PixelToPosEstimator

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December 30, 2018

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Introduction

PixelToPosEstimator is a C library providing structures and functions to estimate 3D position from a 2D image.

The problem is as follow: given the 2D image of a set of points laying on a plane seen from a point of view, if we know the 3D position of the point of view and the 3D position and 2D position in the image of at least 3 points on the plane, how to estimate the 3D position of other points from their 2D position in the image.

PixelToPosEstimator provides a solution by using the known points to search the parameters optimizing a model of the projection from the 3D

coordinates to the 2D coordinates, and then uses this optimized model to calculate other points. The optimization is performed using the GenAlg library.

It uses the PBErr, PBMath, GSet, GenAlg libraries.

1 Definitions

The problem consists of finding the function F() such as $\overrightarrow{R_p} = F(\overrightarrow{S_p})$, where $\overrightarrow{R_p}$ is the 3D coordinates of the point p and $\overrightarrow{S_p}$ is the screen coordinates of the point p, shorten below as, respectively, \overrightarrow{R} , \overrightarrow{S} .

Screen coordinates system $(\overrightarrow{0}, \overrightarrow{u}, \overrightarrow{v})$ is as follow: $\overrightarrow{0}$ is at the top-left corner, \overrightarrow{u} is toward the right and \overrightarrow{v} is toward the bottom. Screen dimensions are noted W for width and H for height.

Lets define \overrightarrow{P}_p , the "polar" coordinates of the point p, shorten below as \overrightarrow{P} , as follow:

$$\overrightarrow{P} = \begin{cases} \frac{S_u - 0.5W}{0.5W} \\ \frac{S_v - 0.5H}{0.5H} \\ 0.5H \end{cases}$$
 (1)

The polar coordinates represents the deviation of the point from the center of the screen relatively to the screen dimensions.

Lets now consider the projection of the screen on \mathcal{S} the unit sphere centered on the camera position \overrightarrow{C} . The camera's orthonormal coordinates system is $(\overrightarrow{C}, \overrightarrow{right}, \overrightarrow{up}, \overrightarrow{depth})$ such as \overrightarrow{depth} is colinear to \overrightarrow{CV} , where \overrightarrow{V} is the point of view of the camera.

if we note α and β the angle of view of the camera along respectively \overrightarrow{x} and \overrightarrow{y} , $\overrightarrow{P_S}$ the projection of \overrightarrow{S} on S is calculated as follow:

$$\overrightarrow{P_{S}'} = Rot_{\overrightarrow{up}}(\overrightarrow{depth}, \alpha P_u) + Rot_{\overrightarrow{right}}(\overrightarrow{depth}, \beta P_v) - \overrightarrow{depth}$$
 (2)

$$\overrightarrow{P_S} = \frac{\overrightarrow{P_S'}}{||\overrightarrow{P_S'}||} \tag{3}$$

where $Rot_{\overrightarrow{w}}(\overrightarrow{A}, \theta)$ is the right-handed rotation of \overrightarrow{A} around \overrightarrow{w} by θ (in radians). We remind that the rotation matrix M is equal to (to shorten notation

 θ is not written in the matrix below):

$$M = \begin{bmatrix} \cos + w_x^2 (1 - \cos) & w_x w_y (1 - \cos) - w_z \sin & w_x w_z (1 - \cos) + w_y \sin \\ w_x w_y (1 - \cos) + w_z \sin & \cos + w_y^2 (1 - \cos) & w_y w_z (1 - \cos) - w_x \sin \\ w_x w_z (1 - \cos) - w_y \sin & w_y w_z (1 - \cos) + w_x \sin & \cos + w_z^2 (1 - \cos) \end{bmatrix}$$
(4)

From $\overrightarrow{P_S}$ it is then possible to calculate \overrightarrow{R} as follow: it is the intersection of the line (CP_S) and the plane $(\overrightarrow{x}, \overrightarrow{z})$:

$$\overrightarrow{R} = (\overrightarrow{C} + \gamma \overrightarrow{CP_S})\Big|_{C_y + \gamma(P_{S_y} - C_y) = 0}$$
(5)

which gives us the expression of the searched function F().

However, this function relies on several unknown values:

- ullet \overrightarrow{V} the point of view of the camera
- α and β the angle of view of the camera
- \overrightarrow{up} the up direction in the camera coordinates system. $(\overrightarrow{right}$ is not an unknown as we can calculate it as follow: $\overrightarrow{right} = \overrightarrow{depth} * \overrightarrow{up}$)

Then, given \mathcal{P} the set of points for which we know both the 3D coordinates and 2D coordinates, we approximate these unknown values by solving the minimization problem:

$$\begin{cases}
V_x, V_y, V_z, \alpha, \beta, up_x, up_y, up_z \in \mathbb{R}^8 \\
Min_{(\mathcal{P}, \overrightarrow{V}, \alpha, \beta, \overrightarrow{up})}(\frac{1}{\mathcal{P}^*} \sum_{p \in \mathcal{P}} || \overrightarrow{R_p} - F_{(\overrightarrow{V}, \alpha, \beta, \overrightarrow{up})}(\overrightarrow{S_p})||)
\end{cases}$$
(6)

2 Interface

```
#include "genalg.h"
// ======== Define ========
#define PTPE_Px(that) VecGet(that->_param, 0)
#define PTPE_Py(that) VecGet(that->_param, 1)
#define PTPE_Pz(that) VecGet(that->_param, 2)
#define PTPE_Sx(that) VecGet(that->_param, 3)
#define PTPE_Sy(that) VecGet(that->_param, 4)
#define PTPE_Upx(that) VecGet(that->_param, 5)
#define PTPE_Upy(that) VecGet(that->_param, 6)
#define PTPE_Upz(that) VecGet(that->_param, 7)
#define PTPE_NBPARAM 8
// ----- PixelToPosEstimator
// ====== Data structure =========
typedef struct PixelToPosEstimator {
  // Camera position
  VecFloat3D _cameraPos;
  // Dimension of the image
  VecFloat2D _imgSize;
  // Projection parameters
  // (Px, Py, Pz, Sx, Sy, Upx, Upy, Upz)
  VecFloat* _param;
} PixelToPosEstimator;
// ======= Functions declaration =========
// Create a new PixelToPosEstimator
PixelToPosEstimator PixelToPosEstimatorCreateStatic(
  VecFloat3D* posCamera, const VecFloat2D* const imgSize);
// Free memory used by the PixelToPosEstimator 'that'
void PixelToPosEstimatorFreeStatic(PixelToPosEstimator* that);
// Convert the screen position to a polar position
VecFloat2D PTPEGetPxToPolar(
  const PixelToPosEstimator* const that,
  const VecFloat2D* const screenPos);
// Calculate the projection parameter using genetic algorithm for
// 'nbEpoch' epochs or until the average error gets below 'prec'
// Search for the parameters Px, Py, Pz in the bounding box defined
// by POVmin-POVmax
// the random generator must be initialized before calling this function
void PTPEInit(PixelToPosEstimator* const that,
  \verb|const GSet*| const posMeter|, const GSet*| const posPixel|,
  const unsigned int nbEpoch, const float prec,
  const VecFloat3D* const POVmin, const VecFloat3D* const POVmax);
// Convert the screen position to a real position
VecFloat3D PTPEGetPxToMeter(
  const PixelToPosEstimator* const that,
  const VecFloat2D* const screenPos);
// Convert the polar position to a real position
VecFloat3D PTPEGetPolarToMeter(
  const PixelToPosEstimator* const that,
  const VecFloat2D* const polarPos);
```

3 Code

3.1 pixeltoposestimator.c

```
#include "pixeltoposestimator.h"
// Create a new PixelToPosEstimator
PixelToPosEstimator PixelToPosEstimatorCreateStatic(
  VecFloat3D* posCamera, const VecFloat2D* const imgSize) {
#if BUILDMODE == 0
  if (posCamera == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'posCamera' is null");
    PBErrCatch(PixelToPosEstimatorErr);
  if (imgSize == NULL) {
    PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'imgSize' is null");
    PBErrCatch(PixelToPosEstimatorErr);
#endif
  // Declare the new estimator
  PixelToPosEstimator estimator;
  // Init the estimator
  estimator._cameraPos = *posCamera;
  estimator._imgSize = *imgSize;
  estimator._param = VecFloatCreate(PTPE_NBPARAM);
  // Return the new estimator
  return estimator;
// Free memory used by the PixelToPosEstimator 'that'
void PixelToPosEstimatorFreeStatic(PixelToPosEstimator* const that) {
  if (that == NULL)
    return;
  VecFree(&(that->_param));
// Convert the polar position to a real position
VecFloat3D PTPEGetPolarToMeter(
  const PixelToPosEstimator* const that,
  const VecFloat2D* const polarPos) {
#if BUILDMODE == 0
  if (that == NULL) {
    PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'that' is null");
    PBErrCatch(PixelToPosEstimatorErr);
  if (polarPos == NULL) {
    PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'polarPos' is null");
   PBErrCatch(PixelToPosEstimatorErr);
#endif
  // Declare a variable to memorize the result
```

```
VecFloat3D res = VecFloatCreateStatic3D();
  // Calculate the real coordinates
  // POV
 VecFloat3D P = VecFloatCreateStatic3D();
  VecSet(&P, 0, PTPE_Px(that));
  VecSet(&P, 1, PTPE_Py(that));
  VecSet(&P, 2, PTPE_Pz(that));
  // Normalized vector Camera->POV
  VecFloat3D CP = VecGetOp(&P, 1.0, &(that->_cameraPos), -1.0);
  VecNormalise(&CP);
  // Normalized up vector
  VecFloat3D Up = VecFloatCreateStatic3D();
  VecSet(&Up, 0, PTPE_Upx(that));
  VecSet(&Up, 1, PTPE_Upy(that));
  VecSet(&Up, 2, PTPE_Upz(that));
  VecNormalise(&Up);
  // Normalized right vector
  VecFloat3D Right = VecCrossProd(&CP, &Up);
  VecNormalise(&Right);
  // Rotation according to up and right
  VecFloat3D Rx = CP;
 VecRotAxis(&Rx, &Up, PTPE_Sx(that) * VecGet(polarPos, 0));
  Rx = VecGetOp(&Rx, 1.0, &CP, -1.0);
  VecFloat3D Ry = CP;
 VecRotAxis(&Ry, &Right, PTPE_Sy(that) * VecGet(polarPos, 1));
  Ry = VecGetOp(&Ry, 1.0, &CP, -1.0);
  // 3d vector from camera corresponding to the polar pos pixel
  VecFloat3D V = VecGetOp(&CP, 1.0, &Rx, 1.0);
  V = VecGetOp(\&V, 1.0, \&Ry, 1.0);
 VecNormalise(&V);
  // Projection to ground plane
 float a = VecGet(&(that->_cameraPos), 1) / VecGet(&V, 1);
  VecSet(&res, 0, VecGet(&(that->_cameraPos), 0) - a * VecGet(&V, 0));
  VecSet(&res, 1, 0.0);
  VecSet(&res, 2, VecGet(&(that->_cameraPos), 2) - a * VecGet(&V, 2));
  // Return the result
 return res;
// Convert the screen position to a polar position
VecFloat2D PTPEGetPxToPolar(
 const PixelToPosEstimator* const that,
 const VecFloat2D* const screenPos) {
#if BUILDMODE == 0
 if (that == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'that' is null");
   PBErrCatch(PixelToPosEstimatorErr);
 if (screenPos == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'screenPos' is null");
   PBErrCatch(PixelToPosEstimatorErr);
 }
#endif
  // Declare a variable to memorize the result
  VecFloat2D res = VecFloatCreateStatic2D();
  // Calculate the polar coordinates
 float w = VecGet(&(that->_imgSize), 0);
 VecSet(&res, 0, (VecGet(screenPos, 0) - 0.5 * w) / (0.5 * w));
```

```
float h = VecGet(&(that->_imgSize), 1);
 VecSet(\&res, 1, (VecGet(screenPos, 1) - 0.5 * h) / (0.5 * h));
  // Return the result
 return res;
// Calculate the projection parameter using genetic algorithm for
// 'nbEpoch' epochs or until the average error gets below 'prec'
// Search for the parameters Px, Py, Pz in the bounding box defined
// by POVmin-POVmax
// the random generator must be initialized before calling this function
void PTPEInit(PixelToPosEstimator* const that,
  const GSet* const posMeter, const GSet* const posPixel,
 const unsigned int nbEpoch, const float prec,
 const VecFloat3D* const POVmin, const VecFloat3D* const POVmax) {
#if BUILDMODE == 0
 if (that == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'that' is null");
   PBErrCatch(PixelToPosEstimatorErr);
  if (posMeter == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'posMeter' is null");
   PBErrCatch(PixelToPosEstimatorErr);
  if (posPixel == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'posPixel' is null");
   PBErrCatch(PixelToPosEstimatorErr);
  if (GSetNbElem(posPixel) != GSetNbElem(posMeter)) {
   PixelToPosEstimatorErr->_type = PBErrTypeInvalidArg;
    sprintf(PixelToPosEstimatorErr->_msg,
      "'posPixel' and 'posMeter' don't have same sizes (%ld==%ld)",
      GSetNbElem(posPixel), GSetNbElem(posMeter));
   PBErrCatch(PixelToPosEstimatorErr);
  if (GSetNbElem(posPixel) <= 2) {</pre>
    PixelToPosEstimatorErr->_type = PBErrTypeInvalidArg;
    sprintf(PixelToPosEstimatorErr->_msg,
      "'posPixel' and 'posMeter' don't have enough elements (%1d>2)",
      GSetNbElem(posPixel));
   PBErrCatch(PixelToPosEstimatorErr);
  if (POVmin == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'POVmin' is null");
   PBErrCatch(PixelToPosEstimatorErr);
  if (POVmax == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'POVmax' is null");
   PBErrCatch(PixelToPosEstimatorErr);
 }
#endif
  // Create the GenAlg
  int lengthAdnF = PTPE_NBPARAM;
  int lengthAdnI = 0;
 GenAlg* ga = GenAlgCreate(GENALG_NBENTITIES, GENALG_NBELITES,
   lengthAdnF, lengthAdnI);
  // Set the boundaries for the parameters
```

```
VecFloat2D boundsF = VecFloatCreateStatic2D();
VecSet(&boundsF, 0, VecGet(POVmin, 0));
VecSet(&boundsF, 1, VecGet(POVmax, 0));
GASetBoundsAdnFloat(ga, 0, &boundsF); // Px
VecSet(&boundsF, 0, VecGet(POVmin, 1));
VecSet(&boundsF, 1, VecGet(POVmax, 1));
GASetBoundsAdnFloat(ga, 1, &boundsF); // Py
VecSet(&boundsF, 0, VecGet(POVmin, 2));
VecSet(&boundsF, 1, VecGet(POVmax, 2));
GASetBoundsAdnFloat(ga, 2, &boundsF); // Pz
VecSet(&boundsF, 0, -PBMATH_HALFPI);
VecSet(&boundsF, 1, PBMATH_HALFPI);
GASetBoundsAdnFloat(ga, 3, &boundsF); // Sx
GASetBoundsAdnFloat(ga, 4, &boundsF); // Sy
VecSet(&boundsF, 0, -1.0); VecSet(&boundsF, 1, 1.0);
GASetBoundsAdnFloat(ga, 5, &boundsF); // Upx
VecSet(&boundsF, 0, 0.0); VecSet(&boundsF, 1, 1.0);
GASetBoundsAdnFloat(ga, 6, &boundsF); // Upy
VecSet(&boundsF, 0, -1.0); VecSet(&boundsF, 1, 1.0);
GASetBoundsAdnFloat(ga, 7, &boundsF); // Upz
// Init the GenAlg
GAInit(ga);
// Variable to memorize the current best adn value
float best = 10000.0;
// Loop on epochs
do {
 //printf("epoch %ld avg err %fm
                                      \r".
 // GAGetCurEpoch(ga), best / (float)GSetNbElem(posMeter));
 //fflush(stdout):
 // Variable to memorize the evaluation of one base
 float ev = 0.0;
 // Loop on adns
 for (int iEnt = 0; iEnt < GAGetNbAdns(ga); ++iEnt) {</pre>
    // Copy the adn into the estimator's parameters
   VecCopy(that->_param, GAAdnAdnF(GAAdn(ga, iEnt)));
   // Reset the evaluation variable
   ev = 0.0:
    // Loop on both sets
   GSetIterForward iterMeter = GSetIterForwardCreateStatic(posMeter);
   GSetIterForward iterPixel = GSetIterForwardCreateStatic(posPixel);
   do {
     \ensuremath{//} Get the screen position
      VecFloat2D* pPixel = GSetIterGet(&iterPixel);
      // Convert to polar position
     VecFloat2D polarPos = PTPEGetPxToPolar(that, pPixel);
      // Convert to real position
     VecFloat3D pEstim = PTPEGetPolarToMeter(that, &polarPos);
      // Get the correct real position
      VecFloat3D* pMeter = GSetIterGet(&iterMeter);
      // Calculate the error
      ev += VecDist(pMeter, &pEstim);
   } while (GSetIterStep(&iterMeter) && GSetIterStep(&iterPixel));
    // Calculate the average error
   ev /= (float)GSetNbElem(posMeter);
   // Update the value of this adn
   GASetAdnValue(ga, GAAdn(ga, iEnt), -1.0 * ev);
    // Update the best value if necessary
    if (ev < best - PBMATH_EPSILON) {</pre>
      best = ev;
      printf("%lu %f ", GAGetCurEpoch(ga), best);
      VecFloatPrint(that->_param, stdout, 6);
     printf("
                      \n"); fflush(stdout);
```

```
}
    // Step the GenAlg
   GAStep(ga);
  } while (GAGetCurEpoch(ga) < nbEpoch && best > prec);
  // Copy the final best adn into the estimator's parameters
 VecCopy(that->_param, GAAdnAdnF(GABestAdn(ga)));
  // Free memory
 GenAlgFree(&ga);
// Convert the screen position to a real position
VecFloat3D PTPEGetPxToMeter(
 const PixelToPosEstimator* const that,
 const VecFloat2D* const screenPos) {
#if BUILDMODE == 0
 if (that == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'that' is null");
   PBErrCatch(PixelToPosEstimatorErr);
 if (screenPos == NULL) {
   PixelToPosEstimatorErr->_type = PBErrTypeNullPointer;
    sprintf(PixelToPosEstimatorErr->_msg, "'screenPos' is null");
   PBErrCatch(PixelToPosEstimatorErr);
#endif
  // Declare a variable to memorize the result
 VecFloat3D res = VecFloatCreateStatic3D();
 // Calculate the real coordinates
 VecFloat2D polarPos = PTPEGetPxToPolar(that, screenPos);
 res = PTPEGetPolarToMeter(that, &polarPos);
 // Return the result
 return res;
```

4 Makefile

\$(\$(repo)_EXENAME).o \

```
# Build mode
# 0: development (max safety, no optimisation)
# 1: release (min safety, optimisation)
# 2: fast and furious (no safety, optimisation)
BUILD_MODE?=1
all: pbmake_wget main ground.png
# Automatic installation of the repository PBMake in the parent folder
pbmake_wget:
if [ ! -d ../PBMake ]; then wget https://github.com/BayashiPascal/PBMake/archive/master.zip; unzip master.zip; rm -f
# Makefile definitions
MAKEFILE_INC=../PBMake/Makefile.inc
include $(MAKEFILE_INC)
# Rules to make the executable
repo=pixeltoposestimator
$($(repo)_EXENAME): \
```

```
$($(repo)_EXE_DEP) \
$($(repo)_DEP)
$(COMPILER) 'echo "$($(repo)_EXE_DEP) $($(repo)_EXENAME).o" | tr ' ' '\n' | sort -u' $(LINK_ARG) $($(repo)_LINK_ARG)
$($(repo)_EXENAME).o: \
$($(repo)_DIR)/$($(repo)_EXENAME).c \
$($(repo)_INC_H_EXE) \
$($(repo)_EXE_DEP)
$(COMPILER) $(BUILD_ARG) $($(repo)_BUILD_ARG) 'echo "$($(repo)_INC_DIR)" | tr ' ' '\n' | sort -u' -c $($(repo)_DIR)/S(S(Repo)_DIR)/S(S(Repo)_BUILD_ARG))
$ground.png: ground.pov
povray -W1280 -H720 -P -Q9 +A -Iground.pov
```

5 Example

5.1 Test case

```
#include "colors.inc"
#include "textures.inc"
\verb|background| \{
color White
#declare CameraPos = <0, 15, 0>;
#declare POV = <50, 0, 50>;
camera {
location CameraPos
look_at POV
  ир у
 right x * 1280 / 720
}
light_source {
CameraPos
White
}
plane {
  y, 0
  texture {
    pigment { color rgb 0.9 }
    finish { ambient 0.9 }
}
sphere {
  <48,0,51>
  .2
 pigment { color Black }
sphere {
  <12,0,28>
  .2
 pigment { color Black }
sphere {
  <33,0,11>
```

```
pigment { color Black }
sphere {
  <22,0,62>
  .2
pigment { color Black }
}
sphere {
  <18,0,25>
  .2
 pigment { color Red }
torus {
  1.02698, .1
  translate <18,0,25>
 pigment { color Red }
sphere {
  <35,0,30>
  .2
 pigment { color Red }
torus {
  1.601299, .1
  translate <35,0,30>
pigment { color Red }
```

In the image below, the four input positions are in black, and the 2 test positions are in red. The red circles show the error range of the estimation.:



5.2 main.c

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
#include <tgmath.h>
#include "pixeltoposestimator.h"
```

```
int main(int argc, char** argv) {
  (void)argc; (void)argv;
  srandom(time(NULL));
  // Read the data from the file in argument
  if (argc != 2) {
    fprintf(stderr, "Usage: main <input file>\n");
   exit(0);
 FILE* inputFile = fopen(argv[1], "r");
  if (inputFile == NULL) {
    fprintf(stderr, "Can't open %s\n", argv[0]);\\
   exit(0);
 VecFloat* posCamera = NULL;
 VecFloat* imgSize = NULL;
 VecLoad(&posCamera, inputFile);
  VecLoad(&imgSize, inputFile);
 VecFloat* POVmin = NULL;
  VecFloat* POVmax = NULL;
 VecLoad(&POVmin, inputFile);
VecLoad(&POVmax, inputFile);
  int nbInput = 0;
  int ret = fscanf(inputFile, "%d", &nbInput);
  GSet inputMeter = GSetCreateStatic();
  GSet inputPixel = GSetCreateStatic();
  for (int iInput = 0; iInput < nbInput; ++iInput) {</pre>
   VecFloat* posMeter = NULL;
    VecFloat* posPixel = NULL;
    VecLoad(&posMeter, inputFile);
    VecLoad(&posPixel, inputFile);
    GSetAppend(&inputMeter, posMeter);
   GSetAppend(&inputPixel, posPixel);
 int nbTest = 0;
 ret = fscanf(inputFile, "%d", &nbTest);
  (void)ret;
  GSet testMeter = GSetCreateStatic();
  GSet testPixel = GSetCreateStatic();
  for (int iInput = 0; iInput < nbTest; ++iInput) {</pre>
   VecFloat* posMeter = NULL;
    VecFloat* posPixel = NULL;
   VecLoad(&posMeter, inputFile);
VecLoad(&posPixel, inputFile);
    GSetAppend(&testMeter, posMeter);
   GSetAppend(&testPixel, posPixel);
 fclose(inputFile);
  // Create the estimator
 PixelToPosEstimator estimator = PixelToPosEstimatorCreateStatic(
    (VecFloat3D*)posCamera, (VecFloat2D*)imgSize);
  // Calculate the projection parameters
 FILE* fileParam = fopen("./param.txt", "r");
  if (fileParam == NULL) {
    printf("Calculate \ the \ projection \ param... \n");
    unsigned int nbEpoch = 500000;
    float prec = 0.001;
   PTPEInit(&estimator, &inputMeter, &inputPixel,
      nbEpoch, prec, (VecFloat3D*)POVmin, (VecFloat3D*)POVmax);
```

```
fileParam = fopen("./param.txt", "w");
  if (!VecSave(estimator._param, fileParam, true)) {
    fprintf(stderr, "Failed to save the parameters\n");
    exit(0);
} else {
  printf("Reuse the projection param...\n");
  if (!VecLoad(&(estimator._param), fileParam)) {
    fprintf(stderr, "Failed to load the parameters\n");
    exit(0);
  }
}
fclose(fileParam);
printf("\n");
printf("Projection param: ");
VecPrint(estimator._param, stdout);printf("\n");
printf("\n");
printf("Input data:\n\n");
float avgErr = 0.0;
float maxErr = 0.0;
for (int iInput = 0; iInput < nbInput; ++iInput) {</pre>
  VecFloat3D* posMeter = (VecFloat3D*)GSetGet(&inputMeter, iInput);
  VecFloat2D* posPixel = (VecFloat2D*)GSetGet(&inputPixel, iInput);
  printf("input #%d (m): ", iInput);
  VecPrint(posMeter, stdout);
  printf(" (px): ");
  VecPrint(posPixel, stdout);
  printf("\n");
  printf(" (screen->real): ");
  VecFloat3D estimPos = PTPEGetPxToMeter(&estimator, posPixel);
  VecPrint(&estimPos, stdout);
  float error = VecDist(&estimPos, posMeter);
  printf(" (error): %fm", error);
  printf("\n\n");
  avgErr += error;
  if (maxErr < error)</pre>
    maxErr = error;
avgErr /= (float)nbInput;
\label{lem:printf("Average error: $$fm\n$", avgErr);}
printf("Max error: %fm\n\n", maxErr);
printf("Test data:\n\n");
avgErr = 0.0;
maxErr = 0.0;
for (int iInput = 0; iInput < nbTest; ++iInput) {</pre>
  VecFloat3D* posMeter = (VecFloat3D*)GSetGet(&testMeter, iInput);
  VecFloat2D* posPixel = (VecFloat2D*)GSetGet(&testPixel, iInput);
  printf("input #%d (m): ", iInput);
  VecPrint(posMeter, stdout);
  printf(" (px): ");
  VecPrint(posPixel, stdout);
  printf("\n");
  printf(" (screen->real): ");
  VecFloat3D estimPos = PTPEGetPxToMeter(&estimator, posPixel);
  VecPrint(&estimPos, stdout);
  float error = VecDist(&estimPos, posMeter);
  printf(" (error): %fm", error);
printf("\n\n");
  avgErr += error;
```

```
if (maxErr < error)</pre>
      maxErr = error;
  avgErr /= (float)nbTest;
  printf("Average error: %fm\n", avgErr);
  printf("Max error: %fm\n", maxErr);
  // Free memory
  PixelToPosEstimatorFreeStatic(&estimator);
  while (GSetNbElem(&inputMeter) > 0) {
    VecFloat* v = GSetPop(&inputMeter);
    VecFree(&v);
  while (GSetNbElem(&inputPixel) > 0) {
    VecFloat* v = GSetPop(&inputPixel);
    VecFree(&v);
  while (GSetNbElem(&testMeter) > 0) {
    VecFloat* v = GSetPop(&testMeter);
    VecFree(&v);
  while (GSetNbElem(&testPixel) > 0) {
    VecFloat* v = GSetPop(&testPixel);
    VecFree(&v);
  // Return success code
 return 0;
    inputTest.txt:
  "_dim":"3",
  _val":["0.0","10.0","0.0"]
  "_dim":"2",
  "_val":["1280.000000","720.000000"]
  "_dim":"3",
  "_val":["0.0","0.0","0.0"]
  "_dim":"3",
  "_val":["10.0","15.0","10.0"]
}
  "_dim":"3",
  "_val":["48.000000","0.000000","51.000000"]
}
  "_dim":"2",
  "_val":["618.000000","361.000000"]
  "_dim":"3",
  "_val":["12.000000","0.000000","28.000000"]
```

```
"_dim":"2",
  "_val":["375.000000","565.000000"]
  "_dim":"3",
  "_val":["33.000000","0.000000","11.000000"]
}
  "_dim":"2",
  "_val":["974.000000","536000000"]
}
  "_dim":"3",
  "_val":["22.000000","0.000000","62.000000"]
  "_dim":"2",
  "_val":["307.000000","387.000000"]
}
2
{
  "_dim":"3",
  "_val":["18.000000","0.000000","25.000000"]
  "_dim":"2",
  "_val":["531.000000","543.000000"]
  "_dim":"3",
  "_val":["35.000000","0.000000","30.000000"]
}
  "_dim":"2",
  "_val":["692.000000","436.000000"]
```

6 Output

```
Calculate the projection param...
0 44.884600 <6.281383,2.544475,4.045629,-0.810402,-1.440463,-0.251248,0.821694,0.853980>
0 44.406651 <3.035180,6.493492,8.269773,-0.487826,0.523906,0.314290,0.622056,0.278442>
0 39.926086 <5.686362,4.805532,4.719906,-0.361895,-1.535800,-0.391348,0.965750,-0.972703>
0 28.386356 < 9.420714,8.037761,8.992093,0.081077,-1.201721,0.260587,0.531561,0.954478>
1 23.291659 <8.907933,8.036860,7.472357,-0.261465,0.341481,-0.964939,0.036744,-0.757546>
1 23.157566 <9.765271,8.092203,8.723720,-0.329725,-0.585552,0.446517,0.302049,-0.367535>
1 18.792313 <9.818071,8.036860,7.472357,1.318501,-0.356141,0.260587,0.531561,0.495598>
2 18.077366 < 9.765271,8.092203,8.738153,0.081077,-0.585552,0.446517,0.531561,-0.376360>
3 17.387600 <3.472870,8.037761,8.994494,-0.157184,-0.585552,-0.469345,0.531561,0.954478>
3 15.448114 < 9.420714, 8.092203, 8.723720, 0.084058, -0.891022, 0.260587, 0.531561, -0.376360>
4 14.997634 <8.924720,8.092203,8.723720,0.084058,-0.782852,0.260587,0.342059,-0.367535>
4 12.908067 < 9.818071, 8.036860, 9.793681, 1.318501, -0.356141, 0.260587, 0.402870, 0.495598>
7 8.401557 <9.818071,8.036860,9.793681,1.188305,-0.356141,0.345925,0.402870,0.495598>
12 7.753658 < 9.420714,8.092203,9.730992,0.775250,-0.891022,0.533777,0.911558,0.495598>
13 7.675824 <9.420714,8.092203,9.781833,0.707945,-0.524464,0.406542,0.770881,0.511776>
13 7.159789 <8.924720,8.036860,9.793681,1.044841,-0.524464,0.315572,0.770881,0.495598>
13 6.693418 < 9.439643, 8.092203, 9.730992, 0.775250, -0.524464, 0.446517, 0.855537, 0.495598>
```

```
14 6.400322 < 9.420714,8.092203,8.480831,1.111742,-0.524464,0.406542,0.770881,0.511776>
15 4.594604 <9.818071,8.092203,9.730992,1.184015,-0.524464,0.345925,0.402870,0.495598>
20 3.776099 < 9.420714, 8.092203, 9.793681, 1.184015, -0.524464, 0.345925, 0.484037, 0.495598>
24 3.525790 < 9.420714, 8.092203, 9.628260, 1.184015, -0.524464, 0.345925, 0.484037, 0.495598>
30 3.258011 < 9.604491, 8.092203, 9.866126, 1.111742, -0.524464, 0.406542, 0.573255, 0.582437 >
32 3.117882 <9.937201,8.092203,9.919612,1.111742,-0.524464,0.345925,0.573255,0.495598>
34 3.117851 <9.937201,8.092203,9.919612,1.111742,-0.524464,0.406542,0.646383,0.582437>
35 2.938462 <9.937201,8.092203,9.919612,1.184015,-0.524464,0.406542,0.560358,0.582437>
48 2.818095 < 9.681943, 8.092203, 9.972069, 1.142336, -0.524464, 0.406542, 0.561197, 0.582437
55 2.797715 <9.604491,8.092203,9.919612,1.142336,-0.524464,0.406542,0.540557,0.582437>
58 2.720654 <9.681943,8.092203,9.919612,1.142336,-0.524464,0.404598,0.573356,0.582437>
82 2.701498 < 9.777955, 8.092203, 9.972069, 1.136984, -0.524464, 0.406542, 0.557293, 0.582437>
102 2.476554 < 9.621267,8.092203,9.919612,1.142336,-0.415372,0.406542,0.534199,0.582437>
107 2.222970 < 9.621267,8.092203,9.919612,1.142336,-0.415372,0.406542,0.534199,0.606424>
111 2.177721 <9.777955,8.092203,9.955930,1.136984,-0.415372,0.406542,0.482520,0.582437>
113 2.126257 <9.785274,8.092203,9.919612,1.142336,-0.415372,0.406542,0.561197,0.587305>
113 2.050461 < 9.621267, 8.092203, 9.919612, 1.142336, -0.415372, 0.406542, 0.586852, 0.606424>
114 1.925390 < 9.777955, 8.092203, 9.919612, 1.136984, -0.415372, 0.406542, 0.612972, 0.606424>
142 1.905300 < 9.621267,8.092203,9.897383,1.120821,-0.415372,0.406542,0.586852,0.606424>
148 1.839559 < 9.777955, 8.092203, 9.955930, 1.136984, -0.415372, 0.406542, 0.597292, 0.606424>
149 1.818513 < 9.689944,8.092203,9.955930,1.103658,-0.415372,0.406542,0.618273,0.606424>
170 1.786256 < 9.763318, 8.092203, 9.955930, 1.128148, -0.415372, 0.406542, 0.607047, 0.606424>
182 1.580445 < 9.777955, 8.092203, 9.919612, 1.136984, -0.314057, 0.406542, 0.553064, 0.606424>
183 1.538658 < 9.915060, 8.092203, 9.955930, 1.120821, -0.314057, 0.406542, 0.612972, 0.606424>
187 1.400943 < 9.787211,8.083845,9.897383,1.125060,-0.314057,0.406542,0.566475,0.606424>
189 1.336716 < 9.584694,8.092203,9.890512,1.125060,-0.314057,0.406542,0.597292,0.620857>
191 1.195886 < 9.645562,8.092203,9.897383,1.098414,-0.314057,0.406542,0.599253,0.606424>
192 1.078981 < 9.631684,8.092203,9.890512,1.103517,-0.314057,0.406542,0.597292,0.620857>
195 1.026388 < 9.631684,8.092203,9.943486,1.103517,-0.314057,0.406542,0.600996,0.620857>
200 1.006481 < 9.606969, 8.092203, 9.890512, 1.098414, -0.314057, 0.406542, 0.600996, 0.620857 >
204 0.923881 < 9.748018,8.092203,9.897383,1.103517,-0.314057,0.406542,0.638712,0.620857>
216 0.922173 < 9.652600, 8.092203, 9.888913, 1.098414, -0.314057, 0.406542, 0.619672, 0.620857>
222 0.763326 < 9.713642,8.092203,9.943486,1.076891,-0.314057,0.406542,0.648829,0.620857>
244 0.756738 < 9.675240,8.092203,9.888913,1.076891,-0.314057,0.406542,0.665544,0.620857>
252 0.751913 <9.695823,8.092203,9.897383,1.076891,-0.314057,0.406542,0.668927,0.620857>
270 0.751425 < 9.742764,8.092203,9.897383,1.076891,-0.314057,0.406542,0.674066,0.620857>
273 0.746165 < 9.695823,8.092203,9.897383,1.076891,-0.314057,0.406542,0.667074,0.620857>
285 0.739344 < 9.752088, 8.092203, 9.923166, 1.076891, -0.314057, 0.406542, 0.667074, 0.620857 >
296 0.731872 <9.773252,8.092203,9.923166,1.076891,-0.314057,0.406542,0.673085,0.620857>
339 0.730829 <9.817637,8.092203,9.923166,1.076891,-0.314057,0.406542,0.684769,0.620857>
361 0.721335 < 9.784201,8.092203,9.923166,1.076891,-0.314057,0.406542,0.679696,0.620857>
370 0.721078 < 9.784201,8.092203,9.923166,1.076891,-0.314057,0.406542,0.679010,0.620857>
460 0.720938 < 9.792299, 8.092203, 9.923930, 1.076891, -0.314057, 0.406542, 0.681922, 0.620857>
491 0.718458 < 9.792299, 8.092203, 9.923166, 1.076014, -0.314057, 0.406542, 0.681922, 0.620857>
539 0.713503 <9.786608,8.092203,9.923166,1.076891,-0.314057,0.406542,0.681922,0.621290>
604 0.712912 <9.792295,8.094030,9.923166,1.076014,-0.314057,0.406542,0.685137,0.621910>
736 0.712580 <9.769989,8.094030,9.923166,1.076014,-0.314057,0.406542,0.681122,0.621910>
1248 0.712495 <4.848133,9.036037,4.851320,0.864740,-0.336921,0.284323,0.975625,0.379136>
1249 0.643722 <4.848133,9.036037,4.862695,0.864740,-0.336921,0.284323,0.985079,0.373942>
1252 0.607572 <4.848133,9.036037,4.862695,0.864740,-0.336921,0.284323,0.994658,0.379136>
1258 0.600365 <4.848133,9.036037,4.862695,0.864740,-0.336921,0.284323,0.996807,0.379136>
1277 0.586545 <4.819316,9.036037,4.851320,0.868794,-0.336921,0.284323,0.999060,0.379136>
1295 0.586414 <4.819316,9.036037,4.851320,0.868794,-0.336921,0.284323,0.999099,0.379136>
1325 0.586258 <4.819316,9.036037,4.851320,0.868794,-0.336921,0.284323,0.999146,0.379136>
1363 0.577828 <4.844653,9.036037,4.866961,0.868794,-0.336921,0.284323,0.999060,0.379136>
1409 0.576681 <4.848133,9.036037,4.862695,0.868794,-0.336921,0.282206,0.998863,0.379136>
1452 0.565243 <4.844776,9.036037,4.862695,0.870687,-0.336921,0.282206,0.998863,0.379136>
1616 0.555914 <4.824059,9.036037,4.862695,0.868794,-0.336921,0.282206,0.999713,0.379136>
1793 0.555356 <4.831511,9.036037,4.862695,0.872947,-0.336921,0.282206,0.999713,0.379136>
1957 0.546738 <4.826589,9.036037,4.871719,0.870251,-0.336921,0.281504,0.999467,0.379136>
2126 0.533117 <4.830008,9.036037,4.862695,0.870251,-0.336921,0.279149,0.998679,0.376354>
2220 0.520408 <4.830008,9.036037,4.862695,0.870251,-0.336921,0.279149,0.999713,0.372581>
```

```
2259 0.519050 <4.845685,9.036037,4.871719,0.870251,-0.336921,0.279149,0.999467,0.373728>
2301 0.497474 <4.830008,9.036037,4.862695,0.870251,-0.336921,0.277030,0.999165,0.372581>
2419 0.494836 <4.819316,9.036037,4.862695,0.870843,-0.336921,0.277030,0.999165,0.372581>
2478 0.486439 <4.830008,9.036037,4.876121,0.870251,-0.336921,0.276127,0.999684,0.372581>
2583 0.478788 <4.845685,9.036037,4.862695,0.870251,-0.336921,0.273472,0.999467,0.368140>
2699 0.457038 <4.830290,9.036037,4.869759,0.870251,-0.336921,0.273472,0.997686,0.368140>
2784 0.456981 <4.830008,9.036037,4.862695,0.870251,-0.336921,0.273472,0.998643,0.365178>
2828 0.453112 <4.835212,9.036037,4.873294,0.870251,-0.336921,0.273472,0.999467,0.368140>
3318 0.433551 <8.511834,8.307278,8.570730,0.868274,-0.336921,0.268581,0.998242,0.363261>
3386 0.431667 <8.518552,8.307278,8.570730,0.869201,-0.336921,0.269664,0.999644,0.363261>
3394 0.426953 <8.495723,8.307278,8.558190,0.875499,-0.336921,0.268581,0.998242,0.363261>
3493 0.422279 <8.478710,8.307278,8.556923,0.874170,-0.336921,0.268581,0.999644,0.363261>
3500 0.420096 <8.467314,8.307278,8.570730,0.868274,-0.336921,0.268581,0.999735,0.363261>
3533 0.410834 <8.474053,8.307278,8.570730,0.869201,-0.336921,0.268581,0.999735,0.363261>
3567 0.405540 <8.489199,8.307278,8.570730,0.870533,-0.336921,0.268581,0.999644,0.363261>
3583 0.402555 <8.489199,8.307278,8.566431,0.870533,-0.336921,0.268581,0.999644,0.363261>
3667 0.401827 <8.478710,8.307278,8.570730,0.870533,-0.336921,0.267957,0.999447,0.363261>
3780 0.399194 <8.476549,8.307278,8.559493,0.870533,-0.336921,0.268581,0.999735,0.362369>
3887 0.396914 <8.476549,8.307278,8.551306,0.870533,-0.336921,0.268581,0.999735,0.362369>
4071 0.395418 <8.465826,8.307278,8.559493,0.870533,-0.336921,0.267957,0.999735,0.362369>
5327 0.391432 <8.479677,8.307278,8.560559,0.870533,-0.336921,0.267957,0.999532,0.361755>
5588 0.390964 <8.470735,8.307278,8.551970,0.870533,-0.336921,0.257371,0.960051,0.346775>
5594 0.372444 <8.498499,8.307278,8.565677,0.870533,-0.336921,0.257371,0.976702,0.346775>
5596 0.370464 <8.498499,8.307278,8.561835,0.870533,-0.336921,0.257371,0.987405,0.346775>
5598 0.367464 <8.498499,8.307278,8.557663,0.870533,-0.336921,0.257371,0.976333,0.346775>
5713 0.367187 <8.498499,8.307278,8.560231,0.870533,-0.336921,0.257371,0.977701,0.346775>
5756 0.366584 <8.503640,8.307278,8.561835,0.870533,-0.336921,0.257371,0.978313,0.346775>
6702 0.343021 <8.503640,8.307428,8.561835,0.865406,-0.327725,0.257371,0.987266,0.348621>
6729\ 0.337664\ < 8.503640, 8.307428, 8.561835, 0.870010, -0.327725, 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.346775 > 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.257371, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.991874, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0.99184, 0
6740 0.335527 <8.503640,8.307428,8.561835,0.870010,-0.327725,0.257371,0.992819,0.346775>
6756 0.329242 <8.503640,8.307428,8.561835,0.870010,-0.327725,0.257371,0.995828,0.346775>
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78127 0.151612 <9.118387,8.172626,9.122255,0.846486,-0.322978,0.128713,0.951663,0.145199>
78147 0.150881 < 9.118387,8.172626,9.127856,0.846486,-0.322978,0.128713,0.960791,0.145199>
78218 0.150298 < 9.118087,8.172626,9.132977,0.846486,-0.322978,0.128713,0.964069,0.145199>
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479597 0.139459 <8.662298,8.266581,8.675541,0.847986,-0.323168,0.143216,0.937165,0.170057>
479749 0.139438 <8.662896,8.266581,8.675541,0.848307,-0.323168,0.143216,0.938612,0.170057>
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482941 0.139231 <8.661727,8.266581,8.676446,0.849234,-0.323168,0.143216,0.943283,0.170057> 483012 0.139086 <8.661727,8.266581,8.676446,0.848192,-0.323168,0.143216,0.938335,0.170057> 483026 0.138948 <8.661727,8.266581,8.676446,0.849234,-0.323168,0.143216,0.942328,0.170057> 483043 0.138932 <8.661727,8.266581,8.676446,0.849234,-0.323168,0.143216,0.942132,0.170057> Projection param: <8.662,8.267,8.676,0.849,-0.323,0.143,0.942,0.170> Input data:
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input #0 (m): <48.000,0.000,51.000> (px): <618.000,361.000>
 (screen->real): <48.006,0.000,50.996> (error): 0.007018m

input #1 (m): <12.000,0.000,28.000> (px): <375.000,565.000>
 (screen->real): <12.419,0.000,27.869> (error): 0.439199m

input #2 (m): <33.000,0.000,11.000> (px): <974.000,536000000.000>
 (screen->real): <32.997,0.000,11.014> (error): 0.014749m

input #3 (m): <22.000,0.000,62.000> (px): <307.000,387.000>
 (screen->real): <21.908,0.000,62.022> (error): 0.094740m

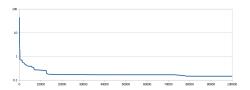
Average error: 0.138927m Max error: 0.439199m

Test data:

input #0 (m): <18.000,0.000,25.000> (px): <531.000,543.000>
 (screen->real): <18.882,0.000,25.527> (error): 1.026980m

input #1 (m): <35.000,0.000,30.000> (px): <692.000,436.000>
 (screen->real): <36.008,0.000,31.244> (error): 1.601299m

Average error: 1.314115m Max error: 1.601299m



param.txt:

{"_dim": "8", "_val": ["8.661727", "8.266581", "8.676446", "0.849234", "-0.323168", "0.143216", "0.941986", "0.170057"]}