

UNIVERSITÀ DEGLI STUDI DI NAPOLI FEDERICO II  
SOFTWARE ENGINEERING – LECTURE 13

# Models and Theories in Human-Computer Interaction

Prof. Luigi Libero Lucio Starace

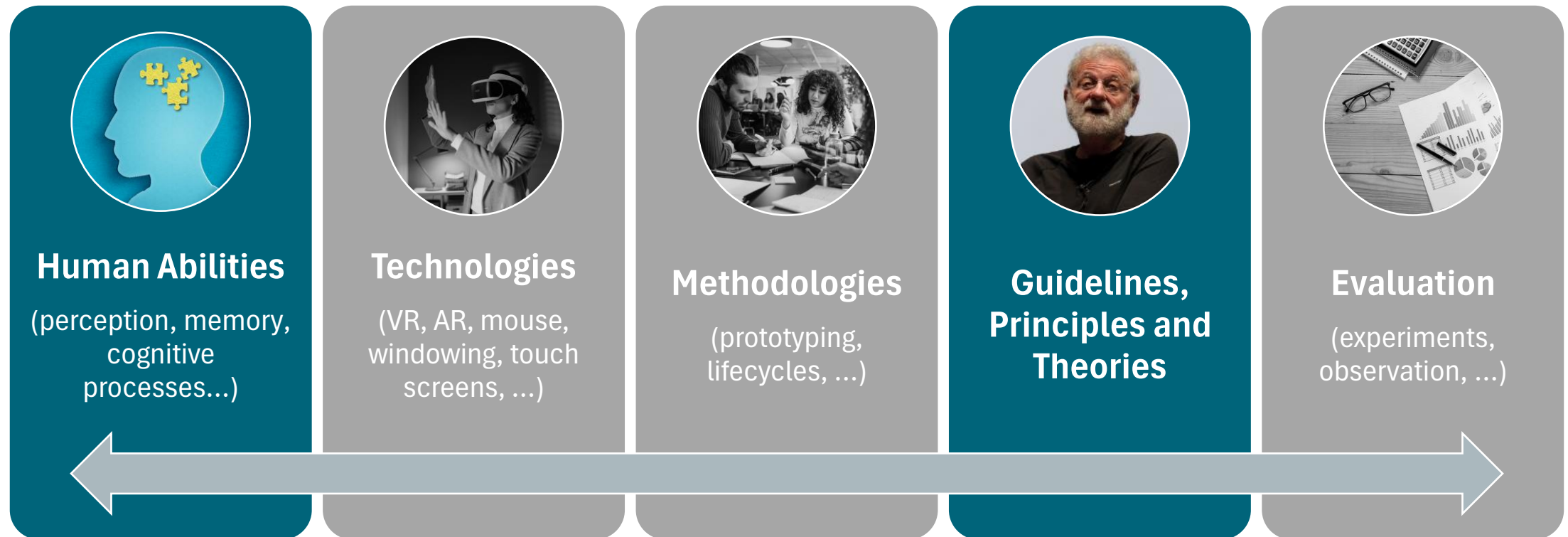
[luigiliberolucio.starace@unina.it](mailto:luigiliberolucio.starace@unina.it)

<https://luistar.github.io>

<https://www.docenti.unina.it/luigiliberolucio.starace>

# Today, on Software Engineering

**Usability Edition**



# What's a model?

A **model** is a simplification (abstraction) of reality

- A perfect mapping of reality is not a model (and not useful!)
  - Precision vs generality
- «*All models are wrong, but some are useful*»

Models allow us to:

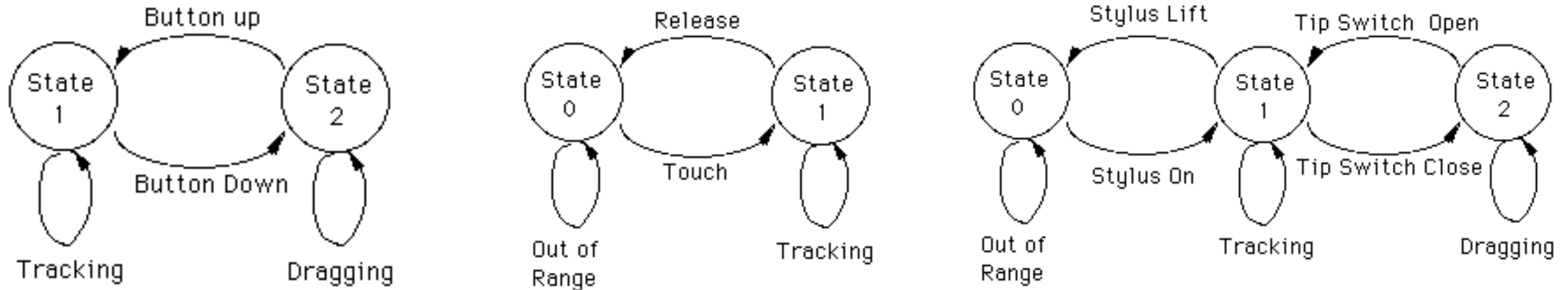
- **Represent** and **reason** about (aspects of) phenomena of interest
- Anticipate (**predict**) outcomes

# HCI models and theories

- In HCI, models and theories aim at explaining how humans interact with computers
- HCI models and theories can be classified as:
  - **Descriptive:** aim at developing a consistent terminology and useful taxonomies
  - **Explanatory:** describe sequence of events, possibly with causal relationship
    - E.g.: Norman's seven stages of action
  - **Predictive:** Aim at enabling the comparison of design alternatives based on numeric predictions of speed or errors
  - **Prescriptive:** Offer guidelines for designers to make decisions

# The three-state model of graphical input

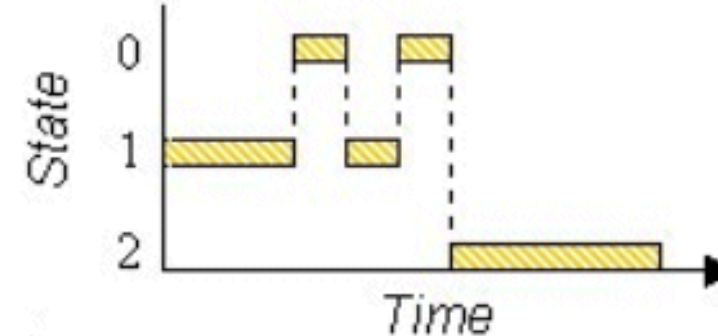
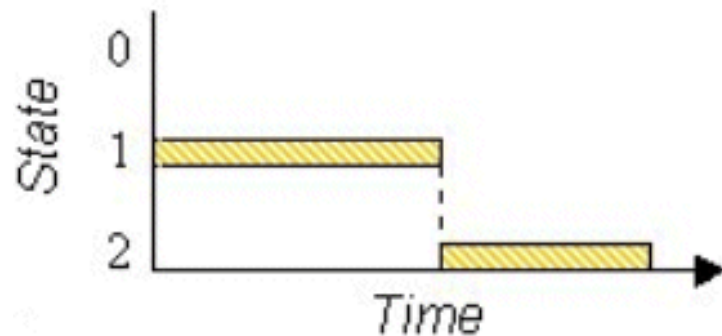
- Proposed by Will Buxton in 1990 [1]
- Describes graphical input with pointing devices
- Different technologies (mouse, trackpads, tablets with stylus, etc...)



[1] Buxton, W. (1990). A Three-State Model of Graphical Input. In INTERACT '90.

# The three-state model of graphical input

- Dragging tasks with a mouse (left) and with a lift-and-tap touchpad (right) (after [1])



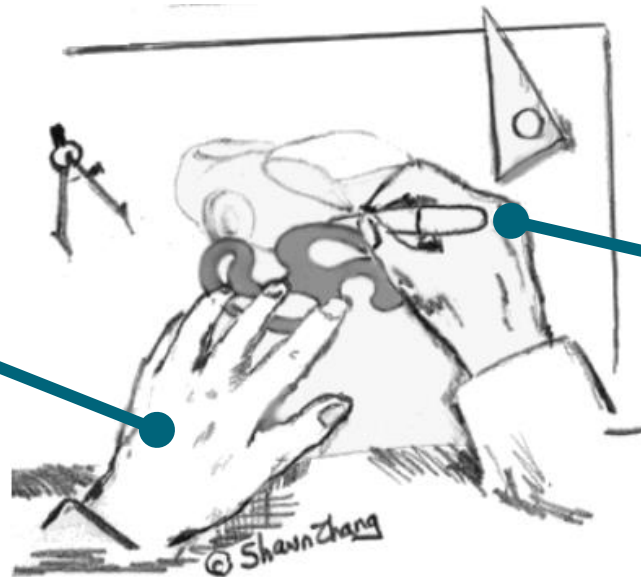
[1] MacKenzie, I. S., & Oniszczak, A. (1997). The tactile touchpad. *CHI '97 Conference on Human Factors in Computing Systems*

# Guiard's model of bimanual skill

- Many interactions are **asymmetric** w.r.t. left/right hand
- Guiard's model describes roles and actions of preferred/non-preferred hands

## Non-preferred

- Leads the preferred hand
- Sets the spatial frame of reference for the preferred hand
- Performs coarse movements



## Preferred

- Follows the non-preferred hand
- Works within established frame of reference set by the non-preferred hand
- Performs fine movements

Two-handed interaction paradigm.  
(Sketch by Shawn Zhang)

# Guiard's model of bimanual skill

- The artist acquires the template with her left hand (*non-preferred hand leads*).
- The template is manipulated over the workspace (*coarse movement, sets the frame of reference*).
- The stylus is acquired in the right hand (*preferred hand follows*) and brought into the vicinity of the template (*works within frame of reference set by the non-preferred hand*).
- Sketching takes place (*preferred hand makes precise movements*).



Two-handed interaction.  
(Sketch by Shawn Zhang)

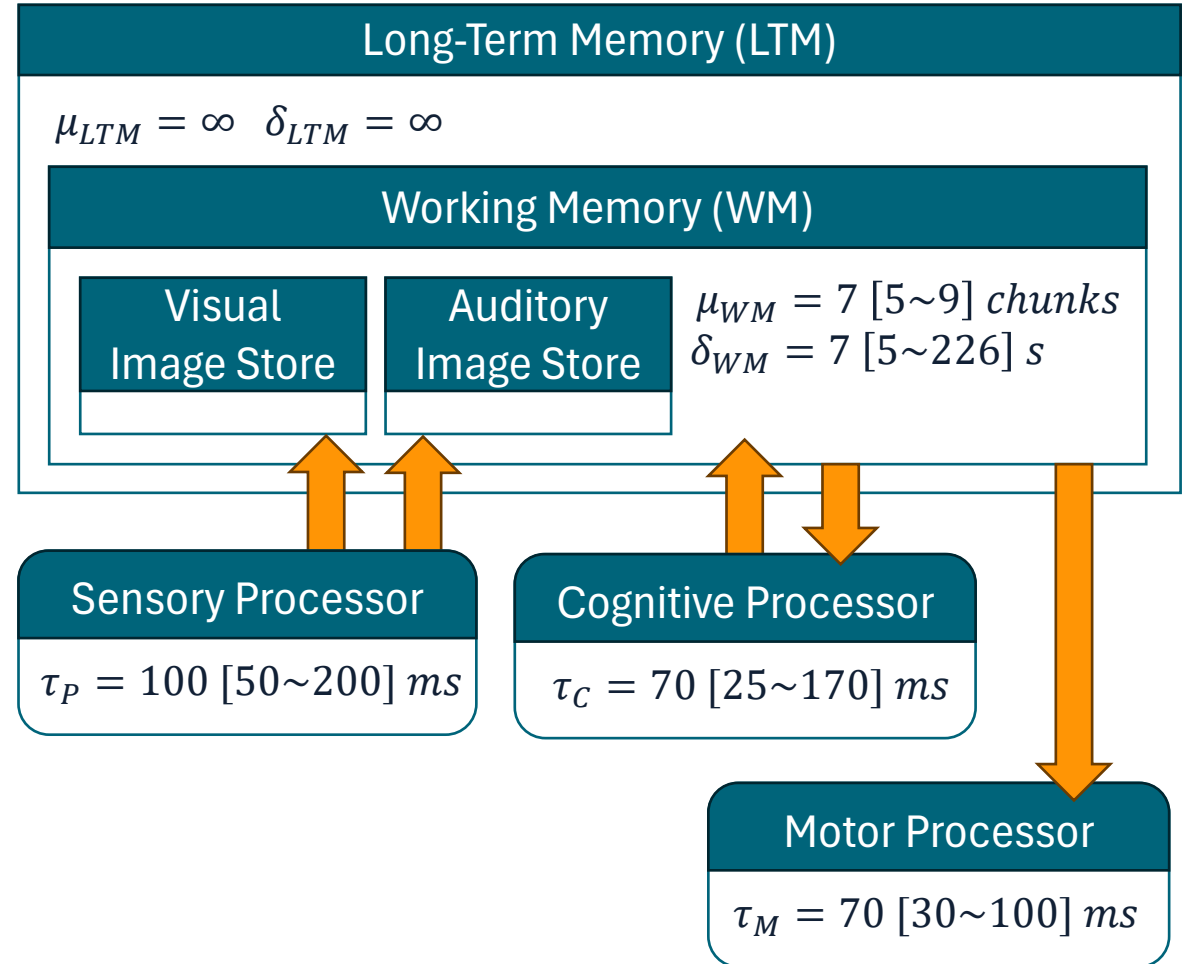


# The Model Human Processor (MHP)

- Developed by Card, Moran and Newell in 1983
- It's a **predictive**, a-priori model
  - Can give approximations of user actions before real users are involved in the testing process (and before the UI is even implemented!)
- A human is modelled by a set of memories and processors that function according to a set of principles
- **Discrete** and **sequential** model

# The Model Human Processor

- Perceptual, Cognitive and Motor processors
- Different types of memories
- Model parameters:
  - Processor cycle times:  $\tau$
  - Memory decay time:  $\delta$
  - Memory capacity:  $\mu$



# MPH: Memories

- **Working Memory (WM)** is a subset of «activated» elements (chunks) from the **Long-Term Memory (LTM)**
  - Chunks can be composed of smaller units like letters in a word
  - A chunk might also consist of several words, as in a well-known phrase
- $\mu_{LTM} = \infty$  and  $\delta_{LTM} = \infty$
- $\mu_{WM} = 7 [5\sim9] \text{ chunks}$
- $\delta_{WM} = 7 [5\sim226] s$ 
  - Decay time for WM largely varies based on the number of stored chunks
  - $\delta_{WM}(1 \text{ chunk}) = 73 [73\sim226]s$
  - $\delta_{WM}(3 \text{ chunks}) = 7 [5\sim34]s$

# Perception of congruent and incongruent stimuli

- Perception times are also influenced by the nature of stimuli
- For example, there is a significant delay in reaction time (**Stroop effect**) between congruent and incongruent stimuli.
- Let's do an experiment!
  - Volunteer needed
  - There will be three columns of words
  - You have to say the COLOR of each words
  - Say «done» when finished

# MHP: Why?

- You can see an interaction as a «program» for the MHP
- You can then «run» it on the MPH to estimate completion time!
  - Humans differ from each other. MPH allows to tune parameters (e.g.: processor cycle times) to target humans with different abilities

# MHP: Example application

- Suppose we are designing the main menu for a command-line utility with 16 different features
- Which alternative would be better?
  - 1x16 (breadth) or 4x4 (nested) menu?

```
*** MAIN MENU ***  
  
A. Feature A  
B. Feature B  
C. Feature C  
...  
O. Feature O  
P. Feature P  
  
Insert your choice>
```

```
*** MAIN MENU ***  
  
A. Submenu A  
B. Submenu B  
C. Submenu C  
D. Submenu D  
  
Insert your choice>
```

```
*** MAIN MENU ***  
  
A. Feature A  
B. Feature B  
C. Feature C  
D. Feature D  
  
Insert your choice>
```

```
*** MAIN MENU ***  
  
E. Feature E  
F. Feature F  
G. Feature G  
H. Feature H  
  
Insert your choice>
```

# MHP Example: Breadth (1x16) Menu

```
foreach item in menu:  
    Execute eye movement to item  
    Perceive item text, transfer to WM  
    Retrieve meaning of item, transfer to WM  
    Match code from displayed to needed item  
    if(Decide on match)  
        break
```

```
Execute eye movement to menu item letter  
Perceive menu item letter, transfer to WM  
Decide on key  
Press key in response
```

Average number of iterations  
in a serial search on 16 items

$\tau_M$   
 $\tau_P$   
 $\tau_C$   
 $\tau_C$   
 $\tau_C$

$(\tau_M + \tau_P + 3\tau_C) \cdot (16 + 1)/2$

$\tau_M$   
 $\tau_P$   
 $\tau_C$   
 $\tau_M$

$2\tau_M + \tau_P + \tau_C$

$$T = (\tau_M + \tau_P + 3\tau_C) \cdot (16 + 1)/2 + 2\tau_M + \tau_P + \tau_C$$
$$= (70 + 100 + 3 \cdot 70) \cdot 8,5 + 2 \cdot 70 + 100 + 70 = \mathbf{3540\ ms}$$

# MHP Example: Depth (4x4) Menu

- Same procedure and steps as the depth menu
- But this time we do 2 serial searches over 4 items

$$\begin{aligned} T &= 2 \cdot [(\tau_M + \tau_P + 3\tau_C) \cdot (4 + 1)/2 + 2\tau_M + \tau_P + \tau_C] \\ &= 2 \cdot [(70 + 100 + 3 \cdot 70) \cdot 2,5 + 2 \cdot 70 + 100 + 70] = \mathbf{2520\ ms} \end{aligned}$$

- The 4x4 menu is predicted to be ~30% faster than the 1x16 one!



# GOMS Model

- **G**oals, **O**perators, **M**ethods, **S**election rules
- Assumptions:
  - Interaction with a system is problem solving
  - Decompose interaction into subproblems
  - Determine goals to «attack» problem
  - Specify sequence of operations used to achieve goals
  - Timing values can be assigned to each operation

# GOMS

- **Goals:**

- What the user wants to achieve (e.g., “start the correct utility function”).

- **Methods:**

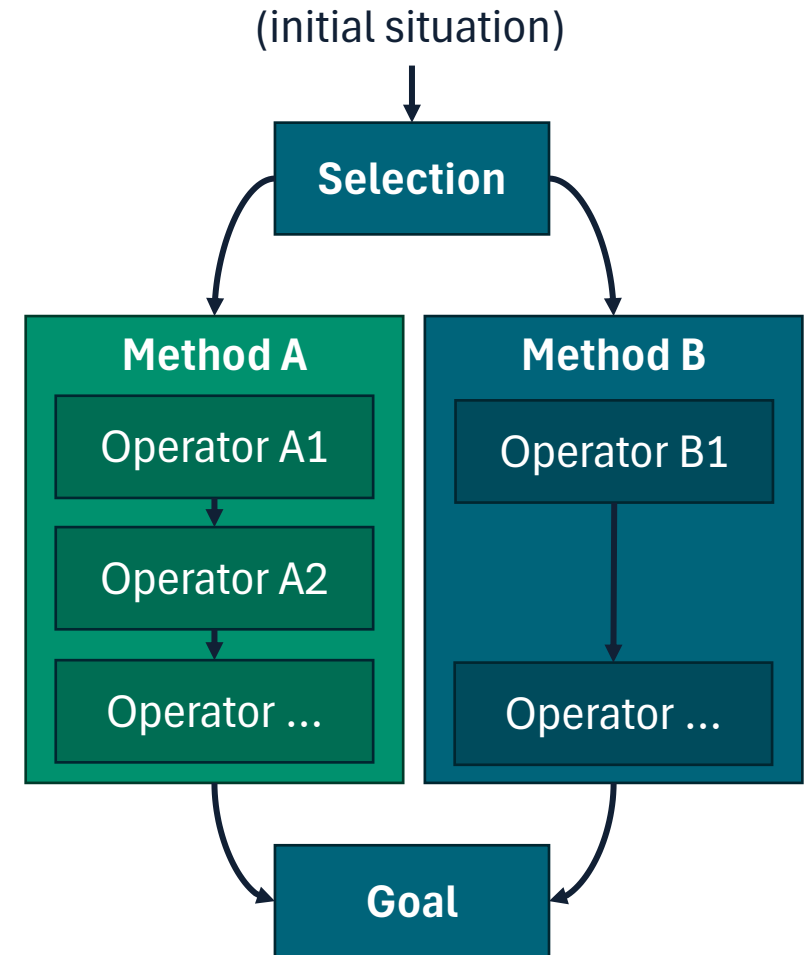
- Possibly alternative sequences of operators used to achieve the goal.

- **Selection rules:**

- Criteria for choosing among different methods.

- **Operators:**

- Basic actions performed by the user (e.g., “move mouse”, “click”, “check setting”).



# GOMS: Example

- **Goal:** delete a word in a document editor
- **Selection rule:** if cursor is at end of word to delete, use Method A, else use Method B
- **Method A:**
  - Press «backspace» key.
  - Check if word is deleted and return to previous operation if needed.
- **Method B:**
  - Move mouse cursor on word.
  - Perform double-click.
  - Press «backspace» key.

# Keyboard Level Model (KLM)

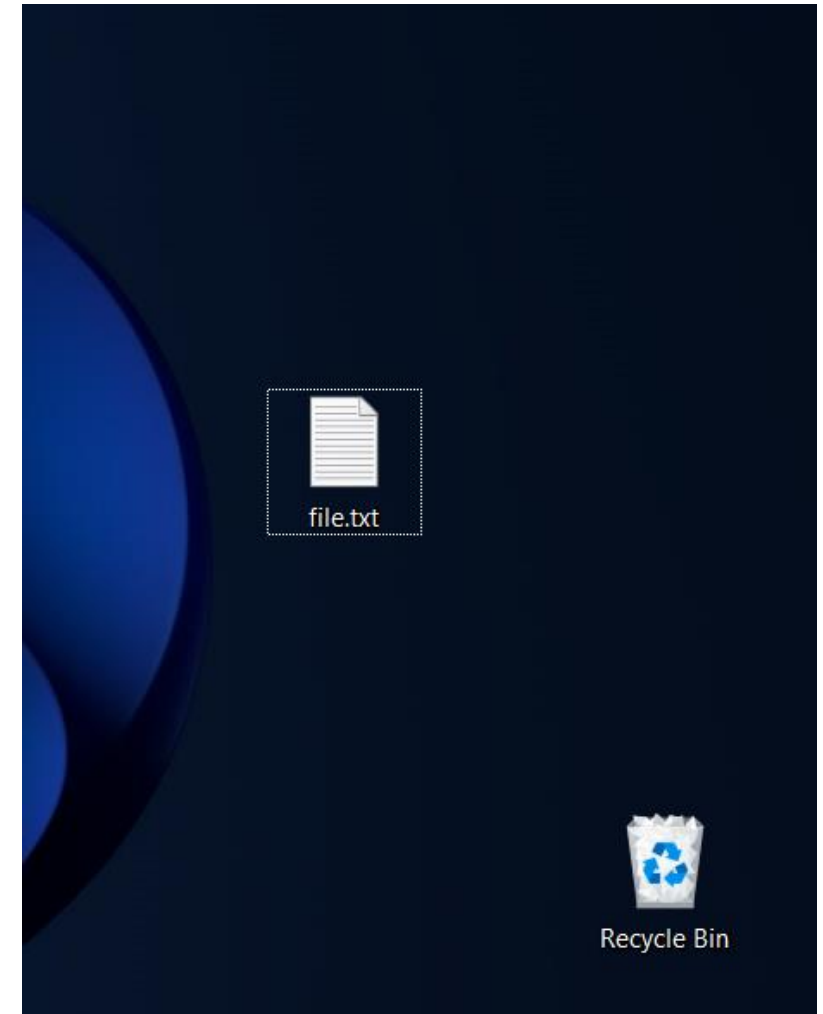
- KLM is one of the simplest GOMS variants
- Focuses on observable behaviour
  - Keystrokes, mouse movements, ...
- Assumes error-free performance
- Common operators and the typical corresponding times:
  - **K (Keystroke)**: 0.2 seconds (200 ms)
  - **P (Pointing with Mouse)**: 1.1 seconds (1100 ms)
  - **B (Pressing/holding/releasing mouse button)**: 0.1 seconds (100 ms)
  - **H (Homing Hands)**: 0.4 seconds (400 ms)
  - **M (Mental Preparation)**: 1.2 seconds (1200 ms)
  - **R (System Response)**: Variable; typically around 0.1 seconds (100 ms)

# KLM Example: deleting a file

We can delete a file by:

- A. Dragging and dropping it to the trash can icon
- B. Selecting it and pressing the «delete» key
- C. Performing a right click on it, then selecting the «move to trash» option

Which alternative is faster?



# KLM Example: deleting a file

## Alternative A operators:

- Prepare to perform action (M)
- Point with the mouse over the file icon (P)
- Press and hold mouse button (B)
- Drag file icon to trash can icon (P)
- Release mouse button (B)

### Assumptions:

- Hand already on mouse
- Trash icon visible
- File icon visible

$$\text{Total time} = M + 2P + 2B = 1.2 \text{ s} + 2 * 1.1 \text{ s} + 2 * 0.1 \text{ s} = \mathbf{3.6 \text{ s}}$$

# KLM Example: deleting a file

## Alternative B operators:

- Prepare to perform action (M)
- Point with the mouse over the file icon (P)
- Perform click (B)
- Move hand to keyboard (H)
- Press «delete» key (K)

### Assumptions:

- Hand already on mouse
- Trash icon visible
- File icon visible

Total time = M + P + B + H + K = 1.2 s + 1.1 s + 0.1 s + 0.4 s + 0.2 s = **3 s**

# KLM Example: deleting a file

## Alternative C operators:

- Prepare to perform action (M)
- Point with the mouse over the file icon (P)
- Perform right click (B)
- Point with mouse over «delete» option in context menu (P)
- Perform click (B)

### Assumptions:

- Hand already on mouse
- Trash icon visible
- File icon visible

Total time =  $M + 2 \cdot P + 2 \cdot B = 1.2 \text{ s} + 2 \cdot 1.1 \text{ s} + 2 \cdot 0.1 \text{ s} = \mathbf{3.6 \text{ s}}$



# The Power Law of Practice

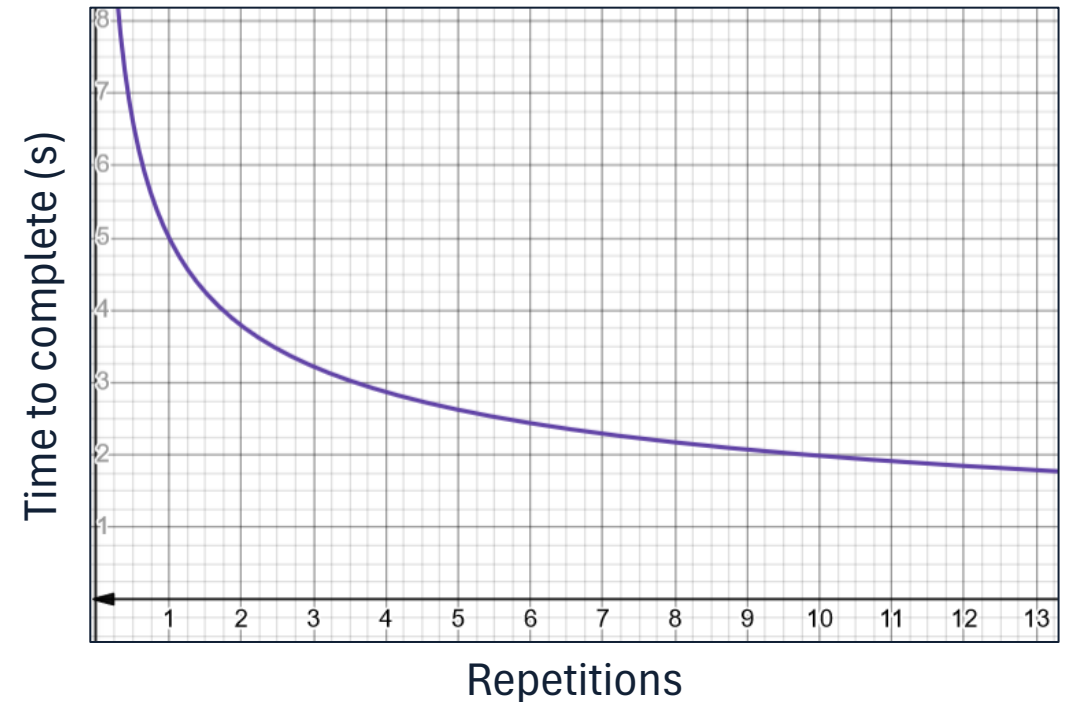
- Allen Newell (cognitive scientist) in the 1980s analyzed reaction times for a variety of tasks in learning experiments
- He noticed that the learning curves obtained in these studies have a very similar shape: that of a **power law**
- The time required to complete a task after  $n$  trials ( $T_n$ ) is close to the time required to complete that task the first time ( $T_1$ ) times  $n^{-a}$

$$T_n \approx T_1 \cdot n^{-a}$$

- $a$  is a parameter comprised between 0.2 and 0.6 (generally  $\sim 0.4$ )

# The Power Law of Practice, in practice

- A user took **5 seconds** to perform a given task the first time they were exposed to the new UI we developed
- How many repetitions would that user need to be able to perform the task in **2 seconds** or less?
  - We can compute an estimation with the power law of practice:  $T_n \approx T_1 \cdot n^{-a}$
  - We solve for  $n$ , assuming  $a = 0.4$
  - $2\text{ s} \leq 5\text{ s} \cdot n^{-0.4}$
  - For  $n = 10$ , we get that  $T_n \approx 1.99\text{ s}$



Plot of the power law of practice, with the given parameters

# Hick's Law

**Hick's law** describes the time it takes for a person to make a decision among a set possible choices.

- Hick's law states that the time  $T$  required to reach a decision increases *logarithmically* with the number of choices.
- In the case of equally probable alternatives:

$$T = a + b \cdot \log_2(n + 1)$$

- $n$  is the number of choices
- $a$  and  $b$  are parameters depending on the context conditions (e.g.: the way choices are presented, the familiarity of the user,...)

# Applying Hick's Law

Which way is faster to select among 64 options?

- One-level 1x64 menu
  - $T = a + b \cdot \log_2(64) = a + 6b$
- Two-level 4x16 menu
  - $T = a + b \cdot \log_2(4) + a + b \cdot \log_2(16) = 2a + 6b$
- Two-level 8x8 menu
  - $T = 2 \cdot (a + b \cdot \log_2(8)) = 2a + 6b$
- Three-level 4x4x4 menu
  - $T = 3 \cdot (a + b \cdot \log_2(4)) = 3a + 6b$
- Six-level 2x2x2x2x2x2 menu
  - $T = 6 \cdot (a + b \cdot \log_2(2)) = 6a + 6b$

# Fitt's Law

Models time to acquire targets in aimed movement

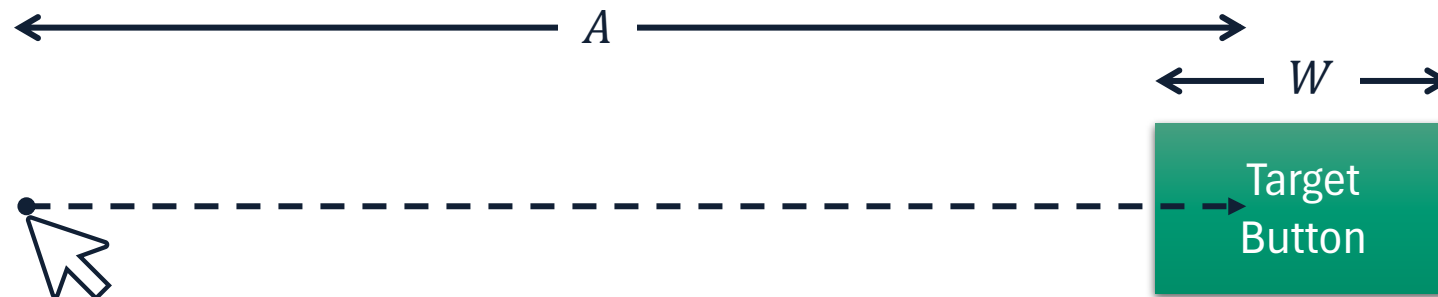
- Reaching for a control in a cockpit
- Moving across a dashboard
- Pulling a defective item from the conveyor belt
- Clicking on icons using a mouse

# Fitt's Law – Index of Difficulty (ID)

- The index of difficulty of a target acquisition task is defined as

$$ID = \log_2 \left( \frac{A}{W} + 1 \right)$$

- $A$  is the **Amplitude** of the movement (distance from start to target)
- $W$  is the **Width** of the target (permissible variability)



# Fitt's Law – Movement Times

- Movement Times (MT) depend on the Difficulty Index ID

$$MT = a + b \cdot ID = a + b \cdot \log_2 \left( \frac{A}{W} + 1 \right)$$

- Movement times also depend on the system, pointing device, user...
  - Can be fitted to specific cases with non-negative parameters  $a$  and  $b$
- It's the equation of a straight line ( $y = mx + c$ ), where  $b$  is the gradient
- $MT$  increases **linearly** with the  $ID$

# Fitt's Law: Applications

If we need to reduce the time needed to perform a target seeking action

- Either we reduce the Amplitude of the movement (move target closer)
- Or we increase the Width of the target
- Or we could work on  $a$  and  $b$



1 cm button 7 cm away

$$ID = \log_2 \left( \frac{7}{1} + 1 \right) = 3$$



1 cm button 3 cm away

$$ID = \log_2 \left( \frac{3}{1} + 1 \right) = 2$$



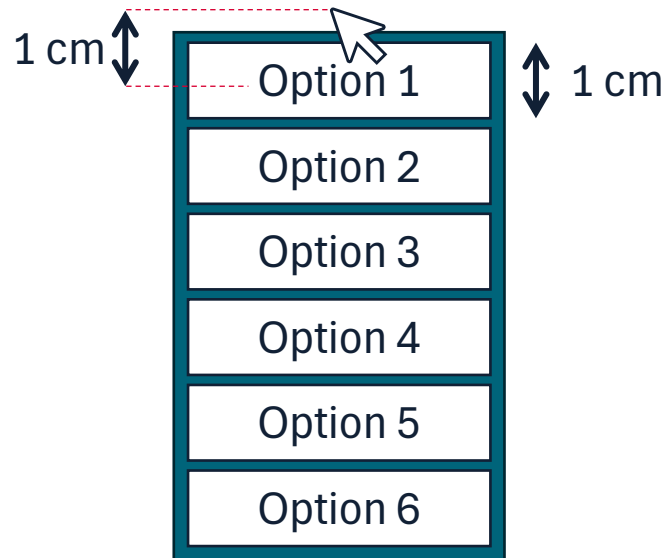
3 cm button 3 cm away

$$ID = \log_2 \left( \frac{3}{3} + 1 \right) = 1$$

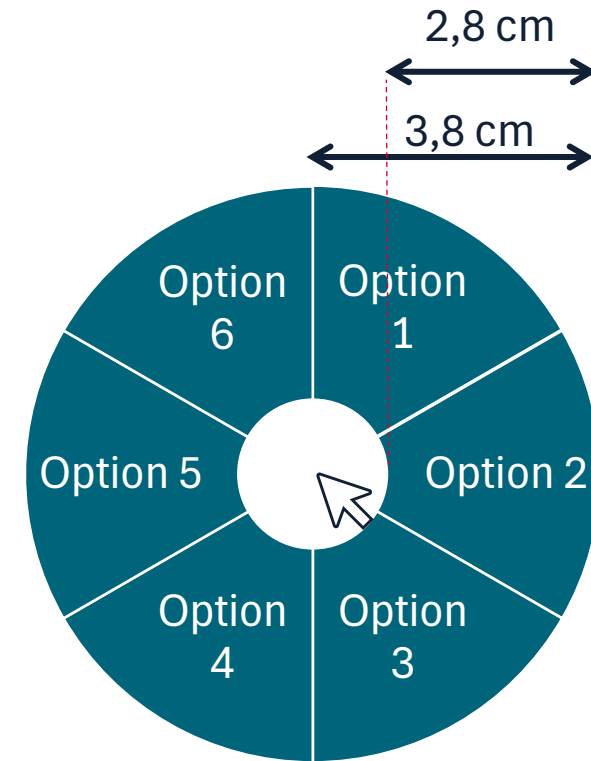


# Fitt's Law: Applications

- Which will be **faster** on average?

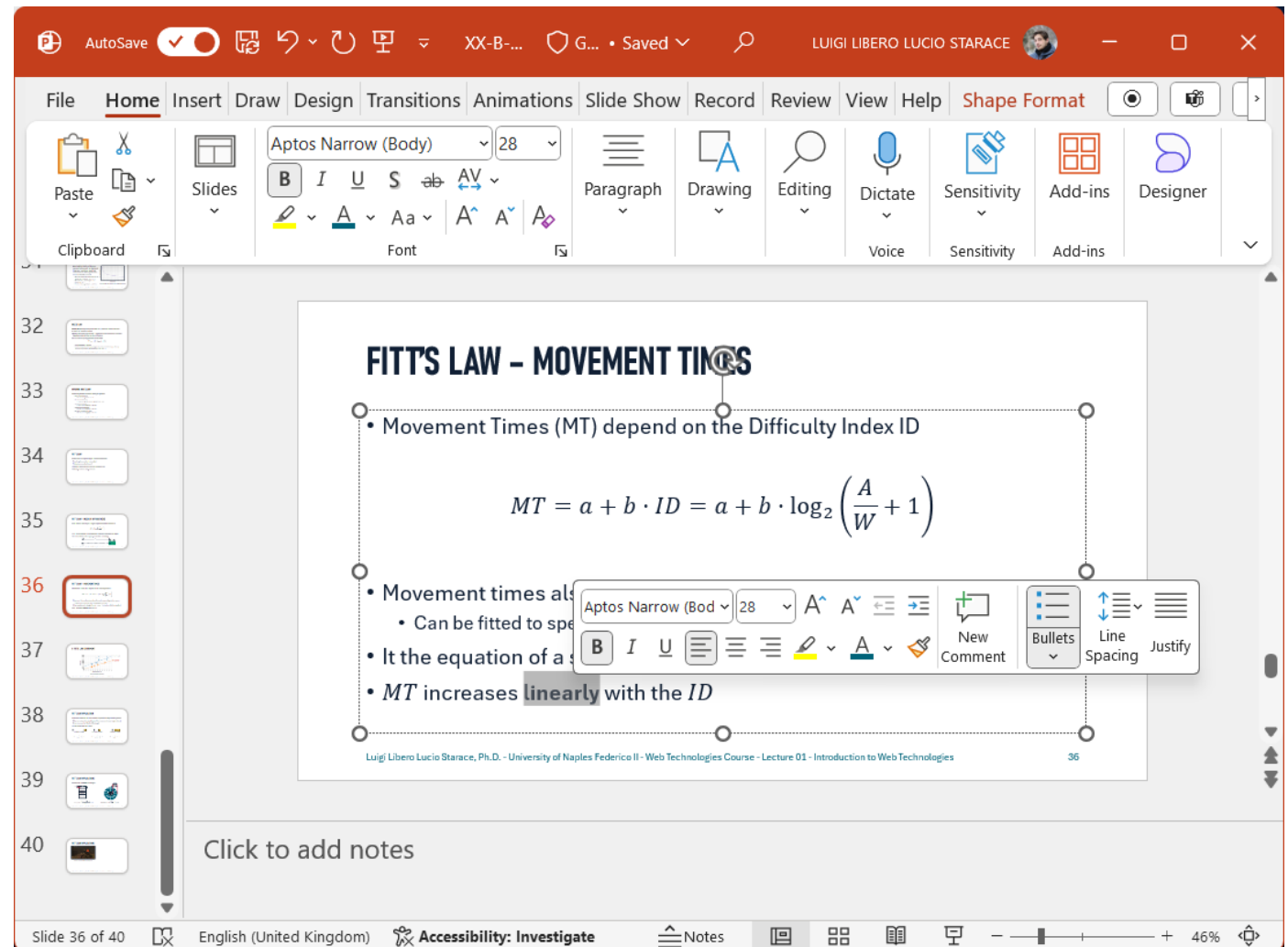
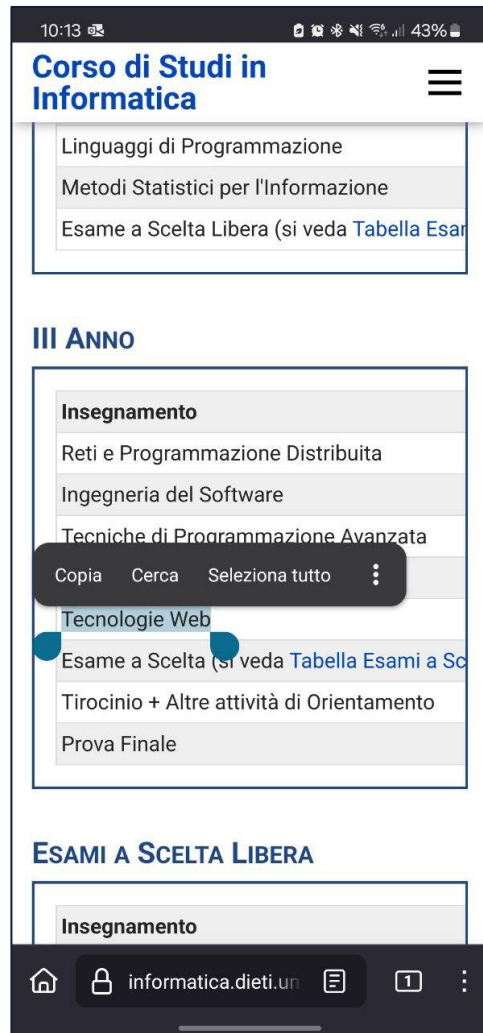


$$\text{Average ID} = \frac{\sum_{i=1}^6 \log_2 \left( \frac{i}{1} + 1 \right)}{6} \approx 2,04$$



$$\text{Average ID} = \log_2 \left( \frac{2,4}{2,8} + 1 \right) \approx 0,89$$

# Fitt's Law: Applications



# Fitt's Law: Applications



Shadow of the Tomb Raider  
(videogame)

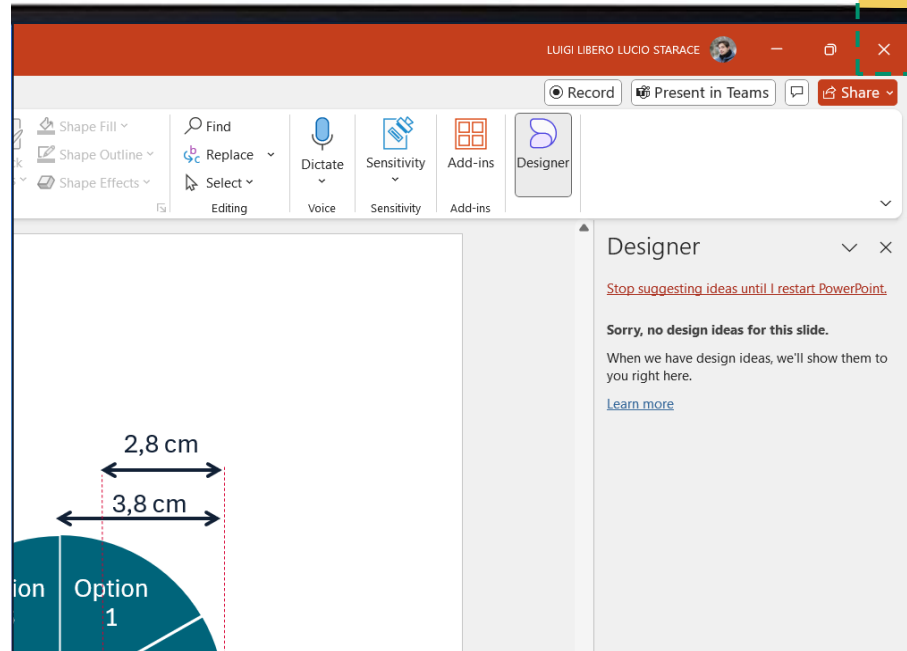


Grand Theft Auto: San Andreas – The Definitive Edition  
(videogame)

# Fitt's Law: Infinite Widths

- With a pointing device, targets near the edges have an infinite width
- These targets are fairly easy to hit, as  $ID = \log_2(A/\infty + 1) = 0!$

Theoretical Effective  
Target Size



# Fitt's Law: Mobile Devices



<https://www.toptal.com/designers/mobile-ui/fitts-law-user-interface-design>



# Readings and references

- Buxton, W. (1990). A Three-State Model of Graphical Input. In D. Diaper et al. (Eds), Human-Computer Interaction - INTERACT '90. Amsterdam: Elsevier Science Publishers B.V. (North-Holland), 449-456.  
<https://www.dgp.toronto.edu/OTP/papers/bill.buxton/3state.html>
- MacKenzie, I. S. (2003). Motor behaviour models for human-computer interaction. In *HCI models, theories, and frameworks: Toward a multidisciplinary science*  
[https://www.yorku.ca/mack/mackenzie\\_chapter.html](https://www.yorku.ca/mack/mackenzie_chapter.html)