	Laplace's Law (a				(adding $\lambda$ counts	,
$P_{MLE}(w_1w_n) = \frac{C(w_1w_n)}{N}$ $P_{MLE}(w_n \mid w_1w_{n-1}) = \frac{C(w_1w_n)}{C(w_1w_{n-1})}$	General rule:	= x) + 1 N: number of observ B: number of potent ues for X	General vations of X	l rule: C(	$X = x + \lambda$ N:	number of observations of X
MLE( $W_n \mid W_1 \dots W_{n-1}$ ) = $\frac{1}{C(w_1w_{n-1})}$ No probability mass for unseen events	$P_{LAP}(X = x) = \frac{C(X)}{N}$	B: number of potent ues for X	ially observable val- PLAP(X	= x) =	N + Bλ B: n ues f	umber of potentially observable val- or X
			NI NI	probabilit	y:	
<ul> <li>Unsuitable for NLP (widely used, though)</li> </ul>	Pr. m (we w ) = 0	N: total nur $(w_1 w_n) + 1$ servations	mber of n-gram ob- P <sub>LAP</sub> (w	$v_1 w_n) =$	$= \frac{C(w_1 \dots w_n) + \lambda}{N + B\lambda}$	N: total number of n-gram ob- servations B: number of potentially observ- able different n-grams
Zipf's Laws (1929)  Word frequency is inversely proportional to its rank	TLAP(W1Wn) =	$\sum_{\substack{(w_1 \dots w_n) + 1 \\ N + B}} N: total num $ servations B; number o able different	f potentially observ- : n-grams			able different n-grams
(speaker/hearer minimum effort) f ~ 1/r	N-gram conditional	probability:	N_gram	condition	al probability: C(w <sub>1</sub>	$(w_n) + \lambda$ B: number of poten-
$m \sim \sqrt{f}$	$P_{LAP}(w_n \mid w_1 \dots w_n)$	$C(w_1w_n) + 1$ $C(w_1w_{n-1}) + B$ $t$	3: number of poten- P <sub>LAP</sub> (w tially observable w <sub>n</sub>	<sub>n</sub>   w <sub>1</sub> w	$v_{n-1}$ ) = $\frac{1}{C(w_1v_n)}$	$(w_n) + \lambda$ B: number of potentially observable $w_n$ values
■ Frequency of intervals between repetitions is inversely proportional to the length of the interval F ~ 1/I		C(N1Nn=1) + 0 V	/alues	alant to line	ar internelation be	tween MLE and uniform prior:
<ul> <li>Frequency based approaches are hard, since most words are rare</li> </ul>		e values of B too much probab	bility with	u = N/(N -	+ Bλ): Prin(X = 2	$\kappa(x) = \mu \frac{C(X = x)}{N} + (1 - \mu) \frac{1}{R}$
<ul> <li>Most common 5% words account for about 50% of a text</li> <li>90% least common words account for less than 10% of the</li> </ul>	N = num trai	s is assigned to unseen events. ning examples, words or cha	racters			
text ■ Almost half of the words in a text occurr only once	the grams is	rds or characters to the pow e. bigram B^2, trigram B^3 et	ici oi		UNTING (discour	It $\delta$ counts, with $0 < \delta < 1$ )
LINEAR DISCOUNTING (discount a proportion $\alpha$ of contraction $\alpha$ )		l possible combinations mini	us the $P_{ABS}(X = x)$	$c_{i} = \begin{cases} \frac{c(x_{i})}{c(x_{i})} \end{cases}$	$\frac{=x)-\delta}{N}$ if $C(w_1$ . $\frac{N_0)\delta/N_0}{N}$ otherwise	$\ldots w_n) > 0$
General rule:	ones that we					
$P_{LIN}(X=x) = \left\{ \begin{array}{ll} (1-\alpha)\frac{C(X=x)}{N} & \text{if } C(X=x) > 0 \\ \alpha/N_0 & \text{otherwise} \end{array} \right.$	<ul><li>Overlag</li></ul>	D.	N gram pr	obability:	N <sub>0</sub> : number of po	ssible values for X observed 0 times
N <sub>0</sub> : number of possible values for X ob	served 0 times sin	$n_{ovt}(X, Y) = \frac{ X \cap Y }{\min( X ,  Y )} = \frac{1}{\min( X ,  Y )}$	$\frac{a}{(a+b,a+c)}$ B. (	) _ ∫	$\frac{C(w_1w_n)-\delta}{N}$ if C	$(w_1 \dots w_n) > 0$
$\begin{split} & \text{N-gram probability:} \\ & P_{LIN}(w_1 \dots w_n) = \left\{ \begin{array}{ll} (1-\alpha) \frac{C(w_1 \dots w_n)}{N} & \text{if } C(w_1 \dots w_n) > \\ \alpha/N_0 & \text{otherwise} \end{array} \right. \end{split}$	0 Cosine.	p. $n_{ovt}(X,Y) = \frac{ X \cap Y }{\min( X , Y )} = \frac{1}{\min( X , Y )}$	TABS(W1	$v_n = \{$	$\frac{(B-N_0)\delta/N_0}{N}$ other	erwise
	_ cosine.	$(X,Y) =  X \cap Y $	α N-gram co	nditional p	robability:	
N <sub>0</sub> : number of possible n-grams ob	served 0 times sum	$cos(A, T) = \frac{1}{\sqrt{ X } \cdot \sqrt{ Y }} = \frac{1}{\sqrt{(a)}}$	$\overline{(a+b)}\sqrt{(a+c)}$	W. W.	$= \begin{cases} \frac{C(w_1w_n)-C(w_1w_{n-1})}{C(w_1w_{n-1})} \end{cases}$	$\frac{\delta}{0}$ if $C(w_1 \dots w_n) > 0$
N-gram conditional probability: $ (1-\alpha) \frac{C(w_1w_n)}{C(w_1w_n)} $ if $C(w_1,w_n)$	w <sub>n</sub> ) > 0 ■ Mat	$a_{\cos}(X,Y) = \frac{ X \cap Y }{\sqrt{ X } \cdot \sqrt{ Y }} = \frac{1}{\sqrt{(\alpha)}}$	ABSUVI	·· 1 · · · · · · · · · · · · · · · · ·	$\frac{(B-N_0)\delta/N_0}{C(w_1w_{n-1})}$	) otherwise
$P_{LIN}(w_n \mid w_1 \dots w_{n-1}) = \left\{ \begin{array}{ll} (1-\alpha) \frac{C(w_1 \dots w_n)}{C(w_1 \dots w_{n-1})} & \text{if } C(w_1 \dots w_n) \\ \alpha/N_0 & \text{otherwise} \end{array} \right.$					N <sub>0</sub> : number of pos.	sible values for w <sub>n</sub> observed 0 times
Distances: $N_0$ : number of possible values for $w_n$ or	bserved 0 times sim	$_{\mathrm{mc}}(X,Y) = \frac{ X \cap Y  +  (\Omega - X) }{ \Omega }$	$\frac{a+b+c+a}{a+b+c+a} = \frac{a+a}{a+b+c+a}$	- d	imilarity to dista	nce and distance to similarity
$sim_{\texttt{dot}}(\vec{x}, \vec{y}) = \vec{x} \cdot \vec{y} = \sum x_i y_i$		■ Dice.			-	
i i		$sim_{dic}(X, Y)$	$= \frac{2 \cdot  X \cap Y }{ X  +  Y } = \frac{2\alpha}{2\alpha + b + 1}$	c	sim(A, B)	$=\frac{1}{1+d(A,B)};$
Minkowski r=1 L1 and r=2 L2 Cosine sim	Camberra distance:		1 4 7 1 1			2 ( 4(, 1, 5)
$ \left( \sum_{i=1}^{N}  x_i - y_i ^r \right)^{\frac{1}{r}} \frac{\sum_{i=1}^{r} x_i y_i}{ \vec{x}  \cdot  \vec{y} } = \frac{\sum_{i} x_i y_i}{\sqrt{\sum_{i} x_i^2} \cdot \sqrt{\sum_{i} x_i^2}} $	$-\sum_{i} \frac{ x_i-y }{ x_i-y }$	<u>lil</u>	X ∩ Y  a		d(A, B) =	$\frac{1}{\sin(A,B)} - 1$
$\left(\sum_{i=1}^{n}  x_i - y_i ^{i}\right) = \sqrt{\sum_{i=1}^{n}  x_i ^{i}} = \sqrt{\sum_{i=1}^{n} x_i^{2}} \cdot \sqrt{\sum_{i=1}^{n} x_i^{2}}$	$=$ $\sum_{i=1}^{\infty}  x_i + y_i $	Jil sim <sub>jac</sub> (X, Y	$I(x) = \frac{1}{ X \cup Y } = \frac{1}{\alpha + b + c}$			i to check features trigrams
γ . γ .	Vit	factored linear models of the previ terbi to check features bigrams	ious exercises:		VICCID	rto cricer reatares trigrams
Feature Templates Features for classification  • Type 1: The entity is word a:		$f(\mathbf{x}_{1:n}) = \underset{\mathbf{y}_{1:n} \in \mathcal{Y}^n}{\operatorname{argmax}} \sum_{i}$	$\sum_{i=1}^{n} \mathbf{w} \cdot \mathbf{f}(\mathbf{x}, i, \mathbf{y}_{i-1}, \mathbf{y}_{i})$			ART, START, a) (initialization, $y_{-1} = y_0 = \text{START}$ )
$\mathbf{f}_{1,l,a}(x_{1:n},i,j,y) = \begin{cases} 1 & \text{if } i = j \text{ and } x \\ 0 & \text{otherwise} \end{cases}$	$y_i = a$ and $y = l$ In $a$	order to compute $f(\mathbf{x}_{1:n})$ we can use the		δ <sub>l</sub> (	$(b, a) = \max_{c \in \mathcal{Y}_{i-2}} \delta_{i-1}(c, b, a) = \operatorname{argmax} \delta_{i-1}(c, b, a)$	$b) + \mathbf{w} \cdot \mathbf{f}(\mathbf{x}, i, c, b, a)$ (recursion, $\forall i > 1$ ) $c, b) + \mathbf{w} \cdot \mathbf{f}(\mathbf{x}, i, c, b, a)$ (backtrace, $\forall i > 1$ )
( o odletwise		<ul> <li>Define δ<sub>i</sub>(a) to be the score of optimal</li> </ul>		1		
Type 2: All entity words are capitalized:		$\delta_i(a) = \max_{\mathbf{y}_{1:i} \in \mathcal{Y}^i: \mathbf{y}_i:}$	$= a \sum_{j=1}^{i} \mathbf{w} \cdot \mathbf{f}(\mathbf{x}, j, \mathbf{y}_{j-1}, \mathbf{y}_{j})$		PCFG get probability o	CNF f dep right-hand side exactly
$\mathbf{f}_{2,l}(x_{1:n},i,j,y) = \begin{cases} 1 & \text{if } \forall k: i \leq k \leq j: cap \\ 0 & \text{otherwise} \end{cases}$	$statized(x_k)$ and $y = l$	Use the following recursions, for all a	$\in \mathcal{Y}$ :	i	tree by just mult	iplying 2 non-terminals or one
<ul> <li>Type 3: The entity contains word a:</li> </ul>			(initialization, assuming y <sub>0</sub> =	START)	all probabilites	terminal
• Type 3: The entity contains word $a$ : $f_{3,l,a}(x_{1:n},i,j,y) = \begin{cases} 1 & \text{if } \exists k: i \leq k \leq j \\ 0 & \text{otherwise} \end{cases}$	$: x_k = a \text{ and } y = l$	$\delta_i(a) = \max_{b \in \mathcal{Y}} \delta_{i-1}(b) + \mathbf{w} \cdot \mathbf{f}$ $\gamma_i(a) = \operatorname{argmax} \delta_{i-1}(b) + \mathbf{w}$	$\mathbf{r}(\mathbf{x}, i, b, a)$ (recursion, $\forall i > 1$ ) $\mathbf{v} \cdot \mathbf{f}(\mathbf{x}, i, b, a)$ (backtrace, $\forall i > 1$ )	1)		
$s_{0,t,u_1=1:00},s_{0},y_1=0$ otherwise						
• Type 4: The entity has at least three words, the first is $a$ and	the second is b:	<ul> <li>The optimal score for x is max<sub>a∈Y</sub> δ<sub>n</sub></li> <li>The optimal sequence ŷ can be recove</li> </ul>				arly algorithm: start with all possible rules
(b) CKY chart: $ (1  j \ge i + 2 \text{ and } x_i = a $	and $x_{i+1} = b$ and $y = l$		0		chart[5]	ntil the last non-terminal. ut point on the first right side constituent
	$0.00448 \text{ S} \rightarrow \text{N}_{11}\text{VP}_{25}$			chart[4]	$S \rightarrow NP_{01}VP_{15} \bullet$ $S \rightarrow NP_{02}VP_{25} \bullet$ te	agonally up [0,1], check/scan first rminal word and compare it to input,
14	(0.35 × 0.4 × 0.032)		chart[3]	10/41		hat fits of the terminal elements.
_				[1,4]	[2.5]	
12	$0.032 \text{ VP} \rightarrow V_{22}\text{ADVI}$ $(0.4 \times 0.5 \times 0.35)$	16)	chart[2]	[1,4]	$ADVP \rightarrow ADV_{23}NP_{35} \bullet$ $VP \rightarrow V_{23}NP_{35} \bullet$ $VP \rightarrow V_{23}NP_{35} \bullet$	ut a point to the next constituent on the ght side,
13 24	$(0.4 \times 0.5 \times 0.$ 35 $0.16 \text{ ADVP} \rightarrow \text{ADV}_{33}$ $(0.65 \times 1.0 \times 0.$	16) NP45 short[1]	$(0.2)$ $NP \rightarrow N_{01}N_{12} \bullet$ $(1.3)$ $NP \rightarrow N_{02}N_{12} \bullet$	[1,4]	2.5   $ADVP \rightarrow ADV_{23}NP_{35} \bullet$   PI $VP \rightarrow V_{23}NP_{35} \bullet$   Pi   3.5   $NP \rightarrow D_{34}N_{43} \bullet$   gc	ut a point to the next constituent on the ght side, o down [1,1] and predict all constituents
Tree Parsing	$(0.4 \times 0.5 \times 0.$ 35 $0.16 \text{ ADVP} \rightarrow \text{ADV}_{33}$	16) NP45 short[1]	$(0.2)$ $NP \rightarrow N_{01}N_{12} \bullet$ $(1.3)$ $NP \rightarrow N_{02}N_{12} \bullet$	[1,4] [2,4] [3,4] D → an•	$ \begin{array}{c c}  2.5  \\ \text{ADVP} \to \text{ADV}_{23} \text{NP}_{35} \bullet \\ \text{VP} \to \text{V}_{23} \text{NP}_{35} \bullet \\ \text{I3.5}  \\ \text{NP} \to \text{D}_{34} \text{N}_{45} \bullet \\ \text{N} \to \text{arrow} \bullet \\ \end{array} $	at a point to the next constituent on the ght side, o down [1,1] and predict all constituents ith a point to their left. econd row bottom up is always for
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		16) NP45 short[1]	(0.2) $NP \rightarrow N_{01}N_{12} \bullet$ $S \rightarrow NP_{02} \bullet VP$ (1.3) (1.3)	[1,4] [2,4] [3,4] D → an• NP → D • N	$\begin{array}{c} \text{(2.5)} \\ \text{ADVP} \to \text{ADV}_{23} \text{NP}_{35} \bullet \\ \text{VP} \to \text{V}_{23} \text{NP}_{35} \bullet \\ \text{(3.5)} \\ \text{NP} \to \text{D}_{34} \text{N}_{45} \bullet \\ \text{N} \to \text{arrow} \bullet \\ \end{array}  \begin{array}{c} \text{pt} \\ \text{rig} \\ \text{gc} \\ \text{te} \\ \text{ab} \end{array}$	at a point to the next constituent on the ght side, o down [1,1] and predict all constituents th a point to their left. scond row bottom up is always for rminal symbols.  Sove is the rules that are combined,
$\begin{array}{c} 12\\ 0.0308\ \mathrm{NP} \rightarrow \mathrm{N}_{11}\mathrm{N}_{22}\\ (0.385\times0.4\times0.2) \end{array}$		$\begin{array}{c} \text{(b)} \\ \text{NP}_{45} \\ \text{(c)} \\ \text$	$\begin{array}{lll} \text{(9.2)} & \text{(1.3)} & \text{(1.3)} & \text{(1.3)} & \text{(1.3)} & \text{(1.3)} & \text{(1.3)} & \text{(2.3)} & $	[1,4] [2,4] [3,4] D → an• NP → D • N	(2.5) ADVP → ADV 23 NP 3.6 Pt 17.5 Pt	ut a point to the next constituent on the this side, down [1,1] and predict all constituents tha point to their left. cond row bottom up is always for rminal symbols. love is the rules that are combined, love is the rules that are predicted and
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		16)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	[1,4] [2,4] [3,4] D → ane NP → D • N	(2.5) ADV23NP35 • PI NP → V23NP35 • PI 1.55	ut a point to the next constituent on the ght side, of down [1,1] and predict all constituents tha point to their left. cond row bottom up is always for rminal symbols. powe is the rules that are combined, clow the ones that are predicted and en to be scanned ount based tasks;
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		160	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13.4] D → an• NP → D • N	(2.5) ADV23NP3.0 PtV → ADV23NP3.0 ptV → ADV23NP3.0 rty = 1.55 y =	ut a point to the next constituent on the ght side, of down [1,1] and predict all constituents tha point to their left. cond row bottom up is always for rminal symbols. sove is the rules that are combined, elow the ones that are predicted and en to be scanned ount based tasks: le have a sample of 1,500 annotated roduct descriptions. 200 are
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		16)	1031   MP	13.4] D → an• NP → D • N	(2.5) ADV_23NP <sub>3.6</sub>   Property   Property	ut a point to the next constituent on the tht side, down [1,1] and predict all constituents the apoint to their left. second row bottom up is always for rminal symbols. sove is the rules that are combined, slow the ones that are predicted and en to be scanned ount based tasks:
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		16)   Note   Chart[1]   Note     1,0,246    Note   Note     Note	1031   MP	11.4]  12.41  13.41  D → ane  NP → D • N  14.41  P	10.00   10.0	ut a point to the next constituent on the ght side, od own [1,1] and predict all constituents the apoint to their left. Constituents the apoint to their left. Stone of row bottom up is always for riminal symbols. So ove is the rules that are combined, below the ones that are predicted and en to be scanned ount based tasks: (e have a sample of 1,500 annotated roduct descriptions. 200 are assified as ELEC, 350 as COMP, 50 as FASH, and 300 as TOOL.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		16)   Note   Chart[1]	1031   May No.   103	[1,4]	130   130	ut a point to the next constituent on the ght side,  b down [1,1] and predict all constituents  tha point to their left.  cond row bottom up is always for  rminal symbols.  sove is the rules that are combined,  elow the ones that are predicted and  en to be scanned  sount based tasks:  le have a sample of 1,500 annotated  roduct descriptions. 200 are  assified as ELEC, 350 as COMP,  50 as FASH, and 300 as TOOL.  60 products contain the word  atterproof. 80 are annotated as
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.4 10.5 10.5 10.5 10.5 10.5 10.5 10.5 10.5	16)	1031   1031	[1.4]	13.00   - 1.00   -	ut a point to the next constituent on the tht side, down [1,1] and predict all constituents the apoint to their left. conditions the apoint to their left. conditions the standard second row bottom up is always for rminal symbols. owe is the rules that are combined, low the ones that are predicted and en to be scanned ount based tasks:  We have a sample of 1,500 annotated roduct descriptions. 200 are assified as ELC, 250 as COMP, 50 as FASH, and 300 as TOOL.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.  35 0.16 ADVP → ADV33 1(0.65 × 1.0 × 0.  0.08 VP → V33VP3 ← 0.5 × 0.  0.246 NP → D14 Ns. (0.5 × 1.0 × 0.4)  → an 0.4 N → arrow  arrow  arrow  the mort likely subtree selected in decorrection using the decorrection using the selected in the conversion using the selected in the selected	16)	1031   1031	1.4	13.00	ut a point to the next constituent on the ght side, ght side, do down [1,1] and predict all constituents tha a point to their left. Condown [1,1] and predict all constituents that a product on the sove is the rules that are combined, below the ones that are predicted and en to be scanned ount based tasks: le have a sample of 1,500 annotated roduct descriptions. 200 are assified as ELEC, 350 as COMP, 50 as FASH, and 300 as TOOL. 60 products contain the word anterprof. 80 are annotated as ASH, 30 as ELEC, and 50 as TOOL. 110 gorducts contain the word and andrade. 95 are annotated as ASH, 30 as ELEC, and 50 as TOOL.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.  35 0.16 ADVP → ADV33 1(0.65 × 1.0 × 0.  0.08 VP → V33VP3 ← 0.5 × 0.  0.246 NP → D14 Ns. (0.5 × 1.0 × 0.4)  → an 0.4 N → arrow  arrow  arrow  the mort likely subtree selected in decorrection using the decorrection using the selected in the conversion using the selected in the selected	16)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1.4	13.54	ut a point to the next constituent on the ght side,  of down [1,1] and predict all constituents  tha point to their left.  cond row bottom up is always for  rminal symbols.  once is the rules that are combined,  elow the ones that are predicted and  en to be scanned  ount based tasks:  fe have a sample of 1,500 annotated  roduct descriptions. 200 are  assified as ELEC, 350 as COMP,  50 as FASH, and 300 as TOOL.  60 products contain the word  atterproof. 80 are annotated as  ASH, 30 as ELEC, and 50 as TOOL.  110 products contain the word  andmade. 95 are annotated as  ASH, and 15 as TOOL.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.  35 0.16 ADVP → ADV33 1(0.65 × 1.0 × 0.  0.08 VP → V33VP3 ← 0.5 × 0.  0.246 NP → D14 Ns. (0.5 × 1.0 × 0.4)  → an 0.4 N → arrow  arrow  arrow  the mort likely subtree selected in decorrection using the decorrection using the selected in the conversion using the selected in the selected	16)	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1.4	13.0   AJW_aNPa   Pi   Pi   Pi   Pi   Pi   Pi   Pi	ut a point to the next constituent on the ght side, ght side, do down [1,1] and predict all constituents tha a point to their left. Condown [1,1] and predict all constituents that a product on the sove is the rules that are combined, below the ones that are predicted and en to be scanned ount based tasks: le have a sample of 1,500 annotated roduct descriptions. 200 are assified as ELEC, 350 as COMP, 50 as FASH, and 300 as TOOL. 60 products contain the word anterprof. 80 are annotated as ASH, 30 as ELEC, and 50 as TOOL. 110 gorducts contain the word and andrade. 95 are annotated as ASH, 30 as ELEC, and 50 as TOOL.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.4  0.16 ADVP → ADV <sub>33</sub> 0.16 ADVP → ADV <sub>34</sub> 0.05 × 1.0 × 0.6  0.240 NP → 10.4 NS  0.05 × 1.0 × 0.6  0.240 NP → 10.4 NS  0.05 × 0.6 × 0.6  0.240 NP → 10.4 NS  0.05 × 0.6 × 0.6	16)	103   103	1.4	ADV	ut a point to the next constituent on the ght side, of the ght side, of down [1,1] and predict all constituents the a point to their left, cond on the side of the
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	(0.4 × 0.5 × 0.4  0.16 ADVP → ADV <sub>33</sub> (0.05 × 1.0 × 0.4  0.048 VP → Y <sub>33</sub> VP <sub>16</sub> ≥ 0.4  2.240 NP → D14 N <sub>35</sub> (0.05 × 1.0 × 0.4  2.240 NP → D14 N <sub>35</sub> (0.05 × 1.0 × 0.4)  ⇒ an 0.4 N → arrow  arrow  the most likely subtree selected in d  where the from the conversion using it from the conversion using it except root node is a coming in (except root node in ocrossing lines	160	103   103	1.4	1.00   1.00	ut a point to the next constituent on the ght down [1,1] and predict all constituents the a point to their left. Conditions up is always for riminal symbols. Once is the rules that are combined, allow the ones that are predicted and en to be scanned until based tasks: le have a sample of 1,500 annotated roduct descriptions. 200 are assified as ELEC, 350 as COMP, 50 as FASH, and 300 as TOOL. 50 products contain the word atterproof. 80 are annotated as ASH, 30 as ELEC, and 50 as TOOL. 110 products contain the word and and and and 50 as TOOL. 110 products contain the word and and 15 as TOOL. 110 products contain the word and and 15 as TOOL. 110 products contain the word and and 15 as TOOL. 110 products contain the word and products contain the word and the same that a Computer product contains word display, MLE(display) (COMP) Probability that a Computer product nations word handmade, statisms word handmade, to that handmade, to that has word with a Computer product that handmade, to that handmade, to that so were than the same than handmade, to that handmade, to the same that handmade, to the same that handmade, to that handmade, that handmade, that handmade, that handmade, that handmade, that handmade, that has handmade, that
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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.4  0.16 ADVP → ADV <sub>33</sub> (0.05 × 1.0 × 6  0.048 VP → Y <sub>33</sub> VF <sub>16</sub> × 6  0.240 NP → D44 N <sub>35</sub> (0.05 × 1.0 × 6  0.240 NP → D44 N <sub>35</sub> (0.05 × 1.0 × 0.4)  → an 0.4 N → arrow  arrow  the most likely subtree selected in the order to the convention using the front the	160	103   103	1.4	130   130	at a point to the next constituent on the ght side, by down [1,1] and predict all constituents tha point to their left. Condition up is always for riminal symbols. Some side of the side
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.4 × 0.5 × 0.  35 0.16 ADVP → ADV33 (10.65 × 1.0 × 0.  0.08 VP → V33VP3 ← 0.  0.246 NP → D14 NS. (0.615 × 1.0 × 0.4)  → an 0.4 N → arrow  an output of the	16)	133   134   135   136   137	1.4	100   100	at a point to the next constituent on the ght side, ght side, ght down [1,1] and predict all constituents the apoint to their left. Conditions are side of the sid

## Word embeddings TF-IDF number occurences RNN schema divdided by number $TF(t,d) = \frac{|\{x \in d: x = t\}|}{|TF(t,d)|}$ One hot vector (dim == vocabulary size) of words in doc Very large vector (millions of words in some applications) Sparse, orthogonal representations $IDF(t, \mathcal{D}) = \log \left( \frac{|\mathcal{D}|}{|\{d \in \mathcal{D}: t \in d\}|} \right)$ Hidden Markov Model No information about how words are related probability of starting with label y probability of transitioning from label y to y No useful vector distance IDI num total Docs. Huge use of memory (if sparse matrices are not used) below frac: num doc where O<sub>ux</sub>: probability of generating symbol x given label y Usual coding of categorical variables for Linear models and $\qquad \qquad \text{Predictions: } p(x,y) = \pi_{y_1} O_{y_1x_1} \prod \mathsf{T}_{y_{1-1}y_1} O_{y_1x_1}$ this term occurs SVMs with the standard kernels $\boldsymbol{U}$ $h^{(1)}$ $h^{(4)}$ GloVe: Global Vectors for Word Representation: Cbow: given context words predict target word 0000 0 000 $W_h$ $W_h$ $W_h$ $W_h$ Co-occurrences matrix probabilites word-word Skipgram: given target word predict context words 00 Probability and Ratio Dot-product for score vector, softmax output, cross k = solidŏ $6.6 \times 10^{-5}$ $3.0 \times 10^{-3}$ entropy loss, minimize negative log likelihood $1.9 \times 10^{-4}$ $1.7 \times 10^{-5}$ W. w w W. $2.2 \times 10^{-5}$ $7.8 \times 10^{-4}$ $2.2 \times 10^{-3}$ $1.8 \times 10^{-5}$ P(k|steam) $8.5\times10^{-2}$ Word2Vec vs GloVe: P(k|ice)/P(k|steam)8.9 1.36 0000 They differ in the way they are trained. GloVe is based on global word to word co-occurrence counts (in the entire corpus). Word2Vec uses co-occurrence within local context (neighbour words). More especifically, GloVe's training objective is to find a feature matrix that factorizes the whole word to word co-ocurrence matrix while keeping most of its variance. Word2Vec is trained using either the skip-gram model, wich tries to predict the context words given a central word; or the cbow model, which tries to predict the central word given all words in its context. Another aspect to consider is the fact that GloVe's training doing time scales with the vocabulary size whereas Word2Vec scales with the corpus size. Neural Networks activation functions ELMO logistic ("sigmoid") hard tanh Can process any length input Computation for step t can (in theory) use information $f(z) = \tanh(z) =$ from many steps back ■ Model size doesn't increase for longer input ■ Same weights applied on every timestep, so there is symmetry in how inputs are processed RNN disadvantages: Recurrent computation is slow Evaluation: In practice, difficult to access information from many steps Perplexity(P) = $\exp \left\{ \frac{1}{N} \sum_{t=1}^{N} \sum_{t=1}^{T_i} \mathcal{L}_t \right\}$ back LSTM gate computations: ■ New cell content: $\tilde{\mathbf{c}}^{(t)} = \tanh(\mathbf{W_c}[h^{(t-1)}, x^{(t)}] + \mathbf{b_c})$ this ■ ELMo uses a two-layer bi-directional LSTM network as its is the new content to be written to the cell architecture FNN schema ■ Cell state: erase ("forget") some content from last cell Each layer has 4096 units and 512-dimensional projections state, and write ("input") some new cell content: ■ The input to the network is a sequence of characters, which are embedded into a 16-dimensional vector $\mathbf{c}^{(t)} = \mathbf{f}^{(t)} \odot \mathbf{c}^{(t-1)} + \mathbf{i}^{(t)} \odot \tilde{\mathbf{c}}^{(t)}$ A convolutional layer with 2048 filters of width 1 to 7 ■ Hidden state: read ("output") some content from the cell: applied to the input character embeddings. The max-pooled output is then re-projected to a $\mathbf{h}^{(t)} = \mathbf{o}^{(t)} \odot \tanh(\mathbf{c}^{(t)})$ T. 512-dimensional vector. ■ The network is pre-trained on a large corpus with the 00000000000 ■ ⊙: Gates are applied using element-wise product following training objective: W lacksquare $\sigma$ : Sigmoid goes returns values from 0 to 1 ■ Language modeling: predict the next word given the previous words (forward LM) and predict the previous word 0000 0000 0000 0000 Transformers: given the next words (backward LM) Positional Encoding formular multihead attention block scaled dot product attention am doing my We can add positional encodings to the input word vectors: $MultiHead(Q, K, V) = [head_1, ..., head_h]W_0$ Fixed. A usual choice is sine and cosine functions of different frequencies, since it allow the model to attend by where $head_i = Attention(QW_i^Q, KW_i^K, VW_i^V)$ relative positions pos is the position $if \ dim = 2i$ $if \ dim = 2i + 1$ of the token in the $Attention(Q,K,V) = softmax(\frac{QK^T}{\sqrt{d_k}})V \qquad \ \ \mathsf{P}(\mathbf{y}|\mathbf{x}) = 0$ $\exp(\sum_{i=1}^{n} \mathbf{w} \cdot \mathbf{f}(\mathbf{x}, i, \mathbf{y}_{i-1}, \mathbf{y}_{i}))$ sentence. dim the dimension of the embeddings i the position within the embedding Example of bias case Application Ethical concern COMPAS predict recidivism risk Accuracy varies with race: Darker skins, higher risk Gender Shades face recognition Accuracy varies with race: Contextual word embeddings. BERT Darker skins, lower accuracy Resource Application Advantatge T<sub>K</sub> T<sub>DEFT</sub> T<sub>i</sub> ... GeBioToolkit Machine Translation Balanced in gender MT-DataSheet for Dataset Machine Translation Details about the corpus BERT article Positional encoding: Tok (SEP) Tok A d-dimensional vector that encodes the wordpiece position in the sentence is added (not oentence Pair Classification Tasks MNLI, QQP, QNLI, STS-B, MRPC, RTE, SWAG to the d-dimensional vector representing the wordpiece. The positional vector uses sinusoidal functions with varying frequences so that when two positions are multiplied, the is scales with the distance between such positions. We need positional encoding because the attention block is not recurrent and does not sense of position/order for each input. Advantages: 100 (MP) 100 1 • It is able to encode distances between inputs even for long sequences · Because it is added and not concatenated, less weights are required (d) Single Sentence Tagging Tasks CoNLL-2003 NER · They are precomputed and don't have to be trained