

Author: Rebecca Lashua

Date: 1/23/2019

## Assignment 2: PART 2

1.

a) The unit cost of each individual push operation (without factoring in resizing) is 50.

Since the capacity is 8, that means it will need to be resized at

index 9: which will add a unit cost of 8 as previous elements are copied over.

index 17: which will add a unit cost of 16 as previous elements are copied over.

index 25: which will add a unit cost of 24 as previous elements are copied over.

index 33: which will add a unit cost of 32 as previous elements are copied over.

index 41: which will add a unit cost of 40 as previous elements are copied over.

index 49: which will add a unit cost of 48 as previous elements are copied over.

That brings us to a total unit cost of:

50 (for each element itself being pushed) + 8 + 16 + 24 + 32 + 40 + 48 = 218

Now when we divide that number by the number of elements pushed (50), we get:

$$218/50 = \mathbf{4.36 \text{ average cost.}}$$

b) The average big-oh complexity for push under this strategy for resizing is  **$O(1)^+$** .

2.

a)

Total cost of pushing each individual element is once again 50 units.

Since the array grows by 2 spaces once it has reached capacity than it will resize at indices:

- 9: adding 8 units when resized
- 11: adding 10 units when resized
- 13: adding 12 units when resized
- 15: adding 14 units when resized
- 17: adding 16 units when resized
- 19: adding 18 units when resized
- 21: adding 20 units when resized
- 23: adding 22 units when resized
- 25: adding 24 units when resized
- 27: adding 26 units when resized
- 29: adding 28 units when resized
- 31: adding 30 units when resized
- 33: adding 32 units when resized
- 35: adding 34 units when resized
- 37: adding 36 units when resized

39: adding 38 units when resized  
41: adding 40 units when resized  
43: adding 42 units when resized  
45: adding 44 units when resized  
47: adding 46 units when resized  
49: adding 48 units when resized

The total cost of resizing throughout this exercise is then

$8+10+12+14+16+18+20+22+24+26+28+30+32+34+36+38+40+42$   
 $+44+46+48 = 588$ .

The cost of pushing each element (50) + the total cost of resizing (588) = 638.

That leaves us with an average cost of  $638 / 50 = \mathbf{12.76}$  units.

b) The average big-oh complexity for push under this strategy for resizing is  **$O(n)$** .