

## Problem Set 5

### 1 The Shock Jump Conditions

Some models for high-energy radiation from compact objects involve gas free-falling onto the surface of the object at a velocity near the object's escape speed. This speed is very supersonic relative to the star, so the gas must pass through a shock (called either an "accretion" or "standoff" shock) before it settles on the surface. Assuming that this is a strong shock, estimate the post-shock temperatures for a white dwarf (with  $M = 1 M_\odot$  and  $R = 10^9$  cm) and a neutron star (with  $M = 1 M_\odot$  and  $R = 10^6$  cm). You can assume  $\gamma = 5/3$ ,  $\mu = m_p$ , and that the standoff shock is just above the surface of the star. (For the pedantic among you: you can use the expressions in this problem set, even though this shock is actually spherical rather than planar.)

```
Pkg.resolve()
Pkg.instantiate()

using DrWatson
using Unitful: Mass, Length
include(scrdir("astr145/main.jl"))
```

```
Updating `~/projects/beforeerr/Project.toml`
[634d3b9d] + DrWatson v2.19.1
[1986cc42] + Unitful v1.27.0
[6112ee07] + UnitfulAstro v1.2.2
Updating `~/projects/beforeerr/Manifest.toml`
[0b6fb165] + ChunkCodecCore v1.0.1
[4c0bbbee4] + ChunkCodecLibZlib v1.0.0
[55437552] + ChunkCodecLibZstd v1.0.0
[634d3b9d] + DrWatson v2.19.1
[5789e2e9] + FileIO v1.17.1
[076d061b] + HashArrayMappedTries v0.2.0
[033835bb] + JLD2 v0.6.3
[692b3bcd] + JLLWrappers v1.7.1
[1914dd2f] + MacroTools v0.5.16
[bac558e1] + OrderedCollections v1.8.1
[aea7be01] + PrecompileTools v1.3.3
[21216c6a] + Preferences v1.5.1
[ae029012] + Requires v1.3.1
[7e506255] + ScopedValues v1.5.0
[6c6a2e73] + Scratch v1.3.0
```

```

[3a884ed6] + UnPack v1.0.2
[1986cc42] + Unitful v1.27.0
[6fb2a4bd] + UnitfulAngles v0.7.2
[6112ee07] + UnitfulAstro v1.2.2
[3161d3a3] + Zstd_jll v1.5.7+1
[0dad84c5] + ArgTools v1.1.2
[56f22d72] + Artifacts v1.11.0
[2a0f44e3] + Base64 v1.11.0
[ade2ca70] + Dates v1.11.0
[f43a241f] + Downloads v1.7.0
[7b1f6079] + FileWatching v1.11.0
[ac6e5ff7] + JuliaSyntaxHighlighting v1.12.0
[b27032c2] + LibCURL v0.6.4
[76f85450] + LibGit2 v1.11.0
[8f399da3] + Libdl v1.11.0
[37e2e46d] + LinearAlgebra v1.12.0
[56ddb016] + Logging v1.11.0
[d6f4376e] + Markdown v1.11.0
[a63ad114] + Mmap v1.11.0
[ca575930] + NetworkOptions v1.3.0
[44cfe95a] + Pkg v1.12.1
[de0858da] + Printf v1.11.0
[9a3f8284] + Random v1.11.0
[ea8e919c] + SHA v0.7.0
[f489334b] + StyledStrings v1.11.0
[fa267f1f] + TOML v1.0.3
[a4e569a6] + Tar v1.10.0
[cf7118a7] + UUIDs v1.11.0
[4ec0a83e] + Unicode v1.11.0
[e66e0078] + CompilerSupportLibraries_jll v1.3.0+1
[deac9b47] + LibCURL_jll v8.15.0+0
[e37daf67] + LibGit2_jll v1.9.0+0
[29816b5a] + LibSSH2_jll v1.11.3+1
[14a3606d] + MozillaCACerts_jll v2025.11.4
[4536629a] + OpenBLAS_jll v0.3.29+0
[458c3c95] + OpenSSL_jll v3.5.4+0
[83775a58] + Zlib_jll v1.3.1+2
[8e850b90] + libblastrampoline_jll v5.15.0+0
[8e850ede] + nghttp2_jll v1.64.0+1
[3f19e933] + p7zip_jll v17.7.0+0

```

```
escape_velocity (generic function with 1 method)
```

```

function postshock_temperature(u1; μ=mp, γ=5 / 3)
    2 * (γ - 1) / (γ + 1)^2 * μ * u1^2 |> uprefered
end

```

```

function postshock_temperature(M::Mass, R::Length)
    v_esc = escape_velocity(M, R)
    kT = postshock_temperature(v_esc)
    T = uconvert(u"K", kT / Unitful.k)
    @show v_esc kT T
end

postshock_temperature(1u"Msun", 1e9u"cm")
postshock_temperature(1u"Msun", 1e6u"cm")

```

```

v_esc = 5.1519402170444485e6 m s-1
kT = 8.324165125889762e-15 kg m2 s-2
T = 6.029168257746727e8 K
v_esc = 1.629186545488269e8 m s-1
kT = 8.324165125889762e-12 kg m2 s-2
T = 6.029168257746727e11 K

```

```

6.029168257746727e11 K

```

## Bibliography