## 1 CP model

N\_bins: the number of bins given N\_items: the number of items given

 $W_j, H_j, C_j$ : the width, height, and cost of bin j, respectively

 $w_i, h_i$ : the width, height of item i, respectively

### 1.1 Decision Variables

\*  $X_{ij} = 1$ : item i packed in bin j

$$\Rightarrow \sum_{i=1}^{\text{N.items}} X_{ij} \geq 1 \Longleftrightarrow Z_j = 1$$
: bin j has been used

\*  $R_i = 1$ : item i rotated 90 degree

#### Item's Coordinate:

 $l_i, r_i, b_i, t_i$ : left, right, bottom and top coordinates of item i

\* First way to approach:

- if item i not rotated:  $R_i = 0$ 

$$\Rightarrow \begin{cases} r_i = l_i + w_i \\ t_i = b_i + h_i \end{cases}$$

- if item i rotated:  $R_i = 1$ 

$$\Rightarrow \begin{cases} r_i = l_i + h_i \\ t_i = b_i + w_i \end{cases}$$

\* Another way to approach:

- if item i not rotated:  $R_i = 0$ 

$$\Rightarrow \begin{cases} w_i = w_i \\ h_i = h_i \end{cases}$$

- if item i rotated:  $R_i = 1$ 

$$\Rightarrow \begin{cases} w_i = h_i \\ h_i = w_i \end{cases}$$

#### 1.2 Constraints

#### 1.2.1 Each item has to be packed in exactly 1 bin:

$$\sum_{j=1}^{\text{N\_bins}} X_{ij} = 1 \text{ for } i \text{ in N\_items}$$

#### 1.2.2 No two items overlap:

if 
$$X_{i_1j} = X_{i_2j} = 1$$

$$r_{i_1} \leq l_{i_2}$$
 or  $r_{i_2} \leq l_{i_1}$  or  $t_{i_1} \leq b_{i_2}$  or  $t_{i_2} \leq b_{i_1}$ 

#### 1.2.3 Items cannot exceed the bin:

if 
$$X_{ij} = 1$$

$$\Rightarrow \begin{cases} w_i \le r_i \le W_j \\ h_i \le t_i \le H_j \end{cases}$$

1

# 1.3 Objective Function

$$\mathbf{minimize} \sum_{j=1}^{\mathrm{N\_bins}} Z_j * C_j$$