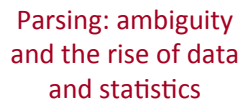


the cat  
a dog  
large in the crate  
barking on the table  
cuddly by the door  
large barking  
to  
for

1



- Wrote symbolic grammar (CFG or often richer) and lexicon
 

S → NP VP	NN → <i>interest</i>
NP → (DT) NN	NNS → <i>rates</i>
NP → NN NNS	NNS → <i>raises</i>
NP → NNP	VBP → <i>interest</i>
VP → V NP	VBZ → <i>rates</i>
- Used grammar/proof systems to prove parses from words
- This scaled very badly and didn't give coverage. For sentence:
 

*Fed raises interest rates 0.5% in effort to control inflation*

  - Minimal grammar: 36 parses
  - Simple 10 rule grammar: 592 parses
  - Real-size broad-coverage grammar: millions of parses

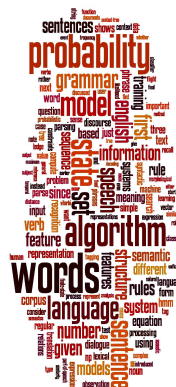
The boy ate the dessert with a spoon/cherry

- Catalan numbers:  $C_n = (2n)!/[(n+1)!n!]$
- An exponentially growing series, which arises in many tree-like contexts:
  - E.g., the number of possible triangulations of a polygon with  $n+2$  sides
    - Turns up in triangulation of probabilistic graphical models....

- Categorical constraints can be added to grammars to limit unlikely/weird parses for sentences
  - But the attempt makes the grammars not robust
    - In traditional systems, commonly 30% of sentences in even an edited text would have *no* parse.
- A less constrained grammar can parse more sentences
  - But simple sentences end up with ever more parses with no way to choose between them
- We need mechanisms that allow us to find the most likely parse(s) for a sentence
  - Statistical parsing lets us work with very loose grammars that admit millions of parses for sentences but still quickly find the best parse(s)

(S  
 (NP-SBJ (DT The) (NN move))  
 (VP (VBD followed)  
 (NP  
 (NP (DT a) (NN round))  
 (PP (IN of)  
 (NP  
 (NP (JJ similar) (NNS increases))  
 (PP (IN by)  
 (NP (JJ other) (NNS lenders)))  
 (PP (IN against)  
 (NP (NP Arizona) (JJ real) (NN estate) (NNS loans))))))  
 (. )  
 (S-ADV  
 (NP-SBJ (-NONE- \*))  
 (VP (VBG reflecting)  
 (NP  
 (NP (DT a) (VBG continuing) (NN decline))  
 (PP-LOC (IN in)  
 (NP (DT that) (NN market))))))  
 (. )

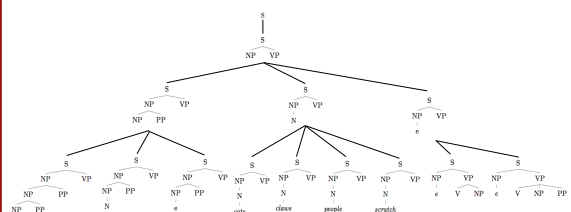
- Starting off, building a treebank seems a lot slower and less useful than building a grammar
- But a treebank gives us many things
  - Reusability of the labor
    - Many parsers, POS taggers, etc.
    - Valuable resource for linguistics
  - Broad coverage
  - Frequencies and distributional information
  - A way to evaluate systems



# Statistical Natural Language Parsing

## Parsing: solving exponential work and ambiguity

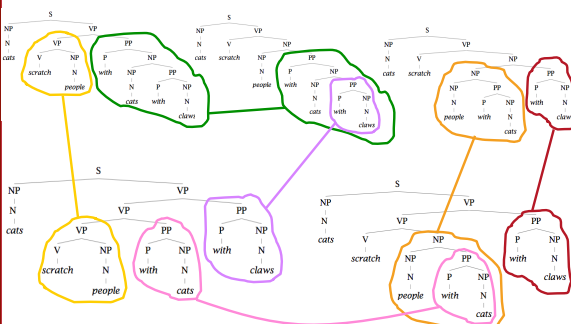
## Top-down parsing



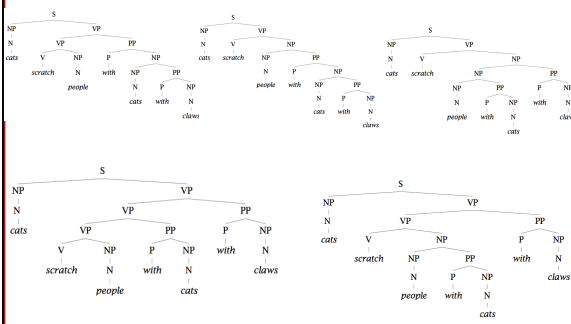
## Shift-reduce parsing: one path

What other search paths are there for parsing this sentence?


**Two problems to solve:**  
**1. Repeated work...**



**Two problems to solve:**  
**1. Repeated work...**



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# Two problems to solve:

## 2. Choosing the correct parse


- How do we work out the correct attachment:
  - She saw the man with a telescope
- Is the problem 'AI complete'? Yes, but ...
- Words are good predictors of attachment
  - Even absent full understanding
- Moscow sent more than 100,000 soldiers into Afghanistan ...
- Sydney Water breached an agreement with NSW Health ...
- Our statistical parsers will try to exploit such statistics.

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# A simple prediction

- Use a likelihood ratio:
  - E.g.,
$$LR(v,n,p) = \frac{P(p|v)}{P(p|n)}$$
  - $P(\text{with}|\text{agreement}) = 0.15$
  - $P(\text{with}|\text{breach}) = 0.02$
  - $LR(\text{breach}, \text{agreement}, \text{with}) = 0.13$   
→ Choose noun attachment




Christopher Manning  
Stanford University  
NLP

# A problematic example

- Chrysler confirmed that it would end its troubled venture with Maserati.
- Should be a noun attachment but get wrong answer:
 

• w	$C(w)$	$C(w, \text{with})$
• end	5156	607
• venture	1442	155

$$P(\text{with} | v) = \frac{607}{5156} \approx 0.118 > P(\text{with} | n) = \frac{155}{1442} \approx 0.107$$



## A problematic example

- What might be wrong here?
  - If you see a V NP PP sequence, then for the PP to attach to the V, then it must also be the case that the NP doesn't have a PP (or other postmodifier)
    - Since, except in extraposition cases, such dependencies can't cross
    - Also, the verb must take an NP object
      - Unlike cases like "end with a bang"
- Parsing allows us to factor in and integrate such constraints.


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The logo of the Stanford University Natural Language Processing (NLP) group. It is a circular seal with 'Stanford University' at the top and 'Natural Language Processing' at the bottom. In the center, there is a stylized mountain range with the letters 'S' above and 'NLP' below.

## Human parsing

- Humans often do ambiguity maintenance
  - *Have the police ... eaten their supper?*
  - *come in and look around.*
  - *taken out and shot.*
- But humans also commit early and are “garden pathed”:
  - *The man who hunts ducks out on weekends.*
  - *The cotton shirts are made from grows in Mississippi.*


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 **A phrase structure grammar**

$S \rightarrow NP VP$	$N \rightarrow \text{people}$
$VP \rightarrow V NP$	$N \rightarrow \text{fish}$
$VP \rightarrow V NP PP$	$N \rightarrow \text{tanks}$
$NP \rightarrow NP NP$	$N \rightarrow \text{rods}$
$NP \rightarrow NP PP$	$V \rightarrow \text{people}$
$NP \rightarrow N$	$V \rightarrow \text{fish}$
$NP \rightarrow e$	$V \rightarrow \text{tanks}$
$PP \rightarrow P NP$	$P \rightarrow \text{with}$


*people fish tanks*  
*people fish with rods*

Christopher Manning

 **Phrase structure grammars = context-free grammars (CFGs)**


- $G = (T, N, S, R)$ 
  - $T$  is a set of terminal symbols
  - $N$  is a set of nonterminal symbols
  - $S$  is the start symbol ( $S \in N$ )
  - $R$  is a set of rules/productions of the form  $X \rightarrow \gamma$ 
    - $X \in N$  and  $\gamma \in (N \cup T)^*$
- A grammar  $G$  generates a language  $L$ .

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 **Phrase structure grammars in NLP**

- $G = (T, C, N, S, L, R)$ 
  - $T$  is a set of terminal symbols
  - $C$  is a set of preterminal symbols
  - $N$  is a set of nonterminal symbols
  - $S$  is the start symbol ( $S \in N$ )
  - $L$  is the lexicon, a set of items of the form  $X \rightarrow x$ 
    - $X \in P$  and  $x \in T$
  - $R$  is the grammar, a set of items of the form  $X \rightarrow \gamma$ 
    - $X \in N$  and  $\gamma \in (N \cup C)^*$
- By usual convention,  $S$  is the start symbol, but in statistical NLP, we usually have an extra node at the top (ROOT, TOP)
- We usually write  $e/\epsilon$  for an empty sequence, rather than nothing


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 **A phrase structure grammar**

$S \rightarrow NP VP$	$N \rightarrow \text{people}$
$VP \rightarrow V NP$	$N \rightarrow \text{fish}$
$VP \rightarrow V NP PP$	$N \rightarrow \text{tanks}$
$NP \rightarrow NP NP$	$N \rightarrow \text{rods}$
$NP \rightarrow NP PP$	$V \rightarrow \text{people}$
$NP \rightarrow N$	$V \rightarrow \text{fish}$
$NP \rightarrow e$	$V \rightarrow \text{tanks}$
$PP \rightarrow P NP$	$P \rightarrow \text{with}$


*people fish tanks*  
*people fish with rods*

Christopher Manning


 **Probabilistic – or stochastic – context-free grammars (PCFGs)**

- $G = (T, N, S, R, P)$ 
  - $T$  is a set of terminal symbols
  - $N$  is a set of nonterminal symbols
  - $S$  is the start symbol ( $S \in N$ )
  - $R$  is a set of rules/productions of the form  $X \rightarrow \gamma$
  - $P$  is a probability function
    - $P: R \rightarrow [0,1]$
    - $\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$
- A grammar  $G$  generates a language model  $L$ .
 
$$\sum_{\gamma \in T^+} P(\gamma) = 1$$

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 **A PCFG**

$S \rightarrow NP VP$	1.0	$N \rightarrow \text{people}$	0.5
$VP \rightarrow V NP$	0.6	$N \rightarrow \text{fish}$	0.2
$VP \rightarrow V NP PP$	0.4	$N \rightarrow \text{tanks}$	0.2
$NP \rightarrow NP NP$	0.1	$N \rightarrow \text{rods}$	0.1
$NP \rightarrow NP PP$	0.2	$V \rightarrow \text{people}$	0.1
$NP \rightarrow N$	0.7	$V \rightarrow \text{fish}$	0.6
$PP \rightarrow P NP$	1.0	$V \rightarrow \text{tanks}$	0.3
		$P \rightarrow \text{with}$	1.0



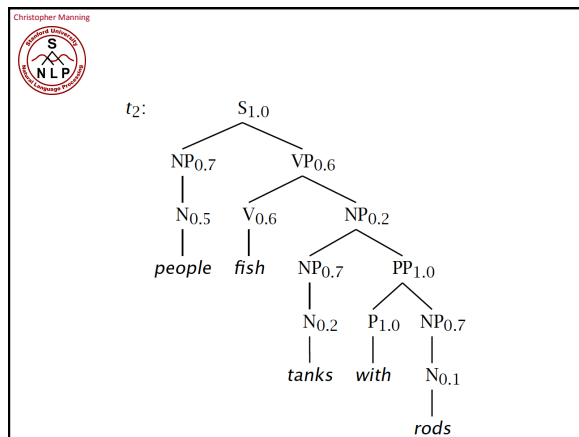
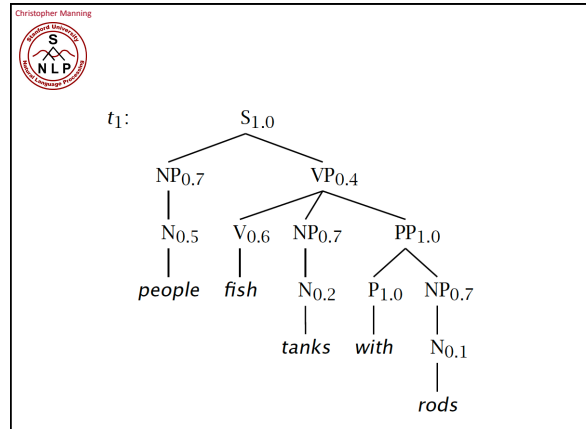
[With empty NP removed so less ambiguous]

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**The probability of trees and strings**

- $P(t)$  - The probability of a tree  $t$  is the product of the probabilities of the rules used to generate it.
- $P(s)$  - The probability of the string  $s$  is the sum of the probabilities of the trees which have that string as their yield

$$P(s) = \sum_j P(s, t) \text{ where } t \text{ is a parse of } s$$

$$= \sum_j P(t)$$


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**Tree and String Probabilities**

- $s = \text{people fish tanks with rods}$
- $P(t_1) = 1.0 \times 0.7 \times 0.4 \times 0.5 \times 0.6 \times 0.7 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1 = 0.0008232$  Verb attach
- $P(t_2) = 1.0 \times 0.7 \times 0.6 \times 0.5 \times 0.6 \times 0.2 \times 0.7 \times 1.0 \times 0.2 \times 1.0 \times 0.7 \times 0.1 = 0.00024696$  Noun attach
- $P(s) = P(t_1) + P(t_2) = 0.0008232 + 0.00024696 = 0.00107016$

