



# A CUDA-based GPU engine for gprMax: Open source FDTD electromagnetic simulation software

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## ABSTRACT

The Finite-Difference Time-Domain (FDTD) method is a popular numerical modelling technique in computational electromagnetics. The volumetric nature of the FDTD technique means simulations often require extensive computational resources (both processing time and memory). The simulation of Ground Penetrating Radar (GPR) is one such challenge, where the GPR transducer, subsurface/structure, and targets must all be included in the model, and must all be adequately discretised. Additionally, forward simulations of GPR can necessitate hundreds of models with different geometries (A-scans) to be executed. This is exacerbated by an order of magnitude when solving the inverse GPR problem or when using forward models to train machine learning algorithms.

We have developed one of the first open source GPU-accelerated FDTD solvers specifically focused on modelling GPR. We designed optimal kernels for GPU execution using NVIDIA's CUDA framework. Our GPU solver achieved performance throughputs of up to 1194 Mcells/s and 3405 Mcells/s on NVIDIA Kepler and Pascal architectures, respectively. This is up to 30 times faster than the parallelised (OpenMP) CPU solver can achieve on a commonly-used desktop CPU (Intel Core i7-4790K). We found the cost-performance benefit of the NVIDIA GeForce-series Pascal-based GPUs – targeted towards the gaming market – to be especially notable, potentially allowing many individuals to benefit from this work using commodity workstations. We also note that the equivalent Tesla-series P100 GPU – targeted towards data-centre usage – demonstrates significant overall performance advantages due to its use of high-bandwidth memory. The performance benefits of our GPU-accelerated solver were demonstrated in a GPR environment by running a large-scale, realistic (including dispersive media, rough surface topography, and detailed antenna model) simulation of a buried anti-personnel landmine scenario.

### New version program summary

Program Title: gprMax

Program Files doi: <http://dx.doi.org/10.17632/kjjm4z87nj.1>

Licensing provisions: GPLv3

Programming language: Python, Cython, CUDA

Journal reference of previous version: Comput. Phys. Comm., 209 (2016), 163–170

Does the new version supersede the previous version?: Yes

Reasons for the new version: Performance improvements due to implementation of CUDA-based GPU engine

Summary of revisions: A FDTD solver has been written in CUDA for execution on NVIDIA GPUs. This is in addition to the existing FDTD solver which has been parallelised using Cython/OpenMP for running on CPUs.

Nature of problem: Classical electrodynamics

Solution method: Finite-Difference Time-Domain (FDTD)

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## 1. Introduction

The desire to simulate larger and more complex scientific problems has created an ever-increasing demand for High-Performance

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Computing (HPC) resources. Parallelised software codes running on HPC facilities have significantly reduced simulation times, and enabled researchers to investigate problems that were not previously computationally feasible. However, HPC facilities are costly to build, maintain, and upgrade, and hence are often only accessible to those working in universities, big businesses, or national research centres. Over the past decade general-purpose computing using graphics processing units (GPGPU) has become a common method for accelerating scientific software. GPGPU is attractive because a GPU has a massively parallel architecture, typically consisting of thousands of efficient cores designed for handling specific tasks simultaneously. In contrast, a CPU has few cores that are designed to handle more generic sequential tasks. Combined with the relatively low cost of GPUs, it makes GPGPU appealing from a cost–performance perspective – from small-scale workstation setups through to large-scale GPU-accelerated HPC facilities. In addition, the creation of programming environments such as CUDA [1], available for NVIDIA GPUs, have made GPGPU computing more accessible to developers without necessitating expertise in computer graphics.

In the field of computational electromagnetics (EM), the Finite-Difference Time-Domain (FDTD) method is one of the most popular numerical techniques for solving EM wave propagation problems. One such set of problems is the simulation of Ground Penetrating Radar (GPR), where the GPR transducer, subsurface/structure, and targets must all be included in the model. GPR antennas are typically impulse-driven and broadband, so the time-domain nature of the FDTD method means this behaviour can be modelled with a single simulation, i.e. separate simulations are not required for each excitation frequency. In general the strengths of the FDTD method are that it is fully explicit, versatile, robust, and relatively simple to implement. However, it can suffer from errors due to 'stair-case' approximations of complex geometrical details, and the aforementioned requirement – to discretise the entire computational domain – can also be disadvantageous in necessitating extensive computational resources. The building block of the FDTD method is the Yee cell [2] in which Maxwell's curl equations are discretised in space and time (usually using second-order accurate derivatives). A leapfrog time-stepping method is used to alternately update the three electric and three magnetic field components in three-dimensional (3D) space. At each time-step the electric and magnetic field updates are performed independently at each point of the computational grid. This grid-based parallelism can be mapped to multiple computational threads running in parallel. This has led to both commercial and open source FDTD EM software being parallelised for CPU solving [3–8] and, more recently, some commercial codes being accelerated using GPGPU. However, there are currently no open source FDTD EM tools that are GPU-accelerated and contain the necessary features to simulate complex, heterogeneous GPR environments. There is a clear need for such tools in areas of GPR research such as full-waveform inversion [9,10] and machine learning [11], where thousands of complex and realistic forward models required to be executed.

We have developed a GPU-accelerated FDTD solver and integrated it into open source EM simulation software that is specifically focused on modelling GPR. In Section 2 we explain the design of the GPU kernels and optimisations that have been employed. Section 3 presents performance comparisons, using simple models, between the existing parallelised CPU solver and our new GPU solver, on a selection of NVIDIA GPUs. In Section 4 we demonstrate the performance of the GPU-accelerated solver with a more representative, realistic GPR simulation, as well as with a large-scale GPR simulation of buried anti-personnel landmines. Finally, Section 5 gives our conclusions.

## 2. Kernel design

A GPU-accelerated FDTD solver has been developed as an integral component of *gprMax*<sup>1</sup> which is open source software that simulates electromagnetic wave propagation, using the FDTD method, for numerical modelling of GPR. *gprMax* is one of the most widely used simulation tools in the GPR community, and has been successfully used for a diverse range of applications in academia and industry [12–17]. It has recently been completely re-written [18] in Python with the CPU solver component written in Cython<sup>2</sup> and parallelised using OpenMP. This recent work [18] also introduced a unique combination of advanced features for simulating GPR including: modelling of dispersive media using multi-pole Debye, Drude or Lorenz expressions [19]; soil modelling using a semi-empirical formulation for dielectric properties and fractals for geometric characteristics [20]; diagonally anisotropic materials; rough surface generation; an unsplit implementation of higher order perfectly matched layers (PMLs) using a recursive integration approach [21]; and the ability to embed complex transducers [22] and targets.

As previously stated one of the reasons the FDTD method is attractive to parallelise is because at each time-step the electric and magnetic field updates can be performed independently at each point of the computational grid. A standard FDTD update equation (omitting the source term) for the electric field component in the  $x$ -direction ( $E_x$ ) is given by (1) [23].

$$E_x \Big|_{i,j+\frac{1}{2},k+\frac{1}{2}}^{n+\frac{1}{2}} = C_{a,E_x} \Big|_{i,j+\frac{1}{2},k+\frac{1}{2}} E_x \Big|_{i,j+\frac{1}{2},k+\frac{1}{2}}^{n-\frac{1}{2}} + C_{b_z,E_x} \Big|_{i,j+\frac{1}{2},k+\frac{1}{2}} \left( H_z \Big|_{i,j+1,k+\frac{1}{2}}^n - H_z \Big|_{i,j,k+\frac{1}{2}}^n \right) - C_{b_y,E_x} \Big|_{i,j+\frac{1}{2},k+\frac{1}{2}} \left( H_y \Big|_{i,j+\frac{1}{2},k+1}^n - H_y \Big|_{i,j+\frac{1}{2},k}^n \right), \quad (1)$$

where  $C_a$  and  $C_b$  are the coefficients related to the material properties,  $H_y$  and  $H_z$  are the magnetic field components in the  $y$ - and  $z$ -directions, the superscript  $n$  denotes the time-step, and the subscripts  $(i, j, k)$  denote the 3D spatial location. It is evident from (1) that updating  $E_x$  is a fully explicit operation, i.e. it depends only on quantities stored in memory from previous time-steps.

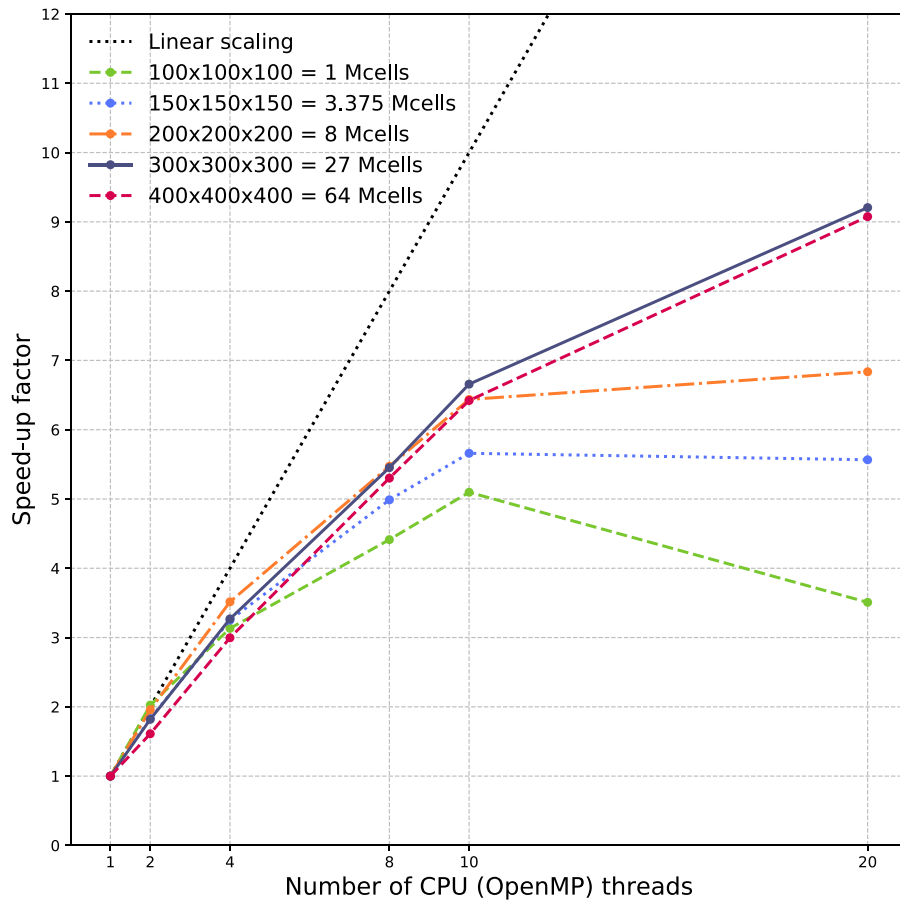
GPUs offer performance advantages over traditional CPUs because they have significantly higher computational floating point performance (through many lightweight cores) coupled with a relatively high bandwidth memory system. The roofline model [24] can be used to determine which of these aspects is the limiting factor, given the ratio of operations to bytes loaded, for any given algorithm. In (1) a total of six field components (electric or magnetic) are either loaded or stored, corresponding to 24 or 48 bytes of data in single or double precision. Seven floating point operations are performed so the ratio is 0.3 (single precision) or 0.15 (double precision), which is much less than the equivalent ratio offered by the hardware (called the "ridge point" in the roofline model terminology). This tells us that the code will not be sensitive to floating point capability, and that the available memory bandwidth will dictate the performance of our algorithm.

Listing 1 shows an example of one of our kernels for updating the electric field for non-dispersive materials. There are several important design decisions and optimisations that we have made with the kernel:

- We use one-dimensional (1D) indexing for defining the number of blocks in a grid, and the number of threads in a

<sup>1</sup> <http://www.gprmax.com>.

<sup>2</sup> <http://www.cython.org>.



**Fig. 1.** Strong scaling CPU solver performance (speed-up compared to a single thread). Different cubic sizes of model domain compared with different numbers of OpenMP threads. CPU: 2 x Intel Xeon E5-2640 v4 2.40 GHz.

**Table 1**  
NVIDIA GPU general specifications.

GPU	Application	Architecture	Cores	Base clock (MHz)	Global memory (GB)
GeForce GTX 1080 Ti	Gaming	Pascal	3584	1480	11
TITAN X	Gaming	Pascal	3584	1417	12
Tesla K40c	Data centre	Kepler	2880	745	12
Tesla K80	Data centre	Kepler	2 × 2496	560	2 × 12
Tesla P100	Data centre	Pascal	3584	1328	16

block. We want to make certain we achieve memory coalescing by ensuring that consecutive threads access consecutive memory locations. This is demonstrated in Listing 1 as  $k$  is the fastest moving thread index, and consecutive  $k$ s correspond to consecutive elements of  $E_x$ . We are aware of other implementations for domain-decomposition using two-dimensional planes or fully 3D indexing [25–27]. However, we found 1D indexing offered simpler implementation, similar performance, and more flexibility in terms of different domain sizes that might be encountered.

- We define macros within all the GPU kernels to convert from traditional 3D subscripts ( $i, j, k$ ) to linear indices that are required to access arrays in GPU memory. The macros are principally used to maintain readability, i.e. both CPU and GPU codes closely resemble the traditional presentation of the FDTD algorithm. If linear indices had been used directly the kernel would be much less readable and would differ from the CPU solver which uses traditional 3D subscripts to access 3D arrays. This design choice takes on further significance for the more complex kernels, such as those used to update the electric and magnetic field components for materials with

multi-pole Debye, Lorenz, or Drude dispersion, or those used to update the PML.

- We make use of the constant memory (64 KB), available through CUDA, on NVIDIA GPUs. Constant memory is cached, so normally costs only a read from cache which is much faster than a read from global memory. Electric and magnetic material coefficients, i.e.  $C_a$  and  $C_b$  from (1), for materials in a model are stored in constant memory.
- We mark pointers to arrays which will be read-only with the `const` and `restrict` qualifiers. This increases the likely-hood that the compiler will detect the read-only condition, and can therefore make use of the texture cache – a special on-chip resource designed to allow efficient read-only access from global memory.
- Finally, we include the functions to update all the electric field components,  $E_x$ ,  $E_y$ , and  $E_z$ ,<sup>3</sup> in a single kernel, to benefit from kernel caching.

<sup>3</sup> For the sake of brevity only the function for updating the  $E_x$  component is shown.

```

// Macros for converting subscripts to linear index:
#define INDEX2D_MAT(m, n) (m)*($NY_MATCOEFFS)+(n)
#define INDEX3D_FIELDS(i, j, k)
    ↪ (i)*($NY_FIELDS)*($NZ_FIELDS)+(j)*($NZ_FIELDS)+(k)
#define INDEX4D_ID(p, i, j, k)
    ↪ (p)*($NX_ID)*($NY_ID)*($NZ_ID)+(i)*($NY_ID)*($NZ_ID)+(j)*($NZ_ID)+(k)

// Material coefficients (read-only) in constant memory (64KB)
__device__ __constant__ $REAL updatecoeffsE[$N_updatecoeffsE];

__global__ void update_e(int NX, int NY, int NZ, const unsigned int*
    ↪ __restrict__ ID, $REAL *Ex, $REAL *Ey, $REAL *Ez, const $REAL*
    ↪ __restrict__ Hx, const $REAL* __restrict__ Hy, const $REAL*
    ↪ __restrict__ Hz) {

    // Obtain the linear index corresponding to the current thread
    int idx = blockIdx.x * blockDim.x + threadIdx.x;

    // Convert the linear index to subscripts for 3D field arrays
    int i = idx / ($NY_FIELDS * $NZ_FIELDS);
    int j = (idx % ($NY_FIELDS * $NZ_FIELDS)) / $NZ_FIELDS;
    int k = (idx % ($NY_FIELDS * $NZ_FIELDS)) % $NZ_FIELDS;

    // Convert the linear index to subscripts for 4D material ID array
    int i_ID = (idx % ($NX_ID * $NY_ID * $NZ_ID)) / ($NY_ID * $NZ_ID);
    int j_ID = ((idx % ($NX_ID * $NY_ID * $NZ_ID)) % ($NY_ID * $NZ_ID)) /
    ↪ $NZ_ID;
    int k_ID = ((idx % ($NX_ID * $NY_ID * $NZ_ID)) % ($NY_ID * $NZ_ID)) %
    ↪ $NZ_ID;

    // Ex component
    if ((NY != 1 || NZ != 1) && i >= 0 && i < NX && j > 0 && j < NY && k >
    ↪ 0 && k < NZ) {
        int materialEx = ID[INDEX4D_ID(0,i_ID,j_ID,k_ID)];

        Ex[INDEX3D_FIELDS(i,j,k)] =
            ↪ updatecoeffsE[INDEX2D_MAT(materialEx,0)] *
            ↪ Ex[INDEX3D_FIELDS(i,j,k)] +
            ↪ updatecoeffsE[INDEX2D_MAT(materialEx,2)] *
            ↪ (Hz[INDEX3D_FIELDS(i,j,k)] - Hz[INDEX3D_FIELDS(i,j-1,k)]) -
            ↪ updatecoeffsE[INDEX2D_MAT(materialEx,3)] *
            ↪ (Hy[INDEX3D_FIELDS(i,j,k)] - Hy[INDEX3D_FIELDS(i,j,k-1)]);
    }
}

```

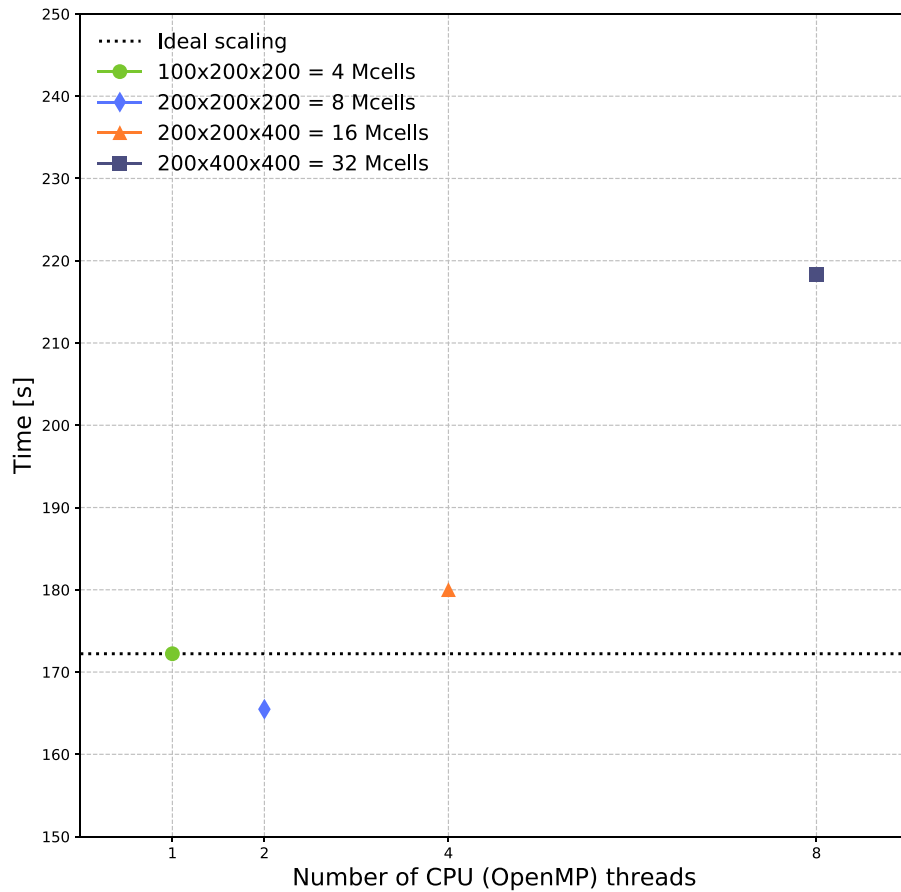
Listing 1: Kernel for electric field updates of non-dispersive materials

### 3. Performance analysis

The host machine used to carry out performance comparisons between the CPU and GPU-accelerated solvers was a SuperMicro SYS-7048GR-TR with 2 x Intel Xeon E5-2640 v4 2.40 GHz processors, 256GB RAM, and CentOS Linux (7.2.1511) operating system. We tested five different NVIDIA GPUs, the specifications of which are given in Table 1. The GPUs feature a mixture of current generation NVIDIA architecture (Pascal) and previous generation (Kepler). The GPUs are also targeted at different applications, with the GeForce GTX 1080 Ti and TITAN X being principally aimed at the computer gaming market, whilst the Tesla K40c, Tesla K80, and Tesla P100 intended to be used in HPC or data centre environments. Before testing our own kernels we ran the BabelStream

benchmark [28] to investigate the maximum achievable memory bandwidth for each GPU. Table 2 presents the results of the BabelStream benchmark alongside the theoretical peak memory bandwidth for each GPU. Table 2 shows that reaching between 66% and 75% theoretical peak memory bandwidth is the maximum performance that we can expect to achieve, with the Pascal generation of GPUs capable of achieving closer to their theoretical peak memory bandwidth than the previous Kepler-based GPUs.

We carried out initial performance testing of the GPU-accelerated solver using models with cubic domains of side length ranging from 100 to 400, or 450 cells. For each of the model sizes the entire domain was filled with free-space, the spatial resolution was  $\Delta x = \Delta y = \Delta z = 1$  mm, and the temporal resolution was  $\Delta t = 1.926$  ps (i.e. at the Courant, Friedrichs and Lewy limit). A Hertzian dipole was used as a (soft/additive) source, and excited



**Fig. 2.** Weak scaling CPU solver performance (execution time compared to a single thread). Size of model domain is increased in proportion to number of OpenMP threads. CPU: 2 x Intel Xeon E5-2640 v4 2.40 GHz.

**Table 2**  
NVIDIA GPU memory bandwidth (FP32)

GPU	Theoretical peak memory bandwidth (GB/s)	BabelStream memory bandwidth (GB/s)	Percentage theoretical peak
GeForce GTX 1080 Ti	484	360	74%
TITAN X	480	360	75%
Tesla K40c	288	191	66%
Tesla K80	2 × 240	160	66%
Tesla P100	732	519	71%

with a waveform of the shape of the first derivative of a Gaussian. The centre frequency of this waveform was 900 MHz. The time histories of the electric and magnetic field components were stored from a single observation point close to the source. Although these initial models are unrepresentative of a typical GPR simulation, they provide a valuable baseline for evaluating the performance of the CPU and GPU-accelerated solvers.

Before evaluating the GPU-accelerated solver an overview of the performance of the CPU solver is presented in Figs. 1 and 2. Fig. 1 shows speed-up factors for different sizes of test model using different numbers of OpenMP threads — from a single thread up to the total number of physical CPU cores available on the host machine ( $2 \times 10 = 20$  threads), i.e. strong scaling. For smaller simulations ( $< \approx 3$  million cells or  $144^3$  model), on this host machine, using more than 10 threads has no impact, or is even detrimental, to performance. This is likely because the computational overhead of creating and destroying the additional threads is greater than the time saved by having more threads doing work. The speed-up trend converges as the number of cells increase, and is almost

identical for the  $300^3$  and  $400^3$  models. At this point the work done by each thread has exceeded the overhead of creating and destroying the thread. The overall speed-up trend decreases beyond 4–8 threads, and falls to around 50% with 20 threads. We would only expect to see ideal speed-up if our algorithm was compute (or cache) bound. Our algorithm is bound by memory bandwidth which is a shared resource across threads. Although adding more threads allows a higher percentage of this to be used, it is not a linear correlation due to the nature of the hardware. Also depending on where the data is allocated on memory in relation to where it is accessed, there may also be non-uniform memory access (NUMA) effects. This behaviour is further evidenced by Fig. 2, which shows execution times when the model size is increased in proportion to the number of threads, i.e. weak scaling. In this test ideal scaling is when the execution time stays constant when larger models with more threads are computed.

A more useful benchmark of performance is to measure the throughput of the solver, typically given by (2).

$$P = \frac{NX \cdot NY \cdot NZ \cdot NT}{T \cdot 1 \times 10^6}, \quad (2)$$

where  $P$  is the throughput in millions of cells per second;  $NX$ ,  $NY$ , and  $NZ$  are the number of cells in domain in the  $x$ ,  $y$ , and  $z$  directions;  $NT$  is the number of time-steps in the simulation; and  $T$  is the runtime of the simulation in seconds. Fig. 3 shows comparisons of performance throughput for the CPU solver on different CPUs:  $1 \times$  Core i7-4790 K CPU (4 GHz, 4 cores),  $2 \times$  Xeon E5520 (2.26 GHz, 8 cores), and  $2 \times$  Xeon E5-2640 v4 (2.4 GHz, 20 cores). It is intended to provide an indicative guide to the performance of the CPU solver on three different Intel CPUs from typical desktop and server machines.



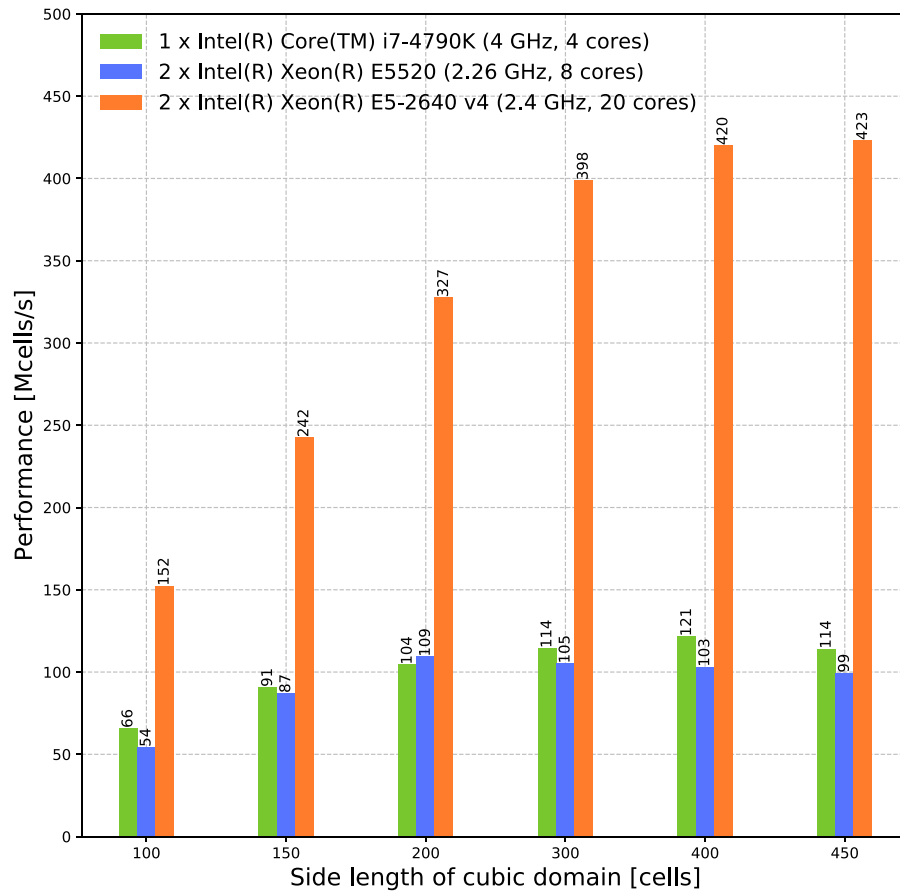


Fig. 3. CPU solver performance throughput on different CPUs.

**Table 3**  
NVIDIA GPU floating point (FP) performance.

GPU	FP32 performance (TFLOPS)	FP64 performance (TFLOPS)
GeForce GTX 1080 Ti	11.3	0.35
TITAN X	11	0.34
Tesla K40c	4.29	1.43
Tesla K80	8.74	2.91
Tesla P100	10.6	5.3

Figs. 4 and 5 show comparisons of performance throughput for both the CPU solver (using 2 × Xeon E5-2640 v4 (2.4 GHz, 20 cores)) and the GPU-accelerated solver on the five different NVIDIA GPU cards. The Kepler-based Tesla K40c and Tesla K80 exhibit similar performance to one another, and the Pascal-based TITAN X and GeForce GTX 1080 Ti also have similar performance to one another in all the tests. This is expected given these cards have similar memory bandwidth. The TITAN X and GeForce GTX 1080 Ti performance is approximately twice the throughput of the Kepler cards. The Tesla P100 has the highest memory bandwidth, and also has the highest performance throughput. The performance throughput for all the GPUs begins to plateau for models sizes of 300<sup>3</sup> and larger, which is because the arrays that the kernels are operating on become large enough to saturate the memory bandwidth.

We investigated both single and double precision performance, as for many GPR simulations single precision output provides sufficient accuracy. Table 3 shows that the Tesla-series cards have peak double precision performance that is half of their peak single precision performance. The TITAN X and GeForce GTX 1080 Ti are designed for single precision performance, so their double

precision performance is worse than half of the single precision performance. However, as previously explained the performance of our GPU kernels is governed by memory bandwidth rather than floating point performance. Figs. 4 and 5 show that the performance of the Tesla-series GPUs as well as the TITAN X and GeForce GTX 1080 Ti GPUs halves when comparing double to single precision. This reduction in performance happens because twice the amount of data is being loaded/stored for the double precision results, so the time doubles because the memory bandwidth is fixed.

Finally, we used the NVIDIA CUDA profiler (nvprof) to measure the actual read/write throughput of our kernels. Summing the average read/write bandwidth for the kernel that updates the electric field gave 320 GB/s, compared to 360 GB/s from the BabelStream benchmark given in Table 2. The kernel that updates the magnetic field gave a similar result. This shows that our kernels are performing in a state that is close to the optimum that can be achieved.

#### 4. GPR example simulations

Following the initial performance assessment of the GPU-accelerated solver with simple models, we carried out further testing with more realistic, representative models for GPR. Both of the presented example simulations use some of the advanced features of gprMax such as: modelling dispersive media (for which GPU kernels have been written) using multi-pole Debye expressions; soil modelling using a semi-empirical formulation for dielectric properties, and fractals for geometric characteristics; rough surface generation; and the ability to embed complex transducers.

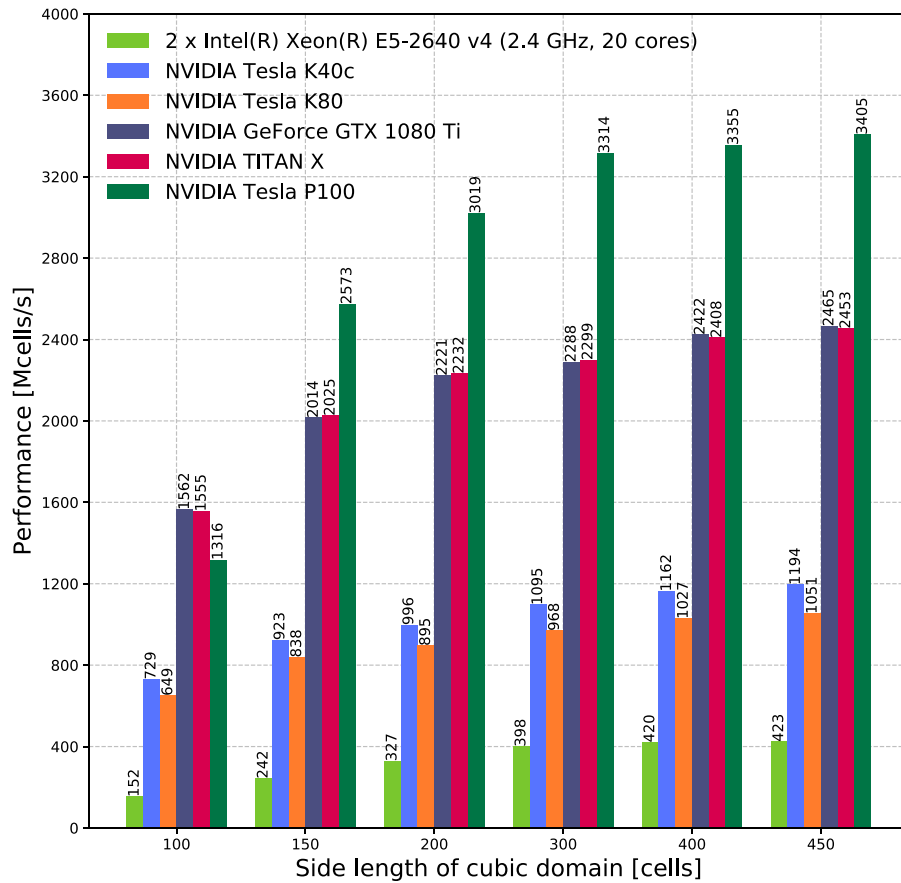


Fig. 4. CPU solver and GPU-accelerated solver performance throughput (FP32).

#### 4.1. Buried utilities model

The first example model represents a common environment for which GPR is used in Civil Engineering, which is detecting and locating buried pipes and utilities. Fig. 6 shows the FDTD mesh of the model which contains: a GPR antenna model, similar to a Geophysical Survey Systems, Inc. (GSSI) 1.5 GHz (Model 5100) antenna; a heterogeneous, dispersive soil with a rough surface; a 100 mm diameter metal pipe with centre at  $x = 0.25$  m,  $z = 0.31$  m; a 300 mm diameter high-density polyethylene (HDPE) pipe with centre at  $x = 0.6$  m,  $z = 0.2$  m; and  $2 \times 50$  mm diameter metal cables with centres at  $x = 0.9$  m,  $z = 0.51$  m and  $x = 1.05$  m,  $z = 0.51$  m. The model domain size was  $600 \times 100 \times 500$  cells, the spatial resolution was  $\Delta x = \Delta y = \Delta z = 2$  mm, and a temporal resolution of  $\Delta t = 3.852$  ps (i.e. at the Courant, Friedrichs and Lewy limit) was used. Firstly, a single model (A-scan) was used to benchmark the performance of each of the different NVIDIA GPUs, with the results shown in Table 4. The pattern of performance between the different GPUs is the same as found for the simple models. However, the absolute values of throughput are three times less than those for the equivalent size of simple model ( $300^3$ ), e.g. TITAN X  $300^3$  model – 2288 Mcells/s, TITAN X buried utilities model – 721 Mcells/s. This reduction in throughput is due to the additional operations (loads and stores) in the more complex kernels, which are required to simulate the soil which has materials with dispersive, i.e. frequency dependent, properties.

Fig. 7 shows the results of the complete simulation, which is a B-scan composed of 91 A-scans with an inline spacing of 10 mm.<sup>4</sup>

<sup>4</sup> The only processing of the B-scan data was to apply a quadratic gain function to enhance the target responses in the lossy soil.

Table 4

Buried utilities model: A-scan runtimes and performance throughput on different NVIDIA GPUs.

CPU/GPU Name	A-scan runtime [s]	Performance [Mcells/s]
2 x Intel(R) Xeon(R) E5-2640 v4	922	127
GeForce GTX 1080 Ti	161	726
TITAN X	162	721
Tesla K40c	374	312
Tesla K80	389	300
Tesla P100	129	906

The interpretation of the B-scan is not the subject of this paper, but typical hyperbolic responses from the cylindrical targets can be observed, including responses from the top and bottom surface of the air-filled HDPE pipe. The B-scan was simulated utilising the MPI task farm functionality of gprMax, which allows models (A-scans in this case) to be task farmed as MPI tasks using either the CPU or GPU-accelerated solver. For the B-scan model the host machine was fitted with  $2 \times$  GeForce GTX 1080 Ti GPUs and  $2 \times$  TITAN X GPUs, and the MPI task farm functionality was used to run 4 A-scans at once in parallel, i.e. one on each of the GPUs. The B-scan simulation (91 A-scans) required at total of 1 h 17 min and 56 s to run on the GPUs. This would have required 23 h and 20 min to run on host with the parallelised (OpenMP) CPU solver.

#### 4.2. Anti-personnel landmine model

To further illustrate the significance of our GPU-accelerated solver for GPR modelling, we present an example of a large-scale

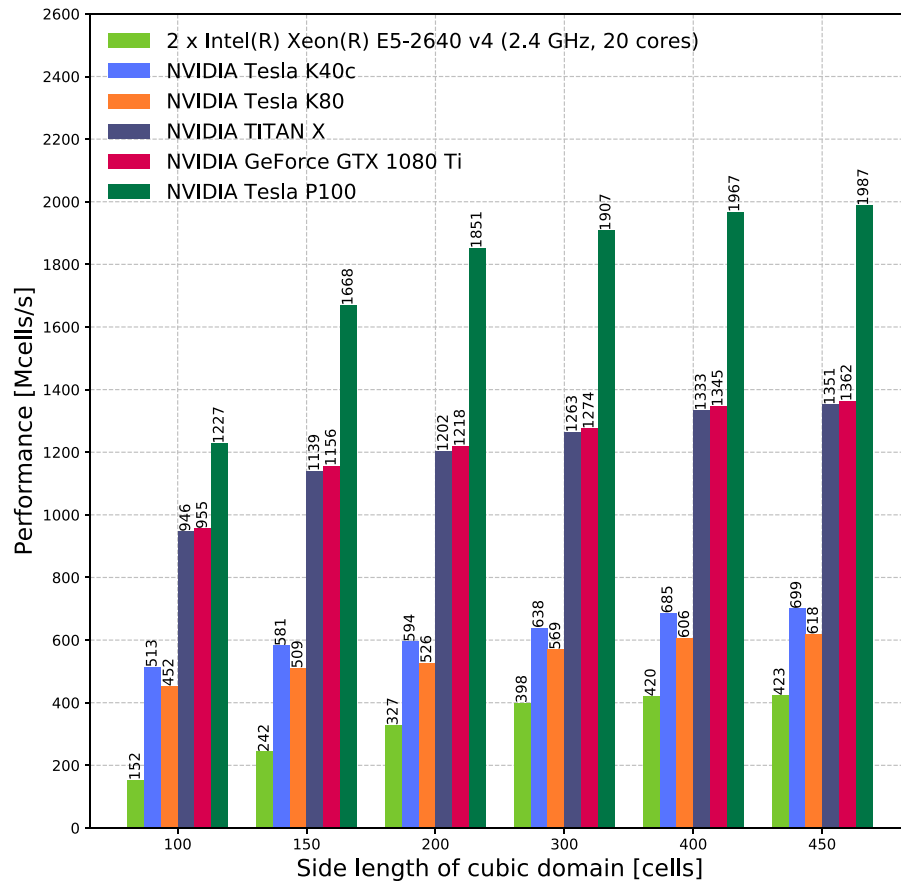


Fig. 5. CPU solver and GPU-accelerated solver performance throughput (FP64).

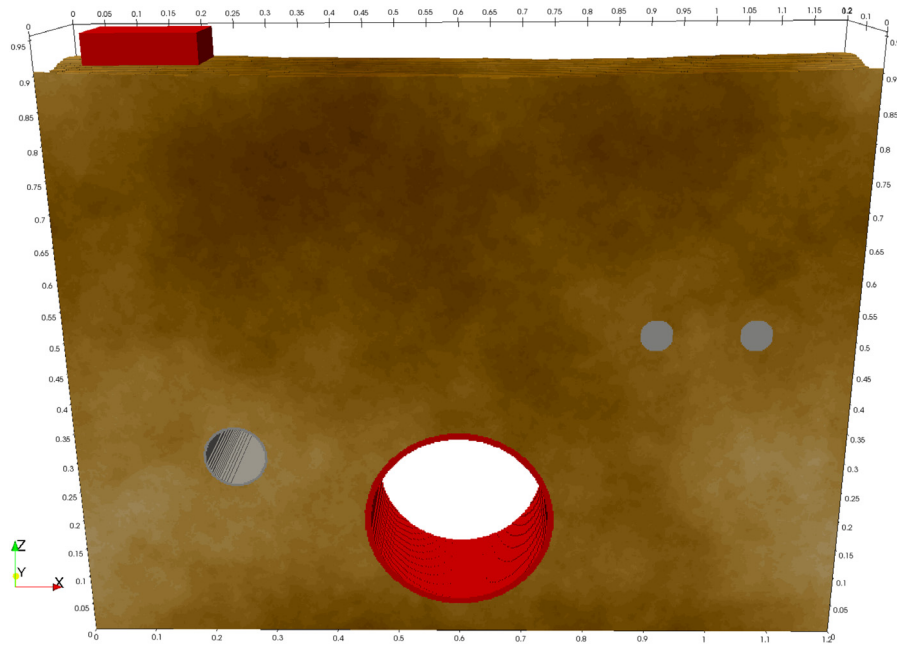


Fig. 6. FDTD mesh of a typical GPR environment for detecting and locating buried pipes and cables.

GPR simulation of buried anti-personnel landmines. This model was conceived for two purposes: firstly, to provide realistic training data for our research into a machine learning framework for the automated detection, location, and identification of landmines using GPR; and secondly, to provide a numerical dataset for GPR

researchers to test their GPR imaging, inversion, and processing algorithms. This latter concept has been well-established in seismic modelling with the Marmousi model [29], however, to our knowledge no such detailed and realistic 3D model exists for GPR. The model is a near-surface example of a fictional but realistic



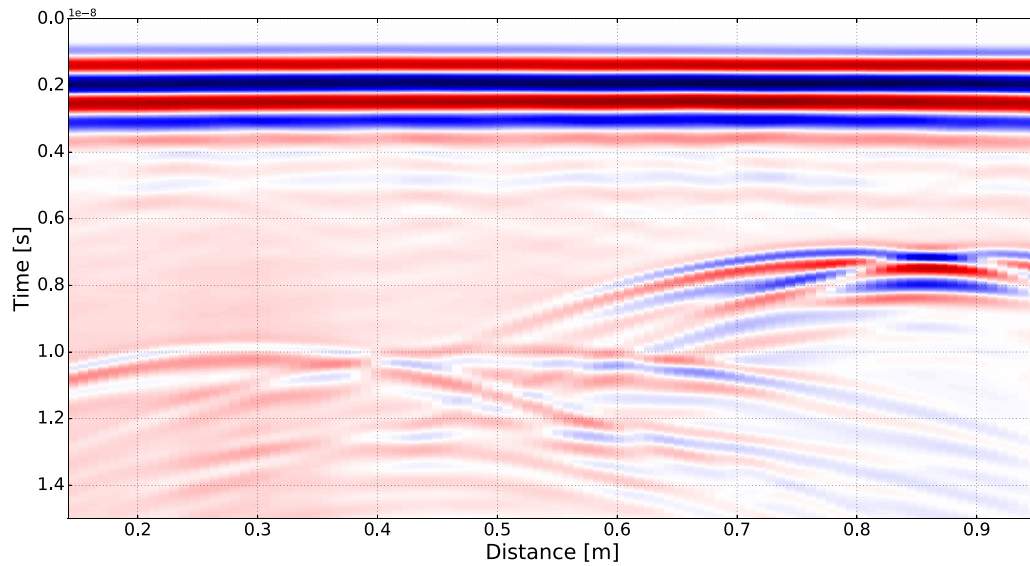


Fig. 7. B-scan data from a typical GPR environment containing buried pipes and cables.

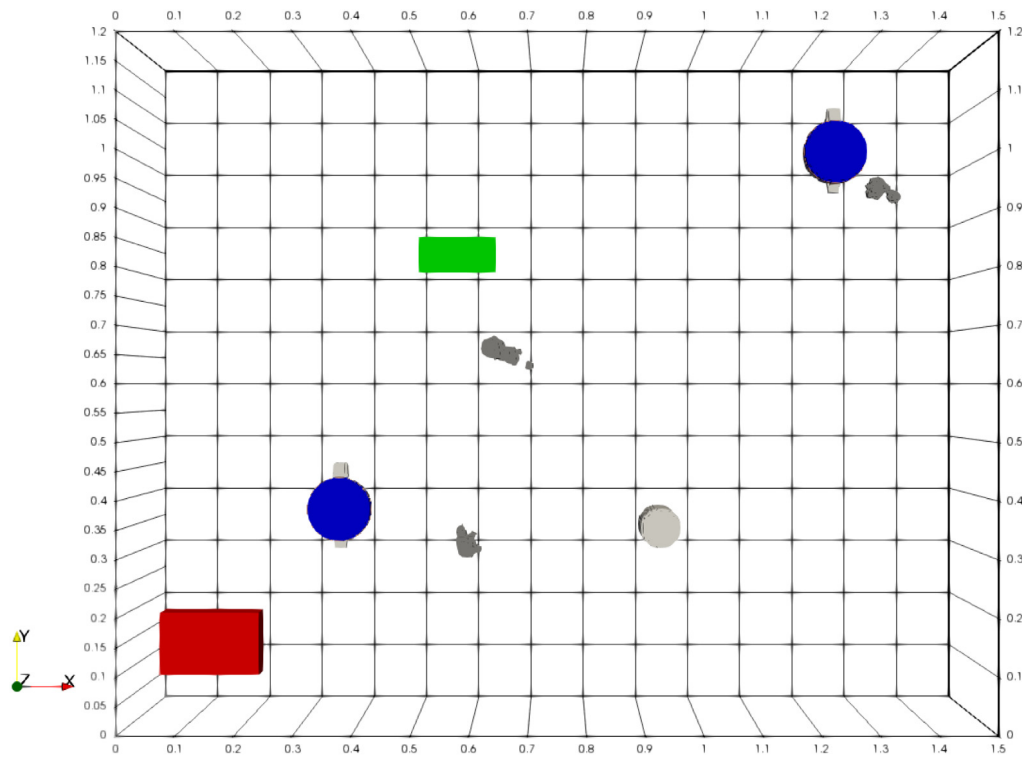
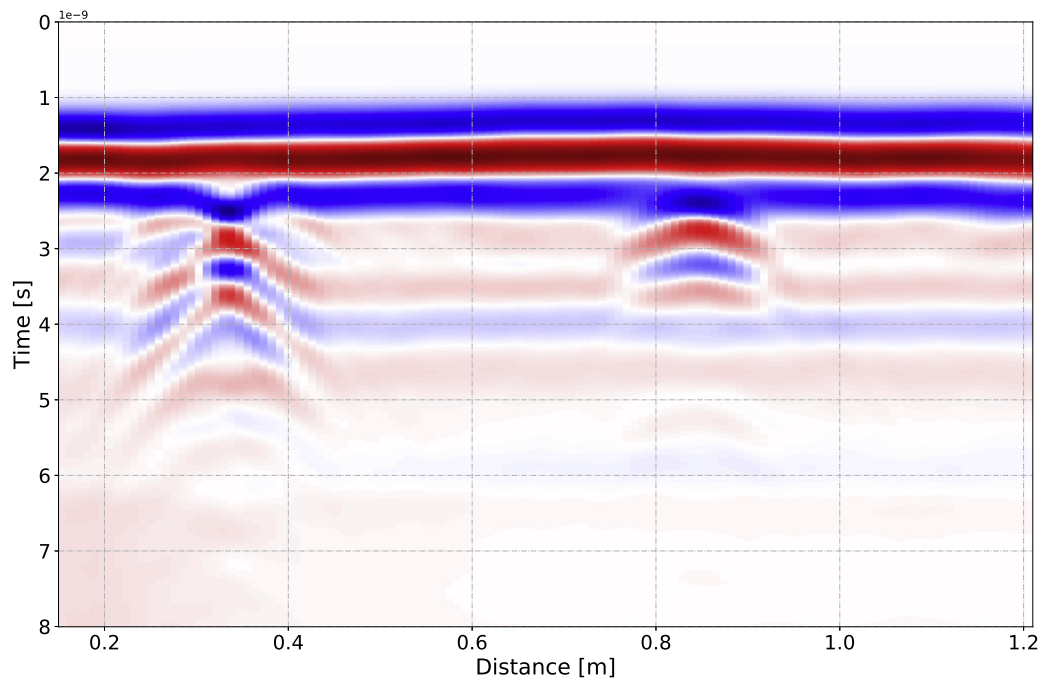


Fig. 8. FDTD mesh of a complex GPR environment for detecting and locating buried anti-personnel landmines. The model contains: buried anti-personnel landmines –  $2 \times$  PMN (blue) and  $1 \times$  PMA-1 (green); a heterogeneous soil with a rough surface (not shown); a GPR antenna model (red); a false metal target (light grey cylinder); and several rocks (dark grey). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

landmine detection scenario – an extremely challenging environment in which GPR is often utilised. The key parameters for the simulation are given in Table 5, and an overview of the geometry of the model is presented in Fig. 8. The simulation contains: anti-personnel landmine models –  $2 \times$  PMN and  $1 \times$  PMA-1; a heterogeneous soil with a rough surface; a GPR antenna model; a false metal target; and several rocks.

The simulation required a total of  $121 \times 37 \times 2 = 8954$  models (A-scans) to image the entire space. An example of one of the B-scans from the simulation is given in Fig. 9. We carried out the simulations on Tesla P100 GPUs on NVIDIA DGX-1 systems that

were part of the Joint Academic Data science Endeavour (JADE) computing facility funded by the Engineering and Physical Sciences Research Council (EPSRC). We were able to use 11 nodes of JADE, where each node contained 8 T P100 GPUs. Each model required 96 s runtime, and therefore the total time to complete the simulation (8954 models) was 2 h and 44 min. This level of performance for such large-scale, realistic GPR simulations would simply not be attainable without the GPU-accelerated solver. It is a significant advancement for areas of GPR research like full-waveform inversion and machine learning, where many thousands of forward models are required.



**Fig. 9.** B-scan data from a GPR environment containing buried anti-personnel landmines, a heterogeneous soil with a rough surface, a GPR antenna model, a false metal target, and rocks.

**Table 5**  
Key parameters for buried landmine model.

Parameter	Value
Domain size (x,y,z)	$1.5 \times 1.2 \times 0.328$ m
Spatial resolution (x,y,z)	$0.002 \times 0.002 \times 0.002$ m
Temporal resolution	$3.852 \times 10^{-12}$ s
Time window	$8 \times 10^{-9}$ s
A-scan sampling interval	0.010 m
A-scans per B-scan	121
B-scan spacing	0.025 m
Number of B-scans (x,y)	$37 \times 37$
Surface roughness (about mean height)	$\pm 0.010$ m

## 5. Conclusion

We have developed a GPU-accelerated FDTD solver using NVIDIA's CUDA framework, and integrated it into open source EM simulation software for modelling GPR. We benchmarked our GPU solver on a range of Kepler- and Pascal-based NVIDIA GPUs, as well as compared performance to the parallelised (OpenMP) CPU solver on a range of desktop and server specification Intel CPUs. Simple models that contained non-dispersive materials and a Hertzian dipole source achieved performance throughputs of up to 1194 Mcells/s and 3405 Mcells/s on Kepler and Pascal architectures, respectively. This is up to 30 times faster than the OpenMP CPU solver can achieve on a commonly-used desktop CPU (Intel Core i7-4790 K). We found the performance of our GPU kernels was largely dependent on the memory bandwidth of the GPU, with the Tesla P100, which had the largest peak theoretical memory bandwidth of the cards we tested (732 GB/s), exhibiting the best performance.

We found the cost-performance benefit of the Pascal-based GPUs that were targeted towards the gaming market, i.e. TITAN X and GeForce GTX 1080 Ti, to be especially notable, potentially allowing many individuals to benefit from this work using commodity workstations. Additionally the equivalent Tesla series P100 GPU (targeted towards data-centre usage) demonstrated significant overall performance advantages due to its use of high bandwidth memory. These benefits can be further enhanced when

combined with our MPI task farm that enables several GPUs to be used in parallel. We expect performance benefits of our GPU solver to rapidly advance GPR research in areas such as full-waveform inversion and machine learning, where typically many thousands of forward simulations require to be executed.

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