

Final Exam – Part II. Written Test

Your name and student number: _____

- You have **70 minutes** to answer to **6 problems** (100 points).
- Total **7 pages** including this cover page and last two blank pages.
- **Writings on the given box are counted only:** no points for writings outside the box.
- Write answers **clearly and legibly**. No points for ambiguous or illegible writings.
- Read the following quote from *Handong CSEE Standard* and declare your agreement below.

Examination

1. Examination is an educational act necessary for evaluation of the students' achievement and for encouraging the students to absorb the material in the process of preparation.
2. Student should do their best to prepare for exams in order to improve her/his own knowledge and skill and should fully engage in the test during examination hour.
3. Accessing or providing unauthorized information, including other students' answer sheets, is regarded as cheating. The use of electronic devices, including cell phones and computers, without permission is strictly prohibited.
4. Entering or leaving the classroom during the examination before the finish time without permission is regarded as cheating.

I uphold Handong Honor Code and Handong CSEE Standard in taking this exam.

your sign: _____

Problem 1 (16 points)

Suppose that h is a min-heap of integer numbers, and the following sequence of operations are given to h . For the last three operations (marked with `/* draw */`), draw the internal status of h after handling each operation.

```
h = new MinHeap() ;  
h.insert(33) ;  
h.insert(34) ;  
h.insert(23) ;  
h.insert(2) ;  
h.removeMin() ;  
h.insert(95) ;  
h.insert(10) ;  
h.insert(3) ;  
h.removeMin() ; /* draw */  
h.insert(14) ; /* draw */  
h.insert(67) ; /* draw */
```

Problem 2 (21 points)

- (1) Write a pseudo-code of Ternary Search which receives a sorted list of N elements and a target element k , and then returns true if and only if k is in the sorted list. Like Binary Search, Ternary Search recursively narrows down search scope, but Ternary Search divides a list into three at a time (not into two as Binary Search does)

- (2) Analyze the worst-case time complexity of your Ternary Search algorithm.

Problem 3 (16 points)

Suppose that there is a school library system that shows poor performance in searching service, and you found that the system that internally uses a hashmap to store many book information entries. You are wondering if the hashmap causes the performance issue. Discuss about different cases where the hashmap can result the bad performance.

Problem 4 (15 points)

Suppose that you conducted sorting of a large number of strings, first with a quick-sort implementation and then with a radix sort implementation. You found that the quick sort case took less time than the radix sort does. Discuss about this situation.

Problem 5 (20 points)

(a) Write an algorithm that determine whether a given binary tree is complete or not, using the Queue data structure.

(b) Analyze the worst-case time complexity of your algorithm.

Problem 6 (12 points)

How many different AVL trees can store keys $\{1, 2, 3, 4\}$? Note that such a AVL tree may be resulted after inserting and deleting different numbers in different orders.

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