

# Empirical Replication Guide for Romer and Romer (2010)

A Replication Recipe for Theory, Plots, Tables, and Graphs

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## 1 Summary of the Theoretical Framework

The full theoretical derivation can be summarized in the following steps:

1. Start with the simple reduced-form relationship:

$$\Delta \ln Y_t = \alpha + \beta \Delta T_t + \varepsilon_t.$$

2. Decompose the error term into a sum of distinct shocks:

$$\varepsilon_t = \sum_{i=1}^K \varepsilon_t^i.$$

3. Model tax changes as driven by endogenous responses and exogenous motivations:

$$\Delta T_t = \sum_{i=1}^K b_t^i \varepsilon_t^i + \sum_{j=1}^L \omega_t^j.$$

4. Substitute the tax-change equation into the output equation and define:

$$\nu_t = \sum_{i=1}^K (1 + \beta b_t^i) \varepsilon_t^i.$$

This yields:

$$\Delta \ln Y_t = \alpha + \beta \sum_{j=1}^L \omega_t^j + \nu_t.$$

5. Use narrative evidence to classify tax changes. Only those tax changes that are exogenous

(i.e., the  $\omega_t^j$  components) are aggregated into the tax shock series:

$$\tau_t = \sum_{j=1}^L \omega_t^j.$$

6. Dynamic effects are captured by a distributed lag model:

$$\Delta \ln Y_t = \alpha + \sum_{i=0}^M \beta_i \Delta T_{t-i} + \varepsilon_t,$$

where the cumulative effect is  $\sum_{i=0}^M \beta_i$ .

7. Anticipation effects are incorporated by including a news variable:

$$\Delta \ln Y_t = a + \sum_{i=0}^M b_i \Delta T_{t-i} + \sum_{j=0}^M c_j \text{NEWS}_{t-j} + \sum_{k=1}^N d_k \Delta \ln Y_{t-k} + e_t.$$

## 2 Data Acquisition and Preparation

### 2.1 Data Sources

- **Replication Package:** First to Obtain the replication dataset from OpenICPSR or the AEA repository. We can visit:

<https://www.openicpsr.org/openicpsr/project/112357/version/V1/view>

- **Macroeconomic Data:**
  - **GDP Data:** Download quarterly real and nominal GDP data from the Bureau of Economic Analysis (BEA) via <https://www.bea.gov/data/gdp/gross-domestic-product>.
  - **Additional Variables:** Obtain variables such as government spending, interest rates (e.g., the Federal funds rate from the Federal Reserve's H15 series), and oil prices (from the Bureau of Labor Statistics) if necessary.

### 2.2 Data Cleaning and Variable Construction

- **Align Time Series:**
- **Normalization:** Convert raw tax revenue changes into percentages by normalizing with nominal GDP.
- **Key Variables:**

- **Real GDP Growth:** Compute the logarithm of real GDP and its quarterly differences.
- **Exogenous Tax Shock Series:** Identify the tax changes classified as exogenous from the narrative coding and aggregate them by quarter. Normalize these by nominal GDP.
- **Alternative Tax Measures:** Construct series for all legislated tax changes and for cyclically adjusted revenue changes.
- **Lagged Variables:** Create lagged variables (e.g., up to 12 lags) for the exogenous tax shock series and for GDP growth to capture dynamic effects.
- **Anticipation Effects (Optional):** If available, construct a “news” variable that represents the present value of future tax changes (using, for example, a three-year Treasury rate as the discount rate).

## 3 Model Specification and Estimation Strategy

### 3.1 Distributed Lag Regressions

- **Baseline Model:** Specify a distributed lag regression of GDP growth on the contemporaneous and lagged values of the exogenous tax shock series:

$$\Delta \ln Y_t = \alpha + \sum_{i=0}^M \beta_i \Delta T_{t-i} + \varepsilon_t.$$

- **Cumulative Multiplier:** Compute the cumulative multiplier as the sum of the estimated coefficients, i.e.,  $\sum_{i=0}^M \beta_i$ .

### 3.2 Extended Model with Controls

- **Incorporate Lagged GDP Growth:** Add several lags of GDP growth to control for the inherent dynamics of the economy:

$$\Delta \ln Y_t = \alpha + \sum_{i=0}^M \beta_i \Delta T_{t-i} + \sum_{j=1}^N \gamma_j \Delta \ln Y_{t-j} + \varepsilon_t.$$

- **Other Controls:** Optionally include additional variables (e.g., government spending, oil prices, interest rates) to test robustness.

### 3.3 Vector Autoregression (VAR)

- **VAR Specification:** Set up a VAR with the exogenous tax shock series and the level of log real GDP:

$$\begin{pmatrix} \tau_t \\ \ln Y_t \end{pmatrix} = A_0 + \sum_{k=1}^p A_k \begin{pmatrix} \tau_{t-k} \\ \ln Y_{t-k} \end{pmatrix} + u_t.$$

- **Impulse Response Functions (IRFs):** Compute IRFs to trace the dynamic response of GDP to a 1% tax shock.

### 3.4 Incorporating Anticipation Effects (Optional)

- **Extended Specification:** Include a “news” variable to capture anticipation effects:

$$\Delta \ln Y_t = a + \sum_{i=0}^M b_i \Delta T_{t-i} + \sum_{j=0}^M c_j \text{NEWS}_{t-j} + \sum_{k=1}^N d_k \Delta \ln Y_{t-k} + e_t.$$

- **Interpretation:** Compare the output response from the news variable versus the response when the tax change is implemented.

## 4 Replication of Figures, Tables, and Graphs

### 4.1 Regression Tables

- Create tables that report:
  - Coefficient estimates, robust standard errors, and t-statistics for the baseline model.
  - Results from the extended model with lagged GDP and additional controls.
  - Comparisons using alternative tax measures (exogenous, all legislated, and cyclically adjusted revenues).

### 4.2 Time Series and Comparative Plots

- Plot the time series of:
  - Exogenous tax shocks.
  - All legislated tax changes.
  - Cyclically adjusted revenue changes.
- Use clear legends and axis labels (e.g., “Percent of GDP”).

### 4.3 Dynamic Multipliers

- Plot the cumulative impact (multiplier) over quarters by summing the coefficients from the distributed lag regression.
- Include confidence intervals or error bars to reflect estimation uncertainty.

### 4.4 Impulse Response Functions (IRFs)

- Generate IRF plots from the VAR model to visualize the dynamic response of log GDP to a tax shock.
- Compare these IRFs with those obtained from the distributed lag regressions.

### 4.5 Subsample and Robustness Plots

- Create additional plots for subsample analyses (e.g., pre-1980 versus post-1980).
- Plot comparisons showing the sensitivity of the results to different lag lengths or the inclusion of control variables.

## 5 Robustness Checks and Sensitivity Analysis

- **Lag Structure:** Estimate models with alternative lag lengths (e.g., 8, 12, 14 lags) to assess stability.
- **Sample Splitting:** Divide the data into different subperiods (e.g., pre-1980 and post-1980) and compare results.
- **Additional Controls:** Incorporate extra variables such as government spending, oil prices, and interest rates to check the robustness of the estimated multipliers.
- **Alternative Tax Measures:** Compare results using the exogenous tax shock series, the series for all legislated tax changes, and the cyclically adjusted revenue changes.
- **Anticipation Effects:** If a news variable is available, test models that incorporate anticipation effects to determine if the output response is driven by the timing of announcements versus implementation.