

aaa

Def: x e y são directamente
proporcionais se $\frac{x}{y}$ é const.

Def: x e y são inversamente
proporcionais se $xy = \text{const.}$

Casos notáveis

$$\begin{aligned} \bullet \quad (\underbrace{xy}_a + \underbrace{2}_b)^2 &= \underbrace{(xy)^2}_{a^2} + \underbrace{2xy \cdot 2}_{2 \cdot a \cdot b} + \underbrace{2^2}_{b^2} = \\ &= x^2 \cdot y^2 + 4xy + 4 \end{aligned}$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a+b)(a-b) = a^2 - b^2$$

$$\bullet \quad \underbrace{16x^4}_{a^2} - \underbrace{8x^2 \cdot 2y}_{-2ab} + \underbrace{4y^2}_{b^2} = \left(\underbrace{4x^2}_a - \underbrace{2y}_b \right)^2$$

$$a^2 = 16x^4 \Leftrightarrow a^2 = 4^2(x^2)^2 \Leftrightarrow a^2 = (4x^2)^2 \Leftrightarrow a = 4x^2$$

$$b^2 = 4y^2 \Leftrightarrow b^2 = 2^2 \cdot y^2 \Leftrightarrow b^2 = (2y)^2 \Leftrightarrow b = 2y$$

$$-2ab = -2 \cdot 4x^2 \cdot 2y = -16x^2y \quad \checkmark$$

$$-x > 2$$

$$x < -2$$

1

$$D = \frac{1}{6} - \frac{x}{2}, 4$$

$$\Leftrightarrow 4x = 1$$