

# SCALABILITY AND ROBUSTNESS OF KANs APPLIED TO REINFORCEMENT LEARNING

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## 1. INTRODUCTION

Kolmogorov-Arnold Networks (KANs) utilize the Kolmogorov-Arnold representation theorem unlike MLPs, which base their structure on the universal approximation theorem. KANs are a combination of splines (optimal for low-dimensional functions) and MLPs (optimal for feature learning).

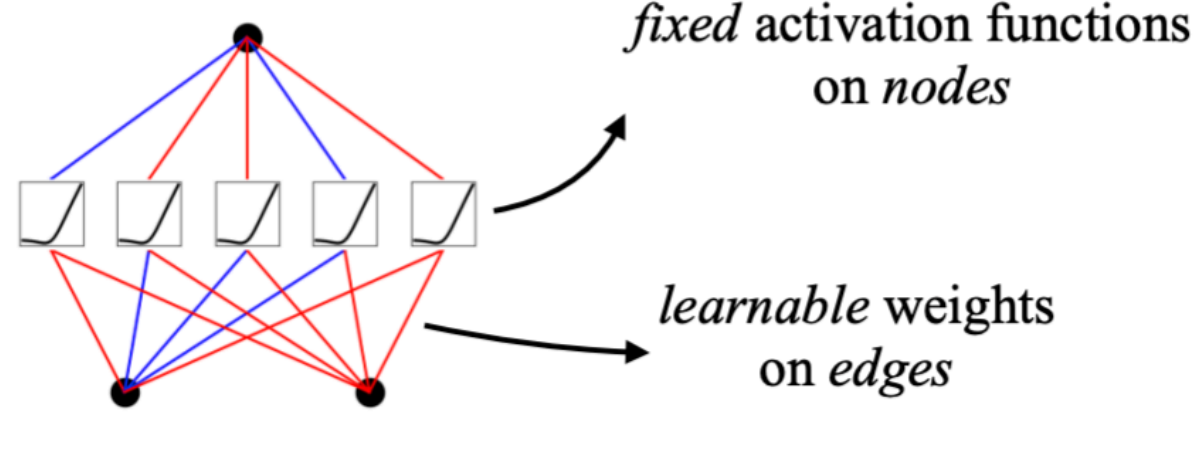
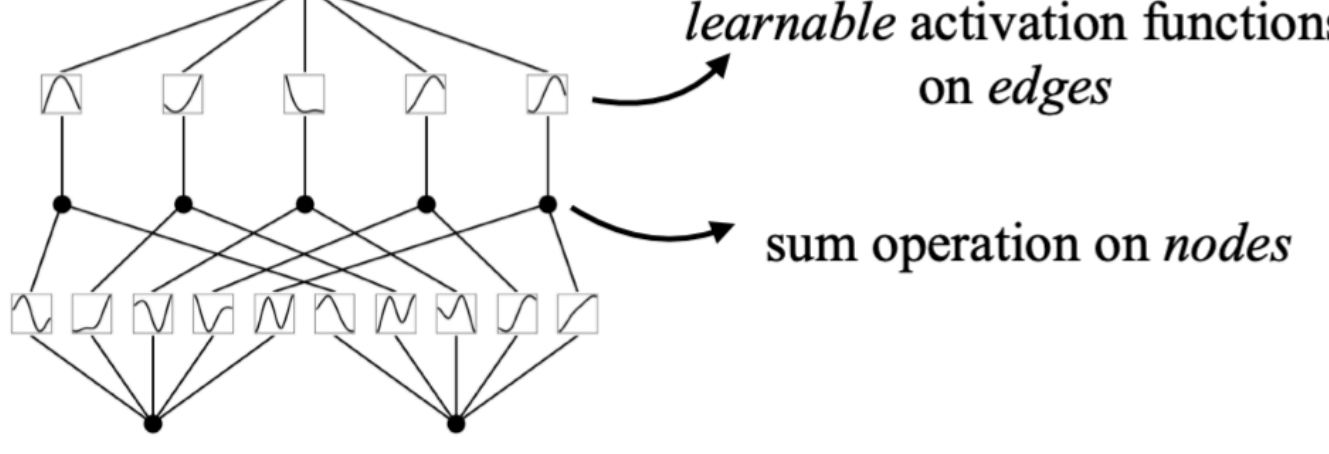
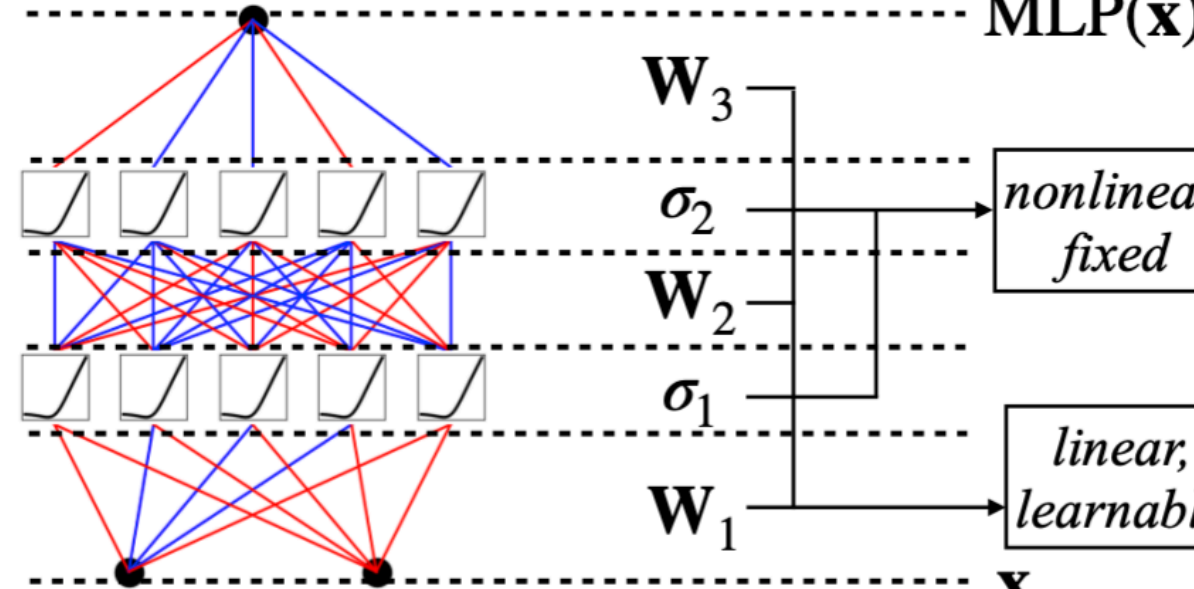
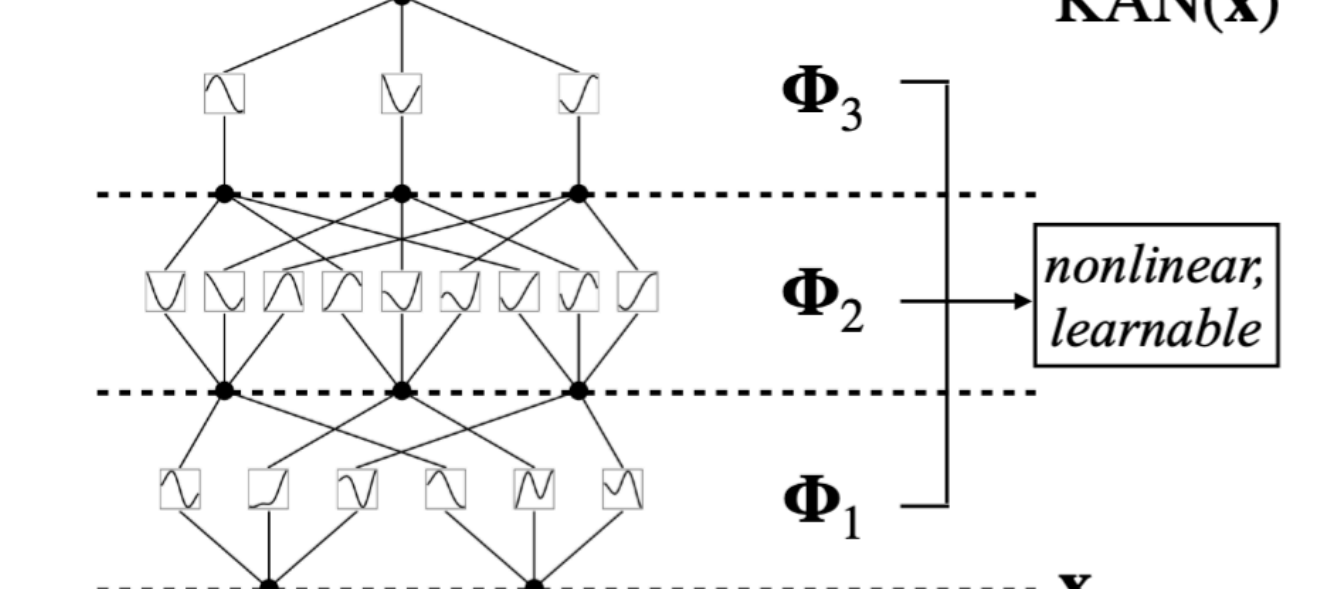
Model	Multi-Layer Perceptron (MLP)	Kolmogorov-Arnold Network (KAN)
Theorem	Universal Approximation Theorem	Kolmogorov-Arnold Representation Theorem
Formula (Shallow)	$f(\mathbf{x}) \approx \sum_{i=1}^{N(e)} a_i \sigma(\mathbf{w}_i \cdot \mathbf{x} + b_i)$	$f(\mathbf{x}) = \sum_{q=1}^{2n+1} \Phi_q \left( \sum_{p=1}^n \phi_{q,p}(x_p) \right)$
Model (Shallow)	(a) 	(b) 
Formula (Deep)	$\text{MLP}(\mathbf{x}) = (\mathbf{W}_3 \circ \sigma_2 \circ \mathbf{W}_2 \circ \sigma_1 \circ \mathbf{W}_1)(\mathbf{x})$	$\text{KAN}(\mathbf{x}) = (\Phi_3 \circ \Phi_2 \circ \Phi_1)(\mathbf{x})$
Model (Deep)	(c) 	(d) 

Fig1. Multi-Layer Perceptrons (MLPs) vs. Kolmogorov-Arnold Networks (KANs) [1]

## 2. METHODS

KANs [2] are integrated into the reinforcement learning framework by replacing the MLP component of Deep Q-Networks (DQN), resulting in the Kolmogorov-Arnold Q-Network (KAQN) [3].

The three points of interest were:

1. Comparing the performance of KANs and MLPs in environments with **varying numbers of distractors**.
2. Evaluating how KANs compare against MLPs in environments with **high complexity**.
3. Investigating how KANs fare compared to MLPs in **non-physics-driven environments**, given that KANs proved effective in physics-driven problems as shown in the original paper [1].

The code of the KANrl repository [3] was modified to implement continuous-space environments and **DDPG** [4].

To mitigate the lengthy processing durations of PyKAN [2], **EfficientKAN** [5] was adopted to ensure more time-efficient execution.

## 3. EXPERIMENTS

### VARYING DISTRACTORS

The Ant-v4 environment [6] was used to experiment with a varying number of distractors. The distractors are noise inputs that do not contribute to the Ant's current state.

The KAN has  $(x+n, 256, 1)$  architecture where  $x$  is the shape of the original observation space and  $n$  distractors are sampled from Gaussian noise.

### HIGH COMPLEXITY

An arbitrary number of legs are added to the Ant using the MorphingAnt [8] environment to increase complexity. The legs are distributed symmetrically around the torso. The shape of the observation space scales with the number of legs  $n$  as:  $observations = 11 + (6 * n)$

## 4. RESULTS

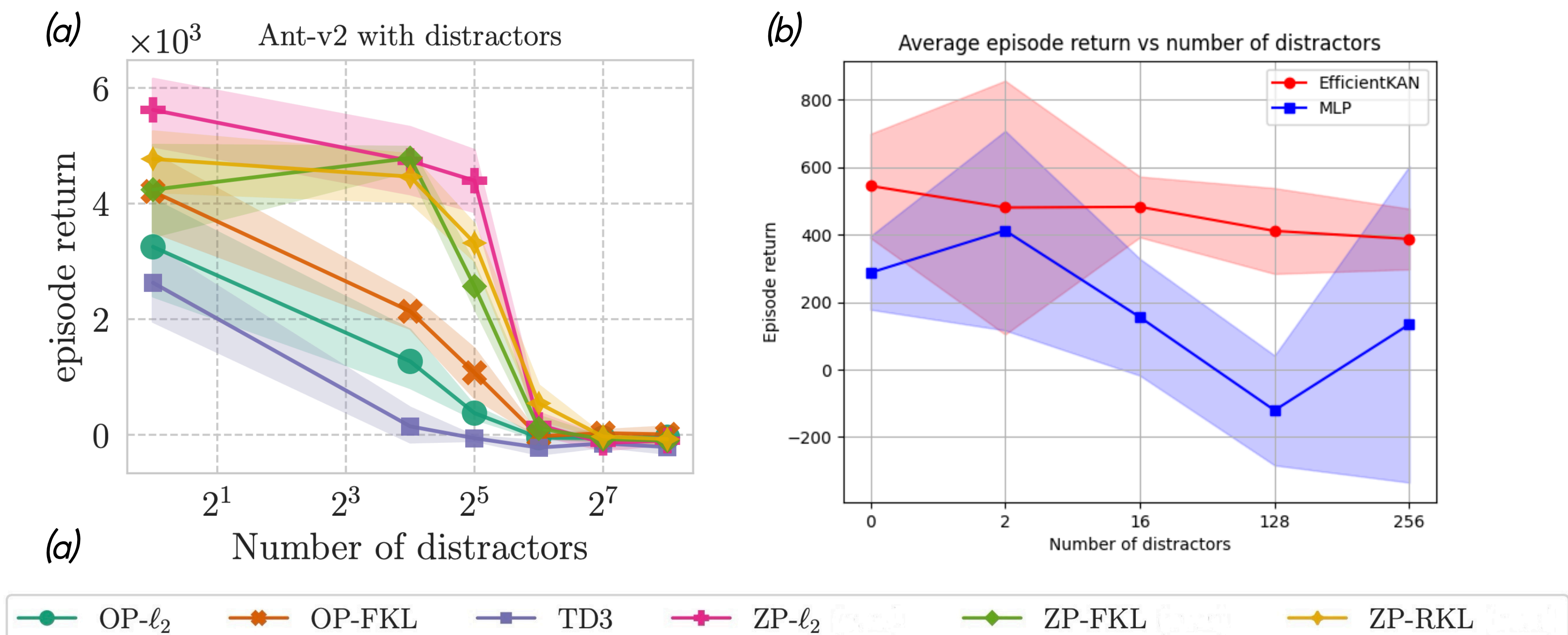


Fig2. Experiments with distractors. (a) Images from Ni, Tianwei et al. [7], (b) Own experiments with KAN and MLP, averaged over 3 seeds (0, 1, 2). KANs appear to be superior to the other baselines and MLP.

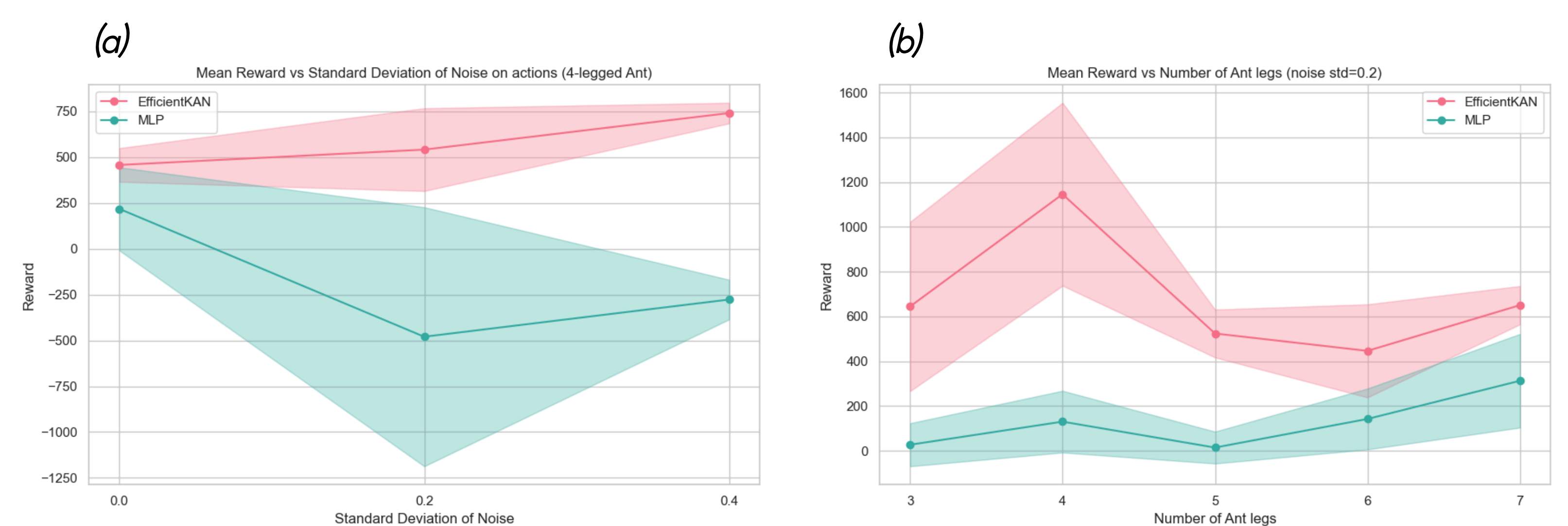


Fig 3. MorphingAnt experiments [8] tested with a fixed seed (0).

- (a) Impact of noise applied to actions on 4-legged Ant training; EfficientKAN improves with noise.  
(b) Training with different leg counts and fixed noise (std=0.2), using healthy\_reward=0.1 to promote movement. All tests use healthy\_reward=1.0 to ensure comparability.

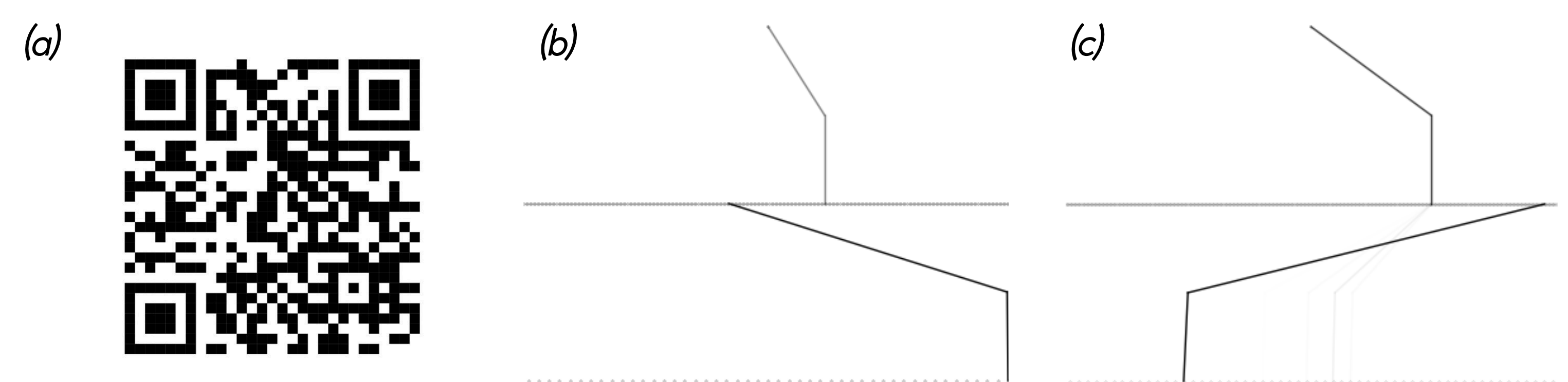


Fig 4. MorphingAnt [8] trained with noise std=0.2 and healthy\_reward=0.1

- (a) Video of episode renders of 4-legged Ant (b) Interpretable graph of the 4-legged Ant KAN with (47, 256, 1) architecture. (c) Interpretable graph of the 5-legged Ant KAN with (56, 512, 1) architecture. These graphs reveal which inputs are most useful for the calculations, making it easier to understand the results.

## 5. CONCLUSION

- **Performance with distractors:** KANs exhibit more stable performance over traditional MLP-based Q-networks with increasing distractors in the environment.
- **Performance in complex environments:** KANs consistently outperform MLPs in increasingly complex environments, with both networks using identical configurations in each case.
- **Robustness:** KANs perform well in continuous environments, making them versatile for various reinforcement learning applications.

### Limitations:

- **Computational Complexity:** Higher complexity leads to greater computational demands and longer training times. Further research is needed for large, dynamic environments.
- **Adaptation Difficulties:** The complex base code complicates adaptation to other environments, which prevented the completion of experiments in non-physics environments.

## REFERENCES

- [1] Liu, Wang, et al. "Kan: Kolmogorov-arnold networks." arXiv:2404.19756 (2024). [2] KAN Github: <https://github.com/KindXiaoming/pykan> [3] KANrl github: <https://github.com/riiswa/kanrl> [4] Lillicrap, Timothy P., et al. "Continuous control with deep reinforcement learning." arXiv preprint arXiv:1509.02971 (2015). [5] EfficientKAN github: <https://github.com/Blealtan/efficient-kan> [6] Ant-v4: <https://gymnasium.farama.org/environments/mujoco/ant/> [7] Ni, Tianwei, et al. "Bridging State and History Representations: Understanding Self-Predictive RL." arXiv preprint arXiv:2401.08898 (2024). [8] MorphingAnt github: [https://github.com/brandontrabucco/morphing-agents/blob/master/morphing\\_agents/mujoco/ant/env.py](https://github.com/brandontrabucco/morphing-agents/blob/master/morphing_agents/mujoco/ant/env.py) [9] Our github link: <https://github.com/BeatrizFernandezLarrubia/kanrl/tree/main>