

DLO Assignment 2:-

(a)

(a). Actual Expression:-

$$\text{Ans: } Y = (\bar{A} \cdot B) \cdot B \cdot \bar{C}$$

Simplified Expression:- $\rightarrow \bar{A}B\bar{C}$

$$(\bar{A} \cdot B) \cdot B \cdot \bar{C}$$

$$\begin{aligned} & (\bar{A} + \bar{B}) \cdot B \cdot \bar{C} \\ & ((\bar{A} + \bar{B}) \cdot B) \cdot \bar{C} \end{aligned} \quad \left. \begin{array}{l} \Rightarrow (\bar{A}B + \bar{B}B) \cdot \bar{C} \\ \Rightarrow \bar{A}B\bar{C} \end{array} \right.$$

(b). Actual Expression:- $F = (x + \bar{y}) \cdot z + (\bar{x} \cdot y \cdot \bar{z})$

$$\text{Ans: } \text{Simplified Expression:- } z(x + \bar{y}) + \bar{x}y\bar{z}$$

$$\begin{aligned} (x + \bar{y}) \cdot z + (\bar{x} \cdot y \cdot \bar{z}) &= xz + \bar{y}z + (\bar{x}y\bar{z}) \\ &= z(x + \bar{y}) + (\bar{x}y\bar{z}) \end{aligned}$$

(c). Actual Expression:- $Z = (B + \bar{C}) \cdot A + (C + \bar{D}) \cdot B + (D \cdot B)$

$$\text{Ans: } \text{Simplified Expression:- } \rightarrow B + A\bar{C}$$

$$\begin{aligned} & A(B + \bar{C}) + B(C + \bar{D}) + (D \cdot B) \\ & AB + A\bar{C} + BC + B\bar{D} + DB \\ & AB + A\bar{C} + BC + B(\bar{D} + D) \end{aligned} \quad \left. \begin{array}{l} \rightarrow AB + A\bar{C} + BC + B \\ \rightarrow AB + A\bar{C} + B(c+1) \\ \rightarrow AB + B + A\bar{C} \\ \rightarrow B(A+1) + A\bar{C} \end{array} \right. \rightarrow [B + A\bar{C}]$$

(d). Actual Expression:- $Y = \overline{\bar{A} \cdot (B \cdot (\bar{B} \cdot C))} + \left((B \cdot (\bar{B} \cdot C)) \oplus (\bar{B}C) \right) \rightarrow \overline{\bar{A} \cdot B(\bar{B}C)} + \left((B \cdot (\bar{B}C)) \oplus BC \right)$

$$\text{Ans: } \text{Simplified Expression:- } 2$$

$$\begin{aligned} & A + \overline{B + (B \cdot C)} + (B \cdot (\bar{B} + \bar{C})) \oplus BC \\ & A + \underbrace{(\bar{B} + B)}_2 \cdot (\bar{B} + C) + \underbrace{B \cdot \bar{B}}_0 + B\bar{C} \oplus BC \\ & A + \bar{B} + C + B\bar{C} \oplus BC \quad \left. \begin{array}{l} \rightarrow A + \bar{B} + C + B \\ \rightarrow A + C \end{array} \right. \rightarrow (1) \\ & A + \bar{B} + C + B(\bar{C} \oplus C) \end{aligned}$$

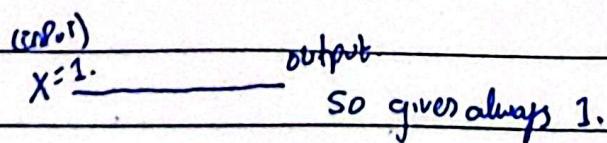
Q2).

$$\begin{aligned}
 \text{Ans:-} \quad & \bar{A}BC + A\bar{B}C + \overline{ABC} + A\bar{B}C + ABC \\
 = & \bar{A}BC + A(\bar{B} + \bar{C}) + \bar{A} + \bar{B} + \bar{C} + A\bar{B}C + ABC \\
 = & (\bar{A} + 1)BC + A\bar{B} + A\bar{C} + \bar{A} + \bar{B} + \bar{C} + A\bar{B}C + \\
 = & (BC + \bar{C}) + A\bar{B} + A\bar{C} + \bar{A} + \bar{B} + A\bar{B}C \\
 = & (B + \bar{C})(C + \bar{C}) + A\bar{B} + \bar{B} + A\bar{C} + \bar{A} + A\bar{B}C \\
 = & (B + \bar{C}) + \bar{B}(A + 1) + A\bar{C} + \bar{A} + A\bar{B}C \\
 = & (B + \bar{C}) + \bar{B} + A\bar{B}C + A\bar{C} + \bar{A} \\
 = & (B + \bar{C}) + \bar{B} + A\bar{B}C + A\bar{C} + \bar{A} \\
 = & 1 + \bar{C}(1 + A) + A\bar{B}C + \bar{A} \\
 = & 1 + A\bar{B}C + \bar{A} = (1 + \bar{A}) + A\bar{B}C \rightarrow 1 + A\bar{B}C = 1
 \end{aligned}$$

Truth Table:-

A	B	C	Output.
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

Logic Circuit:-



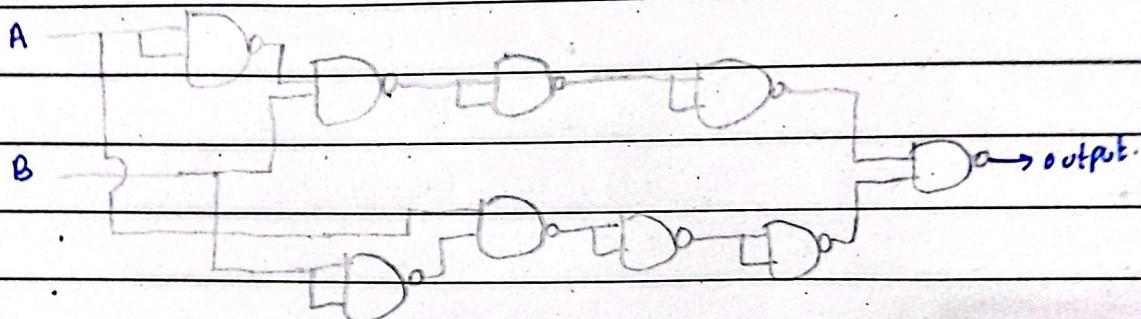
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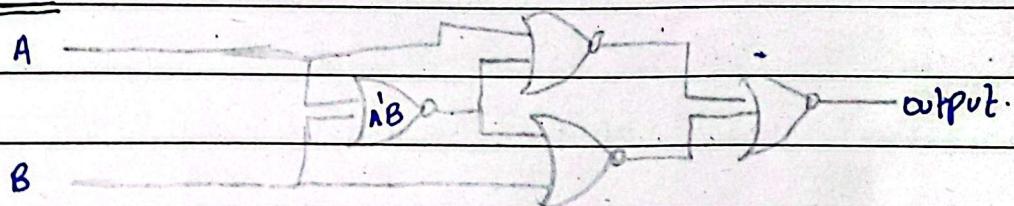
Q3).

(i). $A'B + B'A$

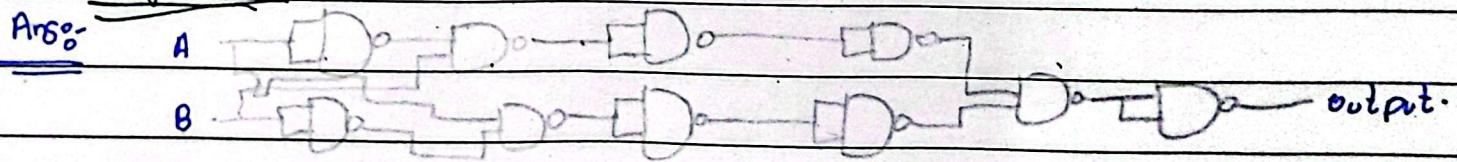
Ans:- Using Nand:-



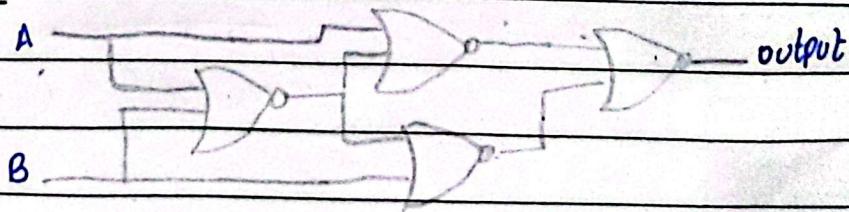
using NOR :-



(ii). Using Nand:- $A'B' + AB$



Using NOR :-



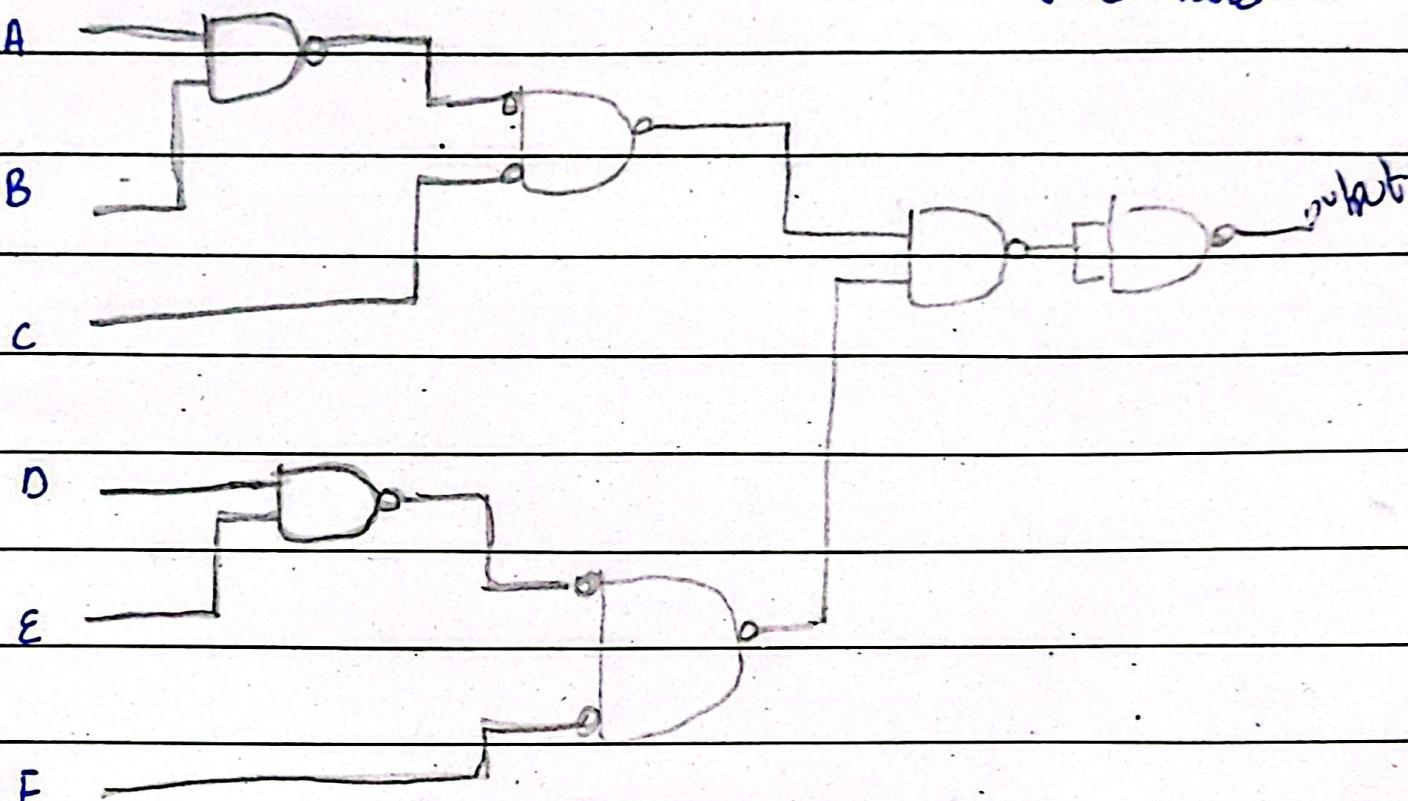
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(Q4).

(i) $(AB + C') \cdot (DE + F')$

"As Negative-OR is Nand so we can implement
As Nand-Nand too."

Ans:-

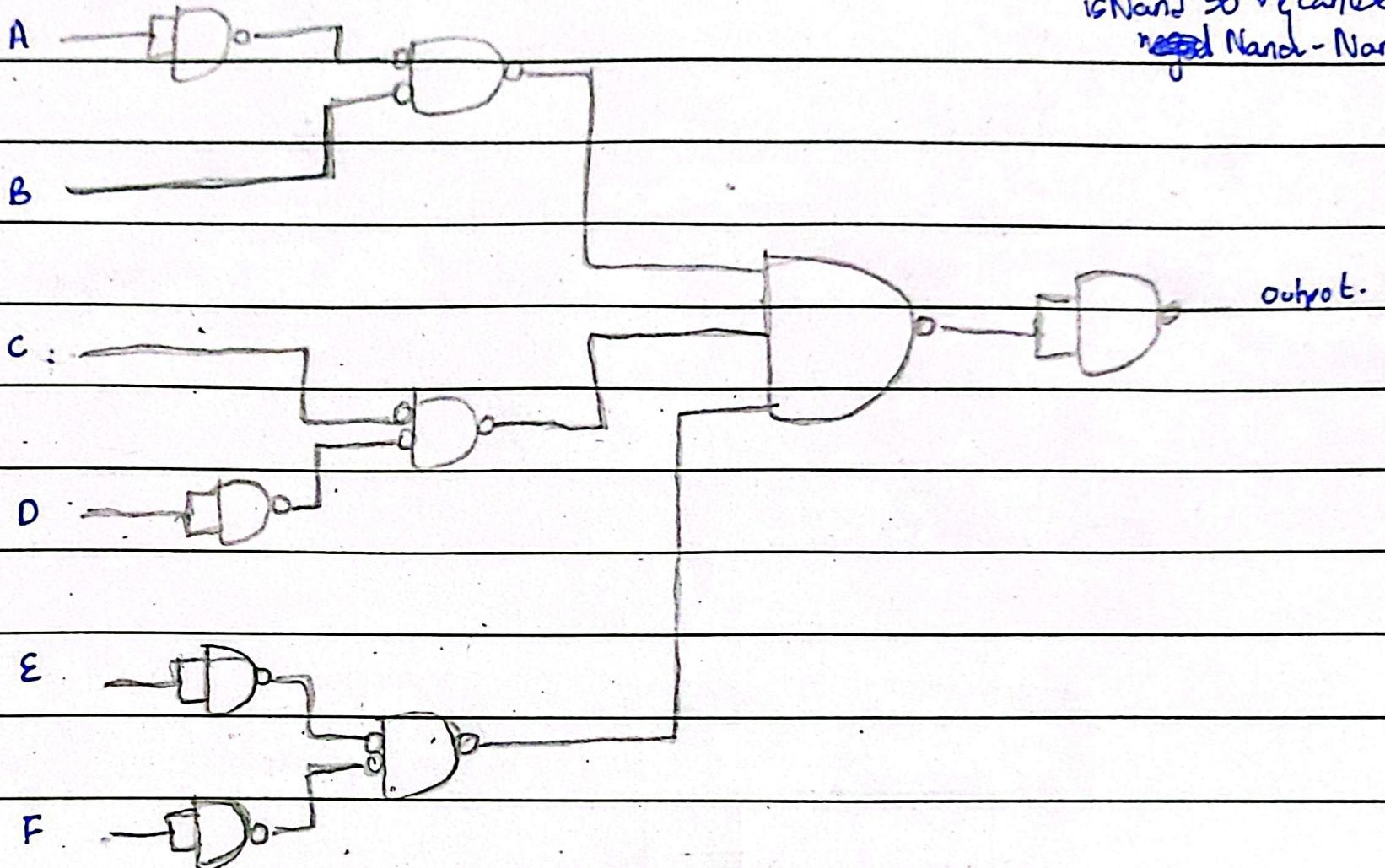


Q4)(ii).

Ans:- $(A' + B) \cdot (C + D') \cdot (E + F)$

"Negative-OR"

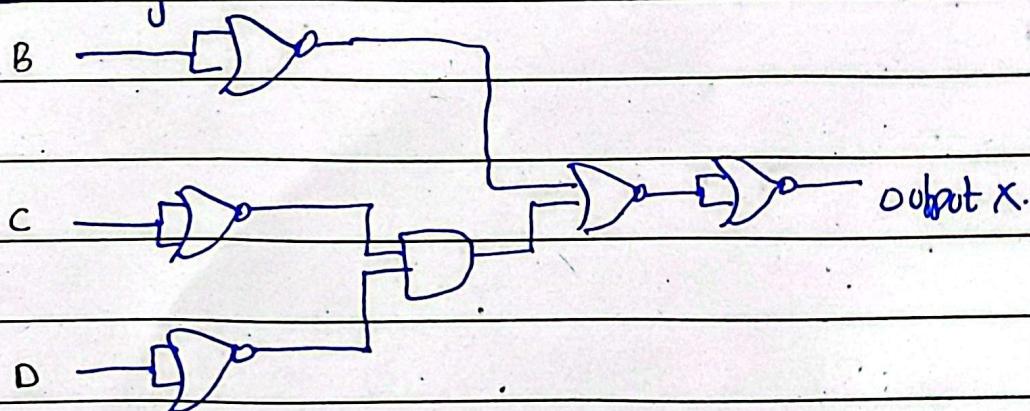
is Nand so we can use
"Nand-Nand too"



$$Q5) (a). \quad F(A, B, C, D) = \Sigma(0, 1, 2, 8, 9, 12) ; \quad J(A, B, C, D) = \Sigma(3, 4, 10, 11).$$

Ans:-

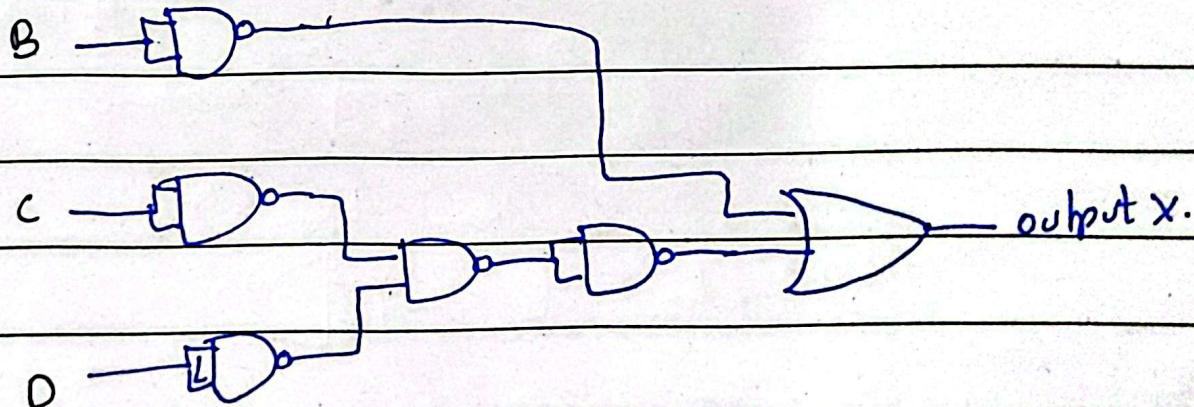
		AB					
		00	01	11	10		
CD	00	1	x	1	1	→(i). (i) + (ii)	
	01	1	0	0	1	= (\bar{C}\bar{D}) + (\bar{B})	
	11	x	0	0	x	SOP = \bar{B} + \bar{C}\bar{D}	
	10	1	0	0	x	→(ii)	

AND-OR :- using SOP. $(\bar{B} + \bar{C}\bar{D})$ 

(b).

Ans:- OR-NAND :-

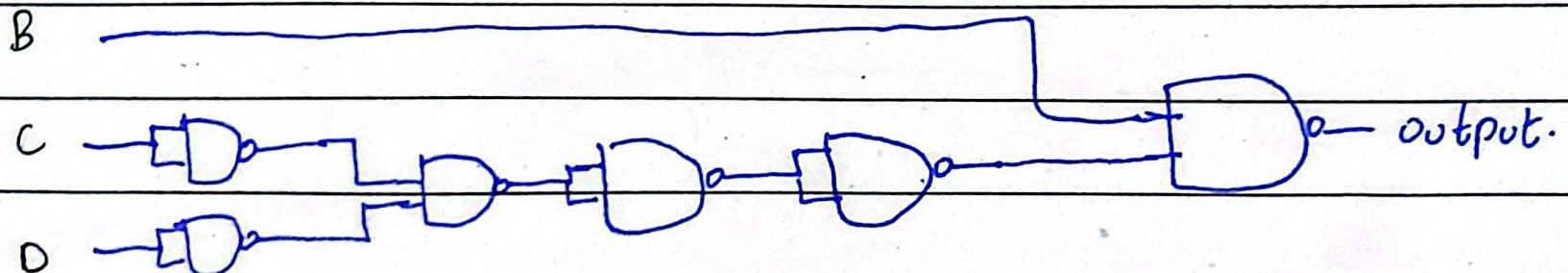
$$\text{using SOP} \rightarrow \bar{B} + \bar{C}\bar{D}$$



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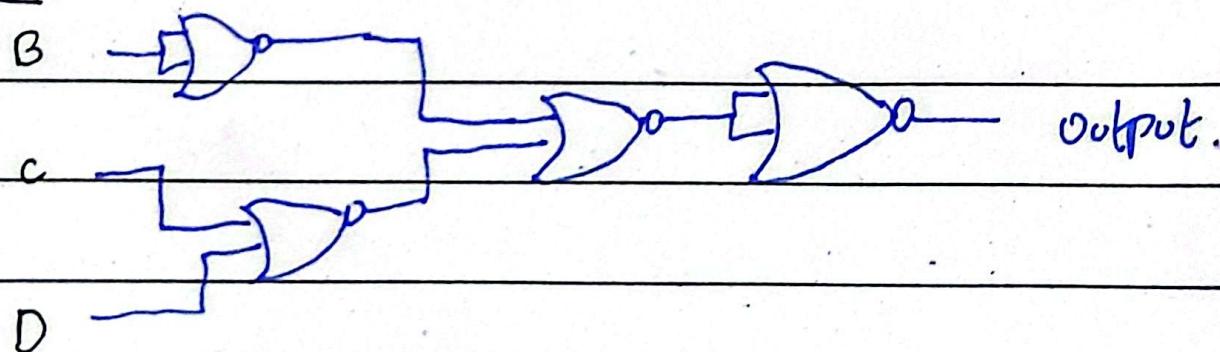
(c) Nand-Nand :-

Ans:-



(d) NOR-NOR :- $SOP \rightarrow (\bar{B} + \bar{C}\bar{D}) \rightarrow \bar{B} + (\bar{C} + \bar{D})$

Ans:-



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(Q6).

Ans - 1 2 3 (Output)

A B C X

0 0 0 1

so Boolean Expression = $\bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C}$

0 0 1 1

0 1 0 1

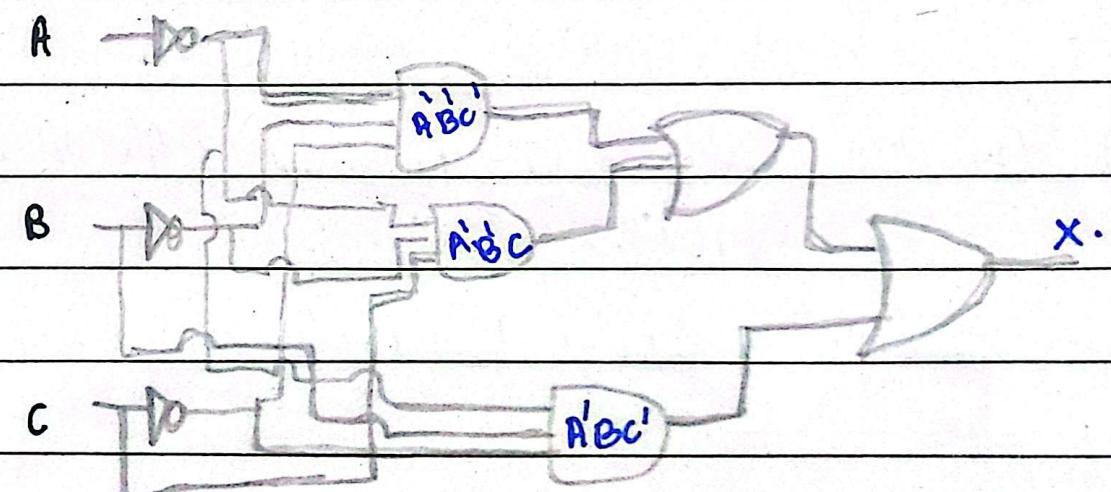
0 1 1 0

1 0 0 0

1 0 1 0

1 1 0 0

1 1 1 0



(Q7)

$$(i). (\bar{A} + \bar{B} + C + D) \cdot (A + \bar{B} + C + D) \cdot (A + B + \bar{C} + \bar{D}) \cdot (A + B + C + \bar{D}) \cdot (\bar{A} + B + C + \bar{D}) \cdot (A + B + \bar{C} + D)$$

Ans:-

		AB			
		00	01	11	10
CD		00	(0)	(0)	(i)
01	0	0	0	(0 → (ii))	(i). (ii). (iii)
11	0	0			$\min = (\bar{B} + C + D) \cdot (B + C + \bar{D}) \cdot (A + B + \bar{C})$.
10	0				SOP expression
				↓ (iii)	

(ii).

Ans:-

standard SOP form = $\bar{A}\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + AB\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + ABC\bar{D} + A\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D}$
 $+ ABC\bar{D} + A\bar{B}C\bar{D}$

(iii).

Ans:-

		AB				
		00	01	11	10	
CD		00	1	0	0	(1 → (i)).
01	0	1	1	0	(ii)	
11	0	1	1	1		$\min = (i) + (ii) + (iii) + (iv)$.
10	0	1	1	1		SOP
				↓ (iii)	↓ (iv)..	$\text{minimum} = \bar{B}\bar{C}\bar{D} + BD + BC + AC$

SOP expression

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Q8). (a).

AB

Ans:-

	00	01	11	10
00	0	0	1	1
01	1	1	0	1

$$\text{MINIMUM POS} = (A+C) \cdot (\bar{A} + \bar{B} + \bar{C})$$

8).

(b) \rightarrow As Y missing

Ans:- $(x + \bar{y})(\bar{x} + z)(x + \bar{y} + \bar{z})(\bar{x} + \bar{y} + z)$

As Z missing

$$(x + \bar{y} + (z \cdot \bar{z})) (\bar{x} + (y \cdot \bar{y}) + z) (x + \bar{y} + \bar{z}) (\bar{x} + \bar{y} + 2)$$

$$((A + (z \cdot \bar{z})) (\bar{x} + z + (y \cdot \bar{y})) (x + \bar{y} + \bar{z}) (\bar{x} + \bar{y} + z)) .$$

$$((A + z) \cdot (A + \bar{z})) \cdot ((B + (y \cdot \bar{y})) (x + \bar{y} + \bar{z}) (\bar{x} + \bar{y} + z)) .$$

$$(x + \bar{y} + 2) \cdot (x + \bar{y} + \bar{z}) \cdot (B + y) \cdot (B + \bar{y}) (x + \bar{y} + \bar{z}) (\bar{x} + \bar{y} + z) .$$

$$(x + \bar{y} + \bar{z}) \cdot (x + \bar{y} + 2) \cdot (x + y + z) \cdot (\bar{x} + \bar{y} + 2) (x + \bar{y} + \bar{z}) (\bar{x} + \bar{y} + z) .$$

↑
same ↑
same ↑
same

$$(x + \bar{y} + 2) \cdot (x + \bar{y} + \bar{z}) \cdot (\bar{x} + y + z) \cdot (\bar{x} + \bar{y} + z)$$

						I	II
00	01	11	Y	10			
0	1	0	0	0	^(I)	so Minimum Pos = (x + y)	$(\bar{x} + z) \cdot (x + \bar{y})$

\hookrightarrow (II)

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Q9)

(A). $(A + \bar{B}) \cdot (A + \bar{C}) \cdot (\bar{A} + \bar{B} + C)$.

Ans:- $(A + \bar{B} + C \cdot \bar{C}) \cdot (A + B\bar{B} + \bar{C}) \cdot (\bar{A} + \bar{B} + C)$.

$$\begin{aligned} & (A + \bar{B} + C) \cdot (A + \bar{B} + \bar{C}) \cdot (A + B + \bar{C}) \cdot (A + \bar{B} + \bar{C}) \cdot (\bar{A} + \bar{B} + C) \\ = & (A + \bar{B} + C) \cdot (A + \bar{B} + \bar{C}) \cdot (A + B + \bar{C}) \cdot (\bar{A} + \bar{B} + C) \end{aligned}$$

		AB					
		00	01	11	10		
C	0	1	0	0	0	(i) \rightarrow (ii)	
	1	0	0	1	1	(i) \rightarrow (ii)	

Min = $AC + \bar{B}\bar{C}$

SOP

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Q9)

(b). $(A + B + C\bar{C} + D\bar{D}) \cdot (\bar{A} + \bar{B} + \bar{C} + D \cdot \bar{D}) \cdot (A \cdot \bar{A} + B + \bar{C} + D) \cdot (A + \bar{B} + C + D)$.

standard
POS = $(\bar{A} + B + C + D) \cdot (\bar{A} + B + C + \bar{D}) \cdot (\bar{A} + B + \bar{C} + D) \cdot (\bar{A} + B + \bar{C} + \bar{D}) \cdot (\bar{A} + \bar{B} + \bar{C} + D) \cdot (A + B + \bar{C} + D) \cdot (A + \bar{B} + C + \bar{D})$.

Ans:-

		AB			
		00	01	11	10
		(i)			
CD	00	1	1	1	0
	01	1	0	1	0
	11	1	1	0	0
	10	0	1	0	0

(i) + (ii) + (iii) + (iv)

$m_{11} = AB\bar{C} + \bar{A}BC + \bar{A}\bar{C}\bar{D} + \bar{A}\bar{B}D$

SOP

(iii) Page Victory

Q10). (a).

Ans- $F(A, B, C, D) = \Sigma(0, 6, 8, 13, 14), \quad d(A, B, C, D) = \Sigma(2, 4, 10) \quad (\text{SOP})$

(POS)- $F(A, B, C, D) = \prod(1, 2, 3, 4, 7, 9, 10, 11, 12, 15), \quad d(A, B, C, D) = \prod(0, 1, 3, 5, 6, 7, 8, 9, 11, 12, 13, 14, 15)$

For SOP:-

		AB					
		00	01	11	10		
		00	1	X	0		
		CD	01	0	0		
		;	11	0	0		
		10	X	1	1		
		↑ (iii)		SOP			
			I + II + III				
			Simplify= $(\bar{A}\bar{C}\bar{D}) + (\bar{B}\bar{C}\bar{D}) + (C\bar{D}) + (\bar{A}\bar{B}\bar{C}D)$.				

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Q10)

(a). FOR Pos^o

	00	01	11	
00	1	X	O	1
01	O	O	1	$(O \rightarrow \text{ii})$
11	O	O	O	$\rightarrow \text{(i)}$
10	X	1	1	X

AB

(iv)

$$(\text{i}) \cdot (\text{ii}) \cdot (\text{iii}) \cdot (\text{iv})$$

$$(\bar{C} + \bar{D}) \cdot (B + \bar{D}) \cdot (\bar{B} + C + D) \cdot (A + \bar{D})$$

(Q10)

(B).

Ans:- $F(A, B, C, D) = \Sigma(1, 3, 5, 7, 9, 15); D(A, B, C, D) = \Sigma(4, 6, 12, 13)$

For SOP :-

		AB				
		00	01	11	10	(iv)
CD	00	0	X	X	0	$(i) + (ii) + (iii) + (iv) + (v)$.
	01	1	1	X	1	$\rightarrow (i)$ Simplified = $A'D + C'D + A'B + BC' + BD$.
11	1	1	1	0	(v).	SOP
	10	0	X	0	0	
		11				

For POS :-

For POS :-

		AB				
		00	01	11	10	
CD	00	0	X	X	0	$(i) \cdot (ii) \cdot (iii)$
	01	1	1	X	1	$\text{Minimized} = (D) \cdot (\bar{A} + B + C) \cdot (\bar{A} + \bar{B} + C)$
11	1	1	1	1	0	$\rightarrow (i)$ POS
	10	0	X	0	0	(i)