

Unsupervised and Unstructured Machine Learning

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Dimensionality Reduction

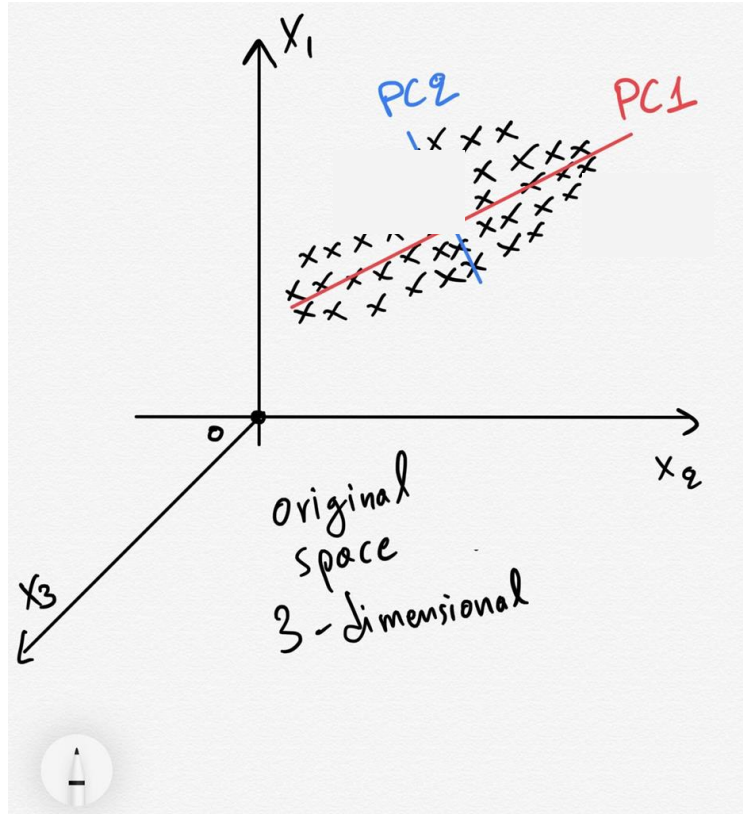
Feature Reduction

Problems with having too many attributes:

- Analyses/Modeling can take a very long time
- Data can take too much space.
- Risk of correlation/redundancy amongst the variables.
 - Difficulty in interpreting the fit of our models.
 - Tend to overemphasize the underlying variable's contribution.
- Helps remove noise.
- Not easy to visualize/interpret.
- Curse of Dimensionality!



Dimensionality Reduction



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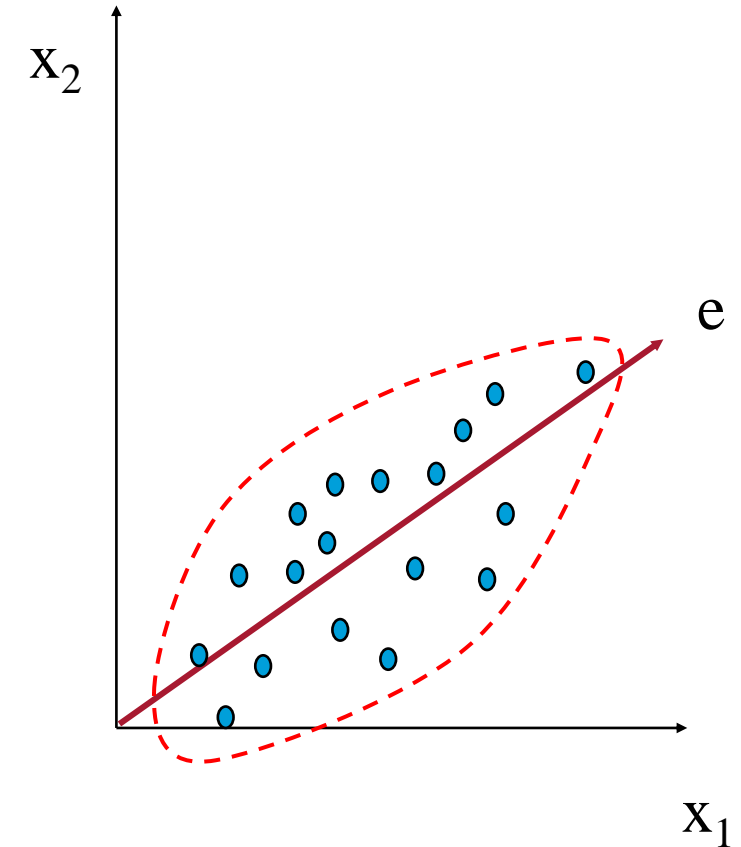
Dimensionality Reduction Techniques

- **Linear:**
 - The new dimensions are a linear combination of the originals.
 - PCA is the prime example of this category.
- **Non-linear:** such, as t-SNE and UMAP.

Principal Component Analysis

Intuition

- Goal is to find direction(s) that captures the largest amount of variation in data.
- We call these direction(s) *principal component(s)*.



Properties of Principal Components

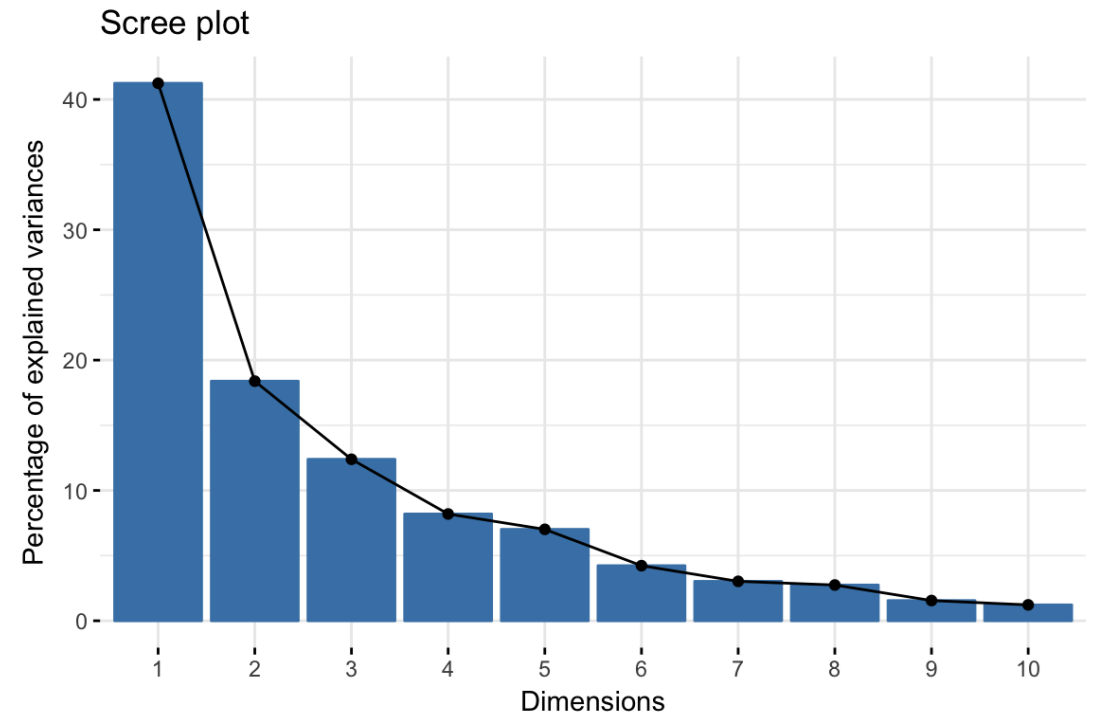
- First component lies along the direction of the data's largest variance/spread.
- Each component is perpendicular to all other components (independence).
- The components are ordered in terms of their ability of explaining the data (i.e., in order of how much variance in the data they capture).
- Let's play with [this](#)

Dimensionality Reduction with PCA

- The number of components available is **equal to** the number of attributes being analyzed.
- However, in *most* analyses, only the first few components account for meaningful amounts of variance (>90%), so only these first few components are retained, interpreted, and used in subsequent analyses.
- When you remove dimensions. You lose some information!

How Many Components do we select?

- Method1: Remove dimensions when reaching a sufficient cumulative explained variance.
- Method2: Elbow method could be used.



Considerations

- PCA assumes the data has linear patterns in terms of the original attribute.
- PCA can be used for Feature Engineering (the new features can be used for down-stream tasks).

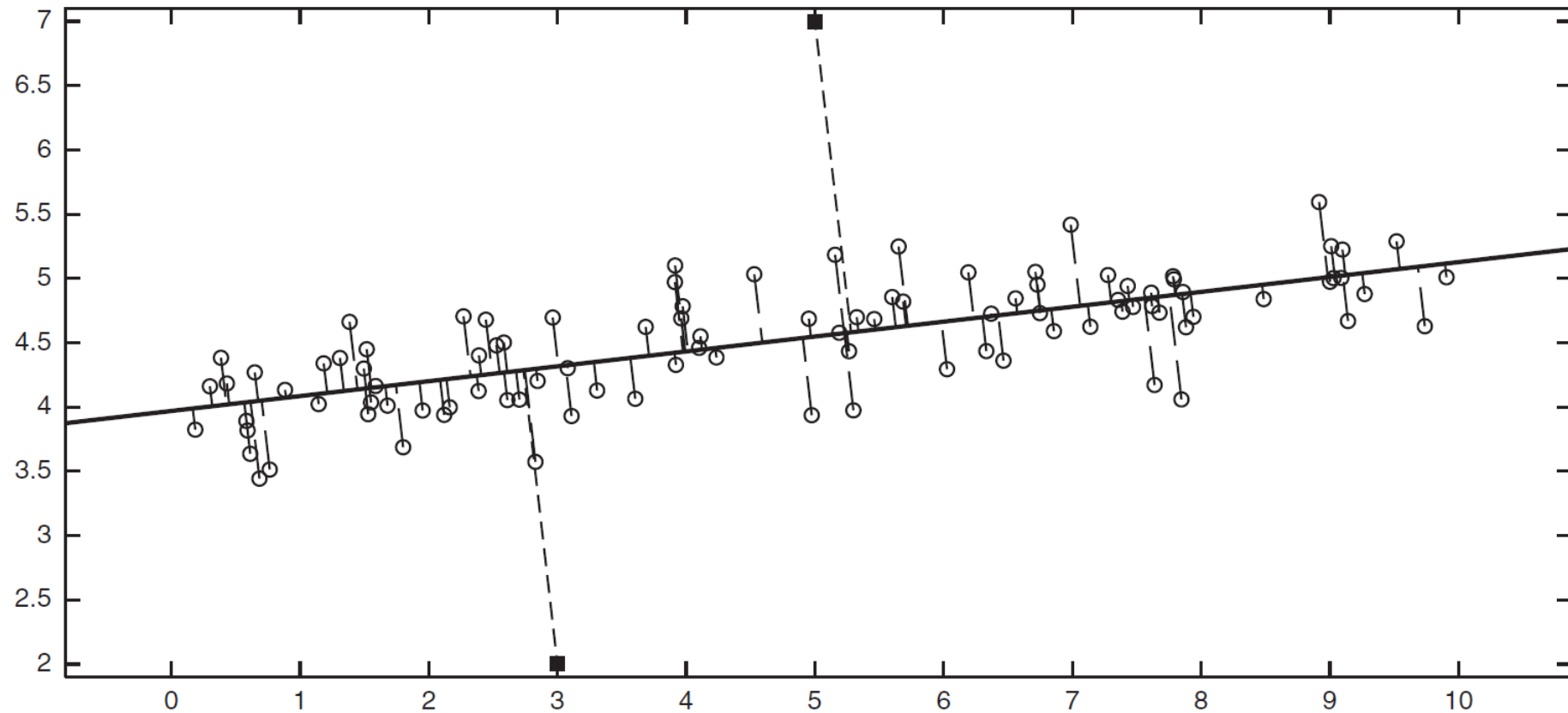
Reconstruction Error

- Let x be the original data point.
- Using PCA, project the point to a lower dimensionality.
- Project the object back to the original space. Call this object \hat{x}

$$\text{Reconstruction Error}(x) = \|x - \hat{x}\|$$

- Points with large reconstruction errors are anomalies

Reconstruction of two-dimensional data



Demo