Homework 1

Problem 1-4

Question: Equations of motion of a simple point mass moving along a straight line are given by Mx"=FMx"=F with measurement of position only. Express the equation in state space form as x=Ax+Bux=Ax+Bu and y=Cxy=Cx.

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clc
close all
clear all
addpath Screws
addpath fcn support
syms m X0 dX0 ddX0 x10 x20 x30 dx10 dx20 dx30
X = sym('x', [3 1]); % 3 dimension position vector
d_X = sym('dx', [3 1]); % velocity vector
V = get vel(X, X, d X);
KE = 1/2*m*V'*V;
[D,C,G] = get mat(KE, 0, X,d X);
D = simplify(D);
C = simplify(C);
G = simplify(G);
Z = [X(1); X(2); X(3); d X(1); d X(2); d X(3)]; %vector in state-space
ddX0 = [0; 0; 0];
X0 = [x10; x20; x30; dx10; dx20; dx30];
F = sym('f', [3 1]);
[A lin,B lin] = linearize DCG(D,C,G,Z,F,X0,ddX0);
A lin = simplify(A lin)
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B_lin = simplify(B_lin)
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B_{lin} =
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$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ \frac{1}{m} & 0 & 0 \\ 0 & \frac{1}{m} & 0 \\ 0 & 0 & \frac{1}{m} \end{pmatrix}$$

So in state space we have:

$$Y = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix} Z$$