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Introduction

0.1 Overview

This manual provides an overview of

0.2 Acknowledgements

0.3 Copyright

0.4 Disclaimer

While every effort is made to ensure the accuracy of the information in this manual, Nichole E. Carlson cannot be held responsible for any errors therein. The software described in this manual is subject to constant improvement and modification. The right is reserved to revise this document and the associated software without notice. Nichole E. Carlson makes no warranty

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about the function of this software.

0.5 Conditions of Use

Use of this package will be in accordance with the following License Agreement.

0.6 License Agreement

General agreement??? Freeware...

0.7 Technical Support

0.8 Conventions Used in This Document

Installation

- 0.9 System Requirements
- 0.10 Installation Procedure
- 0.11 File Naming Convention
- 0.12 Other Required Software

The Deconvolution Model

Let $y_i(t_j)$ be the observed hormone concentration for subject i at time t_{ij} where i = 1, ..., S and $j = 1, ..., m_i$, where S is the number of subjects in the study, each with m_i time points of observation. Although the number and timing of observations can theoretically differ by subject, in general study designs, the observation times are common across subjects. Thus, in future notation, $t_{ij} = t_j$ and $m_i = m$. i can be eliminated for the single-subject model. Further, let $C_i(t_j)$ be the true hormone concentration for subject i at time t_j . The observed and true concentrations are linked through the following statistical model:

$$\log[y_i(t_j)] = \log[C_i(t_j)] + \epsilon_i(t_j)$$

where $\epsilon_i(t_j) \sim N(0, \sigma_{\epsilon i}^2)$, and $\epsilon_i(t_j)$ represents technical and biologic variability. Concentrations are limited to positive values, so our model is on the log scale. $C_i(t_j)$ is defined by the following convolution integral:

$$C_i(t_j) = B_i(t_j) + \int_{-\infty}^{t_j} S_i(z; \boldsymbol{\theta}_{s,i}) * E_i(t_j - z; \boldsymbol{\theta}_{e,i}) dz$$

where $S_i(z; \boldsymbol{\theta}_{s,i})$ is a function that models secretion and $E_i(t_j - z; \boldsymbol{\theta}_{e,i})$ is a function that models hormone elimination. $S_i(z; \boldsymbol{\theta}_{s,i})$ models the pulsatile hormone release and depends on a set of parameters $\boldsymbol{\theta}_{s,i}$. The function $E_i(t_j - z; \boldsymbol{\theta}_{e,i})$ describes the removal of the hormone from the blood (elimination) and depends on a set of parameters, $\boldsymbol{\theta}_{e,i}$. $B_i(t_j)$ describes the non-pulsatile (baseline) concentration and is often assumed constant $(B_i(t_j) = B_i)$.

The secretion function, $S_i(z; \boldsymbol{\theta}_{s,i})$

It is common for pulsatile secretion to be defined by a series of Gaussian components, each with "pulse specific" parameters. So, assuming subject i experiences N_i pulses by the end of the study,

$$S_i(z, \boldsymbol{\theta}_{s,i}) = \sum_{k=1}^{N_i} \frac{\alpha_{ik}}{\sqrt{2\pi\omega_{ik}}} e^{-\frac{1}{2\omega_{ik}}(z-\tau_{ik})^2}$$
(1)

The values α_{ik} , ω_{ik} , and τ_{ik} are the mass, width, and location, respectively, for the kth pulse. Therefore, $\boldsymbol{\theta}_{s,i} = (\boldsymbol{\alpha}_i, \boldsymbol{\omega}_i, \boldsymbol{\tau}_i)^T$, where $\boldsymbol{\alpha}_i$ represents the vector of pulse masses: $\boldsymbol{\alpha}_i = (\alpha_{i1}, \alpha_{i2}, ..., \alpha_{iN_i})^T$ and $\boldsymbol{\omega}_i$ and $\boldsymbol{\tau}_i$ are defined as the vectors of pulse widths and pulse locations, respectively.

We assume that the pulse specific parameters have the following distri-

butions:

$$\log \alpha_{ik} \stackrel{iid}{\sim} N(\mu_{ai}, \nu_{ai}^2)$$
$$\log \omega_{ik} \stackrel{iid}{\sim} N(\mu_{wi}, \nu_{wi}^2)$$
$$\tau_{ik}|N_i \stackrel{iid}{\sim} U^{(3N_i+2)}[a, b]$$

The elimination function, $E_i(t_j - z; \boldsymbol{\theta}_{e,i})$

It is common for elimination to be described by the exponential distribution with decay rate λ_i , or equivalently, half-life H_i .

$$E_i(t_j - z, \boldsymbol{\theta}_{e,i}) = e^{-\lambda_i(t_j - z)} = e^{-\frac{\log 2}{H_i}(t_j - z)}$$
(2)

Therefore, $\theta_{e,i} = H_i$.

The deconvolution model

Putting together the secretion (1) and elimination (2) functions, the statistical model of observed hormone concentration at time t_j is:

$$\log[y_i(t_j)] = \log\left[B_i + \int_{-\infty}^{t_j} \sum_{k=1}^{N_i} \frac{\alpha_{ik}}{\sqrt{2\pi\omega_{ik}}} e^{-\frac{1}{2\omega_{ik}}(z-\tau_{ik})^2} e^{-\lambda_i(t_j-z)} dz\right] + \epsilon_i(t_j)$$
(3)

where B_i is the time constant baseline concentration.

In summary, there are 8 common parameters for one subject: number of pulses (n_i) , Baseline secretion (B_i) , average pulse mass (μ_{ai}) , average pulse duration (μ_{wi}) , half-life (H_i) , model error (ϵ_i) , variation between pulse mass

 (ν_{ai}^2) , and variation between pulse width (ν_{wi}^2) . The first 5 parameters usually have important physiological indications, while the last three variance parameters can be treated as nuisance parameters. Estimation of each pulse is composed of 3 parameters: individual pulse mass (α_{ik}) , individual pulse duration (ω_{ik}) , and pulse location (λ_{ik}) .

Bayesian Modeling

0.13 Introduction of Bayesian Statistics

(The wording might be too statistical) The most important feature of Bayesian statistics is incorporating subjective knowledge and the confidence of that knowledge, quantified in the form of prior distribution, into interpretation of probabilities. The frequentist assume that a parameter is an unknown constant, and the inference made upon that parameter is presented in a point estimation and a corresponding variance related to the uncertainty. On the other way, a Bayesian considers a parameter as a random variable, and the estimation of the parameter is in the form of a posterior distribution.

The Bayes theorem of single parameter, in its most common form, is

$$P(\theta|X) = \frac{P(X|\theta)P(\theta)}{P(\theta)} = \frac{P(X|\theta)P(\theta)}{\sum_{\theta} P(X|\theta)P(\theta)}$$
(4)

BAYESIAN MODELING

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 $P(\theta|X)$ is the posterior distribution of the parameter of interest, and

 $P(X|\theta)$ is the likelihood function of data given the parameter, and $P(\theta)$ is

the prior distribution of the parameter, sometimes denoted by $\pi(X)$. The

prior distribution is pre-specified before collecting data. The priors can be

non-informative or informative . When little is known about the hormone

under study, the goal is to limit the influence of the prior to minimum (i.e.,

to be non-informative) and let the data dominate the estimation. This is

done by setting a large variance in the prior, reflecting lack of information

available about the parameter. When historical or biologic knowledge exists,

we can incorporate that knowledge into the model by setting the mean of

the prior to match prior information and setting a smaller variance.

Prior Distribution 0.14

The influence of the prior (and the sample size) is illustrated in the following

graphs.

(Normal-Normal)

Graph1: flat prior with moderate sample size (n=10)

Graph2: flat prior with larger sample size (n=1000)

Graph3: informative prior with moderate sample size.

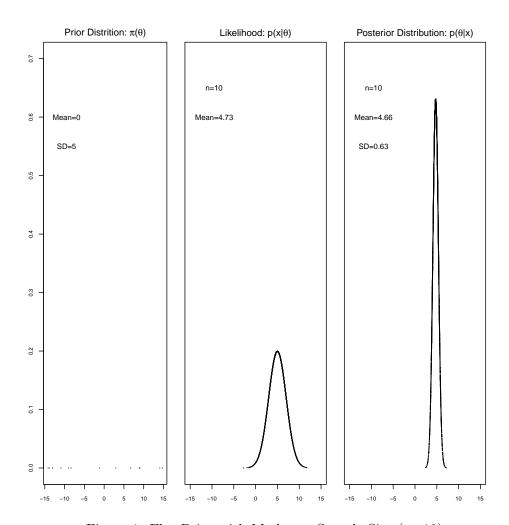


Figure 1: Flat Prior with Moderate Sample Size (n=10)

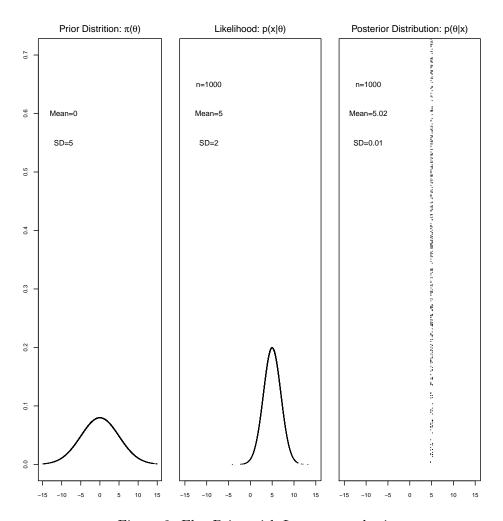


Figure 2: Flat Prior with Larger sample size

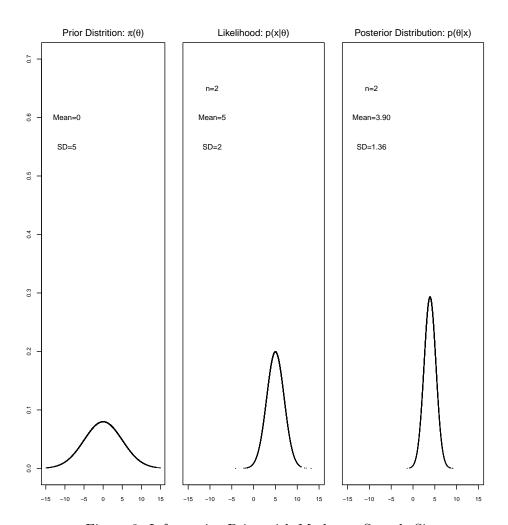


Figure 3: Informative Prior with Moderate Sample Size $\,$

0.15 Bayesian Estimation

The posterior distribution of the parameter usually does not have a closed form when the model have more than one parameters, as in the hormone concentrations. As a consequence, the desired distribution cannot be computed directly. Instead, they need to be simulated using Monte-Carlo Markov Chain (MCMC). (Do we need to introduce Gibbs sampling and MH here? or more details about MCMC). In addition, the number of parameters is not fixed from iteration to iteration because the number of pulses is not known and also needs to be simulated. We consider using birth-death M-CMC (BDMCMC) given its suscess in other pulse estimation problems [ref]. A single iteration of BDMCMC occurs in two stages. First, the number of components is simulated using a birth-death process. Next, conditional on the number of components, the remaining parameters are updated using traditional MCMC. The full algorithm iterates between these two steps. In more detail, one iteration of our BDMCMC algorithm occurs as follows:

- (1) Conditioned on the current values of $(\boldsymbol{\alpha}_i, \, \boldsymbol{\omega}_i, \, \boldsymbol{\tau}_i, \, \mu_{ai}, \, \mu_{wi}, \, \nu_{ai}, \, \nu_{wi}, \, B_i, \, H_i, \, N_i, \, \sigma_{ei}^2)$, update $N_i, \, \boldsymbol{\alpha}_i, \, \boldsymbol{\omega}_i$, and $\boldsymbol{\tau}_i$ by running the birth-death process.
- (2) Conditioned on the current values of $(\nu_{ai}, \nu_{wi}, B_i, H_i, N_i, \alpha_i, \omega_i, \tau_i, \sigma_{\epsilon i}^2)$, update μ_{ai} and μ_{wi} , each by Gibbs sampler [?].
- (3) Conditioned on the current values of $(\mu_{ai}, \mu_{wi}, B_i, H_i, N_i, \alpha_i, \omega_i, \omega_i)$

 τ_i , $\sigma_{\epsilon i}^2$), update ν_{ai} and ν_{wi} , each by a random walk Metropolis-Hastings sampler.

- (4) Conditioned on the current values of $(\mu_{ai}, \mu_{wi}, \nu_{ai}, \nu_{wi}, N_i, \alpha_i, \omega_i, \tau_i, \sigma_{\epsilon i}^2)$, update B_i and H_i by a Metropolis-Hastings sampler. These are drawn together since their estimates are highly correlated.
- (5) Conditioned on the current values of $(\mu_{ai}, \mu_{wi}, \nu_{ai}, \nu_{wi}, N_i, B_i, H_i, \boldsymbol{\tau}_i, \sigma_{\epsilon i}^2)$, update $(\alpha_{i1}, \omega_{i1}, \alpha_{i2}, \omega_{i2}, ..., \alpha_{iN_i}, \omega_{iN_i})$, each by a Metropolis-Hastings sampler.
- (6) Conditioned on the current values of $(\mu_{ai}, \mu_{wi}, \nu_{ai}, \nu_{wi}, N_i, B_i, H_i, \alpha_i, \omega_i, \sigma_{\epsilon i}^2)$, update $(\tau_{i1}, \tau_{i2}, ..., \tau_{iN_i})$, each by a Metropolis-Hastings sampler.
- (7) Conditioned on the current values of $(\mu_{ai}, \mu_{wi}, \nu_{ai}, \nu_{wi}, N_i, B_i, H_i, \alpha_i, \omega_i, \tau_i)$, update $\sigma_{\epsilon i}^2$ by Gibbs sampler.
- (8) Return to step (1).

BDMCMC:Single

hormone-single subject

modeling

0.16 General Usage Information

0.17 Quick Start

Bayesian Analysis of Pulsatile Hormone Levels (BAPHL) is a software package developed by the PI's research group to analyze pulsing hormones by a front end GUI interface in a Bayesian way.

The software is started by executing the file RAPHL.exe. The main window that looks like Figure 4 will appear. This windows has a menu bar, a console output field, a panel of buttons to the right of the console

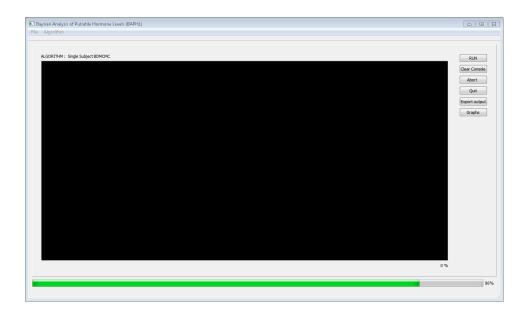


Figure 4: Start Screeen of BAPHL

output, and a progress bar on the bottom. To use the BAPHL software, the user Start a new analysis by clicking the "Algorithm" menu item and then "Single Subject". A dialog box as shown in Figure 6 will pop up.

Click the "General" tab (Figure ??). Click "Browse" to select the input data file, which defaults to an example file named "subjmodel61s1.dat". Change "Rate of writing to files (Iterations)" to 10, and "Rate of console refresh (Iterations)" to 50. The two parameters specify how often data is output to files and the main screen. Enter 10 for Constant birth rate. Enter 1000 for MCMC Iteration Count. Enter 1 for Bur in count (Iterations).

Click the "Baseline" tab (Figure 7). Enter 3 for Prior mean, 100 for

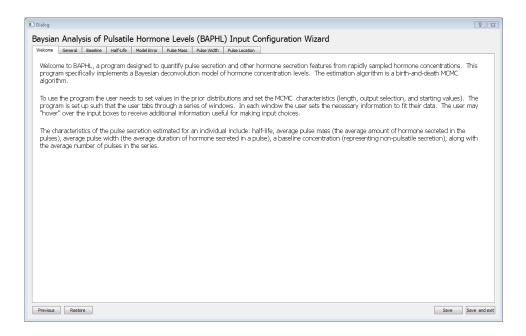


Figure 5: Bayesian Analysis of Pulsatile Hormone Levels (BAPHL) Input Configuration Wizard

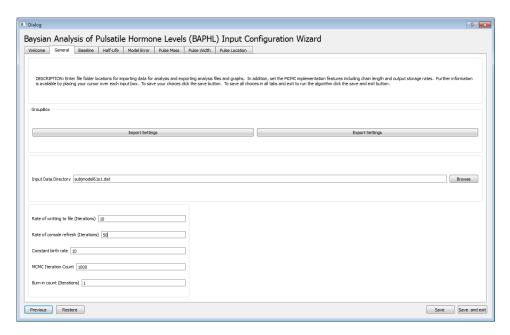


Figure 6: "General" Tab

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Prior variance, 0.015 for Proposal variance, and 2.5 for Starting value.

Click the "Half-Life" tab (Figure 8). Enter 45 for Prior mean, 100 for Prior variance, 0.90 for Correlation proposal for halflife, 50 for Proposal variance, and 45 for Starting value.

Click the "Model Error" tab (Figure 10). Enter 0.0001 for Shape of Prior, 0.0001 for Rate of Prior, and 0.25 for Initial value for mode error.

Click the "Pulse Mass" tab (Figure ??). Enter 1 for Mean of prior for mean pulse mass, 10 for variance of prior for mean pulse mass, 200 for Prior On SD of pulse masses, 0.9 for Proposal variance for individual pulse masses, 0.5 for Proposal variance for SD of pulse masses, 1 for Initial value for mean pulse mass, and 1 for Initial value SD of pulse masses.

Click the "Pulse Width" tab (Figure 11). Enter 1.5 for Mean of prior for mean pulse width, 10 for Variance of prior for mean pulse width, 200 for Prior on SD of pulse widths, 4 for Proposal variance for individual pulse widths, 6 for Proposal variance for SD of pulse widths, 1 for Initial value SD of pulse width, and 1.5 for Initial value of mean pulse width.

Click the "Pulse Location" tab (Figure 12). Enter 12 for Rate in poisson prior on number of pulses in a series, 3 for Pulse Location Distn Order Stat, 1 for Proposal variance for individual pulse location, and 1 for Length of birthdeath process for each iteration.

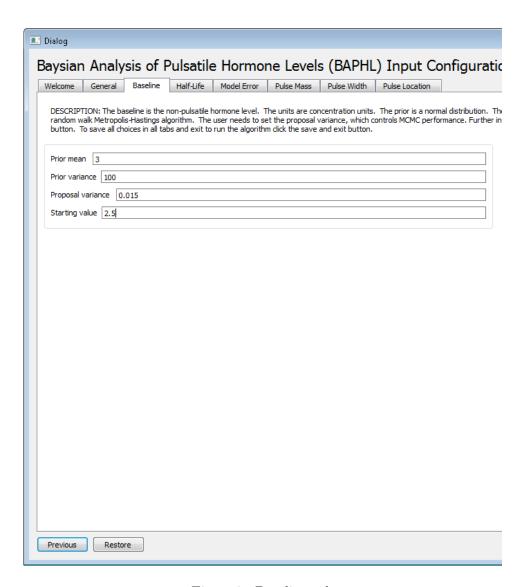


Figure 7: Baseline tab

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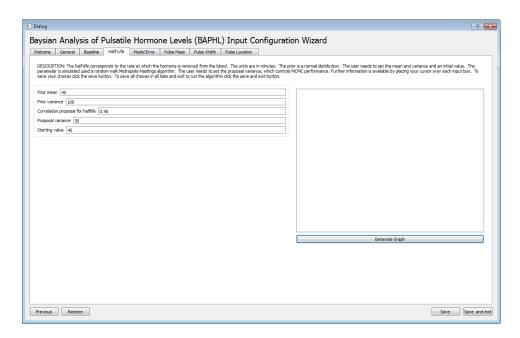


Figure 8: Half-Life tab

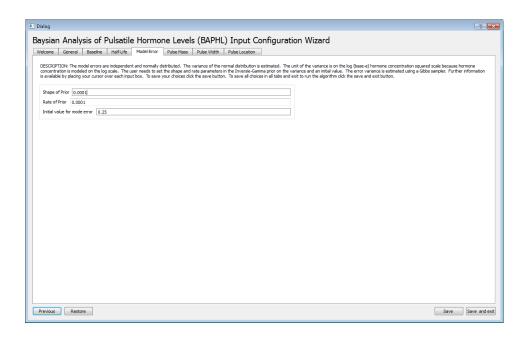


Figure 9: Model Error tab

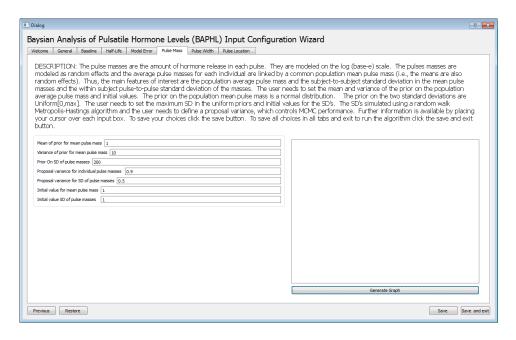


Figure 10: Model Error tab

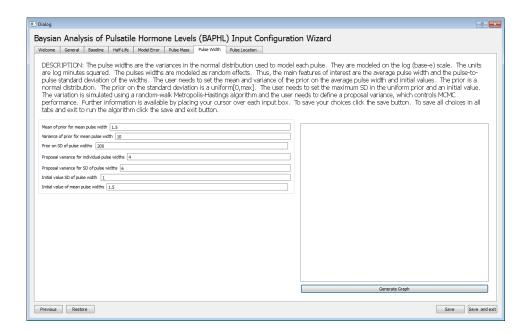


Figure 11: Pulse Width tab

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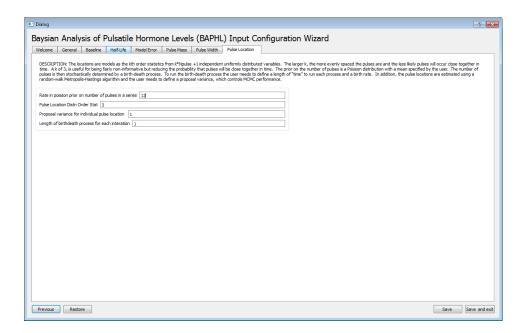


Figure 12: Pulse Location tab

Click on "Save" button to save the settings in this dialog box. Activate the main window by clicking on the window title. Click on the "Run" button to start the analysis. The console output field will be populated by the results of every 50 iteration, as specified in "General" tab (Figure 13).

After console stops refreshing, the output can be demonstrated by clicking the "Graphs" tab and the output can be exported and saved in a directory by clicking the "Export output" tab.

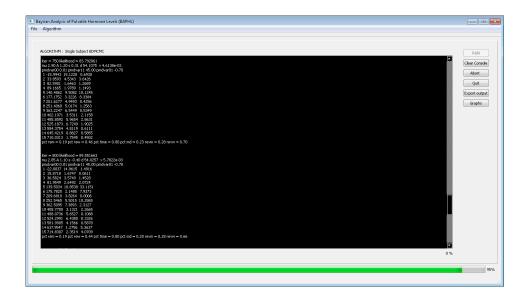


Figure 13: Console output

0.18 Data File Formats

The first row will be ignored by the software. The first column is the index of observations and will be ignored by the software. The second column is the time of observation, and the third column is the measured concentration. User does not need to specify the inter-assay or intra-assay correlation coefficients. The length of each column needs to be the same. Missing observations, if present, should be estimated by interpolating between neighboring observations.

0.19 Graphing the Data

A graphing tool is utilized to demonstrate the distribution visually when the prior distribution is normal. (An graph example). By clicking on the "Generate Graph" button, the curve of the probability density function (PDF) of the prior normal distribution will be generated. A normal distribution is usually bell-shaped and symmetric. The peak (mode) of the distribution represents most likely values (a priori??) and the range of X-axis should cover the range of all biological possible values of the parameter.

0.20 General Tab

To use the BAPHL software, the user needs to provide the following information:

- 1. A dataset that contains the rapidly sampled hormone concentration time series, in a format specified in section "data format".
- 2. Folder name where the output file of the estimated hormone parameters will be saved.
- 3. MCMC parameters, including how many iteration to run, the frequency of writing to file and console refresh, burn-in count, and birth-rate in the birth-death process. The default value for MCMC number of

iterations is 500,000. The number of iterations needed to achieve good mixing properties and to collect enough information to summarize the feature of each parameters ranges from ranges from 150,000 to 1,000,000. The rate of writing to file specify how often the program output the current value of the parameter in the MCMC simulation, and the default value is one output every 50 iteration. This process is called thinning, and it is useful to reduce demands for data storage and lower the correlation between successive draws, and therefore enhance the performance of the MCMC simulation. However, with increasing spacing between saving values, the numbers of iteration required to collect the information of the posterior distribution is also increased. The suggested value is from 20 to 100 iterations. The rate of console refresh specifies how often the output is written to screen, and the default value is every 5000 iterations. The screen output contains the current values of parameters, including the common parameters shared by all subjects, such as baseline secretion, pulse-specific parameters for each secretion event, including pulse mass, pulse width the pulse location, and the acceptance rate of each parameters. Good MCMC behavior is more likely when the acceptance rate is between 25% to 50%. Burn-in count is the number of the MCMC draws at the beginning that will be discarded when summarizing the posterior distribution. Usually the first 5% to 25% of the MCMC draws are discarded to lower the dependence of the posterior distribution on starting values. The birth-rate is set as the possible number of pulses in each subject. For human luteinizing hormone (LH), the pulsing frequency is usually 1 pulse per hour. Deviation from correct birth-rate is not likely to result in biased estimation, but will cause longer time to the MCMC to converge.

0.21 Baseline Tab

The Baseline is the non-pulsatile, constant hormone level. The prior is a normal distribution with user-specified mean and variance. We suggest to set the mean equal to the fitted value from other sources, e.g., 4 concentration units for human LH, and a relatively larger, or uninformative variance, like 1000. The posterior distribution of the parameter is simulated using a random walk Metropolis-Hastings algorithm. The user needs to specify the starting value and the proposal variance which controls MCMC performance. A starting value is usually set equal or closed to the prior mean, and the posterior distribution should not depend on the starting value if the MCMC is mixing well. A proposal variance is used to draw each MCMC

simulation. The suggested proposal variance for baseline is 0.015 to start with, and is updated every 500 iterations in the first 2000 iterations. The proposal variance governs the performance of the MCMC simulation, and should be properly chosen so that the acceptance rate is between 25% to 50%. If the acceptance rate is below 25%, the user is suggested to use a smaller proposal variance and vice versa.

0.22 Half-life Tab

The half-life corresponds to the rate at which the hormone is removed from the blood. More specifically, the half-life is the amount of time required for the hormone concentration to fall to half of its peak value. The prior is a normal distribution with user-specified mean and variance. We suggest to set the mean equal to the fitted value from other sources, e.g., 45 minutes for human LH, and a relatively larger, or uninformative variance, like 1000. The posterior distribution of the parameter is simulated using a random walk Metropolis-Hastings algorithm. The user needs to specify the starting value, the proposal variance and correlation which controls MCMC performance. A starting value is usually set equal or closed to the prior mean, and the posterior distribution should not depend on the starting value if the MCMC is mixing well. A proposal variance is used to draw each M-

CMC simulation The suggested proposal variance for half-life is 50 to start with, and is updated every 500 iterations in the first 2000 iterations. The proposal variance governs the performance of the MCMC simulation, and should be properly chosen so that the acceptance rate is between 25% to 50%. If the acceptance rate is below 25%, the user is suggested to use a smaller proposal variance and vice versa. The estimation of half-life is highly negatively correlated with baseline, and they are drawn simultaneously in each MCMC iteration. A correlation proposal for baseline and half-life also needs to be specified, and the default value is -0.85.

0.23 Model Error Tab

The model error are independent and normally distributed with mean 0. The unit of log is on the log (base-e) unit because the hormone concentration needs to be positive and is modeled on the log scale. A conjugate gamma family prior is used for model error and the posterior is drawn using a Gibbs sampler. The user needs to specify the rate and shape parameter for the inverse-Gamma distribution, which are both 0.0001 by default (here is an error: the default is 0.01 in hover). Values closed to 0 imply a uninformative prior for both rate and shape.

0.24 Pulse Mass Tab

The pulse masses are the amount of hormone released in each pulse. They are modeled using a random effect model on the log scale, with a unique mean and variance for each subject in the single subject model, and average pulse masses for each subjected linked by a common population mean pulse mass in the population. Thus, the main features of interest are the average pulse mass and pulse-to-pulse variability in one subject in the single subject model, and population-average pulse mass with subject-to-subject variability in the population model. The prior for pulse mass mean is a normal distribution, and the prior for pulse mass variance is a uniform distribution of [0, Max]. In the single-subject model, the user needs to specify the mean and variance for the normal prior distribution, and the Max for the uniform distribution. We suggest to set the mean equal to the fitted value from other sources, e.g., 1 (on the log scale) for human LH, and a relatively large value for the prior variance (the default is 1000). We also suggest using a larger upper boundary for the variance, and the default value is 200. A Gibbs sampler is utilized to estimate the mean pulse mass, and the user only needs to specify the initial value for mean pulse mass. A starting value is usually set equal or closed to the prior mean, and the posterior distribution should not depend on the starting value if the MCM-

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C is mixing well. The individual pulse mass and pulse mass variance and simulated using Metropolis-Hastings algorithm. A proposal variance is used to draw each MCMC simulation. The suggested proposal variance is 0.9 for individual pulse mass and 0.5 for pulse mass variance to start with, and is updated every 500 iterations in the first 2000 iterations. The proposal variance governs the performance of the MCMC simulation, and should be properly chosen so that the acceptance rate is between 25% to 50%. If the acceptance rate is below 25%, the user is suggested to use a smaller proposal variance and vice versa.

0.25 Pulse Width Tab

The pulse width describes the spread, or duration of each pulsing event. They are modeled using a random effect model on the log scale, with a unique mean and variance for each subject in the single subject model, and average pulse width for each subjected linked by a common population mean pulse mass in the population. Thus, the main features of interest are the average pulse width and pulse-to-pulse variability in one subject in the single subject model, and population-average pulse width with subject-to-subject variability in the population model. The prior for pulse width mean is a normal distribution, and the prior for pulse width variance is a

uniform distribution of [0, Max]. In the single-subject model, the user needs to specify the mean and variance for the normal prior distribution, and the Max for the uniform distribution. We suggest to set the mean equal to the fitted value from other sources, e.g., 1 (on the log scale) for human LH, and a relatively large value for the prior variance (the default is 1000). We also suggest using a larger upper boundary for the variance, and the default value is 200. A Gibbs sampler is utilized to estimate the mean pulse width, and the user only needs to specify the initial value for mean pulse width. A starting value is usually set equal or closed to the prior mean, and the posterior distribution should not depend on the starting value if the MCMC is mixing well. The individual pulse width and pulse width variance and simulated using Metropolis-Hastings algorithm. A proposal variance is used to draw each MCMC simulation. The suggested proposal variance is 0.9 for individual pulse width and 0.5 for pulse width variance to start with, and is updated every 500 iterations in the first 2000 iterations. The proposal variance governs the performance of the MCMC simulation, and should be properly chosen so that the acceptance rate is between 25% to 50%. If the acceptance rate is below 25%, the user is suggested to use a smaller proposal variance and vice versa.

0.26 Pulse Locations Tab

The locations are modeled as the kth order statistics from kN + 1 independent uniformly distributed random variable from a time window slightly larger than the observation time period, where k is a user-specified integers, and N is the number of pulsing event. A larger k yield more evenly spaced pulsed and thus less likely pulses that are too closed together. The default value for k is 3, which is fairly non-informative but reducing the probability that the pulses will be close together in time. The prior on the number of pulses is a Poisson distribution with a mean specified by the user. For human LH we suggest that the Poisson rate is 1 times the observation time in hours. The number of pulses is then stochastically determined by a birthdeath process. The user needs to define the length of "time" to run each process, and the default value is 1. A larger value will facilitate pulse-fitting but takes longer time for each iteration. In addition, each pulse location is estimated using a random-walk Metropolis-Hastings algorithm and the user needs to define a proposal variance, which control MCMC performance. The suggested proposal variance is 1 for pule location, and is updated every 500 iterations in the first 2000 iterations. The proposal variance governs the performance of the MCMC simulation, and should be properly chosen so that the acceptance rate is between 25% to 50%. If the acceptance rate is below 25%, the user is suggested to use a smaller proposal variance and vice versa.

0.27 Console Output

Once the estimation has started, The console output field will be populated by the results of every 50 iteration, as specified in "General" tab (Figure 14). The Console output is very important in monitoring the performance of the MCMC simulation. The output includes all parameters of each pulses in the current iteration. The first column is the pulse order, the second column is the pulse mass, and the third column is the pulse width. It also includes the acceptance rate for each parameter if estimated using the Metropolis-Hastings algorithm (Do we need to change the name shown in the console or I made a table for each output with a parameter?, like "pct md is the acceptance rate for pulse half-life and baseline).

0.28 Graphical Output

After console stops refreshing, the output can be demonstrated by clicking the "Graphs" and the clicking the "Generate Graph" tab (Figure 15). The first 4 sets of graphs show the traceplot the histogram for each parameter.

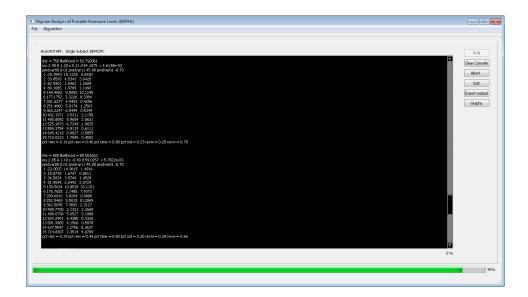


Figure 14: Console Output tab

Traceplot is a plot of iteration vs simulation draws, and a histogram displays the distribution of the posterior simulation draws. Both plots are used for diagnosing for poor performance of the MCMC simulations. In Bayesian algorithm, simulation draws are used to summarize posterior distribution of the parameters of interest. There are majorally two issues: the chain may not converge to its stationary distribution, and the chain may not mix well. A failure to reach stationary distribution can be recognized from a traceplot as the mean and variance of is not constant over time (Figure 16). This usually requires more iterations and longer burn-in counts, which can be changed in the "General Tab". Poor mixing is always associated with high correlation with subsequent draws, and thus statistical analysis

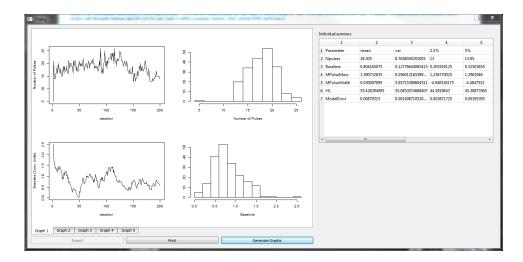


Figure 15: Graph Output tab

based on independent observations may not be valid. A chain is mixing well if it traverses from in the parameter space rapidly (Figure 17)(Figure 18), with the acceptance rate between 25% to 50%. A poor mixing can be fixed by changing the proposal variance of this parameter. A histogram is used to check the posterior draws of the parameter. (check for normality? regions of extreme values?) The graph5 (Figure 19) demonstrated the fit of the posterior draws of the Bayesian model. The top plosts show the fits of simulated series from reference dataset. The dashed black line represents the observed concentration; the solid red line is the fitted concentration, and the dashed grey line is the 95% equal tails credible interval of the concentration. The bottom plots are histograms of draws of pulse locations.

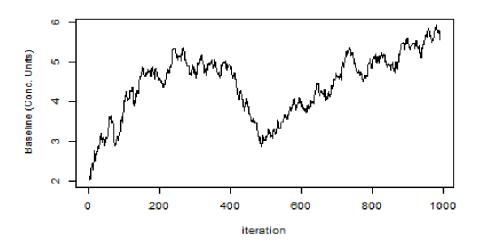


Figure 16: Example of No Convergence

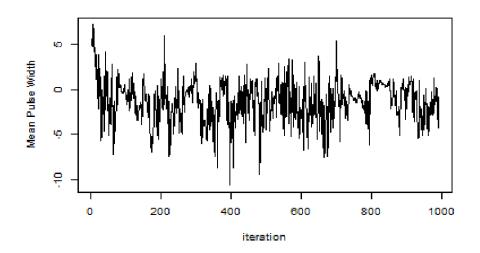


Figure 17: Example of Good Mixing

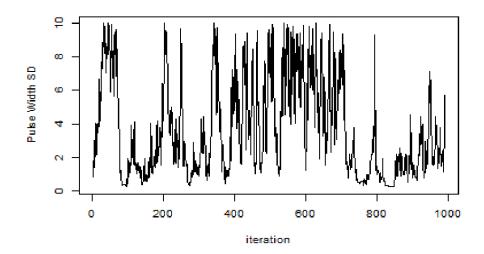


Figure 18: Example of Poor Mixing

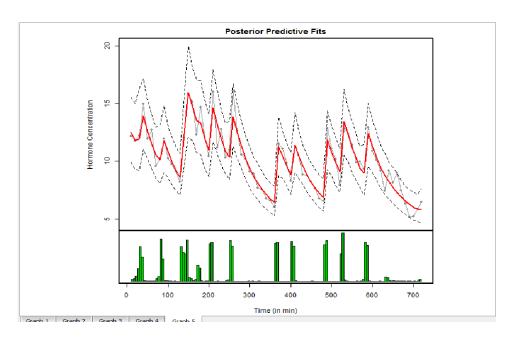


Figure 19: The Fit of the Posterior Draws

0.29 Tabular Output

A tabular output will be generated simultaneously with graphical output.

The table summarized the mean, variance and quantile for number of pulses,

baseline, mean pulse mass (on the log scale), mean pulse width (on the log

scale), half life and model error of the MCMC draws after the burn-in period.

For example, the posterior mean for baseline is 4.56 with variance 0.46 and

a 95% equal tail credible interval of (3.11, 5.67). (1, I cannot copy the whole

table...)

(2, Do we need to keep so many digits?)

Statistical Details 0.30

0.30.1The model and priors

0.30.2**Estimation: BDMCMC**

PopBDMCMC: Single

hormone-population

modeling

BivBDMCMC:Multiple
hormone -single subject
modeling