

## Objectives:

- Creating and manipulating matrix
- Matrix Arithmetique
- Plotting graphs and working with matlab built in functions (exp,log,sqrt)
- Tasks

## Matrix:

### Introduction:

Variables that we created so far can hold only 1 value but

### Creating matrix:

There are 3 types of matrix

#### Column matrix

This matrix represents horizontal vector to create it we use

```
first_matrix=[1; 2; 3; 4]
```

#### Ligne matrix

This matrix represents vertical vector to create it we use

```
second_matrix = [1, 2, 3, 4]
% or we can use
second_matrix2 = [1 2 3 4]
```

### Remarque:

We can notice then when we want to fill next column on matrix we use space or , and when we want to fill next line we use ;

### Rectangular matrix

It matrix of shape (n\*m) we can create it using

```
third_matrix = [1 2 3;4 5 6;7 8 9]
```

### Accessing elements of matrix

To access the elements of matrix we use the indexing method, first element has index 0 and so on , for column and line matrix 1 index is enough , for rectangular matrix we use double indexing method first index represents lines second index represents column

```
matrix_1=[1; 2; 3; 4]
disp(matrix_1(3)) % This will display the third element which is 3
matrix_2 = [1, 2, 3, 4]
disp(matrix_2(1)) % This will display the first element which is 1
```

```
matrix_3 = [1 2 3;4 5 6;7 8 9]
disp(matrix_3(2,3)) % This will display the third element of the second line which is 6
```

## Matrix Arithmetique

### Addition and Soustraction

If 2 matrix have same size we can add or soustract them using + -

```
matrix_a = [4 5;6 0];
matrix_b = [1 2;3 2];
matrix_c = matrix_a + matrix_b;
matrix_d = matrix_a - matrix_b;
disp(matrix_c);
disp(matrix_d);
```

### Remarque

to calculate the size of matrix we use the function size() it will return 2 numbers first one represent number of lines second one represent number of column.

```
a = [4 5 3;6 0 2];
a_size = size(a);
disp(a_size)
```

### Multiplication And division:

#### Multiplication:

there is 3 types of multiplication

- multiplying matrix by number we just do  $n * M$
- multiplying elements of 2 matrix together, the 2 matrix should have same size we do  $M1.*M2$  it same for division to divide element by element we use  $M1./M2$ , to calculate the square of each element inside matrix we can do  $M.*M$  or we can do  $M.^2$
- multiplication matricielle number of column of first matrix should equal number of line of second one we do  $M1*M2$

```
n = 5;
M1 = [1 2;3 2];
M2 = [4 9;7 8];
M3 = [2 5;4 3;2 1];
m1 = n * M1;
m2 = M1 .* M2;
m3 = M3 * M1;
m4 = M3 .^ 2;
disp("m1 : ");
disp(m1);
disp("m2 : ");
disp(m2);
disp("m3 : ");
disp(m3);
```

```
disp("m4 : ");
disp(m4);
disp("m5 : ");
disp(m5);
```

## Division:

we have also 3 type of division

- dividing matrix by number we just do  $M / n$
- dividing elements of 2 matrix together, the 2 matrix should have same size we do  $M1 ./ M2$
- division of 2 matrix  $M1/M2$  and in this case it will calculate  $M1 * \text{Inv}(M2)$

```
n = 5;
M1 = [1 2; 3 2];
M2 = [4 9; 7 8];
M3 = [2 5; 4 3; 2 1];
m1 = M1 / n;
m2 = M1 ./ M2;
m3 = M2 / M1;
disp("m1 : ");
disp(m1);
disp("m2 : ");
disp(m2);
disp("m3 : ");
disp(m3);
```

## Inverse and determinant of matrix

We calculate determinant of matrix using **det(m1)**, if determinant isn't null we can calculate the inverse of m1

to calculate determinant and inverse the matrix should be square number of column is equal number of lines

There is 2 methods to calculate inverse of matrix:

- using the command `inv()`
- using  $m1^{(-1)}$

```
m = [4 5; 5 3];
d = det(m);
inverse1 = inv(m);
inverse2 = m^(-1);
disp("determinant : ");
disp(d);
disp("inverse method 1 :");
disp(inverse1);
disp("inverse method 2 :");
disp(inverse2);
```

## Remarques

- Matrix M multiplied by its inverse will give us identity matrix I
- Matrix identity I is like 1 any matrix multiplied by this matrix will stay the same  $M \cdot I = M$

## Create interval of value

Sometimes we need to create matrix column of element between 2 numbers. Let's suppose we want to create matrix column that have all numbers from -10 to 10. We can do it as we saw before but when the low and upper bar of the interval change this becomes more difficult to fix that MATLAB provides us with a way to do it using

$m = \text{start}:\text{end}$  the default step between each value is 1 to change that we can add the step so it becomes  $m = \text{start}:\text{step}:\text{end}$

```
first_interval = 4:20;
second_interval = 0:0.1:5;
disp("first interval");
disp(first_interval);
disp("second interval");
disp(second_interval);
```

## Slice and combine matrix

### Slicing matrix

We use slicing to get sub matrix from a parent matrix to get slice from a matrix we use interval instead of row and column index, for the interval we set start and end

```
parent_matrix = [4 5 8 9;4 5 8 9;4 5 8 9;4 5 8 9;4 5 8 9;4 5 8 9];
child_matrix = parent_matrix(1:3,2:3);
disp("child matrix is :");
disp(child_matrix);
```

### Combine matrix together

There are 2 ways to combine matrix

- vertical combine they should have same number of lines we just do  $m = [m_1; m_2]$
- horizontal combine they should have same number of columns we do that by using  $m = [m_1; m_2]$

```
M_1 = [4 5];
M_2 = [3 2;4 8];
M_3 = [M_1;M_2];
disp("Vertical combine of M_1 and M_2");
disp(M_3)
m_1 = [3 2;4 8];
m_2 = [3 2 6 9 10 11;4 8 3 2 8 7];
m_3 = [m_1 m_2];
disp("Horizontal combine of m_1 and m_2");
disp(m_3)
```

## Transpose of matrix and some special matrix

Transpose of matrix is inverting lines and column that mean we turn lines to columns and column to lines we do that using : ' or transpose()

Matrixe identite is square matrix that have 1 and it diagonal and 0 else where we create it using eyes()

Matrix of ones is matrix that full of ones we create it using onese(n,m) n is number of lines and m numbers of column , if it is suqre we can do ones(m)

Matrix of zeros is matrix that full of zeros we create it using zeros(n,m) n is number of lines and m numbers of column , if it is suqre we can do zeros(m)

Finally to get the diagonal of matrix we use diag()

```
G = [4 5 1;2 5 0;4 2 3]
G_t = G'
G_T = transpose(G)
identity_matrix = eye(5)
matrix_of_zeros = zeros(4,5)
matrix_of_ones = ones(4,5)
diagonal = diag(G)
```

## Working with Graph

we saw so far how to work with matrix and how to work with data ow it time to see this data, matab have many tools that help to visualise data and one of them is plots

## Ploting simple functions

lets suppose we have the followig function

$$f(x) = x^2$$

The steps to draw this function are as follow :

- Create variable x represent the interval that we want to draw our function in
- Calculate y
- Using plot to draw the function
- Adding title to the figure and titles for each axis and a legend

```
x = -10:0.1:10;
y = x .^ 2;
plot(x,y);
title("Y = X^2")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("y = x ^ 2")
```

## Plotting multiple graph in same figure

There is 2 way to plot graph in same figure :

### Method 1 Hold on

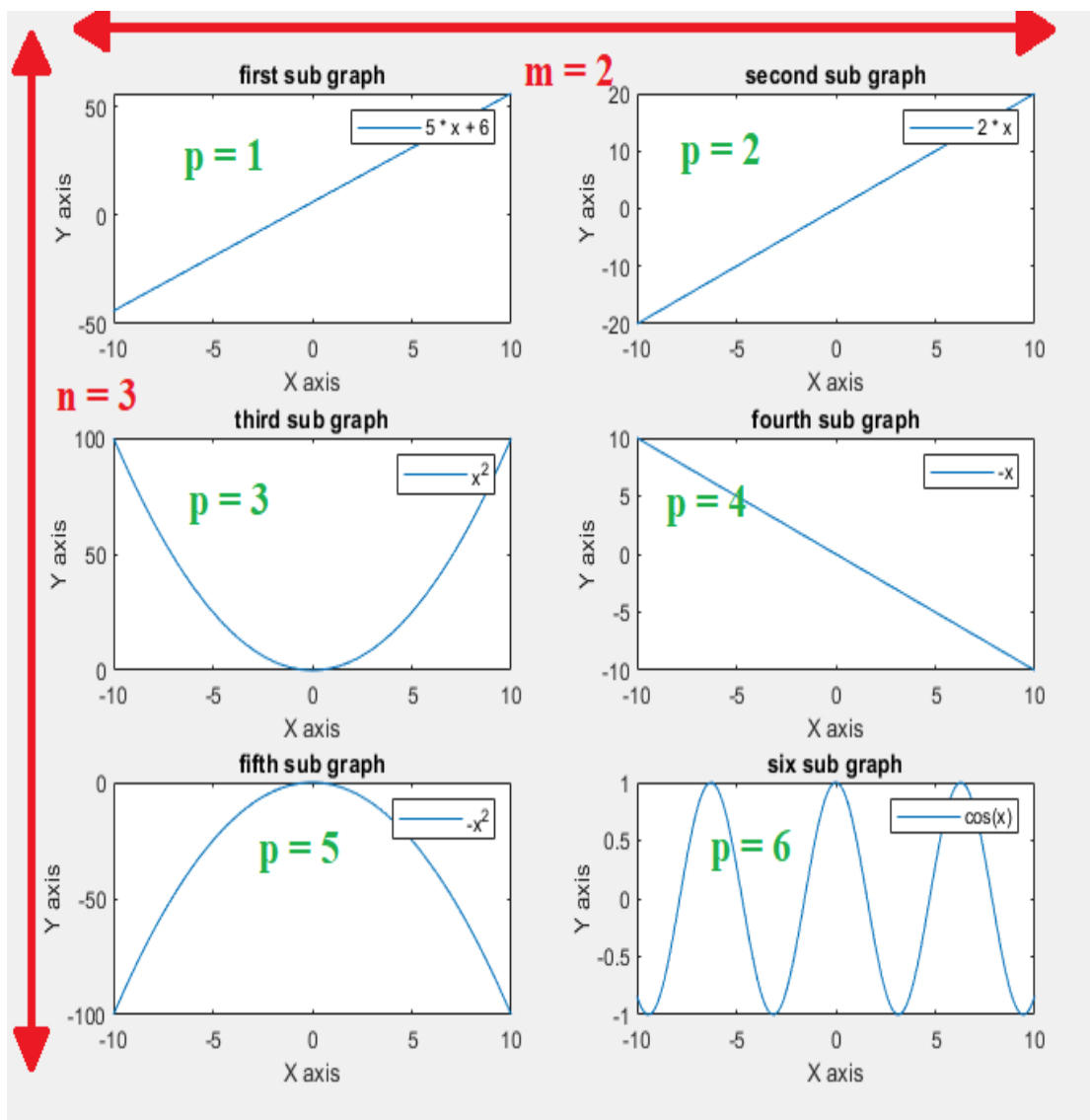
By using the keyword **hold on** matlab to keep the current graph and draw the new graph in top of it

```
x = -10:0.1:10;  
y1 = 5 * x + 6;  
y2 = 2 * x;  
plot(x,y1)  
hold on;  
plot(x,y2)  
title(" plotting using hold on")  
xlabel(" X axis ")  
ylabel(" Y axis ")  
legend("5 * x + 6","2 * x")
```

### Dividing the figure

The other method to plot graph in same figure is by dividing the figure to many subfigure we use this by using the function subplot(n,m,p)

- n is number of lines that will figure will be divides by
- m is number of column that will figure will be divides by
- p position where we want to put our subplot counting start from top left till bottom right



```
x = -10:0.1:10;
y1 = 5 * x + 6;
y2 = 2 * x;
y3 = x .^ 2;
y4 = -x;
y5 = -x .^ 2;
y6 = cos(x);

subplot(3,2,1)
plot(x,y1)
title(" first sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("5 * x + 6")
subplot(3,2,2)
plot(x,y2)
title(" second sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
```

```

legend("2 * x")
subplot(3,2,3)
plot(x,y3)
title(" third sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("x^2")
subplot(3,2,4)
plot(x,y4)
title(" fourth sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("-x")
subplot(3,2,5)
plot(x,y5)
title(" fifth sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("-x^2")
subplot(3,2,6)
plot(x,y6)
title(" six sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("cos(x)")

```

## Ploting Graph in diffirent figures

Last way to plot multiple graph is using deffirent figures for each graph , to do what all what we need to do is using the function **figure()** inside it number of the figure

```

x = -10:0.1:10;
y1 = 5 * x + 6;
y2 = 2 * x;
figure(1)
plot(x,y1)
title(" first sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("5 * x + 6")
figure(2)
plot(x,y2)
title(" second sub graph ")
xlabel(" X axis ")
ylabel(" Y axis ")
legend("2 * x")

```

## Remarque

we can costumize plot for example changing color and plot using stars instead of line ...

```

x = -10:1:10;
y1 = 5 * x + 6;

```



```
y2 = 2 * x;  
figure(1)  
plot(x,y1,'r*')  
title(" first sub graph ")  
xlabel(" X axis ")  
ylabel(" Y axis ")  
legend("5 * x + 6")  
figure(2)  
plot(x,y2,'ro')  
title(" second sub graph ")  
xlabel(" X axis ")  
ylabel(" Y axis ")  
legend("2 * x")
```

This table of costumization parametres and what they do

Line Style	Description
-	Solid line (default)
--	Dashed line
:	Dotted line
-.	Dash-dot line

Marker	Description
o	Circle
+	Plus sign
*	Asterisk
.	Point
x	Cross
s	Square
d	Diamond
^	Upward-pointing triangle
v	Downward-pointing triangle
>	Right-pointing triangle
<	Left-pointing triangle
p	Pentagram
h	Hexagram

Color	Description
y	yellow
m	magenta
c	cyan
r	red
g	green
b	blue
w	white
k	black

## Tasks :

### Task 1 :

Using graph and interval from -20 to 20 solve this function

$$f(x) = x^2$$

$$g(x) = 3x + 4$$

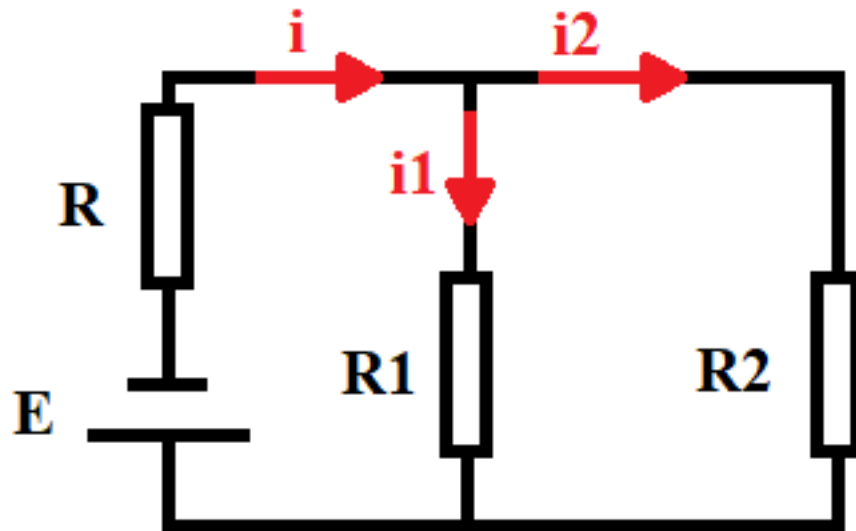
$$f(x) < g(x)$$

%Solution

### Task 2 :

We Have the following circuit and the systemes of equation that each maille represent , using matrix arithmetique find **i1** and **i2**

$$E = 5 \text{ v}, R = 2\Omega, R1 = 5\Omega, R2 = 7\Omega$$



$$i = i1 + i2$$

$$E = Ri + R1i1$$

$$E = Ri2 + R2i2$$

using the first equation we can say

$$E = R(i1 + i2) + R1i1$$

$$E = R(i1 + i2) + R2i2$$

the final result become :

$$E = Ri2 + (R1 + R)i1$$

$$E = Ri1 + (R2 + R)i2$$

we will get this system of equations :

$$5 = 2 * i2 + 7 * i1$$

$$5 = 2 * i1 + 9 * i2$$

**Hint:**

When we have system of equations we can use the matrix representation of the system as follow

$$2x + 3y = 5$$

$$x + 7y = 6$$

$$\begin{bmatrix} 2 & 3 \\ 1 & 7 \end{bmatrix} * \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 6 \end{bmatrix}$$

Where

$$A = \begin{bmatrix} 2 & 3 \\ 1 & 7 \end{bmatrix}$$

$$X = \begin{bmatrix} x \\ y \end{bmatrix}$$

$$B = \begin{bmatrix} 5 \\ 6 \end{bmatrix}$$

we will get

$$AX = B$$

$$A^{-1}AX = A^{-1}B$$

$$X = A^{-1}B$$

% Solution