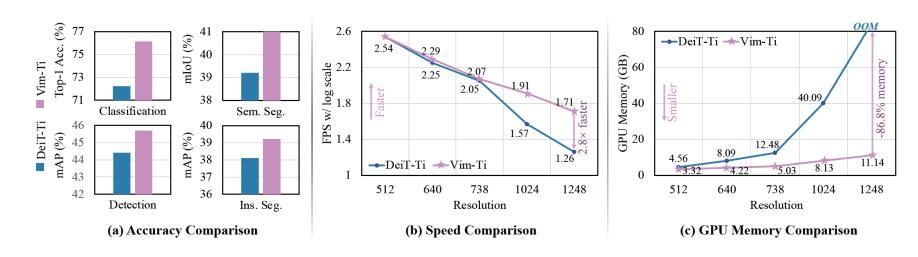
# Vision Mamba: Efficient Visual Representation Learning with Bidirectional State Space Model

Authors: Lianghui Zhu, Bencheng Liao, Qian Zhang, Xinlong Wang, Wenyu Liu, Xinggang Wang

## **Motivation**

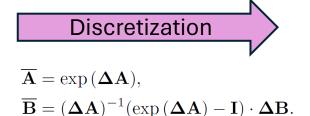
- Introducing Vision Mamba (Vim) with Bidirectional SSM
- Improving existing SOTA Transformer based models (DeiT) for high resolution in terms of:
  - Memory efficiency
  - Performance in Vision Tasks



# State Space Models (SSM)

They are inspired in basic 1-D continuous differential models for sequences

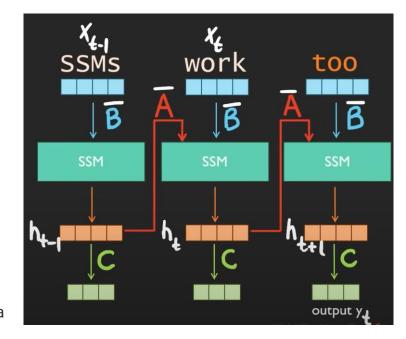
$$h'(t) = \mathbf{A}h(t) + \mathbf{B}x(t),$$
  
 $y(t) = \mathbf{C}h(t).$ 



**Learnable parameters:** Step size ( $\Delta$ ), B, C **Method:** Convolution (Efficient in GPU)

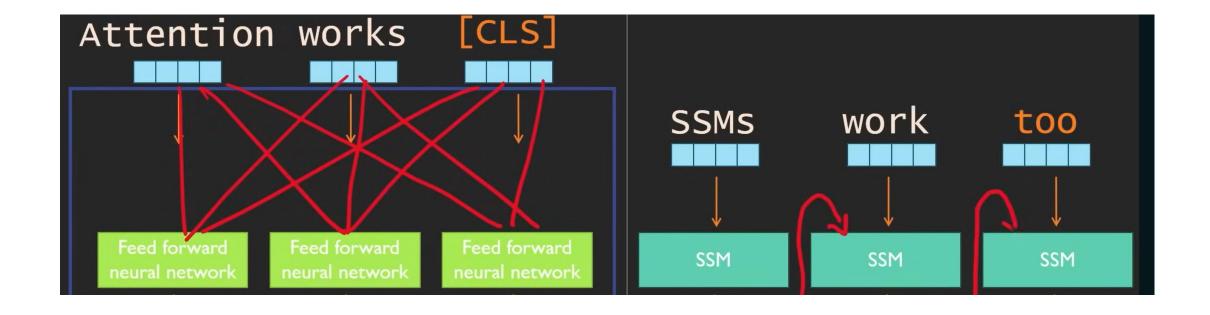
$$\overline{\mathbf{K}} = (\mathbf{C}\overline{\mathbf{B}}, \mathbf{C}\overline{\mathbf{A}}\overline{\mathbf{B}}, \dots, \mathbf{C}\overline{\mathbf{A}}^{\mathtt{M}-1}\overline{\mathbf{B}}),$$
  
 $\mathbf{y} = \mathbf{x} * \overline{\mathbf{K}},$ 

$$h_t = \overline{\mathbf{A}}h_{t-1} + \overline{\mathbf{B}}x_t,$$
$$y_t = \mathbf{C}h_t.$$



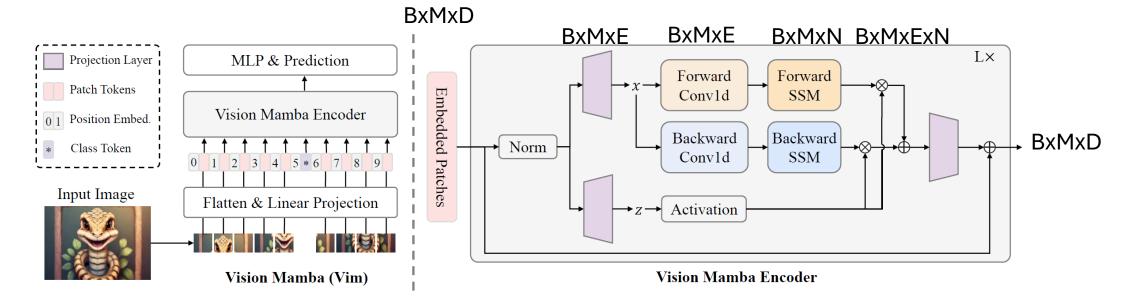
<sup>\*</sup>Images: AICoffeeBreak, (2024, April 08). MAMBA and State Space Models explained | SSM explained [Video]. YouTube. URL: https://www.youtube.com/watch?v=vrF3MtGwD0Y&t=1s&ab\_channel=AICoffeeBreakwithLetitia

## SSMs vs. Transformers (Efficiency)



<sup>\*</sup>Images: AICoffeeBreak, (2024, April 08). MAMBA and State Space Models explained | SSM explained [Video]. YouTube. URL: https://www.youtube.com/watch?v=vrF3MtGwD0Y&t=1s&ab\_channel=AICoffeeBreakwithLetitia

## Vision Mamba



$$\mathbf{T}_0 = [\mathbf{t}_{cls}; \mathbf{t}_p^1 \mathbf{W}; \mathbf{t}_p^2 \mathbf{W}; \cdots; \mathbf{t}_p^J \mathbf{W}] + \mathbf{E}_{pos},$$
 L: Num  $\mathbf{T}_l = \mathbf{Vim}(\mathbf{T}_{1-1}) + \mathbf{T}_{1-1},$  E: Expand  $\hat{p} = \mathbf{MLP}(\mathbf{f}),$  N: SSM

	Tiny	Small
L: Number of vim blocks	24	24
D: Hidden state dimension	192	384
E: Expanded state dimension	384	768
N: SSM dimensión	16	16

Method	image size	#param.	ImageNet top-1 acc.			
	Convnet	ts				
ResNet-18	$224^{2}$	12M	69.8			
ResNet-50	$224^{2}$	25M	76.2			
ResNet-101	$224^{2}$	45M	77.4			
ResNet-152	$224^{2}$	60M	78.3			
ResNeXt50-32×4d	$224^{2}$	25M	77.6			
RegNetY-4GF	$224^{2}$	21M	80.0			
Transformers						
ViT-B/16	$384^{2}$	86M	77.9			
ViT-L/16	$384^{2}$	307M	76.5			
DeiT-Ti	$224^{2}$	6M	72.2			
DeiT-S	$224^{2}$	22M	79.8			
DeiT-B	$224^{2}$	86M	81.8			
	SSMs					
S4ND-ViT-B	$224^{2}$	89M	80.4			
Vim-Ti	$224^{2}$	7M	76.1			
Vim-Ti <sup>†</sup>	$224^{2}$	7M	78.3 +2.2			
Vim-S	$224^{2}$	26M	80.5			
Vim-S <sup>†</sup>	$224^{2}$	26M	81.6 +1.1			

Table 1. Comparison with different backbones on ImageNet-1K validation set.  $^{\dagger}$  represents the model is fine-tuned with our long sequence setting.

#### **ImageNet-1K** Dataset:

- 1.28M training images
- **50K validation** images
- 1,000 categories

**Long Sequence Fine-Tuning**: Double of patches than DeiT with the same size (stride 8, 16x16).

Method	image	#param.	ImageNet
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	Convnet	ts	
ResNet-18	$224^{2}$	12M	69.8
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#### Results:

3.9 points higher for Vim-Tiny over DeiT-Tiny

+3.9

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- Vim-S achieves results similar to DeiT-B with LSFT

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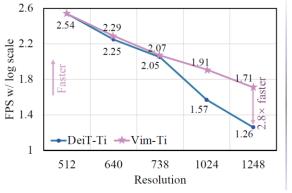
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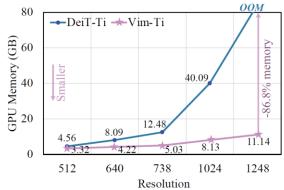
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- 3.9 points higher for Vim-Tiny over DeiT-Tiny
- 0.7 points higher for Vim-Small over DeiT-Small
- Vim-S achieves results similar to DeiT-B with LSFT
- 1248×1248: Vim is 2.8× faster than DeiT and saves 86.8% GPU memory in batch inference





Method	Backbone	image size	#param.	val mIoU
DeepLab v3+	ResNet-101	$ \begin{array}{ c c c } 512^{2} \\ 512^{2} \\ 512^{2} \end{array} $	63M	44.1
UperNet	ResNet-50		67M	41.2
UperNet	ResNet-101		86M	44.9
UperNet	DeiT-Ti	$\begin{vmatrix} 512^2 \\ 512^2 \end{vmatrix}$	11M	39.2
UperNet	DeiT-S		43M	44.0
UperNet	Vim-Ti	$512^2$ $512^2$	13M	41.0
UperNet	Vim-S		46M	44.9

Table 2. Results of semantic segmentation on the ADE20K val set.

#### **ADE20K** Dataset:

- **20K training** images
- **2K validation** images
- 150 categories
- **UperNet** framework

Method	Backbone	image size	#param.	val mIoU	A
DeepLab v3+ UperNet UperNet	ResNet-101 ResNet-50 ResNet-101	$ \begin{array}{ c c c } 512^{2} \\ 512^{2} \\ 512^{2} \end{array} $	63M 67M 86M	44.1 41.2 44.9	
UperNet UperNet	DeiT-Ti DeiT-S	$512^2$ $512^2$	11M 43M	39.2 44.0	+1.8
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#### **Results:**

• 1.8 mIoU higher for Vim-Ti over DeiT-Ti

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- 1.8 mloU higher for Vim-Ti over DeiT-Ti
- 0.9 mloU higher for Vim-S over DeiT-S
- Vim-S similar to ResNet-101 but 2x fewer parameters

# Experiments: Object Detection and Instance Segmentation

Backbone	AP <sup>box</sup>	AP <sub>50</sub> <sup>box</sup>	AP <sub>75</sub> <sup>box</sup>	AP <sub>s</sub> box	AP <sub>m</sub> box	$AP_l^{box}$
DeiT-Ti	44.4	63.0	47.8	26.1	47.4	61.8
Vim-Ti	45.7	63.9	49.6	26.1	49.0	63.2
Backbone	AP <sup>masl</sup>	k AP <sub>50</sub> <sup>masl</sup>	k AP <sub>75</sub>	AP <sub>s</sub> <sup>mas</sup>	k AP <sub>m</sub> asl	k AP <sub>l</sub> mask
Backbone DeiT-Ti	AP <sup>masl</sup> 38.1	k AP <sub>50</sub> AP <sub>50</sub> 59.9	AP <sub>75</sub> AP <sub>75</sub> 40.5	AP <sub>s</sub> <sup>mas</sup> 18.1	k AP <sub>m</sub> <sup>masl</sup> 40.5	<sup>k</sup> AP <sub>1</sub> <sup>mask</sup> 58.4

Table 3. Results of object detection and instance segmentation on the COCO val set using Cascade Mask R-CNN [4] framework.

#### COCO 2017 Dataset:

- 118K training images
- **5K validation** images
- Cascade Mask R-CNN base framework

# Experiments: Object Detection and Instance Segmentation

Backbone	AP <sup>box</sup>	AP <sub>50</sub> <sup>box</sup>	AP <sub>75</sub> <sup>box</sup>	AP <sub>s</sub> box	$AP_{m}^{box}$	$AP_l^{box}$
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Backbone	AP <sup>mask</sup>	AP <sub>50</sub>	AP <sub>75</sub>	AP <sub>s</sub> <sup>masl</sup>	k AP <sub>m</sub> ask	$^{\kappa}AP_{l}^{mas}$
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	30.1	57.7	10.5	10.1	10.5	50.1

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#### Results:

 Vim-Ti surpasses DeiT-Ti for medium-size and big objects, demonstrating better long-range context learning

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Backbone DeiT-Ti	AP <sup>mask</sup> 38.1	59.9	40.5	$AP_s^{mas}$ $18.1$	<sup>k</sup> AP <sub>m</sub> <sup>mask</sup> 40.5	AP <sub>1</sub> <sup>mask</sup> 58.4

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- Vim-Ti surpasses DeiT-Ti for medium-size and big objects, demonstrating better long-range context learning
- Not necessary window attention

### Conclusions

- Computational complexity linear on sequence length as shown for text
- Modeling power similar to DeiT and superior for higher resolution images thanks to efficient long sequences management
- Possible alternative to Transformer based backbones

#### **Future Lines:**

- Broader Exploration. Running on different Datasets and Frameworks
- Self-Supervised Learning
- Comparison of improvements for SOTA systems based on Transformers
- As with Transformer architecture, opening a path to explore nexxtgeneration AI based applications.

### References

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