VecGet(&v4, 0);
        for (int i = 1; i < 4; ++i)
            a = a * b[i] + VecGet(&v4, i);
        if (a != acheck[iCheck]) {

```

```

        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStep(&v4, &bv4));
iCheck = 0;
do {
    int a = VecGet(v, VecGetDim(v) - 1);
    for (int i = VecGetDim(v) - 2; i >= 0; --i)
        a = a * b[i] + VecGet(v, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(v, bv));
iCheck = 0;
do {
    int a = VecGet(&v2, 1);
    a = a * b[0] + VecGet(&v2, 0);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(&v2, &bv2));
iCheck = 0;
do {
    int a = VecGet(&v3, 2);
    for (int i = 1; i >= 0; --i)
        a = a * b[i] + VecGet(&v3, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(&v3, &bv3));
iCheck = 0;
do {
    int a = VecGet(&v4, 3);
    for (int i = 2; i >= 0; --i)
        a = a * b[i] + VecGet(&v4, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(&v4, &bv4));
VecFree(&v);
VecFree(&bv);
VecShort2D w = VecShortCreateStatic2D();
VecShort2D wDelta = VecShortCreateStatic2D();
VecShort2D wBound = VecShortCreateStatic2D();
VecSet(&wDelta, 0, 2);
VecSet(&wDelta, 1, 3);
VecSet(&wBound, 0, 4);
VecSet(&wBound, 1, 6);

```

```

int checkDelta[8] = {0, 0, 0, 3, 2, 0, 2, 3};
iCheck = 0;
do {
    if (VecGet(&w, 0) != checkDelta[iCheck * 2] ||
        VecGet(&w, 1) != checkDelta[iCheck * 2 + 1]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortStepDelta NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStepDelta(&w, &wBound, &wDelta));
int checkDeltaB[8] = {0, 0, 2, 0, 0, 3, 2, 3};
VecSetNull(&w);
iCheck = 0;
do {
    if (VecGet(&w, 0) != checkDeltaB[iCheck * 2] ||
        VecGet(&w, 1) != checkDeltaB[iCheck * 2 + 1]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortStepDelta NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStepDelta(&w, &wBound, &wDelta));

printf("UnitTestVecShortStep OK\n");
}

void UnitTestVecShortHamiltonDist() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    VecShort* w = VecShortCreate(5);
    VecShort2D w2 = VecShortCreateStatic2D();
    VecShort3D w3 = VecShortCreateStatic3D();
    VecShort4D w4 = VecShortCreateStatic4D();
    short b[5] = {-2, -1, 0, 1, 2};
    for (int i = 5; i--;) VecSet(v, i, b[i]);
    for (int i = 2; i--;) VecSet(&v2, i, b[i]);
    for (int i = 3; i--;) VecSet(&v3, i, b[i]);
    for (int i = 4; i--;) VecSet(&v4, i, b[i]);
    for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
    for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
    for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
    for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
    short dist = VecHamiltonDist(v, w);
    if (dist != 13) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
        PBErrCatch(PBMathErr);
    }
    dist = VecHamiltonDist(&v2, &w2);
    if (dist != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
        PBErrCatch(PBMathErr);
    }
    dist = VecHamiltonDist(&v3, &w3);
    if (dist != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
        PBErrCatch(PBMathErr);
    }
}

```

```

    }
    dist = VecHamiltonDist(&v4, &w4);
    if (dist != 8) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortHamiltonDist NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecShortHamiltonDist OK\n");
}

void UnitTestVecShortIsEqual() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecShort* w = VecShortCreate(5);
    VecShort2D w2 = VecShortCreateStatic2D();
    VecShort3D w3 = VecShortCreateStatic3D();
    VecShort4D w4 = VecShortCreateStatic4D();
    if (VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v4, &w4)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    for (int i = 5; i--;) VecSet(w, i, i + 1);
    for (int i = 2; i--;) VecSet(&w2, i, i + 1);
    for (int i = 3; i--;) VecSet(&w3, i, i + 1);
    for (int i = 4; i--;) VecSet(&w4, i, i + 1);
    if (!VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
    }
}

```

```

    PBErCatch(PBMathErr);
}
if (!VecIsEqual(&v4, &w4)) {
    PBMathErr->_type = PBErTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortIsEqual NOK");
    PBErCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecShortIsEqual OK\n");
}

void UnitTestVecShortCopy() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecShort* w = VecShortCreate(5);
    VecShort2D w2 = VecShortCreateStatic2D();
    VecShort3D w3 = VecShortCreateStatic3D();
    VecShort4D w4 = VecShortCreateStatic4D();
    VecCopy(w, v);
    VecCopy(&w2, &v2);
    VecCopy(&w3, &v3);
    VecCopy(&w4, &v4);
    if (!VecIsEqual(v, w)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecIsEqual(&v4, &w4)) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortCopy NOK");
        PBErCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecShortCopy OK\n");
}

void UnitTestVecShortDotProd() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    VecShort* w = VecShortCreate(5);
    VecShort2D w2 = VecShortCreateStatic2D();
    VecShort3D w3 = VecShortCreateStatic3D();

```

```

VecShort4D w4 = VecShortCreateStatic4D();
short b[5] = {-2, -1, 0, 1, 2};
for (int i = 5; i--;) VecSet(v, i, b[i]);
for (int i = 2; i--;) VecSet(&v2, i, b[i]);
for (int i = 3; i--;) VecSet(&v3, i, b[i]);
for (int i = 4; i--;) VecSet(&v4, i, b[i]);
for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
short prod = VecDotProd(v, w);
if (prod != -10) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
    PBErrCatch(PBMathErr);
}
prod = VecDotProd(&v2, &w2);
if (prod != 1) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
    PBErrCatch(PBMathErr);
}
prod = VecDotProd(&v3, &w3);
if (prod != -2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
    PBErrCatch(PBMathErr);
}
prod = VecDotProd(&v4, &w4);
if (prod != -6) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortDotProd NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecShortDotProd OK\n");
}

void UnitTestSpeedVecShort() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    int nbTest = 100000;

    srandom(RANDOMSEED);
    int i = nbTest;
    clock_t clockBefore = clock();
    for (; i--;) {
        int j = INT(rnd()) * ((float)(VecGetDim(v) - 1) - PBMathEpsilon);
        short val = 1;
        VecSet(v, j, val);
        short valb = VecGet(v, j);
        valb = valb;
    }
    clock_t clockAfter = clock();
    double timeV = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srandom(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();

```



```

short* array = malloc(sizeof(short) * 5);
for (; i--;) {
    int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMath_EPSILON));
    short val = 1;
    array[j] = val;
    short valb = array[j];
    valb = valb;
}
clockAfter = clock();
double timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecShort: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 5.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
    PErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (1.0 - PBMath_EPSILON));
    short val = 1;
    VecSet(&v2, j, val);
    short valb = VecGet(&v2, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
short array2[2];
for (; i--;) {
    int j = INT(rnd() * (1.0 - PBMath_EPSILON));
    short val = 1;
    array2[j] = val;
    short valb = array2[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecShort2D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
    PErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;

```

```

clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    short val = 1;
    VecSet(&v3, j, val);
    short valb = VecGet(&v3, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
short array3[3];
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    short val = 1;
    array3[j] = val;
    short valb = array3[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecShort3D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
    PErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMath_EPSILON));
    short val = 1;
    VecSet(&v4, j, val);
    short valb = VecGet(&v4, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
short array4[4];
for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMath_EPSILON));
    short val = 1;
    array4[j] = val;
    short valb = array4[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /

```

```

        CLOCKS_PER_SEC * 1000.0;
        printf("VecShort4D: %fms, array: %fms\n",
            timeV / (float)nbTest, timeRef / (float)nbTest);
        if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
            PBMathErr->_fatal = false;
#endif
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestSpeedVecShort NOK");
            PBErrCatch(PBMathErr);
        }

        VecFree(&v);
        free(array);
        printf("UnitTestSpeedVecShort OK\n");
    }

void UnitTestVecShortToFloat() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecFloat* w = VecShortToFloat(v);
    VecFloat2D w2 = VecShortToFloat2D(&v2);
    VecFloat3D w3 = VecShortToFloat3D(&v3);
    VecPrintln(w, stdout);
    VecPrintln(&w2, stdout);
    VecPrintln(&w3, stdout);
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecShortToFloat OK\n");
}

void UnitTestVecLongToFloat() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecFloat* w = VecLongToFloat(v);
    VecFloat2D w2 = VecLongToFloat2D(&v2);
    VecFloat3D w3 = VecLongToFloat3D(&v3);
    VecPrintln(w, stdout);
    VecPrintln(&w2, stdout);
    VecPrintln(&w3, stdout);
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecLongToFloat OK\n");
}

void UnitTestVecShortOp() {
    VecShort* v = VecShortCreate(5);
    VecShort2D v2 = VecShortCreateStatic2D();
    VecShort3D v3 = VecShortCreateStatic3D();
    VecShort4D v4 = VecShortCreateStatic4D();

```

```

VecShort* w = VecShortCreate(5);
VecShort2D w2 = VecShortCreateStatic2D();
VecShort3D w3 = VecShortCreateStatic3D();
VecShort4D w4 = VecShortCreateStatic4D();
for (int i = 5; i--;) VecSet(v, i, i + 1);
for (int i = 2; i--;) VecSet(&v2, i, i + 1);
for (int i = 3; i--;) VecSet(&v3, i, i + 1);
short a[2] = {-1, 2};
short b[5] = {-2, -1, 0, 1, 2};
for (int i = 5; i--;) VecSet(v, i, b[i]);
for (int i = 2; i--;) VecSet(&v2, i, b[i]);
for (int i = 3; i--;) VecSet(&v3, i, b[i]);
for (int i = 4; i--;) VecSet(&v4, i, b[i]);
for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
VecShort* u = VecGetOp(v, a[0], w, a[1]);
VecShort2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
VecShort3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
VecShort4D u4 = VecGetOp(&v4, a[0], &w4, a[1]);
short checku[5] = {8,5,2,-1,-4};
short checku2[2] = {2,-1};
short checku3[3] = {4,1,-2};
short checku4[4] = {6,3,0,-3};
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(u, i), checku[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 4; i--;)
    if (!ISEQUALF(VecGet(&u4, i), checku4[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortGetOp NOK");
        PBErrCatch(PBMathErr);
    }
VecOp(v, a[0], w, a[1]);
VecOp(&v2, a[0], &w2, a[1]);
VecOp(&v3, a[0], &w3, a[1]);
VecOp(&v4, a[0], &w4, a[1]);
if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v2, &u2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecShortOp NOK");
    PBErrCatch(PBMathErr);
}

```

```

    }
    if (!VecIsEqual(&v3, &u3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortOp NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v4, &u4)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecShortOp NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    VecFree(&u);
    printf("UnitTestVecShortOp OK\n");
}

void UnitTestVecShortShiftStep() {
    VecShort3D v = VecShortCreateStatic3D();
    VecShort3D from = VecShortCreateStatic3D();
    VecShort3D to = VecShortCreateStatic3D();
    VecSet(&from, 0, 0);
    VecSet(&from, 1, 1);
    VecSet(&from, 2, 2);
    VecSet(&to, 0, 3);
    VecSet(&to, 1, 4);
    VecSet(&to, 2, 5);
    VecCopy(&v, &from);
    short check[81] = {
        0, 1, 2, 0, 1, 3, 0, 1, 4,
        0, 2, 2, 0, 2, 3, 0, 2, 4,
        0, 3, 2, 0, 3, 3, 0, 3, 4,
        1, 1, 2, 1, 1, 3, 1, 1, 4,
        1, 2, 2, 1, 2, 3, 1, 2, 4,
        1, 3, 2, 1, 3, 3, 1, 3, 4,
        2, 1, 2, 2, 1, 3, 2, 1, 4,
        2, 2, 2, 2, 2, 3, 2, 2, 4,
        2, 3, 2, 2, 3, 3, 2, 3, 4
    };
    int iCheck = 0;
    do {
        for (int i = 0; i < 3; ++i) {
            if (ISEQUALF(check[iCheck], VecGet(&v, i)) == false) {
                PBMathErr->_type = PBErrTypeUnitTestFailed;
                sprintf(PBMathErr->_msg, "VecShiftStep NOK");
                PBErrCatch(PBMathErr);
            }
            ++iCheck;
        }
    } while(VecShiftStep(&v, &from, &to));
    printf("UnitTestVecShortShiftStep OK\n");
}

void UnitTestVecShortGetMinMax() {
    VecShort3D v = VecShortCreateStatic3D();
    VecSet(&v, 0, 2); VecSet(&v, 1, 4); VecSet(&v, 2, 3);
    short val = VecGetMaxVal(&v);
    if (val != 4) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
        PBErrCatch(PBMathErr);
    }
}

```

```

    if (VecGetIMaxVal(&v) != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetIMaxVal NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
    val = VecGetMinVal(&v);
    if (val != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 2); VecSet(&v, 1, -4); VecSet(&v, 2, 3);
    val = VecGetMaxValAbs(&v);
    if (val != -4) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, -2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
    val = VecGetMinValAbs(&v);
    if (val != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
        PBErrCatch(PBMathErr);
    }
    printf("UnitTestVecShortGetMinMax OK\n");
}

void UnitTestVecShortHadamardProd() {
    VecShort* u = VecShortCreate(3);
    for (int i = 3; i--;)
        VecSet(u, i, i + 2);
    VecShort* uprod = VecGetHadamardProd(u, u);
    VecHadamardProd(u, u);
    short checku[3] = {4, 9, 16};
    for (int i = 3; i--;)
        if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(uprod, u) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&uprod);
    VecFree(&u);
    VecShort2D v = VecShortCreateStatic2D();
    for (int i = 2; i--;)
        VecSet(&v, i, i + 2);
    VecShort2D vprod = VecGetHadamardProd(&v, &v);
    VecHadamardProd(&v, &v);
    short checkv[2] = {4, 9};
    for (int i = 2; i--;)
        if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(&vprod, &v) == false) {

```

```

    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
    PBErrCatch(PBMathErr);
}
VecShort3D w = VecShortCreateStatic3D();
for (int i = 3; i--;)
    VecSet(&w, i, i + 2);
VecShort3D wprod = VecGetHadamardProd(&w, &w);
VecHadamardProd(&w, &w);
short checkw[3] = {4, 9, 16};
for (int i = 3; i--;)
    if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
if (VecIsEqual(&wprod, &w) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
    PBErrCatch(PBMathErr);
}
VecShort4D x = VecShortCreateStatic4D();
for (int i = 4; i--;)
    VecSet(&x, i, i + 2);
VecShort4D xprod = VecGetHadamardProd(&x, &x);
VecHadamardProd(&x, &x);
short checkx[4] = {4, 9, 16, 25};
for (int i = 4; i--;)
    if (ISEQUALF(VecGet(&xprod, i), checkx[i]) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
if (VecIsEqual(&xprod, &x) == false) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
    PBErrCatch(PBMathErr);
}
printf("UnitTestVecShortHadamardProd OK\n");
}

void UnitTestVecShort() {
    UnitTestVecShortCreateFree();
    UnitTestVecShortClone();
    UnitTestVecShortLoadSave();
    UnitTestVecShortGetSetDim();
    UnitTestVecShortStep();
    UnitTestVecShortHamiltonDist();
    UnitTestVecShortIsEqual();
    UnitTestVecShortDotProd();
    UnitTestVecShortCopy();
    UnitTestSpeedVecShort();
    UnitTestVecShortToFloat();
    UnitTestVecLongToFloat();
    UnitTestVecShortOp();
    UnitTestVecShortShiftStep();
    UnitTestVecShortGetMinMax();
    UnitTestVecShortHadamardProd();
    printf("UnitTestVecShort OK\n");
}

void UnitTestVecLongCreateFree() {

```

```

VecLong* v = VecLongCreate(5);
VecLong2D v2 = VecLongCreateStatic2D();
VecLong3D v3 = VecLongCreateStatic3D();
VecLong4D v4 = VecLongCreateStatic4D();
VecPrintln(v, stdout);
VecPrintln(&v2, stdout);
VecPrintln(&v3, stdout);
VecPrintln(&v4, stdout);
VecFree(&v);
if (v != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "VecLong is not null after VecFree");
    PBErrCatch(PBMathErr);
}
printf("VecLongCreateFree OK\n");
}

void UnitTestVecLongClone() {
    VecLong* v = VecLongCreate(5);
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    VecLong* w = VecClone(v);
    if (memcmp(v, w, sizeof(VecLong) + sizeof(long) * 5) != 0) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongClone NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("_VecLongClone OK\n");
}

void UnitTestVecLongLoadSave() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    FILE* f = fopen("./UnitTestVecLongLoadSave.txt", "w");
    if (f == NULL) {
        PBMathErr->_type = PBErrTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestVecLongLoadSave.txt for writing");
        PBErrCatch(PBMathErr);
    }
    bool compact = false;
    if (!VecSave(v, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongSave NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecSave(&v2, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongSave NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecSave(&v3, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongSave NOK");
        PBErrCatch(PBMathErr);
    }

```



```

}
if (!VecSave(&v4, f, compact)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongSave NOK");
    PBErrCatch(PBMathErr);
}
fclose(f);
VecLong* w = VecLongCreate(2);
f = fopen("./UnitTestVecLongLoadSave.txt", "r");
if (f == NULL) {
    PBMathErr->_type = PBErrTypeOther;
    sprintf(PBMathErr->_msg,
        "Can't open ./UnitTestVecLongLoadSave.txt for reading");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(v, w, sizeof(VecLong) + sizeof(long) * 5) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v2, w, sizeof(VecLong) + sizeof(long) * 2) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v3, w, sizeof(VecLong) + sizeof(long) * 3) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
    PBErrCatch(PBMathErr);
}
if (!VecLoad(&w, f)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoad NOK");
    PBErrCatch(PBMathErr);
}
if (memcmp(&v4, w, sizeof(VecLong) + sizeof(long) * 4) != 0) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongLoadSave NOK");
    PBErrCatch(PBMathErr);
}
fclose(f);
VecFree(&v);
VecFree(&w);
int ret = system("cat ./UnitTestVecLongLoadSave.txt");
printf("_VecLongLoadSave OK\n");
ret = ret;
}

```

```

void UnitTestVecLongGetSetDim() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    if (VecGetDim(v) != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongGetDim NOK");
        PBErrCatch(PBMathErr);
    }
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    for (int i = 5; i--;)
        if (v->_val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (v2._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (v3._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (v4._val[i] != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 5; i--;)
        if (VecGet(v, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != i + 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
}

```

```

    }
    for (int i = 5; i--;) VecSetAdd(v, i, i + 1);
    for (int i = 2; i--;) VecSetAdd(&v2, i, i + 1);
    for (int i = 3; i--;) VecSetAdd(&v3, i, i + 1);
    for (int i = 4; i--;) VecSetAdd(&v4, i, i + 1);
    for (int i = 5; i--;)
        if (VecGet(v, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != 2 * (i + 1)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongSetAdd NOK");
            PBErrCatch(PBMathErr);
        }
    VecSetNull(v);
    VecSetNull(&v2);
    VecSetNull(&v3);
    VecSetNull(&v4);
    for (int i = 5; i--;)
        if (VecGet(v, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != 0) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongGet NOK");
            PBErrCatch(PBMathErr);
        }
    VecSetAll(v, 1);
    VecSetAll(&v2, 1);
    VecSetAll(&v3, 1);
    VecSetAll(&v4, 1);
    for (int i = 5; i--;)

```

```

        if (VecGet(v, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 2; i--;)
        if (VecGet(&v2, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 3; i--;)
        if (VecGet(&v3, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    for (int i = 4; i--;)
        if (VecGet(&v4, i) != 1) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongAll NOK");
            PBErrCatch(PBMathErr);
        }
    }
    VecFree(&v);
    printf("_VecLongGetSetDim OK\n");
}

void UnitTestVecLongStep() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    VecLong* bv = VecLongCreate(5);
    VecLong2D bv2 = VecLongCreateStatic2D();
    VecLong3D bv3 = VecLongCreateStatic3D();
    VecLong4D bv4 = VecLongCreateStatic4D();
    long b[5] = {2, 3, 4, 5, 6};
    for (int i = 5; i--;) VecSet(bv, i, b[i]);
    for (int i = 2; i--;) VecSet(&bv2, i, b[i]);
    for (int i = 3; i--;) VecSet(&bv3, i, b[i]);
    for (int i = 4; i--;) VecSet(&bv4, i, b[i]);
    int acheck[2 * 3 * 4 * 5 * 6];
    for (int i = 0; i < 2 * 3 * 4 * 5 * 6; ++i)
        acheck[i] = i;
    int iCheck = 0;
    do {
        int a = VecGet(v, 0);
        for (int i = 1; i < VecGetDim(v); ++i)
            a = a * b[i] + VecGet(v, i);
        if (a != acheck[iCheck]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecLongStep NOK");
            PBErrCatch(PBMathErr);
        }
        ++iCheck;
    } while (VecStep(v, bv));
    iCheck = 0;
    do {
        int a = VecGet(&v2, 0);
        for (int i = 1; i < 2; ++i)
            a = a * b[i] + VecGet(&v2, i);
        if (a != acheck[iCheck]) {

```

```

        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStep(&v2, &bv2));
iCheck = 0;
do {
    int a = VecGet(&v3, 0);
    for (int i = 1; i < 3; ++i)
        a = a * b[i] + VecGet(&v3, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStep(&v3, &bv3));
iCheck = 0;
do {
    int a = VecGet(&v4, 0);
    for (int i = 1; i < 4; ++i)
        a = a * b[i] + VecGet(&v4, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStep(&v4, &bv4));
iCheck = 0;
do {
    int a = VecGet(v, VecGetDim(v) - 1);
    for (int i = VecGetDim(v) - 2; i >= 0; --i)
        a = a * b[i] + VecGet(v, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(v, bv));
iCheck = 0;
do {
    int a = VecGet(&v2, 1);
    a = a * b[0] + VecGet(&v2, 0);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
        PBErrCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(&v2, &bv2));
iCheck = 0;
do {
    int a = VecGet(&v3, 2);
    for (int i = 1; i >= 0; --i)
        a = a * b[i] + VecGet(&v3, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
        PBErrCatch(PBMathErr);
    }

```

```

    }
    ++iCheck;
} while (VecPStep(&v3, &bv3));
iCheck = 0;
do {
    int a = VecGet(&v4, 3);
    for (int i = 2; i >= 0; --i)
        a = a * b[i] + VecGet(&v4, i);
    if (a != acheck[iCheck]) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongPStep NOK");
        PBErCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStep(&v4, &bv4));
VecFree(&v);
VecFree(&bv);
VecLong2D w = VecLongCreateStatic2D();
VecLong2D wDelta = VecLongCreateStatic2D();
VecLong2D wBound = VecLongCreateStatic2D();
VecSet(&wDelta, 0, 2);
VecSet(&wDelta, 1, 3);
VecSet(&wBound, 0, 4);
VecSet(&wBound, 1, 6);
int checkDelta[8] = {0, 0, 0, 3, 2, 0, 2, 3};
iCheck = 0;
do {
    if (VecGet(&w, 0) != checkDelta[iCheck * 2] ||
        VecGet(&w, 1) != checkDelta[iCheck * 2 + 1]) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongStepDelta NOK");
        PBErCatch(PBMathErr);
    }
    ++iCheck;
} while (VecStepDelta(&w, &wBound, &wDelta));
int checkDeltaB[8] = {0, 0, 2, 0, 0, 3, 2, 3};
VecSetNull(&w);
iCheck = 0;
do {
    if (VecGet(&w, 0) != checkDeltaB[iCheck * 2] ||
        VecGet(&w, 1) != checkDeltaB[iCheck * 2 + 1]) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongStepDelta NOK");
        PBErCatch(PBMathErr);
    }
    ++iCheck;
} while (VecPStepDelta(&w, &wBound, &wDelta));

printf("UnitTestVecLongStep OK\n");
}

void UnitTestVecLongHamiltonDist() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    VecLong* w = VecLongCreate(5);
    VecLong2D w2 = VecLongCreateStatic2D();
    VecLong3D w3 = VecLongCreateStatic3D();
    VecLong4D w4 = VecLongCreateStatic4D();
    long b[5] = {-2, -1, 0, 1, 2};
    for (int i = 5; i--;) VecSet(v, i, b[i]);

```

```

for (int i = 2; i--;) VecSet(&v2, i, b[i]);
for (int i = 3; i--;) VecSet(&v3, i, b[i]);
for (int i = 4; i--;) VecSet(&v4, i, b[i]);
for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
long dist = VecHamiltonDist(v, w);
if (dist != 13) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
dist = VecHamiltonDist(&v2, &w2);
if (dist != 2) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
dist = VecHamiltonDist(&v3, &w3);
if (dist != 5) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
dist = VecHamiltonDist(&v4, &w4);
if (dist != 8) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecLongHamiltonDist OK\n");
}

void UnitTestVecLongIsEqual() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecLong* w = VecLongCreate(5);
    VecLong2D w2 = VecLongCreateStatic2D();
    VecLong3D w3 = VecLongCreateStatic3D();
    VecLong4D w4 = VecLongCreateStatic4D();
    if (VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    }
}

```

```

    PBErriCatch(PBMathErr);
}
if (VecIsEqual(&v4, &w4)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErriCatch(PBMathErr);
}
for (int i = 5; i--;) VecSet(w, i, i + 1);
for (int i = 2; i--;) VecSet(&w2, i, i + 1);
for (int i = 3; i--;) VecSet(&w3, i, i + 1);
for (int i = 4; i--;) VecSet(&w4, i, i + 1);
if (!VecIsEqual(v, w)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErriCatch(PBMathErr);
}
if (!VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErriCatch(PBMathErr);
}
if (!VecIsEqual(&v3, &w3)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErriCatch(PBMathErr);
}
if (!VecIsEqual(&v4, &w4)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongIsEqual NOK");
    PBErriCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecLongIsEqual OK\n");
}

void UnitTestVecLongCopy() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    for (int i = 4; i--;) VecSet(&v4, i, i + 1);
    VecLong* w = VecLongCreate(5);
    VecLong2D w2 = VecLongCreateStatic2D();
    VecLong3D w3 = VecLongCreateStatic3D();
    VecLong4D w4 = VecLongCreateStatic4D();
    VecCopy(w, v);
    VecCopy(&w2, &v2);
    VecCopy(&w3, &v3);
    VecCopy(&w4, &v4);
    if (!VecIsEqual(v, w)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
        PBErriCatch(PBMathErr);
    }
    if (!VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
        PBErriCatch(PBMathErr);
    }
}

```



```

    }
    if (!VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v4, &w4)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongCopy NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecLongCopy OK\n");
}

void UnitTestVecLongDotProd() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    VecLong* w = VecLongCreate(5);
    VecLong2D w2 = VecLongCreateStatic2D();
    VecLong3D w3 = VecLongCreateStatic3D();
    VecLong4D w4 = VecLongCreateStatic4D();
    long b[5] = {-2, -1, 0, 1, 2};
    for (int i = 5; i--;) VecSet(v, i, b[i]);
    for (int i = 2; i--;) VecSet(&v2, i, b[i]);
    for (int i = 3; i--;) VecSet(&v3, i, b[i]);
    for (int i = 4; i--;) VecSet(&v4, i, b[i]);
    for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
    for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
    for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
    for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
    long prod = VecDotProd(v, w);
    if (prod != -10) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
        PBErrCatch(PBMathErr);
    }
    prod = VecDotProd(&v2, &w2);
    if (prod != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
        PBErrCatch(PBMathErr);
    }
    prod = VecDotProd(&v3, &w3);
    if (prod != -2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
        PBErrCatch(PBMathErr);
    }
    prod = VecDotProd(&v4, &w4);
    if (prod != -6) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongDotProd NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecLongDotProd OK\n");
}

```

```

void UnitTestSpeedVecLong() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    int nbTest = 100000;

    srandom(RANDOMSEED);
    int i = nbTest;
    clock_t clockBefore = clock();
    for (; i--;) {
        int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
        long val = 1;
        VecSet(v, j, val);
        long valb = VecGet(v, j);
        valb = valb;
    }
    clock_t clockAfter = clock();
    double timeV = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srandom(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();
    long* array = malloc(sizeof(long) * 5);
    for (; i--;) {
        int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMATH_EPSILON));
        long val = 1;
        array[j] = val;
        long valb = array[j];
        valb = valb;
    }
    clockAfter = clock();
    double timeRef = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    printf("VecLong: %fms, array: %fms\n",
        timeV / (float)nbTest, timeRef / (float)nbTest);
    if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
        PBMathErr->_fatal = false;
#endif
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
        PBErrCatch(PBMathErr);
    }

    srandom(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();
    for (; i--;) {
        int j = INT(rnd() * (1.0 - PBMATH_EPSILON));
        long val = 1;
        VecSet(&v2, j, val);
        long valb = VecGet(&v2, j);
        valb = valb;
    }
    clockAfter = clock();
    timeV = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srandom(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();

```

```

long array2[2];
for (; i--;) {
    int j = INT(rnd() * (1.0 - PBMath_EPSILON));
    long val = 1;
    array2[j] = val;
    long valb = array2[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecLong2D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
    PBErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    long val = 1;
    VecSet(&v3, j, val);
    long valb = VecGet(&v3, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
long array3[3];
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    long val = 1;
    array3[j] = val;
    long valb = array3[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecLong3D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
    PBErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;

```

```

clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMath_EPSILON));
    long val = 1;
    VecSet(&v4, j, val);
    long valb = VecGet(&v4, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
long array4[4];
for (; i--;) {
    int j = INT(rnd() * (3.0 - PBMath_EPSILON));
    long val = 1;
    array4[j] = val;
    long valb = array4[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecLong4D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecLong NOK");
    PBErrCatch(PBMathErr);
}

VecFree(&v);
free(array);
printf("UnitTestSpeedVecLong OK\n");
}

void UnitTestVecLongOp() {
    VecLong* v = VecLongCreate(5);
    VecLong2D v2 = VecLongCreateStatic2D();
    VecLong3D v3 = VecLongCreateStatic3D();
    VecLong4D v4 = VecLongCreateStatic4D();
    VecLong* w = VecLongCreate(5);
    VecLong2D w2 = VecLongCreateStatic2D();
    VecLong3D w3 = VecLongCreateStatic3D();
    VecLong4D w4 = VecLongCreateStatic4D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    long a[2] = {-1, 2};
    long b[5] = {-2, -1, 0, 1, 2};
    for (int i = 5; i--;) VecSet(v, i, b[i]);
    for (int i = 2; i--;) VecSet(&v2, i, b[i]);
    for (int i = 3; i--;) VecSet(&v3, i, b[i]);
    for (int i = 4; i--;) VecSet(&v4, i, b[i]);
    for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1);
    for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1);
    for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1);
}

```

```

for (int i = 4; i--;) VecSet(&w4, i, b[3 - i] + 1);
VecLong* u = VecGetOp(v, a[0], w, a[1]);
VecLong2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
VecLong3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
VecLong4D u4 = VecGetOp(&v4, a[0], &w4, a[1]);
long checku[5] = {8,5,2,-1,-4};
long checku2[2] = {2,-1};
long checku3[3] = {4,1,-2};
long checku4[4] = {6,3,0,-3};
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(u, i), checku[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 4; i--;)
    if (!ISEQUALF(VecGet(&u4, i), checku4[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecLongGetOp NOK");
        PBErrCatch(PBMathErr);
    }
VecOp(v, a[0], w, a[1]);
VecOp(&v2, a[0], &w2, a[1]);
VecOp(&v3, a[0], &w3, a[1]);
VecOp(&v4, a[0], &w4, a[1]);
if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v2, &u2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v3, &u3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v4, &u4)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecLongOp NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
VecFree(&u);
printf("UnitTestVecLongOp OK\n");
}

```

```

void UnitTestVecLongShiftStep() {
    VecLong3D v = VecLongCreateStatic3D();
    VecLong3D from = VecLongCreateStatic3D();
    VecLong3D to = VecLongCreateStatic3D();
    VecSet(&from, 0, 0);
    VecSet(&from, 1, 1);
    VecSet(&from, 2, 2);
    VecSet(&to, 0, 3);
    VecSet(&to, 1, 4);
    VecSet(&to, 2, 5);
    VecCopy(&v, &from);
    long check[81] = {
        0, 1, 2, 0, 1, 3, 0, 1, 4,
        0, 2, 2, 0, 2, 3, 0, 2, 4,
        0, 3, 2, 0, 3, 3, 0, 3, 4,
        1, 1, 2, 1, 1, 3, 1, 1, 4,
        1, 2, 2, 1, 2, 3, 1, 2, 4,
        1, 3, 2, 1, 3, 3, 1, 3, 4,
        2, 1, 2, 2, 1, 3, 2, 1, 4,
        2, 2, 2, 2, 2, 3, 2, 2, 4,
        2, 3, 2, 2, 3, 3, 2, 3, 4
    };
    int iCheck = 0;
    do {
        for (int i = 0; i < 3; ++i) {
            if (ISEQUALF(check[iCheck], VecGet(&v, i)) == false) {
                PBMathErr->_type = PBErrTypeUnitTestFailed;
                sprintf(PBMathErr->_msg, "VecShiftStep NOK");
                PBErrCatch(PBMathErr);
            }
            ++iCheck;
        }
    } while(VecShiftStep(&v, &from, &to));
    printf("UnitTestVecLongShiftStep OK\n");
}

void UnitTestVecLongGetMinMax() {
    VecLong3D v = VecLongCreateStatic3D();
    VecSet(&v, 0, 2); VecSet(&v, 1, 4); VecSet(&v, 2, 3);
    long val = VecGetMaxVal(&v);
    if (val != 4) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMaxVal NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecGetIMaxVal(&v) != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetIMaxVal NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
    val = VecGetMinVal(&v);
    if (val != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMinVal NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 2); VecSet(&v, 1, -4); VecSet(&v, 2, 3);
    val = VecGetMaxValAbs(&v);
    if (val != -4) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
    }
}

```

```

        sprintf(PBMathErr->_msg, "VecGetMaxValAbs NOK");
        PBErCatch(PBMathErr);
    }
    VecSet(&v, 0, -2); VecSet(&v, 1, 1); VecSet(&v, 2, 3);
    val = VecGetMinValAbs(&v);
    if (val != 1) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetMinValAbs NOK");
        PBErCatch(PBMathErr);
    }
    printf("UnitTestVecLongGetMinMax OK\n");
}

void UnitTestVecLongHadamardProd() {
    VecLong* u = VecLongCreate(3);
    for (int i = 3; i--;)
        VecSet(u, i, i + 2);
    VecLong* uprod = VecGetHadamardProd(u, u);
    VecHadamardProd(u, u);
    long checku[3] = {4, 9, 16};
    for (int i = 3; i--;)
        if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErCatch(PBMathErr);
        }
    if (VecIsEqual(uprod, u) == false) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErCatch(PBMathErr);
    }
    VecFree(&uprod);
    VecFree(&u);
    VecLong2D v = VecLongCreateStatic2D();
    for (int i = 2; i--;)
        VecSet(&v, i, i + 2);
    VecLong2D vprod = VecGetHadamardProd(&v, &v);
    VecHadamardProd(&v, &v);
    long checkv[2] = {4, 9};
    for (int i = 2; i--;)
        if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErCatch(PBMathErr);
        }
    if (VecIsEqual(&vprod, &v) == false) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErCatch(PBMathErr);
    }
    VecLong3D w = VecLongCreateStatic3D();
    for (int i = 3; i--;)
        VecSet(&w, i, i + 2);
    VecLong3D wprod = VecGetHadamardProd(&w, &w);
    VecHadamardProd(&w, &w);
    long checkw[3] = {4, 9, 16};
    for (int i = 3; i--;)
        if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErCatch(PBMathErr);
        }
}

```

```

    if (VecIsEqual(&wprod, &w) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    VecLong4D x = VecLongCreateStatic4D();
    for (int i = 4; i--;)
        VecSet(&x, i, i + 2);
    VecLong4D xprod = VecGetHadamardProd(&x, &x);
    VecHadamardProd(&x, &x);
    long checkx[4] = {4, 9, 16, 25};
    for (int i = 4; i--;)
        if (ISEQUALF(VecGet(&xprod, i), checkx[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(&xprod, &x) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    printf("UnitTestVecLongHadamardProd OK\n");
}

void UnitTestVecLongGetNewDim() {
    VecLong* v = VecLongCreate(3);
    for (int i = 3; i--;)
        VecSet(v, i, i);
    VecLong* u = VecGetNewDim(v, 2);
    if (VecGetDim(u) != 2 ||
        VecGet(u, 0) != 0 ||
        VecGet(u, 1) != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetNewDim NOK 1");
        PBErrCatch(PBMathErr);
    }
    VecLong* w = VecGetNewDim(v, 4);
    if (VecGetDim(w) != 4 ||
        VecGet(w, 0) != 0 ||
        VecGet(w, 1) != 1 ||
        VecGet(w, 2) != 2 ||
        VecGet(w, 3) != 0) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecGetNewDim NOK 2");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&u);
    VecFree(&w);
    printf("UnitTestVecLongGetNewDim OK\n");
}

void UnitTestVecLong() {
    UnitTestVecLongCreateFree();
    UnitTestVecLongClone();
    UnitTestVecLongLoadSave();
    UnitTestVecLongGetSetDim();
    UnitTestVecLongStep();
    UnitTestVecLongHamiltonDist();
    UnitTestVecLongIsEqual();
    UnitTestVecLongDotProd();
}

```



```

    UnitTestVecLongCopy();
    UnitTestSpeedVecLong();
    UnitTestVecLongOp();
    UnitTestVecLongShiftStep();
    UnitTestVecLongGetMinMax();
    UnitTestVecLongHadamardProd();
    UnitTestVecLongGetNewDim();
    printf("UnitTestVecLong OK\n");
}

void UnitTestVecFloatCreateFree() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    VecPrintln(v, stdout);
    VecPrintln(&v2, stdout);
    VecPrintln(&v3, stdout);
    _VecFloatFree(&v);
    if (v != NULL) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecFloat is not null after _VecFloatFree");
        PBErrCatch(PBMathErr);
    }
    printf("VecFloatCreateFree OK\n");
}

void UnitTestVecFloatClone() {
    VecFloat* v = VecFloatCreate(5);
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    VecFloat* w = VecClone(v);
    if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatClone NOK");
        PBErrCatch(PBMathErr);
    }
    _VecFloatFree(&v);
    _VecFloatFree(&w);
    printf("_VecFloatClone OK\n");
}

void UnitTestVecFloatLoadSave() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    FILE* f = fopen("./UnitTestVecFloatLoadSave.txt", "w");
    if (f == NULL) {
        PBMathErr->_type = PBErrTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestVecFloatLoadSave.txt for writing");
        PBErrCatch(PBMathErr);
    }
    bool compact = false;
    if (!VecSave(v, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecSave(&v2, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
    }
}

```

```

        sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
        PBErriCatch(PBMathErr);
    }
    if (!VecSave(&v3, f, compact)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSave NOK");
        PBErriCatch(PBMathErr);
    }
    fclose(f);
    VecFloat* w = VecFloatCreate(2);
    f = fopen("./UnitTestVecFloatLoadSave.txt", "r");
    if (f == NULL) {
        PBMathErr->_type = PBErriTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestVecFloatLoadSave.txt for reading");
        PBErriCatch(PBMathErr);
    }
    if (!VecLoad(&w, f)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
        PBErriCatch(PBMathErr);
    }
    if (memcmp(v, w, sizeof(VecFloat) + sizeof(float) * 5) != 0) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
        PBErriCatch(PBMathErr);
    }
    if (!VecLoad(&w, f)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
        PBErriCatch(PBMathErr);
    }
    if (memcmp(&v2, w, sizeof(VecFloat) + sizeof(float) * 2) != 0) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
        PBErriCatch(PBMathErr);
    }
    if (!VecLoad(&w, f)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoad NOK");
        PBErriCatch(PBMathErr);
    }
    if (memcmp(&v3, w, sizeof(VecFloat) + sizeof(float) * 3) != 0) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatLoadSave NOK");
        PBErriCatch(PBMathErr);
    }
    fclose(f);
    VecFree(&v);
    VecFree(&w);
    int ret = system("cat ./UnitTestVecFloatLoadSave.txt");
    printf("_VecFloatLoadSave OK\n");
    ret = ret;
}

void UnitTestVecFloatGetSetDim() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    if (VecGetDim(v) != 5) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetDim NOK");
    }
}

```

```

    PBErrCatch(PBMathErr);
}
for (int i = 5; i--;) VecSet(v, i, (float)(i + 1));
for (int i = 2; i--;) VecSet(&v2, i, (float)(i + 1));
for (int i = 3; i--;) VecSet(&v3, i, (float)(i + 1));
for (int i = 5; i--;)
    if (!ISEQUALF(v->_val[i], (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(v2._val[i], (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(v3._val[i], (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGet NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 5; i--;) VecSetAdd(v, i, (float)(i + 1));
for (int i = 2; i--;) VecSetAdd(&v2, i, (float)(i + 1));
for (int i = 3; i--;) VecSetAdd(&v3, i, (float)(i + 1));
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), 2.0 * (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), 2.0 * (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), 2.0 * (float)(i + 1))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAdd NOK");
        PBErrCatch(PBMathErr);
    }
}

```

```

VecSetNull(v);
VecSetNull(&v2);
VecSetNull(&v3);
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), 0.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), 0.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), 0.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetNull NOK");
        PBErrCatch(PBMathErr);
    }
VecSetAll(v, 1.0);
VecSetAll(&v2, 1.0);
VecSetAll(&v3, 1.0);
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), 1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), 1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), 1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatSetAll NOK");
        PBErrCatch(PBMathErr);
    }
VecFree(&v);
printf("_VecFloatGetSetDim OK\n");
}

void UnitTestVecFloatCopy() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    VecFloat* w = VecFloatCreate(5);
    VecFloat2D w2 = VecFloatCreateStatic2D();
    VecFloat3D w3 = VecFloatCreateStatic3D();
    VecCopy(w, v);
    VecCopy(&w2, &v2);
    VecCopy(&w3, &v3);
    if (!VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
    }
}

```

```

    PBErriCatch(PBMathErr);
}
if (!VecIsEqual(&v2, &w2)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
    PBErriCatch(PBMathErr);
}
if (!VecIsEqual(&v3, &w3)) {
    PBMathErr->_type = PBErriTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatCopy NOK");
    PBErriCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecFloatCopy OK\n");
}

void UnitTestVecFloatNorm() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    if (!ISEQUALF(VecNorm(v), 7.416198)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
        PBErriCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(&v2), 2.236068)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
        PBErriCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(&v3), 3.741657)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNorm NOK");
        PBErriCatch(PBMathErr);
    }
    VecNormalise(v);
    VecNormalise(&v2);
    VecNormalise(&v3);
    if (!ISEQUALF(VecNorm(v), 1.0)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
        PBErriCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(&v2), 1.0)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
        PBErriCatch(PBMathErr);
    }
    if (!ISEQUALF(VecNorm(&v3), 1.0)) {
        PBMathErr->_type = PBErriTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatNormalise NOK");
        PBErriCatch(PBMathErr);
    }
    VecFree(&v);
    printf("UnitTestVecFloatNorm OK\n");
}

void UnitTestVecFloatDist() {

```

```

VecFloat* v = VecFloatCreate(5);
VecFloat2D v2 = VecFloatCreateStatic2D();
VecFloat3D v3 = VecFloatCreateStatic3D();
VecFloat* w = VecFloatCreate(5);
VecFloat2D w2 = VecFloatCreateStatic2D();
VecFloat3D w3 = VecFloatCreateStatic3D();
float b[5] = {-2.0, -1.0, 0.0, 1.0, 2.0};
for (int i = 5; i--;) VecSet(v, i, b[i]);
for (int i = 2; i--;) VecSet(&v2, i, b[i]);
for (int i = 3; i--;) VecSet(&v3, i, b[i]);
for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1.5);
for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
if (!ISEQUALF(VecDist(v, w), 7.158911)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecDist(&v2, &w2), 2.549510)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecDist(&v3, &w3), 3.840573)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecHamiltonDist(v, w), 13.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecHamiltonDist(&v2, &w2), 3.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecHamiltonDist(&v3, &w3), 5.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatHamiltonDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecPixelDist(v, w), 13.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecPixelDist(&v2, &w2), 2.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
    PBErrCatch(PBMathErr);
}
if (!ISEQUALF(VecPixelDist(&v3, &w3), 5.0)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatPixelDist NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecFloatDist OK\n");
}

```

```

void UnitTestVecFloatIsEqual() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    VecFloat* w = VecFloatCreate(5);
    VecFloat2D w2 = VecFloatCreateStatic2D();
    VecFloat3D w3 = VecFloatCreateStatic3D();
    if (VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    for (int i = 5; i--;) VecSet(w, i, i + 1);
    for (int i = 2; i--;) VecSet(&w2, i, i + 1);
    for (int i = 3; i--;) VecSet(&w3, i, i + 1);
    if (!VecIsEqual(v, w)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v2, &w2)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(&v3, &w3)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatIsEqual NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&v);
    VecFree(&w);
    printf("UnitTestVecFloatIsEqual OK\n");
}

void UnitTestVecFloatScale() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    float a = 0.1;
    VecFloat* w = VecGetScale(v, a);
    VecFloat2D w2 = VecGetScale(&v2, a);
    VecFloat3D w3 = VecGetScale(&v3, a);
    VecScale(v, a);
    VecScale(&v2, a);
}

```

```

VecScale(&v3, a);
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(w, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&w2, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&w3, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetScale NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(v, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&v2, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&v3, i), (float)(i + 1) * a)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatScale NOK");
        PBErrCatch(PBMathErr);
    }
VecFree(&v);
VecFree(&w);
printf("UnitTestVecFloatScale OK\n");
}

void UnitTestVecFloatOp() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    VecFloat* w = VecFloatCreate(5);
    VecFloat2D w2 = VecFloatCreateStatic2D();
    VecFloat3D w3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    float a[2] = {-0.1, 2.0};
    float b[5] = {-2.0, -1.0, 0.0, 1.0, 2.0};
    for (int i = 5; i--;) VecSet(v, i, b[i]);
    for (int i = 2; i--;) VecSet(&v2, i, b[i]);
    for (int i = 3; i--;) VecSet(&v3, i, b[i]);
    for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 0.5);
    for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 0.5);
    for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 0.5);
    VecFloat* u = VecGetOp(v, a[0], w, a[1]);
    VecFloat2D u2 = VecGetOp(&v2, a[0], &w2, a[1]);
}

```



```

VecFloat3D u3 = VecGetOp(&v3, a[0], &w3, a[1]);
float checku[5] = {5.2, 3.1, 1.0, -1.1, -3.2};
float checku2[2] = {-0.8, -2.9};
float checku3[3] = {1.2, -0.9, -3.0};
for (int i = 5; i--;)
    if (!ISEQUALF(VecGet(u, i), checku[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 2; i--;)
    if (!ISEQUALF(VecGet(&u2, i), checku2[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
        PBErrCatch(PBMathErr);
    }
for (int i = 3; i--;)
    if (!ISEQUALF(VecGet(&u3, i), checku3[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_VecFloatGetOp NOK");
        PBErrCatch(PBMathErr);
    }
VecOp(v, a[0], w, a[1]);
VecOp(&v2, a[0], &w2, a[1]);
VecOp(&v3, a[0], &w3, a[1]);
if (!VecIsEqual(v, u)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v2, &u2)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
    PBErrCatch(PBMathErr);
}
if (!VecIsEqual(&v3, &u3)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatOp NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
VecFree(&u);
printf("UnitTestVecFloatOp OK\n");
}

void UnitTestVecFloatDotProd() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    VecFloat* w = VecFloatCreate(5);
    VecFloat2D w2 = VecFloatCreateStatic2D();
    VecFloat3D w3 = VecFloatCreateStatic3D();
    float b[5] = {-2.0, -1.0, 0.0, 1.0, 2.0};
    for (int i = 5; i--;) VecSet(v, i, b[i]);
    for (int i = 2; i--;) VecSet(&v2, i, b[i]);
    for (int i = 3; i--;) VecSet(&v3, i, b[i]);
    for (int i = 5; i--;) VecSet(w, i, b[4 - i] + 1.5);
    for (int i = 2; i--;) VecSet(&w2, i, b[1 - i] + 1.5);
    for (int i = 3; i--;) VecSet(&w3, i, b[2 - i] + 1.5);
    float prod = VecDotProd(v, w);
    if (!ISEQUALF(prod, -10.0)) {

```

```

    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
}
prod = VecDotProd(&v2, &w2);
if (!ISEQUALF(prod, -0.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
}
prod = VecDotProd(&v3, &w3);
if (!ISEQUALF(prod, -3.5)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatDotProd NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecFloatDotProd OK\n");
}

void UnitTestVecFloatCrossProd() {
    VecFloat* v = VecFloatCreate(3);
    VecFloat3D v3 = VecFloatCreateStatic3D();
    VecFloat* w = VecFloatCreate(3);
    VecFloat3D w3 = VecFloatCreateStatic3D();
    float a[3] = {3.0, -3.0, 1.0};
    float b[3] = {4.0, 9.0, 2.0};
    float c[3] = {-15.0, -2.0, 39.0};
    for (int i = 3; i--;) VecSet(v, i, a[i]);
    for (int i = 3; i--;) VecSet(&v3, i, a[i]);
    for (int i = 3; i--;) VecSet(w, i, b[i]);
    for (int i = 3; i--;) VecSet(&w3, i, b[i]);
    VecFloat* prod = VecCrossProd(v, w);
    for (int i = 3; i--;)
        if (!ISEQUALF(VecGet(prod, i), c[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatCrossProd NOK");
            PBErrCatch(PBMathErr);
        }
    VecFloat3D prod3 = VecCrossProd(&v3, &w3);
    for (int i = 3; i--;)
        if (!ISEQUALF(VecGet(&prod3, i), c[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatCrossProd3D NOK");
            PBErrCatch(PBMathErr);
        }
    VecFree(&v);
    VecFree(&w);
    VecFree(&prod);
    printf("UnitTestVecFloatCrossProd OK\n");
}

void UnitTestVecFloatRotAngleTo() {
    VecFloat* v = VecFloatCreate(2);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat* w = VecFloatCreate(2);
    VecFloat2D w2 = VecFloatCreateStatic2D();
    VecSet(v, 0, 1.0);
    VecSet(&v2, 0, 1.0);
    VecSet(w, 0, 1.0);
    VecSet(&w2, 0, 1.0);

```

```

float a = 0.0;
float da = PBMath_TWOPI_DIV_360;
for (int i = 360; i--;) {
    VecRot(v, da);
    VecNormalise(v);
    VecRot(&v2, da);
    VecNormalise(&v2);
    a += da;
    if (ISEQUALF(a, PBMath_PI)) {
        a = -PBMath_PI;
        if (!ISEQUALF(fabs(VecAngleTo(w, v)), fabs(a))) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
            PBErrCatch(PBMathErr);
        }
        if (!ISEQUALF(fabs(VecAngleTo(&w2, &v2)), fabs(a))) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
            PBErrCatch(PBMathErr);
        }
    } else {
        if (!ISEQUALF(VecAngleTo(w, v), a)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
            PBErrCatch(PBMathErr);
        }
        if (!ISEQUALF(VecAngleTo(&w2, &v2), a)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "_VecFloatAngleTo NOK");
            PBErrCatch(PBMathErr);
        }
    }
}
VecSet(v, 0, 1.0);
VecSet(v, 1, 0.0);
VecRot(v, PBMath_QUARTERPI);
VecFloatPrint(v, stdout, 6); printf("\n");
if (!ISEQUALF(VecGet(v, 0), 0.707107) ||
    !ISEQUALF(VecGet(v, 1), 0.707107)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "_VecFloatRot NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);
VecFree(&w);
printf("UnitTestVecFloatAngleTo OK\n");
}

void UnitTestVecFloatToShort() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    for (int i = 5; i--;) VecSet(v, i, i + 1);
    for (int i = 2; i--;) VecSet(&v2, i, i + 1);
    for (int i = 3; i--;) VecSet(&v3, i, i + 1);
    VecShort* w = VecFloatToShort(v);
    VecShort2D w2 = VecFloatToShort2D(&v2);
    VecShort3D w3 = VecFloatToShort3D(&v3);
    VecPrintln(w, stdout);
    VecPrintln(&w2, stdout);
    VecPrintln(&w3, stdout);
    VecFree(&v);
}

```

```

    VecFree(&w);
    printf("UnitTestVecFloatToShort OK\n");
}

void UnitTestSpeedVecFloat() {
    VecFloat* v = VecFloatCreate(5);
    VecFloat2D v2 = VecFloatCreateStatic2D();
    VecFloat3D v3 = VecFloatCreateStatic3D();
    int nbTest = 100000;

    srand(RANDOMSEED);
    int i = nbTest;
    clock_t clockBefore = clock();
    for (; i--;) {
        int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMath_EPSILON));
        float val = 1.0;
        VecSet(v, j, val);
        float valb = VecGet(v, j);
        valb = valb;
    }
    clock_t clockAfter = clock();
    double timeV = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srand(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();
    float* array = malloc(sizeof(float) * 5);
    for (; i--;) {
        int j = INT(rnd() * ((float)(VecGetDim(v) - 1) - PBMath_EPSILON));
        float val = 1.0;
        array[j] = val;
        float valb = array[j];
        valb = valb;
    }
    clockAfter = clock();
    double timeRef = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    printf("VecFloat: %fms, array: %fms\n",
        timeV / (float)nbTest, timeRef / (float)nbTest);
    if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#ifdef BUILDMODE == 0
        PBMathErr->_fatal = false;
#endif
        PBMathErr->_type = PErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
        PErrCatch(PBMathErr);
    }

    srand(RANDOMSEED);
    i = nbTest;
    clockBefore = clock();
    for (; i--;) {
        int j = INT(rnd() * (1.0 - PBMath_EPSILON));
        float val = 1.0;
        VecSet(&v2, j, val);
        float valb = VecGet(&v2, j);
        valb = valb;
    }
    clockAfter = clock();
    timeV = ((double)(clockAfter - clockBefore)) /
        CLOCKS_PER_SEC * 1000.0;
    srand(RANDOMSEED);

```

```

i = nbTest;
clockBefore = clock();
float array2[2];
for (; i--;) {
    int j = INT(rnd() * (1.0 - PBMath_EPSILON));
    float val = 1.0;
    array2[j] = val;
    float valb = array2[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecFloat2D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#ifdef BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
    PBErrCatch(PBMathErr);
}

srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    float val = 1.0;
    VecSet(&v3, j, val);
    float valb = VecGet(&v3, j);
    valb = valb;
}
clockAfter = clock();
timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
float array3[3];
for (; i--;) {
    int j = INT(rnd() * (2.0 - PBMath_EPSILON));
    float val = 1.0;
    array3[j] = val;
    float valb = array3[j];
    valb = valb;
}
clockAfter = clock();
timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("VecFloat3D: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#ifdef BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedVecFloat NOK");
    PBErrCatch(PBMathErr);
}
VecFree(&v);

```

```

    free(array);
    printf("UnitTestSpeedVecFloat OK\n");
}

void UnitTestVecFloatRotAxis() {
    VecFloat3D v = VecFloatCreateStatic3D();
    VecSet(&v, 0, 1.0); VecSet(&v, 1, 0.0); VecSet(&v, 2, 1.0);
    VecFloat3D axis = VecFloatCreateStatic3D();
    VecSet(&axis, 0, 1.0); VecSet(&axis, 1, 1.0); VecSet(&axis, 2, 1.0);
    VecNormalise(&axis);
    float theta = PBMath_PI;
    VecRotAxis(&v, &axis, theta);
    if (!ISEQUALF(VecGet(&v, 0), 0.333333) ||
        !ISEQUALF(VecGet(&v, 1), 1.333333) ||
        !ISEQUALF(VecGet(&v, 2), 0.333333)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecRotAxis NOK");
        PBErrCatch(PBMathErr);
    }
    theta = PBMath_HALFPI;
    VecRotAxis(&v, &axis, theta);
    if (!ISEQUALF(VecGet(&v, 0), 0.089316) ||
        !ISEQUALF(VecGet(&v, 1), 0.666666) ||
        !ISEQUALF(VecGet(&v, 2), 1.244017)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecRotAxis NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
    theta = PBMath_PI;
    VecRotX(&v, theta);
    if (!ISEQUALF(VecGet(&v, 0), 1.0) ||
        !ISEQUALF(VecGet(&v, 1), -1.0) ||
        !ISEQUALF(VecGet(&v, 2), -1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecRotX NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
    theta = PBMath_PI;
    VecRotY(&v, theta);
    if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
        !ISEQUALF(VecGet(&v, 1), 1.0) ||
        !ISEQUALF(VecGet(&v, 2), -1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecRotY NOK");
        PBErrCatch(PBMathErr);
    }
    VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 1.0);
    theta = PBMath_PI;
    VecRotZ(&v, theta);
    if (!ISEQUALF(VecGet(&v, 0), -1.0) ||
        !ISEQUALF(VecGet(&v, 1), -1.0) ||
        !ISEQUALF(VecGet(&v, 2), 1.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecRotZ NOK");
        PBErrCatch(PBMathErr);
    }
    printf("UnitTestVecFloatRotAxis OK\n");
}

void UnitTestVecFloatGetMinMax() {

```

```

VecFloat2D v = VecFloatCreateStatic2D();
VecSet(&v, 0, 1.0); VecSet(&v, 1, 2.0);
float val = VecGetMaxVal(&v);
if (ISEQUALF(val, 2.0) == false) {
    PBMATHErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMATHErr->_msg, "VecGetMaxVal NOK");
    PBErrCatch(PBMATHErr);
}
if (VecGetIMaxVal(&v) != 1) {
    PBMATHErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMATHErr->_msg, "VecGetIMaxVal NOK");
    PBErrCatch(PBMATHErr);
}
val = VecGetMinVal(&v);
if (ISEQUALF(val, 1.0) == false) {
    PBMATHErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMATHErr->_msg, "VecGetMinVal NOK");
    PBErrCatch(PBMATHErr);
}
VecSet(&v, 0, 1.0); VecSet(&v, 1, -2.0);
val = VecGetMaxValAbs(&v);
if (ISEQUALF(val, -2.0) == false) {
    PBMATHErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMATHErr->_msg, "VecGetMaxValAbs NOK");
    PBErrCatch(PBMATHErr);
}
val = VecGetMinValAbs(&v);
if (ISEQUALF(val, 1.0) == false) {
    PBMATHErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMATHErr->_msg, "VecGetMinValAbs NOK");
    PBErrCatch(PBMATHErr);
}
printf("UnitTestVecFloatGetMinMax OK\n");
}

void UnitTestVecFloatGetNewDim() {
    VecFloat* v = VecFloatCreate(3);
    for (int i = 3; i--;)
        VecSet(v, i, (float)i);
    VecFloat* u = VecGetNewDim(v, 2);
    if (VecGetDim(u) != 2 ||
        ISEQUALF(VecGet(u, 0), 0.0) == false ||
        ISEQUALF(VecGet(u, 1), 1.0) == false) {
        PBMATHErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMATHErr->_msg, "VecGetNewDim NOK");
        PBErrCatch(PBMATHErr);
    }
    VecFloat* w = VecGetNewDim(v, 4);
    if (VecGetDim(w) != 4 ||
        ISEQUALF(VecGet(w, 0), 0.0) == false ||
        ISEQUALF(VecGet(w, 1), 1.0) == false ||
        ISEQUALF(VecGet(w, 2), 2.0) == false ||
        ISEQUALF(VecGet(w, 3), 0.0) == false) {
        PBMATHErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMATHErr->_msg, "VecGetNewDim NOK");
        PBErrCatch(PBMATHErr);
    }
    VecFree(&v);
    VecFree(&u);
    VecFree(&w);
    printf("UnitTestVecFloatGetNewDim OK\n");
}

```

```

void UnitTestVecFloatHadamardProd() {
    VecFloat* u = VecFloatCreate(3);
    for (int i = 3; i--;)
        VecSet(u, i, (float)i + 2.0);
    VecFloat* uprod = VecGetHadamardProd(u, u);
    VecHadamardProd(u, u);
    float checku[3] = {4.0, 9.0, 16.0};
    for (int i = 3; i--;)
        if (ISEQUALF(VecGet(uprod, i), checku[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(uprod, u) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    VecFree(&uprod);
    VecFree(&u);
    VecFloat2D v = VecFloatCreateStatic2D();
    for (int i = 2; i--;)
        VecSet(&v, i, (float)i + 2.0);
    VecFloat2D vprod = VecGetHadamardProd(&v, &v);
    VecHadamardProd(&v, &v);
    float checkv[2] = {4.0, 9.0};
    for (int i = 2; i--;)
        if (ISEQUALF(VecGet(&vprod, i), checkv[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(&vprod, &v) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    VecFloat3D w = VecFloatCreateStatic3D();
    for (int i = 3; i--;)
        VecSet(&w, i, (float)i + 2.0);
    VecFloat3D wprod = VecGetHadamardProd(&w, &w);
    VecHadamardProd(&w, &w);
    float checkw[3] = {4.0, 9.0, 16.0};
    for (int i = 3; i--;)
        if (ISEQUALF(VecGet(&wprod, i), checkw[i]) == false) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "VecGetHadamardProd NOK");
            PBErrCatch(PBMathErr);
        }
    if (VecIsEqual(&wprod, &w) == false) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "VecHadamardProd NOK");
        PBErrCatch(PBMathErr);
    }
    printf("UnitTestVecFloatHadamardProd OK\n");
}

void UnitTestVecFloat() {
    UnitTestVecFloatCreateFree();
    UnitTestVecFloatClone();
    UnitTestVecFloatLoadSave();
}

```



```

    UnitTestVecFloatGetSetDim();
    UnitTestVecFloatCopy();
    UnitTestVecFloatNorm();
    UnitTestVecFloatDist();
    UnitTestVecFloatIsEqual();
    UnitTestVecFloatScale();
    UnitTestVecFloatOp();
    UnitTestVecFloatDotProd();
    UnitTestVecFloatCrossProd();
    UnitTestVecFloatRotAngleTo();
    UnitTestVecFloatToShort();
    UnitTestVecFloatGetMinMax();
    UnitTestVecFloatRotAxis();
    UnitTestVecFloatGetNewDim();
    UnitTestVecFloatHadamardProd();
    UnitTestSpeedVecFloat();
    printf("UnitTestVecFloat OK\n");
}

void UnitTestMatFloatCreateFree() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    for (int i = VecGet(&dim, 0) * VecGet(&dim, 1); i--;) {
        if (!ISEQUALF(mat->_val[i], 0.0)) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatCreateFree NOK");
            PBErrCatch(PBMathErr);
        }
    }
    MatFree(&mat);
    if (mat != NULL) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "mat is not null after MatFree");
        PBErrCatch(PBMathErr);
    }
    printf("UnitTestMatFloatCreateFree OK\n");
}

void UnitTestMatFloatGetSetDim() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    if (!VecIsEqual(&(mat->_dim), &dim)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
        PBErrCatch(PBMathErr);
    }
    if (!VecIsEqual(MatDim(mat), &dim)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
        PBErrCatch(PBMathErr);
    }
    if (MatGetNbRow(mat) != 3) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "MatGetNbRow NOK");
        PBErrCatch(PBMathErr);
    }
    if (MatGetNbCol(mat) != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
    }
}

```

```

        sprintf(PBMathErr->_msg, "MatGetNbCol NOK");
        PBErCatch(PBMathErr);
    }
    VecShort2D i = VecShortCreateStatic2D();
    float v = 1.0;
    do {
        MatSet(mat, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    v = 1.0;
    for (int j = 0; j < VecGet(&dim, 0); ++j) {
        for (int k = 0; k < VecGet(&dim, 1); ++k) {
            if (!ISEQUALF(mat->_val[k * VecGet(&dim, 0) + j], v)) {
                PBMathErr->_type = PBErTypeUnitTestFailed;
                sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
                PBErCatch(PBMathErr);
            }
            v += 1.0;
        }
    }
    VecSetNull(&i);
    v = 1.0;
    do {
        float w = MatGet(mat, &i);
        if (!ISEQUALF(v, w)) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatGetSetDim NOK");
            PBErCatch(PBMathErr);
        }
        v += 1.0;
    } while(VecStep(&i, &dim));
    MatFree(&mat);
    printf("UnitTestMatFloatGetSetDim OK\n");
}

void UnitTestMatFloatCloneIsEqual() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v = 1.0;
    do {
        MatSet(mat, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    MatFloat* clone = MatClone(mat);
    if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
        PBErCatch(PBMathErr);
    }
    VecSetNull(&i);
    do {
        if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatClone NOK");
            PBErCatch(PBMathErr);
        }
    } while(VecStep(&i, &dim));
    if (MatIsEqual(mat, clone) == false) {
        PBMathErr->_type = PBErTypeUnitTestFailed;
    }
}

```

```

        sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK1");
        PBErCatch(PBMathErr);
    }
    VecSet(&i, 0, 0); VecSet(&i, 1, 0);
    MatSet(clone, &i, -1.0);
    if (MatIsEqual(mat, clone) == true) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatIsEqual NOK2");
        PBErCatch(PBMathErr);
    }
    MatFree(&mat);
    MatFree(&clone);
    printf("UnitTestMatFloatCloneIsEqual OK\n");
}

void UnitTestMatFloatLoadSave() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v = 1.0;
    do {
        MatSet(mat, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    FILE* f = fopen("./UnitTestMatFloatLoadSave.txt", "w");
    if (f == NULL) {
        PBMathErr->_type = PBErrTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestMatFloatLoadSave.txt for writing");
        PBErCatch(PBMathErr);
    }
    bool compact = false;
    if (!MatSave(mat, f, compact)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_MatFloatSave NOK");
        PBErCatch(PBMathErr);
    }
    fclose(f);
    MatFloat* clone = MatFloatCreate(&dim);
    f = fopen("./UnitTestMatFloatLoadSave.txt", "r");
    if (f == NULL) {
        PBMathErr->_type = PBErrTypeOther;
        sprintf(PBMathErr->_msg,
            "Can't open ./UnitTestMatFloatLoadSave.txt for reading");
        PBErCatch(PBMathErr);
    }
    if (!MatLoad(&clone, f)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "_MatFloatLoad NOK");
        PBErCatch(PBMathErr);
    }
    if (!VecIsEqual(&(mat->_dim), &(clone->_dim))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
        PBErCatch(PBMathErr);
    }
    VecSetNull(&i);
    do {
        if (!ISEQUALF(MatGet(mat, &i), MatGet(clone, &i))) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;

```

```

        sprintf(PBMathErr->_msg, "UnitTestMatFloatLoadSave NOK");
        PBErCatch(PBMathErr);
    }
} while(VecStep(&i, &dim));
fclose(f);
MatFree(&mat);
MatFree(&clone);
int ret = system("cat ./UnitTestMatFloatLoadSave.txt");
ret = ret;
printf("UnitTestMatFloatLoadSave OK\n");
}

void UnitTestMatFloatTransposeScale() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v[6] = {3.0, 2.0, 1.0, 2.0, -2.0, 1.0};
    int j = 0;
    do {
        MatSet(mat, &i, v[j]);
        ++j;
    } while(VecStep(&i, &dim));
    MatFloat* trans = MatGetTranspose(mat);
    float w[6] = {3.0, 2.0, 2.0, -2.0, 1.0, 1.0};
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 2);
    VecSetNull(&i);
    j = 0;
    do {
        if (!ISEQUALF(MatGet(trans, &i), w[j])) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatTranspose NOK");
            PBErCatch(PBMathErr);
        }
        ++j;
    } while(VecStep(&i, &dim));
    MatScale(mat, 2.0);
    j = 0;
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    VecSetNull(&i);
    float u[6] = {6.0, 4.0, 2.0, 4.0, -4.0, 2.0};
    do {
        if (!ISEQUALF(MatGet(mat, &i), u[j])) {
            PBMathErr->_type = PBErTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "MatScale NOK");
            PBErCatch(PBMathErr);
        }
        ++j;
    } while(VecStep(&i, &dim));
    MatFree(&mat);
    MatFree(&trans);
    printf("UnitTestMatFloatTransposeScale OK\n");
}

void UnitTestMatFloatInv() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);

```

```

VecShort2D i = VecShortCreateStatic2D();
float v[9] = {3.0, 2.0, 0.0, 0.0, 0.0, 1.0, 2.0, -2.0, 1.0};
int j = 0;
do {
    MatSet(mat, &i, v[j]);
    ++j;
} while(VecStep(&i, &dim));
MatFloat* inv = MatGetInv(mat);
float w[9] = {0.2, -0.2, 0.2, 0.2, 0.3, -0.3, 0.0, 1.0, 0.0};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), w[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (1)");
        PBErrCatch(PBMathErr);
    }
    ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);
VecSet(&dim, 0, 2);
VecSet(&dim, 1, 2);
mat = MatFloatCreate(&dim);
float vb[4] = {4.0, 2.0, 7.0, 6.0};
VecSetNull(&i);
j = 0;
do {
    MatSet(mat, &i, vb[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
float wb[4] = {0.6, -0.2, -0.7, 0.4};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), wb[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (2)");
        PBErrCatch(PBMathErr);
    }
    ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);

VecSet(&dim, 0, 4);
VecSet(&dim, 1, 4);
mat = MatFloatCreate(&dim);
float vc[16] = {4, 0, 0, 0, 0, 1, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    MatSet(mat, &i, vc[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv == NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (3)");
    PBErrCatch(PBMathErr);
}

```

```

}
float wc[16] = {0.25, 0, 0, 0, 0, 0, 1, -1, 0, 0, 0, 0.5, 0, -0.25, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), wc[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (4)");
        PBErrCatch(PBMathErr);
    }
    ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);

mat = MatFloatCreate(&dim);
float vd[16] = {4, 0, 0, 0, 0, 0, 2, 0, 0, 1, 2, 0, 1, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    MatSet(mat, &i, vd[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv == NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (3)");
    PBErrCatch(PBMathErr);
}
float wd[16] = {0.25, 0, 0, 0, 0, 0, -1, 1, 0, 0, 0.5, 0, 0, -0.25, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), wd[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (5)");
        PBErrCatch(PBMathErr);
    }
    ++j;
} while(VecStep(&i, &dim));
MatFree(&mat);
MatFree(&inv);

mat = MatFloatCreate(&dim);
float ve[16] = {4, 0, 0, 0, 0, 0, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    MatSet(mat, &i, ve[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (6)");
    PBErrCatch(PBMathErr);
}
MatFree(&mat);

mat = MatFloatCreate(&dim);
float vf[16] = {0, 1, 2, 0, 0, 0, 2, 0, 1, 0, 0, 1, 4, 0, 0, 0};
VecSetNull(&i);

```

```

j = 0;
do {
    MatSet(mat, &i, vf[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (7)");
    PBErrCatch(PBMathErr);
}
/* TODO
if (inv == NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (7)");
    PBErrCatch(PBMathErr);
}
float wf[16] = {0, 0, 0, 0.25, 1, -1, 0, 0, 0, 0.5, 0, 0, 0, 0, 1, -0.25};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), wf[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (8)");
        PBErrCatch(PBMathErr);
    }
    ++j;
} while(VecStep(&i, &dim));
MatFree(&inv);
*/
MatFree(&mat);

mat = MatFloatCreate(&dim);
float vg[16] = {0, 1, 2, 0, 0, 0, 2, 0, 4, 0, 0, 0, 1, 0, 0, 1};
VecSetNull(&i);
j = 0;
do {
    MatSet(mat, &i, vg[j]);
    ++j;
} while(VecStep(&i, &dim));
inv = MatGetInv(mat);
if (inv != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (9)");
    PBErrCatch(PBMathErr);
}
/* TODO
if (inv == NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (9)");
    PBErrCatch(PBMathErr);
}
float wg[16] = {0, 0, 0.25, 0, 1, -1, 0, 0, 0, 0.5, 0, 0, 0, 0, -0.25, 1};
VecSetNull(&i);
j = 0;
do {
    if (!ISEQUALF(MatGet(inv, &i), wg[j])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatInv NOK (10)");
        PBErrCatch(PBMathErr);
    }
    ++j;
}

```

```

    } while(VecStep(&i, &dim));
    MatFree(&inv);
    /*
    MatFree(&mat);

    printf("UnitTestMatFloatInv OK\n");
}

void UnitTestMatFloatProdVecFloat() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v = 1.0;
    do {
        MatSet(mat, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    VecFloat2D u = VecFloatCreateStatic2D();
    for (int j = 2; j--;)
        VecSet(&u, j, (float)j + 1.0);
    VecFloat* w = MatGetProdVec(mat, &u);
    float b[3] = {9.0, 12.0, 15.0};
    for (int j = 3; j--;) {
        if (!ISEQUALF(VecGet(w, j), b[j])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatProdVecFloat NOK");
            PBErrCatch(PBMathErr);
        }
    }
    MatFree(&mat);
    VecFree(&w);
    printf("UnitTestMatFloatProdVecFloat OK\n");
}

void UnitTestMatFloatProdMatFloat() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 2);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v = 1.0;
    do {
        MatSet(mat, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* matb = MatFloatCreate(&dim);
    VecSetNull(&i);
    v = 1.0;
    do {
        MatSet(matb, &i, v);
        v += 1.0;
    } while(VecStep(&i, &dim));
    MatFloat* matc = MatGetProdMat(mat, matb);
    float w[4] = {22.0, 28.0, 49.0, 64.0};
    VecSetNull(&i);
    int j = 0;
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 2);

```



```

    if (!VecIsEqual(&dim, &(matc->_dim))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
        PBErrCatch(PBMathErr);
    }
    do {
        if (!ISEQUALF(MatGet(matc, &i), w[j])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestMatFloatProdMatFloat NOK");
            PBErrCatch(PBMathErr);
        }
        ++j;
    } while(VecStep(&i, &dim));
    MatFree(&mat);
    MatFree(&matb);
    MatFree(&matc);
    printf("UnitTestMatFloatProdMatFloat OK\n");
}

void UnitTestMatFloatProdVecVecTranspose() {
    VecFloat2D v = VecFloatCreateStatic2D();
    VecFloat3D w = VecFloatCreateStatic3D();
    VecSet(&v, 0, 2.0);
    VecSet(&v, 1, 3.0);
    VecSet(&w, 0, 4.0);
    VecSet(&w, 1, 5.0);
    VecSet(&w, 2, 6.0);
    MatFloat* mat = MatGetProdVecVecTranspose(&v, &w);
    VecShort2D pos = VecShortCreateStatic2D();
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 2);
    float check[6] = {8.0, 12.0, 10.0, 15.0, 12.0, 18.0};
    int i = 0;
    do {
        if (!ISEQUALF(MatGet(mat, &pos), check[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "MatGetProdVecVecTranspose NOK");
            PBErrCatch(PBMathErr);
        }
        ++i;
    } while (VecStep(&pos, &dim));
    MatFree(&mat);
    printf("UnitTestMatFloatProdVecVecTranspose OK\n");
}

void UnitTestMatFloatGetEigenValues() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D pos = VecShortCreateStatic2D();
    float check[3][3] = {
        { 2.92, 0.86, -1.15},
        { 0.86, 6.51, 3.32},
        {-1.15, 3.32, 4.57}
    };
    do {
        MatSet(mat, &pos, check[VecGet(&pos, 1)][VecGet(&pos, 0)]);
    } while (VecStep(&pos, &dim));
    printf("mat:\n"); MatPrintln(mat, stdout);
    GSetVecFloat set = MatGetEigenValues(mat);

```

```

printf("Eigen values: ");
VecPrintln(GSetGet(&set, 0), stdout);
VecFloat3D checkValues = VecFloatCreateStatic3D();
VecSet(&checkValues, 0, 8.998802);
VecSet(&checkValues, 1, 3.996595);
VecSet(&checkValues, 2, 1.004607);
if (!VecIsEqual(GSetGet(&set, 0), &checkValues)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
    PBErrCatch(PBMathErr);
}
printf("Eigen vector 1: ");
VecPrintln(GSetGet(&set, 1), stdout);
printf("Eigen vector 2: ");
VecPrintln(GSetGet(&set, 2), stdout);
printf("Eigen vector 3: ");
VecPrintln(GSetGet(&set, 3), stdout);
VecFloat3D checkVecA = VecFloatCreateStatic3D();
VecSet(&checkVecA, 0, 0.000290);
VecSet(&checkVecA, 1, -0.800102);
VecSet(&checkVecA, 2, -0.599864);
if (!VecIsEqual(GSetGet(&set, 1), &checkVecA)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
    PBErrCatch(PBMathErr);
}
VecFloat3D checkVecB = VecFloatCreateStatic3D();
VecSet(&checkVecB, 0, 0.800110);
VecSet(&checkVecB, 1, 0.360017);
VecSet(&checkVecB, 2, -0.479806);
if (!VecIsEqual(GSetGet(&set, 2), &checkVecB)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
    PBErrCatch(PBMathErr);
}
VecFloat3D checkVecC = VecFloatCreateStatic3D();
VecSet(&checkVecC, 0, 0.599855);
VecSet(&checkVecC, 1, -0.479817);
VecSet(&checkVecC, 2, 0.640273);
if (!VecIsEqual(GSetGet(&set, 3), &checkVecC)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetEigenValues NOK");
    PBErrCatch(PBMathErr);
}
do {
    VecFloat* v = GSetPop(&set);
    VecFree(&v);
} while (GSetNbElem(&set) > 0);
MatFree(&mat);
printf("UnitTestMatFloatGetEigenValues OK\n");
}

void UnitTestSpeedMatFloat() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    int nbTest = 100000;
    srandom(RANDOMSEED);
    int i = nbTest;
    clock_t clockBefore = clock();
    VecShort2D j = VecShortCreateStatic2D();

```

```

for (; i--;) {
    float val = 1.0;
    MatSet(mat, &j, val);
    float valb = MatGet(mat, &j);
    valb = valb;
    VecStep(&j, &dim);
}
clock_t clockAfter = clock();
double timeV = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
srandom(RANDOMSEED);
i = nbTest;
clockBefore = clock();
float* array = malloc(sizeof(float) * 9);
short *ptr = j._val;
for (; i--;) {
    float val = 1.0;
    int k = ptr[1] * 3 + ptr[0];
    array[k] = val;
    float valb = array[k];
    valb = valb;
    VecStep(&j, &dim);
}
clockAfter = clock();
double timeRef = ((double)(clockAfter - clockBefore)) /
    CLOCKS_PER_SEC * 1000.0;
printf("MatFloat: %fms, array: %fms\n",
    timeV / (float)nbTest, timeRef / (float)nbTest);
if (timeV / (float)nbTest > 2.0 * timeRef / (float)nbTest) {
#if BUILDMODE == 0
    PBMathErr->_fatal = false;
#endif
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestSpeedMatFloat NOK");
    PBErrCatch(PBMathErr);
}
MatFree(&mat);
free(array);
printf("UnitTestSpeedMatFloat OK\n");
}

void UnitTestMatFloatGetQR() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 4);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D pos = VecShortCreateStatic2D();
    float val[4][3] = {
        {-1.0, -1.0, 1.0},
        { 1.0,  3.0, 3.0},
        {-1.0, -1.0, 5.0},
        { 1.0,  3.0, 7.0}
    };
    do {
        MatSet(mat, &pos, val[VecGet(&pos, 1)][VecGet(&pos, 0)]);
    } while (VecStep(&pos, &dim));
    QRDecomp qr = MatGetQR(mat);
    MatFloat* QR = MatGetProdMat(qr._Q, qr._R);

    printf("mat:\n");
    MatPrintln(mat, stdout);
    printf("Q:\n");
}

```

```

MatPrintln(qr._Q, stdout);
printf("R:\n");
MatPrintln(qr._R, stdout);
printf("QR:\n");
MatPrintln(QR, stdout);

MatFloat* Q = MatFloatCreate(&dim);
VecSetNull(&pos);
float checkQ[4][3] = {
    {-0.5, -0.5, 0.5},
    { 0.5, -0.5, 0.5},
    {-0.5, -0.5, -0.5},
    { 0.5, -0.5, -0.5}
};
do {
    MatSet(Q, &pos, checkQ[VecGet(&pos, 1)][VecGet(&pos, 0)]);
} while (VecStep(&pos, &dim));
VecSet(&dim, 1, 3);
MatFloat* R = MatFloatCreate(&dim);
VecSetNull(&pos);
float checkR[3][3] = {
    {2.0, 4.0, 2.0},
    {0.0, -2.0, -8.0},
    {0.0, 0.0, -4.0}
};
do {
    MatSet(R, &pos, checkR[VecGet(&pos, 1)][VecGet(&pos, 0)]);
} while (VecStep(&pos, &dim));
if (!MatIsEqual(Q, qr._Q) || !MatIsEqual(R, qr._R) ||
    !MatIsEqual(QR, mat)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "MatGetQR NOK");
    PBErrCatch(PBMathErr);
}
MatFree(&mat);
MatFree(&Q);
MatFree(&R);
MatFree(&QR);
QRDecompFreeStatic(&qr);
printf("UnitTestMatFloatGetQR OK\n");
}

void UnitTestMatFloat() {
    UnitTestMatFloatCreateFree();
    UnitTestMatFloatGetSetDim();
    UnitTestMatFloatCloneIsEqual();
    UnitTestMatFloatLoadSave();
    UnitTestMatFloatInv();
    UnitTestMatFloatTransposeScale();
    UnitTestMatFloatProdVecFloat();
    UnitTestMatFloatProdMatFloat();
    UnitTestMatFloatGetQR();
    UnitTestMatFloatProdVecVecTranspose();
    UnitTestMatFloatGetEigenValues();
    UnitTestSpeedMatFloat();
    printf("UnitTestMatFloat OK\n");
}

void UnitTestSysLinEq() {
    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 3);
    VecSet(&dim, 1, 3);

```

```

MatFloat* mat = MatFloatCreate(&dim);
float a[9] = {2.0, 2.0, 6.0, 1.0, 6.0, 8.0, 3.0, 8.0, 18.0};
VecShort2D index = VecShortCreateStatic2D();
int j = 0;
do {
    MatSet(mat, &index, a[j]);
    ++j;
} while(VecStep(&index, &dim));
VecFloat3D v = VecFloatCreateStatic3D();
float b[3] = {1.0, 3.0, 5.0};
for (int i = 3; i--;)
    VecSet(&v, i, b[i]);
SysLinEq* sys = SysLinEqCreate(mat, &v);
VecFloat* res = SysLinEqSolve(sys);
float c[3] = {0.3, 0.4, 0};
for (int i = 3; i--;) {
    if (!ISEQUALF(c[i], VecGet(res, i))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
        PBErrCatch(PBMathErr);
    }
}
float ab[9] = {3.0, 2.0, -1.0, 2.0, -2.0, 0.5, -1.0, 4.0, -1.0};
VecSetNull(&index);
j = 0;
do {
    MatSet(mat, &index, ab[j]);
    ++j;
} while(VecStep(&index, &dim));
SysLinEqSetM(sys, mat);
float bb[3] = {1.0, -2.0, 0.0};
for (int i = 3; i--;)
    VecSet(&v, i, bb[i]);
SysLinEqSetV(sys, &v);
VecFree(&res);
res = SysLinEqSolve(sys);
float cb[3] = {1.0, -2.0, -2.0};
for (int i = 3; i--;) {
    if (!ISEQUALF(cb[i], VecGet(res, i))) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "SysLinEqSolve NOK");
        PBErrCatch(PBMathErr);
    }
}
VecFree(&res);
SysLinEqFree(&sys);
if (sys != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "sys is not null after free");
    PBErrCatch(PBMathErr);
}
MatFree(&mat);
printf("UnitTestSysLinEq OK\n");
}

void UnitTestGauss() {
    srandom(RANDOMSEED);
    float mean = 1.0;
    float sigma = 0.5;
    Gauss *gauss = GaussCreate(mean, sigma);
    if (!ISEQUALF(gauss->_mean, mean) ||
        !ISEQUALF(gauss->_sigma, sigma)) {

```

```

    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussCreate NOK");
    PBErrCatch(PBMathErr);
}
float a[22] = {0.000268, 0.001224, 0.004768, 0.015831, 0.044789,
    0.107982, 0.221842, 0.388372, 0.579383, 0.736540, 0.797885,
    0.736540, 0.579383, 0.388372, 0.221842, 0.107982, 0.044789,
    0.015831, 0.004768, 0.001224, 0.000268};
for (int i = -5; i <= 15; ++i) {
    if (!ISEQUALF(GaussGet(gauss, (float)i * 0.2), a[i + 5])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestGaussGet NOK");
        PBErrCatch(PBMathErr);
    }
}
int nbsample = 1000000;
double sum = 0.0;
double sumsquare = 0.0;
for (int i = nbsample; i--;) {
    float v = GaussRnd(gauss);
    sum += v;
    sumsquare += fsquare(v);
}
double avg = sum / (double)nbsample;
double sig = sqrtf(sumsquare / (double)nbsample - fsquare(avg));
if (fabs(avg - mean) > 0.001 ||
    fabs(sig - sigma) > 0.001) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "UnitTestGaussRnd NOK");
    PBErrCatch(PBMathErr);
}
GaussFree(&gauss);
if (gauss != NULL) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "gauss is not null after free");
    PBErrCatch(PBMathErr);
}
printf("UnitTestGauss OK\n");
}

void UnitTestSmoother() {
    float smooth[11] = {0.0, 0.028, 0.104, 0.216, 0.352, 0.5, 0.648,
        0.784, 0.896, 0.972, 1.0};
    float smoother[11] = {0.0, 0.00856, 0.05792, 0.16308, 0.31744, 0.5,
        0.68256, 0.83692, 0.94208, 0.99144, 1.0};
    for (int i = 0; i <= 10; ++i) {
        if (!ISEQUALF(SmoothStep((float)i * 0.1), smooth[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestSmooth NOK");
            PBErrCatch(PBMathErr);
        }
        if (!ISEQUALF(SmootherStep((float)i * 0.1), smoother[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "UnitTestSmoother NOK");
            PBErrCatch(PBMathErr);
        }
    }
    printf("UnitTestSmoother OK\n");
}

void UnitTestConv() {
    float rad[5] = {0.0, PBMath_TWOPI, PBMath_PI, PBMath_HALFPI, 3.0 * PBMath_HALFPI};

```

```

float deg[5] = {0.0, 360.0, 180.0, 90.0, 270.0};
for (int i = 5; i--;) {
    if (!ISEQUALF(ConvRad2Deg(rad[i]), deg[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestConvRad2Deg NOK");
        PBErrCatch(PBMathErr);
    }
    if (!ISEQUALF(ConvDeg2Rad(deg[i]), rad[i])) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "UnitTestConvDeg2Rad NOK");
        PBErrCatch(PBMathErr);
    }
}
printf("UnitTestConv OK\n");
}

void UnitTestThueMorseSeq() {
    long seq_2[16] = {0,1,1,0,1,0,0,1,1,0,0,1,0,1,1,0};
    long seq_3[27] = {0,1,2,1,2,0,2,0,1,1,2,0,2,0,1,0,
        1,2,2,0,1,0,1,2,1,2,0};
    long seq_4[64] = {0,1,2,3,1,2,3,0,2,3,0,1,3,0,1,2,
        1,2,3,0,2,3,0,1,3,0,1,2,0,1,2,3,2,3,0,1,3,0,1,2,
        0,1,2,3,1,2,3,0,3,0,1,2,0,1,2,3,1,2,3,0,2,3,0,1};
    for (long iElem = 0; iElem < 16; ++iElem) {
        long thuemorse = ThueMorseSeqGetNthElem(iElem, 2);
        if (thuemorse != seq_2[iElem]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "ThueMorseSeqGetNthElem NOK (%ld,2)",
                iElem);
            PBErrCatch(PBMathErr);
        }
    }
    for (long iElem = 0; iElem < 27; ++iElem) {
        long thuemorse = ThueMorseSeqGetNthElem(iElem, 3);
        if (thuemorse != seq_3[iElem]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "ThueMorseSeqGetNthElem NOK (%ld,3)",
                iElem);
            PBErrCatch(PBMathErr);
        }
    }
    for (long iElem = 0; iElem < 64; ++iElem) {
        long thuemorse = ThueMorseSeqGetNthElem(iElem, 4);
        if (thuemorse != seq_4[iElem]) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "ThueMorseSeqGetNthElem NOK (%ld,4)",
                iElem);
            PBErrCatch(PBMathErr);
        }
    }
    printf("UnitTestThueMorseSeq OK\n");
}

void UnitTestGetAreaTriangleHero() {
    double area = GetAreaTriangleHero(5.0, 29.0, 30.0);
    if (!ISEQUALF(area, 72.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetAreaTriangleHero NOK (%f)",
            area);
        PBErrCatch(PBMathErr);
    }
}

```

```

    printf("UnitTestGetAreaTriangleHero OK\n");
}

void UnitTestGetFibonacciSeq() {
    unsigned long* seq = GetFibonacciSeq(14);
    if (
        seq[0] != 1 ||
        seq[1] != 1 ||
        seq[2] != 2 ||
        seq[3] != 3 ||
        seq[4] != 5 ||
        seq[5] != 8 ||
        seq[6] != 13 ||
        seq[7] != 21 ||
        seq[8] != 34 ||
        seq[9] != 55 ||
        seq[10] != 89 ||
        seq[11] != 144 ||
        seq[12] != 233 ||
        seq[13] != 377) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetFibonacciSeq NOK");
        PBErrCatch(PBMathErr);
    }
    free(seq);

    printf("UnitTestGetFibonacciSeq OK\n");
}

void UnitTestGetFibonacciLattice() {

    unsigned long nbPoints = 0;
    float* latticeGrid =
        GetFibonacciGridLattice(
            5,
            &nbPoints);
    if (nbPoints != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetFibonacciGridLattice NOK");
        PBErrCatch(PBMathErr);
    }
    float checkGrid[10] =
    {
        0.000000, 0.000000,
        0.200000, 0.600000,
        0.400000, 0.200000,
        0.600000, 0.800000,
        0.800000, 0.400000
    };
    for (int i = 0; i < 10; ++i) {
        if (!ISEQUALF(latticeGrid[i], checkGrid[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "GetFibonacciGridLattice NOK");
            PBErrCatch(PBMathErr);
        }
    }
    free(latticeGrid);

    nbPoints = 0;
    float* latticePolar =
        GetFibonacciPolarLattice(
            5,

```



```

        &nbPoints);
    if (nbPoints != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetFibonacciPolarLattice NOK");
        PBErrCatch(PBMathErr);
    }
    float checkPolar[10] =
    {
        0.000000, 0.000000,
        0.447214, 3.769911,
        0.632456, 1.256637,
        0.774597, 5.026548,
        0.894427, 2.513275
    };
    for (int i = 0; i < 10; ++i) {
        if (!ISEQUALF(latticePolar[i], checkPolar[i])) {
            PBMathErr->_type = PBErrTypeUnitTestFailed;
            sprintf(PBMathErr->_msg, "GetFibonacciPolarLattice NOK");
            PBErrCatch(PBMathErr);
        }
    }
    free(latticePolar);

    printf("UnitTestGetFibonacciLattice OK\n");
}

void UnitTestGetGCD() {

    unsigned int gcd = GetGCD(4, 6);
    if (gcd != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetGCD NOK");
        PBErrCatch(PBMathErr);
    }
    gcd = GetGCD(6, 4);
    if (gcd != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetGCD NOK");
        PBErrCatch(PBMathErr);
    }
    gcd = GetGCD(10, 6);
    if (gcd != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "GetGCD NOK");
        PBErrCatch(PBMathErr);
    }

    printf("UnitTestGetGCD OK\n");
}

void UnitTestBasicFunctions() {
    UnitTestConv();
    UnitTestPowi();
    UnitTestFastPow();
    UnitTestSpeedFastPow();
    UnitTestFSquare();
    UnitTestConv();
    UnitTestThueMorseSeq();
    UnitTestGetAreaTriangleHero();
    UnitTestGetFibonacciSeq();
}

```

```

    UnitTestGetFibonacciLattice();
    UnitTestGetGCD();
    printf("UnitTestBasicFunctions OK\n");
}

void UnitTestRatio() {
    Ratio ratio = RatioCreateStatic(1, 2, 3);
    if (
        ratio._base != 1 ||
        ratio._numerator != 2 ||
        ratio._denominator != 3) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioCreateStatic NOK");
        PBErrCatch(PBMathErr);
    }
    if (RatioGetBase(&ratio) != 1) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioGetBase NOK");
        PBErrCatch(PBMathErr);
    }
    if (RatioGetNumerator(&ratio) != 2) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioGetNumerator NOK");
        PBErrCatch(PBMathErr);
    }
    if (RatioGetDenominator(&ratio) != 3) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioGetDenominator NOK");
        PBErrCatch(PBMathErr);
    }
    if (!ISEQUALF(RatioToFloat(&ratio), 1.666666)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioToFloat NOK");
        PBErrCatch(PBMathErr);
    }
    RatioSetBase(&ratio, 4);
    if (RatioGetBase(&ratio) != 4) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioSetBase NOK");
        PBErrCatch(PBMathErr);
    }
    RatioSetNumerator(&ratio, 5);
    if (RatioGetNumerator(&ratio) != 5) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioSetNumerator NOK");
        PBErrCatch(PBMathErr);
    }
    RatioSetDenominator(&ratio, 6);
    if (RatioGetDenominator(&ratio) != 6) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "RatioSetDenominator NOK");
        PBErrCatch(PBMathErr);
    }
    Ratio ratiob = RatioCreateStatic(0, 10, 6);
    RatioPrint(&ratiob, stdout);
    printf(" -> ");
    RatioReduce(&ratiob);
    RatioPrintLn(&ratiob, stdout);
    if (
        ratiob._base != 1 ||
        ratiob._numerator != 2 ||
        ratiob._denominator != 3) {

```

```

    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "RatioReduce NOK");
    PBErrCatch(PBMathErr);
}
Ratio ratioc = RatioFromFloat(1.666666);
printf("1.666666=");
RatioPrintln(&ratioc, stdout);
if (
    ratioc._base != 1 ||
    ratioc._numerator != 2 ||
    ratioc._denominator != 3 ||
    !ISEQUALF(RatioToFloat(&ratioc), 1.666666)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "RatioFromFloat NOK");
    PBErrCatch(PBMathErr);
}
ratioc = RatioFromFloat(PBMATH_PI);
printf("PI=");
RatioPrintln(&ratioc, stdout);
if (
    ratioc._base != 3 ||
    ratioc._numerator != 16 ||
    ratioc._denominator != 113 ||
    !ISEQUALF(RatioToFloat(&ratioc), PBMATH_PI)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "RatioFromFloat NOK");
    PBErrCatch(PBMathErr);
}

printf("UnitTestRatio OK\n");
}

void UnitTestLSLR() {

    VecShort2D dim = VecShortCreateStatic2D();
    VecSet(&dim, 0, 2);
    VecSet(&dim, 1, 3);
    MatFloat* mat = MatFloatCreate(&dim);
    VecShort2D i = VecShortCreateStatic2D();
    float v[6] = {1.0, 1.0, 1.0, 1.0, 2.0, 3.0};
    int j = 0;
    do {
        MatSet(mat, &i, v[j]);
        ++j;
    } while(VecStep(&i, &dim));
    LeastSquareLinReg lslr = LeastSquareLinRegCreateStatic(mat);
    VecFloat* Y = VecFloatCreate(3);
    VecSet(Y, 0, 3.0);
    VecSet(Y, 1, 5.0);
    VecSet(Y, 2, 7.0);
    VecFloat* beta = LSLRSolve(&lslr, Y);
    VecFloat* check = VecFloatCreate(2);
    VecSet(check, 0, 1.0);
    VecSet(check, 1, 2.0);
    if (
        VecIsEqual(beta, check) == false ||
        !ISEQUALF(LSLRGetBias(&lslr), 0.0)) {
        PBMathErr->_type = PBErrTypeUnitTestFailed;
        sprintf(PBMathErr->_msg, "LSLRSolve NOK (1)");
        PBErrCatch(PBMathErr);
    }
    VecFree(&beta);
}

```

```

VecSet(Y, 0, 2.75);
VecSet(Y, 1, 5.25);
VecSet(Y, 2, 6.75);
beta = LSLRSolve(&lslr, Y);
VecSet(check, 0, 0.916666);
VecSet(check, 1, 2.0);
if (
    VecIsEqual(beta, check) == false ||
    !ISEQUALF(LSLRGetBias(&lslr), 0.408248)) {
    PBMathErr->_type = PBErrTypeUnitTestFailed;
    sprintf(PBMathErr->_msg, "LSLRSolve NOK (2)");
    PBErrCatch(PBMathErr);
}
VecFree(&beta);
VecFree(&check);
VecFree(&Y);
MatFree(&mat);
LeastSquareLinRegFreeStatic(&lslr);
printf("UnitTestLSLR OK\n");
}

void UnitTestAll() {
    UnitTestVecShort();
    UnitTestVecLong();
    UnitTestVecFloat();
    UnitTestMatFloat();
    UnitTestSysLinEq();
    UnitTestGauss();
    UnitTestSmoother();
    UnitTestBasicFunctions();
    UnitTestRatio();
    UnitTestLSLR();
    printf("UnitTestAll OK\n");
}

int main() {
    UnitTestAll();
    // Return success code
    return 0;
}

```

## 6 Unit tests output

```

{
  "_dim": "5",
  "_val": ["1", "2", "3", "4", "5"]
}
{
  "_dim": "2",
  "_val": ["1", "2"]
}
{
  "_dim": "3",
  "_val": ["1", "2", "3"]
}
{
  "_dim": "4",
  "_val": ["1", "2", "3", "4"]
}

```

```

}
{
  "_dim": "5",
  "_val": ["1", "2", "3", "4", "5"]
}
{
  "_dim": "2",
  "_val": ["1", "2"]
}
{
  "_dim": "3",
  "_val": ["1", "2", "3"]
}
{
  "_dim": "4",
  "_val": ["1", "2", "3", "4"]
}
{
  "_dim": "5",
  "_val": ["1.000000", "2.000000", "3.000000", "4.000000", "5.000000"]
}
{
  "_dim": "2",
  "_val": ["1.000000", "2.000000"]
}
{
  "_dim": "3",
  "_val": ["1.000000", "2.000000", "3.000000"]
}
{
  "_nbRow": "2",
  "_nbCol": "3",
  "_val": ["1.000000", "2.000000", "3.000000", "4.000000", "5.000000", "6.000000"]
}
[0,0,0,0,0]
[0,0]
[0,0,0]
[0,0,0,0]
VecShortCreateFree OK
_VecShortClone OK
_VecShortLoadSave OK
_VecShortGetSetDim OK
UnitTestVecShortStep OK
UnitTestVecShortHamiltonDist OK
UnitTestVecShortIsEqual OK
UnitTestVecShortDotProd OK
UnitTestVecShortCopy OK
VecShort: 0.000054ms, array: 0.000014ms
VecShort2D: 0.000006ms, array: 0.000007ms
VecShort3D: 0.000006ms, array: 0.000006ms
VecShort4D: 0.000007ms, array: 0.000007ms
UnitTestSpeedVecShort OK
[1.000,2.000,3.000,4.000,5.000]
[1.000,2.000]
[1.000,2.000,3.000]
UnitTestVecShortToFloat OK
[1.000,2.000,3.000,4.000,5.000]
[1.000,2.000]
[1.000,2.000,3.000]
UnitTestVecLongToFloat OK
UnitTestVecShortOp OK
UnitTestVecShortShiftStep OK

```

```

UnitTestVecShortGetMinMax OK
UnitTestVecShortHadamardProd OK
UnitTestVecShort OK
[0,0,0,0,0]
[0,0]
[0,0,0]
[0,0,0,0]
VecLongCreateFree OK
_VecLongClone OK
_VecLongLoadSave OK
_VecLongGetSetDim OK
UnitTestVecLongStep OK
UnitTestVecLongHamiltonDist OK
UnitTestVecLongIsEqual OK
UnitTestVecLongDotProd OK
UnitTestVecLongCopy OK
VecLong: 0.000014ms, array: 0.000014ms
VecLong2D: 0.000007ms, array: 0.000006ms
VecLong3D: 0.000006ms, array: 0.000007ms
VecLong4D: 0.000006ms, array: 0.000007ms
UnitTestSpeedVecLong OK
UnitTestVecLongOp OK
UnitTestVecLongShiftStep OK
UnitTestVecLongGetMinMax OK
UnitTestVecLongHadamardProd OK
UnitTestVecLongGetNewDim OK
UnitTestVecLong OK
[0.000,0.000,0.000,0.000,0.000]
[0.000,0.000]
[0.000,0.000,0.000]
VecFloatCreateFree OK
_VecFloatClone OK
_VecFloatLoadSave OK
_VecFloatGetSetDim OK
UnitTestVecFloatCopy OK
UnitTestVecFloatNorm OK
UnitTestVecFloatDist OK
UnitTestVecFloatIsEqual OK
UnitTestVecFloatScale OK
UnitTestVecFloatOp OK
UnitTestVecFloatDotProd OK
UnitTestVecFloatCrossProd OK
[0.707107,0.707107]
UnitTestVecFloatAngleTo OK
[1,2,3,4,5]
[1,2]
[1,2,3]
UnitTestVecFloatToShort OK
UnitTestVecFloatGetMinMax OK
UnitTestVecFloatRotAxis OK
UnitTestVecFloatGetNewDim OK
UnitTestVecFloatHadamardProd OK
VecFloat: 0.000015ms, array: 0.000015ms
VecFloat2D: 0.000006ms, array: 0.000007ms
VecFloat3D: 0.000006ms, array: 0.000006ms
UnitTestSpeedVecFloat OK
UnitTestVecFloat OK
UnitTestMatFloatCreateFree OK
UnitTestMatFloatGetSetDim OK
UnitTestMatFloatCloneIsEqual OK
UnitTestMatFloatLoadSave OK
UnitTestMatFloatInv OK

```

```

UnitTestMatFloatTransposeScale OK
UnitTestMatFloatProdVecFloat OK
UnitTestMatFloatProdMatFloat OK
mat:
[-1.000, -1.000,  1.000
  1.000,  3.000,  3.000
 -1.000, -1.000,  5.000
  1.000,  3.000,  7.000]
Q:
[-0.500, -0.500,  0.500
  0.500, -0.500,  0.500
 -0.500, -0.500, -0.500
  0.500, -0.500, -0.500]
R:
[ 2.000,  4.000,  2.000
 -0.000, -2.000, -8.000
  0.000, -0.000, -4.000]
QR:
[-1.000, -1.000,  1.000
  1.000,  3.000,  3.000
 -1.000, -1.000,  5.000
  1.000,  3.000,  7.000]
UnitTestMatFloatGetQR OK
UnitTestMatFloatProdVecVecTranspose OK
mat:
[ 2.920,  0.860, -1.150
  0.860,  6.510,  3.320
 -1.150,  3.320,  4.570]
Eigen values: [8.999,3.997,1.005]
Eigen vector 1: [0.000,-0.800,-0.600]
Eigen vector 2: [0.800,0.360,-0.480]
Eigen vector 3: [0.600,-0.480,0.640]
UnitTestMatFloatGetEigenValues OK
MatFloat: 0.000003ms, array: 0.000002ms
UnitTestSpeedMatFloat OK
UnitTestMatFloat OK
UnitTestSysLinEq OK
UnitTestGauss OK
UnitTestSmoother OK
UnitTestConv OK
powi OK
average error: 0.000000 < 0.000010, max error: 0.000000 < 0.000100
fastpow OK
fastpow: 0.000013ms, pow: 0.000057ms
speed fastpow OK
fsquare OK
UnitTestConv OK
UnitTestThueMorseSeq OK
UnitTestGetAreaTriangleHero OK
UnitTestGetFibonacciSeq OK
UnitTestGetFibonacciLattice OK
UnitTestGetGCD OK
UnitTestBasicFunctions OK
0+10/6 -> 1+2/3
1.666666=1+2/3
PI=3+16/113
UnitTestRatio OK
UnitTestLSLR OK
UnitTestAll OK

```

## 7 Examples

UnitTestVecShortLoadSave.txt:

```
{
  "_dim": "5",
  "_val": ["1", "2", "3", "4", "5"]
}
{
  "_dim": "2",
  "_val": ["1", "2"]
}
{
  "_dim": "3",
  "_val": ["1", "2", "3"]
}
{
  "_dim": "4",
  "_val": ["1", "2", "3", "4"]
}
```

UnitTestVecLongLoadSave.txt:

```
{
  "_dim": "5",
  "_val": ["1", "2", "3", "4", "5"]
}
{
  "_dim": "2",
  "_val": ["1", "2"]
}
{
  "_dim": "3",
  "_val": ["1", "2", "3"]
}
{
  "_dim": "4",
  "_val": ["1", "2", "3", "4"]
}
```

UnitTestVecFloatLoadSave.txt:

```
{
  "_dim": "5",
  "_val": ["1.000000", "2.000000", "3.000000", "4.000000", "5.000000"]
}
{
  "_dim": "2",
  "_val": ["1.000000", "2.000000"]
}
{
  "_dim": "3",
  "_val": ["1.000000", "2.000000", "3.000000"]
}
```

matfloat.txt:

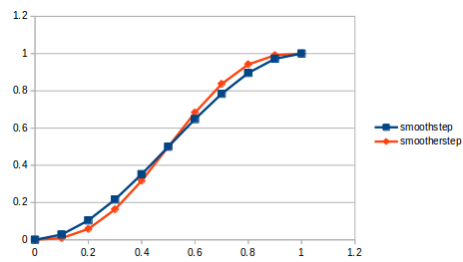


```

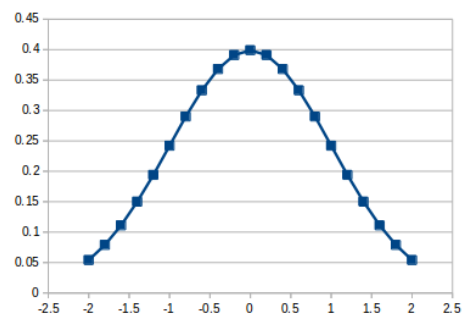
3 2
0.500000 2.000000 0.000000
2.000000 0.000000 1.000000

```

smoother functions:



gauss function (mean:0.0, sigma:1.0):



gauss rand function (mean:1.0, sigma:0.5):

