Data Science for Economists

Lecture 8: Regression analysis in R

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Today's lecture explores

Software requirements

R packages

It's important to note that "base" R already provides all of the tools to implement a fixed effects regression, **but** you'll quickly hit walls due to memory caps. Instead, I want to introduce **fixest**, short for Fixed-Effects Estimation, which provides lightning fast fixed effects estimation and make your life much easier.

- New: fixest, wooldridge
- Already used: tidyverse, hrbrthemes, listviewer, estimatr, ivreg, sandwich, lmtest, mfx, margins, broom, modelsummary, vtable, rstanarm

A convenient way to install (if necessary) and load everything is by running the below code chunk.

Panel models

Dataset

Let me introduce the dataset we'll be using, crime4. It comes from Jeffrey Wooldridge's R package – Dr. Wooldridge is one of the most accomplished professors of econometrics on the planet. I was tipped off about his package by Nick Huntington-Klein's own lecture notes..

Fixed effects with the fixest package

The simplest (and least efficient) way to include fixed effects in a regression model is, of course, to use dummy variables. However, it isn't very efficient or scalable. What's the point learning all that stuff about the Frisch-Waugh-Lovell, withingroup transformations, etc. etc. if we can't use them in our software routines? Again, there are several options to choose from here. For example, many of you are probably familiar with the excellent **Ife** package (link), which offers near-identical functionality to the popular Stata library, **reghdfe** (link). However, for fixed effects models in R, I am going to advocate that you look no further than the **fixest** package (link).

fixest is relatively new on the scene and has quickly become one of my absolute favourite packages. It has an *boatload* of functionality built in to it: support for nonlinear models, high-dimensional fixed effects, multiway clustering, multimodel estimation, LaTeX tables, etc, etc. It is also insanely fast... as in, up to orders of magnitude faster than **Ife** (in R) or **reghdfe** (in Stata). I won't be able to cover all of **fixest**'s features in depth here — see the introductory vignette for a thorough walkthrough — but I hope to least give you a sense of why I am so enthusiastic about it. Let's start off with a simple example before moving on to something slightly more demanding.

Simple FE model The package's main function is fixest::feols(), which is used for estimating linear fixed effects models. The syntax is such that you first specify the regression model as per normal, and then list the fixed effect(s) after a |. An example may help to illustrate. Let's say that we again want to run our simple regression of mass on height, but this time control for species-level fixed effects.¹

```
# library(fixest) ## Already loaded

ols_fe = feols(mass ~ height | species, data = starwars) ## Fixed effect(s) go after the "|"
ols_fe

## OLS estimation, Dep. Var.: mass
## Observations: 58
## Fixed-effects: species: 31
## Standard-errors: Clustered (species)
## Estimate Std. Error t value Pr(>|t|)
## height 0.974876    0.044291 22.0105 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## RMSE: 9.69063    Adj. R2: 0.99282
## Within R2: 0.662493</pre>
```

Note that the resulting model object has automatically clustered the standard errors by the fixed effect variable (i.e. species). We'll explore some more options for adjusting standard errors in **fixest** objects shortly. But to preview things, you can specify the standard errors you want at estimation time... or you can adjust the standard errors for any existing model via summary.fixest(). For example, here are two equivalent ways to specify vanilla (iid) standard errors:

¹Since we specify "species" in the fixed effects slot below, feols() will automatically coerce it to a factor variable even though we didn't explicitly tell it to.

Specify SEs at estimation time.

Adjust SEs of an existing model (ols_fe) on the fly.

```
feols(mass ~ height | species,
                                               summary(ols_fe,
      data = starwars, se = 'standard')
                                                       se = 'standard')
## OLS estimation, Dep. Var.: mass
                                              ## OLS estimation, Dep. Var.: mass
                                              ## Observations: 58
## Observations: 58
## Fixed-effects: species: 31
                                              ## Fixed-effects: species: 31
                                              ## Standard-errors: IID
## Standard-errors: IID
                                                         Estimate Std. Error t value
                                                                                       Pr(>|t|)
         Estimate Std. Error t value
                                        Pr(>|t ##
                    0.136463 7.1439 1.3797e-O## *hexight 0.974876
                                                                  0.136463 7.1439 1.3797e-07 ***
## height 0.974876
                                              ## ---
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' ## OSignif O.dodes: 10 '***' 0.001 '**' 0.05 '.' 0
                                              ## RMSE: 9.69063
                                                                    Adj. R2: 0.99282
## RMSE: 9.69063
                     Adj. R2: 0.99282
                   Within R2: 0.662493
                                                                  Within R2: 0.662493
```

Before continuing, let's quickly save a "tidied" data frame of the coefficients for later use. I'll use iid standard errors again, if only to show you that the broom::tidy() method for fixest objects also accepts an se argument. This basically just provides another convenient way for you to adjust standard errors for your models on the fly.

```
# coefs_fe = tidy(summary(ols_fe, se = 'standard'), conf.int = TRUE) ## same as below
coefs_fe = tidy(ols_fe, se = 'standard', conf.int = TRUE)
```

High dimensional FEs and multiway clustering As I already mentioned above, **fixest** supports (arbitrarily) high-dimensional fixed effects and (up to fourway) multiway clustering. To see this in action, let's add "homeworld" as an additional fixed effect to the model.

```
## We now have two fixed effects: species and homeworld
ols_hdfe = feols(mass ~ height | species + homeworld, data = starwars)
ols_hdfe
## OLS estimation, Dep. Var.: mass
## Observations: 55
## Fixed-effects: species: 30, homeworld: 38
## Standard-errors: Clustered (species)
##
         Estimate Std. Error t value Pr(>|t|)
## height 0.755844
                    0.332888 2.27057 0.03078 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 7.45791
                    Adj. R2: 1.00768
                  Within R2: 0.487231
```

Easy enough, but the standard errors of the above model are automatically clustered by species, i.e. the first fixed effect variable. Let's go a step further and cluster by both "species" and "homeworld". ² **fixest** provides several ways for us to do this — via the se or cluster arguments — and, again, you can specify your clustering strategy at estimation time, or adjust the standard errors of an existing model on-the-fly. I'll (re)assign the model to the same ols_hdfe object, but you could, of course, create a new object if you so wished.

```
## Cluster by both species and homeworld

## These next few lines all do the same thing. Pick your favourite!

## Specify desired SEs at estimation time...

# ols_hdfe = feols(mass ~ height | species + homeworld, se = 'twoway', data = starwars)

# ols_hdfe = feols(mass ~ height | species + homeworld, cluster = c('species', 'homeworld'), data = starward

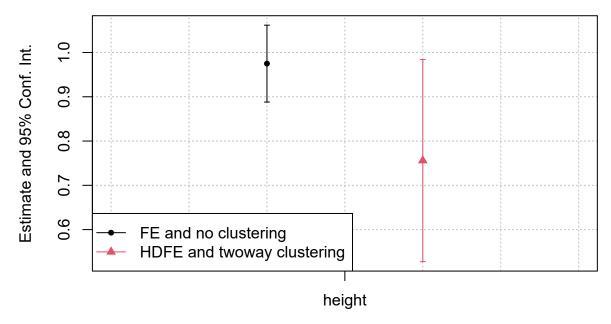
# ols_hdfe = feols(mass ~ height | species + homeworld, cluster = ~ species + homeworld, data = starward

# ols_hdfe = feols(mass ~ height | species + homeworld, cluster = ~ species + homeworld, data = starward
```

²I make no claims to this is a particularly good or sensible clustering strategy, but just go with it.

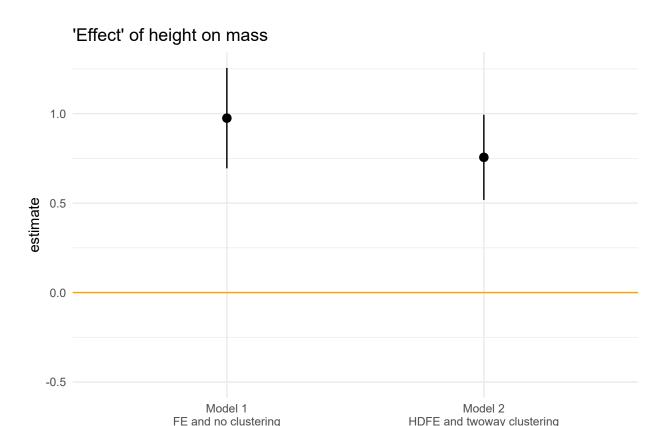
```
##... or, adjust the SEs of an existing model on the fly
# ols_hdfe = summary(ols_hdfe, se = 'twoway')
# ols_hdfe = summary(ols_hdfe, cluster = c('species', 'homeworld'))
ols_hdfe = summary(ols_hdfe, cluster = ~ species + homeworld) ## I'll go with this one
ols_hdfe
## OLS estimation, Dep. Var.: mass
## Observations: 55
## Fixed-effects: species: 30, homeworld: 38
## Standard-errors: Clustered (species & homeworld)
         Estimate Std. Error t value Pr(>|t|)
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 7.45791 Adj. R2: 1.00768
                 Within R2: 0.487231
Comparing our model coefficients I want to quickly flag that fixest provides some really nice, built-in functions for
comparing models. For example, you can get regression tables with fixest::etable().
etable(ols_fe, ols_hdfe)
##
                             ols fe
                                           ols_hdfe
## Dependent Var.:
                                                mass
                              mass
## height 0.9749*** (0.0443) 0.7558*** (0.1164)
## Fixed-Effects: -----
## species
                               Yes
## homeworld
                              No
## S.E.: Clustered by: species by: spec. & home.
## Observations
                               58
                            0.99672
## R2
                                             0.99815
## Within R2
                            0.66249
                                             0.48723
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Similarly, the fixest::coefplot() function for plotting estimation results:
```

Effect on mass



coefplot() is especially useful for tracing the evolution of treatment effects over time, as in a difference-indifferences setup (see Examples). However, I realise some people may find it a bit off-putting that it produces base R plots, rather than a ggplot2 object. We'll get to an automated ggplot2 coefficient plot solution further below with modelsummary::modelplot(). Nevertheless, let me close this out this section by demonstrating the relative ease with which you can do this "manually". Consider the below example, which leverages the fact that we have saved (or can save) regression models as data frames with broom::tidy(). As I suggested earlier, this makes it simple to construct our own bespoke coefficient plots.

```
# library(qqplot2) ## Already loaded
## First get tidied output of the ols_hdfe object
coefs_hdfe = tidy(ols_hdfe, conf.int = TRUE)
bind_rows(
  coefs_fe %>% mutate(reg = "Model 1\nFE and no clustering"),
  coefs_hdfe %>% mutate(reg = "Model 2\nHDFE and twoway clustering")
  ) %>%
  ggplot(aes(x=reg, y=estimate, ymin=conf.low, ymax=conf.high)) +
  geom_pointrange() +
  labs(Title = "Marginal effect of height on mass") +
  geom_hline(yintercept = 0, col = "orange") +
  ylim(-0.5, NA) + ## Added a bit more bottom space to emphasize the zero line
  labs(
    title = "'Effect' of height on mass",
    caption = "Data: Characters from the Star Wars universe"
    ) +
  theme(axis.title.x = element_blank())
```



Data: Characters from the Star Wars universe

FWIW, we'd normally expect our standard errors to blow up with clustering. Here that effect appears to be outweighed by the increased precision brought on by additional fixed effects. Still, I wouldn't put too much thought into it. Our clustering choice doesn't make much sense and I really just trying to demonstrate the package syntax.

Aside on standard errors We've now seen the various options that fixest has for specifying different standard error structures. In short, you invoke either of the se or cluster arguments. Moreover, you can choose to do so either at estimation time, or by adjusting the standard errors for an existing model post-estimation (e.g. with summary.fixest(mod, cluster = ...)). There are two additional points that I want to draw your attention to.

First, if you're coming from another statistical language, adjusting the standard errors post-estimation (rather than always at estimation time) may seem slightly odd. But this behaviour is actually extremely powerful, because it allows us to analyse the effect of different error structures *on-the-fly* without having to rerun the entire model again. **fixest** is already the fastest game in town, but just think about the implied time savings for really large models.³ I'm a huge fan of the flexibility, safety, and speed that on-the-fly standard error adjustment offers us. I even wrote a whole blog post about it if you'd like to read more.

Second, reconciling standard errors across different software is a much more complicated process than you may realise. There are a number of unresolved theoretical issues to consider — especially when it comes to multiway clustering — and package maintainers have to make a number of arbitrary decisions about the best way to account for these. See here for a detailed discussion. Luckily, Laurent (the **fixest** package author) has taken the time to write out a detailed vignette about how to replicate standard errors from other methods and software packages.⁴

³To be clear, adjusting the standard errors via, say, summary.fixest() completes instantaneously.

⁴If you want a deep dive into the theory with even more simulations, then this paper by the authors of the **sandwich** paper is another excellent resource.

Presentation

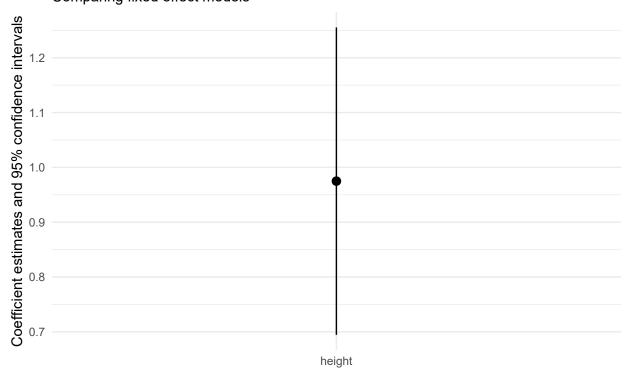
Figures

Coefficient plots We've already worked through an example of how to extract and compare model coefficients here. I use this "manual" approach to visualizing coefficient estimates all the time. However, our focus on **modelsummary** in the preceding section provides a nice segue to another one of the package's features: modelplot(). Consider the following, which shows both the degree to which modelplot() automates everything and the fact that it readily accepts regular ggplot2 syntax.

```
# library(modelsummary) ## Already loaded
mods = list('FE, no clustering' = summary(ols_fe, se = 'standard'))

modelplot(mods) +
    ## You can further modify with normal ggplot2 commands...
coord_flip() +
labs(
    title = "'Effect' of height on mass",
    subtitle = "Comparing fixed effect models"
    )
```

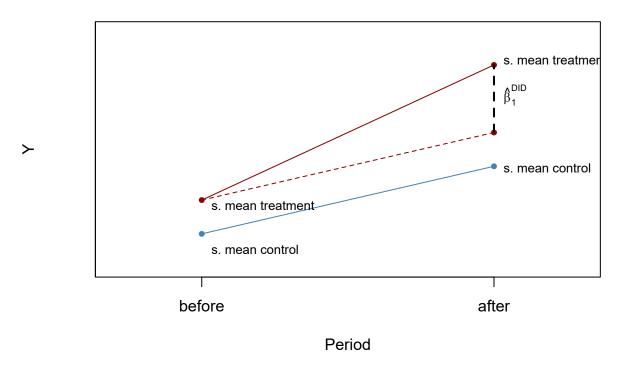
'Effect' of height on mass Comparing fixed effect models



Difference-in-differences

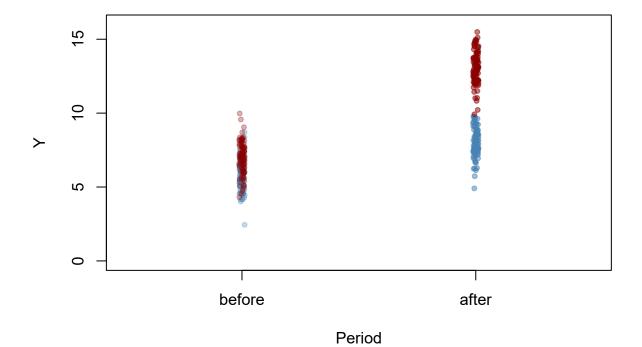
One of the most popular uses of fixed effects is to implement difference-in-difference designs. I vusalize how that works for you below.

The Differences-in-Differences Estimator



Diff-in-diff with data

Artificial Data for DID Estimation



Instrumental variables

As you would have guessed by now, there are a number of ways to run instrumental variable (IV) regressions in R. I'll walk through three different options using the ivreg::ivreg(), estimatr::iv_robust(), and fixest::feols() functions, respectively. These are all going to follow a similar syntax, where the IV first-stage regression is specified in a multi-part formula (i.e. where formula parts are separated by one or more pipes, |). However, there are also some subtle and important differences, which is why I want to go through each of them. After that, I'll let you decide which of the three options is your favourite.

The dataset that we'll be using for this section describes cigarette demand for the 48 continental US states in 1995, and is taken from the **ivreg** package. Here's a quick a peek:

```
data("CigaretteDemand", package = "ivreg")
head(CigaretteDemand)
                  rprice rincome salestax
##
          packs
                                              cigtax packsdiff pricediff
## AL 101.08543 103.9182 12.91535 0.9216975 26.57481 -0.1418075 0.09010222
## AR 111.04297 115.1854 12.16907 5.4850193 36.41732 -0.1462808 0.19998082
## AZ 71.95417 130.3199 13.53964 6.2057067 42.86964 -0.3733741 0.25576681
## CA 56.85931 138.1264 16.07359 9.0363074 40.02625 -0.5682141 0.32079587
## CD 82.58292 109.8097 16.31556 0.0000000 28.87139 -0.3132622 0.22587189
## CT
      79.47219 143.2287 20.96236 8.1072834 48.55643 -0.3184911 0.18546746
##
      incomediff salestaxdiff cigtaxdiff
## AL 0.18222144
                   0.1332853 -3.62965832
## AR 0.15055894
                   5.4850193 2.03070663
## AZ 0.05379983
                   1.4004856 14.05923036
## CA 0.02266877
                   3.3634447 15.86267924
                   0.0000000 0.06098283
## CO 0.13002974
## CT 0.18404197
                   -0.7062239 9.52297455
```

Now, assume that we are interested in regressing the number of cigarettes packs consumed per capita on their average price and people's real incomes. The problem is that the price is endogenous, because it is simultaneously determined by demand and supply. So we need to instrument for it using cigarette sales tax. That is, we want to run the following two-stage IV regression.

$$Price_i = \pi_0 + \pi_1 Sales Tax_i + v_i \qquad \text{(First stage)}$$

$$Packs_i = \beta_0 + \beta_2 \widehat{Price}_i + \beta_1 Real Income_i + u_i \qquad \text{(Second stage)}$$

IV with fixest::feols()

Finally, we get back to the fixest::feols() function that we've already seen above. Truth be told, this is the IV option that I use most often in my own work. In part, this statement reflects the fact that I work mostly with panel data and will invariably be using **fixest** anyway. But I also happen to like its IV syntax a lot. The key thing is to specify the IV first-stage as a separate formula in the *final* slot of the model call. For example, if we had fe fixed effects, then the model call would be y ~ ex | fe | en ~ in. Since we don't have any fixed effects in our current cigarette demand example, the first-stage will come directly after the exogenous variables:

```
# library(fixest) ## Already loaded

iv_feols =
  feols(
    log(packs) ~ log(rincome) | ## y ~ ex
        log(rprice) ~ salestax, ## en ~ in (IV first-stage; must be the final slot)
    data = CigaretteDemand
```

⁵This closely resembles Stata's approach to writing out the IV first-stage, where you specify the endogenous variable(s) and the instruments together in a slot.

```
# summary(iv_feols, stage = 1) ## Show the 1st stage in detail
iv_feols
## TSLS estimation, Dep. Var.: log(packs), Endo.: log(rprice), Instr.: salestax
## Second stage: Dep. Var.: log(packs)
## Observations: 48
## Standard-errors: IID
##
                   Estimate Std. Error
                                         t value
                                                   Pr(>|t|)
## (Intercept)
                   9.430658
                              1.358366 6.942648 1.2395e-08 ***
## fit log(rprice) -1.143375
                              0.359486 -3.180583 2.6617e-03 **
## log(rincome)
                   0.214515
                              0.268585 0.798687 4.2867e-01
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
                   Adj. R2: 0.393109
## RMSE: 0.183555
## F-test (1st stage), log(rprice): stat = 45.2 , p = 2.655e-8, on 1 and 45 DoF.
##
                       Wu-Hausman: stat = 1.102, p = 0.299559, on 1 and 44 DoF.
```

Again, I emphasise that the IV first-stage must always come last in the feols() model call. Just to be pedantic — but also to demonstrate how easy **fixest**'s IV functionality extends to panel settings — here's a final feols() example. This time, I'll use a panel version of the same US cigarette demand data that includes entries from both 1985 and 1995. The dataset originally comes from the **AER** package, but we can download it from the web as follows. Note that I'm going to modify some variables to make it better comparable to our previous examples.

```
## Get the data
url = 'https://vincentarelbundock.github.io/Rdatasets/csv/AER/CigarettesSW.csv'
cigs_panel =
  read.csv(url, row.names = 1) %>%
  mutate(
    rprice = price/cpi,
    rincome = income/population/cpi
    )
head(cigs_panel)
```

```
##
    state year
                 cpi population
                                   packs
                                            income tax
                                                            price
## 1
       AL 1985 1.076
                        3973000 116.4863 46014968 32.5 102.18167 33.34834
## 2
       AR 1985 1.076
                        2327000 128.5346 26210736 37.0 101.47500 37.00000
## 3
       AZ 1985 1.076
                        3184000 104.5226 43956936 31.0 108.57875 36.17042
       CA 1985 1.076
                       26444000 100.3630 447102816 26.0 107.83734 32.10400
       CO 1985 1.076
                        3209000 112.9635 49466672 31.0 94.26666 31.00000
## 5
## 6
       CT 1985 1.076
                        3201000 109.2784 60063368 42.0 128.02499 51.48333
##
       rprice rincome
## 1 94.96438 10.76387
## 2 94.30762 10.46817
## 3 100.90962 12.83046
## 4 100.22058 15.71332
## 5 87.60842 14.32619
## 6 118.98234 17.43861
```

Let's run a panel IV now, where we'll explicitly account for year and state fixed effects.

```
iv_feols_panel =
  feols(
    log(packs) ~ log(rincome) |
    year + state |  ## Now include FEs slot
    log(rprice) ~ taxs,  ## IV first-stage still comes last
```

```
data = cigs_panel
)
# summary(iv_feols_panel, stage = 1) ## Show the 1st stage in detail
iv_feols_panel
```

```
## TSLS estimation, Dep. Var.: log(packs), Endo.: log(rprice), Instr.: taxs
## Second stage: Dep. Var.: log(packs)
## Observations: 96
## Fixed-effects: year: 2, state: 48
## Standard-errors: Clustered (year)
                    Estimate Std. Error
                                              t value
                                                        Pr(>|t|)
## fit_log(rprice) -1.279349
                               2.11e-15 -6.071802e+14 1.0485e-15 ***
## log(rincome)
                    0.443422
                               1.41e-15 3.138717e+14 2.0283e-15 ***
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## RMSE: 0.044789
                      Adj. R2: 0.92791
                    Within R2: 0.533965
                                                  , p = 7.535e-14, on 1 and 46 DoF.
## F-test (1st stage), log(rprice): stat = 111.0
##
                        Wu-Hausman: stat =
                                             6.02154, p = 0.018161 , on 1 and 44 DoF.
```

Good news, our coefficients are around the same magnitude. But the increased precision of the panel model has yielded gains in statistical significance.

Further resources

- Ed Rubin has outstanding teaching notes for econometrics with R on his website. This includes both undergradand graduate-level courses. Seriously, check them out.
- Several introductory texts are freely available, including *Introduction to Econometrics with R* (Christoph Hanck *et al.*), *Using R for Introductory Econometrics* (Florian Heiss), and *Modern Dive* (Chester Ismay and Albert Kim).
- Tyler Ransom has a nice cheat sheet for common regression tasks and specifications.
- Itamar Caspi has written a neat unofficial appendix to this lecture, *recipes for Dummies*. The title might be a little inscrutable if you haven't heard of the recipes package before, but basically it handles "tidy" data preprocessing, which is an especially important topic for machine learning methods. We'll get to that later in course, but check out Itamar's post for a good introduction.
- I promised to provide some links to time series analysis. The good news is that R's support for time series is very, very good. The Time Series Analysis task view on CRAN offers an excellent overview of available packages and their functionality.
- Lastly, for more on visualizing regression output, I highly encourage you to look over Chapter 6 of Kieran Healy's *Data Visualization: A Practical Guide*. Not only will learn how to produce beautiful and effective model visualizations, but you'll also pick up a variety of technical tips.