# Big Data and Economics

Fixed Effects and Difference-in-differences

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Today's lecture explores

### **Software requirements**

#### R packages

It's important to note that "base" R already provides all of the tools to implement a fixed effects regression, **but** you'll quickly hit walls due to memory caps. Instead, I want to introduce **fixest**, short for Fixed-Effects Estimation, which provides lightning fast fixed effects estimation and make your life much easier.

- · New: fixest, wooldridge
- Already used: modelsummary, broom, tidyverse

A convenient way to install (if necessary) and load everything is by running the below code chunk.

```
## Load and install the packages that we'll be using today
if (!require("pacman")) install.packages("pacman")
pacman::p_load(modelsummary, broom, fixest, wooldridge, tidyverse)

## My preferred ggplot2 plotting theme (optional)
theme_set(theme_minimal())
```

**Note on fixest and feols** I'll be using fixest and feols throughout these notes. The fixest package is a new package that is very fast and has a lot of functionality. It has several bits of funtionality like feols() and etable(), which are powerful functions for making regressions and putting the output into tables that work well together. feols() works very much like lm() in base R, but with a few added bonuses.

#### Review of last lecture

Last lecture we covered how fixed effects are extremely useful for removing variation between units. That means any of the average differences between groups of the fixed effect are removed. We can then look at underlying variation within these groups to see if there is a relationship between our variables of interest.

This is extremely useful for dealing with omitted variable bias. If we have an omitted variable that is correlated with our independent variable, we can't tell if the relationship we see is due to the independent variable or the omitted variable. But if we have a fixed effect for the omitted variable, we can remove the variation between units and then look at the variation within units.

In practice, fixed effects amount to de-meaning our variables of interest. There are a handful of ways to do this.

#### Panel models

A panel dataset is one in which we view a single unit over multiple periods of time, so a balanced panel has the same number of observations for each unit. For example, we might have data on 100 countries over 10 years, or 50 US states over 20 years. We can then take unit fixed effects, which lets us compare between years within a single unit. Similarly, we can take time fixed effects to compare between units within a given point in time. If our dataset has other dimensions that vary in a way that is not collinear with unit or time, we can also take a fixed effect for that – though again, you want to be careful about throwing in fixed effects.

#### **Dataset**

Let me introduce the dataset we'll be using, crime4. It comes from Jeffrey Wooldridge's R package – Dr. Wooldridge is one of the most accomplished professors of econometrics on the planet. I was tipped off about his package by Nick Huntington-Klein's own lecture notes.. The dataset shows county probability of arrest and county crime rate by year.

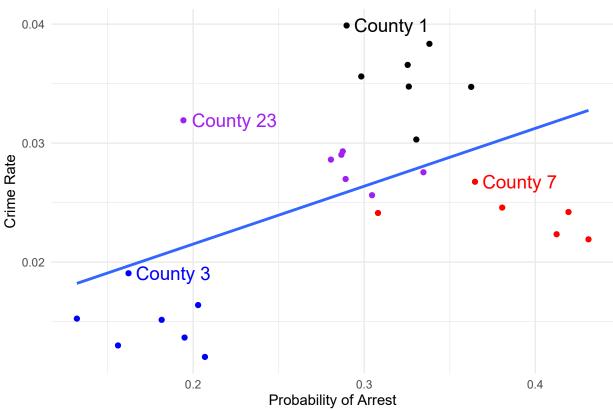
```
data(crime4)
crime4 %>%
  dplyr::select(county, year, crmrte, prbarr) %>%
  rename(County = county,
         Year = year,
         CrimeRate = crmrte,
         ProbofArrest = prbarr) %>%
  slice(1:9)
## # A tibble: 630 x 4
## # Groups:
               County [90]
##
      County Year CrimeRate ProbofArrest
##
       <int> <int>
                       <dbl>
                                     <dbl>
##
   1
           1
                81
                      0.0399
                                     0.290
##
   2
           1
                82
                      0.0383
                                     0.338
##
   3
           1
                83
                      0.0303
                                     0.330
   4
                84
                      0.0347
                                     0.363
##
           1
##
    5
           1
                85
                      0.0366
                                     0.325
##
   6
           1
                86
                      0.0348
                                     0.326
##
   7
           1
                87
                      0.0356
                                     0.298
           3
                                     0.203
##
   8
                81
                      0.0164
##
   9
           3
                82
                      0.0191
                                     0.162
           3
                83
                      0.0151
                                     0.182
## 10
## # i 620 more rows
```

#### Let's visualize it

Below I visualize the data for just a few counties. Note the positive slope when pooling! Is that surprising?

```
geom_text(hjust = -.1, size = 14/.pt) +
labs(x = 'Probability of Arrest',
    y = 'Crime Rate',
    caption = 'One outlier eliminated in County 7.') +
#scale_x_continuous(limits = c(.15, 2.5)) +
guides(color = FALSE, label = FALSE) +
scale_color_manual(values = c('black','blue','red','purple')) +
geom_smooth(method = 'lm', aes(color = NULL, label = NULL), se = FALSE)
```

## `geom\_smooth()` using formula = 'y ~ x'



One outlier eliminated in County 7.

### Let's try the de-meaning approach

We can use group\_by to get means-within-groups and subtract them out.

### And Regress!

```
orig_data <- lm(crmrte ~ prbarr, data = crime4)
de_mean <- lm(demeaned_crime ~ demeaned_prbarr, data = crime4)
msummary(list(orig_data, de_mean))</pre>
```

	(1)	(2)
(Intercept)	0.043	0.000
	(0.001)	(0.000)
prbarr	-0.038	
	(0.004)	
demeaned_prbarr		-0.002
		(0.002)
Num.Obs.	630	630
R2	0.129	0.001
R2 Adj.	0.127	-0.001
AIC	-3347.3	-4549.6
BIC	-3334.0	-4536.3
Log.Lik.	1676.651	2277.823
F	92.646	
RMSE	0.02	0.01

Note the coefficient has flipped!

#### Interpreting a Within Relationship

How can we interpret that slope of -0.02? This is all within variation so our interpretation must be within-county. So, "comparing a county in year A where its arrest probability is 1 (100 percentage points) higher than it is in year B, we expect the number of crimes per person to drop by .02." Or if we think we've causally identified it (and want to work on a more realistic scale), "raising the arrest probability by 1 percentage point in a county reduces the number of crimes per person in that county by .0002". We're basically "controlling for county" (and will do that explicitly in a moment). So your interpretation should think of it in that way - holding county constant i.e. comparing two observations with the same value of county i.e. comparing a county to itself at a different point in time.

#### Concept checks

- Do you think the model we've presented is sufficient to have a causal interpretation of the effect of arrest probability on crime?
- What assumptions would we need to make to have a causal interpretation?
- What potential confounders are there?
- Why does subtracting the within-individual mean of each variable "control for individual"?
- In a sentence, interpret the slope coefficient in the estimated model  $(Y_{i\underline{t}} \bar{Y}_i) = 2 + 3(X_{it} \bar{X}_i)$  where Y is "blood pressure", X is "stress at work", and i is an individual person, and  $\bar{Y}_i$  means average of  $Y_i$
- Is this relationship causal? If not, what assumptions are required for it to be causal?

### Can we do that all at once? Yes, with the Least Squares Dummy Variable Approach

De-meaning takes some steps which could get tedious to write out. Another way is to include a dummy or category variable for each county. This is called the Least Squares Dummy Variable approach.

You end up with the same results as if we de-meaned.

```
lsdv <- lm(crmrte ~ prbarr + factor(county), data = crime4)
msummary(list(orig_data, de_mean, lsdv), keep = c('prbarr', 'demeaned_prob'))</pre>
```

Hey look, the coefficient is the same!

### Why LSDV?

- A benefit of the LSDV approach is that it calculates the fixed effects  $\alpha_i$  for you
- · We left those out of the table with the coefs argument of msummary (we rarely want them) but here they are:

	(1)	(2)	(3)
prbarr	-0.038		-0.002
	(0.004)		(0.003)
demeaned_prbarr		-0.002	
		(0.002)	
Num.Obs.	630	630	630
R2	0.129	0.001	0.871
R2 Adj.	0.127	-0.001	0.849
AIC	-3347.3	-4549.6	-4371.6
BIC	-3334.0	-4536.3	-3962.6
Log.Lik.	1676.651	2277.823	2277.823
F	92.646		40.351
RMSE	0.02	0.01	0.01

#### lsdv

```
##
##
   Call:
##
   lm(formula = crmrte ~ prbarr + factor(county), data = crime4)
##
   Coefficients:
##
                                  prbarr
                                             factor(county)3
                                                                 factor(county)5
         (Intercept)
                                                  -0.0211038
##
           0.0363976
                              -0.0020232
                                                                       -0.0227439
##
     factor(county)7
                         factor(county)9
                                            factor(county)11
                                                                factor(county)13
##
          -0.0125058
                               -0.0240486
                                                  -0.0183143
                                                                       -0.0032912
##
    factor(county)15
                        factor(county)17
                                            factor(county)19
                                                                factor(county)21
          -0.0179836
                              -0.0146255
                                                  -0.0185499
                                                                        0.0035485
##
##
    factor(county)23
                        factor(county)25
                                            factor(county)27
                                                                factor(county)33
##
          -0.0073943
                              -0.0034639
                                                  -0.0012558
                                                                       -0.0198379
##
    factor(county)35
                        factor(county)37
                                            factor(county)39
                                                                factor(county)41
           0.0070240
                              -0.0143802
##
                                                  -0.0212591
                                                                       -0.0115589
##
    factor(county)45
                        factor(county)47
                                            factor(county)49
                                                                factor(county)51
##
          -0.0008915
                              -0.0053747
                                                  -0.0015888
                                                                        0.0318754
##
    factor(county)53
                        factor(county)55
                                            factor(county)57
                                                                factor(county)59
##
          -0.0186603
                               0.0221664
                                                  -0.0063204
                                                                       -0.0178825
##
    factor(county)61
                        factor(county)63
                                            factor(county)65
                                                                factor(county)67
##
          -0.0149666
                               0.0381621
                                                    0.0198140
                                                                        0.0214212
##
    factor(county)69
                        factor(county)71
                                            factor(county)77
                                                                factor(county)79
##
          -0.0211463
                               0.0228639
                                                    0.0022599
                                                                       -0.0215523
##
    factor(county)81
                        factor(county)83
                                            factor(county)85
                                                                factor(county)87
           0.0205261
                              -0.0064776
                                                    0.0051594
                                                                       -0.0078661
##
##
    factor(county)89
                        factor(county)91
                                            factor(county)93
                                                                factor(county)97
##
          -0.0088413
                              -0.0040777
                                                  -0.0018436
                                                                        0.0021169
                                                               factor(county)107
##
    factor(county)99
                       factor(county)101
                                           factor(county)105
##
          -0.0192747
                              -0.0027612
                                                    0.0143055
                                                                        0.0108018
                                                               factor(county)115
##
   factor(county)109
                       factor(county)111
                                           factor(county)113
##
          -0.0170930
                              -0.0187163
                                                  -0.0239391
                                                                       -0.0301032
##
   factor(county)117
                       factor(county)119
                                           factor(county)123
                                                               factor(county)125
##
          -0.0169581
                               0.0526182
                                                  -0.0023063
                                                                       -0.0091250
##
   factor(county)127
                       factor(county)129
                                           factor(county)131
                                                               factor(county)133
##
           0.0028419
                               0.0386488
                                                  -0.0179728
                                                                        0.0098405
## factor(county)135
                       factor(county)137
                                           factor(county)139
                                                               factor(county)141
```

```
##
           0.0188796
                             -0.0220273
                                                -0.0066127
                                                                     0.0337109
## factor(county)143
                     factor(county)145 factor(county)147 factor(county)149
          -0.0139798
##
                             -0.0071850
                                                 0.0166929
                                                                    -0.0200991
## factor(county)151
                     factor(county)153
                                         factor(county)155 factor(county)157
##
          -0.0114062
                             -0.0047028
                                                -0.0026681
                                                                    -0.0058717
                     factor(county)161 factor(county)163 factor(county)165
## factor(county)159
          -0.0043145
                             -0.0154759
                                                -0.0147833
                                                                     0.0082355
##
## factor(county)167
                      factor(county)169 factor(county)171 factor(county)173
##
          -0.0128534
                             -0.0232628
                                                -0.0141934
                                                                    -0.0242636
## factor(county)175
                      factor(county)179
                                         factor(county)181 factor(county)183
          -0.0175234
                             -0.0077435
                                                 0.0232585
                                                                     0.0175664
                                                            factor(county)191
## factor(county)185
                      factor(county)187
                                         factor(county)189
                                                                     0.0015451
##
          -0.0243118
                             -0.0078490
                                                -0.0071590
## factor(county)193
                                         factor(county)197
                      factor(county)195
##
          -0.0152095
                              0.0097064
                                                -0.0209701
```

THe interpretation is exactly the same as with a categorical variable - we have an omitted county, and these show the difference relative to that omitted county

**NOTE:** See how I put factor() around county? That is to ensure it reads county, which is the county fips code as a categorical variable instead of as a numerical variable. If you don't do that, it will read it as a numerical variable and you'll get a different result:

```
lm(crmrte ~ prbarr + county, data = crime4)

##
## Call:
## lm(formula = crmrte ~ prbarr + county, data = crime4)
##
## Coefficients:
## (Intercept) prbarr county
## 4.213e-02 -3.788e-02 1.094e-05
```

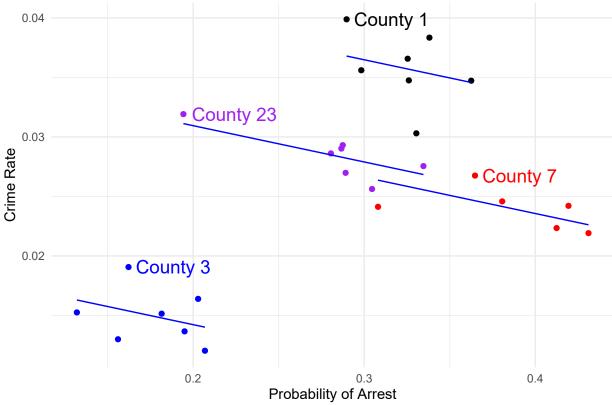
This is saying that as FIPS code increases by one, the crime rate increases by 0.000011... that's nonsense. There's an urban legend of an economist who took the log of the NAICS industry classification code for quite some time before realizing they meant to use a categorical variable. Correcting that mistake completely changed their results.

# Why LSDV?

This also makes clear another element of what's happening! Just like with a categorical var, the line is moving *up and down* to meet the counties. Graphically, de-meaning moves all the points together in the middle to draw a line, while LSDV moves the line up and down to meet the points

```
)) %>%
ggplot(aes(x = prbarr, y = crmrte, color = factor(county), label = label)) +
geom_point() +
geom_text(hjust = -.1, size = 14/.pt) +
geom_line(aes(y = pred, group = county), color = 'blue') +
labs(x = 'Probability of Arrest',
     y = 'Crime Rate',
     caption = 'One outlier eliminated in County 7.') +
\#scale_x\_continuous(limits = c(.15, 2.5)) +
guides(color = FALSE, label = FALSE) +
scale_color_manual(values = c('black','blue','red','purple'))
```

## Warning: Removed 23 rows containing missing values (`geom\_text()`).



One outlier eliminated in County 7.

# The "Pros" don't use LSDV

Most people do not use LSDB - it is computationally expensive. If you get too many fixed effects or too big of data, it just will not wrong. The professionally-written commands use de-meaning, like fixest, which is less computationally expensive. See for yourself! Look, we even used the **etable** function.

```
pro <- feols(crmrte ~ prbarr | county, data = crime4)</pre>
de_mean <- feols(demeaned_crime ~ demeaned_prbarr, data = crime4)</pre>
etable(de_mean, pro)
##
                                                        pro
```

de\_mean ## Dependent Var.: demeaned\_crime crmrte ## ## Constant

```
## demeaned_prbarr -0.0020 (0.0025)
               -0.0020 (0.0026)
## prbarr
## Fixed-Effects: -----
## county
                       Nο
## ______ _____
                IID by: county
630 630
## S.E. type
## Observations
                    0.00106
                              0.87076
## R.2
## Within R2
                               0.00106
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

To explain the **fixest** package, let's dive a bit deeper into the crime data. It has tons of variables we could use. We could account for variation by year for example.

```
##
                 County FE
                               Year FE County and Yea..
## Dependent Var.:
                   crmrte
##
## prbarr -0.0020 (0.0026) -0.0378** (0.0090) -0.0011 (0.0026)
## Fixed-Effects: -----
## county
                     Yes
                                  No
## year
                     No
                                 Yes
                                             Yes
## ______ ______
## S.E.: Clustered by: county by: year by: county ## Observations 630 630 630
                 ## R2
                                          0.87735
## Within R2
                                          0.00034
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

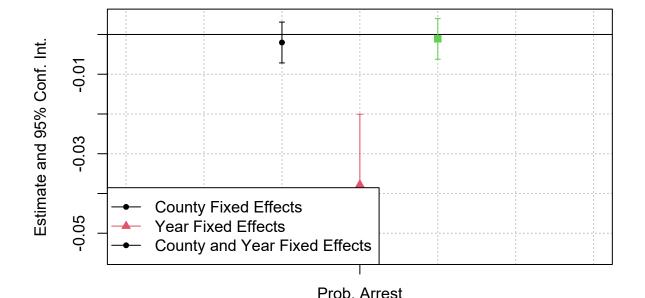
Pretty neat right? Just sticking something after the | allows you to residualize its fixed effect!

```
## County FE Year FE County and Yea..
## Dependent Var.: Crime Rate Crime Rate Crime Rate
```

```
##
                   -0.0020 (0.0026) -0.0378** (0.0090) -0.0011 (0.0026)
## Prob. Arrest
## Fixed-Effects:
## County
                                Yes
                                                    No
                                                                     Yes
## Year
                                 No
                                                    Yes
                                                                     Yes
##
## S.E.: Clustered
                         by: County
                                              by: Year
                                                             by: County
## Observations
                                630
                                                    630
                                                                     630
## R2
                            0.87076
                                               0.13347
                                                                 0.87735
                                                                 0.00034
## Within R2
                            0.00106
                                               0.12764
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# I don't want to keep writing in ,dict=dct. So I'll use setFixestDict
# This applies to every etable in the session
setFixest_dict(dict)
```

**Visualization** Similarly, the fixest::coefplot() function for plotting estimation results:

# **Effect on Crime Rate**

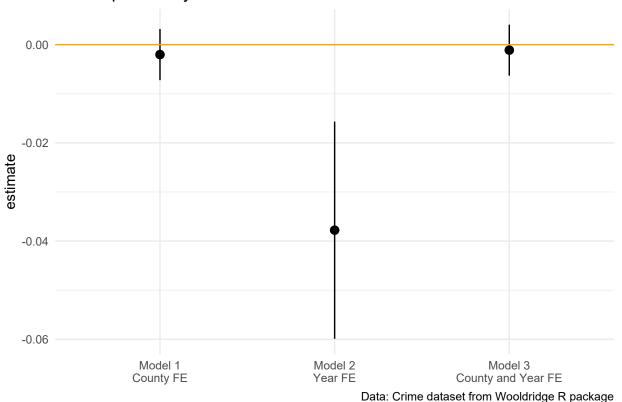


coefplot() is especially useful for tracing the evolution of treatment effects over time, as in a difference-indifferences setup (see Examples). However, I realise some people may find it a bit off-putting that it produces base R plots, rather than a ggplot2 object. We'll get to an automated ggplot2 coefficient plot solution further below with modelsummary::modelplot(). Nevertheless, let me close this out this section by demonstrating the relative ease with which you can do this "manually". Consider the below example, which leverages the fact that we have saved (or can save) regression models as data frames with broom::tidy(). As I suggested earlier, this makes it simple to construct our own

bespoke coefficient plots.

```
# library(ggplot2) ## Already loaded
## First get tidied output of the ols_hdfe object
coefs_crime_county_fe = tidy(crime_county_fe, conf.int = TRUE)
coefs_crime_year_fe = tidy(crime_year_fe, conf.int = TRUE)
coefs_crime_county_year_fe = tidy(crime_county_year_fe, conf.int = TRUE)
bind rows(
  coefs_crime_county_fe %>% mutate(reg = "Model 1\nCounty FE"),
  coefs_crime_year_fe %>% mutate(reg = "Model 2\nYear FE"),
  coefs_crime_county_year_fe %>% mutate(reg="Model 3\nCounty and Year FE")
  ) %>%
  ggplot(aes(x=reg, y=estimate, ymin=conf.low, ymax=conf.high)) +
  geom_pointrange() +
  labs(Title = "Marginal effect of probability of arrest on crime rate") +
  geom_hline(yintercept = 0, col = "orange") +
  labs(
   title = "'Effect' probability of arrest on crime rate",
    caption = "Data: Crime dataset from Wooldridge R package"
  theme(axis.title.x = element_blank())
```

# 'Effect' probability of arrest on crime rate



**What if we wanted to change the clustering of the standard errors?** Did you notice the S.E. type above? It autoclustered by the fixed effects – specifically the fixed effect with the most levels. **fixest** does that by default, but maybe you disagree!

Sometimes you want to cluster standard errors a new way. Well that is something you can do with fixest and its delight-

fully well-designed etable() function. You can specify the cluster variable with cluster() or the type of standard errors you want with se() and get different types of standard errors. Below I specify standard errors clustered by state and then an assumption of independent and identically distributed errors. (The most vanilla standard errors you can assume and rarely the ones we believe explain real world phenomena.)

```
##
                                          Year FE County and Yea..
                      County FE
                      Crime Rate
                                       Crime Rate
                                                      Crime Rate
## Dependent Var.:
## Prob. Arrest
              -0.0020 (0.0027) -0.0378*** (0.0040) -0.0011 (0.0026)
## Fixed-Effects: -----
## County
                            Yes
                                              No
                                                             Yes
                                              Yes
## Year
                           No
## S.E. type
                            IID
                                              IID
                                                             IID
## Observations
                            630
                                              630
                                                             630
                        0.87076
## R2
                                         0.13347
                                                         0.87735
                                         0.12764
## Within R2
                        0.00106
                                                         0.00034
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
etable(list('County FE'=crime_county_fe,
          'Year FE'=crime_year_fe,
          'County and Year FE'=crime_county_year_fe),
       cluster='county')
```

```
##
                    County FE
                                      Year FE County and Yea..
## Dependent Var.:
                    Crime Rate
                                    Crime Rate
                                                 Crime Rate
## Prob. Arrest -0.0020 (0.0026) -0.0378*** (0.0103) -0.0011 (0.0026)
## Fixed-Effects: ------
## County
                         Yes
                                         Nο
## Year
                         No
                                         Yes
## S.E.: Clustered by: County by: County
## Observations
                       630
                                       630
                                                       630
## R2
                      0.87076
                                     0.13347
                                                    0.87735
                      0.00106
                                      0.12764
## Within R2
                                                    0.00034
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

We'd normally expect our standard errors to blow up with clustering and we see something similar here. Why is that?

Yes, I know this is a lot on stuff you've only barely experienced before. But you're going to come across these terms when you read papers and I want you to know how to play with them when you're trying to learn by doing.

**Aside on standard errors** We've now seen the various options that **fixest** has for specifying different standard error structures. In short, you invoke either of the se or cluster arguments. Moreover, you can choose to do so either at estimation time, or by adjusting the standard errors for an existing model post-estimation (e.g. with summary.fixest(mod, cluster = ...)). There are two additional points that I want to draw your attention to.

First, if you're coming from another statistical language, adjusting the standard errors post-estimation (rather than always

at estimation time) may seem slightly odd. But this behaviour is actually extremely powerful, because it allows us to analyse the effect of different error structures *on-the-fly* without having to rerun the entire model again. **fixest** is already the fastest game in town, but just think about the implied time savings for really large models. I'm a huge fan of the flexibility, safety, and speed that on-the-fly standard error adjustment offers us. I even wrote a whole blog post about it if you'd like to read more

Second, reconciling standard errors across different software is a much more complicated process than you may realise. There are a number of unresolved theoretical issues to consider — especially when it comes to multiway clustering — and package maintainers have to make a number of arbitrary decisions about the best way to account for these. See here for a detailed discussion. Luckily, Laurent (the **fixest** package author) has taken the time to write out a detailed vignette about how to replicate standard errors from other methods and software packages.<sup>2</sup>

**Multiple estimations** But won't it get tedious writing out all these variations of fixed effects over and over with the feols() repeated? Sure will. That's where the **fixest** package comes in handy.

**fixest** allows you to do multiple estimations in one command and it does is it fast! Why is it so fast? It leverages the demeaning trick mentioned above. If a fixed effect is used in multiple estimations, it saves the outcome variable de-meaned of that fixed effect to use in all the other estimations. That saves a bunch of time!

This is also a really smart big data technique we'll get into more later in the course. It does a task once instead of multiple times to save time and processing power.

Here's a demo using the stepwise sw0() function, which adds fixed effects – starting with none step-by-step:

```
Crime Rate
## Dependent Var.:
                             Crime Rate
                                                                   Crime Rate
##
## Constant
                     0.0432*** (0.0014)
                    -0.0379*** (0.0039) -0.0020 (0.0026) -0.0378** (0.0090)
## Prob. Arrest
## Fixed-Effects:
## County
                                     No
                                                      Yes
                                                                            No
## Year
                                     No
                                                        No
                                                                           Yes
## S.E. type
                                               by: County
                                     IID
                                                                     by: Year
## Observations
                                     630
                                                      630
                                                                           630
## R2
                                0.12856
                                                  0.87076
                                                                      0.13347
## Within R2
                                                  0.00106
                                                                       0.12764
##
##
                    crime_many_fes.4
## Dependent Var.:
                          Crime Rate
##
## Constant
                    -0.0011 (0.0026)
## Prob. Arrest
## Fixed-Effects:
## County
                                 Yes
## Year
                                 Yes
## S.E. type
                          by: County
```

<sup>&</sup>lt;sup>1</sup>To be clear, adjusting the standard errors via, say, summary.fixest() completes instantaneously.

<sup>&</sup>lt;sup>2</sup>If you want a deep dive into the theory with even more simulations, then this paper by the authors of the **sandwich** paper is another excellent resource.

```
## Observations 630
## R2 0.87735
## Within R2 0.00034
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

These results are the same as above. Oh and guess what? You can get a lot more complicated than that!

Wouldnt it be nice to have better names of our variables? We can do that uing a dict, which is just a fancy vector with names.

Here's the basics of how it works.<sup>3</sup> You can specify:

- 1. One or more rhs variable using c(var1, var2, var3)
- 2. One or more fixed effects using the stepwise functions sw(), sw0(), csw(), and csw0().
- 3. One or more independent variable using the stepwise functions sw(), sw0(), csw(), and csw0().
- 4. Different samples using the split or fsplit option.

And here's multiple estimations used to their "fuller" potential:

```
crime_many_estimations <- feols(c(crmrte,prbconv) ~ csw(prbarr, avgsen, polpc) |</pre>
 sw0(county, year, county+year),
 data=crime4,
 fsplit=~urban)
etable(crime_many_estimations[lhs='crmrte',sample=1],title='Crime Rate',notes='Note: Estimates from var
##
                crime_many_estim..1 crime_many_estim..2 crime_many_estim..3
## Sample (urban)
                      Full sample Full sample
                                                          Full sample
## Dependent Var.:
                      Crime Rate
                                        Crime Rate
                                                          Crime Rate
## Constant
                0.0432*** (0.0014) 0.0406*** (0.0026) 0.0397*** (0.0025)
                -0.0379*** (0.0039) -0.0381*** (0.0039) -0.0478*** (0.0039)
## Prob. Arrest
                                    0.0003 (0.0003) 0.0003 (0.0002)
## Avg. Sentence
## polpc
                                                     2.089*** (0.2442)
## Fixed-Effects: -----
## County
                               No
                                                No
## Year
                              No
## S.E. type
                              IID
                                               IID
                              630
                                             630
## Observations
                                                                 630
## R2
                          0.12856
                                           0.13055
                                                              0.22159
## Within R2
##
##
                crime_many_es..4 crime_many_es..5 crime_many_est..6
## Sample (urban)
                  Full sample
                                Full sample
                                               Full sample
                    Crime Rate
                                    Crime Rate
                                                    Crime Rate
## Dependent Var.:
## Constant
## Prob. Arrest
                -0.0020 (0.0026) -0.0019 (0.0027) -0.0043 (0.0028)
                               7.12e-5 (0.0001) 0.0002* (0.0001)
## Avg. Sentence
                                              1.735*** (0.3191)
## polpc
## Fixed-Effects: -----
## County
                           Yes
                                          Yes
                                                          Yes
## Year
                            No
                                           No
  -----
```

<sup>&</sup>lt;sup>3</sup>You can find a more in-depth explanation at the Multiple Estimation vignette.

```
## S.E. type by: County by: County
                  630
                              630
0.87084
## Observations
                                            630
0.89669
                                                   630
                     0.87076
## Within R2
                     0.00106
                                 0.00164
                                               0.20150
##
             crime_many_esti..7 crime_many_esti..8 crime_many_esti..9
## Sample (urban) Full sample Full sample Full sample
## Dependent Var.: Crime Rate Crime Rate Crime Rate
##
## Constant
## Prob. Arrest -0.0378** (0.0090) -0.0379** (0.0088) -0.0478** (0.0086)
## Avg. Sentence
                               0.0002 (0.0002) 0.0002 (0.0002)
                                              2.134* (0.7683)
## polpc
## Fixed-Effects: ------
## County
                         No
                                        No
## Year
                         Yes
                                        Yes
## ______ ______
## S.E. type by: Year by: Year by: Year ## Observations 630 630 630 630 ## R2 0.13347 0.13463 0.22896
## Within R2
                      0.12764
                                    0.12881
                                                   0.22377
##
       crime_many_e..10 crime_many_e..11 crime_many_es..12
## Sample (urban) Full sample Full sample Full sample
                 Crime Rate
## Dependent Var.:
                              Crime Rate
                                            Crime Rate
## Constant
## Prob. Arrest -0.0011 (0.0026) -0.0012 (0.0026) -0.0038 (0.0027)
               -9.4e-5 (0.0001) 5.05e-5 (0.0001)
## Avg. Sentence
                             1.821*** (0.3223)
## polpc
## Fixed-Effects: ------
## County
                        Yes
                                     Yes
                       Yes
                                    Yes
## S.E. type by: County by: County ## Observations 630 630 630
## R2
                    0.87735
                                 0.87746
                                               0.90563
                     0.00034
## Within R2
                                 0.00125 0.23086
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
etable(crime_many_estimations[lhs='prbconv',sample=1],title='Probability of Conviction',notes='Note: Es
             crime_many_esti..1 crime_many_es..2 crime_many_est..3
## Sample (urban) Full sample Full sample Full sample
## Dependent Var.: Prob. Conviction Prob. Conviction Prob. Conviction
## Constant 0.5807*** (0.1385) 0.5018. (0.2628) 0.3759 (0.2338)
## Prob. Arrest
              0.3512 (0.3937) 0.3464 (0.3942) -1.029** (0.3662)
## Avg. Sentence
                      0.0090 (0.0254) 0.0068 (0.0226)
                                     296.5*** (22.92)
## Fixed-Effects: ------
                                No
## County
                          No
## Year
                          No
                                      No
```

## \_\_\_\_\_\_ \_\_\_\_\_

```
IID
                                  IID
630
0.00146
## S.E. type
                                                             IID
                             630
## Observations
                                                            630
                                                       630
0.21216
## R2
                          0.00127
## Within R2
##
               crime_many_es..4 crime_many_es..5 crime_many_es..6
## Sample (urban) Full sample Full sample Full sample
## Dependent Var.: Prob. Conviction Prob. Conviction Prob. Conviction
##
## Constant
## Prob. Arrest -2.941 (2.064) -2.940 (2.074) -3.394 (2.559)
## Avg. Sentence
                               0.0008 (0.0342) 0.0301 (0.0299)
                                            328.8* (142.5)
## polpc
## Fixed-Effects: -----
## County
                           Yes
                                          Yes
## Year
                            No
                                           No
## ______ _____
## S.E. type by: County by: County ## Observations 630 630 630 630 ## R2 0.33114 0.43784 ## Within R2 0.04762 0.04762 0.19955
##
## crime_many_es..7 crime_many_es..8 crime_many_es..9
## Sample (urban) Full sample Full sample Full sample
## Dependent Var.: Prob. Conviction Prob. Conviction Prob. Conviction
## Constant
## Prob. Arrest 0.3665 (0.3999) 0.3571 (0.4001) -1.008 (0.7845)
                  0.0138 (0.0358) 0.0074 (0.0274)
## Avg. Sentence
                                 294.5. (125.8)
## polpc
## Fixed-Effects: ------
## County
                            No
                                           No
## Year
                           Yes
                                          Yes
## S.E. type by: Year by: Year by: Year ## Observations 630 630 630 630 ## R2 0.01355 0.01398 0.22043 ## Within R2 0.00139 0.00182 0.21082
##
           crime_many_e..10 crime_many_e..11 crime_many_e..12
## Sample (urban) Full sample Full sample Full sample
## Dependent Var.: Prob. Conviction Prob. Conviction Prob. Conviction
## Constant
## Prob. Arrest -2.939 (2.077) -2.931 (2.079) -3.388 (2.552)
                                0.0104 (0.0277) 0.0361 (0.0269)
## Avg. Sentence
                                               324.6* (139.9)
## polpc
## Fixed-Effects: -----
                                           Yes
## County
                           Yes
                                                          Yes
                          Yes
                                    Yes
## Year
## ______ _____
## S.E. type by: County by: County by: County ## Observations 630 630 630 630 ## R2 0.34289 0.34305 0.44589
```

```
0.04784 0.04807 0.19709
## Within R2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
etable(crime_many_estimations[lhs='crmrte',sample=2],title='Crime Rate in Urban Areas',notes='Note: Est
             crime_many_estim..1 crime_many_estim..2 crime_many_estim..3
## Sample (urban) 0 0 0
## Dependent Var.: Crime Rate Crime Rate Crime Rate
## Constant 0.0370*** (0.0012) 0.0392*** (0.0023) 0.0385*** (0.0021)
## Prob. Arrest -0.0270*** (0.0034) -0.0267*** (0.0034) -0.0356*** (0.0033)
## Avg. Sentence
                                -0.0003 (0.0002) -0.0003 (0.0002)
## polpc
                                         1.819*** (0.2036)
## Fixed-Effects: -------- ------
## County
                            No
                                            No
## Year
                            No
                                            No
                                   IID
574
0.10240
                    IID
574
## Observations
                       0.10023
                                                       0.21267
## Within R2
        crime_many_es..4 crime_many_es..5 crime_many_est..6
## Sample (urban)
                0 0 0
## Dependent Var.: Crime Rate Crime Rate Crime Rate
## Constant
## Prob. Arrest -0.0017 (0.0026) -0.0017 (0.0026) -0.0041 (0.0027)
               1.95e-5 (0.0001) 0.0002. (0.0001)
## Avg. Sentence
                              1.722*** (0.3264)
## polpc
## Fixed-Effects: ------
## County
                         Yes
                                      Yes
## Year
## S.E. type by: County by: County by: County ## Observations 574 574 574 574 ## R2 0.80689 0.80690 0.84780 ## Within R2 0.00084 0.00088 0.21251
## crime_many_esti..7 crime_many_esti..8 crime_many_esti..9
## Sample (urban)
                0 0 0
## Dependent Var.: Crime Rate Crime Rate Crime Rate
## Constant
## Prob. Arrest -0.0268** (0.0058) -0.0264** (0.0059) -0.0355** (0.0064)
                -0.0004* (0.0001) -0.0004. (0.0002)
## Avg. Sentence
                                               1.865* (0.7238)
## polpc
## Fixed-Effects: ------
## County
                           No
                                          No
                                                          No
                                   Yes
                          Yes
## S.E. type by: Year by: Year by: Year ## Observations 574 574 574 574 ## R2 0.10602 0.10988 0.22501
                                                    574
0.22501
```

```
0.09934 0.10323 0.21922
## Within R2
##
         crime_many_e..10 crime_many_e..11 crime_many_es..12
##
## Sample (urban) 0 0 0
## Dependent Var.: Crime Rate Crime Rate Crime Rate
## Constant
## Prob. Arrest -0.0010 (0.0026) -0.0011 (0.0026) -0.0036 (0.0026)
## Avg. Sentence -0.0001 (0.0001) 3.91e-5 (0.0001)
                                     1.805*** (0.3295)
## polpc
## Fixed-Effects: -----
                                Yes
                         Yes
## County
                                                      Yes
                        Yes
## Year
                                      Yes
                                                      Yes
## S.E. type by: County by: County by: County ## Observations 574 574 574 574 ## R2 0.81420 0.81446 0.85886
                                574
0.81446
                      0.00030
                                   0.00168
## Within R2
                                                 0.24061
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
etable(crime_many_estimations[lhs='crmrte',sample=3],title='Crime Rate in Rural Areas',notes='Note: Est
##
              crime_many_estim..1 crime_many_estim..2 crime_many_estim..3
## Sample (urban)
## Dependent Var.: Crime Rate Crime Rate
                                                      Crime Rate
## Constant 0.1055*** (0.0078) 0.0990*** (0.0100) 0.0775*** (0.0138)
## Prob. Arrest -0.1995*** (0.0368) -0.2033*** (0.0369) -0.2014*** (0.0357)
                                 0.0007 (0.0007) 0.0004 (0.0007)
## Avg. Sentence
## polpc
                                                   11.94* (5.472)
## Fixed-Effects: -------- ------
## County
                            No
                                            No
## Year

    IID
    IID

    56
    56

    0.35269
    0.36588

## S.E. type
## Observations
## R2
                                                        0.41909
## Within R2
       crime_many_est..4 crime_many_est..5 crime_many_est..6
## Sample (urban)
                1 1 1
## Dependent Var.: Crime Rate Crime Rate Crime Rate
## Constant
## Prob. Arrest -0.1903. (0.0823) -0.1871. (0.0801) -0.1811* (0.0741)
                0.0008 (0.0005) 0.0007 (0.0005)
## Avg. Sentence
## polpc
                                              8.647 (6.132)
## Fixed-Effects: -----
## County
                         Yes
                                        Yes
                                                        Yes
## S.E. type by: County by: County ## Observations 56 56 56 56 56 ## R2 0.88722 0.89616 0.90231
```

## ##	Within R2	0.20282	0.26602	0.30946
##		crime_many_estim	7 crime_many_esti	m8 crime_many_estim9
##	Sample (urban)		1	1 1
##	Dependent Var.:	Crime Rat	ce Crime	Rate Crime Rate
##				
	Constant			
		-0.1979*** (0.0149		175) -0.1982*** (0.0137)
	Avg. Sentence		0.0005 (0.0	007) -4.93e-5 (0.0007)
	polpc			13.42** (3.493)
	Fixed-Effects:			
	County	N		No No
	Year	Υe		Yes Yes
##	~			
	S.E. type	by: Yea	•	· ·
	Observations		66	56 56
	R2	0.3999		
##	Within R2	0.3640	0.3	0.43076
##		crime many es 10	crime many es 11	crime_many_es12
	Sample (urban)	1	1	1
	_	Crime Rate	Crime Rate	=
##	Joponadno (ar.)	0111110 114400	01 21110 10000	0220
##	Constant			
##	Prob. Arrest	-0.1694. (0.0771)	-0.1723. (0.0733)	-0.1709* (0.0703)
##	Avg. Sentence		0.0002 (0.0005)	3.84e-5 (0.0006)
##	polpc			11.27 (6.369)
##	Fixed-Effects:			
##	County	Yes	Yes	Yes
##	Year	Yes	Yes	Yes
##				
	S.E. type	by: County	•	by: County
	Observations	56	56	
	R2	0.93501	0.93554	
	Within R2	0.23564	0.24188	0.30840
	Cimif and a	0	0.01 1#1.0 0F 1.1	0 1 1 1 1
##	Signii. codes: (	0 '***' 0.001 '**'	0.01 ** 0.05 '.'	0.1 1

**Concept check** In our second table, the probability of conviction regressed on probability of arrest is almost certainly not causal. It is a pretty bogus regresion since both that are heavily affected by government decisions.

Can we say any of the above are causal? What would we need to assume?

# Difference-in-differences

One of the most popular uses of fixed effects is to implement difference-in-difference designs we've discussed. Here's a quick visualization. Let's walk through an example that uses the National Supported Work Demonstration dataset that Lalonde (1986) published on.<sup>4</sup>

### Lalonde (1986)

The neat thing about these data is Lalonde (and a follow-up by Dehejia and Wahba (2022)) compare experimental to non-experimental data. The experimental data is from a randomized control trial (RCT) of a job training program. The non-experimental data is a random sample of US households.

<sup>&</sup>lt;sup>4</sup>I take this example from an activity devised by Scott Cunningham and Kyle Butts.

#### **Earned Income Tax Credit**

The Earned Income Tax Credit (EITC) was increased for parents in 1993. The EITC is a tax credit for low-income workers. It is a refundable tax credit, meaning that if the credit exceeds the amount of taxes owed, the excess is returned to the taxpayer. The EITC is designed to supplement wages for low-to-moderate income workers. The amount of the credit depends on income and number of children.

The EITC is also designed to incentivize work. It initially increases as earnings increase, before leveling off and falling once earnings reach a threshold level and the worker transitions out of "low-income."

Effectively at low-income levels, the EITC increases the dollars earned from working – either on the intensive margin (one more hour) or extensive margin (working vs. not working). But does it effect labor supply?

Let's focus on how this affects labor supply of single mothers who are the primary beneficiaries of . This example is borrowed from Nick Huntington-Klein and pulled from work by Bruce Meyer (2002).

We walked through this example in the lecture, but let's do it again.

#### Diff-in-diff with data

Let's load in the data.

We do not have an individual identifier in these data, so we can't add an individual fixed effect. We can add other fixed effects if we believe there is endogenous variation in the treatment between the groups of the fixed effect.

Still, let's work through how to visualize the data to check for no pre-trends and treatment effects change over time. We checked averages for our two groups before – not bad!

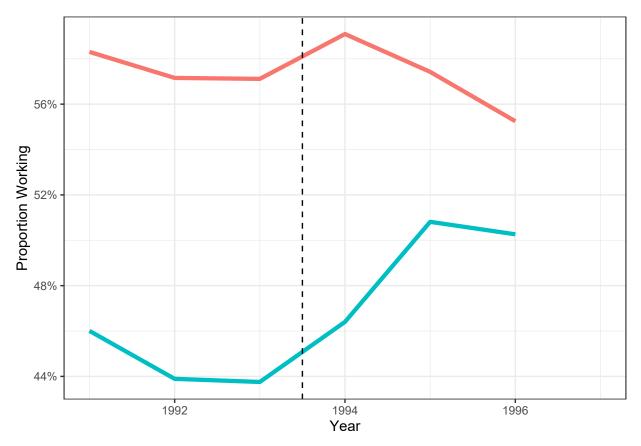
```
## `summarise()` has grouped output by 'year', 'treated'. You can override using
## the `.groups` argument.

## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.

## i Please use `linewidth` instead.

## This warning is displayed once every 8 hours.

## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
```



But the lines are a little far apart, so it makes it tricky to visualize the difference. And we don't know the confident interval on the difference between these. Let's try to get that!

**Introducing** the i() function. This handy little guy is a function that creates an interaction term. It's a little tricky to use, but it's worth it. Basically, what you do is you feed it a factor variable, an interacted variable, then a reference value of the factor variable – all coefficients will relative to the level when the factor variable equals the reference value.

```
## OLS estimation, Dep. Var.: work
## Observations: 13,746
## Fixed-effects: year: 6, treated: 2
## Standard-errors: Heteroskedasticity-robust
##
               Estimate Std. Error t value Pr(>|t|)
## year::1995:treated 0.067488
                      0.030154 2.238086 0.0252314 *
## year::1996:treated 0.083754
                      0.030552 2.741312 0.0061274 **
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## RMSE: 0.496477
               Adj. R2: 0.012584
             Within R2: 0.001075
```

So what does this output mean? Well it tells us the difference between the treated and untreated groups over time! But relative to when? It is all relative to the reference value, when year=1993. That is often called the "omitted" year. I chose the period just before the EITC expansion.

**Challenge**: What regression did we just run? Write it out. We have a year fixed effect and a treated fixed effect. Note the treated fixed effect is defined across individuals because we do not have an individual identifier!

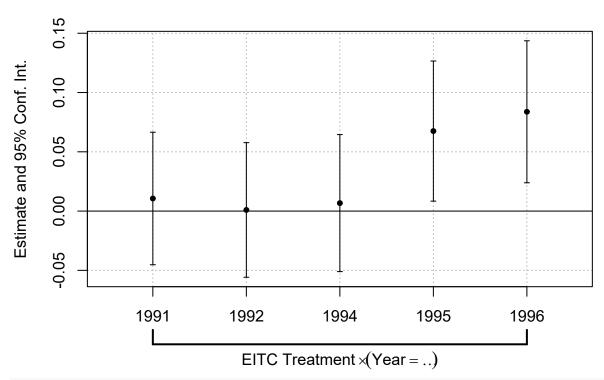
But how do we visualize this? We have a few options. They both work the same way as the examples with coefplot()

and ggplot() above though. Note, I introduce a dict to improve the labels.

The plots show that prior to 1994, the labor supply decisions of women with and without children were on a similar trend (though it is a fairly short trend).

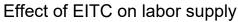
```
coefplot(eitc_did,dict=c('treated'='EITC Treatment','year'='Year'))
```

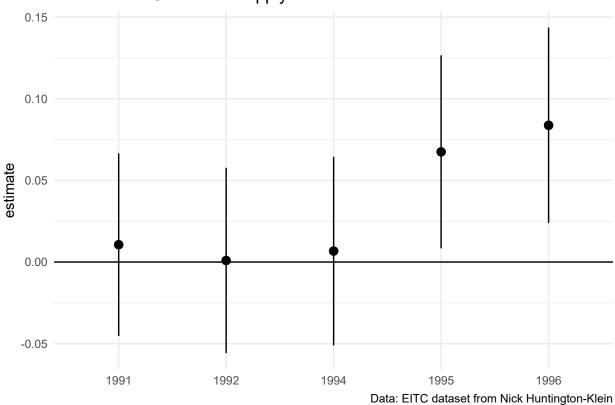
# Effect on work



```
coef_eitc_did <- tidy(eitc_did, conf.int = TRUE) %>%
  mutate(year=str_extract(term,'\\d{4}')) # Regular expressions to extract year

ggplot(coef_eitc_did, aes(x=year, y=estimate, ymin=conf.low, ymax=conf.high)) +
  geom_pointrange() +
  geom_hline(yintercept = 0, col = "black") +
  labs(
    title = "Effect of EITC on labor supply",
    caption = "Data: EITC dataset from Nick Huntington-Klein"
    ) +
  theme(axis.title.x = element_blank())
```

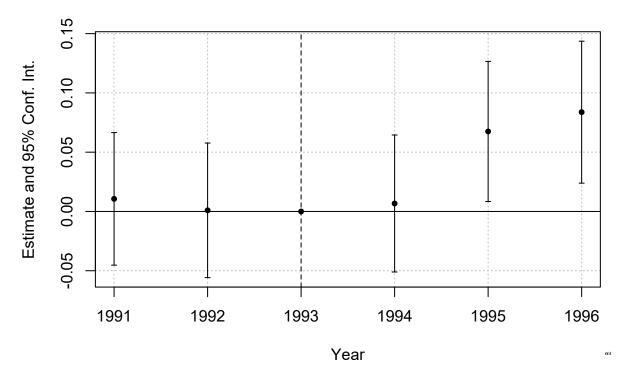




And then we also have iplot(), which works directly with i(). It works well for quick visualization, but it can be a little clunky to make as beautiful plots as you can with ggplot.

iplot(eitc\_did,dict=c('treated'='EITC Treatment','year'='Year'))

# Effect on work



#### **Further resources**

- Ed Rubin has outstanding teaching notes for econometrics with R on his website. This includes both undergradand graduate-level courses. Seriously, check them out.
- Several introductory texts are freely available, including *Introduction to Econometrics with R* (Christoph Hanck *et al.*), *Using R for Introductory Econometrics* (Florian Heiss), and *Modern Dive* (Chester Ismay and Albert Kim).
- Tyler Ransom has a nice cheat sheet for common regression tasks and specifications.
- Itamar Caspi has written a neat unofficial appendix to this lecture, *recipes for Dummies*. The title might be a little inscrutable if you haven't heard of the recipes package before, but basically it handles "tidy" data preprocessing, which is an especially important topic for machine learning methods. We'll get to that later in course, but check out Itamar's post for a good introduction.
- I promised to provide some links to time series analysis. The good news is that R's support for time series is very, very good. The Time Series Analysis task view on CRAN offers an excellent overview of available packages and their functionality.
- Lastly, for more on visualizing regression output, I highly encourage you to look over Chapter 6 of Kieran Healy's *Data Visualization: A Practical Guide*. Not only will learn how to produce beautiful and effective model visualizations, but you'll also pick up a variety of technical tips.