

Parity  $\rightarrow$  no. of 1's are present in the given code. ①

There are 2 types of Parity

Odd Parity  $\rightarrow$  If the no. of ones present in the code is odd

then this is called odd Parity.

For eg. In a 5 bit code

11010  $\rightarrow$  eg. of odd parity (3 ones are present)

To make this code as odd parity code, we need to add  $P_{od} = 0$

Eg. 11011  $\rightarrow$  eg. of To make this code as odd parity code, we need to add  ~~$P_{od}$~~   $P_{od} = 1$  [ $P_{od} \rightarrow$  odd parity bit]

Even Parity  $\rightarrow$  If the no. of ones present in the code is even then this is called even Parity.

Eg.  $\rightarrow$  1100101  $\rightarrow$  eg. of even Parity (4 ones)

To make this code as even parity,  
we need to add even parity bit

$$P_{ev} = 0$$

e.g. 11010 → To make this code as even parity code, we need to add  $P_{ev} = 1$

Use of Parity bit generator &  
Parity checker

When digital data is transmitted from ~~one~~ transmitter to receiver, it is necessary to know at the receiving end whether the received data is error free.



A simple form of error detection is achieved by adding an extra bit to the transmitted word. This additional bit is known as

Parity bit and it decides whether the data transmitted is free of error or not. (3)

⇒ To detect ~~and~~ the error in the digital data at the receiver end we use Parity bit.

Even Parity generator →  
← Even Parity generator will maintain the data in even no. of ones.

Let we are taken 3 bit message

A, B, C

we can draw truth table for 3

bit data

A	B	C	P <sub>ev</sub>
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

In this truth table, we will P<sub>ev</sub> generate even parity for given 8 possible Combinations

Parity bit, we draw 8 cell K-map.

	BC	00	01	11	10
A	0	1	1	1	1
i	1	1	1	1	1
	1	1	1	1	1

4 single grouping

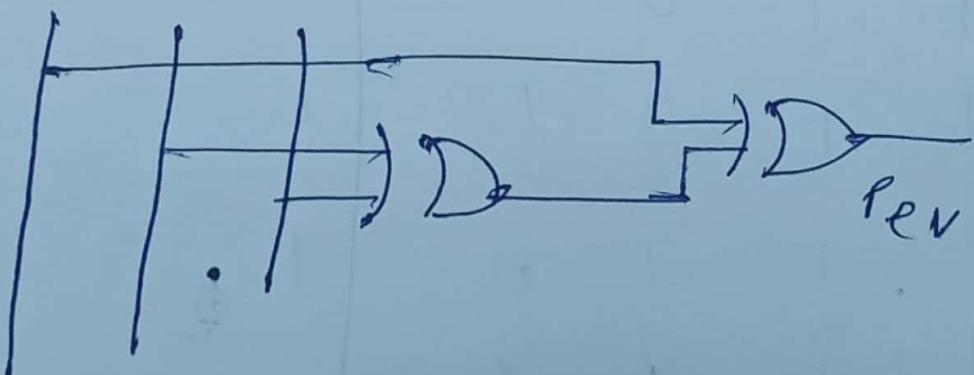
$$\begin{aligned}
 P_{ev} &= \overline{A}\overline{B}C + \overline{A}B\overline{C} + A\overline{B}\overline{C} + A\overline{B}C \\
 &= \overline{A}(\overline{B}C + B\overline{C}) + A(B\overline{C} + \overline{B}\overline{C}) \\
 &= \overline{A}(B \oplus C) + A(\overline{B} \oplus \overline{C}) \\
 &= \overline{A}x + A\overline{x} \\
 &= \overline{A}A \oplus x \quad x = B \oplus C
 \end{aligned}$$

$$P_{ev} = A \oplus (B \oplus C)$$

This is the expression for even parity.

Logic dig. for even parity generator

A    B    C



X-OR Gate used to generate even Parity.

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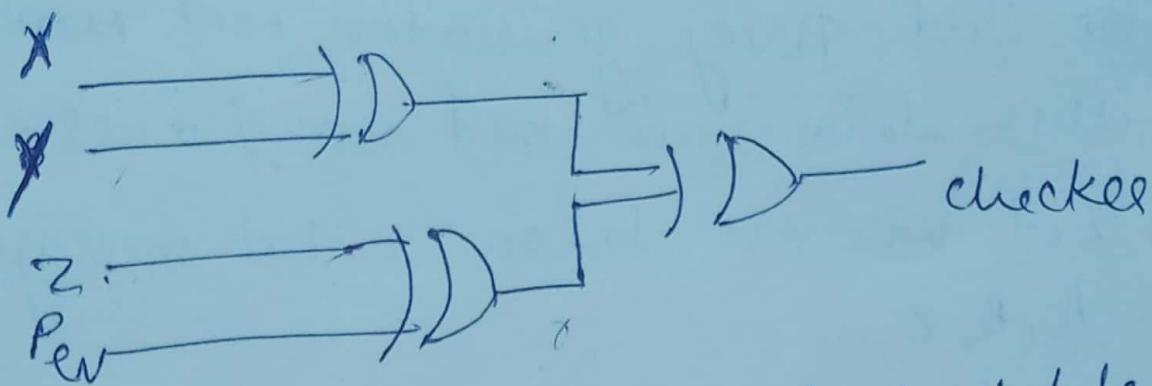
## Even Parity checker

Now we will send 3 kit data along with even parity bit to the receiver end

By	z	Pev	checker	x, y, z ↓ Received data
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	if checker = 0 No error
0	1	0	1	if checker = 1 error
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

(6)

even  
Parity checker ckt  $\rightarrow$



It is clear from the truth table  
as even no. of ones are present  
checker shows 0.

& if odd no. of ones are present  
checker shows 1. This is  
nothing but the function of  
X - OR gate.

# Odd Parity generator →

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- Odd parity generator will maintain the data in odd no. of ones.

Let we are taken 3 bit message

A, B, C

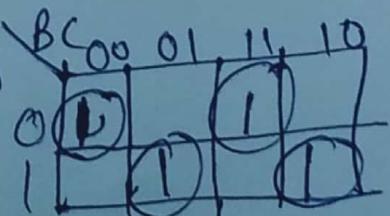
we can draw truth table for 3 bit data

A	B	C	Parity
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

Here, we will generate  
Parity will generate  
odd parity for  
given possible  
combinations.

8 cell

Now we will draw k-map for the  
odd parity bit A



4 single grouping

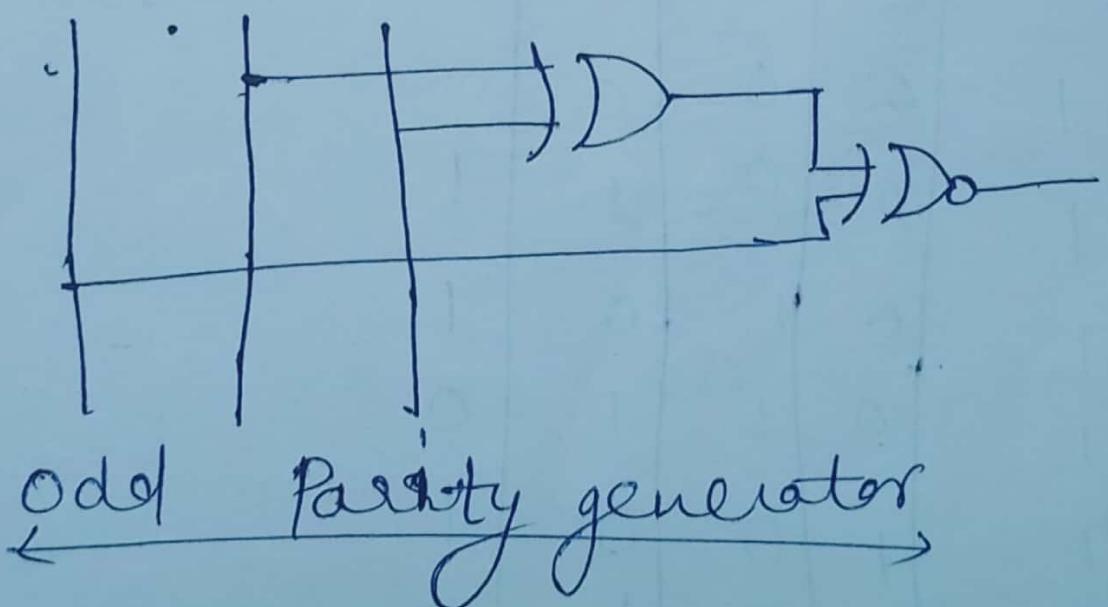
(8)

$$\begin{aligned}P_{od} &= \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}C + ABC \\&= \bar{A}(B\bar{C} + \bar{B}\bar{C}) + A(\bar{B}C + B\bar{C}) \\&= \bar{A}(\bar{B} \oplus C) + A(B \oplus C) \\&= \bar{A}\bar{x} + Ax \quad x = B \oplus C \\&= \overline{\bar{A} \oplus x} \quad \overline{\bar{A} \oplus x} = A \odot x \\&= A \odot x\end{aligned}$$

$$P_{od} = A \odot (B \oplus C)$$

$$\begin{array}{c} \overline{\bar{A} \oplus x} = A \odot x \\ \downarrow \\ A \times \text{Not } x \end{array}$$

logic dig → A B C



# Odd Parity checker

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Now we will send 3 bit data along with odd parity bit to the receiver end (total 4 bit data)

x	y	z	Parity	checker
0	0	0	0	1
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

if checker = 0

No error

if checker = 1

Error

-

-

-

-

-

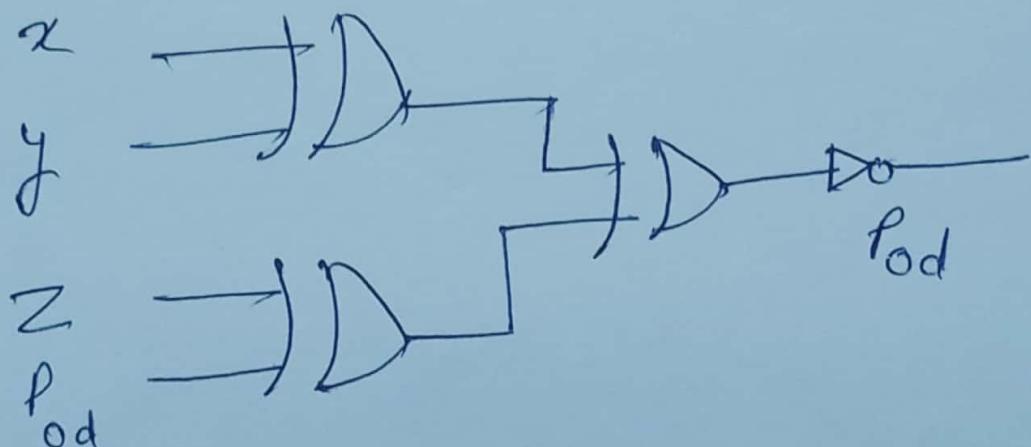
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Odd Parity checker ckt  $\rightarrow$  ⑩

It is clear from the truth table as odd no. of ones are present checker shows 0 as even no. of ones are present checker shows 1.

This is nothing but the truth table of X-NOR Gate

Odd Parity checker ckt  $\rightarrow$



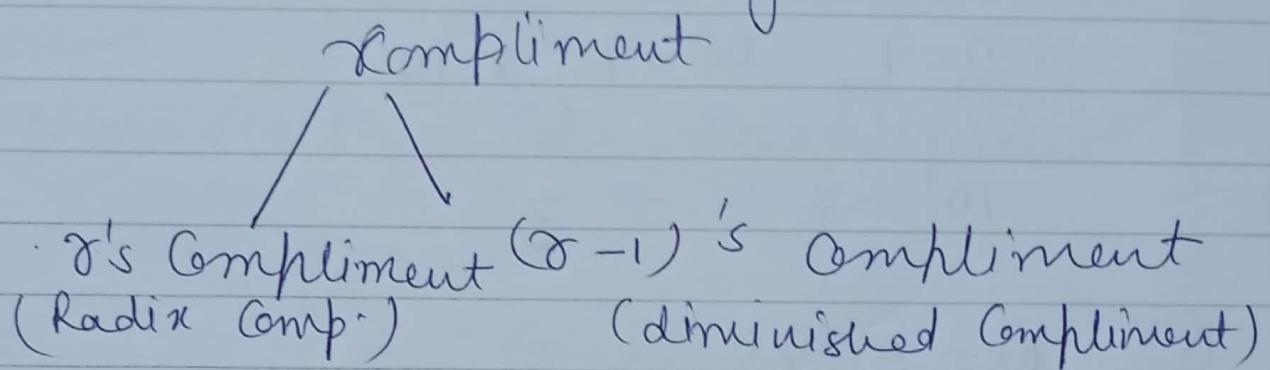
# Complements →

①

M T W T F S S  
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Complements are used in digital computers for simplifying the subtraction operation and for logical manipulation.

There are 2 types of Complements for each base or system



For binary,  $\tau = 2$

Therefore 1's, 2's Complements are possible in binary.

In decimal no. system  $\tau = 10$

$\therefore$  9's, ~~10's~~ 10's Complements are possible.

For 2's & ~~10's~~ 10's

for 2's Complement & 10's Complement  
(9's Complement)

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Formula is  $\vartheta^s$ 's (Compliment)

$$\vartheta^n - N$$

$n$  is the number given

$\vartheta$ , " base

$n$  - no. of digit in the number given

Q. Compliment of  $(7)_{10}$

$$n=1, N=7, \vartheta=10$$

$$10^1 - 7 = 3$$

Q.  $N = 5690$

$$\vartheta^n - N$$

$$10^4 - 5690$$

$$10000 - 5690 = 4310$$

Q.  $N = 1101$  find  $\vartheta$ 's compliment

$$2^4 - 1101$$

$$16 - 1101$$

$$10000 - 1101$$

W

3

M	T	W	T	F	S	S
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 Date / / /

$$\begin{array}{r}
 1 & 1 & 0 & 1 & 0 & 1 \\
 - & 1 & 1 & 0 & 1 \\
 \hline
 0 & 0 & 1 & 1
 \end{array}$$

$$\begin{array}{r}
 10000 - 1101 \\
 = \underline{\underline{11}}
 \end{array} \quad (16 - 13 = 3)$$

H.W.  $N = 76895$        $10^{\text{th}}$  Compliment

$N = 11011$        $\alpha^{\text{'s}}$  Compliment

For  $(\alpha-1)$ 's Compliment  
formula

$$(\alpha^n - 1) - N$$

$N$  - number given

$n$  - no. of digits in the number

$\alpha$  - base

$\alpha$ 's Compliment of 0011 is 1100 ✓  
by formula →

$$(\alpha^n - 1) - 0011$$

$$\begin{array}{r}
 15 - 0011 \Rightarrow 1111 - 0011 \\
 = 1100 \quad \checkmark
 \end{array}$$

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9's Compliment of 1234

I<sup>st</sup> Method →

subtract the given no. from 9999

$$\begin{array}{r} 9999 \\ - 1234 \\ \hline 8765 \end{array}$$

II<sup>nd</sup> Method →

$$(2^n - 1) - N$$

$$\begin{aligned} (10^4 - 1) - 1234 \\ 9999 - 1234 \\ = 8765 \end{aligned}$$

ex → subtract 1101

$$- 1001$$

by 2's Compliment method

~~4100~~ 1's Compliment of 1001

$$\text{is } 0110$$

$$\text{Add } 1$$

$$\begin{array}{r} \\ + 1 \\ \hline 0111 \end{array}$$

W —

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$$\begin{array}{r}
 \phantom{0} \\
 + 1101 \\
 \phantom{0}0111 \\
 \hline
 10100
 \end{array}$$

If there is left most digit is 1  $\Rightarrow$  answer is +ve and in that case the left most digit dropped and the answer is lead from the remaining digit

$\Rightarrow$  Answer is 0100

$$\left[ \begin{array}{r}
 1101 \rightarrow 13 \\
 1001 \rightarrow 9 \\
 \hline
 100
 \end{array} \right]$$

~~$$\begin{array}{r}
 \phantom{0}0100 \\
 - 0111 \\
 \hline
 \end{array}$$~~

1's Compliment of 0111 is 1000

Now

~~$$\begin{array}{r}
 0100 \\
 1000 \\
 \hline
 1100
 \end{array}$$~~

If there is a 0 in the left most digit then answer will be negative (-ve). Zero is dropped

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and remainder is converted to its  
2's Compliment.

~~is Compliment of 1100 is 0011  
2's Compliment

$$\begin{array}{r}
 0011 \\
 + 1 \\
 \hline
 100
 \end{array}$$~~

~~eg. 01 00  
 - 01 11~~

~~1's Comp. of 0111 is 1000  
 2's Comp. → Add~~

$$\begin{array}{r}
 1000 \\
 + 1 \\
 \hline
 1001
 \end{array}$$

~~$$\begin{array}{r}
 0100 \\
 + 1001 \\
 \hline
 1101
 \end{array}$$~~

if there is no extra digit  $\Rightarrow$  0 in  
the left most digit  $\Rightarrow$  Answer  
is -ve. In that case, zero  
is dropped and then to convert  
1101 into +ive no. we take  
2's Comp of 1101

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M	T	W	T	F	S	S
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1101  
1's Comp.  
2's Comp.

$$\begin{array}{r}
 0010 \\
 + \cancel{0} \quad 1 \\
 \hline
 0011
 \end{array}$$

Again there is no extra digit (Carry) : so we take the answer as -0011.

example → subtract 72532 - 13250  
First find 10's Compliment of 13250

$$\begin{array}{r}
 99999 \\
 - 13250 \\
 \hline
 86749 \\
 + 1 \\
 \hline
 86750
 \end{array}$$

$$\begin{array}{r}
 \text{Now } 72532 \\
 + 86750 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 \text{Sum } 159282 \\
 \hline
 \end{array}$$

there is carry of 1  $\Rightarrow$  Ans is +ve and we can ignore it.

$$\text{So } 7252 - 13250 = 59282$$

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Now subtract

$$13250 - \cancel{72} 72532$$

First find 10's complement of  
72532

$$\begin{array}{r}
 99999 \\
 +2532 \\
 \hline
 27487 \\
 +1 \\
 \hline
 27468
 \end{array}$$

$$\begin{array}{r}
 13250 \\
 27468 \\
 \hline
 \end{array}$$

$$\text{sum } \underline{40718}$$

there is no end carry  
 $\Rightarrow$  answer is -ve and then  
take 10's Compliment of 40718

$$\begin{array}{r}
 99999 \\
 40718 \\
 \hline
 59281 \\
 +1 \\
 \hline
 \text{W } 59282
 \end{array}$$

$\Rightarrow$  there is no end  
carry  $\Rightarrow$  Ans is  
- 59282

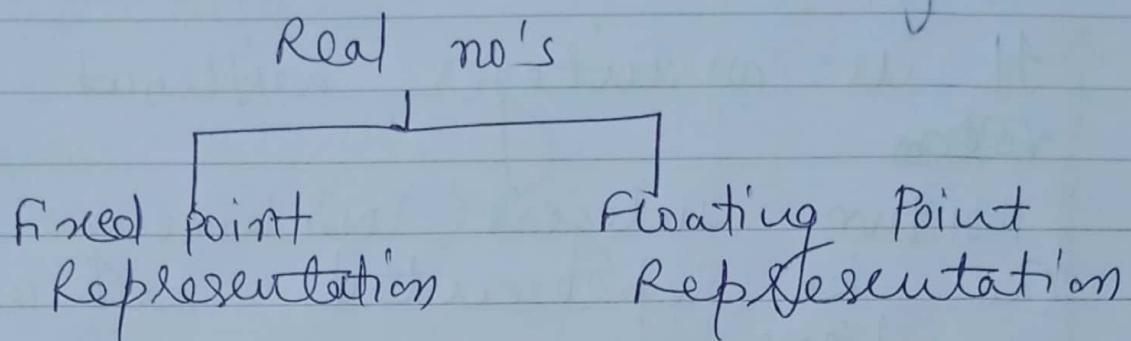
③

## Fixed Point Representation →

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In order to represent real no's.  
(Integer part + fractional part) in  
modern computers, there are  
2 approaches



Fixed point representation → It  
means there is a fixed no. of  
digits after a decimal point.  
This implies binary point should  
be fixed.

Fixed point representation is  
of 2 types

(1) unsigned fixed point number.

(2) signed fixed point number.

Signed fixed point number can  
be represented in 3 ways.

(16)

- a) signed - magnitude representations
- b) signed 1's Compliment,,
- c) " 2's " ,,,

## Unsigned Fixed Point numbers →

It is an integer without a sign.

~~values~~

Positive integers including zero,  
can be represented as unsigned  
numbers.

Its range is between 0 & +ve infinity.  
Most significant bit of an unsigned no. is always zero.  
For eg. for 8 bit integer  
it should follow the range 0 to 255.

eg. I store 7 in an 8 bit memory  
(location?)

First step → Convert 7 into binary

Add five 0's to make total of  
 $N(8)$  bits

00000111

→ zero means +ve integer

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Eg. 2 store 258 into a 16 bit memory location.

⇒ change 258 into binary

.1.000 00010

2	258	
2	129	0
2	64	1
2	32	0
2	16	0
2	8	0
2	4	0
2	2	0
	1	0

Add Seven 0's to make total N(16) bits

000 0000 1000 00010

So 0000 00010000 0010

will be stored in 16 bit memory location.

Eg. of storing unsigned integer in 8 diff locations

decimal	8 bit location	16 bit location
7	00000111	0000000000000111
234	11101010	0000000011101010
258	overflow	0000000100000010
24, 760	overflow	0.110000010111000
1, 24, 5878	overflow	overflow

W

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e.g. Represent fixed point representation of unsigned binary no. 0 110 110 using four integer bits & 3 fractional bits.

no. can be divided into 3 parts

sign part	integer part	fractional part
-----------	--------------	-----------------

0 110 110  
↓  
sign bit

Integer part is always included with the sign bit.

0 110 . 110

Now Convert  $(0110.110)_2$  into Decimal

$$0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3}$$

$$0 + 4 + 2 + 0 + 0.5 + 0.25 + 0 \\ = (6.75)_{10}$$

W

# Signed fixed point no. 13

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When an integer binary no. is +ve the sign is 0 & If it is -ve, the sign will be 1 and the rest of the number may be represented in ~~the~~ any of the 3 ways!

a) Signed - Magnitude representation  
The signed - magnitude representation of a negative number consists of magnitude and a negative sign.

e.g. +14 to be stored in 8 bit register

(i) Change 14 to binary 1110  
Now to make it of total N(8) bits  
add ~~0~~ four 0's  
00001110

No w

-14 to be stored in 8 bit register

↓  
1 0001110

First Most significant bit will be 1  
That represent number is -ve.

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(1)

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The signed magnitude system is used in ordinary arithmetic but it is awkward when employed in computer arithmetic.

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b) Signed - 1's Compliment representation

In this method 1's Compliment of the positive value has to be taken.

Eg (-14) → Convert +14 into binary

00001110

Now 1's Compliment of 00001110  
is

11110001

So 11110001 will be stored in  
8 bit register

The 1's Compliment imposes difficulties & seldomly used for arithmetic operations.

c) Signed - 2's Compliment representation  
→ In this method 2's Compliment of the +ive value has to be taken.

Eg (-14) → 00001110

No with 1's Compliment 11110001

Compliment

+ 1

11110010

N

2's

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1111 0010 will be stored in  
8 bit memory location.

e.g. represent (-7.5)<sub>10</sub> using 8-bit binary representation with 4 integer digit & 4 fraction bit

$$(-7.5)_{10} = (111 \cdot 1)_2$$

$$\begin{array}{r} 0.5 \times 2 = 1.0 \\ 0.0 \end{array}$$

$$(0111 \cdot 1000)_2$$

Now find 2's Comp.

$$\begin{array}{r} 1's \text{ Comp} \quad 1000 \cdot 0111 \\ 2's \text{ Comp} \quad \underline{-} \\ \hline 1000 \cdot 1000 \end{array}$$

$$(-7.5)_{10} = (1000 \cdot 1000)_2$$

e.g. Compute  $0.75 + (-0.625)$   
using fixed point numbers

Step 1 0.75 Convert into binary

$$0000 \cdot 1100$$

$$\begin{array}{r} 0.75 \times 2 = 1.5 \quad 1 \\ 0.5 \times 2 = 1.0 \quad 1 \\ 0.0 \times 2 = 0 \quad 0 \end{array}$$

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Now step 2

$0.625$  converting binary

$$0000 \cdot 1010$$

Now 2's Complement for  $(-0.625)$

$$1111 \cdot 0110$$

Step -3

$$\text{Now } 0.75 + (-0.625)$$

$$\begin{array}{r} 0000 \cdot 1100 \\ + 1111 \cdot 0110 \\ \hline 10000 \cdot 0010 \end{array}$$

extra there is carry in the MSB.  
no. is +ve & it will be discarded.

ex. Assume no. using 32 bit format  
which reserve 1 bit for sign  
15 bits for integer & 16 bits  
for fractional part

no. is  $-43.625$ 

S	I	F
1	15	16

Now step 1  $43.625$  in binary form

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101011 1010

0000000001010111010000000000

2	43	
2	21	1
2	10	1
2	5	0
2	2	1
2	1	0

Just a representation  
Representation

10000000001010111010000000000000

$$\begin{array}{r}
 0.625 \times 2 = 1.25 \quad 1 \\
 0.25 \times 2 = 0.5 \quad 0 \\
 0.5 \times 2 = 1.0 \quad 1 \\
 0 \qquad \qquad \qquad 0
 \end{array}$$

by finding exact value of -43.625 can be obtained  
 0000000001010111010000000000000

[11111111010100.0110000000000000]

eg. Convert decimal no. 7.75 to  
fixed point binary no.

7.75

step 1 Convert 7.75 into binary form

111.110

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The following binary no are stored using 2's Complement in a 12 bit register with 4 bits after binary point. Convert it into decimal fraction.

0 . 1111 1111 111											
Sign & Integer											Fraction
-128	64	32	16	8	4	2	1	0.5	0.25	0.125	0.0625
0	1	1	1	1	1	1	1	1	1	1	1

→ last no. represents sign bit  
- put at MSB

$$0 + 64 + 32 + 16 + 8 + 4 + 2 + 1 + 0.5 + 0.25 \\ + 0.125 + 0.0625$$

$$\Rightarrow 127.9375$$

Convert into 1111 1111.1111

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sign & integer

fraction

128	64	32	16	8	4	2	1	0.8	0.25	0.125	0.0625
1	1	1	1	1	1	1	1	1	1	1	1

$$-128 + 64 + 32 + 16 + 8 + 4 + 2 + 1 + \\ 0.5 + 0.25 + 0.125 + 0.0625$$

$$\Rightarrow -0.0625$$

eg

0 0 0 0 0 111.0010

sign & integer      fraction

-128	64	32	16	8	4	2	1	0.8	0.25	0.125	0.0625
0	0	0	0	0	1	1	1	0	0	1	0

$$4 + 2 + 1 + 0.125 \neq 7.125$$

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(2)

Q using 2's Compliment, Convert the following decimal no. into fixed point binary no. to be stored in 16 bit register with 4 bits after binary point

Ex. 7.5

111.1000

000000000000111.1000

Ex.

-45.75

45.75  $\Rightarrow$  101101.1100

(000000101101.1100)

Now

$-(45.75) \rightarrow$  2's Comp. of 000000001101.1100

$-(45.75)_{10} = (11111010010.0100)_2$

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# Floating Point Representation →

The floating point representation of a number has 3 parts.

- a) Mantissa (M)
- b) Base (B)
- c) Exponent (E)

In floating point representation, binary point floats to the right of the MSB and an exponent is used.

The fixed point mantissa may be a fraction or an integer.

The value of the exponent indicates that the actual position of the decimal point.

The scientific representation of a floating point no. is of the form

$$\boxed{\pm M \times B^E}$$

only the mantissa & exponent are physically represented in the register (including their signs).

The radix  $B$  and radix point are always assumed.

Floating point representation is used to represent very small as well as very large no.

eg

$$0.0000657$$

$$6.57 \times 10^{-5}$$

~~$$6.7 \times 10^0$$~~

~~$$6.7 \times 10^5$$~~

$$M \quad B^E$$

eg.	Number	Mantissa	Base	Exponent
	$9 \times 10^8$	9	10	8
	$110 \times 2^7$	110	2	7

$$4364.784 \quad 4364784 \quad 10 \quad -3$$

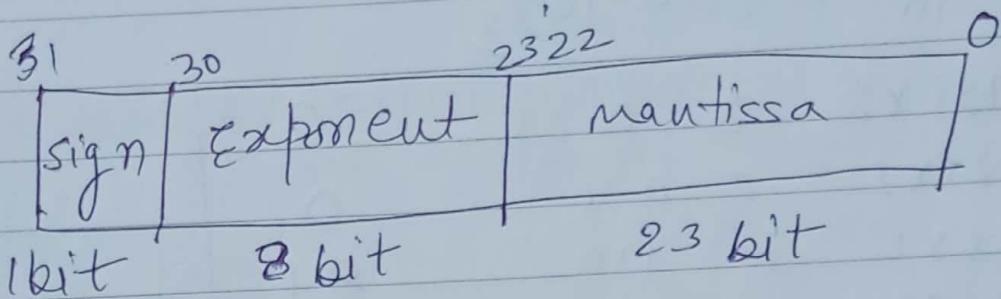
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EEE 754 floating point no representation →

Can be represented in 2 ways  
single precision format →

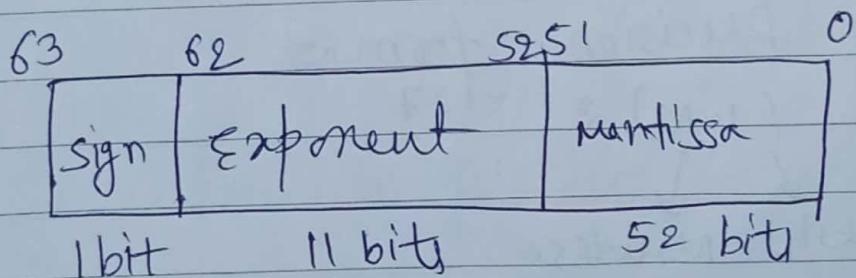
It can represent no's upto 32 bit



if sign bit is zero → +ve no'  
 " " " is one → -ve no.

b) Double precision formation →

It can represent no's upto 64 bits



WV

eg: → Represent double precision (1259.125)<sub>10</sub> in single format.

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Step - 1 Convert (1259.125)<sub>10</sub> to (??)<sub>2</sub>

$$(1259)_{10} \rightarrow (10011101011)_2$$

$$(0.125)_{10} = (0010)_2$$

$$\begin{array}{rcl}
 0.125 \times 2 & = & 0.25 & 0 \\
 0.25 \times 2 & = & 0.5 & 0 \\
 0.5 \times 2 & = & 1.0 & \cancel{1} \\
 1.0 \times 2 & = & 0 & 0
 \end{array}$$

$$(1259.125)_{10} = (10011101011.0010)_2$$

Step - 2 → Normalize the number

For single precision format

$$(1.N)_2 E - 127$$

Sign bit      Mantissa

127 - Bias no. for 32 bit

For double precision format

$$(1.N)_2 E - 1023$$

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Now  $(10011101011, 0010)_2$

$$1.0011101011 \times 2^{10}$$

Step-3 single precision format

$$[1.N]_2 E-127$$

$$1.00111010110010 \times 2^{10}$$



$$\Rightarrow E-127=10$$

$$\Rightarrow E=137=(10001001)_2$$

$$\begin{array}{r}
 137 \\
 2 \overline{) 68} \\
 2 \overline{) 34} \\
 2 \overline{) 17} \\
 2 \overline{) 8} \\
 2 \overline{) 4} \\
 2 \overline{) 2} \\
 1
 \end{array}$$

0	10001001	001110101100100
1bit	8 bits	23 bits

Step-4 Double precision format

$$[1.N]_2 E-1023$$

$$1.00111010110010 \times 2^{10}$$

$$E - 1023 = 10$$

$$E = 1033$$

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$$(1033)_{10} = (10000001001)_2$$

0	1000 000100100111010110010...
---	-------------------------------

Q. Represent IEEE standard for given no

$$1.00010100 \times 2^{-10}$$

31	30	23 22	0
0	01110101	00010100 ... 000	

23 bit

$$E - 127 = -10$$

$$E = 117$$

$$= (110101)_2$$

$$(1.N) \times 2^E$$

$$\begin{array}{r} 2 | 117 \\ 2 | 58 \quad 1 \\ 2 | 29 \quad 0 \\ 2 | 14 \quad 1 \\ 2 | 7 \quad 0 \\ 2 | 3 \quad 1 \\ 2 | 1 \quad 1 \\ \hline & 000 \end{array}$$

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Represent in floating pt representation

1.11011110010

$$1.11011110010 \times 2^6$$

0	110	11011110010
---	-----	-------------

Normalize floating Point no. →

In Computer, Real no's are represented in the form of normalize floating point no.

~~eg~~ A no. is said to be normalised if

- ①  $0.1 \leq \text{mantissa} < 1$  (The integer part should be zero.)
- ② In a given decimal no. before decimal point, it should always be zero. Immediately after decimal point no. should be non-zero.

12.56

$$0.1256 \times 10^2$$

$$123.46 \times 10^{-6}$$

$$0.12346 \times 10^{-3}$$

WV

$$0.00246 \times 10^{-3}$$

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$$0.246 \times 10^{-5}$$

00011010    8bit binary no. is  
not normalized

To make it normalize

$$0.\underline{11010} \times 2^{-3}$$

~~Mantissa~~

Mantissa — 11010000

Normalized numbers provide the maximum ~~for~~ possible precision for the floating-point no.

W —

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e.g. Convert the following floating point binary number into decimal in a single precision format.

① ~~011010000000000011~~

Assume 9 bits as Mantissa & 6 bits exponent.

0	110100000	000011	
sign	Mantissa	6bit exponent	

Exponent →

-32	16	8	4	2	1
0	0	0	1	1	

= 3

$$\text{Exponent} = 2^3$$

~~01101000000000~~

~~0.1101000000 × 2^3~~

~~0.1101000000 × 2^3~~

~~0110.100000~~  
- 8 4 2 1 | 0.5 0.25 0.125 0.0625  
0 1 1 0 | 1 0 0 0 0

$$4 + 2 + 0.5 = 0.875(6.5)_{10}$$

$$(0110100000000011)_2 = (6.5)_{10}$$

eg 01010100000000 10  
 9 bits mantissa  
 6 bits exponent

0	101010000	000010
1		

exponent → 2.  
 $2^2$        $2^5 2^4 2^3 2^2 2^1 2^0$   
 000010

$$0101010000 \times 2^2$$

421    0.5025 0.125

$$\cancel{0} + \cancel{2} + 0 \mid + 0.5 + 0 + 0.125 + 0$$

~~2.625~~  $(2.625)_{10}$

W

23

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eg. Convert the following floating point binary no. into decimal.  
 Assume 10 bits for Mantissa & 5 bit for exponent both in 2's complement

0 11011 0000000100

0	110110	000	00100
---	--------	-----	-------

1bit      10bits

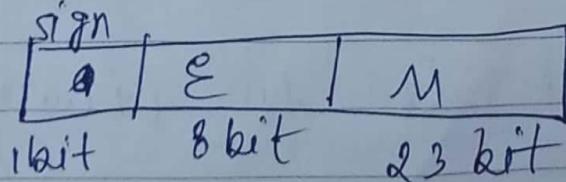
$\times 2^4$

0 1101 | 1.00000  $\times 2^4$

$$1 + 4 + 8 + 0.5 = \underbrace{(13.5)}_{10}$$

eg. How to represent a number in IEEE 754 32 bit floating pt no-

263.3



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$$\Rightarrow (263)_{10} = ( )_2 = 100000111 \quad (3^{\text{rd}})$$

$$\Rightarrow (0.3)_{10} = ( )_2 = 010011001100$$

$$0.3 \times 2 = 0.6 \quad 0$$

$$0.6 \times 2 = 1.2 \quad 1$$

$$0.2 \times 2 = 0.4 \quad 0$$

$$0.4 \times 2 = 0.8 \quad 0$$

$$0.8 \times 2 = 1.6 \quad 1$$

$$0.6 \times 2 = 1.2 \quad 1$$

$$0.2 \times 2 = 0.4 \quad 0$$

$$0.4 \times 2 = 0.8 \quad 0$$

$$0.8 \times 2 = 1.6 \quad 1$$

$$0.6 \times 2 = 1.2 \quad 1$$

$$0.2 \times 2 = 0.4 \quad 0$$

Now step -1

$$(263.3)_{10} = (100000111 \cdot 010011001100)_2$$

step -2  $1.00000111010011001100 \times 2^8$

Step-3  $[1.N]_2 E -127$  standard form

Exponent is in binary form.

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Compare  $(1 \cdot N)_2 \times E-127 = 2^8$

$$E-127 = 8$$

$$E = 135$$

$$E = 135 = 10000111$$

$$\begin{array}{r} 2 | 135 \\ 2 | 67 \\ 2 | 33 \\ 2 | 16 \\ 2 | 8 \\ 2 | 4 \\ 2 | 2 \\ 1 \end{array}$$

Now

0	10000111	0000011010011001100110
---	----------	------------------------

eg. Convert 0100000000111110

1 as sign bit, 9 bit as integer & 6 bit as exponent

S	M	E
0	100000000	111110

step 1 write the binary no. in a proper format.

-32	16	8	4	2	1
1	1	1	1	1	0

$$\begin{aligned} -32 + 16 + 8 + 4 + 2 + 0 \\ \therefore \text{Exponent is } -2 \end{aligned}$$

$$\Rightarrow 0.10000000 \times 2^{-2}$$

Now put the decimal point according to the exponent.

so actual no. is

$$0.0010000000$$

$$\begin{array}{r} 2 | 0.10000000 \\ 0 | 0.125 \end{array} = 0.125$$

$$\Rightarrow 0.100$$

$$\therefore (01000000111110)_2 = (0.125)_{10}$$

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Gray Code → The table below

gives gray code with their equivalent decimal & binary code.

Decimal no.	Gray Code	Binary
0	000(0)	0000
1	0001	0001
2	0011	0010
3	0010	0011
4	0110	0100
5	0111	0101
6	0101	0110
7	0100	0111
8	1100	1000
9	1101	1001
10	1111	1010
11	1110	1011
12	1010	1100
13	1011	1101
14	1001	1110
15	1000	1111

Comparison between Gray Code &  
Binary Code →

The Comparison between Gray Codes  
and binary code is as given

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in the above table. If we take any 2 consecutive decimal no's in gray code then we see that there is a change in only one bit position. Now we consider the binary corresponding decimal no. 3 & 4. If we notice that there is a change in 3 bit position. This greatly enhance the chances of error whereas in the gray code, since only one bit changes between decimal no's 3 & 4 the chances of error reduced. Again the another advantage is it takes a finite time for changes in bit position. Therefore Gray code circuitry can operate at higher speed.

Disadvantages → The disadvantage with the Gray code is that it cannot be used in arithmetic operation. For arithmetic operation Gray Code must be change to binary form.

Gray Code to Binary Conversion →

eg. convert 101101101 into  
Binary Conversion

step - 1 Gray code 101101101

First digit remain as it is and  
next 7 bits will be obtained by  
cross XOR operation.

$$\begin{array}{cccccccccc}
 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \\
 & | & | & | & | & | & | & | & | \\
 1 & & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0
 \end{array}$$

So binary no. is 110110110

Binary to Gray Code Conversion →

eg. Convert 11001110 into Gray code.

Binary no. 11001110

step - 1 first bit remain as it is and for  
second bit onwards we have to do

X - OR operations.

110001110

10101001

so Gray code is 10101001

011

↓  
001

## Excess - 3 Code →

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The excess - 3 code is a non-weighted code used to express code decimal numbers. It is a self Complementarily binary coded decimal (BCD) code and numerical system which has biased representation. It is particularly significant for arithmetic operations as it overcomes short coming encountered while using 8421 BCD code to add 2 decimal digits whose sum exceeds 9.

### Representation →

It can be obtained by adding 3 to each decimal digit

### 'Binary to Excess-3 Code Conversion'

Step 1 - Find the decimal equivalent of the given binary no.

Step 2 - Add 3 to each digit of decimal number

Step 3 - Convert the newly obtained decimal no. back to binary no. W

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to get required excess-3 equivalent

e.g. A find the excess 3 of 0100

step-1 Decimal equivalent of 0100  
is 4.

step-2 Add 3 in that

$$\begin{array}{r} 4 \\ + 3 \\ \hline 7 \end{array}$$

step-3 Binary conversion of 7 is 0111

Table - 1 shows the excess - 3 codes  
for decimal digits

Decimal	B CD	excess - 3 code
0	00 00	0011
1	00 01	0100
2	00 10	0101
3	00 11	0110
4	01 00	0111
5	01 01	1000
6	01 10	1001
7	01 11	1010
8	10 00	1011
9	10 01	1100

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eg. Convert 23 to X-3 code

Step - 1 Add 3 in each of the decimal no.

$$\begin{array}{r}
 23 \\
 + 33 \\
 \hline
 56
 \end{array}$$

Step - Convert 56 into ~~BCD~~ BCD  
01010110

eg. Convert 15.46 into excess 3

Step - 1 Add 3 into both digit in the decimal no.

$$\begin{array}{r}
 15 \cdot 46 \\
 + 33 \cdot 33 \\
 \hline
 48 \cdot 79
 \end{array}$$

Step - 2 Convert 48.79 into BCD

0100 1000 · 0111 001

WV

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Excess-3 to BCD and decimal number. →

eg. <sup>excess-3</sup> 1001001 ~~BCD~~ Convert it into BCD & decimal no.

1001001  
make a grouping of 4 bit for each group i.e.

0100 1001  
Now subtract 3(0011) from each four bit group that will be BCD

$$\begin{array}{r} 0100 \ 1001 \\ - 0011 \ 0011 \\ \hline 0001 \ 0110 \end{array}$$

Now convert this 0001 0110 into decimal

$$(0001 \ 0110)_{BCD} = (16)_{10}$$

W

## Excess - 3 Addition →

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1. Take excess-3 code for decimal numbers
2. Add excess-3 codes
3. If carry is there then add 3  
else subtract 3.

e.g. Add 4 & 8

step-1 take excess 3 for 4 is

$$\begin{array}{r} 4 \\ + 3 \\ \hline 7 \end{array} = \del{001}0111$$

for 8 excess-3 code is

$$\begin{array}{r} 8 \\ - 3 \\ \hline 11 \end{array}$$

~~0001 0001~~ 1011

Now

$$\begin{array}{r} 0111 \\ + 1011 \\ \hline 10010 \end{array}$$

there is a carry  $\Rightarrow$  Add 3

$$\begin{array}{r} 0001 0010 \\ 0011 0011 \\ \hline 0100 0101 \end{array}$$

W

CROSS check

$$\begin{array}{r}
 0100 \\
 \downarrow 4 \\
 1
 \end{array}
 \quad
 \begin{array}{r}
 0101 \\
 \downarrow 5 \\
 2
 \end{array}
 \quad
 \rightarrow \text{in excess 3} \\
 \text{in decimal}$$

$$\begin{array}{r}
 4 \\
 + 8 \\
 \hline
 12
 \end{array}$$

Advantages of Excess - 3 Code →

- a) These are unweighted BCD.
- b) These are self Complementary codes.
- c) It is particularly significant for arithmetic operations as it overcomes short coming encountered while using 8421 BCD code to add 2 decimal digits whose sums exceed 9.

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## ASCII CODE →

ASCII stands for American standard code for information interchange. It is the standard code commonly used for the transmission of binary information. Each character is represented by a 7-bit code and usually an eighth bit is inserted for parity. The code consists of 128 characters. Ninety-five characters represent graphic symbols that include upper & lower case letters, numerals 0 to 9, punctuation marks, and special symbols. 33 characters represent format effectors, which are functional characters for controlling the layout of printing or display devices such as carriage return, line feed, horizontal tabulation, and back space. The other 10 characters are used to direct the data communication flow and report its status.

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Some important ASCII codes are given below →

Table - 1

32 - space	42 - *	61 - =
33 - !	43 - +	62 - >
34 - "	44 - ,	63 - ?
35 - #	45 - -	64 - @
36 - \$	46 - .	65-90 - (A-Z) Cap
37 - .	47 - /	91 - [
38 - &	48 - 57 - (0-9)	92 - \
39 - '	58 - ;	93 - ]
40 - (	59 - ;	94 - ^
41 - )	60 - <	95 - _

96 - ' (grave accent)

97 - 122 (a - z) small

123 - {

124 - | (vertical line or strike line)

125 - }

126 - ~

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eg.  $(10010011000011001101)_2$  Convert  
 into ASCII

Step - 1 Convert Binary into decimal  
 then decimal to ASCII

Step - 2 Make a group of 7 bit

$\begin{array}{cccccc} & & & & 64 & 32 & 16 & 8 & 4 & 2 & 1 \\ \hline 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \end{array}$

Step - 3 Convert into decimal  
 ↓              ↓              ↓  
 73            65            77

Convert these decimal into ASCII with the help of Table 1.

I AM

I AM  $\equiv$  ~~1000~~  $(10010011000011001101)$

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