

**NEW YORK INSTITUTE OF TECHNOLOGY**  
**College of Engineering and Computing Sciences**  
**DTSC 620 (Fall 2022)**  
**Classification with Bayes' Classification Rule**

Table 1 gives the joint distribution between two binary-valued features and three classes  $\{U_1, U_2, U_3\}$ .

$f_1$	$f_2$	$U$	$P(f_1, f_2, U)$
1	0	$U_1$	0.1
0	0	$U_1$	0.1
0	1	$U_1$	0.1
1	1	$U_1$	0.1
1	0	$U_2$	0.1
0	0	$U_2$	0.05
0	1	$U_2$	0.05
1	1	$U_2$	0.05
1	0	$U_3$	0.1
0	0	$U_3$	0.2
0	1	$U_3$	0.05
1	1	$U_3$	0.0

**Table 1.**

- (a) Given a test feature vector  $\langle f_1 = 0, f_2 = 0 \rangle$ , use Bayes classification rule and the information provided in **Table 1**, to find the class to which this vector belongs.

$$\langle f_1 = 0, f_2 = 0 \rangle \Rightarrow U_3$$

$$P(f_1 = 0, f_2 = 0, U = U_1) = 0.1$$

$$P(f_1 = 0, f_2 = 0, U = U_2) = 0.05$$

$$P(f_1 = 0, f_2 = 0, U = U_3) = 0.2$$

- (b) Given the test feature  $f'_1 = 0$ , use Bayes classification rule and the information provided in **Table 1**, to find the class to which this vector belongs.

$$f'_1 = 0 \Rightarrow U3$$

$$P(f'_1 = 0, U = U1) \Rightarrow 0.1 + 0.1 \Rightarrow 0.2$$

$$P(f'_1 = 0, U = U2) \Rightarrow 0.05 + 0.05 \Rightarrow 0.1$$

$$P(f'_1 = 0, U = U3) \Rightarrow 0.2 + 0.05 \Rightarrow 0.25$$