

PERCEPTRON ALGORITHM:

(1)

- ① For each node in the output layer:
 - Calculate the error which can only takes the values 1 and -1
 - If the error is 0, the goal has been achieved. Otherwise, we adjust the weights.
 - Do not alter weights from inactivated input nodes.
 - Decrease the weight if the error was 1, increase ~~it~~ the weight if the error was -1.

⇒ RULES :-

- ① Weight change = some small constant *
(target activation - spontaneous output activation) * input activation.

If we speak of error instead of the "Target activation of minus the spontaneous output activation", then.

Weight change = some small constant * error * input activation.

PERCEPTRON Algorithm in pseudo-code (2)

Start with random initial weights
[e.g: uniform random in $[-0.3, 0.3]$]

Do

{

For all patterns p

{

For all output Nodes j

{

Calculate Activation(j)

~~Error~~

Error $_j$ = Target Value $_j$ for Pattern p -
Activation $_j$

For all input Nodes i To output Node j

{

DeltaWeight = Learning Constant * Error $_j$ *
Activation $_i$

Weight = Weight + DeltaWeight.

}

}

}

}

Until "Error is sufficiently small" or "Time-out"

PERCEPTRON LEARNING RULE

(3)

How do we find the weights using a learning procedure?

- ① Choose initial weights randomly.
- ② Present a randomly chosen pattern x .
- ③ Update weights using Delta rule ∴

$$w_{ij}(t+1) = w_{ij}(t) + \epsilon x_i * x_j$$

where $\epsilon x_i = (\text{target}_i - \text{output}_i)$.

- ④ Repeat step ② and step ③ until the stopping criteria (convergence, maximum no. of iterations) is reached.

Perceptron Convergence Theorem :-

→ If a pattern set can be expanded by a two layer perceptron, then the perceptron learning rule will always be able to find some correct weights.

PERCEPTRON LIMITATION:

A single layer perceptron can only learn LINEARLY SEPARABLE problems.

Boolean AND function is linearly separable, whereas Boolean XOR function (and the parity problem in general) is not.

TRAINING SET:

$$\left\{ p_1 = \begin{bmatrix} -1 \\ 1 \\ -1 \end{bmatrix}, t_1 = [1] \right\} \left\{ p_2 = \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}, t_2 = [0] \right\}$$

Random Initial weights:

$$W = \begin{bmatrix} 0.5 & -1 & -0.5 \end{bmatrix} \quad b = 0.5$$

First Iteration:

$$a = \text{hardlim}(Wp_1 + b) = \text{hardlim} \left(\begin{bmatrix} 0.5 & -1 & -0.5 \end{bmatrix} \begin{bmatrix} -1 \\ 1 \\ -1 \end{bmatrix} + 0.5 \right)$$

$$W^{\text{new}} = W^{\text{old}} + e p^T = \begin{bmatrix} 0.5 & -1 & -0.5 \end{bmatrix} + (1) \begin{bmatrix} -1 & 1 & -1 \end{bmatrix} \\ = \begin{bmatrix} -0.5 & 0 & -1.5 \end{bmatrix}$$

$$b^{\text{new}} = b^{\text{old}} + e = 0.5 + (1) = 1.5$$