

Tópicos de Matemática Elementar I

Parte 1 - Conjunto dos Números Racionais

Equações e Inequações de 1ª ordem

Frações

Exercício 1

$$1.) 24x - 3 = 2x \quad (=)$$

$$(\Rightarrow) 24x = 2x + 3 \quad (=)$$

$$(\Rightarrow) 24x - 2x = 3 \quad (=)$$

$$(\Rightarrow) 22x = 3 \quad (=)$$

$$(\Rightarrow) x = \frac{3}{22} //$$

$$2.) -x + 3 + 2x = 4x + 15 \quad (=)$$

$$(\Rightarrow) -x + 3 + 2x - 4x = 15 \quad (=)$$

$$(\Rightarrow) -x + 2x - 4x = 15 - 3 \quad (=)$$

$$(\Rightarrow) -3x = 12 \quad (=)$$

$$(\Rightarrow) -x = \frac{12}{3} \quad (=)$$

$$(\Rightarrow) x = -\frac{12}{3} \quad (=: 3) \quad (=)$$

$$(\Rightarrow) x = -4 //$$

$$3.) x + 1 = x - 1 \quad (=)$$

$$(\Rightarrow) x - x + 1 = -1 \quad (=)$$

$$(\Rightarrow) x - x = -1 - 1 \quad (=)$$

$$(\Rightarrow) x - x = -2 \quad (=)$$

$$(\Rightarrow) 0 = -2 // \text{ Falso}$$

$$4.) x = x \quad (=)$$

$$(\Rightarrow) x - x = 0 \quad (=)$$

$$(\Rightarrow) 0 = 0 // \text{ Verdadeiro}$$

Exercício 2

1.) $2x + 1 \leq 24$ (=)

(=) $2x \leq 24 - 1$ (=)

(=) $2x \leq 23$ (=)

(=) $x \leq \frac{23}{2}$ // $CS =]-\infty, \frac{23}{2}]$

2.) $-x + 3 \geq x + 1$ (=)

(=) $-x + 3 - x \geq +1$ (=)

(=) $-x - x \geq 1 - 3$ (=)

(=) $-2x \geq -2$ (=)

(=) $\frac{-2x}{2} \geq \frac{-2}{2}$ (=)

(=) $-x \geq -1$ (=)

(=) $x \leq 1$ // $CS =]-\infty, 1]$

3.) $\frac{x}{3} + 1 < x - 1$ (=)

(=) $\frac{x}{3} - x + 1 < -1$ (=)

(=) $\frac{x}{3} - x < -1 - 1$ (=)

(=) $3 \cdot \frac{1}{3} \cdot x - x < -1 - 1$ (=)

(=) $x - 3x < -3 - 3$ (=)

(=) $-2x < -6$ (=)

(=) $2x > 6$ (=)

(=) $x > \frac{6}{2}$ (=)

(=) $x > 3$ // $CS =]3, +\infty[$

CA

$$3 \times \frac{1}{3} = \frac{3}{3} = 1$$

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Exercício 3

$$1.) \frac{12}{7} - \frac{3}{7} = \frac{9}{7}$$

$$2.) \frac{10}{3} - \frac{8}{3} + \frac{2}{3} = \frac{4}{3} //$$

$$3.) -\frac{2}{9} + \frac{3}{4} = -\frac{8}{36} + \frac{27}{36} = \frac{19}{36} //$$

$$4.) \frac{1}{2} \times \frac{25}{3} = \frac{1 \times 25}{2 \times 3} = \frac{25}{6} //$$

Exercício 4

$$1.) \frac{7}{6} + x = \frac{11}{6} \quad (=)$$

$$(\Rightarrow) x = \frac{11}{6} - \frac{7}{6} \quad (=)$$

$$(\Rightarrow) x = \frac{4}{6} \quad (=)$$

$$(\Rightarrow) x = \frac{2}{3} //$$

$$2.) \frac{3}{4} + x = 1 \quad (=)$$

$$(\Rightarrow) \frac{3}{4} + x = \frac{4}{4} \quad (=)$$

$$(\Rightarrow) x = \frac{4}{4} - \frac{3}{4} \quad (=)$$

$$(\Rightarrow) x = \frac{1}{4} //$$

$$3.) x - \frac{2}{9} = \frac{3}{4} \quad (=)$$

$$(\Rightarrow) x = \frac{3}{4} + \frac{2}{9} \quad (=)$$

$$(\Rightarrow) x = \frac{27}{36} + \frac{8}{36} \quad (=)$$

$$(\Rightarrow) x = \frac{35}{36} //$$