# Shapoid

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## Introduction

Shapoid is a C library providing the Shapoid structure and its functions which can be used to manipulate Shapoid objects (see next section for details).

It also provides the ShapoidIter structure and its functions which can be used to sequantially loop through the surface/volume/... of a Shapoid.

It uses the PBErr, PBMath and GSet libraries.

### 1 Definitions

A Shapoid is a geometry defined by its dimension  $D \in \mathbb{N}_{+}^{*}$  equals to the number of dimensions of the space it exists in, its position  $\overrightarrow{P}$ , and its axis  $(\overrightarrow{A_0}, \overrightarrow{A_1}, ..., \overrightarrow{A_{D-1}})$ .  $A_i$  and P are vectors of dimension D. In what follows I'll use I as notation for the interval [0, D-1] for simplification.

Shapoids are classified in three groups: Facoid, Pyramidoid and Spheroid. The volume of a Shapoid is defined by, for a Facoid:

$$\left\{ \sum_{i \in I} v_i \overrightarrow{A}_i + \overrightarrow{P} \right\}, v_i \in [0.0, 1.0]$$
 (1)

for a Pyramidoid:

$$\left\{ \sum_{i \in I} v_i \overrightarrow{A}_i + \overrightarrow{P} \right\}, v_i \in [0.0, 1.0], \sum_{i \in I} v_i \le 1.0$$
 (2)

and for a Spheroid:

$$\left\{ \sum_{i \in I} v_i \overrightarrow{A}_i + \overrightarrow{P} \right\},$$

$$v_i \in [-0.5, 0.5], \quad \sum_{i \in I} v_i^2 \le 0.25$$
(3)

#### 1.1 Transformation

A translation of a Shapoid by  $\overrightarrow{T}$  is obtained as follow:

$$\left(\overrightarrow{P}, \left\{\overrightarrow{A}_i\right\}_{i \in I}\right) \mapsto \left(\overrightarrow{P} + \overrightarrow{T}, \left\{\overrightarrow{A}_i\right\}_{i \in I}\right) \tag{4}$$

A scale of a Shapoid by  $\overrightarrow{S}$  is obtained as follow:

$$\left(\overrightarrow{P}, \left\{\overrightarrow{A}_{i}\right\}_{i \in I}\right) \mapsto \left(\overrightarrow{P}, \left\{\overrightarrow{A}_{i}'\right\}_{i \in I}\right) \tag{5}$$

where

$$\overrightarrow{A}_i' = S_i \overrightarrow{A}_i' \tag{6}$$

For Shapoid whose dimension D is equal to 2, a rotation by angle  $\theta$  is obtained as follow:

$$(\overrightarrow{P}, \overrightarrow{A_0}, \overrightarrow{A_1}) \mapsto (\overrightarrow{P}, \overrightarrow{A_0}, \overrightarrow{A_1})$$
 (7)

where

$$\overrightarrow{A}_{i}' = \begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix} \overrightarrow{A}_{i}$$
 (8)

#### 1.2 Shapoid's coordinate system

The Shapoid's coordinate system is the system having  $\overrightarrow{P}$  as origin and  $\overrightarrow{A_i}$  as axis. One can change from the Shapoid's coordinate system  $(\overrightarrow{X}^S)$  to the standard coordinate system  $(\overrightarrow{X})$  as follow:

$$\overrightarrow{X} = \left[ \left( \overrightarrow{A_0} \right) \left( \overrightarrow{A_1} \right) \dots \left( \overrightarrow{A_{D-1}} \right) \right] \overrightarrow{X^S} + \overrightarrow{P}$$
 (9)

and reciprocally, from the standard coordinate system to the Shapoid's coordinate system:

$$\overrightarrow{X^S} = \left[ \left( \overrightarrow{A_0} \right) \left( \overrightarrow{A_1} \right) \dots \left( \overrightarrow{A_{D-1}} \right) \right]^{-1} \left( \overrightarrow{X} - \overrightarrow{P} \right) \tag{10}$$

#### 1.3 Insideness

 $\overrightarrow{X}$  is inside the Shapoid S if, for a Facoid:

$$\forall i \in I, 0.0 \le X_i^S \le 1.0 \tag{11}$$

for a Pyramidoid:

$$\begin{cases} \forall i \in I, 0.0 \le X_i^S \le 1.0\\ \sum_{i \in I} X_i^S \le 1.0 \end{cases}$$
 (12)

for a Spheroid:

$$\left| \left| \overrightarrow{X^S} \right| \right| \le 0.5 \tag{13}$$

## 1.4 Bounding box

A bounding box of a Shapoid is a Facoid whose axis are colinear to axis of the standard coordinate system, and including the Shapoid in its volume. While the smallest possible bounding box can be easily obtained for Facoid and Pyramidoid, it's more complicate for Spheroid. Then we

will consider for the Spheroid the bounding box of the equivalent Facoid  $\left(\overrightarrow{P} - \sum_{i \in I} \left(0.5 * \overrightarrow{A_i}\right), \left\{\overrightarrow{A_i}\right\}_{i \in I}\right)$  which gives the smallest bounding box when axis of the Spheroid are colinear to axis of the standard coordinate system and a bounding box slightly too large when not colinear.

The bounding box is defined as follow, for a Facoid:

$$\left(\overrightarrow{P'}, \left\{\overrightarrow{A_i'}\right\}_{i \in I}\right) \tag{14}$$

where

$$\begin{cases}
P'_{i} = P_{i} + \sum_{j \in I^{-}} A_{ji} \\
A'_{ij} = 0.0, i \neq j \\
A'_{ij} = \sum_{k \in I^{+}} A_{kj} - \sum_{k \in I^{-}} A_{kj}, i = j
\end{cases}$$
(15)

and,  $I^+$  and  $I^-$  are the subsets of I such as  $\forall j \in I^+, A_{ij} \geq 0.0$  and  $\forall j \in I^-, A_{ij} < 0.0$ .

for a Pyramidoid:

$$\left(\overrightarrow{P'}, \left\{\overrightarrow{A'_i}\right\}_{i \in I}\right) \tag{16}$$

where

$$\begin{cases}
P'_{i} = P_{i} + Min\left(Min_{j \in I}(A_{ji}), 0.0\right) \\
A'_{ij} = 0.0, i \neq j \\
A'_{ij} = Max_{k \in I}(A_{kj}) - Min_{k \in I}(A_{kj}), i = j
\end{cases}$$
(17)

## 1.5 Depth and Center

Depth  $\mathbf{D}_S(\overrightarrow{X})$  of position  $\overrightarrow{X}$  a Shapoid S is a value ranging from 0.0 if  $\overrightarrow{X}$  is on the surface of the Shapoid, to 1.0 if  $\overrightarrow{X}$  is at the farthest location from the surface inside the Shapoid. Depth is by definition equal to 0.0 if  $\overrightarrow{X}$  is outside the Shapoid. Depth is continuous and derivable on the volume of the Shapoid. It is defined by, for a Facoid:

$$\mathbf{D}_{S}(\overrightarrow{X}) = \prod_{i \in I} (1.0 - 4.0 * (0.5 - X_{i}^{S})^{2})$$
(18)

for a Pyramidoid:

$$\mathbf{D}_{S}(\overrightarrow{X}) = \prod_{i \in I} \left( 1.0 - 4.0 * \left( 0.5 - \frac{X_{i}^{S}}{1.0 - \sum_{j \in I - \{i\}} X_{j}^{S}} \right)^{2} \right)$$
(19)

and for a Spheroid:

$$\mathbf{D}_{S}(\overrightarrow{X}) = 1.0 - 2.0 * \left| |\overrightarrow{X}^{S}| \right| \tag{20}$$

The maximum depth is obtained at  $\overrightarrow{C}$  such as, for a Facoid:

$$\forall i \in I, C_i^S = 0.5 \tag{21}$$

for a Pyramidoid:

$$\forall i \in I, C_i^S = \frac{1}{D+1} \tag{22}$$

for a Spheroid:

$$\forall i \in I, C_i^S = 0.0 \tag{23}$$

 $\overrightarrow{C}$  is called the center of the Shapoid.

#### 1.6 Iterator on Spheroid

While a sequential path through a Facoid and a Pyramidoid is obvious, path through a Spheroid is more complex. The solution implemented is described below.

Given a Spheroid of dimension N we start from an arbitrary position: <0,0,...,-0.5>. From there we step the axis starting from the first one. If we could step an axis the step algorithm stops and return the new position as it could successfully step. However, if we could step on an axis other than the first one, it means we have modified the constraint for previous axis, the constraint being "is inside the spheroid". Then we reposition the axis before the stepped one to its lower possible value. It will allow it to step again at the next iteration on a new boundary defined by other axis values, and this scale up naturally to any dimension. Care must be care to the case when an axis reaches its upper value: the delta given by the user and the influence of other axis value make it jumps "over" the boundary in most cases. To keep things neat and clean we recalculate the exact value of the axis for its last step instead of using the delta given by the user.

The calculation of the lower and upper values of an axis given the values of other axis can be performed as follow:

Lets note  $\overrightarrow{P}=< p_0, p_1, ..., p_{N-1}>$  the position in a Spheroid of dimension N. A position will be on the boundary of the Spheroid if and only if  $||\overrightarrow{P}||=0.5$ . We want to calculate  $\alpha$  which bring a position  $\overrightarrow{P}'$  inside the Spheroid to a position  $\overrightarrow{P}$  on the boundary of the Spheroid by modifying the axis i (i.e.  $p_i=p_i'+\alpha$  and  $p_j=p_j', j\neq i$ ). Lets note  $n=||\overrightarrow{P}'||$ . We have:

$$p_0^{\prime 2} + p_1^{\prime 2} + \dots + p_i^{\prime 2} + \dots + p_{N-1}^{\prime 2} = n^2$$
 (24)

and

$$p_0^2 + p_1^2 + \dots + p_i^2 + \dots + p_{N-1}^2 = 0.25$$
 (25)

equivalent to

$$p_0^{\prime 2} + p_1^{\prime 2} + \dots + (p_i^{\prime} + \alpha)^2 + \dots + p_{N-1}^{\prime 2} = 0.25$$
 (26)

by substracting (24) and (26) we have

$$p_i^{\prime 2} - (p_i^{\prime} + \alpha)^2 = n^2 - 0.25 \tag{27}$$

equivalent to

$$p_i^{\prime 2} - (p_i^{\prime 2} + \alpha^2 + 2p_i^{\prime}\alpha) = n^2 - 0.25$$
 (28)

equivalent to

$$-\alpha^2 - 2p_i'\alpha - (n^2 - 0.25) = 0 (29)$$

simplified to

$$\alpha^2 + 2p_i'\alpha + (n^2 - 0.25) = 0 \tag{30}$$

This quadratic equation can be solved directly to obtain  $\alpha$ :

$$\alpha = \frac{-2p_i' \pm \sqrt{4p_i'^2 - 4(n^2 - 0.25)}}{2}$$
(31)

Which gives the two solutions defining the lower and upper boundaries of the Spheroid on the axis i.

This result can then be used to solve our problem with what I'll call the "Wormy Algorithm":

```
flag := true
norm := Norm(P)
iDim := 0
loop until (iDim < N and flag == true)</pre>
  prevNorm := norm
  P_iDim := P_iDim + delta
  norm := Norm(P)
  if (prevNorm < 0.5 and norm > 0.5)
    P_iDim := 0
    norm := Norm(P)
    val := 0.5 * Sqrt(-4.0 * (norm^2 - 0.25))
    P iDim := val
    norm := 0.5
    flag := false
    iDim := iDim - 1
    if (norm > 0.5)
      P_iDim := 0
      flag := false
      iDim := iDim - 1
    end if
  end if
  iDim := iDim + 1
end loop
if (flag == false)
  iDim := iDim - 1
  if (iDim \geq = 0)
    P_{iDim} := P_{iDim} + 0.5 * (-2.0 * P_{iDim} - 0.5)
      Sqrt(4.0 * (P_iDim)^2 - 4.0 * (norm^2 - 0.25)))
  end if
end if
return Not(flag)
```

This algorithm step P to the next position in the path by delta and returns true if we haven't reached the end of the path, or false if we have reached the end of the path (i.e. if we have iterated through all the surface/volume/... of the Spheroid). Remember that P must be initialised to <0,0,...,-0.5> as the beginning of the path, and that ShapoidIter iterates coordinates in the Shapoid's coordinate system.

## 1.7 Collision detection of Spheroid

The detection of collision between two Spheroids is done as follow. One of the spheroid is converted into the coordinates system of the other and checked against a circle of radius 0.5 centered at the origin of the system. By checking that the position of the converted Spheroid is less than its minor radius plus 0.5 or more than its major radius plus 0.5, the trivial cases of, respectively, interesection and non intersection can be performed. In other cases an incremental search from the center of the converted Spheroid toward the nearest

point to the origin inside this Spheroid is performed. The intersection can then be checked by testing if the distance of this point to the origin is less or equal than 0.5.

### 2 Interface

```
// ====== SHAPOID.H ========
#ifndef SHAPOID_H
#define SHAPOID_H
// ======== Include ========
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <string.h>
#include <stdbool.h>
#include "pberr.h"
#include "pbmath.h"
#include "gset.h"
// ======= Define ========
#define CloneShapoidType(T) typedef struct T {Shapoid _s;} T
#define SpheroidCreate(Dim) \
  (Spheroid*)ShapoidCreate(Dim, ShapoidTypeSpheroid)
#define FacoidCreate(Dim) \
  (Facoid*)ShapoidCreate(Dim, ShapoidTypeFacoid)
#define PvramidoidCreate(Dim) \
  (Pyramidoid*)ShapoidCreate(Dim, ShapoidTypePyramidoid)
#define ShapoidGetCoverage(ShapoidA, ShapoidB) \
  _ShapoidGetCoverageDelta((Shapoid* const)ShapoidA, \
  (Shapoid* const)ShapoidB, 0.1)
#define ShapoidGetCoverageDelta(ShapoidA, ShapoidB, Prec) \
  _ShapoidGetCoverageDelta((Shapoid* const)ShapoidA, \
  (Shapoid* const)ShapoidB, Prec)
#define ShapoidIterCreateStatic(Shap, Delta) \
  _ShapoidIterCreateStatic((Shapoid* const)(Shap), (VecFloat*)(Delta))
#define ShapoidIterSetShapoid(Iter, Shap) \
  _ShapoidIterSetShapoid(Iter, (Shapoid* const)(Shap))
#define ShapoidIterSetDelta(Iter, Delta) \
  _ShapoidIterSetDelta(Iter, (VecFloat* const)(Delta))
extern const char* ShapoidTypeString[3];
// ----- ShapoidIter
// ========= Data structure ==========
typedef enum ShapoidType {
  ShapoidTypeFacoid, ShapoidTypeSpheroid,
```

```
ShapoidTypePyramidoid
} ShapoidType;
// Don't forget to update ShapoidTypeString in shapoid.c when adding
// new type
typedef struct Shapoid {
  // Position of origin
  VecFloat* _pos;
  // Dimension
  int _dim;
  // Vectors defining axes
  VecFloat** _axis;
  // Type of Shapoid
  ShapoidType _type;
  // Linear sytem used to import coordinates
  SysLinEq* _sysLinEqImport;
} Shapoid;
CloneShapoidType(Facoid);
CloneShapoidType(Pyramidoid);
typedef struct Spheroid {
  Shapoid _s;
  //\ {\rm Major} and minor axis for optimization
  int _majAxis;
  int _minAxis;
} Spheroid;
//CloneShapoidType(Spheroid);
// ====== Functions declaration =========
// Create a Shapoid of dimension 'dim' and type 'type', default values:
// _pos = null vector
// _axis[d] = unit vector along dimension d
Shapoid* ShapoidCreate(const int dim, const ShapoidType type);
// Clone a Shapoid
Shapoid* _ShapoidClone(const Shapoid* const that);
inline Facoid* FacoidClone(const Facoid* const that) {
  return (Facoid*)_ShapoidClone((const Shapoid*)that);
}
inline Pyramidoid* PyramidoidClone(const Pyramidoid* const that) {
 return (Pyramidoid*)_ShapoidClone((const Shapoid*)that);
inline Spheroid* SpheroidClone(const Spheroid* const that) {
  return (Spheroid*)_ShapoidClone((const Shapoid*)that);
// Free memory used by a Shapoid
void _ShapoidFree(Shapoid** that);
// Function which return the JSON encoding of 'that'
JSONNode* _ShapoidEncodeAsJSON(const Shapoid* const that);
// Function which decode from JSON encoding 'json' to 'that'
bool _ShapoidDecodeAsJSON(Shapoid** that, const JSONNode* const json);
// Load the Shapoid of type 'type' from the stream
// If the Shapoid is already allocated, it is freed before loading
// Return true upon success else false
bool _ShapoidLoad(Shapoid** that, FILE* const stream);
#if BUILDMODE != 0
inline
```

```
bool FacoidLoad(Facoid** that, FILE* const stream);
#if BUILDMODE != 0
inline
#endif
bool PyramidoidLoad(Pyramidoid** that, FILE* const stream);
#if BUILDMODE != 0
inline
#endif
bool SpheroidLoad(Spheroid** that, FILE* const stream);
// Save the Shapoid to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
// Return true upon success else false
bool _ShapoidSave(const Shapoid* const that, FILE* const stream,
 const bool compact);
// Print the Shapoid on 'stream'
void _ShapoidPrintln(const Shapoid* const that, FILE* const stream);
// Get the dimension of the Shapoid
#if BUILDMODE != 0
inline
#endif
int _ShapoidGetDim(const Shapoid* const that);
// Get the type of the Shapoid
#if BUILDMODE != 0
inline
#endif
ShapoidType _ShapoidGetType(const Shapoid* const that);
// Get the type of the Shapoid as a string
// Return a pointer to a constant string (not to be freed)
#if BUILDMODE != 0
inline
const char* _ShapoidGetTypeAsString(const Shapoid* const that);
// Return a VecFloat equals to the position of the Shapoid
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidGetPos(const Shapoid* const that);
// Return a VecFloat equals to the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidGetAxis(const Shapoid* const that, const int dim);
// Return the position of the Shapoid
#if BUILDMODE != 0
inline
#endif
const VecFloat* _ShapoidPos(const Shapoid* const that);
// Return the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
```

```
const VecFloat* _ShapoidAxis(const Shapoid* const that, const int dim);
// Set the position of the Shapoid to 'pos'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetPos(Shapoid* const that, const VecFloat* const pos);
// Set the 'iElem'-th value of the position of the Shapoid to 'val'
#if BUILDMODE != 0
inline
#endif
void _ShapoidPosSet(Shapoid* const that, const int iElem,
 const float val);
// Set the 'iElem'-th value of the position of the Shapoid to 'val'
// added to its current value
#if BUILDMODE != 0
inline
#endif
void _ShapoidPosSetAdd(Shapoid* const that, const int iElem,
 const float val);
// Get the 'iElem'-th value of the position of the Shapoid
#if BUILDMODE != 0
inline
#endif
float _ShapoidPosGet(const Shapoid* const that, const int iElem);
// Set the position of the Shapoid such as its center is at 'pos'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetCenterPos(Shapoid* const that,
 const VecFloat* const pos);
// Set the 'dim'-th axis of the Shapoid to 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetAxis(Shapoid* const that, const int dim,
  const VecFloat* const v);
// Set the 'iElem'-th element of the 'dim'-th axis of the Shapoid to 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisSet(Shapoid* const that, const int dim,
 const int iElem, const float v);
// Set the 'iElem'-th element of the 'dim'-th axis of the Shapoid to
// 'v' added to its current value
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisSetAdd(Shapoid* const that, const int dim,
  const int iElem, const float v);
// Get the 'iElem'-th element of the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
```

```
float _ShapoidAxisGet(const Shapoid* const that, const int dim,
  const int iElem);
// Scale the 'dim'-th axis of the Shapoid by 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisScale(Shapoid* const that, const int dim,
 const float v);
// Translate the Shapoid by 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidTranslate(Shapoid* const that, const VecFloat* const v);
// Scale the Shapoid by 'v' (each axis is multiplied by v[iAxis])
#if BUILDMODE != 0
inline
#endif
void _ShapoidScaleVector(Shapoid* const that, const VecFloat* const v);
// Scale the Shapoid by 'c'
#if BUILDMODE != 0
inline
#endif
void _ShapoidScaleScalar(Shapoid* const that, const float c);
// Scale the Shapoid by 'v' (each axis is multiplied by v[iAxis])
// and translate the Shapoid such as its center after scaling
// is at the same position than before scaling
#if BUILDMODE != 0
inline
#endif
void _ShapoidGrowVector(Shapoid* const that, const VecFloat* const v);
// Scale the Shapoid by 'c'
// and translate the Shapoid such as its center after scaling
// is at the same position than before scaling
#if BUILDMODE != 0
inline
#endif
void _ShapoidGrowScalar(Shapoid* const that, const float c);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to its center
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotCenter(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to its position
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotStart(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
#if BUILDMODE != 0
inline
```

```
#endif
void _ShapoidRotOrigin(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisCenter(Shapoid* const that,
 const VecFloat3D* const axis, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisStart(Shapoid* const that,
  const VecFloat3D* const axis, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisOrigin(Shapoid* const that,
 const VecFloat3D* const axis, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around X
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXCenter(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around {\tt X}
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXStart(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around X
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXOrigin(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around Y
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotYCenter(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around Y
```

```
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotYStart(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around Y
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotYOrigin(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around Z
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotZCenter(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around Z
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotZStart(Shapoid* const that, const float theta);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around Z
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotZOrigin(Shapoid* const that, const float theta);
// Convert the coordinates of 'pos' from standard coordinate system
// toward the Shapoid coordinates system
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidImportCoord(const Shapoid* const that,
  const VecFloat* const pos);
// Convert the coordinates of 'pos' from the Shapoid coordinates system
// toward standard coordinate system
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidExportCoord(const Shapoid* const that,
  const VecFloat* const pos);
// Return true if 'pos' (in standard coordinates system) is inside the
// Shapoid
// Else return false
#if BUILDMODE != 0
inline
bool _ShapoidIsPosInside(const Shapoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
```

```
bool FacoidIsPosInside(const Facoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
bool PyramidoidIsPosInside(const Pyramidoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
bool SpheroidIsPosInside(const Spheroid* const that,
  const VecFloat* const pos);
// Get a bounding box of the Shapoid. The bounding box is aligned
// on the standard coordinate system (its axis are colinear with
// the axis of the standard coordinate system).
// The bounding box is returned as a Facoid, which position is
// at the minimum value along each axis.
Facoid* _ShapoidGetBoundingBox(const Shapoid* const that);
Facoid* FacoidGetBoundingBox(const Facoid* const that);
Facoid* PyramidoidGetBoundingBox(const Pyramidoid* const that);
Facoid* SpheroidGetBoundingBox(const Spheroid* const that);
// Get the bounding box of a set of Facoid. The bounding box is aligned
// on the standard coordinate system (its axis are colinear with
// the axis of the standard coordinate system).
// The bounding box is returned as a Facoid, which position is
// at the minimum value along each axis.
Facoid* ShapoidGetBoundingBoxSet(const GSetShapoid* const set);
// Get the depth value in the Shapoid of 'pos' in standard coordinate
// system
// The depth is defined as follow: the point with depth equals 1.0 is
// the farthest point from the surface of the Shapoid (inside it),
// points with depth equals to 0.0 are point on the surface of the
// Shapoid. Depth is continuous and derivable over the volume of the
// Shapoid
// Return 0.0 if pos is outside the Shapoid
#if BUILDMODE != 0
inline
#endif
float _ShapoidGetPosDepth(const Shapoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
float FacoidGetPosDepth(const Facoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
float PyramidoidGetPosDepth(const Pyramidoid* const that,
  const VecFloat* const pos);
#if BUILDMODE != 0
inline
#endif
float SpheroidGetPosDepth(const Spheroid* const that,
  const VecFloat* const pos);
// Get the center of the shapoid in standard coordinate system
#if BUILDMODE != 0
inline
```

```
VecFloat* _ShapoidGetCenter(const Shapoid* const that);
#if BUILDMODE != 0
inline
#endif
VecFloat* FacoidGetCenter(const Facoid* const that);
#if BUILDMODE != 0
inline
#endif
VecFloat* PyramidoidGetCenter(const Pyramidoid* const that);
#if BUILDMODE != 0
inline
#endif
VecFloat* SpheroidGetCenter(const Spheroid* const that);
// Get the percentage of 'tho' included into 'that' (in [0.0, 1.0])
// 0.0 -> 'tho' is completely outside of 'that'
// 1.0 -> 'tho' is completely inside of 'that'
// 'that' and 'tho' must me of same dimensions
// delta is the step of the algorithm (in ]0.0, 1.0])
// small -> slow but precise
// big -> fast but rough
float _ShapoidGetCoverageDelta(const Shapoid* const that,
  const Shapoid* const tho, const float delta);
// Update the system of linear equation used to import coordinates
#if BUILDMODE != 0
inline
#endif
void ShapoidUpdateSysLinEqImport(Shapoid* const that);
// Check if shapoid 'that' and 'tho' are equals
#if BUILDMODE != 0
inline
#endif
bool _ShapoidIsEqual(const Shapoid* const that,
  const Shapoid* const tho);
// Add a copy of the Facoid 'that' to the GSet 'set' (containing
// other Facoid), taking care to avoid overlaping Facoid
// The copy of 'that' may be resized or divided
// The Facoid in the set and 'that' must be aligned with the
// coordinates system axis and have
// same dimensions
void FacoidAlignedAddClippedToSet(const Facoid* const that,
  GSetShapoid* const set);
// Check if the Facoid 'that' is completely included into the Facoid
// 'facoid'
// Both Facoid must be aligned with the coordinates system and have
// same dimensions
// Return true if it is included, false else
bool FacoidAlignedIsInsideFacoidAligned(const Facoid* const that,
  const Facoid* const facoid);
// Check if the Facoid 'that' is completely excluded from the Facoid
// Both Facoid must be aligned with the coordinates system and have
// same dimensions
// Return true if it is excluded, false else
bool FacoidAlignedIsOutsideFacoidAligned(const Facoid* const that,
  const Facoid* const facoid);
```

```
// Get a GSet of Facoid aligned with coordinates system covering the
// Facoid 'that' except for area in the Facoid 'facoid'
// Both Facoid must be aligned with the coordinates system and have
// same dimensions
GSetShapoid* FacoidAlignedSplitExcludingFacoidAligned(
  const Facoid* const that, const Facoid* const facoid);
// Return true if 'that' intersects 'tho'
// Return false else
// 'that' and 'tho' must have same dimension
bool _SpheroidIsInterSpheroid(const Spheroid* const that,
  const Spheroid* const tho);
// Update the major and minor axis of the Spheroid 'that'
void SpheroidUpdateMajMinAxis(Spheroid* const that);
// Get the maximum distance from the center of the Shapoid 'that' and
// Currenty only defined for spheroid, return 0.0 else
float _ShapoidGetBoundingRadius(const Shapoid* const that);
// ----- ShapoidIter
// ========= Data structure ==========
typedef struct ShapoidIter {
  // Attached shapoid
  const Shapoid* _shap;
  // Delta step
  VecFloat* _delta;
  // Current position (in internal coordinates of the shapoid)
  VecFloat* _pos;
} ShapoidIter;
// ========= Functions declaration ==========
// Create a new iterator on the Shapoid 'shap' with a step of 'delta'
// (step on the internal coordinates of the Shapoid)
// The iterator is initialized and ready to be stepped
ShapoidIter _ShapoidIterCreateStatic(const Shapoid* const shap,
  const VecFloat* const delta);
// Free the memory used by the ShapoidIter 'that'
void ShapoidIterFreeStatic(ShapoidIter* const that);
// Reinitialise the ShapoidIter 'that' to its starting position
void ShapoidIterInit(ShapoidIter* const that);
// Step the ShapoidIter 'that'
// Return false if the iterator is at its end and couldn't be stepped
bool ShapoidIterStep(ShapoidIter* const that);
// Return the current position in Shapoid coordinates of the
// ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
VecFloat* ShapoidIterGetInternalPos(const ShapoidIter* const that);
// Return the current position in standard coordinates of the
// ShapoidIter 'that'
```

```
#if BUILDMODE != 0
inline
#endif
VecFloat* ShapoidIterGetExternalPos(const ShapoidIter* const that);
// Set the attached Shapoid of the ShapoidIter 'that' to 'shap'
// The iterator is reset to its initial position
#if BUILDMODE != 0
inline
#endif
void _ShapoidIterSetShapoid(ShapoidIter* const that,
  const Shapoid* const shap);
// Get the Shapoid of the ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
const Shapoid* ShapoidIterShapoid(const ShapoidIter* const that);
// Set the delta of the ShapoidIter 'that' to a copy of 'delta'
#if BUILDMODE != 0
inline
#endif
void _ShapoidIterSetDelta(ShapoidIter* const that,
  const VecFloat* const delta);
// Get the delta of the ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
const VecFloat* ShapoidIterDelta(const ShapoidIter* const that);
// ======== Polymorphism =========
#define ShapoidClone(Shap) _Generic(Shap, \
  Shapoid*: _ShapoidClone, \
  Facoid*: FacoidClone, \
  Pyramidoid*: PyramidoidClone, \
  Spheroid*: SpheroidClone, \
  default: PBErrInvalidPolymorphism)(Shap)
#define ShapoidFree(ShapRef) _Generic(ShapRef, \
  Shapoid**: _ShapoidFree, \
  Facoid**: _ShapoidFree, \
  Pyramidoid**: _ShapoidFree, \
  Spheroid**: _ShapoidFree, \
  default: PBErrInvalidPolymorphism)((Shapoid**)(ShapRef))
#define ShapoidEncodeAsJSON(Shap) _Generic(Shap, \
  {\tt Shapoid*: \_ShapoidEncodeAsJSON, \ } \\
  Facoid*: _ShapoidEncodeAsJSON, \
  Pyramidoid*: _ShapoidEncodeAsJSON, \
  Spheroid*: _ShapoidEncodeAsJSON, \
  const Shapoid*: _ShapoidEncodeAsJSON, \
const Facoid*: _ShapoidEncodeAsJSON, \
  const Pyramidoid*: _ShapoidEncodeAsJSON, \
  const Spheroid*: _ShapoidEncodeAsJSON, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)Shap)
#define ShapoidDecodeAsJSON(ShapRef, Json) _Generic(ShapRef, \
  Shapoid**: _ShapoidDecodeAsJSON, \
  Facoid**: _ShapoidDecodeAsJSON, \
```

```
Pyramidoid**: _ShapoidDecodeAsJSON, \
  Spheroid**: _ShapoidDecodeAsJSON, \
  default: PBErrInvalidPolymorphism)((Shapoid**)ShapRef, Json)
#define ShapoidLoad(ShapRef, Stream) _Generic(ShapRef, \
  Shapoid**: _ShapoidLoad, \
 Facoid**: FacoidLoad, \
  Pyramidoid**: PyramidoidLoad, \
 Spheroid**: SpheroidLoad, \
  default: PBErrInvalidPolymorphism)(ShapRef, Stream)
#define ShapoidSave(Shap, Stream, Compact) _Generic(Shap, \
  Shapoid*: _ShapoidSave, \
  Facoid*: _ShapoidSave, \
 Pyramidoid*: _ShapoidSave, \
 Spheroid*: _ShapoidSave, \
 const Shapoid*: _ShapoidSave, \
  const Facoid*: _ShapoidSave, \
  const Pyramidoid*: _ShapoidSave, \
  const Spheroid*: _ShapoidSave, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), \
   Stream, Compact)
#define ShapoidPrintln(Shap, Stream) _Generic(Shap, \
 Shapoid*: _ShapoidPrintln, \
 Facoid*: _ShapoidPrintln, \
  Pyramidoid*: _ShapoidPrintln, \
 Spheroid*: _ShapoidPrintln, \
  const Shapoid*: _ShapoidPrintln, \
 const Facoid*: _ShapoidPrintln, \
  const Pyramidoid*: _ShapoidPrintln, \
  const Spheroid*: _ShapoidPrintln, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), Stream)
#define ShapoidGetType(Shap) _Generic(Shap, \
 {\tt Shapoid*: \_ShapoidGetType, \ } \\
 Facoid*: _ShapoidGetType, \
  Pyramidoid*: _ShapoidGetType, \
 Spheroid*: _ShapoidGetType, \
  const Shapoid*: _ShapoidGetType, \
  const Facoid*: _ShapoidGetType, \
  const Pyramidoid*: _ShapoidGetType, \
  const Spheroid*: _ShapoidGetType, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap))
#define ShapoidGetTypeAsString(Shap) _Generic(Shap, \
 Shapoid*: _ShapoidGetTypeAsString, \
  Facoid*: _ShapoidGetTypeAsString, \
 Pyramidoid*: _ShapoidGetTypeAsString, \
  Spheroid*: _ShapoidGetTypeAsString, \
 const Shapoid*: _ShapoidGetTypeAsString, \
const Facoid*: _ShapoidGetTypeAsString, \
  const Pyramidoid*: _ShapoidGetTypeAsString, \
  const Spheroid*: _ShapoidGetTypeAsString, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap))
#define ShapoidGetDim(Shap) _Generic(Shap, \
  Shapoid*: _ShapoidGetDim, \
  Facoid*: _ShapoidGetDim, \
 Pyramidoid*: _ShapoidGetDim, \
 Spheroid*: _ShapoidGetDim, \
  const Shapoid*: _ShapoidGetDim, \
```

```
\verb|const Facoid*: \_ShapoidGetDim|, \  \  \, \backslash \\
  const Pyramidoid*: _ShapoidGetDim, \
  const Spheroid*: _ShapoidGetDim, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap))
\verb|#define ShapoidGetPos(Shap) _Generic(Shap, \\ \\ \\ \\ \\
  Shapoid*: _ShapoidGetPos, \
  Facoid*: _ShapoidGetPos, \
 Pyramidoid*: _ShapoidGetPos, \
 {\tt Spheroid*: \_ShapoidGetPos, \ } \\
 const Shapoid*: _ShapoidGetPos, \
  const Facoid*: _ShapoidGetPos, \
  const Pyramidoid*: _ShapoidGetPos, \
 const Spheroid*: _ShapoidGetPos, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap))
#define ShapoidPos(Shap) _Generic(Shap, \
 Shapoid*: _ShapoidPos, \
  Facoid*: _ShapoidPos, \
 Pyramidoid*: _ShapoidPos, \
 Spheroid*: _ShapoidPos, \
 const Shapoid*: _ShapoidPos, \
const Facoid*: _ShapoidPos, \
  const Pyramidoid*: _ShapoidPos, \
  const Spheroid*: _ShapoidPos, \
  default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap))
\verb|#define ShapoidSetAxis(Shap, Index, Vec) _Generic(Shap, \\ \\
 Shapoid*: _ShapoidSetAxis, \
 Facoid*: _ShapoidSetAxis, \
 Pyramidoid*: _ShapoidSetAxis, \
 Spheroid*: _ShapoidSetAxis, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Index, \
    (VecFloat*)Vec)
#define ShapoidSetPos(Shap, Vec) _Generic(Shap, \
 Shapoid*: _ShapoidSetPos, \
 Facoid*: _ShapoidSetPos, \
 Pyramidoid*: _ShapoidSetPos, \
 Spheroid*: _ShapoidSetPos, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), (VecFloat*)Vec)
#define ShapoidPosSet(Shap, Index, Val) _Generic(Shap, \
 Shapoid*: _ShapoidPosSet, \
 Facoid*: _ShapoidPosSet, \
 Pyramidoid*: _ShapoidPosSet, \
 {\tt Spheroid*: \_ShapoidPosSet, \setminus}
  default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Index, Val)
\verb|#define ShapoidPosSetAdd(Shap, Index, Val) _Generic(Shap, \\ \\
  Shapoid*: _ShapoidPosSetAdd, \
 Facoid*: _ShapoidPosSetAdd, \
 Pyramidoid*: _ShapoidPosSetAdd, \
 Spheroid*: _ShapoidPosSetAdd, \
  default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Index, Val)
#define ShapoidPosGet(Shap, Index) _Generic(Shap, \
  Shapoid*: _ShapoidPosGet, \
  Facoid*: _ShapoidPosGet, \
 Pyramidoid*: _ShapoidPosGet, \
 Spheroid*: _ShapoidPosGet, \
  const Shapoid*: _ShapoidPosGet, \
```

```
const Facoid*: _ShapoidPosGet, \
 const Pyramidoid*: _ShapoidPosGet, \
 const Spheroid*: _ShapoidPosGet, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Index)
#define ShapoidSetCenterPos(Shap, Vec) _Generic(Shap, \
 Shapoid*: _ShapoidSetCenterPos, \
 Facoid*: _ShapoidSetCenterPos, \
 Pyramidoid*: _ShapoidSetCenterPos, \
 Spheroid*: _ShapoidSetCenterPos, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), (VecFloat*)Vec)
#define ShapoidGetAxis(Shap, Index) _Generic(Shap, \
 Shapoid*: _ShapoidGetAxis, \
 Facoid*: _ShapoidGetAxis, \
 Pyramidoid*: _ShapoidGetAxis, \
 Spheroid*: _ShapoidGetAxis, \
 const Shapoid*: _ShapoidGetAxis, \
 const Facoid*: _ShapoidGetAxis, \
 const Pyramidoid*: _ShapoidGetAxis, \
 const Spheroid*: _ShapoidGetAxis, \
 default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), Index)
#define ShapoidAxis(Shap, Index) _Generic(Shap, \
 Shapoid*: _ShapoidAxis, \
 Facoid*: \_ShapoidAxis, \setminus
 Pyramidoid*: _ShapoidAxis, \
 Spheroid*: _ShapoidAxis, \
 const Shapoid*: _ShapoidAxis, \
 const Facoid*: _ShapoidAxis, \
 const Pyramidoid*: _ShapoidAxis, \
 const Spheroid*: _ShapoidAxis, \
 default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), Index)
#define ShapoidAxisSet(Shap, Dim, Index, Val) _Generic(Shap, \
 Shapoid*: _ShapoidAxisSet, \
 Facoid*: _ShapoidAxisSet, \
 Pyramidoid*: _ShapoidAxisSet, \
 Spheroid*: _ShapoidAxisSet, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Dim, Index, Val)
#define ShapoidAxisSetAdd(Shap, Dim, Index, Val) _Generic(Shap, \
 Shapoid*: _ShapoidAxisSetAdd, \
 Facoid*: _ShapoidAxisSetAdd, \
 Pyramidoid*: _ShapoidAxisSetAdd, \
 Spheroid*: _ShapoidAxisSetAdd, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Dim, Index, Val)
#define ShapoidAxisGet(Shap, Dim, Index) _Generic(Shap, \
 Shapoid*: _ShapoidAxisGet, \
 Facoid*: _ShapoidAxisGet, \
 Pyramidoid*: _ShapoidAxisGet, \
 Spheroid*: _ShapoidAxisGet, \
 const Facoid*: _ShapoidAxisGet, \
 const Pyramidoid*: _ShapoidAxisGet, \
 const Spheroid*: _ShapoidAxisGet, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Dim, Index)
#define ShapoidAxisScale(Shap, Dim, Val) _Generic(Shap, \
 Shapoid*: _ShapoidAxisScale, \
 Facoid*: _ShapoidAxisScale, \
```

```
Pyramidoid*: _ShapoidAxisScale, \
 Spheroid*: _ShapoidAxisScale, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Dim, Val)
#define ShapoidTranslate(Shap, Vec) _Generic(Shap, \
 {\tt Shapoid*: \_ShapoidTranslate, \ } \\
 Facoid*: \_ShapoidTranslate, \setminus
 Pyramidoid*: _ShapoidTranslate, \
 Spheroid*: _ShapoidTranslate, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), (VecFloat*)Vec)
#define ShapoidIsEqual(ShapA, ShapB) _Generic(ShapA, \
 Shapoid*: _Generic(ShapB, \
   Shapoid*: _ShapoidIsEqual, \
   Facoid*: _ShapoidIsEqual, \
   Pyramidoid*: _ShapoidIsEqual, \
   Spheroid*: _ShapoidIsEqual, \
   const Shapoid*: _ShapoidIsEqual, \
   const Facoid*: _ShapoidIsEqual, \
   const Pyramidoid*: _ShapoidIsEqual, \
   const Spheroid*: _ShapoidIsEqual, \
   default: PBErrInvalidPolymorphism), \
 Facoid*: _Generic(ShapB, \
   Shapoid*: _ShapoidIsEqual, \
   Facoid*: _ShapoidIsEqual, \
   Pyramidoid*: _ShapoidIsEqual, \
   Spheroid*: _ShapoidIsEqual, \
   const Shapoid*: _ShapoidIsEqual, \
const Facoid*: _ShapoidIsEqual, \
   const Pyramidoid*: _ShapoidIsEqual, \
   const Spheroid*: _ShapoidIsEqual, \
   default: PBErrInvalidPolymorphism), \
 Pyramidoid*: _Generic(ShapB, \
   Shapoid*: _ShapoidIsEqual, \
   Facoid*: _ShapoidIsEqual, \
   Pyramidoid*: _ShapoidIsEqual, \
   Spheroid*: _ShapoidIsEqual, \
   const Shapoid*: _ShapoidIsEqual, \
   const Facoid*: _ShapoidIsEqual, \
   const Pyramidoid*: _ShapoidIsEqual, \
   const Spheroid*: _ShapoidIsEqual, \
   default: PBErrInvalidPolymorphism), \
 Spheroid*: _Generic(ShapB, \
   Shapoid*: _ShapoidIsEqual, \
   Facoid*: _ShapoidIsEqual, \
   Pyramidoid*: _ShapoidIsEqual, \
   Spheroid*: _ShapoidIsEqual, \
   const Shapoid*: _ShapoidIsEqual, \
   const Facoid*: _ShapoidIsEqual, \
   const Spheroid*: _ShapoidIsEqual, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)((const Shapoid*)(ShapA), \
   (const Shapoid*)(ShapB))
Shapoid*: _ShapoidGetBoundingBox, \
 Facoid*: FacoidGetBoundingBox, \
 Pyramidoid*: PyramidoidGetBoundingBox, \
 Spheroid*: SpheroidGetBoundingBox, \
 const Shapoid*: _ShapoidGetBoundingBox, \
 const Facoid*: FacoidGetBoundingBox, \
```

```
const Pyramidoid*: PyramidoidGetBoundingBox, \
 const Spheroid*: SpheroidGetBoundingBox, \
 GSetShapoid*: ShapoidGetBoundingBoxSet, \
 const GSetShapoid*: ShapoidGetBoundingBoxSet, \
 default: PBErrInvalidPolymorphism)(Shap)
#define ShapoidScale(Shap, Scale) _Generic(Scale, \
 VecFloat*: _ShapoidScaleVector, \
 VecFloat2D*: _ShapoidScaleVector, \
 VecFloat3D*: _ShapoidScaleVector, \
 float: _ShapoidScaleScalar, \
 const VecFloat*: _ShapoidScaleVector, \
 const VecFloat2D*: _ShapoidScaleVector, \
 const VecFloat3D*: _ShapoidScaleVector, \
 const float: _ShapoidScaleScalar, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Scale)
#define ShapoidGrow(Shap, Scale) _Generic(Shap, \
 Shapoid*: _Generic(Scale, \
   VecFloat*: _ShapoidGrowVector, \
   float: _ShapoidGrowScalar, \
   default: PBErrInvalidPolymorphism), \
 Facoid*: _Generic(Scale, \
   VecFloat*: _ShapoidGrowVector, \
   float: _ShapoidGrowScalar, \
   default: PBErrInvalidPolymorphism), \
 Pyramidoid*: _Generic(Scale, \
   VecFloat*: _ShapoidGrowVector, \
   float: _ShapoidGrowScalar, \
   default: PBErrInvalidPolymorphism), \
 Spheroid*: _Generic(Scale, \
   VecFloat*: _ShapoidGrowVector, \
   float: _ShapoidGrowScalar, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Scale)
#define ShapoidGetCenter(Shap) _Generic(Shap, \
 Shapoid*: _ShapoidGetCenter, \
 Facoid*: FacoidGetCenter, \
 Pyramidoid*: PyramidoidGetCenter, \
 Spheroid*: SpheroidGetCenter, \
 const Shapoid*: _ShapoidGetCenter, \
 const Facoid*: FacoidGetCenter, \
 const Pyramidoid*: PyramidoidGetCenter, \
 const Spheroid*: SpheroidGetCenter, \
 default: PBErrInvalidPolymorphism)(Shap)
#define ShapoidRotCenter(Shap, Theta) _Generic(Shap, \
 {\tt Shapoid*: \_ShapoidRotCenter, \ } \\
 Facoid*: _ShapoidRotCenter, \
 Pyramidoid*: _ShapoidRotCenter, \
 Spheroid*: _ShapoidRotCenter, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotOrigin(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotOrigin, \
 Facoid*: _ShapoidRotOrigin, \
 Pyramidoid*: _ShapoidRotOrigin, \
 Spheroid*: _ShapoidRotOrigin, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotStart(Shap, Theta) _Generic(Shap, \
```

```
Shapoid*: _ShapoidRotStart, \
 Facoid*: _ShapoidRotStart, \
 Pyramidoid*: _ShapoidRotStart, \
 Spheroid*: _ShapoidRotStart, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotAxisCenter(Shap, Axis, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotAxisCenter, \
 Facoid*: _ShapoidRotAxisCenter, \
 Pyramidoid*: _ShapoidRotAxisCenter, \
 Spheroid*: _ShapoidRotAxisCenter, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Axis, Theta)
#define ShapoidRotAxisOrigin(Shap, Axis, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotAxisOrigin, \
 Facoid*: _ShapoidRotAxisOrigin, \
 Pyramidoid*: _ShapoidRotAxisOrigin, \
 Spheroid*: _ShapoidRotAxisOrigin, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Axis, Theta)
Shapoid*: _ShapoidRotAxisStart, \
 Facoid*: _ShapoidRotAxisStart, \
 Pyramidoid*: _ShapoidRotAxisStart, \
 Spheroid*: _ShapoidRotAxisStart, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Axis, Theta)
\verb|#define ShapoidRotXCenter(Shap, Theta) _Generic(Shap, \\ \\ \\
 Shapoid*: _ShapoidRotXCenter, \
 Facoid*: _ShapoidRotXCenter, \
 Pyramidoid*: _ShapoidRotXCenter, \
 Spheroid*: _ShapoidRotXCenter, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotXOrigin(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotXOrigin, \
 Facoid*: _ShapoidRotXOrigin, \
 Pyramidoid*: _ShapoidRotXOrigin, \
 Spheroid*: _ShapoidRotXOrigin, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotXStart(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotXStart, \
 Facoid*: _ShapoidRotXStart, \
 Pyramidoid*: _ShapoidRotXStart, \
 Spheroid*: _ShapoidRotXStart, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotYCenter(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotYCenter, \
 Facoid*: _ShapoidRotYCenter, \
 Pyramidoid*: _ShapoidRotYCenter, \
 Spheroid*: _ShapoidRotYCenter, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotYOrigin(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotYOrigin, \
 Facoid*: _ShapoidRotYOrigin, \
 Pyramidoid*: _ShapoidRotYOrigin, \
 Spheroid*: _ShapoidRotYOrigin, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
```

```
#define ShapoidRotYStart(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotYStart, \
 Facoid*: _ShapoidRotYStart, \
 Pyramidoid*: _ShapoidRotYStart, \
 Spheroid*: _ShapoidRotYStart, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotZCenter(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotZCenter, \
 Facoid*: _ShapoidRotZCenter, \
 Pyramidoid*: _ShapoidRotZCenter, \
 Spheroid*: _ShapoidRotZCenter, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotZOrigin(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotZOrigin, \
 Facoid*: _ShapoidRotZOrigin, \
 Pyramidoid*: _ShapoidRotZOrigin, \
 Spheroid*: _ShapoidRotZOrigin, \
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidRotZStart(Shap, Theta) _Generic(Shap, \
 Shapoid*: _ShapoidRotZStart, \
 Facoid*: _ShapoidRotZStart, \
 Pyramidoid*: _ShapoidRotZStart, \
 {\tt Spheroid*: \_ShapoidRotZStart, \ } \\
 default: PBErrInvalidPolymorphism)((Shapoid*)(Shap), Theta)
#define ShapoidImportCoord(Shap, VecPos) _Generic(Shap, \
 Shapoid*: _ShapoidImportCoord, \
 Facoid*: _ShapoidImportCoord, \
 Pyramidoid*: _ShapoidImportCoord, \
 Spheroid*: _ShapoidImportCoord, \
 const Shapoid*: _ShapoidImportCoord, \
 const Facoid*: _ShapoidImportCoord, \
 const Pyramidoid*: _ShapoidImportCoord, \
 const Spheroid*: _ShapoidImportCoord, \
 default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), \
   (const VecFloat*)VecPos)
#define ShapoidExportCoord(Shap, VecPos) _Generic(Shap, \
 Shapoid*: _ShapoidExportCoord, \
 Facoid*: _ShapoidExportCoord, \
 Pyramidoid*: _ShapoidExportCoord, \
 Spheroid*: _ShapoidExportCoord, \
 const Shapoid*: _ShapoidExportCoord, \
 const Facoid*: _ShapoidExportCoord, \
 const Pyramidoid*: _ShapoidExportCoord, \
 const Spheroid*: _ShapoidExportCoord, \
 default: PBErrInvalidPolymorphism)((const Shapoid*)(Shap), \
    (const VecFloat*)VecPos)
#define ShapoidIsPosInside(Shap, VecPos) _Generic(Shap, \
 Shapoid*: _ShapoidIsPosInside, \
 Facoid*: FacoidIsPosInside, \
 Pyramidoid*: PyramidoidIsPosInside, \
 Spheroid*: SpheroidIsPosInside, \
 const Shapoid*: _ShapoidIsPosInside, \
 const Facoid*: FacoidIsPosInside, \
 const Pyramidoid*: PyramidoidIsPosInside, \
 const Spheroid*: SpheroidIsPosInside, \
 default: PBErrInvalidPolymorphism)(Shap, VecPos)
```

```
#define ShapoidGetPosDepth(Shap, VecPos) _Generic(Shap, \
 Shapoid*: _ShapoidGetPosDepth, \
 Facoid*: FacoidGetPosDepth, \
 Pyramidoid*: PyramidoidGetPosDepth, \
 Spheroid*: SpheroidGetPosDepth, \
 const Shapoid*: _ShapoidGetPosDepth, \
 const Facoid*: FacoidGetPosDepth, \
 const Pyramidoid*: PyramidoidGetPosDepth, \
 const Spheroid*: SpheroidGetPosDepth, \
 default: PBErrInvalidPolymorphism)(Shap, (VecFloat*)VecPos)
#define ShapoidIsInter(ShapA, ShapB) _Generic(ShapA, \
 Spheroid*: _Generic(ShapB, \
   Spheroid*: _SpheroidIsInterSpheroid, \
   const Spheroid*: _SpheroidIsInterSpheroid, \
   default: PBErrInvalidPolymorphism), \
 const Spheroid*: _Generic(ShapB, \
   Spheroid*: _SpheroidIsInterSpheroid, \
   const Spheroid*: _SpheroidIsInterSpheroid, \
   default: PBErrInvalidPolymorphism), \
 default: PBErrInvalidPolymorphism) (ShapA, ShapB)
#define ShapoidGetBoundingRadius(Shap) _Generic(Shap, \
 Shapoid*: _ShapoidGetBoundingRadius, \
 Pyramidoid*: _ShapoidGetBoundingRadius, \
 Facoid*: _ShapoidGetBoundingRadius, \
 Spheroid*: _ShapoidGetBoundingRadius, \
 const Shapoid*: _ShapoidGetBoundingRadius, \
 const Pyramidoid*: _ShapoidGetBoundingRadius, \
 const Facoid*: _ShapoidGetBoundingRadius, \
 const Spheroid*: _ShapoidGetBoundingRadius, \
 default: PBErrInvalidPolymorphism) ((const Shapoid*)(Shap))
// ======== Inliner ========
#if BUILDMODE != 0
#include "shapoid-inline.c"
#endif
#endif
```

#### 3 Code

#### 3.1 shapoid.c

```
// ----- SHAPOID.C ------

// ----- Include -----

#include "shapoid.h"

#if BUILDMODE == 0

#include "shapoid-inline.c"

#endif
```

```
// ----- Shapoid
// ======== Define ========
const char* ShapoidTypeString[3] = {
  (const char*)"Facoid", (const char*)"Spheroid",
  (const char*)"Pyramidoid"};
// ======== Functions implementation ===========
// Create a Shapoid of dimension 'dim' and type 'type', default values:
// _pos = null vector
// _axis[d] = unit vector along dimension d
Shapoid* ShapoidCreate(const int dim, const ShapoidType type) {
#if BUILDMODE == 0
 if (dim <= 0) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Invalid dimension (%d>0)", dim);
   PBErrCatch(ShapoidErr);
 }
#endif
 // Declare a vector used for initialisation
 VecShort2D d = VecShortCreateStatic2D();
  // Declare a identity matrix used for initialisation
 VecSet(&d, 0, dim);
 VecSet(&d, 1, dim);
  MatFloat* mat = MatFloatCreate(&d);
 MatSetIdentity(mat);
  // Allocate memory
 Shapoid* that = NULL;
  if (type == ShapoidTypeSpheroid)
    that = PBErrMalloc(ShapoidErr, sizeof(Spheroid));
    that = PBErrMalloc(ShapoidErr, sizeof(Shapoid));
  // Init pointers
 that->_pos = NULL;
  that->_axis = NULL;
  that->_sysLinEqImport = NULL;
  // Set the dimension and type
  that->_type = type;
  that->_dim = dim;
  // Allocate memory for position
  that->_pos = VecFloatCreate(dim);
  // Allocate memory for array of axis
  that->_axis = PBErrMalloc(ShapoidErr, sizeof(VecFloat*) * dim);
  for (int iAxis = dim; iAxis--;)
   that->_axis[iAxis] = NULL;
  // Allocate memory for each axis
 for (int iAxis = 0; iAxis < dim; ++iAxis) {</pre>
    // Allocate memory for position
    that->_axis[iAxis] = VecFloatCreate(dim);
    // Set value of the axis
   VecSet(that->_axis[iAxis], iAxis, 1.0);
 // Create the linear system for coordinate importation
  that->_sysLinEqImport = SysLinEqCreate(mat, (VecFloat*)NULL);
  // Free memory
 MatFree(&mat);
  // Specific properties of Spheroid
  if (type == ShapoidTypeSpheroid) {
    ((Spheroid*)that)->_majAxis = 0;
    ((Spheroid*)that)->_minAxis = 0;
```

```
// Return the new Shapoid
 return that;
// Clone a Shapoid
Shapoid* _ShapoidClone(const Shapoid* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
  // Create a clone
 Shapoid* clone = ShapoidCreate(that->_dim, that->_type);
 // Set the position and axis of the clone
 ShapoidSetPos(clone, that->_pos);
  for (int iAxis = clone->_dim; iAxis--;)
   VecCopy(clone->_axis[iAxis], that->_axis[iAxis]);
 ShapoidUpdateSysLinEqImport(clone);
  // Clone the SysLinEq
 SysLinEqFree(&(clone->_sysLinEqImport));
  clone->_sysLinEqImport = SysLinEqClone(that->_sysLinEqImport);
  // If it's a spheroid, copy the spheroid properties too
  if (that->_type == ShapoidTypeSpheroid) {
    ((Spheroid*)clone)->_majAxis = ((Spheroid*)that)->_majAxis;
    ((Spheroid*)clone)->_minAxis = ((Spheroid*)that)->_minAxis;
 // Return the clone
 return clone;
// Free memory used by a Shapoid
void _ShapoidFree(Shapoid** that) {
 // Check argument
 if (that == NULL || *that == NULL)
   return;
  // Free memory
 for (int iAxis = (*that)->_dim; iAxis--;)
   VecFree((*that)->_axis + iAxis);
  free((*that)->_axis);
 VecFree(&((*that)->_pos));
 SysLinEqFree(&((*that)->_sysLinEqImport));
 free(*that):
  *that = NULL;
// Function which return the JSON encoding of 'that'
JSONNode* _ShapoidEncodeAsJSON(const Shapoid* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
   PBErrCatch(PBMathErr);
 }
#endif
  // Create the JSON structure
  JSONNode* json = JSONCreate();
  // Declare a buffer to convert value into string
 char val[100];
  // Encode the dimension
```

```
sprintf(val, "%d", that->_dim);
  JSONAddProp(json, "_dim", val);
  // Encode the type
  sprintf(val, "%u", that->_type);
JSONAddProp(json, "_type", val);
  // Encode the position
  JSONAddProp(json, "_pos", VecEncodeAsJSON(ShapoidPos(that)));
  // Encode the axis
  JSONArrayStruct setAxis = JSONArrayStructCreateStatic();
  // For each axis
  for (int iAxis = 0; iAxis < that->_dim; ++iAxis)
    JSONArrayStructAdd(&setAxis,
      VecEncodeAsJSON(ShapoidAxis(that, iAxis)));
  JSONAddProp(json, "_axis", &setAxis);
  // Free memory
  JSONArrayStructFlush(&setAxis);
  // Return the created JSON
  return json;
// Function which decode from JSON encoding 'json' to 'that'
bool _ShapoidDecodeAsJSON(Shapoid** that, const JSONNode* const json) {
#if BUILDMODE == 0
  if (that == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'that' is null");
    PBErrCatch(PBMathErr);
  if (json == NULL) {
    PBMathErr->_type = PBErrTypeNullPointer;
    sprintf(PBMathErr->_msg, "'json' is null");
    PBErrCatch(PBMathErr);
#endif
  // If 'that' is already allocated
  if (*that != NULL)
   // Free memory
    ShapoidFree(that);
  // Get the dim from the JSON
  JSONNode* prop = JSONProperty(json, "_dim");
  if (prop == NULL) {
   return false;
  int dim = atoi(JSONLabel(JSONValue(prop, 0)));
  // Get the type from the JSON
  prop = JSONProperty(json, "_type");
  if (prop == NULL) {
   return false;
  ShapoidType type = atoi(JSONLabel(JSONValue(prop, 0)));
  // If data are invalid
  if (dim <= 0)
    return false;
  // Allocate memory
  *that = ShapoidCreate(dim, type);
  // Get the position from the {\tt JSON}
  prop = JSONProperty(json, "_pos");
  if (prop == NULL) {
    return false;
  if (!VecDecodeAsJSON(&((*that)->_pos), prop)) {
    return false;
```

```
// Decode the axis
  prop = JSONProperty(json, "_axis");
  if (prop == NULL) {
    return false;
  if (JSONGetNbValue(prop) != dim) {
    return false;
  for (int iAxis = 0; iAxis < dim; ++iAxis) {</pre>
    JSONNode* axis = JSONValue(prop, iAxis);
    if (!VecDecodeAsJSON((*that)->_axis + iAxis, axis))
      return false;
    // If the axis is not of the correct dimension
    if (VecGetDim((*that)->_axis[iAxis]) != (*that)->_dim)
      return false;
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(*that);
  // If it's a Spheroid
  if ((*that)->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)*that);
  // Return the success code
 return true;
// Load the Shapoid from the stream
// If the Shapoid is already allocated, it is freed before loading
// Return true upon success else false
bool _ShapoidLoad(Shapoid** that, FILE* const stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (stream == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'stream' is null");
    PBErrCatch(ShapoidErr);
  // Declare a json to load the encoded data
  JSONNode* json = JSONCreate();
  // Load the whole encoded data
  if (!JSONLoad(json, stream)) {
   return false;
  // Decode the data from the {\tt JSON}
  if (!ShapoidDecodeAsJSON(that, json)) {
   return false;
  }
  // Free the memory used by the JSON
  JSONFree(&json);
  // Return success code
 return true;
// Save the Shapoid to the stream
// If 'compact' equals true it saves in compact form, else it saves in
// readable form
```

```
// Return true upon success else false
bool _ShapoidSave(const Shapoid* const that, FILE* const stream,
  const bool compact) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (stream == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'stream' is null");
    PBErrCatch(ShapoidErr);
#endif
  // Get the JSON encoding
  JSONNode* json = ShapoidEncodeAsJSON(that);
  // Save the JSON
  if (!JSONSave(json, stream, compact)) {
    return false;
  1
  // Free memory
  JSONFree(&json);
  // Return success code
 return true;
// Print the Shapoid on 'stream'
void _ShapoidPrintln(const Shapoid* const that, FILE* const stream) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (stream == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'stream' is null");
    PBErrCatch(ShapoidErr);
  }
#endif
  \ensuremath{//} Print the Shapoid
  fprintf(stream, "Type: %s\n", ShapoidTypeString[that->_type]);
  fprintf(stream, "Dim: %d\n", that->_dim);
fprintf(stream, "Pos: ");
  VecPrint(that->_pos, stream);
  fprintf(stream, \ "\n");
  for (int iAxis = 0; iAxis < that->_dim; ++iAxis) {
    fprintf(stream, "Axis(%d): ", iAxis);
    VecPrint(that->_axis[iAxis], stream);
    fprintf(stream, "\n");
}
// Get a bounding box of the Shapoid. The bounding box is aligned
// on the standard coordinate system (its axis are colinear with
// the axis of the standard coordinate system).
// The bounding box is returned as a Facoid, which position is
// at the minimum value along each axis.
Facoid* _ShapoidGetBoundingBox(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
```

```
ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
    PBErrCatch(ShapoidErr);
#endif
  // If the Shapoid is a Facoid
  if (that->_type == ShapoidTypeFacoid) {
    return FacoidGetBoundingBox((Facoid*)that);
  // Else, if the Shapoid is a Pyramidoid
  } else if (that->_type == ShapoidTypePyramidoid) {
    return PyramidoidGetBoundingBox((Pyramidoid*)that);
  // Else, if the Shapoid is a Spheroid
  } else if (that->_type == ShapoidTypeSpheroid) {
    return SpheroidGetBoundingBox((Spheroid*)that);
  } else {
    return NULL;
Facoid* FacoidGetBoundingBox(const Facoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  // Declare a variable to memorize the result
  Facoid* res = FacoidCreate(ShapoidGetDim(that));
  // For each axis
  for (int dim = ShapoidGetDim(that); dim--;) {
    // Declare a variable to memorize the bound of the interval on
    // this axis
    float bound[2];
    bound[0] = bound[1] = VecGet(((Shapoid*)that)->_pos, dim);
    // For each parameter
    for (int param = ShapoidGetDim(that); param--;) {
      // Get the value of the axis influencing the current dimension
      float v = VecGet(((Shapoid*)that)->_axis[param], dim);
      \ensuremath{//} If the value is negative, update the minimum bound
      if (v < 0.0)
        bound[0] += v;
      // Else, if the value is negative, update the minimum bound
        bound[1] += v;
    }
    // Memorize the result
    VecSet(((Shapoid*)res)->_pos, dim, bound[0]);
    VecSet(((Shapoid*)res)->_axis[dim], dim, bound[1] - bound[0]);
  // Return the result
  return res;
Facoid* PyramidoidGetBoundingBox(const Pyramidoid* const that) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  // Declare a variable to memorize the result
  Facoid* res = FacoidCreate(ShapoidGetDim(that));
  // For each axis
  for (int dim = ShapoidGetDim(that); dim--;) {
    ^{-} Declare a variable to memorize the bound of the interval on
    // this axis
    float bound[2];
    bound[0] = bound[1] = 0.0;
    // For each parameter
    for (int param = ShapoidGetDim(that); param--;) {
      // Get the value of the axis influencing the current dimension
      float v = VecGet(((Shapoid*)that)->_axis[param], dim);
      // Search the min and max values
      if (v < bound[0])
        bound[0] = v;
      if (v > bound[1])
        bound[1] = v;
    if (bound[0] > 0.0)
      bound[0] = 0.0;
    if (bound[1] < 0.0)
      bound[1] = 0.0;
    // Memorize the result
    VecSet(((Shapoid*)res)->_pos, dim,
      ShapoidPosGet(that, dim) + bound[0]);
    VecSet(((Shapoid*)res)->_axis[dim], dim, bound[1] - bound[0]);
  // Return the result
  return res;
Facoid* SpheroidGetBoundingBox(const Spheroid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  \ensuremath{//} Declare a variable to memorize the result
  Facoid* res = FacoidCreate(ShapoidGetDim(that));
  // In case of a Spheroid, things get complicate
  // We'll approximate the bounding box of the Spheroid
  // with the one of the same Spheroid viewed as a Facoid
  // and simply take care that the _pos is at the center of the
  // Spheroid
  // For each axis
  for (int dim = ShapoidGetDim(that); dim--;) {
    \ensuremath{//} Declare a variable to memorize the bound of the interval on
    // this axis
    float bound[2];
    bound[0] = VecGet(((Shapoid*)that)->_pos, dim);
    // Correct position
    // For each parameter
    for (int param = ShapoidGetDim(that); param--;) {
```

```
// Get the value of the axis influencing the current dimension
      float v = VecGet(((Shapoid*)that)->_axis[param], dim);
      // Correct the pos
      bound[0] -= 0.5 * v;
    bound[1] = bound[0];
    // For each parameter
    for (int param = ShapoidGetDim(that); param--;) {
      // Get the value of the axis influencing the current dimension
      float v = VecGet(((Shapoid*)that)->_axis[param], dim);
      // If the value is negative, update the minimum bound
      if (v < 0.0)
        bound[0] += v;
      // Else, if the value is negative, update the minimum bound
      else
        bound[1] += v;
    // Memorize the result
    VecSet(((Shapoid*)res)->_pos, dim, bound[0]);
    VecSet(((Shapoid*)res)->_axis[dim], dim, bound[1] - bound[0]);
  // Return the result
  return res;
// Get the bounding box of a set of Facoid. The bounding box is aligned
// on the standard coordinate system (its axis are colinear with
// the axis of the standard coordinate system).
// The bounding box is returned as a Facoid, which position is
// at the minimum value along each axis.
Facoid* ShapoidGetBoundingBoxSet(const GSetShapoid* const set) {
#if BUILDMODE == 0
  if (set == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'set' is null");
    PBErrCatch(ShapoidErr);
  if (GSetNbElem(set) > 0) {
    GSetIterForward iter = GSetIterForwardCreateStatic(set);
    int dim = ((Shapoid*)GSetIterGet(&iter))->_dim;
    do {
      if (((Shapoid*)GSetIterGet(&iter))->_dim != dim) {
        ShapoidErr->_type = PBErrTypeInvalidArg;
        sprintf(ShapoidErr->_msg,
          "'set' contains Shapoids of various dimensions");
        PBErrCatch(ShapoidErr);
    } while (GSetIterStep(&iter));
  }
#endif
  // Declare a variable for the result
  Facoid* res = NULL;
  if (GSetNbElem(set) > 0) {
    // Declare an interator on the elements of the set
    GSetIterForward iter = GSetIterForwardCreateStatic(set);
    // Loop on element of the set
    do {
      // Declare a pointer to the Facoid
      Shapoid* shapoid = GSetIterGet(&iter);
      // If it's the first Facoid in the set
      if (res == NULL) {
        // Get the bounding box of this shapoid
```

```
res = ShapoidGetBoundingBox(shapoid);
      // Else, this is not the first Shapoid in the set
      } else {
        // Get the bounding box of this shapoid
        Facoid* bound = ShapoidGetBoundingBox(shapoid);
        // For each dimension
        for (int iDim = ShapoidGetDim(res); iDim--;) {
          // Update the bounding box
          if (VecGet(((Shapoid*)bound)->_pos, iDim) <</pre>
            VecGet(((Shapoid*)res)->_pos, iDim)) {
            VecSetAdd(((Shapoid*)res)->_axis[iDim], iDim,
              VecGet(((Shapoid*)res)->_pos, iDim)
              VecGet(((Shapoid*)bound)->_pos, iDim));
            VecSet(((Shapoid*)res)->_pos, iDim,
            VecGet(((Shapoid*)bound)->_pos, iDim));
          if (VecGet(((Shapoid*)bound)->_pos, iDim) +
            VecGet(((Shapoid*)bound)->_axis[iDim], iDim) >
            VecGet(((Shapoid*)res)->_pos, iDim) +
            VecGet(((Shapoid*)res)->_axis[iDim], iDim))
            VecSetAdd(((Shapoid*)res)->_axis[iDim], iDim,
              VecGet(((Shapoid*)bound)->_axis[iDim], iDim) -
              VecGet(((Shapoid*)res)->_pos, iDim));
        // Free memory used by the bounding box
       ShapoidFree(&bound);
   } while (GSetIterStep(&iter));
 // Return the result
 return res;
// Get the percentage of 'tho' included 'that' (in [0.0, 1.0])
// 0.0 -> 'tho' is completely outside of 'that'
// 1.0 -> 'tho' is completely inside of 'that'
// 'that' and 'tho' must me of same dimensions
// delta is the step of the algorithm (in ]0.0, 1.0])
// small -> slow but precise
// big -> fast but rough
float _ShapoidGetCoverageDelta(const Shapoid* const that,
 const Shapoid* const tho, const float delta) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (tho == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'tho' is null");
   PBErrCatch(ShapoidErr);
  if (ShapoidGetDim(that) != ShapoidGetDim(tho)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "Shapoids dimensions are different (%d==%d)",
      ShapoidGetDim(that), ShapoidGetDim(tho));
    PBErrCatch(ShapoidErr);
  if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
```

```
that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
    PBErrCatch(ShapoidErr);
  }
#endif
  // Declare variables to compute the result
  float ratio = 0.0;
  float sum = 0.0;
  // Declare variables for the relative and absolute position in 'tho'
  VecFloat* pRel = VecFloatCreate(ShapoidGetDim(that));
  VecFloat* pStd = NULL;
  // Declare a variable to memorize the last index in dimension
  int lastI = VecGetDim(pRel) - 1;
  // Declare a variable to memorize the max value of coordinates
  float max = 1.0;
  // If 'tho' is a spheroid, correct the start coordinates and range
  if (tho->_type == ShapoidTypeSpheroid) {
    for (int iDim = ShapoidGetDim(that); iDim--;)
      VecSet(pRel, iDim, -0.5);
  // Loop on relative coordinates
  while (VecGet(pRel, lastI) <= max + PBMATH_EPSILON) {</pre>
    // Get the coordinates in standard system
    pStd = ShapoidExportCoord(tho, pRel);
    // If this position is inside 'tho'
    if (ShapoidIsPosInside(tho, pStd) == true) {
      // If this position is inside 'that'
      if (ShapoidIsPosInside(that, pStd) == true)
        // Increment the ratio
        ratio += 1.0;
      sum += 1.0;
    }
    // Free memory
    VecFree(&pStd);
    // Step the relative coordinates
    int iDim = 0;
    while (iDim >= 0) {
      VecSetAdd(pRel, iDim, delta);
      if (iDim != lastI &&
        VecGet(pRel, iDim) > max + PBMATH_EPSILON) {
        VecSet(pRel, iDim, max - 1.0);
        ++iDim;
      } else {
        iDim = -1;
      }
   }
  \ensuremath{//} Finish the computation of the ratio
  ratio /= sum;
  // Free memory
  VecFree(&pRel);
  // Return the result
 return ratio;
// Add a copy of the Facoid 'that' to the GSet 'set' (containing
// other Facoid), taking care to avoid overlaping Facoid
// The copy of 'that' made be resized or divided
// The Facoid in the set and 'that' must be aligned with the
// coordinates system axis and have
```

```
// same dimensions
void FacoidAlignedAddClippedToSet(const Facoid* const that,
 GSetShapoid* const set) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (set == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'set' is null");
   PBErrCatch(ShapoidErr);
#endif
  // If the set is empty
 if (GSetNbElem(set) == 0) {
    // Add a clone of the facoid
    GSetAppend(set, FacoidClone(that));
  // Else, the set is not empty
 } else {
    // Create a set of sub facoid to be added and initialize it with a
    // clone of 'that'
    GSetShapoid setToAdd = GSetShapoidCreateStatic();
    GSetAppend(&setToAdd, FacoidClone(that));
    // For each sub facoid to add
    GSetIterForward iterToAdd = GSetIterForwardCreateStatic(&setToAdd);
    do {
     // Get the current facoid to add
     Facoid* facoidToAdd = GSetIterGet(&iterToAdd);
      // Declare a flag to skip the loop when possible
     bool flagSkip = false;
      // For each facoid in the set
     GSetIterForward iter = GSetIterForwardCreateStatic(set);
      do {
       // Get the current facoid
       Facoid* facoid = GSetIterGet(&iter);
        // If the facoid to be added is completely included into this
        // facoid
        if (FacoidAlignedIsInsideFacoidAligned(facoidToAdd, facoid)) {
          // This facoid doesn't need to be added, delete it
          ShapoidFree(&facoidToAdd);
          GSetIterSetData(&iterToAdd, NULL);
          // And skip the other facoids in the set
          flagSkip = true;
        // Else, if this facoid is completely include in the facoid to
        // be added
        } else if (FacoidAlignedIsInsideFacoidAligned(facoid,
          facoidToAdd)) {
          // Remove the facoid in the set
          ShapoidFree(&facoid);
          GSetIterSetData(&iter, NULL);
        // Else, if both facoid are in intersection
        } else if (!FacoidAlignedIsOutsideFacoidAligned(facoidToAdd,
          facoid)) {
          // Split the facoid to be added into new facoids
          // which cover the non intersecting area
          GSetShapoid* split =
            FacoidAlignedSplitExcludingFacoidAligned(facoidToAdd,
              facoid);
          GSetAppendSet(&setToAdd, split);
          GSetFree(&split);
```

```
// Delete the splitted facoid
          ShapoidFree(&facoidToAdd);
          GSetIterSetData(&iterToAdd, NULL);
          // And skip the other facoids in the set
          flagSkip = true;
        // Else the facoid to add is completely outside, leave it as
        // it is
     } while (!flagSkip && GSetIterStep(&iter));
    } while (GSetIterStep(&iterToAdd));
    // When we arrive here the set 'setToAdd' contains the facoids
    // to be added to 'set'
    GSetAppendSet(set, &setToAdd);
    // There may have been deleted facoid, ensure the resulting set
    // is clean by removing null pointer
    GSetRemoveAll(set, (Shapoid*)NULL);
    // Free memory used by \bar{t}he set of sub facoid to add
    GSetFlush(&setToAdd);
// Check if the Facoid 'that' is completely included into the Facoid
// 'facoid'
// Both Facoid must be aligned with the coordinates system
// 'that' and 'facoid' must have same dimensions and have
// same dimensions
// Return true if it is included, false else
bool FacoidAlignedIsInsideFacoidAligned(const Facoid* const that,
 const Facoid* const facoid) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (facoid == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'facoid' is null");
   PBErrCatch(ShapoidErr);
 if (ShapoidGetDim(that) != ShapoidGetDim(facoid)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' and 'facoid' have different dimensions (%d==%d)",
     ShapoidGetDim(that), ShapoidGetDim(facoid));
   PBErrCatch(ShapoidErr);
#endif
 // Check inclusion for each axis
 for (int iAxis = ShapoidGetDim(that); iAxis--;)
    // If 'that' is outside 'facoid' for this axis
    if (ShapoidPosGet(that, iAxis) <</pre>
     ShapoidPosGet(facoid, iAxis) ||
      ShapoidPosGet(that, iAxis) +
     ShapoidAxisGet(that, iAxis, iAxis) >
      ShapoidPosGet(facoid, iAxis) +
      ShapoidAxisGet(facoid, iAxis, iAxis))
      // Return false
      return false;
  // If we reach here it means 'that' is inside 'facoid', return true
 return true;
```

```
// Check if the Facoid 'that' is completely excluded from the Facoid
// Both Facoid must be aligned with the coordinates system and have
// same dimensions
// Return true if it is excluded, false else
bool FacoidAlignedIsOutsideFacoidAligned(const Facoid* const that,
  const Facoid* const facoid) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (facoid == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'facoid' is null");
   PBErrCatch(ShapoidErr);
 if (ShapoidGetDim(that) != ShapoidGetDim(facoid)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' and 'facoid' have different dimensions (%d==%d)",
     ShapoidGetDim(that), ShapoidGetDim(facoid));
   PBErrCatch(ShapoidErr);
#endif
  // Check exclusion for each axis
 for (int iAxis = ShapoidGetDim(that); iAxis--;)
    // If 'that' is outside 'facoid' for this axis
    if (ShapoidPosGet(that, iAxis) >
      ShapoidPosGet(facoid, iAxis) +
     ShapoidAxisGet(facoid, iAxis, iAxis) - PBMATH_EPSILON ||
      ShapoidPosGet(that, iAxis) +
      ShapoidAxisGet(that, iAxis, iAxis) <</pre>
     ShapoidPosGet(facoid, iAxis) + PBMATH_EPSILON)
      // Return true
     return true;
  // If we reach here it means 'that' intersects 'facoid', return false
 return false;
// Get a GSet of Facoid aligned with coordinates system covering the
// Facoid 'that' except for area in the Facoid 'facoid'
// Both Facoid must be aligned with the coordinates system and have
// same dimensions
{\tt GSetShapoid*}\ {\tt FacoidAlignedSplitExcludingFacoidAligned(}
 const Facoid* const that, const Facoid* const facoid) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (facoid == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'facoid' is null");
   PBErrCatch(ShapoidErr);
  if (ShapoidGetDim(that) != ShapoidGetDim(facoid)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
```

```
"'that' and 'facoid' have different dimensions (%d==%d)",
      ShapoidGetDim(that), ShapoidGetDim(facoid));
   PBErrCatch(ShapoidErr);
 }
#endif
  // Ladies and Gentleman, here comes the infamous "Gruyere Algorithm"
  // Declare the result GSet
  GSetShapoid* set = GSetShapoidCreate();
  // Declare a clone of the original facoid
 Facoid* src = FacoidClone(that);
  // For each axis
  for (int iAxis = ShapoidGetDim(that); iAxis--;) {
    // If 'src' has area on the left of 'facoid' along this axis
    if (ShapoidPosGet(src, iAxis) < ShapoidPosGet(facoid, iAxis)) {</pre>
      // Create the facoid made of this area
     Facoid* sub = FacoidClone(src);
     ShapoidAxisSet(sub, iAxis, iAxis,
        ShapoidPosGet(facoid, iAxis) - ShapoidPosGet(src, iAxis));
      // Add it to the result set
     GSetAppend(set, sub);
      // Chop the added area from 'src'
      ShapoidAxisSetAdd(src, iAxis, iAxis,
        -1.0 * ShapoidAxisGet(sub, iAxis, iAxis));
     ShapoidPosSet(src, iAxis, ShapoidPosGet(facoid, iAxis));
    // If 'src' has area on the right of 'facoid' along this axis
    if (ShapoidPosGet(src, iAxis) + ShapoidAxisGet(src, iAxis, iAxis) >
      ShapoidPosGet(facoid, iAxis) +
      ShapoidAxisGet(facoid, iAxis, iAxis)) {
      // Create the facoid made of this area
      Facoid* sub = FacoidClone(src);
      ShapoidAxisSet(sub, iAxis, iAxis,
        (ShapoidPosGet(src, iAxis) +
        ShapoidAxisGet(src, iAxis, iAxis)) -
        (ShapoidPosGet(facoid, iAxis) +
        ShapoidAxisGet(facoid, iAxis, iAxis)));
      ShapoidPosSet(sub, iAxis, ShapoidPosGet(facoid, iAxis) +
        ShapoidAxisGet(facoid, iAxis, iAxis));
      // Add it to the result set
      GSetAppend(set, sub);
      // Chop the added area from 'src'
     ShapoidAxisSetAdd(src, iAxis, iAxis,
        -1.0 * ShapoidAxisGet(sub, iAxis, iAxis));
    // If 'src' is empty
    if (ISEQUALF(ShapoidAxisGet(src, iAxis, iAxis), 0.0))
      // End the loop
      iAxis = 0;
  // Free memory
 ShapoidFree(&src);
 // Return the result set
 return set;
// Return true if 'that' intersects 'tho'
// Return false else
// 'that' and 'tho' must have same dimension
// https://hal.inria.fr/hal-00646511/PDF/CCD.3.0.pdf
bool _SpheroidIsInterSpheroid(const Spheroid* const that,
 const Spheroid* const tho) {
#if BUILDMODE == 0
```

```
if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (tho == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'tho' is null");
   PBErrCatch(ShapoidErr);
 if (ShapoidGetDim(that) != ShapoidGetDim(tho)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' and 'tho' have different dimensions (%d==%d)",
      ShapoidGetDim(that), ShapoidGetDim(tho));
   PBErrCatch(ShapoidErr);
 }
#endif
  // Create the projection of 'tho' in 'that' 's coordinates space
  Spheroid* proj = SpheroidCreate(ShapoidGetDim(tho));
  VecFloat* v = ShapoidImportCoord(that, ShapoidPos(tho));
 ShapoidSetPos(proj, v);
 VecFree(&v);
  for (int iAxis = ShapoidGetDim(tho); iAxis--;) {
    v = ShapoidImportCoord(that, ShapoidAxis(tho, iAxis));
   ShapoidSetAxis(proj, iAxis, v);
    VecFree(&v);
 }
  // Declare a variable to memorize the distance to the origin of
 // 'that' 's coordinate system
 float dist = VecNorm(ShapoidPos(proj));
  // Check for trivial cases
  float majRadius = 0.5 * VecNorm(ShapoidAxis(proj, proj->_majAxis));
  if (dist > majRadius + 0.5) {
    ShapoidFree(&proj);
    VecFree(&v):
    return false:
  } else if (proj->_majAxis == proj->_minAxis) {
    ShapoidFree(&proj);
    VecFree(&v);
   return true;
 float minRadius = 0.5 * VecNorm(ShapoidAxis(proj, proj->_minAxis));
  if (dist <= minRadius + 0.5) {</pre>
    ShapoidFree(&proj);
    VecFree(&v);
   return true;
 // Non trivial case
  // Search a position in the projection of 'tho' less than 1.0 units
  // from the origin in 'that' 's coordinates space
  // Declare a variable to move in the projection's coordinates space
 VecFloat* pos = VecFloatCreate(ShapoidGetDim(tho));
  // Declare a variable to memorize the derivative
  VecFloat* dPos = VecFloatCreate(ShapoidGetDim(tho));
  // Declare a variable to memorize the step for derivate calculation
  float delta = 0.01;
  // Declare a flag to stop the loop in case of deadlock
  bool flag = false;
  // Loop until we find a solution or deadlock
  while (dist > 0.5 && !flag) {
    // Calculate the derivative along each axis
```

```
v = VecFloatCreate(VecGetDim(pos));
    for (int iAxis = ShapoidGetDim(tho); iAxis--;) {
      // Copy the current position
     VecCopy(v, pos);
      \ensuremath{//} Move a delta along the current axis
      VecSetAdd(v, iAxis, delta);
      // Get the cooridnate in 'that' 's coordinates system
      VecFloat* w = ShapoidExportCoord(proj, v);
      // Calculate the distance ot origin of 'that' 's coordinates
      // system
     float dp = VecNorm(w);
      // Free memory
     VecFree(&w);
      // Do the same thing with minus delta
     VecSetAdd(v, iAxis, -2.0 * delta);
     w = ShapoidExportCoord(proj, v);
     float dm = VecNorm(w);
     VecFree(&w);
      // Calculate the derivative along the current axis
      VecSet(dPos, iAxis, (dp - dm) / (2.0 * delta));
   }
    // Free memory
    VecFree(&v);
    // Move toward better solution
    // Declare a variable to memorize the next position
    VecFloat* nPos = VecGetOp(pos, 1.0, dPos, -1.0);
    // Ensure the position stay inside the Spheroid
    if (VecNorm(nPos) > 0.5) {
     VecNormalise(nPos);
     VecScale(nPos, 0.5);
    \ensuremath{//} If we are stuck to the same position
    if (VecDist(pos, nPos) < PBMATH_EPSILON)</pre>
     // Stop the loop
      flag = true;
    // Else we keep moving
    else {
      VecCopy(pos, nPos);
     // Update the current distance
     v = ShapoidExportCoord(proj, pos);
     dist = VecNorm(v);
     VecFree(&v);
    // Free memory
    VecFree(&nPos);
  // Free memory
 ShapoidFree(&proj);
 VecFree(&pos);
 VecFree(&dPos);
  // If we have found a position less than one unit from the origin
  // of 'that' 's coordinates system
  if (dist <= 0.5)
    // The spheroids intersect
   return true;
  else
    // The spheroids do not intersect
    return false;
// Update the major and minor axis of the Spheroid 'that'
void SpheroidUpdateMajMinAxis(Spheroid* const that) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  that->_{maj}Axis = 0;
  float maj = VecNorm(ShapoidAxis(that, 0));
  that->_{minAxis} = 0;
  float min = maj;
  for (int iAxis = ShapoidGetDim(that); iAxis-- && iAxis != 0;) {
    float n = VecNorm(ShapoidAxis(that, iAxis));
    if (n > maj) {
     maj = n;
     that->_majAxis = iAxis;
    } else if (n < min) {</pre>
     min = n;
      that->_minAxis = iAxis;
 }
}
// Get the maximum distance from the center of the Shapoid 'that' and
// its surface
// Currenty only defined for spheroid, return 0.0 else
float _ShapoidGetBoundingRadius(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  if (ShapoidGetType(that) == ShapoidTypeSpheroid) {
      VecNorm(ShapoidAxis(that, ((Spheroid*)that)->_majAxis)) * 0.5;
  return 0.0;
// ----- ShapoidIter
// ========= Functions declaration ==========
// Step the ShapoidIter 'that' for a Facoid
// Return false if the iterator is at its end and couldn't be stepped
bool _ShapoidIterStepFacoid(ShapoidIter* const that);
// Step the ShapoidIter 'that' for a Pyramidoid
// Return false if the iterator is at its end and couldn't be stepped
bool _ShapoidIterStepPyramidoid(ShapoidIter* const that);
// Step the ShapoidIter 'that' for a Spheroid
// Return false if the iterator is at its end and couldn't be stepped
bool _ShapoidIterStepSpheroid(ShapoidIter* const that);
// ====== Functions implementation =========
// Create a new iterator on the Shapoid 'shap' with a step of 'delta'
// (step on the internal coordinates of the Shapoid)
// The iterator is initialized and ready to be stepped
```

```
ShapoidIter _ShapoidIterCreateStatic(const Shapoid* const shap,
 const VecFloat* const delta) {
#if BUILDMODE == 0
 if (shap == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'shap' is null");
   PBErrCatch(ShapoidErr);
 if (delta == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'delta' is null");
   PBErrCatch(ShapoidErr);
 if (VecGetDim(delta) != ShapoidGetDim(shap)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'delta' dimensions and 'shap' dimensions don't match (%d==%d)",
     VecGetDim(delta), ShapoidGetDim(shap));
   PBErrCatch(ShapoidErr);
#endif
  // Declare the new iterator
 ShapoidIter iter;
 // Set properties
 iter._shap = shap;
 iter._delta = VecClone(delta);
  iter._pos = VecFloatCreate(VecGetDim(delta));
  // Init the position
 ShapoidIterInit(&iter);
 // Return the new iterator
 return iter;
// Free the memory used by the ShapoidIter 'that'
void ShapoidIterFreeStatic(ShapoidIter* const that) {
 // Check argument
 if (that == NULL)
    // Nothing to do
   return;
  // Free memory
 VecFree(&(that->_delta));
 VecFree(&(that->_pos));
// Reinitialise the ShapoidIter 'that' to its starting position
void ShapoidIterInit(ShapoidIter* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
 // Initialise according to the type of Shapoid
  switch(ShapoidGetType(that->_shap)) {
   case ShapoidTypeFacoid:
    case ShapoidTypePyramidoid:
     VecSetNull(that->_pos);
     break;
    case ShapoidTypeSpheroid:
     VecSetNull(that->_pos);
      VecSet(that->_pos, VecGetDim(that->_pos) - 1, -0.5);
```

```
break;
    default:
      break;
}
// Step the ShapoidIter 'that'
// Return false if the iterator is at its end and couldn't be stepped
bool ShapoidIterStep(ShapoidIter* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  }
#endif
  // Declare a flag for the return value
  bool flag = true;
  // Step according to the type of Shapoid
  switch(ShapoidGetType(that->_shap)) {
    {\tt case \ ShapoidTypeFacoid:}
      flag = _ShapoidIterStepFacoid(that);
      break;
    \verb|case ShapoidTypePyramidoid:|\\
      flag = _ShapoidIterStepPyramidoid(that);
      break;
    case ShapoidTypeSpheroid:
      flag = _ShapoidIterStepSpheroid(that);
      break:
    default:
      break;
 return flag;
}
// Step the ShapoidIter 'that' for a Facoid
// Return false if the iterator is at its end and couldn't be stepped
bool _ShapoidIterStepFacoid(ShapoidIter* const that) {
  ^{-} // Declare a variable for the returned flag
  bool ret = true;
  // Declare a variable to memorise the dimension currently increasing
  int iDim = VecGetDim(that->_pos) - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    VecSetAdd(that->_pos, iDim, VecGet(that->_delta, iDim));
    if (VecGet(that->_pos, iDim) > 1.0 + PBMATH_EPSILON) {
      VecSet(that->_pos, iDim, 0.0);
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
  return ret;
// Step the ShapoidIter 'that' for a Pyramidoid
// Return false if the iterator is at its end and couldn't be stepped
```

```
bool _ShapoidIterStepPyramidoid(ShapoidIter* const that) {
  // Declare a variable for the returned flag
  bool ret = true;
  \ensuremath{//} Declare a variable to memorise the dimension currently increasing
  int iDim = VecGetDim(that->_pos) - 1;
  // Declare a flag for the loop condition
  bool flag = true;
  // Increment
  do {
    VecSetAdd(that->_pos, iDim, VecGet(that->_delta, iDim));
    float sum = 0.0;
    for (int iAxis = VecGetDim(that->_pos); iAxis--;)
      sum += VecGet(that->_pos, iAxis);
    if (sum > 1.0 + PBMATH_EPSILON) {
      VecSet(that->_pos, iDim, 0.0);
      --iDim;
    } else {
      flag = false;
  } while (iDim >= 0 && flag == true);
  if (iDim == -1)
    ret = false;
  // Return the flag
 return ret;
// Step the ShapoidIter 'that' for a Spheroid
// Return false if the iterator is at its end and couldn't be stepped
bool _ShapoidIterStepSpheroid(ShapoidIter* const that) {
  // Declare a variable to memorise the dimension currently increasing
  int iDim = 0;
  // Declare a flag for the loop condition
  bool flag = true;
  // Declare a variable to memorize the norm of the current position
  float norm = VecNorm(that->_pos);
  // Ladies and Gentleman, here comes the infamous "Worm Algorithm"
  // Increment from the first axis
  for (iDim = 0; iDim < VecGetDim(that->_pos) && flag == true; ++iDim) {
    float prevNorm = norm;
    // Try to step in this axis
    VecSetAdd(that->_pos, iDim, VecGet(that->_delta, iDim));
    // Get the norm of the new position
    norm = VecNorm(that->_pos);
    // If we have just jumped over the boundary if (prevNorm < 0.5 - PBMATH_EPSILON &&
      norm >= 0.5 + PBMATH_EPSILON) {
      // Correct the step to reach exactly the boundary
      // Set the current axis to relax the constraint
      VecSet(that->_pos, iDim, 0.0);
      // Calculate the value for this axis which put back the position
      // at the boundary of the Spheroid (on positive side as we want
      // the end of the boundary)
      norm = VecNorm(that->_pos);
      float val = 0.5 * sqrt(-4.0 * (fastpow(norm, 2) - 0.25));
      VecSet(that->_pos, iDim, val);
      // Correct the norm
      norm = 0.5;
      // We could step on this axis, stop here
      flag = false;
      // To cancel the increment in the loop
      --iDim:
    } else {
```

```
// If the new position is out of bound it means we reach the
    // boundary
    if (norm >= 0.5 + PBMATH_EPSILON) {
      // Set the current axis to 0.0 to relax the constraint on
      // other axis
      VecSet(that->_pos, iDim, 0.0);
    } else {
      // We could step on this axis, stop here
      flag = false;
      \ensuremath{//} To cancel the increment in the loop
      --iDim;
 }
// If we could step, it has modified the constraint on the previous
// axis which must then be updated
if (flag == false) {
  --iDim;
  // If there is actually a previous axis
  if (iDim >= 0) {
    // Calculate the value for this axis which put back the position
    // at the boundary of the Spheroid (on negative side as we will
    // increment from there)
    float val = VecGet(that->_pos, iDim) +
      0.5 * (-2.0 * VecGet(that->_pos, iDim) -
      sqrt(4.0 * (fastpow(VecGet(that->_pos, iDim), 2) -
      fastpow(norm, 2) + 0.25)));
    VecSet(that->_pos, iDim, val);
// Return the negative of the flag
return !flag;
```

## 3.2 shapoid-inline.c

```
// ======= SHAPOID-INLINE.C =========
// ----- Shapoid
// ======= Functions implementation ==========
// Get the dimension of the Shapoid
#if BUILDMODE != 0
inline
int _ShapoidGetDim(const Shapoid* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
   sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
 // Return the dimension
 return that->_dim;
// Get the dimension of the Shapoid
#if BUILDMODE != 0
```

```
inline
#endif
ShapoidType _ShapoidGetType(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
 // Return the type
 return that->_type;
// Get the type of the Shapoid as a string
// Return a pointer to a constant string (not to be freed)
#if BUILDMODE != 0
inline
#endif
const char* _ShapoidGetTypeAsString(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
  // Return the type
  return ShapoidTypeString[that->_type];
// Return a VecFloat equals to the position of the Shapoid
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidGetPos(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  // Return a clone of the position
 return VecClone(that->_pos);
// Return a VecFloat equals to the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidGetAxis(const Shapoid* const that, const int dim) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (dim < 0 || dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
```

```
PBErrCatch(ShapoidErr);
  }
#endif
 // Return a clone of the axis
 return VecClone(that->_axis[dim]);
// Return the position of the Shapoid
#if BUILDMODE != 0
inline
#endif
const VecFloat* _ShapoidPos(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  }
#endif
  // Return the position
 return that->_pos;
// Return the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
const VecFloat* _ShapoidAxis(const Shapoid* const that, const int dim) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (\dim < 0 \mid \mid \dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
   PBErrCatch(ShapoidErr);
 }
#endif
  // Return the axis
 return that->_axis[dim];
// Set the position of the Shapoid to 'pos'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetPos(Shapoid* const that, const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != that->_dim) {
```

```
ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      VecGetDim(pos), that->_dim);
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the position
  VecCopy(that->_pos, pos);
// Set the 'iElem'-th value of the position of the Shapoid to 'val'
#if BUILDMODE != 0
inline
#endif
void _ShapoidPosSet(Shapoid* const that, const int iElem,
  const float val) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (iElem < 0 || iElem >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'iElem' is invalid (0<=%d<%d)",
      iElem, that->_dim);
    PBErrCatch(ShapoidErr);
#endif
  // Set the position
  VecSet(that->_pos, iElem, val);
// Set the 'iElem'-th value of the position of the Shapoid to 'val'
// added to its current value
#if BUILDMODE != 0
inline
\verb"void _ShapoidPosSetAdd(Shapoid* const that, const int iElem",
  const float val) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (iElem < 0 || iElem >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'iElem' is invalid (0<=%d<%d)",
      iElem, that->_dim);
   PBErrCatch(ShapoidErr);
 }
#endif
  // Set the position
  VecSetAdd(that->_pos, iElem, val);
// Set the 'iElem'-th value of the position of the Shapoid to 'val'
#if BUILDMODE != 0
inline
#endif
float _ShapoidPosGet(const Shapoid* const that, const int iElem) {
```

```
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (iElem < 0 || iElem >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'iElem' is invalid (0<=%d<%d)",
      iElem, that->_dim);
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the position
  return VecGet(that->_pos, iElem);
// Set the position of the Shapoid such as its center is at 'pos'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetCenterPos(Shapoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      VecGetDim(pos), that->_dim);
    PBErrCatch(ShapoidErr);
  }
#endif
  VecFloat* v = ShapoidGetCenter(that);
  VecOp(v, -1.0, ShapoidPos(that), 1.0);
  VecOp(v, 1.0, pos, 1.0);
  ShapoidSetPos(that, v);
  VecFree(&v);
}
// Set the 'dim'-th axis of the Shapoid to 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidSetAxis(Shapoid* const that, const int dim,
 const VecFloat* const v) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (v == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
```

```
sprintf(ShapoidErr->_msg, "'v' is null");
    PBErrCatch(ShapoidErr);
  if (dim < 0 || dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
    PBErrCatch(ShapoidErr);
  if (VecGetDim(v) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'v' 's dimension is invalid (%d==%d)",
      dim, VecGetDim(v));
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the axis
  VecCopy(that->_axis[dim], v);
  // Update the SysLinEq
  {\tt ShapoidUpdateSysLinEqImport(that);}
  // If it's a Spheroid
  if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
// Set the 'iElem'-th element of the 'dim'-th axis of the Shapoid to 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisSet(Shapoid* const that, const int dim,
  const int iElem, const float v) { }
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (\dim < 0 \mid \mid \dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(ShapoidErr->\_msg,\ "Axis'\ index\ is\ invalid\ (0<=\%d<\%d)",}
      dim, that->_dim);
    PBErrCatch(ShapoidErr);
  if (iElem < 0 || iElem >= VecGetDim(ShapoidAxis(that, dim))) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(ShapoidErr->\_msg,\ "iElem\ is\ invalid\ (0<=\%d<\%d)",}
      iElem, VecGetDim(ShapoidAxis(that, dim)));
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the axis
  VecSet(that->_axis[dim], iElem, v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
  // If it's a Spheroid
  if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
// Set the 'iElem'-th element of the 'dim'-th axis of the Shapoid to
```

```
// 'v' added to its current value
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisSetAdd(Shapoid* const that, const int dim,
  const int iElem, const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (dim < 0 || dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
    PBErrCatch(ShapoidErr);
  }
  if (iElem < 0 || iElem >= VecGetDim(ShapoidAxis(that, dim))) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(ShapoidErr->\_msg,\ "iElem\ is\ invalid\ (0<=\%d<\%d)",}
      iElem, VecGetDim(ShapoidAxis(that, dim)));
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the axis
  VecSetAdd(that->_axis[dim], iElem, v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
  // If it's a Spheroid
  if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
}
// Get the 'iElem'-th element of the 'dim'-th axis of the Shapoid
#if BUILDMODE != 0
inline
#endif
float _ShapoidAxisGet(const Shapoid* const that, const int dim,
 const int iElem) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (dim < 0 || dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
    PBErrCatch(ShapoidErr);
  if (iElem < 0 || iElem >= VecGetDim(ShapoidAxis(that, dim))) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "iElem is invalid (0<=%d<%d)",
      iElem, VecGetDim(ShapoidAxis(that, dim)));
    PBErrCatch(ShapoidErr);
  }
#endif
  // Set the axis
  return VecGet(that->_axis[dim], iElem);
```

```
// Scale the 'dim'-th axis of the Shapoid by 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidAxisScale(Shapoid* const that, const int dim,
  const float v) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (\dim < 0 \mid \mid \dim >= that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "Axis' index is invalid (0<=%d<%d)",
      dim, that->_dim);
    PBErrCatch(ShapoidErr);
#endif
  // Set the axis
  VecScale(that->_axis[dim], v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
  // If it's a Spheroid
  if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
// Translate the Shapoid by 'v'
#if BUILDMODE != 0
inline
#endif
void _ShapoidTranslate(Shapoid* const that, const VecFloat* const v) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (v == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'v' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(v) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'v' 's dimension is invalid (%d==%d)",
      that->_dim, VecGetDim(v));
    PBErrCatch(ShapoidErr);
  }
#endif
  \begin{subarray}{ll} \end{subarray} Translate the position
  VecOp(that->_pos, 1.0, v, 1.0);
// Scale the Shapoid by 'v' (each axis is multiplied by v[iAxis])
#if BUILDMODE != 0
inline
#endif
```

```
void _ShapoidScaleVector(Shapoid* const that, const VecFloat* const v) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (v == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'v' is null");
    PBErrCatch(ShapoidErr);
 if (VecGetDim(v) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'v' 's dimension is invalid (%d==%d)",
      that->_dim, VecGetDim(v));
   PBErrCatch(ShapoidErr);
 }
#endif
 // Scale each axis
 for (int iAxis = that->_dim; iAxis--;)
   VecScale(that->_axis[iAxis], VecGet(v, iAxis));
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
  // If it's a Spheroid
  if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
// Scale the Shapoid by 'c'
#if BUILDMODE != 0
inline
#endif
void _ShapoidScaleScalar(Shapoid* const that, const float c) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
 // Scale each axis
 for (int iAxis = that->_dim; iAxis--;)
   VecScale(that->_axis[iAxis], c);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
  // If it's a Spheroid
 if (that->_type == ShapoidTypeSpheroid)
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
// Scale the Shapoid by 'v' (each axis is multiplied by v[iAxis])
// and translate the Shapoid such as its center after scaling
// is at the same position than before scaling
#if BUILDMODE != 0
inline
#endif
void _ShapoidGrowVector(Shapoid* const that, const VecFloat* const v) {
#if BUILDMODE == 0
 if (that == NULL) {
```

```
ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (v == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'v' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(v) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'v' 's dimension is invalid (%d==%d)",
     that->_dim, VecGetDim(v));
   PBErrCatch(ShapoidErr);
  if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
#endif
  // If the shapoid is a spheroid
  if (that->_type == ShapoidTypeSpheroid) {
    // Scale
    ShapoidScale(that, v);
    // Update the major and minor axis
    SpheroidUpdateMajMinAxis((Spheroid*)that);
  // Else, the shapoid is not a spheroid
  } else {
    // Memorize the center
    VecFloat* centerA = ShapoidGetCenter(that);
    // Scale
    ShapoidScale(that, v);
    // Reposition to keep center at the same position
    VecFloat* centerB = ShapoidGetCenter(that);
    VecOp(centerA, 1.0, centerB, -1.0);
    VecOp(that->_pos, 1.0, centerA, 1.0);
    VecFree(&centerA);
    VecFree(&centerB);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Scale the Shapoid by 'c'
// and translate the Shapoid such as its center after scaling
// is at the same position than before scaling
#if BUILDMODE != 0
inline
#endif
void _ShapoidGrowScalar(Shapoid* const that, const float c) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
```

```
ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
 }
#endif
  // If the shapoid is a spheroid
 if (that->_type == ShapoidTypeSpheroid) {
    // Scale
   ShapoidScale(that, c);
    // Update the major and minor axis
   SpheroidUpdateMajMinAxis((Spheroid*)that);
  \ensuremath{//} Else, the shapoid is not a spheroid
  } else {
    // Memorize the center
    VecFloat* centerA = ShapoidGetCenter(that);
    // Scale
    ShapoidScale(that, c);
    // Reposition to keep center at the same position
    VecFloat* centerB = ShapoidGetCenter(that);
    VecOp(centerA, 1.0, centerB, -1.0);
    VecOp(that->_pos, 1.0, centerA, 1.0);
    VecFree(&centerA);
   VecFree(&centerB);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to its center
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotCenter(Shapoid* const that, const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 }
 if (that->_dim != 2) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==2)", that->_dim);
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
   ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
 }
#endif
 // If it's a spheroid
 if (that->_type == ShapoidTypeSpheroid) {
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRot(that->_axis[iAxis], theta);
  // Else, it's not a spheroid
 } else {
    VecFloat* center = ShapoidGetCenter(that);
```

```
// Rotate each axis
    for (int iAxis = that->_dim; iAxis--;)
      VecRot(that->_axis[iAxis], theta);
    // Reposition the origin
    VecFloat* v = VecGetOp(that->_pos, 1.0, center, -1.0);
    VecRot(v, theta);
    VecOp(v, 1.0, center, 1.0);
    VecCopy(that->_pos, v);
    VecFree(&center);
    VecFree(&v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to its position
#if BUILDMODE != 0
#endif
void _ShapoidRotStart(Shapoid* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (that->_dim != 2) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==2)", that->_dim);
   PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRot(that->_axis[iAxis], theta);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 2 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
#if BUILDMODE != 0
inline
#endif
#if BUILDMODE == 0
  if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  }
  if (that->_dim != 2) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==2)", that->_dim);
   PBErrCatch(ShapoidErr);
  }
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
```

```
VecRot(that->_axis[iAxis], theta);
  // Reposition the origin
  VecRot(that->_pos, theta);
  // Update the SysLinEq
 {\tt ShapoidUpdateSysLinEqImport(that);}
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisCenter(Shapoid* const that,
 const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 }
 if (axis == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'axis' is null");
   PBErrCatch(ShapoidErr);
 if (VecGetDim(axis) != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'axis' 's dimension is invalid (%d==3)", VecGetDim(axis));
   PBErrCatch(ShapoidErr);
 if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
#endif
 // If it's a spheroid
  if (that->_type == ShapoidTypeSpheroid) {
 // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotAxis(that->_axis[iAxis], axis, theta);
  // Else, it's not a spheroid
 } else {
    VecFloat* center = ShapoidGetCenter(that);
    // Rotate each axis
    for (int iAxis = that->_dim; iAxis--;)
      VecRotAxis(that->_axis[iAxis], axis, theta);
    // Reposition the origin
    VecFloat* v = VecGetOp(that->_pos, 1.0, center, -1.0);
    VecRotAxis(v, axis, theta);
    VecOp(v, 1.0, center, 1.0);
    VecCopy(that->_pos, v);
```

```
VecFree(&center);
    VecFree(&v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisStart(Shapoid* const that,
  const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  }
  if (axis == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'axis' is null");
   PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
    PBErrCatch(ShapoidErr);
  if (VecGetDim(axis) != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'axis' 's dimension is invalid (%d==3)", VecGetDim(axis));
   PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotAxis(that->_axis[iAxis], axis, theta);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around 'axis'
// 'axis' must be normalized
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotAxisOrigin(Shapoid* const that,
  const VecFloat3D* const axis, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (axis == NULL) {
```

```
ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'axis' is null");
    PBErrCatch(ShapoidErr);
 if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
 if (VecGetDim(axis) != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'axis' 's dimension is invalid (%d==3)", VecGetDim(axis));
   PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
 for (int iAxis = that->_dim; iAxis--;)
   VecRotAxis(that->_axis[iAxis], axis, theta);
  // Reposition the origin
  VecRotAxis(that->_pos, axis, theta);
 // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around X
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXCenter(Shapoid* const that, const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
#endif
 // If it's a spheroid
 if (that->_type == ShapoidTypeSpheroid) {
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotX(that->_axis[iAxis], theta);
  // Else, it's not a spheroid
    VecFloat* center = ShapoidGetCenter(that);
    // Rotate each axis
   for (int iAxis = that->_dim; iAxis--;)
```

```
VecRotX(that->_axis[iAxis], theta);
    // Reposition the origin
    VecFloat* v = VecGetOp(that->_pos, 1.0, center, -1.0);
    VecRotX(v, theta);
    VecOp(v, 1.0, center, 1.0);
    VecCopy(that->_pos, v);
    VecFree(&center);
    VecFree(&v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around X
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXStart(Shapoid* const that,
 float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
   VecRotX(that->_axis[iAxis], theta);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
}
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around X
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotXOrigin(Shapoid* const that,
  float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (d=3)", that->_dim);
    PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
```

```
for (int iAxis = that->_dim; iAxis--;)
    VecRotX(that->_axis[iAxis], theta);
  // Reposition the origin
 VecRotX(that->_pos, theta);
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around Y
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotYCenter(Shapoid* const that, const float theta) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
 }
#endif
 // If it's a spheroid
 if (that->_type == ShapoidTypeSpheroid) {
  // Rotate each axis
 for (int iAxis = that->_dim; iAxis--;)
   VecRotY(that->_axis[iAxis], theta);
  // Else, it's not a spheroid
  } else {
   VecFloat* center = ShapoidGetCenter(that);
    // Rotate each axis
    for (int iAxis = that->_dim; iAxis--;)
     VecRotY(that->_axis[iAxis], theta);
    // Reposition the origin
    VecFloat* v = VecGetOp(that->_pos, 1.0, center, -1.0);
    VecRotY(v, theta);
    VecOp(v, 1.0, center, 1.0);
    VecCopy(that->_pos, v);
    VecFree(&center);
    VecFree(&v);
 }
  // Update the SysLinEq
 ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around Y
#if BUILDMODE != 0
inline
#endif
```

```
void _ShapoidRotYStart(Shapoid* const that,
  float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  }
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
    PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotY(that->_axis[iAxis], theta);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
}
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around Y
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotYOrigin(Shapoid* const that,
 float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (d=3)", that->_dim);
   PBErrCatch(ShapoidErr);
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotY(that->_axis[iAxis], theta);
  // Reposition the origin
  VecRotY(that->_pos, theta);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its center around Z
#if BUILDMODE != 0
inline
void _ShapoidRotZCenter(Shapoid* const that, const float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
```

```
PBErrCatch(ShapoidErr);
  }
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
    PBErrCatch(ShapoidErr);
  if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
  }
#endif
 // If it's a spheroid
  if (that->_type == ShapoidTypeSpheroid) {
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotZ(that->_axis[iAxis], theta);
  // Else, it's not a spheroid
  } else {
    VecFloat* center = ShapoidGetCenter(that);
    // Rotate each axis
    for (int iAxis = that->_dim; iAxis--;)
      VecRotZ(that->_axis[iAxis], theta);
    // Reposition the origin
    VecFloat* v = VecGetOp(that->_pos, 1.0, center, -1.0);
    VecRotZ(v, theta);
    VecOp(v, 1.0, center, 1.0);
    VecCopy(that->_pos, v);
    VecFree(&center);
    VecFree(&v);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to its position around Z
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotZStart(Shapoid* const that,
  float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
   PBErrCatch(ShapoidErr);
 7
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotZ(that->_axis[iAxis], theta);
```

```
// Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Rotate the Shapoid of dimension 3 by 'theta' (in radians, CCW)
// relatively to the origin of the global coordinates system
// around Z
#if BUILDMODE != 0
inline
#endif
void _ShapoidRotZOrigin(Shapoid* const that,
  float theta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (that->_dim != 3) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg,
      "'that' 's dimension is invalid (%d==3)", that->_dim);
    PBErrCatch(ShapoidErr);
  }
#endif
  // Rotate each axis
  for (int iAxis = that->_dim; iAxis--;)
    VecRotZ(that->_axis[iAxis], theta);
  // Reposition the origin
  VecRotZ(that->_pos, theta);
  // Update the SysLinEq
  ShapoidUpdateSysLinEqImport(that);
// Convert the coordinates of 'pos' from standard coordinate system
// toward the Shapoid coordinates system
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidImportCoord(const Shapoid* const that,
  const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      that->_dim, VecGetDim(pos));
   PBErrCatch(ShapoidErr);
  7
#endif
  // Update the system solver for the requested position
  VecFloat* v = VecGetOp(pos, 1.0, that->_pos, -1.0);
  SysLinEqSetV(that->_sysLinEqImport, v);
```

```
// Solve the system
 VecFloat* res = SysLinEqSolve(that->_sysLinEqImport);
  // Free memory
 VecFree(&v);
  // return the result
 return res;
#if BUILDMODE != 0
inline
#endif
// Convert the coordinates of 'pos' from the Shapoid coordinates system
// toward standard coordinate system
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidExportCoord(const Shapoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
   PBErrCatch(ShapoidErr);
 if (VecGetDim(pos) != that->_dim) {
   ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
     that->_dim, VecGetDim(pos));
   PBErrCatch(ShapoidErr);
#endif
  // Allocate memory for the result
  VecFloat* res = VecClone(that->_pos);
 for (int dim = that->_dim; dim--;)
    VecOp(res, 1.0, that->_axis[dim], VecGet(pos, dim));
  // Return the result
 return res;
// Get the center of the shapoid in standard coordinate system
#if BUILDMODE != 0
inline
#endif
VecFloat* _ShapoidGetCenter(const Shapoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
```

```
#endif
  if (ShapoidGetType(that) == ShapoidTypeFacoid)
   return FacoidGetCenter((Facoid*)that);
  else if (ShapoidGetType(that) == ShapoidTypePyramidoid)
    return PyramidoidGetCenter((Pyramidoid*)that);
  else if (ShapoidGetType(that) == ShapoidTypeSpheroid)
   return SpheroidGetCenter((Spheroid*)that);
  else
    return NULL;
#if BUILDMODE != 0
inline
#endif
VecFloat* FacoidGetCenter(const Facoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  }
#endif
  \ensuremath{//} Declare a variable to memorize the result in Shapoid
  // coordinate system
  VecFloat* coord = VecFloatCreate(ShapoidGetDim(that));
  // For each dimension
  for (int dim = ShapoidGetDim(that); dim--;)
   VecSet(coord, dim, 0.5);
  // Convert the coordinates in standard coordinate system
  VecFloat* res = ShapoidExportCoord(that, coord);
  // Free memory
  VecFree(&coord);
  // Return the result
  return res;
#if BUILDMODE != 0
inline
#endif
VecFloat* PyramidoidGetCenter(const Pyramidoid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
 }
#endif
  // Declare a variable to memorize the result in Shapoid
  // coordinate system
  VecFloat* coord = VecFloatCreate(ShapoidGetDim(that));
  // For each dimension
  for (int dim = ShapoidGetDim(that); dim--;)
    VecSet(coord, dim, 1.0 / (1.0 + ShapoidGetDim(that)));
  // Convert the coordinates in standard coordinate system
  VecFloat* res = ShapoidExportCoord(that, coord);
  // Free memory
  VecFree(&coord);
  // Return the result
  return res;
#if BUILDMODE != 0
```

```
inline
#endif
VecFloat* SpheroidGetCenter(const Spheroid* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  // Declare a variable to memorize the result in Shapoid
  // coordinate system
  VecFloat* coord = VecFloatCreate(ShapoidGetDim(that));
  // Convert the coordinates in standard coordinate system
  VecFloat* res = ShapoidExportCoord(that, coord);
  // Free memory
  VecFree(&coord);
  // Return the result
 return res;
// Check if shapoid 'that' and 'tho' are equals
#if BUILDMODE != 0
inline
#endif
bool _ShapoidIsEqual(const Shapoid* const that,
  const Shapoid* const tho) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  if (tho == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'tho' is null");
    PBErrCatch(ShapoidErr);
#endif
  // Check the dimension, type and position
  if (that->_dim != tho->_dim ||
    that->_type != tho->_type ||
    VecIsEqual(that->_pos, tho->_pos) == false)
    return false;
  // Check the axis
  for (int i = that->_dim; i--;)
    if (VecIsEqual(that->_axis[i], tho->_axis[i]) == false)
      return false;
  // If the Shapoid is a Spheroid, check Spheroid properties
  if (that->_type == ShapoidTypeSpheroid) {
    if (((Spheroid*)that)->_majAxis != ((Spheroid*)tho)->_majAxis ||
      ((Spheroid*)that)->_minAxis != ((Spheroid*)tho)->_minAxis)
      return false;
  // Return the success code
 return true;
// Update the system of linear equation used to import coordinates
#if BUILDMODE != 0
inline
#endif
```

```
void ShapoidUpdateSysLinEqImport(Shapoid* const that) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
 VecShort2D dim = VecShortCreateStatic2D();
  // Set a pointer to the matrix in the SysLinEq
 MatFloat* mat = MatClone(that->_sysLinEqImport->_M);
  // Set the values of the matrix
 for (VecSet(\&dim, 0, 0); VecGet(\&dim, 0) < that->_dim;
    VecSetAdd(&dim, 0, 1)) {
    for (VecSet(&dim, 1, 0); VecGet(&dim, 1) < that->_dim;
      VecSetAdd(&dim, 1, 1)) {
     MatSet(mat, &dim, VecGet(that->_axis[VecGet(&dim, 0)],
        VecGet(&dim, 1)));
  // Update the SysLinEq
 SysLinEqSetM(that->_sysLinEqImport, mat);
 // Free memory
 MatFree(&mat);
// Return true if 'pos' (in stand coordinate system) is inside the
// Shapoid
// Else return false
#if BUILDMODE != 0
inline
#endif
bool _ShapoidIsPosInside(const Shapoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (pos == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
   PBErrCatch(ShapoidErr);
 if (VecGetDim(pos) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
     that->_dim, VecGetDim(pos));
   PBErrCatch(ShapoidErr);
 if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
   PBErrCatch(ShapoidErr);
#endif
 // If the Shapoid is a Facoid
 if (that->_type == ShapoidTypeFacoid) {
   return FacoidIsPosInside((Facoid*)that, pos);
```

```
// Else, if the Shapoid is a Pyramidoid
 } else if (that->_type == ShapoidTypePyramidoid) {
    return PyramidoidIsPosInside((Pyramidoid*)that, pos);
  // Else, if the Shapoid is a Spheroid
 } else if (that->_type == ShapoidTypeSpheroid) {
    return SpheroidIsPosInside((Spheroid*)that, pos);
 } else
    return false;
#if BUILDMODE != 0
inline
#endif
bool FacoidIsPosInside(const Facoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
   PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
     ShapoidGetDim(that), VecGetDim(pos));
   PBErrCatch(ShapoidErr);
#endif
  // Get the coordinates of pos in the Shapoid coordinate system
  VecFloat* coord = ShapoidImportCoord(that, pos);
 // Declare a variable to memorize the result
 bool ret = false;
  // pos is in the Shapoid if all the coord in Shapoid coord
  // system are in [0.0, 1.0]
 ret = true;
 for (int dim = ShapoidGetDim(that); dim-- && ret == true;) {
   float v = VecGet(coord, dim);
    if (v < 0.0 \mid \mid v > 1.0)
     ret = false;
 // Free memory
 VecFree(&coord);
  // Return the result
 return ret;
#if BUILDMODE != 0
inline
#endif
bool PyramidoidIsPosInside(const Pyramidoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
```

```
if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      ShapoidGetDim(that), VecGetDim(pos));
    PBErrCatch(ShapoidErr);
  }
#endif
  // Get the coordinates of pos in the Shapoid coordinate system
  VecFloat* coord = ShapoidImportCoord(that, pos);
  // Declare a variable to memorize the result
  bool ret = false;
  \ensuremath{//} pos is in the Shapoid if all the coord in Shapoid coord
  // system are in [0.0, 1.0] and their sum is in [0.0, 1.0]
  float sum = 0.0:
  for (int dim = ShapoidGetDim(that); dim-- && ret == true;) {
    float v = VecGet(coord, dim);
    sum += v;
    if (v < 0.0 \mid \mid v > 1.0)
      ret = false;
  if (ret == true && sum > 1.0)
   ret = false;
  // Free memory
  VecFree(&coord);
  // Return the result
  return ret;
#if BUILDMODE != 0
inline
#endif
bool SpheroidIsPosInside(const Spheroid* const that,
  const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      ShapoidGetDim(that), VecGetDim(pos));
    PBErrCatch(ShapoidErr);
  }
  // Get the coordinates of pos in the Shapoid coordinate system
  VecFloat* coord = ShapoidImportCoord(that, pos);
  // Declare a variable to memorize the result
  bool ret = false;
  // pos is in the Shapoid if its norm is in [0.0, 0.5]
```

```
float norm = VecNorm(coord);
  if (norm \le 0.5)
    ret = true;
  // Free memory
  VecFree(&coord);
  // Return the result
  return ret;
}
// Get the depth value in the Shapoid of 'pos'
// The depth is defined as follow: the point with depth equals 1.0 is
// the farthest point from the surface of the Shapoid (inside it),
// points with depth equals to 0.0 are point on the surface of the
// Shapoid. Depth is continuous and derivable over the volume of the
// Shapoid
#if BUILDMODE != 0
inline
#endif
float _ShapoidGetPosDepth(const Shapoid* const that,
  const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != that->_dim) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    {\tt sprintf(ShapoidErr->\_msg, "'pos' 's \ dimension \ is \ invalid \ (\%d==\%d)",}
      that->_dim, VecGetDim(pos));
    PBErrCatch(ShapoidErr);
  if (that->_type != ShapoidTypeFacoid &&
    that->_type != ShapoidTypeSpheroid &&
    that->_type != ShapoidTypePyramidoid) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
sprintf(ShapoidErr->_msg, "No implementation for 'that' 's type");
    PBErrCatch(ShapoidErr);
#endif
  // If the Shapoid is a Facoid
  if (that->_type == ShapoidTypeFacoid) {
    return FacoidGetPosDepth((Facoid*)that, pos);
  // Else, if the Shapoid is a Pyramidoid
  } else if (that->_type == ShapoidTypePyramidoid) {
    return PyramidoidGetPosDepth((Pyramidoid*)that, pos);
  // Else, if the Shapoid is a Spheroid
  } else if (that->_type == ShapoidTypeSpheroid) {
    return SpheroidGetPosDepth((Spheroid*)that, pos);
  } else {
    return 0.0;
}
#if BUILDMODE != 0
inline
#endif
```

```
float FacoidGetPosDepth(const Facoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 }
 if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
   PBErrCatch(ShapoidErr);
 if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
     ShapoidGetDim(that), VecGetDim(pos));
   PBErrCatch(ShapoidErr);
#endif
  // Get the coordinates of pos in the Shapoid coordinate system
  VecFloat* coord = ShapoidImportCoord(that, pos);
 // Declare a variable to memorize the result
  float ret = 1.0;
 for (int dim = ShapoidGetDim(that); dim-- && ret > PBMATH_EPSILON;) {
    float v = VecGet(coord, dim);
    if (v < 0.0 \mid \mid VecGet(coord, dim) > 1.0)
     ret = 0.0;
    else
     ret *= 1.0 - pow(0.5 - v, 2.0) * 4.0;
 }
  // Free memory
 VecFree(&coord);
  // Return the result
 return ret;
#if BUILDMODE != 0
inline
#endif
float PyramidoidGetPosDepth(const Pyramidoid* const that,
 const VecFloat* const pos) {
#if BUILDMODE == 0
 if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
 if (pos == NULL) {
   ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
   PBErrCatch(ShapoidErr);
 }
  if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      ShapoidGetDim(that), VecGetDim(pos));
   PBErrCatch(ShapoidErr);
 }
#endif
  // Get the coordinates of pos in the Shapoid coordinate system
 VecFloat* coord = ShapoidImportCoord(that, pos);
```

```
// Declare a variable to memorize the result
  float ret = 1.0;
  float sum = 0.0;
  bool flag = true;
  for (int dim = ShapoidGetDim(that); dim-- && ret > PBMATH_EPSILON;) {
    float v = VecGet(coord, dim);
    sum += v;
    if (v < 0.0 \mid \mid v > 1.0)
      flag = false;
  if (flag == true && sum > 1.0)
    flag = false;
  if (flag == false)
   ret = 0.0;
  else {
    ret = 1.0;
    for (int dim = ShapoidGetDim(that); dim--;) {
      float z = 0.0;
      for (int d = ShapoidGetDim(that); d--;)
        if (d != dim)
          z += VecGet(coord, d);
      ret *=
        (1.0 - 4.0 * pow(0.5 - VecGet(coord, dim) / (1.0 - z), 2.0));
    }
  }
  // Free memory
  VecFree(&coord);
  // Return the result
  return ret;
#if BUILDMODE != 0
inline
#endif
float SpheroidGetPosDepth(const Spheroid* const that,
  const VecFloat* const pos) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
  if (pos == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'pos' is null");
    PBErrCatch(ShapoidErr);
  if (VecGetDim(pos) != ShapoidGetDim(that)) {
    ShapoidErr->_type = PBErrTypeInvalidArg;
    sprintf(ShapoidErr->_msg, "'pos' 's dimension is invalid (%d==%d)",
      ShapoidGetDim(that), VecGetDim(pos));
    PBErrCatch(ShapoidErr);
  }
#endif
  // \ensuremath{\mathsf{Get}} the coordinates of pos in the Shapoid coordinate system
  VecFloat* coord = ShapoidImportCoord(that, pos);
  // Declare a variable to memorize the result
  float ret = 0.0;
  float norm = VecNorm(coord);
  if (norm <= 0.5)
    ret = 1.0 - norm * 2.0;
  // Free memory
```

```
VecFree(&coord);
  // Return the result
 return ret;
#if BUILDMODE != 0
inline
#endif
bool FacoidLoad(Facoid** that, FILE* const stream) {
  bool ret = _ShapoidLoad((Shapoid**)that, stream);
  if (!ret || ShapoidGetType(*that) != ShapoidTypeFacoid) {
    ShapoidFree(that);
    return false;
 return true;
#if BUILDMODE != 0
#endif
bool PyramidoidLoad(Pyramidoid** that, FILE* const stream) {
  bool ret = _ShapoidLoad((Shapoid**)that, stream);
  if (!ret || ShapoidGetType(*that) != ShapoidTypePyramidoid) {
    ShapoidFree(that);
    return false;
 return true;
#if BUILDMODE != 0
inline
#endif
bool SpheroidLoad(Spheroid** that, FILE* const stream) {
  bool ret = _ShapoidLoad((Shapoid**)that, stream);
  if (!ret || ShapoidGetType(*that) != ShapoidTypeSpheroid) {
    ShapoidFree(that);
    return false;
  return true;
// ----- ShapoidIter
// ====== Functions implementation =========
// Return the current position in Shapoid coordinates of the
// ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
VecFloat* ShapoidIterGetInternalPos(const ShapoidIter* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
  return VecClone(that->_pos);
// Return the current position in standard coordinates of the
```

```
// ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
VecFloat* ShapoidIterGetExternalPos(const ShapoidIter* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
 return ShapoidExportCoord(that->_shap, that->_pos);
// Set the attached Shapoid of the ShapoidIter 'that' to 'shap'
// The iterator is reset to its initial position
#if BUILDMODE != 0
#endif
void _ShapoidIterSetShapoid(ShapoidIter* const that,
 const Shapoid* const shap) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
    PBErrCatch(ShapoidErr);
#endif
 that->_shap = shap;
// Get the Shapoid of the ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
const Shapoid* ShapoidIterShapoid(const ShapoidIter* const that) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
#endif
 return that->_shap;
// Set the delta of the ShapoidIter 'that' to a copy of 'delta'
#if BUILDMODE != 0
inline
#endif
void _ShapoidIterSetDelta(ShapoidIter* const that,
  const VecFloat* const delta) {
#if BUILDMODE == 0
  if (that == NULL) {
    ShapoidErr->_type = PBErrTypeNullPointer;
    sprintf(ShapoidErr->_msg, "'that' is null");
   PBErrCatch(ShapoidErr);
  }
#endif
  VecFree(&(that->_delta));
  that->_delta = VecClone(delta);
```

```
}
// Get the delta of the ShapoidIter 'that'
#if BUILDMODE != 0
inline
#endif
const VecFloat* ShapoidIterDelta(const ShapoidIter* const that) {
#if BUILDMODE == 0
    if (that == NULL) {
        ShapoidErr->_type = PBErrTypeNullPointer;
        sprintf(ShapoidErr->_msg, "'that' is null");
        PBErrCatch(ShapoidErr);
    }
#endif
    return that->_delta;
}
```

## 4 Makefile

#directory
PBERRDIR=../PBErr

```
PBMATHDIR=../PBMath
GSETDIR=../GSet
GTREEDIR=../GTree
PBJSONDIR=../PBJson
# Build mode
# 0: development (max safety, no optimisation)
# 1: release (min safety, optimisation)
# 2: fast and furious (no safety, optimisation)
BUILDMODE=1
include $(PBERRDIR)/Makefile.inc
INCPATH=-I./ -I$(PBERRDIR)/ -I$(PBMATHDIR)/ -I$(GSETDIR)/ -I$(PBJSONDIR)/ -I$(GTREEDIR)/
BUILDOPTIONS=$(BUILDPARAM) $(INCPATH)
# compiler
COMPILER=gcc
#rules
all : main
main: main.o pberr.o shapoid.o Makefile pbmath.o gset.o pbjson.o gtree.o
$(COMPILER) main.o pberr.o shapoid.o pbmath.o gset.o pbjson.o gtree.o $(LINKOPTIONS) -o main
main.o : main.c $(PBERRDIR)/pberr.h shapoid.h shapoid-inline.c Makefile
$(COMPILER) $(BUILDOPTIONS) -c main.c
shapoid.o : shapoid.c shapoid.h shapoid-inline.c $(PBMATHDIR)/pbmath.h $(GSETDIR)/gset.h $(PBERRDIR)/pberr.h Makefile
$(COMPILER) $(BUILDOPTIONS) -c shapoid.c
pbjson.o: $(PBJSONDIR)/pbjson.c $(PBJSONDIR)/pbjson-inline.c $(PBJSONDIR)/pbjson.h Makefile
$(COMPILER) $(BUILDOPTIONS) -c $(PBJSONDIR)/pbjson.c
gtree.o : $(GTREEDIR)/gtree.c $(GTREEDIR)/gtree.h $(GTREEDIR)/gtree-inline.c Makefile $(GSETDIR)/gset-inline.c $(GSE
$(COMPILER) $(BUILDOPTIONS) -c $(GTREEDIR)/gtree.c
```

pberr.o : \$(PBERRDIR)/pberr.c \$(PBERRDIR)/pberr.h Makefile

```
$(COMPILER) $(BUILDOPTIONS) -c $(PBERRDIR)/pberr.c

pbmath.o : $(PBMATHDIR)/pbmath.c $(PBMATHDIR)/pbmath-inline.c $(PBMATHDIR)/pbmath.h Makefile $(PBERRDIR)/pberr.h $(COMPILER) $(BUILDOPTIONS) -c $(PBMATHDIR)/pbmath.c

gset.o : $(GSETDIR)/gset.c $(GSETDIR)/gset-inline.c $(GSETDIR)/gset.h Makefile $(PBERRDIR)/pberr.h $(COMPILER) $(BUILDOPTIONS) -c $(GSETDIR)/gset.c

clean :
    rm -rf *.o main

valgrind :
    valgrind -v --track-origins=yes --leak-check=full --gen-suppressions=yes --show-leak-kinds=all ./main

unitTest :
    main > unitTest.txt; diff unitTest.txt unitTestRef.txt
```

## 5 Unit tests

```
#include <stdlib.h>
#include <stdio.h>
#include <time.h>
#include <string.h>
#include <time.h>
#include <unistd.h>
#include <sys/time.h>
#include "pberr.h"
#include "shapoid.h"
#define RANDOMSEED 0
void UnitTestCreateCloneIsEqualFree() {
  int dim = 3:
  Shapoid* facoid = ShapoidCreate(dim, ShapoidTypeFacoid);
  if (facoid == NULL || facoid->_dim != dim ||
    facoid->_type != ShapoidTypeFacoid || facoid->_pos == NULL ||
    VecGetDim(facoid->_pos) != dim || facoid->_sysLinEqImport == NULL ||
    facoid->_axis == NULL) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidCreate failed");
    PBErrCatch(ShapoidErr);
  for (int iDim = dim; iDim--;) {
    if (ISEQUALF(VecGet(facoid->_pos, iDim), 0.0) == false ||
      facoid->_axis[iDim] == NULL ||
      VecGetDim(facoid->_axis[iDim]) != dim) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidCreate failed");
      PBErrCatch(ShapoidErr);
    for (int jDim = dim; jDim--;) {
      if ((iDim == jDim &&
        ISEQUALF(VecGet(facoid->_axis[iDim], jDim), 1.0) == false) ||
        (iDim != jDim &&
        ISEQUALF(VecGet(facoid->_axis[iDim], jDim), 0.0) == false)) {
        ShapoidErr->_type = PBErrTypeUnitTestFailed;
        sprintf(ShapoidErr->_msg, "ShapoidCreate failed");
        PBErrCatch(ShapoidErr);
```

```
if (ISEQUALF(VecGet(facoid->_sysLinEqImport->_V, iDim),
    0.0) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidCreate failed");
    PBErrCatch(ShapoidErr);
 }
VecShort2D u = VecShortCreateStatic2D();
VecSet(&u, 0, dim); VecSet(&u, 1, dim);
VecShort2D v = VecShortCreateStatic2D();
  if ((VecGet(&v, 0) == VecGet(&v, 1) &&
    ISEQUALF(MatGet(facoid->_sysLinEqImport->_M, &v), 1.0) == false) ||
    (VecGet(&v, 0) != VecGet(&v, 1) &&
    ISEQUALF(MatGet(facoid->_sysLinEqImport->_M, &v), 0.0) == false) ||
    (VecGet(&v, 0) == VecGet(&v, 1) &&
    ISEQUALF(MatGet(facoid->_sysLinEqImport->_Minv, &v),
      1.0) == false) ||
    (VecGet(&v, 0) != VecGet(&v, 1) &&
    ISEQUALF(MatGet(facoid->_sysLinEqImport->_Minv, &v),
      0.0) == false)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidCreate failed");
    PBErrCatch(ShapoidErr);
} while (VecStep(&v, &u));
Shapoid* clone = ShapoidClone(facoid);
if (facoid->_dim != clone->_dim ||
  facoid->_type != clone->_type ||
  VecIsEqual(facoid->_pos, clone->_pos) == false ||
  MatIsEqual(facoid->_sysLinEqImport->_M,
    clone->_sysLinEqImport->_M) == false ||
  MatIsEqual(facoid->_sysLinEqImport->_Minv,
    clone->_sysLinEqImport->_Minv) == false ||
  VecIsEqual(facoid->_sysLinEqImport->_V,
    clone->_sysLinEqImport->_V) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidClone failed");
  PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  if (VecIsEqual(facoid->_axis[i], clone->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
sprintf(ShapoidErr->_msg, "ShapoidClone failed");
    PBErrCatch(ShapoidErr);
 }
if (ShapoidIsEqual(facoid, clone) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidIsEqual failed");
  PBErrCatch(ShapoidErr);
}
clone->_type = ShapoidTypePyramidoid;
if (ShapoidIsEqual(facoid, clone) == true) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidIsEqual failed");
  PBErrCatch(ShapoidErr);
clone->_type = facoid->_type;
clone->_dim = dim + 1;
if (ShapoidIsEqual(facoid, clone) == true) {
```

```
ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidIsEqual failed");
   PBErrCatch(ShapoidErr);
 clone->_dim = facoid->_dim;
 VecSet(clone->_pos, 0, 1.0);
 if (ShapoidIsEqual(facoid, clone) == true) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidIsEqual failed");
   PBErrCatch(ShapoidErr);
 VecSet(clone->_pos, 0, 0.0);
 VecSet(clone->_axis[0], 0, 2.0);
 if (ShapoidIsEqual(facoid, clone) == true) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidIsEqual failed");
   PBErrCatch(ShapoidErr);
 VecSet(clone->_axis[0], 0, 1.0);
 ShapoidFree(&facoid);
 if (facoid != NULL) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidFree failed");
   PBErrCatch(ShapoidErr);
 ShapoidFree(&clone);
 printf("UnitTestCreateCloneIsEqualFree OK\n");
void UnitTestLoadSavePrint() {
 int dim = 3;
 Facoid* facoid = FacoidCreate(dim);
 FILE* file = fopen("./facoid.txt", "w");
 if (ShapoidSave(facoid, file, false) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidSave failed");
   PBErrCatch(ShapoidErr);
 fclose(file);
 file = fopen("./facoid.txt", "r");
 Facoid* load = FacoidCreate(dim);
 if (ShapoidLoad(&load, file) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidLoad failed");
   PBErrCatch(ShapoidErr);
 fclose(file);
 if (ShapoidIsEqual(facoid, load) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidLoad/Save failed");
   PBErrCatch(ShapoidErr);
 ShapoidPrintln(facoid, stdout);
 ShapoidFree(&facoid);
 ShapoidFree(&load);
 printf("UnitTestLoadSavePrint OK\n");
void UnitTestGetSetTypeDimPosAxis() {
 int dim = 3;
 Facoid* facoid = FacoidCreate(dim);
 Pyramidoid* pyramidoid = PyramidoidCreate(dim);
```

```
Spheroid* spheroid = SpheroidCreate(dim);
if (ShapoidGetType(facoid) != ShapoidTypeFacoid ||
  ShapoidGetType(pyramidoid) != ShapoidTypePyramidoid ||
  ShapoidGetType(spheroid) != ShapoidTypeSpheroid) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidGetType failed");
 PBErrCatch(ShapoidErr);
if (ShapoidGetDim(facoid) != dim) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidGetDim failed");
 PBErrCatch(ShapoidErr);
VecFloat* v = VecFloatCreate(dim);
VecFloat* u = ShapoidGetPos(facoid);
if (VecIsEqual(v, u) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidGetPos failed");
  PBErrCatch(ShapoidErr);
VecFree(&u);
for (int i = dim; i--;) {
 u = ShapoidGetAxis(facoid, i);
  for (int j = dim; j--;)
    if ((i == j && ISEQUALF(VecGet(u, j), 1.0) == false) ||
      (i != j && ISEQUALF(VecGet(u, j), 0.0) == false)) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidGetAxis failed");
     PBErrCatch(ShapoidErr);
 VecFree(&u);
for (int i = dim; i--;)
  VecSet(v, i, (float)i);
ShapoidSetPos(facoid, v);
if (VecIsEqual(v, ShapoidPos(facoid)) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidSetPos failed");
 PBErrCatch(ShapoidErr);
}
for (int i = dim; i--;) {
  VecSetNull(v);
  VecSet(v, i, 2.0);
  ShapoidSetAxis(facoid, i, v);
  if (VecIsEqual(v, ShapoidAxis(facoid, i)) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidSetAxis failed");
   PBErrCatch(ShapoidErr);
for (int i = dim; i--;)
  VecSet(v. i. i):
ShapoidSetCenterPos(facoid, v);
VecFloat* center = ShapoidGetCenter(facoid);
if (VecIsEqual(v, center) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidSetCenterPos failed");
 PBErrCatch(ShapoidErr);
VecFree(&center);
VecSet(v, 0, 1.0); VecSet(v, 1, 2.0); VecSet(v, 2, 0.5);
ShapoidScale(spheroid, v);
```

```
if (!ISEQUALF(ShapoidGetBoundingRadius(spheroid), 1.0)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingRadius failed");
   PBErrCatch(ShapoidErr);
  VecFree(&v);
 ShapoidPosSet(facoid, 1, -1.0);
  if (!ISEQUALF(((Shapoid*)facoid)->_pos->_val[1], -1.0)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidPosSet failed");
    PBErrCatch(ShapoidErr);
 ShapoidPosSetAdd(facoid, 1, -1.0);
  if (!ISEQUALF(((Shapoid*)facoid)->_pos->_val[1], -2.0)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidPosSet failed");
   PBErrCatch(ShapoidErr);
  ShapoidAxisSet(facoid, 2, 1, -1.0);
  if (!ISEQUALF(((Shapoid*)facoid)->_axis[2]->_val[1], -1.0)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidAxisSet failed");
   PBErrCatch(ShapoidErr);
 ShapoidAxisSetAdd(facoid, 2, 1, -1.0);
  if (!ISEQUALF(((Shapoid*)facoid)->_axis[2]->_val[1], -2.0)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidAxisSetAdd failed");
   PBErrCatch(ShapoidErr);
 VecFloat* w = ShapoidGetAxis(facoid, 2);
  VecScale(w, 2.0);
  ShapoidAxisScale(facoid, 2, 2.0);
  if (!VecIsEqual(ShapoidAxis(facoid, 2), w)) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidAxisScale failed");
   PBErrCatch(ShapoidErr);
 VecFree(&w);
  for (int i = dim; i--;) {
    if (!ISEQUALF(ShapoidPosGet(facoid, i),
      VecGet(ShapoidGetPos(facoid), i))) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidPosGet failed");
     PBErrCatch(ShapoidErr);
    for (int j = dim; j--;) {
      if (!ISEQUALF(ShapoidAxisGet(facoid, i, j),
        VecGet(ShapoidGetAxis(facoid, i), j))) {
        ShapoidErr->_type = PBErrTypeUnitTestFailed;
        sprintf(ShapoidErr->_msg, "ShapoidAxisGet failed");
        PBErrCatch(ShapoidErr);
     }
   }
 ShapoidFree(&facoid);
 ShapoidFree(&pyramidoid);
 ShapoidFree(&spheroid);
 printf("UnitTestGetSetTypeDimPosAxis OK\n");
void UnitTestTranslateScaleGrow() {
```

```
int dim = 2;
Facoid* facoid = FacoidCreate(dim);
VecFloat* v = VecFloatCreate(dim);
for (int i = dim; i--;)
  VecSet(v, i, 1.0);
ShapoidTranslate(facoid, v);
if (VecIsEqual(v, ((Shapoid*)facoid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidTranslate failed");
  PBErrCatch(ShapoidErr);
float scale = 2.0;
ShapoidScale(facoid, scale);
VecSetNull(v);
VecSetNull(((Shapoid*)facoid)->_pos);
if (VecIsEqual(v, ((Shapoid*)facoid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidScaleScalar failed");
  PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
      VecSet(v, j, scale);
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)facoid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
sprintf(ShapoidErr->_msg, "_ShapoidScaleScalar failed");
    PBErrCatch(ShapoidErr);
 }
for (int i = dim; i--;)
  VecSet(v, i, 1.0 + (float)i);
ShapoidScale(facoid, v);
VecSetNull(v):
if (VecIsEqual(v, ((Shapoid*)facoid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidScaleVector failed");
  PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
      VecSet(v, j, scale * (1.0 + (float)i));
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)facoid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidScaleVector failed");
    PBErrCatch(ShapoidErr);
ShapoidFree(&facoid);
facoid = FacoidCreate(dim);
scale = 2.0;
ShapoidGrow(facoid, scale);
for (int i = dim; i--;)
  VecSet(v, i, -0.5);
if (VecIsEqual(v, ((Shapoid*)facoid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
```

```
PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
   if (i == j)
      VecSet(v, j, scale);
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)facoid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
   PBErrCatch(ShapoidErr);
 }
Pyramidoid* pyramidoid = PyramidoidCreate(dim);
VecFloat* centerA = ShapoidGetCenter(pyramidoid);
ShapoidGrow(pyramidoid, scale);
VecFloat* centerB = ShapoidGetCenter(pyramidoid);
if (VecIsEqual(centerA, centerB) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
 PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
      VecSet(v, j, scale);
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)pyramidoid)->_axis[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
   PBErrCatch(ShapoidErr);
 }
VecFree(&centerA);
VecFree(&centerB);
Spheroid* spheroid = SpheroidCreate(dim);
ShapoidGrow(spheroid, scale);
VecSetNull(v);
if (VecIsEqual(v, ((Shapoid*)spheroid)->_pos) == false) {
 ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
 PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
     VecSet(v, j, scale);
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)spheroid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidGrowScalar failed");
   PBErrCatch(ShapoidErr);
 }
VecFloat* scalev = VecFloatCreate(dim);
for (int i = dim; i--;)
 VecSet(scalev, i, 1.0 + (float)i);
ShapoidFree(&facoid);
ShapoidFree(&pyramidoid);
```

```
ShapoidFree(&spheroid);
facoid = FacoidCreate(dim);
ShapoidGrow(facoid, scalev);
float pa[2] = \{0.000, -0.500\};
for (int i = dim; i--;)
  VecSet(v, i, pa[i]);
if (VecIsEqual(v, ((Shapoid*)facoid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
 PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
   if (i == j)
     VecSet(v, j, VecGet(scalev, i));
    else
     VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)facoid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
   PBErrCatch(ShapoidErr);
 }
}
pyramidoid = PyramidoidCreate(dim);
centerA = ShapoidGetCenter(pyramidoid);
ShapoidGrow(pyramidoid, scalev);
centerB = ShapoidGetCenter(pyramidoid);
if (VecIsEqual(centerA, centerB) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
 PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
     VecSet(v, j, VecGet(scalev, i));
    else
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)pyramidoid)->_axis[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
   PBErrCatch(ShapoidErr);
 }
}
VecFree(&centerA);
VecFree(&centerB);
spheroid = SpheroidCreate(dim);
ShapoidGrow(spheroid, scalev);
VecSetNull(v);
if (VecIsEqual(v, ((Shapoid*)spheroid)->_pos) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
 PBErrCatch(ShapoidErr);
for (int i = dim; i--;) {
  for (int j = dim; j--;)
    if (i == j)
     VecSet(v, j, VecGet(scalev, i));
      VecSet(v, j, 0.0);
  if (VecIsEqual(v, ((Shapoid*)spheroid)->_axis[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(ShapoidErr->_msg, "_ShapoidGrowVector failed");
     PBErrCatch(ShapoidErr);
 }
 VecFree(&scalev);
  VecFree(&v);
 ShapoidFree(&facoid);
 ShapoidFree(&pyramidoid);
 ShapoidFree(&spheroid);
 printf("UnitTestTranslateScaleGrow OK\n");
void UnitTestRotate() {
 int dim = 2;
 Facoid* facoid = FacoidCreate(dim);
 Pyramidoid* pyramidoid = PyramidoidCreate(dim);
 Spheroid* spheroid = SpheroidCreate(dim);
  float theta = PBMATH_HALFPI;
  ShapoidRotCenter(facoid, theta);
 float pb[2] = \{1.0, 0.0\};
  float pc[2] = \{0.0, 1.0\};
  float pd[2] = \{-1.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pb[i]) == false ||
     ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
      pc[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
     pd[i]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
     sprintf(ShapoidErr->_msg, "ShapoidRotCenter failed");
     PBErrCatch(ShapoidErr);
   }
 ShapoidRotCenter(pyramidoid, theta);
  float pe[2] = \{0.6666667, 0.0\};
 float pf[2] = \{0.0, 1.0\};
  float pg[2] = \{-1.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
     pe[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
     pf[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
     pg[i]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
     sprintf(ShapoidErr->_msg, "ShapoidRotCenter failed");
     PBErrCatch(ShapoidErr);
   }
 ShapoidRotCenter(spheroid, theta);
  float ph[2] = \{0.0, 0.0\};
 float pi[2] = \{0.0, 1.0\};
  float pj[2] = \{-1.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
     ph[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
     pi[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
     pj[i]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotCenter failed");
```

```
PBErrCatch(ShapoidErr);
 }
ShapoidRotOrigin(facoid, theta);
float pk[2] = \{0.0, 1.0\};
float pl[2] = \{-1.0, 0.0\};
float pm[2] = \{0.0, -1.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pl[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pm[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotOrigin failed");
    PBErrCatch(ShapoidErr);
ShapoidRotOrigin(pyramidoid, theta);
float pn[2] = {0.0, 0.6666667};
float po[2] = {-1.0, 0.0};
float pp[2] = \{0.0, -1.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
    pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
    po[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
    pp[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotOrigin failed");
    PBErrCatch(ShapoidErr);
ShapoidRotOrigin(spheroid, theta);
float pq[2] = \{0.0, 0.0\};
float pr[2] = \{-1.0, 0.0\};
float ps[2] = {0.0, -1.0};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
    pr[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
    ps[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotOrigin failed");
    PBErrCatch(ShapoidErr);
ShapoidRotStart(facoid, theta);
float pt[2] = \{0.0, 1.0\};
float pu[2] = {0.0, -1.0};
float pv[2] = \{1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pt[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pu[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pv[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotStart failed");
```

```
PBErrCatch(ShapoidErr);
   }
  ShapoidRotStart(pyramidoid, theta);
  float pw[2] = \{0.0, 0.6666667\};
  float px[2] = \{0.0, -1.0\};
  float py[2] = {1.0, 0.0};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
      pw[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
      px[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
      py[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotStart failed");
      PBErrCatch(ShapoidErr);
   }
  ShapoidRotStart(spheroid, theta);
  float pz[2] = \{0.0, 0.0\};
  float paa[2] = \{0.0, -1.0\};
  float pab[2] = \{1.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
      pz[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
      paa[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
      pab[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotStart failed");
      PBErrCatch(ShapoidErr);
   }
  ShapoidFree(&facoid);
  ShapoidFree(&pyramidoid);
  ShapoidFree(&spheroid);
 printf("UnitTestRotate OK\n");
}
void UnitTestRotateAxis() {
  int dim = 3;
  Facoid* facoid = FacoidCreate(dim):
  Pyramidoid* pyramidoid = PyramidoidCreate(dim);
  Spheroid* spheroid = SpheroidCreate(dim);
  float theta = PBMATH_HALFPI;
  VecFloat3D axis = VecFloatCreateStatic3D();
  VecSet(&axis, 0, 1.0); VecSet(&axis, 1, 1.0); VecSet(&axis, 2, 1.0);
  VecNormalise(&axis);
  ShapoidRotAxisCenter(facoid, &axis, theta);
  float pb[3] = \{0.0, 0.0, 0.0\};
  float pc[3] = \{0.333333, 0.910684, -0.244017\};
  float pd[3] = {-0.244017, 0.333333, 0.910684};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pb[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
      pc[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
      pd[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotAxisCenter failed");
```

```
PBErrCatch(ShapoidErr);
 }
ShapoidRotAxisCenter(pyramidoid, &axis, theta);
float pe[3] = {0.000000, 0.000000, 0.000000};
float pf[3] = {0.3333333, 0.910684, -0.244017};
float pg[3] = \{-0.244017, 0.333333, 0.910684\};
for (int i = dim; i--;) {
 if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
   pe[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   pf[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
   pg[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotAxisCenter failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotAxisCenter(spheroid, &axis, theta);
float ph[3] = \{0.0, 0.0, 0.0\};
float pi[3] = {0.3333333, 0.910684, -0.244017};
float pj[3] = {-0.244017, 0.333333, 0.910684};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    ph[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
   pi[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
   pj[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotAxisCenter failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotAxisOrigin(facoid, &axis, theta);
float pk[3] = \{0.0, 0.0, 0.0\};
float pl[3] = \{-0.333333, 0.666667, 0.666667\};
float pm[3] = {0.666667, -0.333333, 0.666667};
for (int i = dim; i--;) {
 if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
   pl[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pm[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotAxisOrigin failed");
   PBErrCatch(ShapoidErr);
ShapoidRotAxisOrigin(pyramidoid, &axis, theta);
float pn[3] = \{0.0, 0.0, 0.0\};
float po[3] = \{-0.333333, 0.666667, 0.666667\};
float pp[3] = {0.666667, -0.333333, 0.666667};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
   pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   po[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
    pp[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(ShapoidErr->_msg, "ShapoidRotAxisOrigin failed");
   PBErrCatch(ShapoidErr);
}
ShapoidRotAxisOrigin(spheroid, &axis, theta);
float pq[3] = \{0.0, 0.0, 0.0\};
float pr[3] = {-0.333333, 0.666667, 0.666667};
float ps[3] = \{0.666667, -0.333333, 0.666667\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
   pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
    pr[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
   ps[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidRotAxisOrigin failed");
   PBErrCatch(ShapoidErr);
ShapoidRotAxisStart(facoid, &axis, theta);
float pt[3] = \{0.0, 0.0, 0.0\};
float pu[3] = {0.3333333, -0.244017, 0.910683};
float pv[3] = {0.910683, 0.333333, -0.244017};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pt[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
   pu[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
   pv[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotAxisStart failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotAxisStart(pyramidoid, &axis, theta);
float pw[3] = \{0.0, 0.0, 0.0\};
float px[3] = \{0.333333, -0.244017, 0.910683\};
float py[3] = {0.910683, 0.333333, -0.244017};
for (int i = dim; i--;) {
 if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
   pw[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   px[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
   py[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotAxisStart failed");
   PBErrCatch(ShapoidErr);
ShapoidRotAxisStart(spheroid, &axis, theta);
float pz[3] = \{0.0, 0.0, 0.0\};
float paa[3] = {0.333333, -0.244017, 0.910683};
float pab[3] = {0.910683, 0.333333, -0.244017};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pz[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
   paa[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
   pab[i]) == false) {
```

```
ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotAxisStart failed");
      PBErrCatch(ShapoidErr);
   }
  }
  ShapoidFree(&facoid);
  ShapoidFree(&pyramidoid);
  ShapoidFree(&spheroid);
  printf("UnitTestRotateAxis OK\n");
void UnitTestRotateX() {
  int dim = 3:
  Facoid* facoid = FacoidCreate(dim);
  Pyramidoid* pyramidoid = PyramidoidCreate(dim);
  Spheroid* spheroid = SpheroidCreate(dim);
  float theta = PBMATH_HALFPI;
  ShapoidRotXCenter(facoid, theta);
  float pb[3] = \{0.0, 1.0, 0.0\};
  float pc[3] = \{1.0, 0.0, 0.0\};
  float pd[3] = \{0.0, 0.0, 1.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pb[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
      pc[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
      pd[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotXCenter failed");
      PBErrCatch(ShapoidErr);
   }
  ShapoidRotXCenter(pyramidoid, theta);
  float pe[3] = \{0.0, 0.5, 0.0\};
  float pf[3] = \{1.0, 0.0, 0.0\};
  float pg[3] = \{0.0, 0.0, 1.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
      pe[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
      pf[i]) == false ||
      {\tt ISEQUALF(VecGet(((Shapoid*)pyramidoid) ->\_axis[1],\ i),}\\
      pg[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotXCenter failed");
      PBErrCatch(ShapoidErr);
   }
  ShapoidRotXCenter(spheroid, theta);
  float ph[3] = \{0.0, 0.0, 0.0\};
  float pi[3] = \{1.0, 0.0, 0.0\};
  float pj[3] = \{0.0, 0.0, 1.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
      ph[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
      pi[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
      pj[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotXCenter failed");
      PBErrCatch(ShapoidErr);
```

```
}
ShapoidRotXOrigin(facoid, theta);
float pk[3] = {0.0, 0.0, 1.0};
float pl[3] = \{1.0, 0.0, 0.0\};
float pm[3] = {0.0, -1.0, 0.0};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pl[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pm[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotXOrigin failed");
    PBErrCatch(ShapoidErr);
 }
ShapoidRotXOrigin(pyramidoid, theta);
float pn[3] = {0.0, 0.0, 0.5};
float po[3] = \{1.0, 0.0, 0.0\};
float pp[3] = \{0.0, -1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
    pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
    po[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
    pp[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotXOrigin failed");
    PBErrCatch(ShapoidErr);
 }
ShapoidRotXOrigin(spheroid, theta);
float pq[3] = \{0.0, 0.0, 0.0\};
float pr[3] = {1.0, 0.0, 0.0};
float ps[3] = \{0.0, -1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
    pr[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
    ps[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotXOrigin failed");
    PBErrCatch(ShapoidErr);
  }
ShapoidRotXStart(facoid, theta);
float pt[3] = \{0.0, 0.0, 1.0\};
float pu[3] = \{1.0, 0.0, 0.0\};
float pv[3] = \{0.0, 0.0, -1.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pt[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pu[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pv[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotXStart failed");
    PBErrCatch(ShapoidErr);
```

```
}
  ShapoidRotXStart(pyramidoid, theta);
 float pw[3] = \{0.0, 0.0, 0.5\};
  float px[3] = \{1.0, 0.0, 0.0\};
 float py[3] = \{0.0, 0.0, -1.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
     pw[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
     px[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
      py[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotXStart failed");
     PBErrCatch(ShapoidErr);
 }
  ShapoidRotXStart(spheroid, theta);
 float pz[3] = \{0.0, 0.0, 0.0\};
  float paa[3] = {1.0, 0.0, 0.0};
  float pab[3] = {0.0, 0.0, -1.0};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
     pz[i]) == false ||
     ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
     paa[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
      pab[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotXStart failed");
     PBErrCatch(ShapoidErr);
 ShapoidFree(&facoid);
 ShapoidFree(&pyramidoid);
 ShapoidFree(&spheroid);
 printf("UnitTestRotateX OK\n");
void UnitTestRotateY() {
 int dim = 3;
  Facoid* facoid = FacoidCreate(dim);
 Pyramidoid* pyramidoid = PyramidoidCreate(dim);
 Spheroid* spheroid = SpheroidCreate(dim);
  float theta = PBMATH_HALFPI;
 ShapoidRotYCenter(facoid, theta);
  float pb[3] = \{0.0, 0.0, 1.0\};
 float pc[3] = \{0.0, 0.0, -1.0\};
  float pd[3] = \{0.0, 1.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pb[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
     pc[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
     pd[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotYCenter failed");
      PBErrCatch(ShapoidErr);
  ShapoidRotYCenter(pyramidoid, theta);
```

```
float pe[3] = \{0.0, 0.0, 0.5\};
float pf[3] = \{0.0, 0.0, -1.0\};
float pg[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
   pe[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   pf[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
   pg[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYCenter failed");
   PBErrCatch(ShapoidErr);
ShapoidRotYCenter(spheroid, theta);
float ph[3] = \{0.0, 0.0, 0.0\};
float pi[3] = \{0.0, 0.0, -1.0\};
float pj[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
   ph[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
   pi[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
    pj[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYCenter failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotYOrigin(facoid, theta);
float pk[3] = \{1.0, 0.0, 0.0\};
float pl[3] = \{-1.0, 0.0, 0.0\};
float pm[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
   pl[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
   pm[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYOrigin failed");
   PBErrCatch(ShapoidErr);
ShapoidRotYOrigin(pyramidoid, theta);
float pn[3] = {0.5, 0.0, 0.0};
float po[3] = \{-1.0, 0.0, 0.0\};
float pp[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
    pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   po[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
   pp[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYOrigin failed");
   PBErrCatch(ShapoidErr);
}
```

```
ShapoidRotYOrigin(spheroid, theta);
float pq[3] = \{0.0, 0.0, 0.0\};
float pr[3] = \{-1.0, 0.0, 0.0\};
float ps[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
   pr[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
   ps[i]) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYOrigin failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotYStart(facoid, theta);
float pt[3] = {1.0, 0.0, 0.0};
float pu[3] = \{0.0, 0.0, 1.0\};
float pv[3] = {0.0, 1.0, 0.0};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pt[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pu[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pv[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYStart failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotYStart(pyramidoid, theta);
float pw[3] = \{0.5, 0.0, 0.0\};
float px[3] = \{0.0, 0.0, 1.0\};
float py[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
   pw[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
   px[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
   py[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYStart failed");
   PBErrCatch(ShapoidErr);
 }
ShapoidRotYStart(spheroid, theta);
float pz[3] = \{0.0, 0.0, 0.0\};
float paa[3] = {0.0, 0.0, 1.0};
float pab[3] = \{0.0, 1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pz[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
    paa[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
    pab[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotYStart failed");
   PBErrCatch(ShapoidErr);
```

```
ShapoidFree(&facoid);
  ShapoidFree(&pyramidoid);
 ShapoidFree(&spheroid);
 printf("UnitTestRotateY OK\n");
void UnitTestRotateZ() {
 int dim = 3;
 Facoid* facoid = FacoidCreate(dim);
  Pyramidoid* pyramidoid = PyramidoidCreate(dim);
 Spheroid* spheroid = SpheroidCreate(dim);
  float theta = PBMATH_HALFPI;
 ShapoidRotZCenter(facoid, theta);
  float pb[3] = \{1.0, 0.0, 0.0\};
  float pc[3] = \{0.0, 1.0, 0.0\};
 float pd[3] = \{-1.0, 0.0, 0.0\};
  for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pb[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
      pc[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
     pd[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotZCenter failed");
     PBErrCatch(ShapoidErr);
   }
 ShapoidRotZCenter(pyramidoid, theta);
 float pe[3] = \{0.5, 0.0, 0.0\};
  float pf[3] = \{0.0, 1.0, 0.0\};
  float pg[3] = \{-1.0, 0.0, 0.0\};
 for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
      pe[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
      pf[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
     pg[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotZCenter failed");
     PBErrCatch(ShapoidErr);
 ShapoidRotZCenter(spheroid, theta);
 float ph[3] = \{0.0, 0.0, 0.0\};
  float pi[3] = {0.0, 1.0, 0.0};
  float pj[3] = \{-1.0, 0.0, 0.0\};
 for (int i = dim; i--;) {
    if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
      ph[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
      pi[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
     pj[i]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidRotZCenter failed");
     PBErrCatch(ShapoidErr);
 ShapoidRotZOrigin(facoid, theta);
 float pk[3] = \{0.0, 1.0, 0.0\};
```

```
float p1[3] = \{-1.0, 0.0, 0.0\};
float pm[3] = \{0.0, -1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pl[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pm[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotZOrigin failed");
    PBErrCatch(ShapoidErr);
ShapoidRotZOrigin(pyramidoid, theta);
float pn[3] = \{0.0, 0.5, 0.0\};
float po[3] = \{-1.0, 0.0, 0.0\};
float pp[3] = \{0.0, -1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
    pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
    po[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
    pp[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotZOrigin failed");
    PBErrCatch(ShapoidErr);
 }
ShapoidRotZOrigin(spheroid, theta);
float pq[3] = \{0.0, 0.0, 0.0\};
float pr[3] = \{-1.0, 0.0, 0.0\};
float ps[3] = \{0.0, -1.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
    pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
    pr[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
    ps[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotZOrigin failed");
    PBErrCatch(ShapoidErr);
 }
ShapoidRotZStart(facoid, theta);
float pt[3] = {0.0, 1.0, 0.0};
float pu[3] = \{0.0, -1.0, 0.0\};
float pv[3] = \{1.0, 0.0, 0.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)facoid)->_pos, i), pt[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[0], i),
    pu[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)facoid)->_axis[1], i),
    pv[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidRotZStart failed");
    PBErrCatch(ShapoidErr);
ShapoidRotZStart(pyramidoid, theta);
float pw[3] = \{0.0, 0.5, 0.0\};
```

```
float px[3] = \{0.0, -1.0, 0.0\};
 float py[3] = \{1.0, 0.0, 0.0\};
 for (int i = dim; i--;) {
   if (ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_pos, i),
     pw[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[0], i),
     px[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)pyramidoid)->_axis[1], i),
     py[i]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
     sprintf(ShapoidErr->_msg, "ShapoidRotZStart failed");
     PBErrCatch(ShapoidErr);
   }
 ShapoidRotZStart(spheroid, theta);
 float pz[3] = \{0.0, 0.0, 0.0\};
 float paa[3] = \{0.0, -1.0, 0.0\};
 float pab[3] = {1.0, 0.0, 0.0};
 for (int i = dim; i--;) {
   if (ISEQUALF(VecGet(((Shapoid*)spheroid)->_pos, i),
     pz[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[0], i),
     paa[i]) == false ||
      ISEQUALF(VecGet(((Shapoid*)spheroid)->_axis[1], i),
     pab[i]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
     sprintf(ShapoidErr->_msg, "ShapoidRotZStart failed");
     PBErrCatch(ShapoidErr);
   }
 ShapoidFree(&facoid);
 ShapoidFree(&pyramidoid);
 ShapoidFree(&spheroid);
 printf("UnitTestRotateZ \ OK\n");\\
void UnitTestImportExportCoordIsPosInside() {
 int dim = 2;
 Facoid* facoid = FacoidCreate(dim);
 Pyramidoid* pyramidoid = PyramidoidCreate(dim);
 Spheroid* spheroid = SpheroidCreate(dim);
 VecFloat* v = VecFloatCreate(dim);
 for (int i = dim; i--;)
   VecSet(v, i, 1.0 + (float)i);
 ShapoidTranslate(facoid, v);
 ShapoidTranslate(pyramidoid, v);
 ShapoidTranslate(spheroid, v);
 float scale = -2.0;
 ShapoidScale(facoid, scale);
 ShapoidScale(pyramidoid, scale);
 ShapoidScale(spheroid, scale);
 int nbTest = 100;
 srandom(RANDOMSEED);
 for (int iTest = nbTest; iTest--;) {
   VecFloat* posReal = VecFloatCreate(dim);
   for (int i = dim; i--;)
     VecSet(posReal, i, (rnd() - 0.5) * 10.0);
   VecFloat* posShapoidA = ShapoidImportCoord(facoid, posReal);
   bool isInside = ShapoidIsPosInside(facoid, posReal);
   if (VecGet(posShapoidA, 0) >= 0.0 &&
     VecGet(posShapoidA, 0) <= 1.0 &&</pre>
     VecGet(posShapoidA, 1) >= 0.0 &&
```

```
VecGet(posShapoidA, 1) <= 1.0) {</pre>
  if (isInside == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
    PBErrCatch(ShapoidErr);
} else {
  if (isInside == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
    PBErrCatch(ShapoidErr);
VecOp(posShapoidA, scale, v, 1.0);
if (VecIsEqual(posReal, posShapoidA) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidImportCoord failed");
  PBErrCatch(ShapoidErr);
VecFree(&posShapoidA);
VecFloat* posShapoidB = ShapoidImportCoord(pyramidoid, posReal);
isInside = ShapoidIsPosInside(pyramidoid, posReal);
if (VecGet(posShapoidB, 0) >= 0.0 &&
  VecGet(posShapoidB, 0) <= 1.0 &&</pre>
  VecGet(posShapoidB, 1) >= 0.0 &&
  VecGet(posShapoidB, 1) <= 1.0 &&</pre>
  VecGet(posShapoidB, 0) + VecGet(posShapoidB, 1) <= 1.0) {</pre>
  if (isInside == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
    PBErrCatch(ShapoidErr);
} else {
  if (isInside == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
    PBErrCatch(ShapoidErr);
VecOp(posShapoidB, scale, v, 1.0);
if (VecIsEqual(posReal, posShapoidB) == false) {
  ShapoidErr->_type = PBErrTypeUnitTestFailed;
  sprintf(ShapoidErr->_msg, "ShapoidImportCoord failed");
  PBErrCatch(ShapoidErr);
VecFree(&posShapoidB);
VecFloat* posShapoidC = ShapoidImportCoord(spheroid, posReal);
isInside = ShapoidIsPosInside(spheroid, posReal);
if (VecGet(posShapoidC, 0) >= -0.5 &&
  VecGet(posShapoidC, 0) <= 0.5 &&
  VecGet(posShapoidC, 1) >= -0.5 &&
  VecGet(posShapoidC, 1) <= 0.5 &&
  pow(VecGet(posShapoidC, 0), 2.0) +
  pow(VecGet(posShapoidC, 1), 2.0) <= 0.25) {</pre>
  if (isInside == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
    PBErrCatch(ShapoidErr);
} else {
  if (isInside == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
```

```
sprintf(ShapoidErr->_msg, "ShapoidIsPosInside failed");
        PBErrCatch(ShapoidErr);
    VecOp(posShapoidC, scale, v, 1.0);
    if (VecIsEqual(posReal, posShapoidC) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidImportCoord failed");
      PBErrCatch(ShapoidErr);
    VecFree(&posShapoidC);
    VecFree(&posReal);
  for (int iTest = nbTest; iTest--;) {
    VecFloat* posShapoid = VecFloatCreate(dim);
    for (int i = dim; i--;)
      VecSet(posShapoid, i, (rnd() - 0.5) * 10.0);
    VecFloat* posRealA = ShapoidExportCoord(facoid, posShapoid);
    VecOp(posRealA, 1.0, v, -1.0);
VecScale(posRealA, 1.0 / scale);
    if (VecIsEqual(posRealA, posShapoid) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidExportCoord failed");
      PBErrCatch(ShapoidErr);
    VecFree(&posRealA);
    VecFloat* posRealB = ShapoidExportCoord(pyramidoid, posShapoid);
    VecOp(posRealB, 1.0, v, -1.0);
VecScale(posRealB, 1.0 / scale);
    if (VecIsEqual(posRealB, posShapoid) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidExportCoord failed");
      PBErrCatch(ShapoidErr);
    VecFree(&posRealB);
    VecFloat* posRealC = ShapoidExportCoord(facoid, posShapoid);
    VecOp(posRealC, 1.0, v, -1.0);
    VecScale(posRealC, 1.0 / scale);
if (VecIsEqual(posRealC, posShapoid) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidExportCoord failed");
      PBErrCatch(ShapoidErr);
    VecFree(&posRealC);
    VecFree(&posShapoid);
  VecFree(&v);
  ShapoidFree(&facoid);
  ShapoidFree(&pyramidoid);
  ShapoidFree(&spheroid);
  printf("UnitTestImportExportCoordIsPosInside OK\n");
void UnitTestGetBoundingBox() {
  int dim = 2;
  Facoid* facoid = FacoidCreate(dim);
  Pyramidoid* pyramidoid = PyramidoidCreate(dim);
  Spheroid* spheroid = SpheroidCreate(dim);
  VecFloat* v = VecFloatCreate(dim);
  for (int i = dim; i--;)
    VecSet(v, i, 1.0 + (float)i);
  ShapoidTranslate(facoid, v);
```

```
ShapoidTranslate(pyramidoid, v);
ShapoidTranslate(spheroid, v);
float scale = -2.0;
ShapoidScale(facoid, scale);
ShapoidScale(pyramidoid, scale);
ShapoidScale(spheroid, scale);
float theta = PBMATH_QUARTERPI;
ShapoidRotCenter(facoid, theta);
ShapoidRotCenter(pyramidoid, theta);
ShapoidRotCenter(spheroid, theta);
Facoid* boundA = ShapoidGetBoundingBox(facoid);
float pa[2] = {-1.414214, -0.414213};
float pb[2] = {2.828427, 0.0};
float pc[2] = \{0.0, 2.828427\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundA)->_pos, i),
    pa[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundA)->_axis[0], i),
    pb[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundA)->_axis[1], i),
    pc[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
 }
Facoid* boundB = ShapoidGetBoundingBox(pyramidoid);
float pd[2] = \{-1.08088, 0.86193\};
float pe[2] = \{2.82843, 0.0\};
float pf[2] = \{0.0, 1.41421\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundB)->_pos, i), pd[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundB)->_axis[0], i),
    pe[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundB)->_axis[1], i),
    pf[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
Facoid* boundC = ShapoidGetBoundingBox(spheroid);
float pg[2] = \{-0.414214, 0.585786\};
float ph[2] = {2.828427, 0.0};
float pi[2] = {0.0, 2.828427};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundC)->_pos, i), pg[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundC)->_axis[0], i),
    ph[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundC)->_axis[1], i),
    pi[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
 }
GSetShapoid set = GSetShapoidCreateStatic();
GSetPush(&set, facoid);
GSetPush(&set, pyramidoid);
GSetPush(&set, spheroid);
Facoid* boundD = ShapoidGetBoundingBox(&set);
float pj[2] = \{-1.41421, -0.41421\};
```

```
float pk[2] = \{3.828427, 0.0\};
float p1[2] = \{0.0, 3.828427\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundD)->_pos, i), pj[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundD)->_axis[0], i),
    pk[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundD)->_axis[1], i),
    pl[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
GSetFlush(&set);
VecSet(v, 0, 2.0); VecSet(v, 1, 4.0);
ShapoidSetPos(facoid, v);
ShapoidSetPos(pyramidoid, v);
VecSet(v, 0, 7.0); VecSet(v, 1, 0.0);
ShapoidSetAxis(facoid, 0, v);
ShapoidSetAxis(pyramidoid, 0, v);
VecSet(v, 0, 0.0); VecSet(v, 1, 4.0);
ShapoidSetAxis(facoid, 1, v);
ShapoidSetAxis(pyramidoid, 1, v);
Facoid* boundE = ShapoidGetBoundingBox(facoid);
float pm[2] = \{2.0, 4.0\};
float pn[2] = \{7.0, 0.0\};
float po[2] = \{0.0, 4.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundE)->_pos, i), pm[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundE)->_axis[0], i),
    pn[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundE)->_axis[1], i),
    po[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
 }
Facoid* boundF = ShapoidGetBoundingBox(pyramidoid);
float pp[2] = \{2.0, 4.0\};
float pq[2] = \{7.0, 0.0\};
float pr[2] = \{0.0, 4.0\};
for (int i = dim; i--;) {
  if (ISEQUALF(VecGet(((Shapoid*)boundF)->_pos, i), pp[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundF)->_axis[0], i),
    pq[i]) == false ||
    ISEQUALF(VecGet(((Shapoid*)boundF)->_axis[1], i),
    pr[i]) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetBoundingBox failed");
    PBErrCatch(ShapoidErr);
}
ShapoidFree(&boundA);
ShapoidFree(&boundB);
ShapoidFree(&boundC);
ShapoidFree(&boundD);
ShapoidFree(&boundE);
ShapoidFree(&boundF);
VecFree(&v);
ShapoidFree(&facoid);
ShapoidFree(&pyramidoid);
```

```
ShapoidFree(&spheroid);
 printf("UnitTestGetBoundingBox OK\n");
void UnitTestGetPosDepthCenterCoverage() {
 int dim = 2;
 Facoid* facoid = FacoidCreate(dim);
 Pyramidoid* pyramidoid = PyramidoidCreate(dim);
 Spheroid* spheroid = SpheroidCreate(dim);
 VecFloat* center = ShapoidGetCenter(facoid);
 if (ISEQUALF(VecGet(center, 0), 0.5) == false ||
   ISEQUALF(VecGet(center, 1), 0.5) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCenter failed");
   PBErrCatch(ShapoidErr);
 VecFree(&center);
 center = ShapoidGetCenter(pyramidoid);
 if (ISEQUALF(VecGet(center, 0), 0.333333) == false ||
   ISEQUALF(VecGet(center, 1), 0.333333) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCenter failed");
   PBErrCatch(ShapoidErr);
 VecFree(&center);
 center = ShapoidGetCenter(spheroid);
 if (ISEQUALF(VecGet(center, 0), 0.0) == false ||
   ISEQUALF(VecGet(center, 1), 0.0) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCenter failed");
   PBErrCatch(ShapoidErr);
 VecFree(&center);
 float coverage = ShapoidGetCoverageDelta(facoid, pyramidoid, 0.001);
 if (ISEQUALF(coverage, 1.0) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
   PBErrCatch(ShapoidErr);
 coverage = ShapoidGetCoverageDelta(pyramidoid, facoid, 0.001);
 if (ISEQUALF(coverage, 0.500499) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
   PBErrCatch(ShapoidErr);
 coverage = ShapoidGetCoverageDelta(pyramidoid, spheroid, 0.001);
 if (ISEQUALF(coverage, 0.24937) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
   PBErrCatch(ShapoidErr);
 coverage = ShapoidGetCoverageDelta(spheroid, pyramidoid, 0.001);
 if (ISEQUALF(coverage, 0.39251) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
   PBErrCatch(ShapoidErr);
 coverage = ShapoidGetCoverageDelta(facoid, spheroid, 0.001);
 if (ISEQUALF(coverage, 0.24937) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
   PBErrCatch(ShapoidErr);
```

```
coverage = ShapoidGetCoverageDelta(spheroid, facoid, 0.001);
  if (ISEQUALF(coverage, 0.196451) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetCoverage failed");
    PBErrCatch(ShapoidErr);
  VecFloat2D pos = VecFloatCreateStatic2D();
  VecSet(&pos, 0, 0.333333); VecSet(&pos, 1, 0.333333);
  float depth = ShapoidGetPosDepth(facoid, (VecFloat*)&pos);
  if (ISEQUALF(depth, 0.790123) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
sprintf(ShapoidErr->_msg, "ShapoidGetPosDepth failed");
    PBErrCatch(ShapoidErr);
  depth = ShapoidGetPosDepth(pyramidoid, (VecFloat*)&pos);
  if (ISEQUALF(depth, 1.0) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetPosDepth failed");
    PBErrCatch(ShapoidErr);
  depth = ShapoidGetPosDepth(spheroid, (VecFloat*)&pos);
  if (ISEQUALF(depth, 0.057192) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidGetPosDepth failed");
    PBErrCatch(ShapoidErr);
  ShapoidFree(&facoid);
  ShapoidFree(&pyramidoid);
  ShapoidFree(&spheroid);
  printf("UnitTestGetPosDepthCenterCoverage OK\n");
void UnitTestFacoidAlignedIsInsideFacoidAligned() {
  Facoid* facA = FacoidCreate(2);
  Facoid* facB = FacoidCreate(2);
  VecFloat2D p = VecFloatCreateStatic2D();
  VecFloat2D u = VecFloatCreateStatic2D();
  VecFloat2D v = VecFloatCreateStatic2D();
  VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.0);
  VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
  ShapoidSetPos(facA, &p);
  ShapoidSetAxis(facA, 0, &u);
  ShapoidSetAxis(facA, 1, &v);
  VecSet(&p, 0, 2.0); VecSet(&p, 1, 2.0);
  VecSet(&u, 0, 0.5); VecSet(&v, 1, 0.5);
  ShapoidSetPos(facB, &p);
  ShapoidSetAxis(facB, 0, &u);
  ShapoidSetAxis(facB, 1, &v);
  if (FacoidAlignedIsInsideFacoidAligned(facA, facB) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsInsideFacoidAligned failed");
    PBErrCatch(ShapoidErr);
  VecSet(&p, 0, 0.1); VecSet(&p, 1, 0.1);
  ShapoidSetPos(facB, &p);
  if (FacoidAlignedIsInsideFacoidAligned(facB, facA) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsInsideFacoidAligned failed");
    PBErrCatch(ShapoidErr);
```

```
VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
  ShapoidSetAxis(facB, 0, &u);
  ShapoidSetAxis(facB, 1, &v);
  if (FacoidAlignedIsInsideFacoidAligned(facB, facA) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsInsideFacoidAligned failed");
   PBErrCatch(ShapoidErr);
 ShapoidFree(&facA);
 ShapoidFree(&facB);
 printf("UnitTestFacoidAlignedIsInsideFacoidAligned OK\n");
void UnitTestFacoidAlignedIsOutsideFacoidAligned() {
 Facoid* facA = FacoidCreate(2);
 Facoid* facB = FacoidCreate(2);
  VecFloat2D p = VecFloatCreateStatic2D();
 VecFloat2D u = VecFloatCreateStatic2D();
  VecFloat2D v = VecFloatCreateStatic2D();
  VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.0);
  VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
  ShapoidSetPos(facA, &p);
  ShapoidSetAxis(facA, 0, &u);
  ShapoidSetAxis(facA, 1, &v);
  VecSet(&p, 0, 2.0); VecSet(&p, 1, 2.0);
  VecSet(&u, 0, 0.5); VecSet(&v, 1, 0.5);
  ShapoidSetPos(facB, &p);
  ShapoidSetAxis(facB, 0, &u);
  ShapoidSetAxis(facB, 1, &v);
  if (FacoidAlignedIsOutsideFacoidAligned(facA, facB) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsOutsideFacoidAligned failed");
    PBErrCatch(ShapoidErr);
  VecSet(&p, 0, 0.1); VecSet(&p, 1, 0.1);
 ShapoidSetPos(facB, &p);
  if (FacoidAlignedIsOutsideFacoidAligned(facB, facA) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsOutsideFacoidAligned failed");
   PBErrCatch(ShapoidErr);
  VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
  ShapoidSetAxis(facB, 0, &u);
  ShapoidSetAxis(facB, 1, &v);
  if (FacoidAlignedIsOutsideFacoidAligned(facB, facA) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedIsOutsideFacoidAligned failed");
   PBErrCatch(ShapoidErr);
 ShapoidFree(&facA);
 ShapoidFree(&facB);
 printf("UnitTestFacoidAlignedIsOutsideFacoidAligned OK\n");
void UnitTestFacoidAlignedSplitExcludingFacoidAligned() {
 Facoid* facA = FacoidCreate(2);
 Facoid* facB = FacoidCreate(2);
```

```
VecFloat2D p = VecFloatCreateStatic2D();
 VecFloat2D u = VecFloatCreateStatic2D();
 VecFloat2D v = VecFloatCreateStatic2D();
 VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.0);
 VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
 ShapoidSetPos(facA, &p);
 ShapoidSetAxis(facA, 0, &u);
 ShapoidSetAxis(facA, 1, &v);
 VecSet(&p, 0, 0.5); VecSet(&p, 1, 0.5);
 VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
 ShapoidSetPos(facB, &p);
 ShapoidSetAxis(facB, 0, &u);
 ShapoidSetAxis(facB, 1, &v);
 GSetShapoid* split =
   FacoidAlignedSplitExcludingFacoidAligned(facA, facB);
 Facoid* facC = (Facoid*)GSetPop(split);
 VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.0);
 VecSet(&u, 0, 1.0); VecSet(&v, 1, 0.5);
 if (VecIsEqual(ShapoidPos(facC), &p) == false ||
   VecIsEqual(ShapoidAxis(facC, 0), &u) == false ||
   VecIsEqual(ShapoidAxis(facC, 1), &v) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg,
      "FacoidAlignedSplitExcludingFacoidAligned failed");
   PBErrCatch(ShapoidErr);
 Facoid* facD = (Facoid*)GSetPop(split);
 VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.5);
 VecSet(&u, 0, 0.5); VecSet(&v, 1, 0.5);
 if (VecIsEqual(ShapoidPos(facD), &p) == false ||
   VecIsEqual(ShapoidAxis(facD, 0), &u) == false ||
   VecIsEqual(ShapoidAxis(facD, 1), &v) == false) {
   ShapoidErr->_type = PBErrTypeUnitTestFailed;
   sprintf(ShapoidErr->_msg,
      "FacoidAlignedSplitExcludingFacoidAligned failed");
   PBErrCatch(ShapoidErr);
 GSetFree(&split);
 ShapoidFree(&facA);
 ShapoidFree(&facB);
 ShapoidFree(&facC);
 ShapoidFree(&facD);
 printf("UnitTestFacoidAlignedSplitExcludingFacoidAligned OK\n");
void UnitTestFacoidAlignedAddClippedToSet() {
 Facoid* facA = FacoidCreate(2);
 VecFloat2D p = VecFloatCreateStatic2D();
 VecFloat2D u = VecFloatCreateStatic2D();
 VecFloat2D v = VecFloatCreateStatic2D();
 VecSet(&p, 0, 0.0); VecSet(&p, 1, 0.0);
 VecSet(&u, 0, 10.0); VecSet(&v, 1, 10.0);
 ShapoidSetPos(facA, &p);
 ShapoidSetAxis(facA, 0, &u);
 ShapoidSetAxis(facA, 1, &v);
 GSetShapoid set = GSetShapoidCreateStatic();
 FacoidAlignedAddClippedToSet(facA, &set);
 VecSet(&p, 0, 15.0); VecSet(&p, 1, 15.0);
 ShapoidSetPos(facA, &p);
 FacoidAlignedAddClippedToSet(facA, &set);
 VecSet(&p, 0, 8.0); VecSet(&p, 1, 8.0);
 ShapoidSetPos(facA, &p);
```

```
FacoidAlignedAddClippedToSet(facA, &set);
  VecSet(&p, 0, 12.0); VecSet(&p, 1, 9.0);
  ShapoidSetPos(facA, &p);
  VecSet(&u, 0, 1.0); VecSet(&v, 1, 10.0);
  ShapoidSetAxis(facA, 0, &u);
  ShapoidSetAxis(facA, 1, &v);
  FacoidAlignedAddClippedToSet(facA, &set);
  VecSet(&p, 0, 5.0); VecSet(&p, 1, 5.0);
  ShapoidSetPos(facA, &p);
  VecSet(&u, 0, 1.0); VecSet(&v, 1, 1.0);
  ShapoidSetAxis(facA, 0, &u);
  ShapoidSetAxis(facA, 1, &v);
  FacoidAlignedAddClippedToSet(facA, &set);
  if (GSetNbElem(&set) != 6) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg,
      "FacoidAlignedAddClippedToSet failed");
   PBErrCatch(ShapoidErr);
 int iCheck = 0;
  float checkp[12] = {
     0.0, 0.0, 15.0, 15.0, 10.0, 8.0, 8.0,
     10.0, 8.0, 15.0, 12.0, 18.0};
  float checku[6] = {10.0, 10.0, 8.0, 10.0, 7.0, 1.0};
  float checkv[6] = {10.0, 10.0, 2.0, 5.0, 3.0, 1.0};
    Facoid* fac = (Facoid*)GSetPop(&set);
    VecSet(&p, 0, checkp[2 * iCheck]);
    VecSet(&p, 1, checkp[2 * iCheck + 1]);
    VecSet(&u, 0, checku[iCheck]); VecSet(&v, 1, checkv[iCheck]);
    if (VecIsEqual(ShapoidPos(fac), &p) == false ||
      VecIsEqual(ShapoidAxis(fac, 0), &u) == false ||
      VecIsEqual(ShapoidAxis(fac, 1), &v) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg,
        "FacoidAlignedAddClippedToSet failed");
     PBErrCatch(ShapoidErr);
    ShapoidFree(&fac);
    ++iCheck;
  } while(GSetNbElem(&set) > 0);
 ShapoidFree(&facA);
 printf("UnitTestFacoidAlignedAddClippedToSet OK\n");
void UnitTestIsInter() {
 Spheroid* spheroidA = SpheroidCreate(3);
 Spheroid* spheroidB = SpheroidCreate(3);
  VecFloat3D v = VecFloatCreateStatic3D();
  if (ShapoidIsInter(spheroidA, spheroidB) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsInter failed");
   PBErrCatch(ShapoidErr);
 VecSet(&v, 0, 1.1);
  ShapoidSetPos(spheroidB, &v);
  if (ShapoidIsInter(spheroidB, spheroidA) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsInter failed");
   PBErrCatch(ShapoidErr);
  VecSet(&v, 1, 1.0);
```

```
ShapoidSetPos(spheroidB, &v);
  if (ShapoidIsInter(spheroidA, spheroidB) == true) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsInter failed");
    PBErrCatch(ShapoidErr);
 VecSet(&v, 0, 0.0); VecSet(&v, 1, 1.1);
  ShapoidSetPos(spheroidB, &v);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 2.0); VecSet(&v, 2, 1.0);
  ShapoidScale(spheroidB, (VecFloat*)&v);
  if (ShapoidIsInter(spheroidA, spheroidB) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsInter failed");
    PBErrCatch(ShapoidErr);
  ShapoidRotZCenter(spheroidB, -PBMATH_QUARTERPI);
  VecSet(&v, 0, 1.0); VecSet(&v, 1, 1.0); VecSet(&v, 2, 0.0);
  ShapoidSetPos(spheroidB, &v);
  if (ShapoidIsInter(spheroidA, spheroidB) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIsInter failed");
   PBErrCatch(ShapoidErr);
 ShapoidFree(&spheroidA);
 ShapoidFree(&spheroidB);
 printf("UnitTestIsInter OK\n");
}
void UnitTestShapoidIterCreateFree() {
 Facoid* facoid = FacoidCreate(2);
  VecFloat2D delta = VecFloatCreateStatic2D();
  ShapoidIter iter = ShapoidIterCreateStatic(facoid, &delta);
  if (iter._shap != (Shapoid*)facoid ||
    iter._pos == NULL ||
    iter._delta == NULL ||
    VecGetDim(iter._pos) != 2 ||
    VecGetDim(iter._delta) != 2) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterFreeStatic failed");
    PBErrCatch(ShapoidErr);
 ShapoidFree(&facoid);
  ShapoidIterFreeStatic(&iter);
  if (iter._pos != NULL ||
    iter._delta != NULL) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterFreeStatic failed");
   PBErrCatch(ShapoidErr);
 printf("UnitTestShapoidIterCreateFree OK\n");
void UnitTestShapoidIterGetSet() {
 Facoid* facoidA = FacoidCreate(2);
 Facoid* facoidB = FacoidCreate(2);
 VecFloat2D deltaA = VecFloatCreateStatic2D();
  VecFloat2D deltaB = VecFloatCreateStatic2D();
  for (int i = 2; i--;) {
    VecSet(&deltaA, i, 0.1);
    VecSet(&deltaB, i, 0.2);
  ShapoidIter iter = ShapoidIterCreateStatic(facoidA, &deltaA);
```

```
if (ShapoidIterShapoid(&iter) != (Shapoid*)facoidA) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterShapoid failed");
    PBErrCatch(ShapoidErr);
  if (VecIsEqual(ShapoidIterDelta(&iter), &deltaA) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterDelta failed");
    PBErrCatch(ShapoidErr);
  ShapoidIterSetShapoid(&iter, facoidB);
  ShapoidIterSetDelta(&iter, &deltaB);
  if (ShapoidIterShapoid(&iter) != (Shapoid*)facoidB) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterSetShapoid failed");
    PBErrCatch(ShapoidErr);
  if (VecIsEqual(ShapoidIterDelta(&iter), &deltaB) == false) {
    ShapoidErr->_type = PBErrTypeUnitTestFailed;
    sprintf(ShapoidErr->_msg, "ShapoidIterSetDelta failed");
    PBErrCatch(ShapoidErr);
  ShapoidFree(&facoidA);
  ShapoidFree(&facoidB);
  ShapoidIterFreeStatic(&iter);
 printf("UnitTestShapoidIterGetSet\ OK\n");\\
}
void UnitTestShapoidIterStepFacoid() {
  Facoid* facoid = FacoidCreate(2);
  VecFloat2D delta = VecFloatCreateStatic2D();
  for (int i = 2; i--;)
    VecSet(&delta, i, 0.25);
  ShapoidIter iter = ShapoidIterCreateStatic(facoid, &delta);
  float check[50] = \{0.000, 0.000, 0.000, 0.250, 0.000, 0.500, 0.000, 0.750,
    0.000, 1.000, 0.250, 0.000, 0.250, 0.250, 0.250, 0.500, 0.250, 0.750, 0.250,
    1.000,0.500,0.000,0.500,0.250,0.500,0.500,0.500,0.750,0.500,1.000,
    0.750, 0.000, 0.750, 0.250, 0.750, 0.500, 0.750, 0.750, 0.750, 1.000, 1.000,
    0.000, 1.000, 0.250, 1.000, 0.500, 1.000, 0.750, 1.000, 1.000
    };
  do {
    VecFloat* v = ShapoidIterGetInternalPos(&iter);
    if (ISEQUALF(VecGet(v, 0), check[2 * iCheck]) == false ||
      ISEQUALF(VecGet(v, 1), check[2 * iCheck + 1]) == false) {
      ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidIterStep failed");
      PBErrCatch(ShapoidErr);
    VecFree(&v);
    ++iCheck:
  } while (ShapoidIterStep(&iter));
  ShapoidFree(&facoid);
  ShapoidIterFreeStatic(&iter);
 printf("UnitTestShapoidIterStepFacoid OK\n");
void UnitTestShapoidIterStepPyramidoid() {
  Pyramidoid* pyramidoid = PyramidoidCreate(3);
  VecFloat3D delta = VecFloatCreateStatic3D();
  for (int i = 3; i--;)
    VecSet(&delta, i, 0.25);
```

```
ShapoidIter iter = ShapoidIterCreateStatic(pyramidoid, &delta);
   int iCheck = 0;
   float check[105] = \{0.000, 0.000, 0.000, 0.000, 0.250, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0
       0.500, 0.000, 0.000, 0.750, 0.000, 0.000, 1.000, 0.000, 0.250, 0.000, 0.000,\\
       0.250, 0.250, 0.000, 0.250, 0.500, 0.000, 0.250, 0.750, 0.000, 0.500, 0.000,
       0.000, 0.500, 0.250, 0.000, 0.500, 0.500, 0.000, 0.750, 0.000, 0.000, 0.750,
       0.250, 0.000, 1.000, 0.000, 0.250, 0.000, 0.000, 0.250, 0.000, 0.250, 0.250,
       0.000,0.500,0.250,0.000,0.750,0.250,0.250,0.000,0.250,0.250,0.250,
       0.250, 0.250, 0.500, 0.250, 0.500, 0.000, 0.250, 0.500, 0.250, 0.250, 0.750,\\
       0.000, 0.500, 0.000, 0.000, 0.500, 0.000, 0.250, 0.500, 0.000, 0.500, 0.500,
       0.250, 0.000, 0.500, 0.250, 0.250, 0.500, 0.500, 0.000, 0.750, 0.000, 0.000,
       0.750, 0.000, 0.250, 0.750, 0.250, 0.000, 1.000, 0.000, 0.000
      };
   do {
       VecFloat* v = ShapoidIterGetInternalPos(&iter);
       if (ISEQUALF(VecGet(v, 0), check[3 * iCheck]) == false ||
          ISEQUALF(VecGet(v, 1), check[3 * iCheck + 1]) == false ||
           \begin{tabular}{ll} ISEQUALF(VecGet(v, 2), check[3 * iCheck + 2]) == false) { } \\ \hline \end{tabular} 
          ShapoidErr->_type = PBErrTypeUnitTestFailed;
          sprintf(ShapoidErr->_msg, "ShapoidIterStep failed");
          PBErrCatch(ShapoidErr);
       VecFree(&v);
       ++iCheck;
   } while (ShapoidIterStep(&iter));
   ShapoidFree(&pyramidoid);
   ShapoidIterFreeStatic(&iter);
   printf("UnitTestShapoidIterStepPyramidoid OK\n");
void UnitTestShapoidIterStepSpheroid() {
   int dim = 3;
   Spheroid* spheroid = SpheroidCreate(dim);
   VecFloat* delta = VecFloatCreate(dim);
   for (int i = dim; i--;)
      VecSet(delta, i, 0.25);
   ShapoidIter iter = ShapoidIterCreateStatic(spheroid, delta);
   int iCheck = 0;
   float check[147] = {
       0.00000, 0.00000, -0.50000, 0.00000, -0.43301, -0.25000, -0.39244,
       -0.18301, -0.25000, -0.14244, -0.18301, -0.25000, 0.10756, -0.18301,
       -0.25000, 0.35756, -0.18301, -0.25000, 0.39244, -0.18301, -0.25000,
       -0.42780,0.06699,-0.25000,-0.17780,0.06699,-0.25000,0.07220,
       0.06699.-0.25000.0.32220.0.06699.-0.25000.0.42780.0.06699.
       -0.25000,-0.29499,0.31699,-0.25000,-0.04499,0.31699,-0.25000,
       0.20501, 0.31699, -0.25000, 0.29499, 0.31699, -0.25000, 0.00000,
       -0.50000, 0.00000, -0.43301, -0.25000, 0.00000, -0.18301, -0.25000,
       0.00000, 0.06699, -0.25000, 0.00000, 0.31699, -0.25000, 0.00000, 0.43301,
       -0.25000, 0.00000, -0.50000, 0.00000, 0.00000, -0.25000, 0.00000, 0.00000,
       0.00000,0.00000,0.00000,0.25000,0.00000,0.00000,0.50000,0.00000
       0.00000, -0.43301, 0.25000, 0.00000, -0.18301, 0.25000, 0.00000, 0.06699,
       0.25000, 0.00000, 0.31699, 0.25000, 0.00000, 0.43301, 0.25000, 0.00000,
       0.00000, 0.50000, 0.00000, 0.00000, -0.43301, 0.25000, -0.39244, -0.18301,
       0.25000, -0.14244, -0.18301, 0.25000, 0.10756, -0.18301, 0.25000, 0.35756,
       \hbox{\tt -0.18301,0.25000,0.39244,-0.18301,0.25000,-0.42780,0.06699,0.25000,}
       -0.17780, 0.06699, 0.25000, 0.07220, 0.06699, 0.25000, 0.32220, 0.06699,\\
       0.25000, 0.42780, 0.06699, 0.25000, -0.29499, 0.31699, 0.25000, -0.04499,
       0.31699, 0.25000, 0.20501, 0.31699, 0.25000, 0.29499, 0.31699, 0.25000,
       0.00000,0.00000,0.50000
      };
   do {
       VecFloat* v = ShapoidIterGetInternalPos(&iter);
```

```
if (ISEQUALF(VecGet(v, 0), check[3 * iCheck]) == false ||
      ISEQUALF(VecGet(v, 1), check[3 * iCheck + 1]) == false ||
      ISEQUALF(VecGet(v, 2), check[3 * iCheck + 2]) == false) {
     ShapoidErr->_type = PBErrTypeUnitTestFailed;
      sprintf(ShapoidErr->_msg, "ShapoidIterStep failed");
     PBErrCatch(ShapoidErr);
    VecFree(&v);
    ++iCheck;
  } while (ShapoidIterStep(&iter));
 ShapoidFree(&spheroid);
 ShapoidIterFreeStatic(&iter);
 VecFree(&delta);
 printf("UnitTestShapoidIterStepSpheroid OK\n");
void UnitTestShapoidIter() {
 UnitTestShapoidIterCreateFree();
  UnitTestShapoidIterGetSet();
 UnitTestShapoidIterStepFacoid();
 UnitTestShapoidIterStepPyramidoid();
 UnitTestShapoidIterStepSpheroid();
 printf("UnitTestShapoidIter OK\n");
void UnitTestAll() {
 UnitTestCreateCloneIsEqualFree();
 UnitTestLoadSavePrint();
 UnitTestGetSetTypeDimPosAxis();
 UnitTestTranslateScaleGrow();
 UnitTestRotate();
 UnitTestRotateAxis();
 UnitTestRotateX();
 UnitTestRotateY();
 UnitTestRotateZ():
 UnitTestImportExportCoordIsPosInside();
 UnitTestGetBoundingBox();
 UnitTestGetPosDepthCenterCoverage();
 UnitTestFacoidAlignedIsInsideFacoidAligned();
 UnitTestFacoidAlignedIsOutsideFacoidAligned();
 UnitTestFacoidAlignedSplitExcludingFacoidAligned();
  UnitTestFacoidAlignedAddClippedToSet();
 UnitTestIsInter();
 UnitTestShapoidIter();
 printf("UnitTestAll OK\n");
int main() {
 UnitTestAll();
  // Return success code
 return 0;
```

## 6 Unit tests output

UnitTestCreateCloneIsEqualFree OK Type: Facoid

```
Pos: <0.000,0.000,0.000>
Axis(0): <1.000,0.000,0.000>
Axis(1): <0.000,1.000,0.000>
Axis(2): <0.000,0.000,1.000>
UnitTestLoadSavePrint OK
UnitTestGetSetTypeDimPosAxis OK
UnitTestTranslateScaleGrow OK
UnitTestRotate OK
{\tt UnitTestRotateAxis} \ {\tt OK}
UnitTestRotateX OK
UnitTestRotateY OK
UnitTestRotateZ OK
UnitTestImportExportCoordIsPosInside OK
{\tt UnitTestGetBoundingBox\ OK}
UnitTestGetPosDepthCenterCoverage OK
UnitTestFacoidAlignedIsInsideFacoidAligned OK
{\tt UnitTestFacoidAlignedIsOutsideFacoidAligned\ OK}
{\tt UnitTestFacoidAlignedSplitExcludingFacoidAligned\ OK}
{\tt UnitTestFacoidAlignedAddClippedToSet} \ \ {\tt OK}
UnitTestIsInter OK
UnitTestShapoidIterCreateFree OK
UnitTestShapoidIterGetSet OK
{\tt UnitTestShapoidIterStepFacoid\ OK}
UnitTestShapoidIterStepPyramidoid OK
{\tt UnitTestShapoidIterStepSpheroid\ OK}
UnitTestShapoidIter OK
UnitTestAll OK
    facoid.txt
  "_dim":"3",
  "_type":"0",
  "_pos":{
    "_dim":"3",
    "_val":["0.000000","0.000000","0.000000"]
  "_axis":[
    {
      "_dim":"3",
      "_val":["1.000000","0.000000","0.000000"]
      "_dim":"3",
      "_val":["0.000000","1.000000","0.000000"]
      "_dim":"3",
      "_val":["0.000000","0.000000","1.000000"]
 ]
```

Example of path on a 2D Spheroid using the ShapoidIterator:

