CLUSTERING

CLUSTERING ALGORITHMS

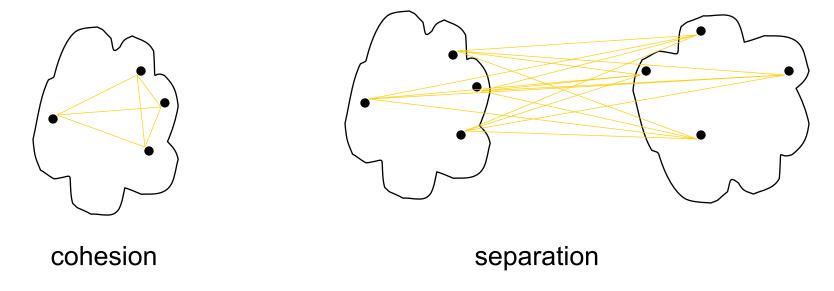
K-means and its variants

Hierarchical clustering

Density-based clustering

UNSUPERVISED MEASURES: COHESION AND SEPARATION

- A proximity graph-based approach can also be used for cohesion and separation.
 - Cluster cohesion is the sum of the weight of all links within a cluster.
 - Cluster separation is the sum of the weights between nodes in the cluster and nodes outside the cluster.

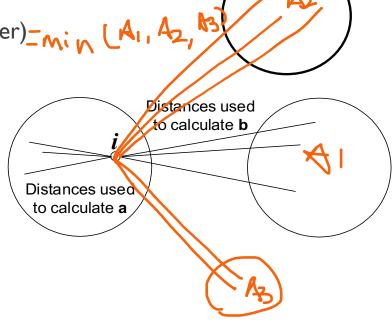


UNSUPERVISED MEASURES: SILHOUETTE COEFFICIENT

- Silhouette coefficient combines ideas of both cohesion and separation, but for individual points, as well as clusters and clusterings
- For an individual point, i
 - Calculate a = average distance of i to the points in its cluster
 - Calculate $b = \min$ (average distance of i to points in another cluster) -min
 - The silhouette coefficient for a point is then given by

$$s = (b - a) / \max(a,b)$$

- Value can vary between -I and I
- Typically ranges between 0 and 1.
- The closer to I the better.



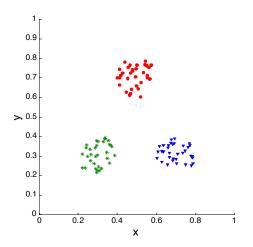
Can calculate the average silhouette coefficient for a cluster or a clustering

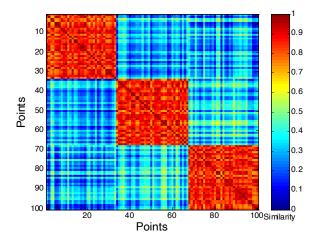
MEASURING CLUSTER VALIDITY VIA CORRELATION

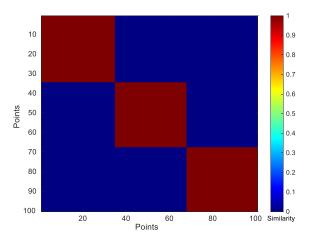
- Two matrices
 - Proximity Matrix
 - Ideal Similarity Matrix
 - One row and one column for each data point
 - An entry is 1 if the associated pair of points belong to the same cluster
 - An entry is 0 if the associated pair of points belongs to different clusters
- Compute the correlation between the two matrices
 - Since the matrices are symmetric, only the correlation between n(n-1) / 2 entries needs to be calculated.
- High magnitude of correlation indicates that points that belong to the same cluster are close to each other.
 - Correlation may be positive or negative depending on whether the similarity matrix is a similarity or dissimilarity matrix
- Not a good measure for some density or contiguity based clusters.

MEASURING CLUSTER VALIDITY VIA CORRELATION

 Correlation of ideal similarity and proximity matrices for the K-means clusterings (partition cluster) of the following wellclustered data set.



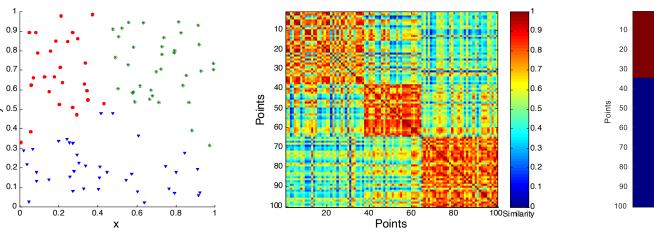


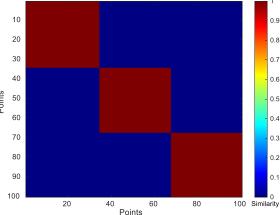


Corr = 0.9235

MEASURING CLUSTER VALIDITY VIA CORRELATION

Correlation of ideal similarity and proximity matrices for the K-means clusterings of the following random data set.

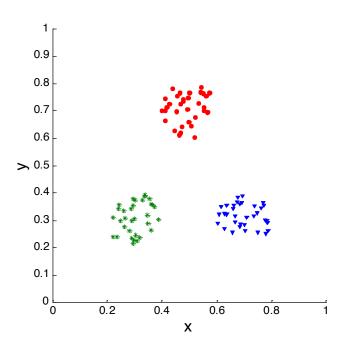


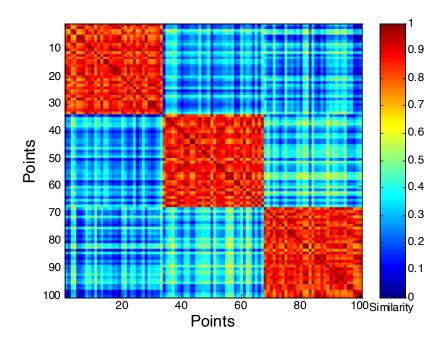


K-means

JUDGING A CLUSTERING VISUALLY BY ITS SIMILARITY MATRIX

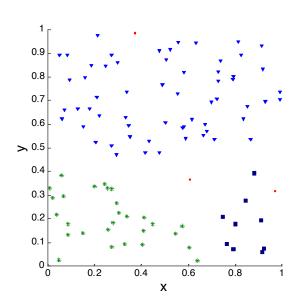
Order the similarity matrix with respect to cluster labels and inspect visually.

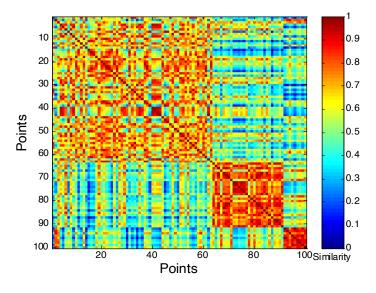




JUDGING A CLUSTERING VISUALLY BY ITS SIMILARITY MATRIX

Clusters in random data are not so crisp

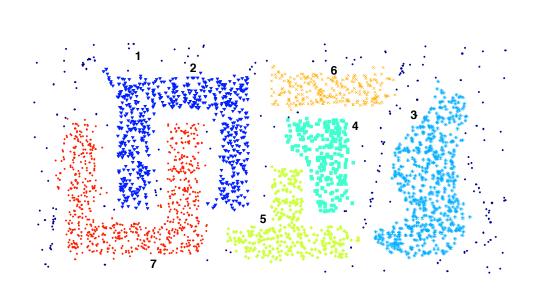


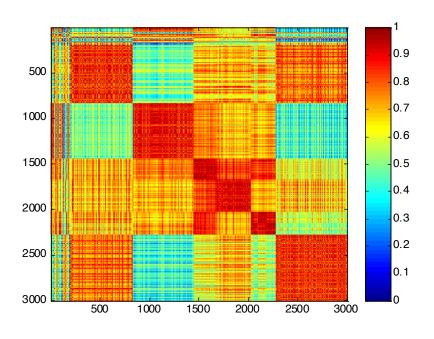


DBSCAN (density based clustering)

Correlation may be not a good measure for some density-based clusters.

JUDGING A CLUSTERING VISUALLY BY ITS SIMILARITY MATRIX





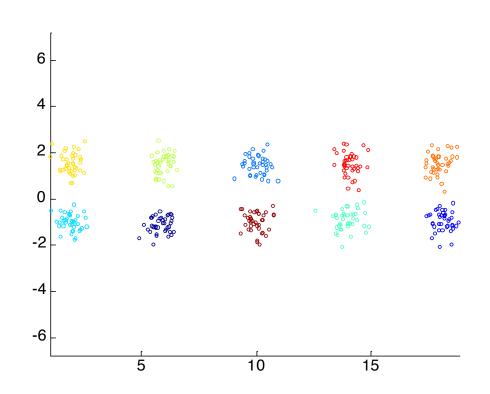
DBSCAN

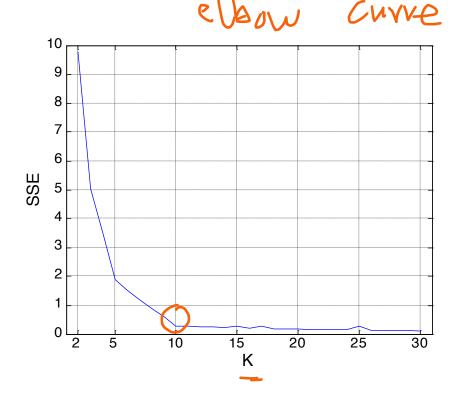
DETERMINING THE CORRECT NUMBER OF CLUSTERS

SSE is good for comparing two clusterings or two clusters

SSE can also be used to estimate the number of clusters

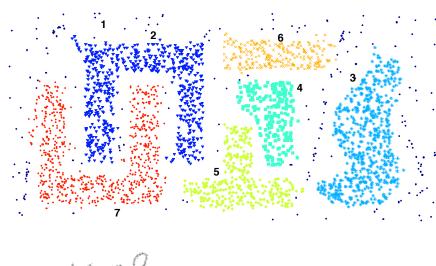
Elbow: after that point, the values of s Do not change dramastically



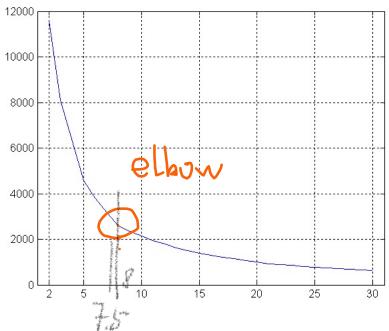


DETERMINING THE CORRECT NUMBER OF CLUSTERS

SSE curve for a more complicated data set







SSE of clusters found using K-means

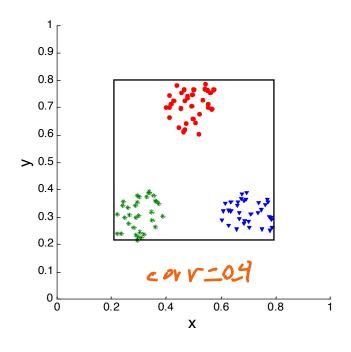
ASSESSING THE SIGNIFICANCE OF CLUSTER VALIDITY MEASURES

- Need a framework to interpret any measure.
 - For example, if our measure of evaluation has the value, 10, is that good, fair, or poor?
- Statistics provide a framework for cluster validity
 - The more "atypical" a clustering result is, the more likely it represents valid structure in the data
 - Compare the value of an index obtained from the given data with those resulting from random data.
 - If the value of the index is unlikely, then the cluster results are valid

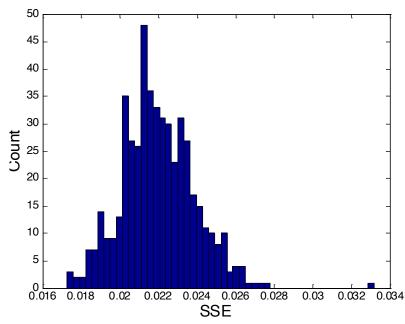
STATISTICAL FRAMEWORK FOR SSE

Example

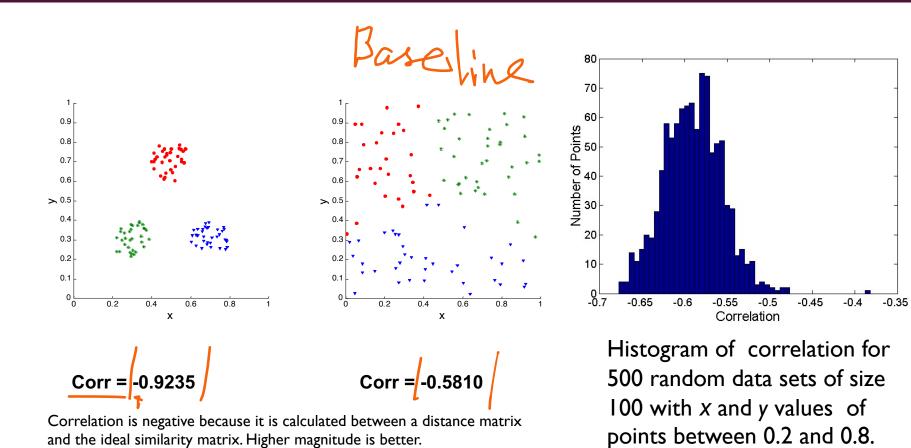
Compare SSE of three cohesive clusters against three clusters in random data



$$SSE = 0.005$$



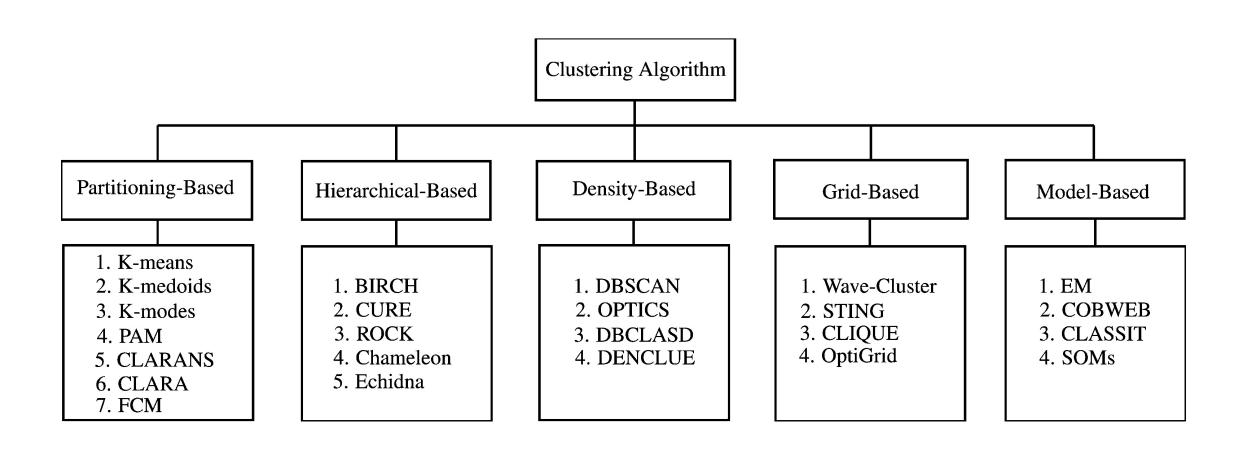
Histogram shows SSE of three clusters in 500 sets of random data points of size 100 distributed over the range 0.2 - 0.8 for x and y values



OTHER CLUSTER METHODS

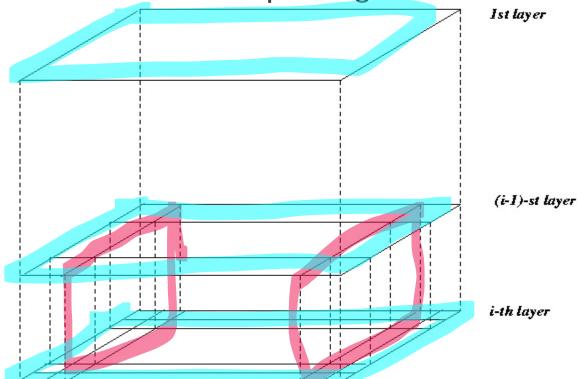
- I. Partitioning Methods
- 2. Hierarchical Methods
- 3. Density-Based Methods
- 4. Grid-Based Methods
- Model-Based Methods
- 6. Clustering High-Dimensional Data
- 7. Constraint-Based Clustering
- 8. Outlier Analysis

SUMMARY



STING: A STATISTICAL INFORMATION GRID APPROACH

- Wang, Yang and Muntz (VLDB'97)
- The spatial area aea is divided into rectangular cells
- There are several levels of cells corresponding to different levels of resolution



THE STING CLUSTERING METHOD

- Each cell at a high level is partitioned into a number of smaller cells in the next lower level
- Statistical info of each cell is calculated and stored beforehand and is used to answer queries
- Parameters of higher level cells can be easily calculated from parameters of lower level cell

(i-1)st layer

count, mean, s, min, max
type of distribution—normal, uniform, etc.

- Use a top-down approach to answer spatial data queries
- Start from a pre-selected layer—typically with a small number of cells
- For each cell in the current level compute the confidence interval

COMMENTS ON STING

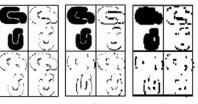
- Remove the irrelevant cells from further consideration
- When finish examining the current layer, proceed to the next lower level
- Repeat this process until the bottom layer is reached
- Advantages:
 - Query-independent, easy to parallelize, incremental update
 - ullet O(K), where K is the number of grid cells at the lowest level
- Disadvantages:
 - All the cluster boundaries are either horizontal or vertical, and no diagonal boundary is detected

WAVE CLUSTER: CLUSTERING BY WAVELET ANALYSIS

- Sheikholeslami, Chatterjee, and Zhang
- A multi-resolution clustering approach which applies wavelet transform to the feature space
- How to apply wavelet transform to find clusters
 - Summarizes the data by imposing a multidimensional grid structure onto data space
 - These multidimensional spatial data objects are represented in a n-dimensional feature space
 - Apply wavelet transform on feature space to find the dense regions in the feature space
 - Apply wavelet transform multiple times which result in clusters at different scales from fine

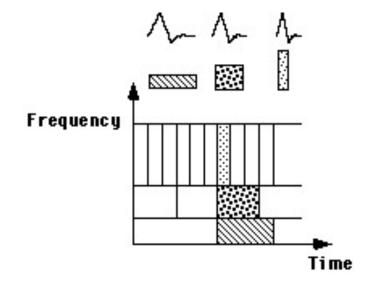


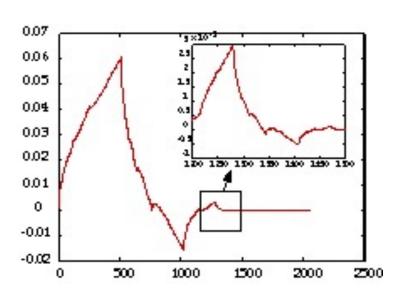
Figure 7.16 A sample of two-dimensional feature space. From [SCZ98].



WAVELET TRANSFORM

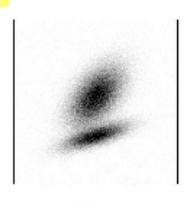
- Wavelet transform: A signal processing technique that decomposes a signal into different frequency sub-band (can be applied to n-dimensional signals)
- Data are transformed to preserve relative distance between objects at different levels of resolution
- Allows natural clusters to become more distinguishable

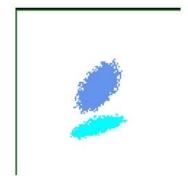




THE WAVECLUSTER ALGORITHM

- Input parameters
 - # of grid cells for each dimension
 - the wavelet, and the # of applications of wavelet transform
- Why is wavelet transformation useful for clustering?
 - Use hat-shape filters to emphasize region where points cluster, but simultaneously suppress weaker information in their boundary
 - Effective removal of outliers, multi-resolution, cost effective
- Major features:
 - Complexity O(N)
 - Detect arbitrary shaped clusters at different scales
 - Not sensitive to noise, not sensitive to input order
 - Only applicable to low dimensional data
- Both grid-based and density-based





h)

QUANTIZATION & TRANSFORMATION

- First, quantize data into m-D grid structure, then wavelet transform
 - a) scale I: high resolution
 - b) scale 2: medium resolution
 - c) scale 3: low resolution

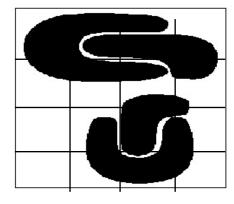
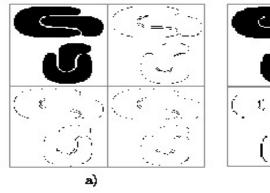
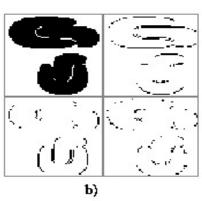


Figure 1: A sample 2-dimensional feature space.





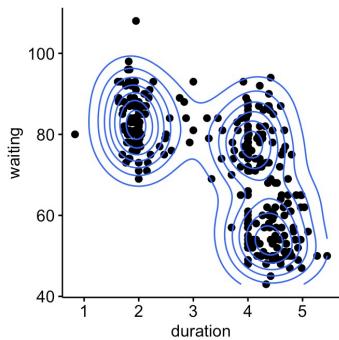


OTHER CLUSTER METHODS

- I. Partitioning Methods (k-means)
- 2. Hierarchical Methods
- 3. Density-Based Methods (non-elliptical shape)
- 4. Grid-Based Methods
- 5. Model-Based Methods
- 6. Clustering High-Dimensional Data
- 7. Constraint-Based Clustering
- 8. Outlier Analysis

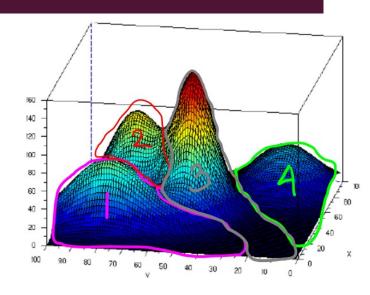
MODEL-BASED CLUSTERING

- What is model-based clustering?
 - Attempt to optimize the fit between the given data and some mathematical model
 - Based on the assumption: Data are generated by a mixture of underlying probability distribution
- Typical methods
 - Statistical approach
 - EM (Expectation maximization), AutoClass
 - Machine learning approach
 - COBWEB, CLASSIT
 - Neural network approach
 - SOM (Self-Organizing Feature Map)



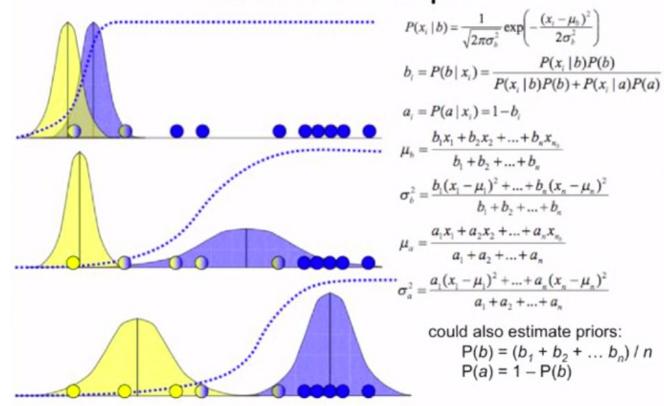
EM — EXPECTATION MAXIMIZATION

- EM A popular iterative refinement algorithm
- An extension to k-means
 - Assign each object to a cluster according to a weight (prob. distribution)
 - New means are computed based on weighted measures
- General idea
 - Starts with an initial estimate of the parameter vector
 - Iteratively rescores the patterns against the mixture density produced by the parameter vector
 - The rescored patterns are used to update the parameter updates
 - Patterns belonging to the same cluster, if they are placed by their scores in a particular component
- Algorithm converges fast but may not be in global optima



EM — EXPECTATION MAXIMIZATION

EM: 1-d example



For each data point, EM calculates a vector of Probabilities.

Each probability will refer to each cluster.

Group the point to the cluster.

THE EM (EXPECTATION MAXIMIZATION) ALGORITHM

- Initially, randomly assign k cluster centers
- Iteratively refine the clusters based on two steps
 - Expectation step: assign each data point X_i to cluster C_i with the following probability

$$P(X_i \in C_k) = p(C_k|X_i) = \frac{p(C_k)p(X_i|C_k)}{p(X_i)},$$

- Maximization step:
 - Estimation of model parameters

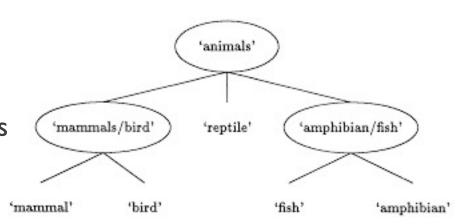
$$m_k = \frac{1}{N} \sum_{i=1}^{N} \frac{X_i P(X_i \in C_k)}{\sum_i P(X_i \in C_i)}$$
.

CONCEPTUAL CLUSTERING

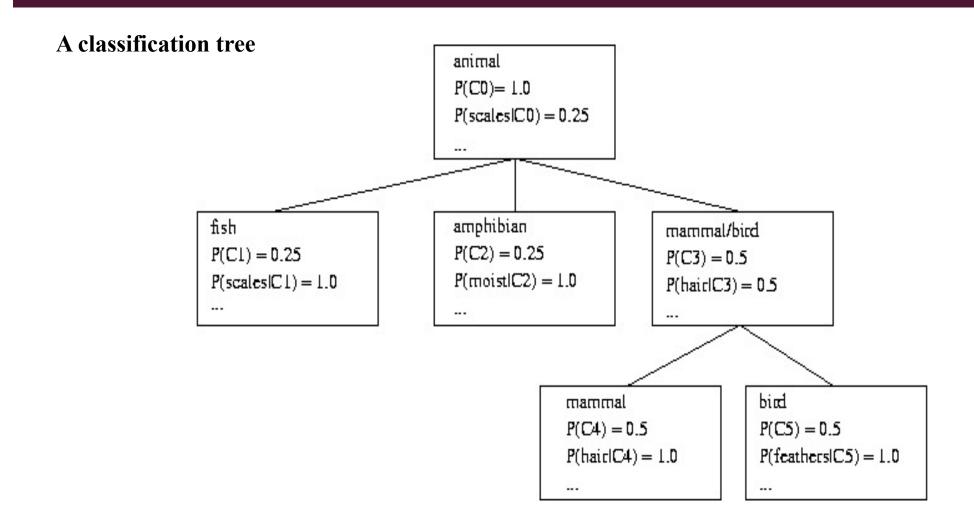
- Conceptual clustering
 - A form of clustering in machine learning
 - Produces a classification scheme for a set of unlabeled objects
 - Finds characteristic description for each concept (class)

COBWEB

- A popular a simple method of incremental conceptual learning
- Creates a hierarchical clustering in the form of a classification tree
- Each node refers to a concept and contains a probabilistic description of that concept



COBWEB CLUSTERING METHOD



MORE ON CONCEPTUAL CLUSTERING

- Limitations of COBWEB
 - The assumption that the attributes are independent of each other is often too strong because correlation may exist
 - Not suitable for clustering large database data skewed tree and expensive probability distributions
- CLASSIT
 - an extension of COBWEB for incremental clustering of continuous data
 - suffers similar problems as COBWEB
- AutoClass (Cheeseman and Stutz, 1996)
 - Uses Bayesian statistical analysis to estimate the number of clusters
 - Popular in industry

NEURAL NETWORK APPROACH

- Neural network approaches
 - Represent each cluster as an exemplar, acting as a "prototype" of the cluster
 - New objects are distributed to the cluster whose exemplar is the most similar according to some distance measure

 | The complete of the cluster whose exemplar is the most similar according to some distance measure

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v UVer- fitting v

- Typical methods
 - SOM (Soft-Organizing feature Map)
 - Competitive learning
 - Involves a hierarchical architecture of several units (neurons)

high dimer => Low features
thousand genear

Neurons compete in a "winner-takes-all" fashion for the object currently being presented

SELF-ORGANIZING FEATURE MAP (SOM)

SOMs, also called topological ordered maps, or Kohonen Self-Organizing Feature Map (KSOMs)

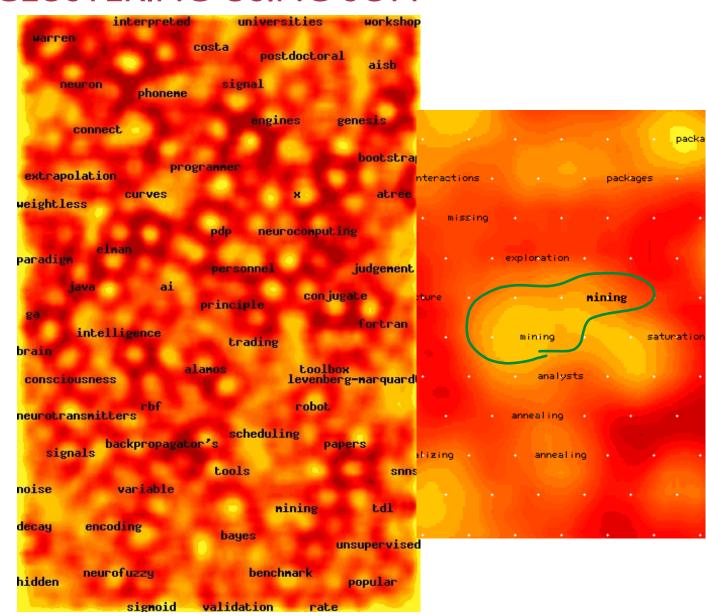
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- It maps all the points in a high-dimensional source space into a 2 to 3-d target space, s.t., the distance and proximity relationship (i.e., topology) are preserved as much as possible
- Similar to k-means: cluster centers tend to lie in a low-dimensional manifold in the feature space
- Clustering is performed by having several units competing for the current object
 - The unit whose weight vector is closest to the current object wins
 - The winner and its neighbors learn by having their weights adjusted
- SOMs are believed to resemble processing that can occur in the brain
- Useful for visualizing high-dimensional data in 2- or 3-D space

WEB DOCUMENT CLUSTERING USING SOM

The result of SOM clustering of
 12088 Web articles (www)

- The picture on the ton fright: drilling down on the keyword "mining"
 - Based on websom.hut.fiWeb page



SUMMARY

