CLASSIFICATION

ROAD MAP

- **Basic concepts and Decision Trees**

- Inferring rudimentary rules

- Covering rules

- Experiments with Weka

EXAMPLE

- A credit card company receives thousands of applications for new cards. Each application contains information about an applicant,

  - age
  - has_job
  - own_house
  - credit rating
  - etc.

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

- **Problem**: to decide whether an application should be approved, or to classify applications into two categories, approved and not approved.

AN EXAMPLE APPLICATION

- An emergency room in a hospital measures 15 variables (e.g., blood pressure, age, heart rate, etc) of newly admitted patients.

- A decision is needed: whether to send a new patient to an intensive-care unit based on the mortality risk.

- Problem: to predict high-risk patients and distinguish them from low-risk patients.

CLASSIFICATION

- Definition:

- Given a collection of records (training set)

- Each record is by characterized by a tuple (x,y), where x is the attribute set and y is the class label

  - x: attribute, predictor, independent variable, input

  - y: class, response, dependent variable, output

  $$x = (Age, Job, \dots, Rating)$$
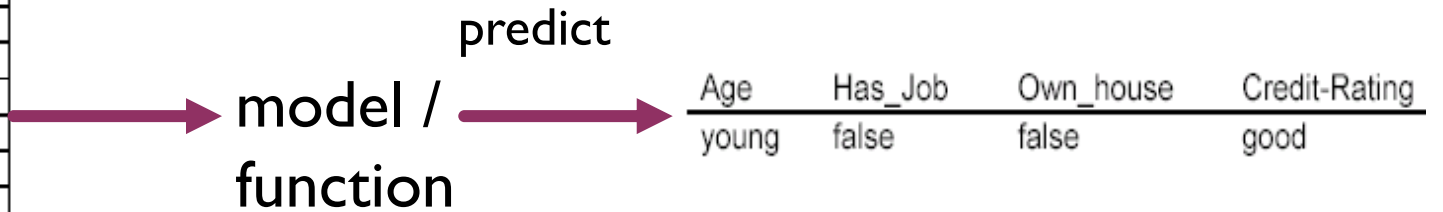
- Our focus:

  Each row = a datapoint

- learn a target function Model

- Use the learned function to predict the values of a discrete class attribute

  - e.g., approve or not-approved, and high-risk or low risk.

Features / variables / attributes

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

Label
= class
= category

ID	Age	Has_Job	Own_House	Credit_Rating	Class
1	young	false	false	fair	No
2	young	false	false	good	No
3	young	true	false	good	Yes
4	young	true	true	fair	Yes
5	young	false	false	fair	No
6	middle	false	false	fair	No
7	middle	false	false	good	No
8	middle	true	true	good	Yes
9	middle	false	true	excellent	Yes
10	middle	false	true	excellent	Yes
11	old	false	true	excellent	Yes
12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

predict

model / function

Age	Has_Job	Own_house	Credit-Rating
young	false	false	good

In real life, it may not follow i.i.d assumption of the supervised learning (classification problem).

Accuracy of correctly classify a datapoint = 8/10 = 80%

SUPERVISED LEARNING PROCESS: TWO STEPS

- **Learning (training)**: learn a model via the training data
- **Testing**: test the model via test data and evaluate the model accuracy

$$Accuracy = \frac{\text{Number of correct classifications}}{\text{Total number of test cases}},$$
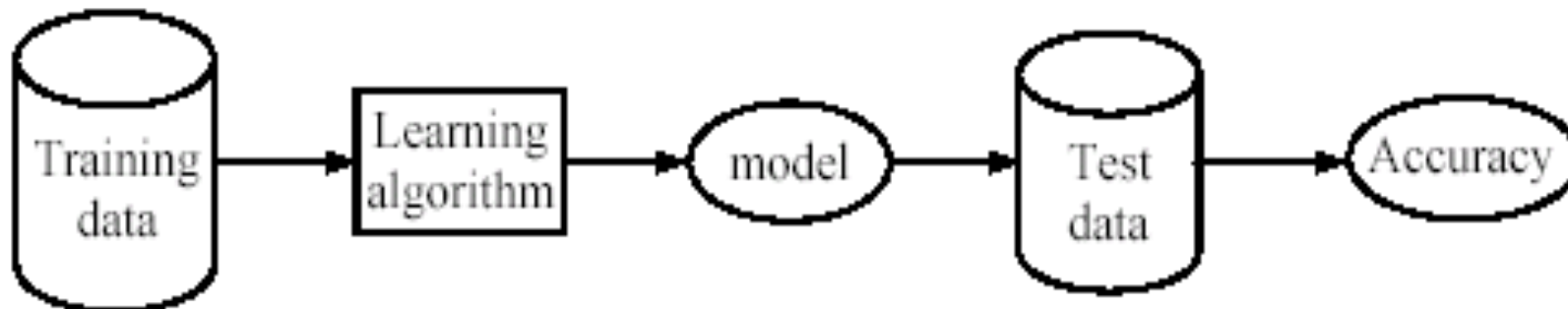
AN EXAMPLE

- **Data**: loan application data
- **Task**: predict whether a loan should be approved or not.
- **Performance measure**: accuracy

No learning: put all test data to the majority class (i.e., Yes):

Accuracy = 8/15 = 53%

- With the learned model, we can do better than 53%.

FUNDAMENTAL ASSUMPTION OF LEARNING

Classification (supervised learning)

Assumption: the distribution of training data is identical to the distribution of test data.

- To achieve good accuracy on the test data, training data must be sufficiently large.
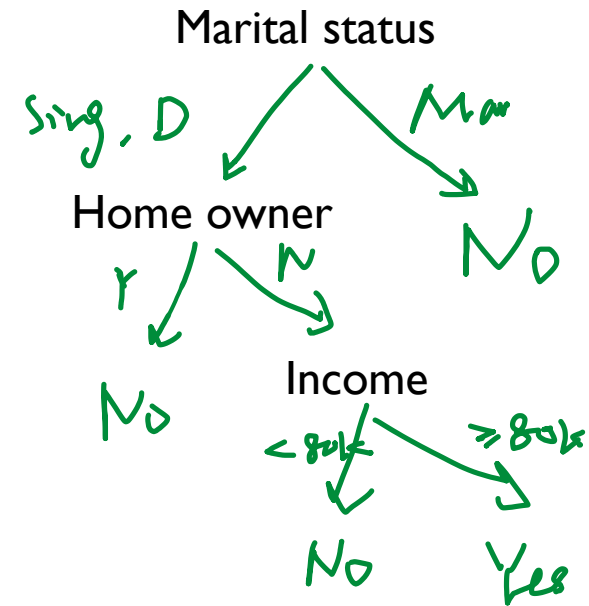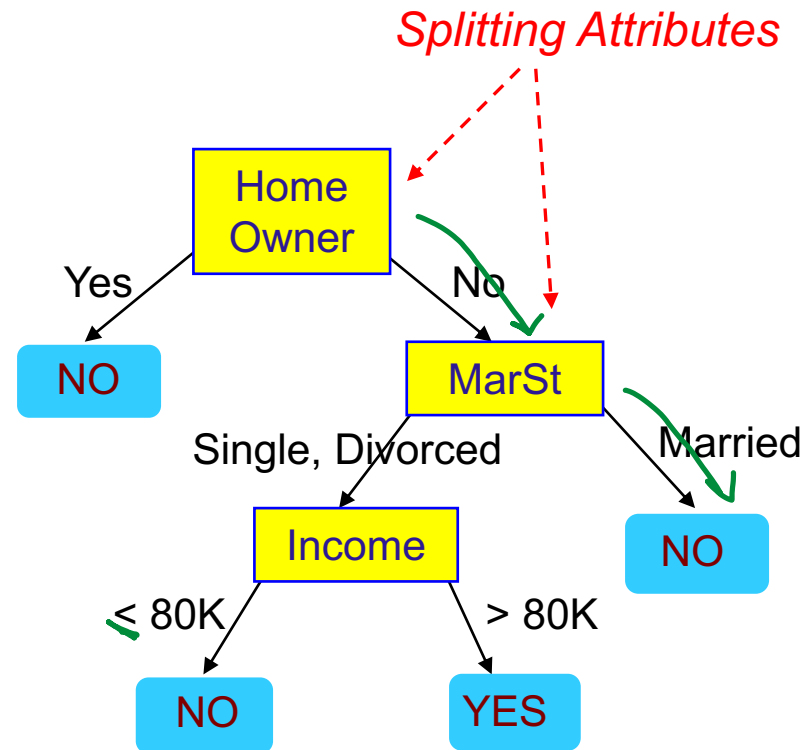
ROAD MAP

- **Basic concepts and Decision Trees**
- Inferring rudimentary rules
- Covering rules
- Experiments with Weka

EXAMPLE OF A DECISION TREE

Home Owner	Marital Status	Annual Income	Defaulted Borrower
No	Married	80K	? _No_

categorical *categorical* *continuous* *class*

ID	Home Owner	Marital Status	Annual Income	Defaulted Borrower
1	Yes	Single	125K	No
2	No	Married	100K	**No**
3	No	Single	70K	No
4	Yes	Married	120K	**No**
5	No	Divorced	95K	**Yes**
6	No	Married	60K	**No**
7	Yes	Divorced	220K	No
8	No	Single	85K	**Yes**
9	No	Married	75K	**No**
10	No	Single	90K	**Yes**

Training Data

Splitting Attributes

Home Owner
- Yes → NO
- No → MarSt
  - Single, Divorced → Income
    - ≤ 80K → NO
    - > 80K → YES
  - Married → NO

Model: Decision Tree

Marital status
- Sing, D
  - Home owner
    - Y → No
    - N → Income
      - <80k → No
      - >80k → Yes
- Mar → No

Start from the root of tree.

Test Data

Home Owner	Marital Status	Annual Income	Defaulted Borrower
No	Married	80K	?

Home Owner

Yes → NO

No → MarSt

Single, Divorced → Income

Married → NO

< 80K → NO

> 80K → YES

APPLY MODEL TO TEST DATA
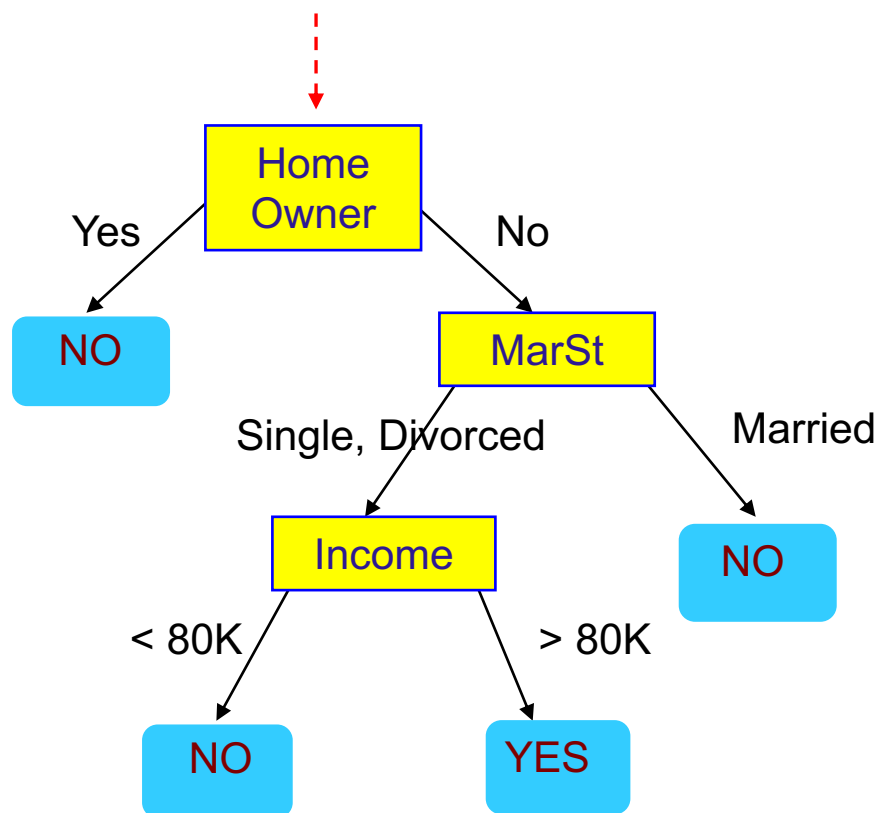
Test Data

Home Owner	Marital Status	Annual Income	Defaulted Borrower
No	Married	80K	?

APPLY MODEL TO TEST DATA
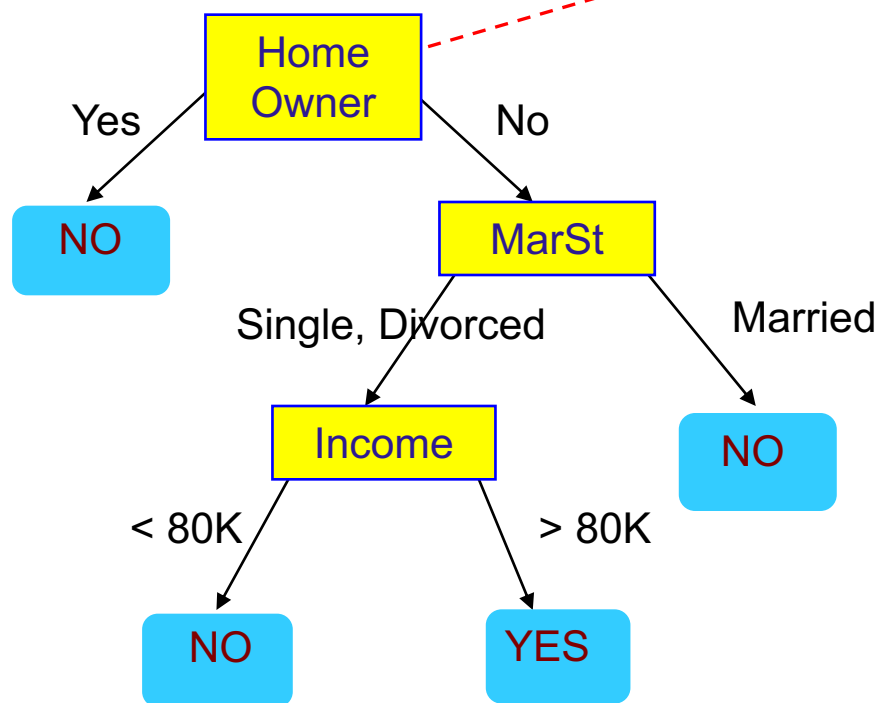
Test Data

Home Owner	Marital Status	Annual Income	Defaulted Borrower
No	Married	80K	?

Assign Defaulted to "No"

categorical *categorical* *continuous* *class*

ID	Home Owner	Marital Status	Annual Income	Defaulted Borrower
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

MarSt

Married → NO

Single, Divorced → Home Owner

Home Owner: Yes → NO

Home Owner: No → Income

Income: < 80K → NO

Income: > 80K → YES

There could be more than one tree that fits the same data!

DECISION TREE CLASSIFICATION TASK

Tid	Attrib1	Attrib2	Attrib3	Class
1	Yes	Large	125K	No
2	No	Medium	100K	No
3	No	Small	70K	No
4	Yes	Medium	120K	No
5	No	Large	95K	Yes
6	No	Medium	60K	No
7	Yes	Large	220K	No
8	No	Small	85K	Yes
9	No	Medium	75K	No
10	No	Small	90K	Yes

Training Set

Tree Induction algorithm

Induction

Learn Model

Model

Decision Tree

Apply Model

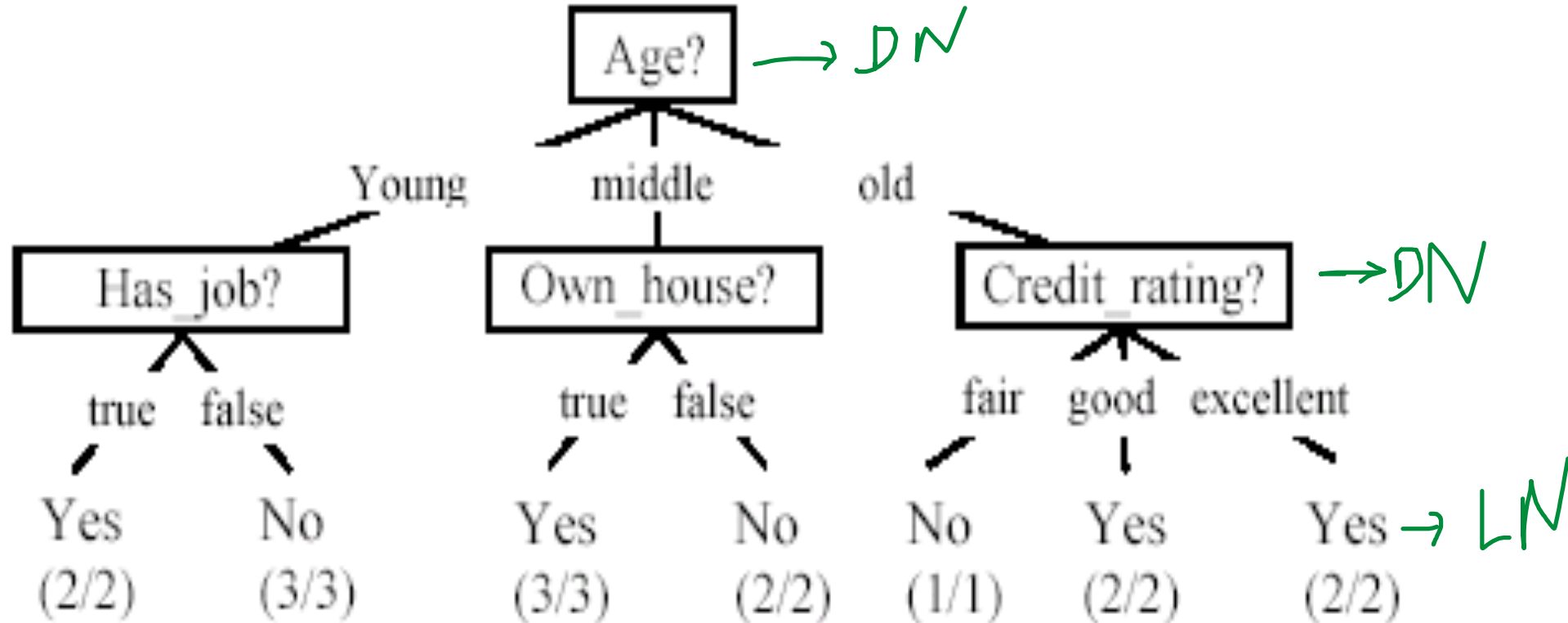| Tid	Attrib1	Attrib2	Attrib3	Class
11	No	Small	55K	?
12	Yes	Medium	80K	?
13	Yes	Large	110K	?
14	No	Small	95K	?
15	No	Large	67K	?

Deduction

Test Set
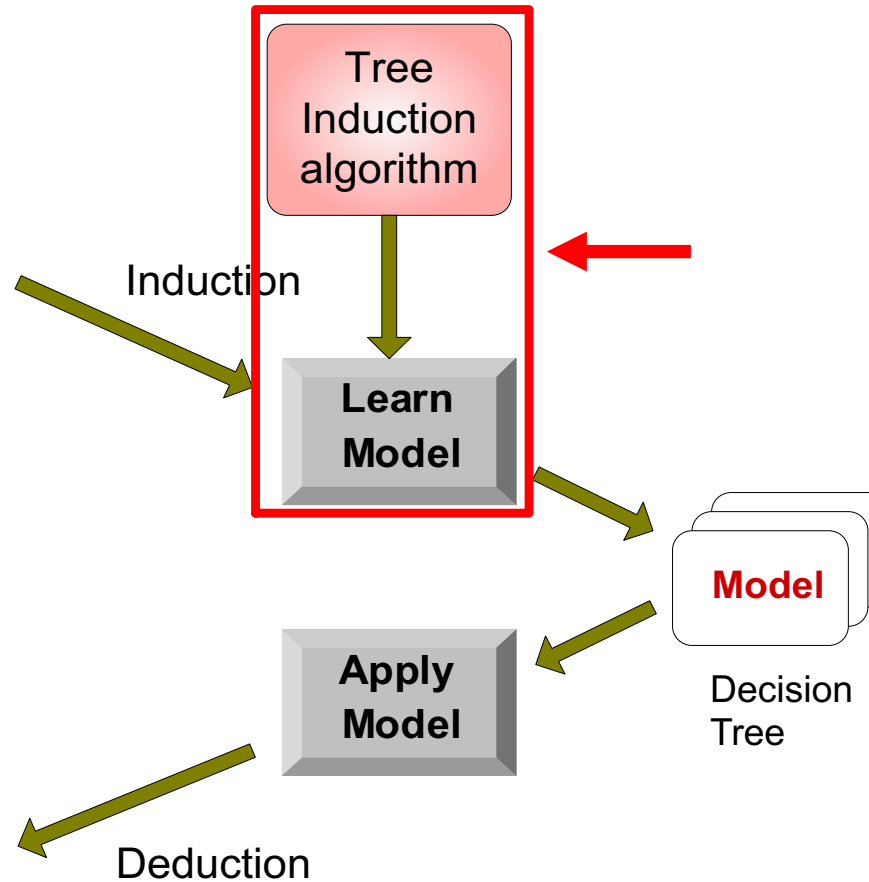
DECISION TREE INDUCTION

- Many Algorithms:
  - Hunt's Algorithm (one of the earliest)
  - CART
  - ID3, C4.5
  - SLIQ,SPRINT

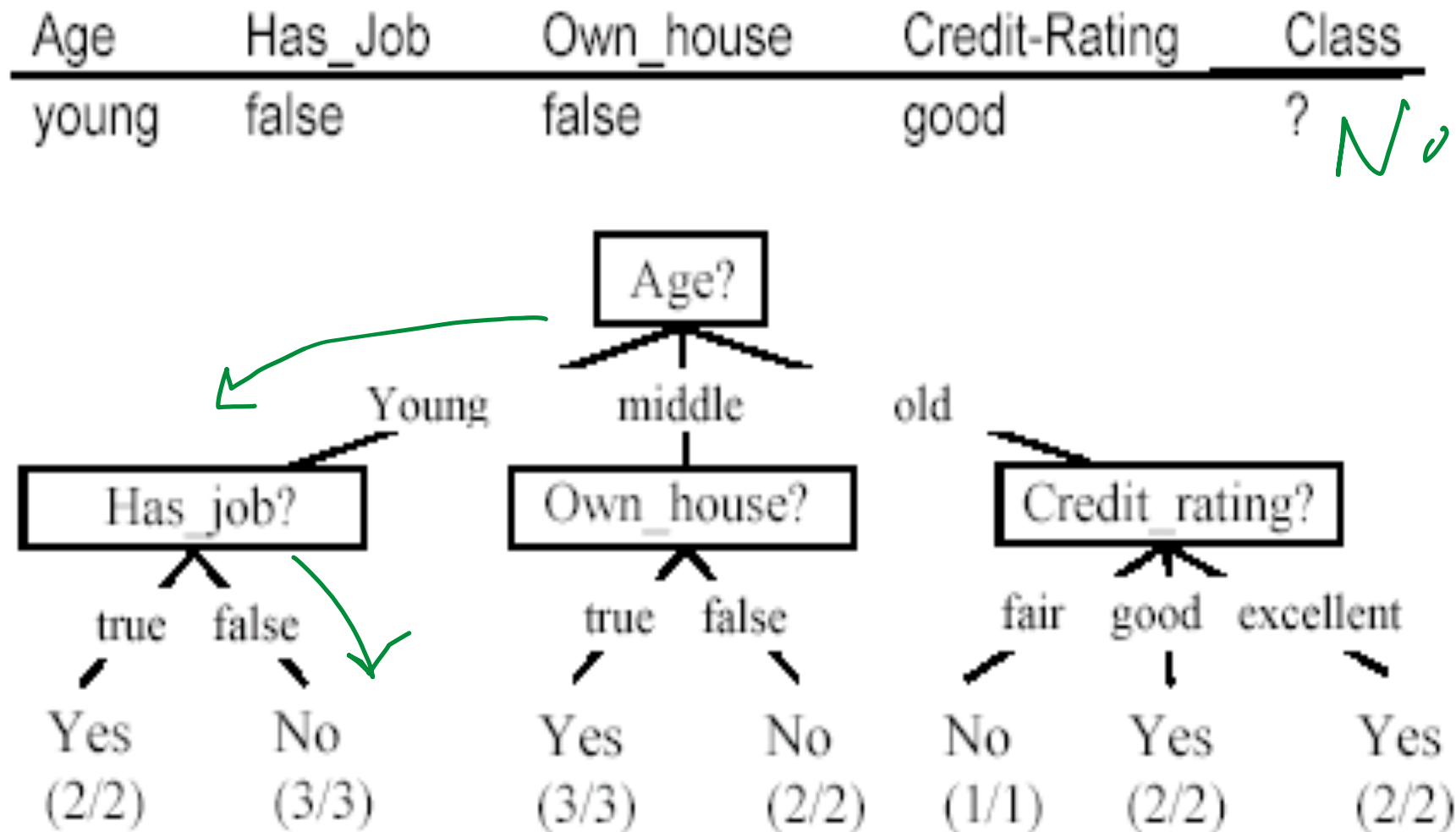| ID	Age	Has_Job	Own_House	Credit_Rating	Class
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5	young	false	false	fair	No
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7	middle	false	false	good	No
8	middle	true	true	good	Yes
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12	old	false	true	good	Yes
13	old	true	false	good	Yes
14	old	true	false	excellent	Yes
15	old	false	false	fair	No

A DECISION TREE FROM THE LOAN DATA

- Decision nodes and leaf nodes (classes)

Age? → DN

Young   middle   old

Has_job?   Own_house?   Credit_rating? → DN

true   false   true   false   fair   good   excellent

Yes   No   Yes   No   No   Yes   Yes → LN
(2/2)   (3/3)   (3/3)   (2/2)   (1/1)   (2/2)   (2/2)

Age	Has_Job	Own_house	Credit-Rating	Class
young	false	false	good	? No

Age?

Young   middle   old

Has_job?   Own_house?   Credit_rating?

true   false   true   false   fair   good   excellent

Yes   No   Yes   No   No   Yes   Yes

(2/2)   (3/3)   (3/3)   (2/2)   (1/1)   (2/2)   (2/2)

20
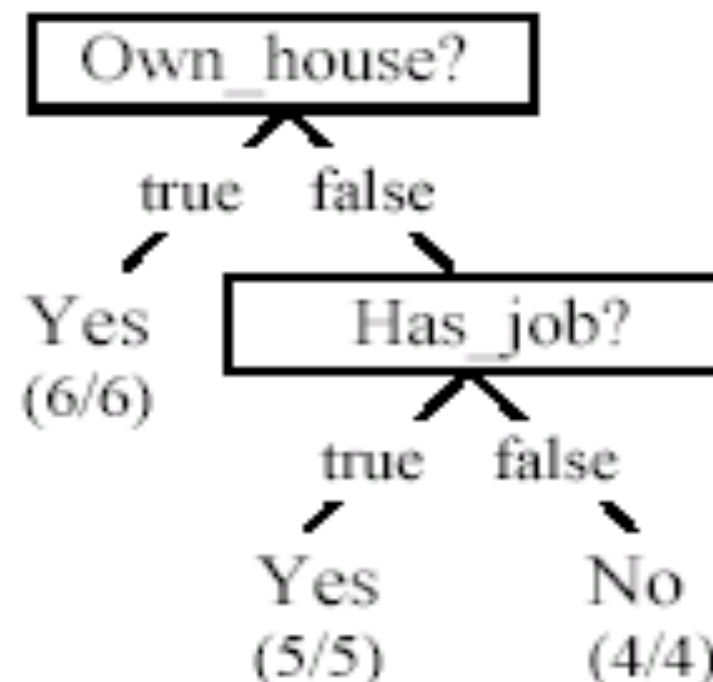
- **No**. There could be many trees.

- We want smaller (easy to understand) and accurate tree (good performance).

Own_house?

true   false

Yes (6/6)

Has_job?

true   false

Yes (5/5)   No (4/4)

21
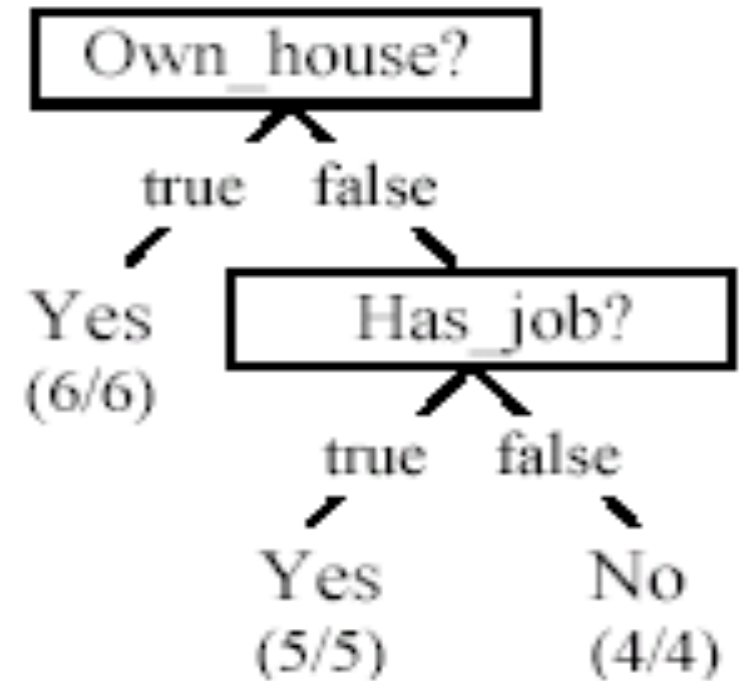
- A decision tree can be converted to a set of rules (if condition)

- Each path from the root to a leaf is a rule.

Own_house?

true   false

Yes
(6/6)

Has_job?

true   false

Yes   No
(5/5)   (4/4)

Own_house = true → Class =Yes   [sup=6/15, conf=6/6]
Own_house = false, Has_job = true → Class = Yes [sup=5/15, conf=5/5]
Own_house = false, Has_job = false → Class = No [sup=4/15, conf=4/4]

ALGORITHM FOR DECISION TREE LEARNING

- Basic algorithm (greedy **divide-and-conquer**)
  - given categorical attributes/features
  - tree is constructed in a **top-down recursive manner**
  - at start, all the training examples are at the root
  - examples are partitioned recursively based on selected attributes
  - attributes are selected based on information gain

ALGORITHM FOR DECISION TREE LEARNING

- When to stop partitioning
  - All examples for a given node belong to the same class
  - There are no remaining attributes for further partitioning
  - There are no examples left