STAT361 Laboratory for Advanced R for Data Science

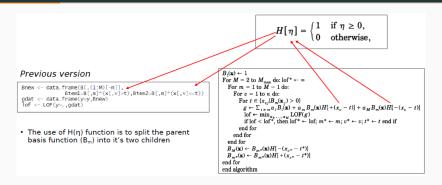
Lab 3

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MARS - Algorithm 1

1. Step Function



Exercise.

- 1. Define function $H(\eta)$
- 2. Replace (x[,v] > t) with $H(+(x_v t))$
- 3. Replace $(x[,v] \le t)$ with $H(-(x_v t))$

- $H(+(x_v t))$: positive values will be indicated as 1
- $H(-(x_v t))$: non-positive values will be indicated as 1

2. Record Splits (s, v, t) using Bfuncs

Each basis function B_m is a product of step functions

$$B_m(\mathbf{x}) = \prod_{k=1}^{K_m} H[s_{km} \cdot (x_{v(k,m)} - t_{km})]$$

- · v: index of the covariate
- t: split point
- K_m : number of splits in B_m
- · m: index of the basis function

Bfuncs[[m]] is a data frame like below:

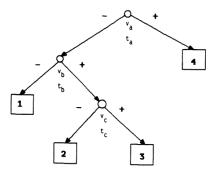
$$egin{bmatrix} s_{1m} & v(1,m) & t_{1m} \ s_{2m} & v(2,m) & t_{2m} \ \dots & \dots & \dots \ s_{K_mm} & v(K_m,m) & t_{K_mm} \end{bmatrix}$$

Exercise:

 Initialize Bfuncs to be an empty list of length M_{max} + 1 (you may use vector())

Bfuncs

$$B_m(\mathbf{x}) = \prod_{k=1}^{K_m} H \left[s_{km} \cdot \left(x_{v(k,m)} - t_{km} \right) \right]$$



$$\begin{split} B_1 &= H[-(x_{v_a} - t_a)] H[-(x_{v_b} - t_b)] \\ B_2 &= H[-(x_{v_a} - t_a)] H[+(x_{v_b} - t_b)] H[-(x_{v_c} - t_c)] \\ B_3 &= H[-(x_{v_a} - t_a)] H[+(x_{v_b} - t_b)] H[+(x_{v_c} - t_c)] \\ B_4 &= H[+(x_{v_a} - t_a)] \end{split}$$

Fig. 1. A binary tree representing a recursive partitioning regression model with the associated basis functions.

2. Record Splits (s, v, t) using Bfuncs

- splits will be replaced by Bfuncs
- Record the best split with a temporary object
- Bfuncs will be updated after a best split is given

```
\begin{array}{l} B_1(\mathbf{x}) \leftarrow 1 \\ \text{For } M = 2 \text{ to } M_{\max} \text{ do: } \text{lof}^* \leftarrow \infty \\ \text{For } m = 1 \text{ to } M - 1 \text{ do:} \\ \text{For } v = 1 \text{ to } n \text{ do:} \\ \text{For } t \in (\mathbf{x}_v) | B_m(\mathbf{x}_j) > 0 \\ g \leftarrow \sum_{i \neq m} a_i B_i(\mathbf{x}) + a_m B_m(\mathbf{x}) H[+(x_v - t)] + a_M B_m(\mathbf{x}) H[-(x_v - t)] \\ \text{lof} \leftarrow \min_{a_1, \dots, a_M} \text{LOF}(g) \\ \text{if } \text{lof} < \text{lof}^*, \text{ then } \text{lof}^* \leftarrow \text{lof}; \ m^* \leftarrow m; \ v^* \leftarrow v; \ t^* \leftarrow t \text{ end if } \\ \text{end for } \\ B_M(\mathbf{x}) \leftarrow B_m * (\mathbf{x}) H[-(x_v - t^*)] \\ B_m * (\mathbf{x}) \leftarrow B_m * (\mathbf{x}) H[+(x_v - t^*)] \\ \text{end for } \\ \text
```

Exercise (continued):

- 2. Copy the data frame **Bfuncs[[mstar]]** to **Bfuncs[[M+1]]** and add a row (s, v, t) to **Bfuncs[[M+1]]** with s = -1, and v, t from the best split
 - · Add the splits of the new child basis function
- 3. Add a row (s, v, t) to Bfuncs[[mstar]] with s = -1, and v, t from the best split
 - · Add the splits of the new child (sibling) basis function

3. Test the revised recpart_fwd()

Test your code as follows:

```
# Test
set.seed(123); n <- 10
x <- data.frame(x1=rnorm(n),x2=rnorm(n))
y <- rnorm(n)
rp_fwd <- recpart_fwd(y,x,Mmax=9)
rp_fwd$Bfuncs</pre>
```

Building R Package

Start an R package

Turn your skeleton implementation of MARS into an R package using the tools in the **devtools package**, as outlined in lecture 5.