Machine Learning **Evaluation Metrics** Confusion Matrix ROC Curve

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Accuracy

True Decisions All Decisions

Imbalanced Data

- 90 normal cases (negative class)
- 10 cancerous cases (positive class)



Sensitivity - Specificity

Sensitivity, Recall, True Positive Rate

$$TPR = \frac{TP}{P} = \frac{TP}{TP + FN}$$

Specificity, Recall, Selectivity, True Negative Rate

$$TNR = \frac{TN}{N} = \frac{TN}{TN + FP}$$



Precision – F1 Score

Precision, Positive/Negative Predictive Value

$$ext{PPV} = rac{ ext{TP}}{ ext{TP} + ext{FP}}$$

F1 Score (Harmonic Mean of Precision and Recall)

$$\mathrm{F_1} = 2 imes rac{\mathrm{PPV} imes \mathrm{TPR}}{\mathrm{PPV} + \mathrm{TPR}} = rac{2\mathrm{TP}}{2\mathrm{TP} + \mathrm{FP} + \mathrm{FN}}$$



Example

20 samples: 10 cancer + 10 normal

Algorithm1:

- all predicted cancer

$$ext{TPR} = rac{ ext{TP}}{ ext{P}} = ext{100\%} \qquad ext{PPV} = rac{ ext{TP}}{ ext{TP} + ext{FP}} = ext{50\%} \quad ext{TNR} = rac{ ext{TN}}{ ext{N}} = ext{0\%}$$

Algorithm2:

- 5 cancerous samples predicted correctly
- 15 samples predicted normal

$$ext{TPR} = rac{ ext{TP}}{ ext{P}} = ext{50\%} \qquad ext{PPV} = rac{ ext{TP}}{ ext{TP} + ext{FP}} = ext{100\%} \quad ext{TNR} = rac{ ext{TN}}{ ext{N}} = ext{100\%}$$



Confusion Matrix (Matching Matrix)

Predicted classes Negative Positive 0 15 negative Negative TN FP Frue label Actual classes positive -Positive FN negative positive Predicted label

https://towardsai.net/p/data-science/how-to-evaluate-you-model-using-the-confusion-matrixe

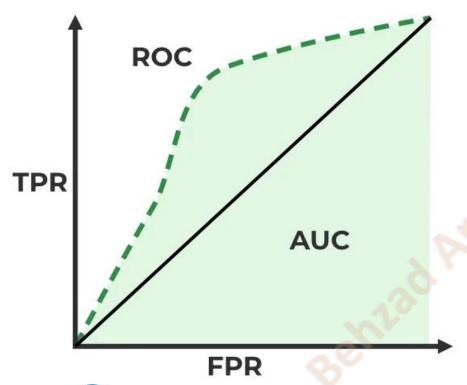






ROC Curve

ROC curve is obtained by plotting TPR against FPR at different **discrimination thresholds**.



https://www.geeksforgeeks.org/auc-roc-curve/







Logistic Regression Discrimination Threshold

Logistic regression model predicts P(Y=1) as a function of X.

$$Ln\left(\frac{P}{1-P}\right) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + ... + \beta_k X_k$$

https://towardsdatascience.com/building-a-logistic-regression-in-python-step-by-step-becd4d56c9c8 https://www.theanalysisfactor.com/what-is-logit-function/



ROC Curve

