

Ecuaciones principales

$$V_e(t) = R\dot{i}_1(t) + L \frac{d[i_1(t) - i_2(t)]}{dt} + R[i_1(t) - i_2(t)]$$

$$L \frac{d[i_1(t) - i_2(t)]}{dt} + R[i_1(t) - i_2(t)] = R\dot{i}_2(t) + R\ddot{i}_2(t) + \frac{1}{C} \int i_2(t) dt$$

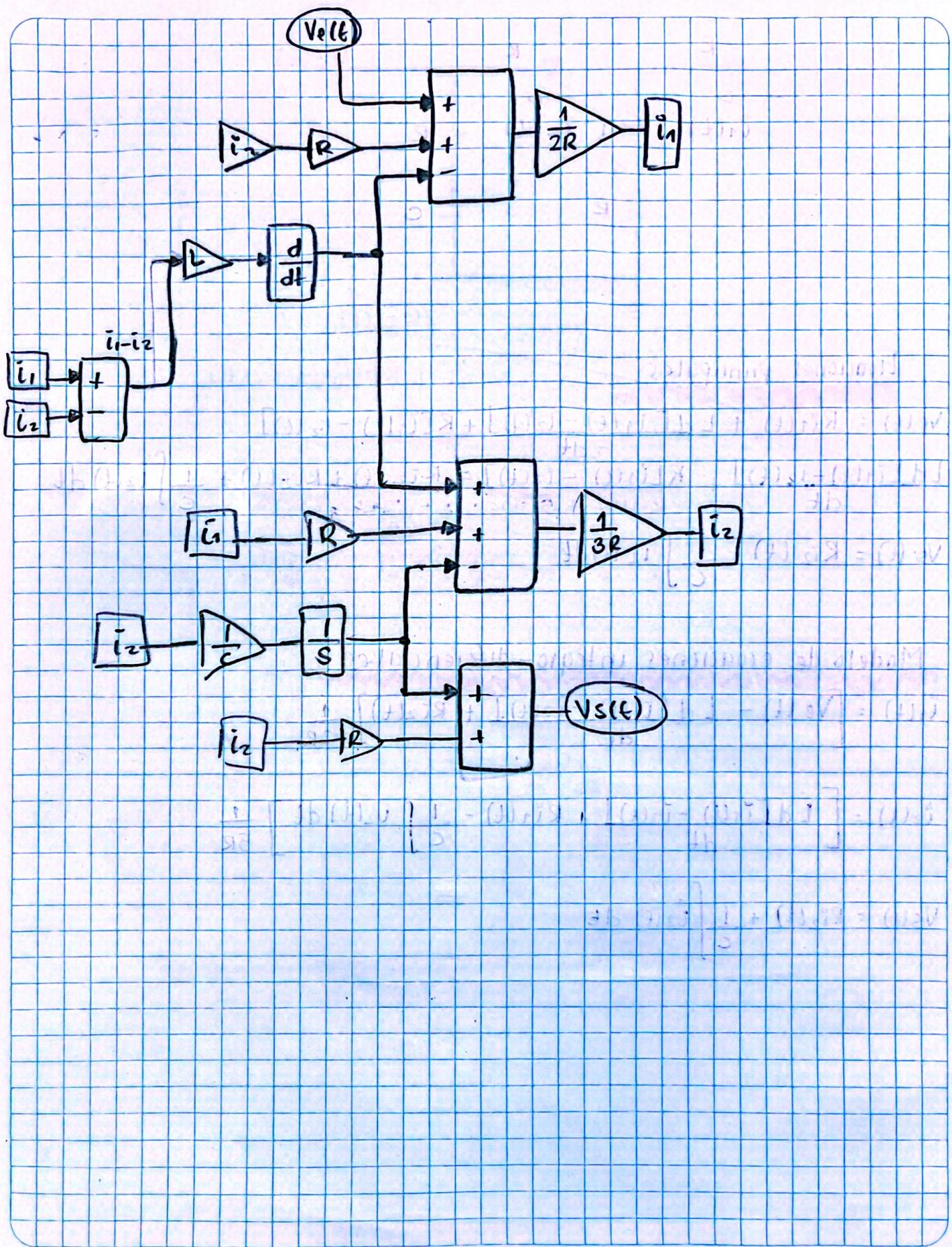
$$V_s(t) = R\dot{i}_2(t) + \frac{1}{C} \int i_2(t) dt \quad \text{esta se queda así.}$$

Modelo de ecuaciones integro-diferenciales.

$$\dot{u}(t) = [V_e(t) - L \frac{d[i_1(t) - i_2(t)]}{dt} + R\dot{i}_2(t)] \frac{1}{2R}$$

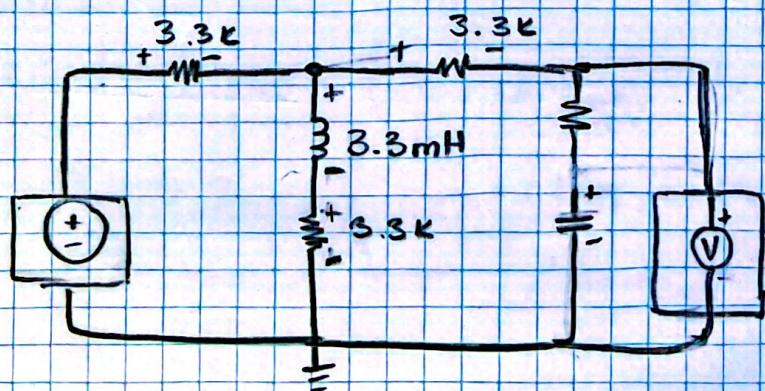
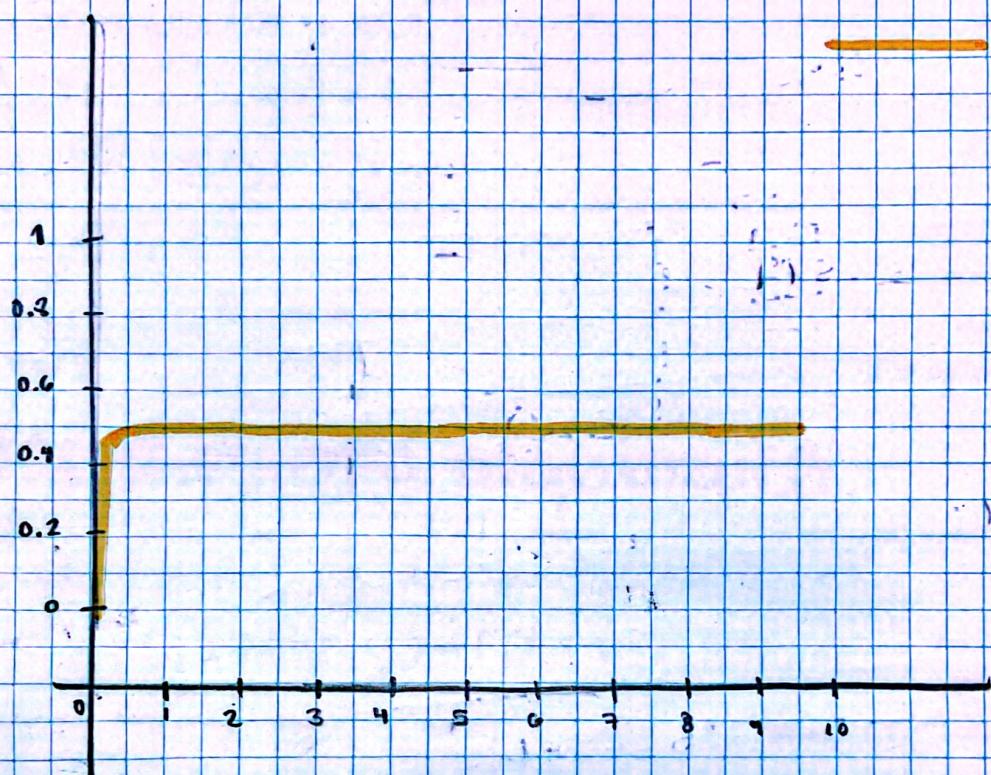
$$i_2(t) = \left[L \frac{d[i_1(t) - i_2(t)]}{dt} + R\dot{i}_1(t) - \frac{1}{C} \int i_2(t) dt \right] \frac{1}{3R}$$

$$V_s(t) = R\dot{i}_2(t) + \frac{1}{C} \int \dot{i}_2(t) dt$$



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PA1(t).



Transformada de Laplace

$$\text{LS}I_1(s) - \text{LS}I_2(s) + RI_1(s) - RI_2(s)$$

$$V_e(s) = RI_1(s) + \text{LS}[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)]$$

$$\text{LS}[I_1(s) - I_2(s)] + R[I_1(s) - I_2(s)] = RI_2(s) + RI_2(s) + \frac{I_2(s)}{CS}$$

$$V_s(s) = RI_2(s) + \frac{I_2(s)}{CS} = \frac{CRS + 1}{CS} I_2(s)$$

$$\frac{V_s(s)}{V_e(s)} = \frac{? I_2(s)}{? I_2(s)}$$

Nota: No debe haber términos negativos!

Procedimiento algebraico.

$$V_e(s) = (R + LS + R)I_1(s) - (LS + R)I_2(s)$$

$$= (LS + 2R)I_1(s) - (LS + R)I_2(s)$$

$$-\cdot-\cdot-\cdot-\cdot-\cdot-\cdot-\cdot-\cdot-\cdot-$$

$$\text{LS}I_1(s) - \text{LS}I_2(s) + RI_1(s) - RI_2(s) = 2RI_2(s) + \frac{I_2(s)}{CS}$$

$$\text{LS}I_1(s) + RI_1(s) = 3RI_2(s) + \text{LS}I_2(s) + \frac{I_2(s)}{CS}$$

$$(LS + R)I_1(s) = (3R + LS + \frac{1}{CS})I_2(s)$$

$$I_1(s) = \frac{3CRS + CLS^2 + 1}{CS(LS + R)} I_2(s) = \frac{CLS^2 + 3CRS + 1}{CS(LS + R)} I_2(s)$$

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$$V_e(s) = \frac{(LS + 2R)(CLS^2 + 3CRS + 1)}{CS(LS + R)} I_2(s) - (LS + R)I_2(s)$$

$$= \left[\frac{(LS + 2R)(CLS^2 + 3CRS + 1) - CS(LS + R)(LS + R)}{CS(LS + R)} \right] I_2(s)$$

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$$R = 3.3 \text{ k} \quad L = 3.3 \text{ mH}$$

$$C = 4.7 \mu\text{F}$$

①

$$\cancel{CL^2S^3} + 3CLR^2S^2 + LS + 2CLR^2S^2 + 6CR^2S + 2R$$

②

$$\cancel{-CL^2S^3} - \cancel{2CLR^2S^2} - CR^2S \rightarrow 5CR^2S$$

$$V_{CS} = \frac{3CLR^2S^2 + (5CR^2 + L)S + 2R}{CS(LS + R)}$$

0.9
setting time

$$V_s(S) = \frac{\cancel{CRS + 1}}{\cancel{CS}} \cancel{I_2(S)}$$

$$\frac{3CLR^2S^2 + (5CR^2 + L)S + 2R}{CS(LS + R)} \cancel{I_2(S)}$$

$$(CRS + 1)(LS + R) = CLR^2S^2 + CR^2S + LS + R$$

$$\boxed{\frac{V_s(S)}{V_{CS}} = \frac{CLR^2S^2 + (CR^2 + L)S + R}{3CLR^2S^2 + (5CR^2 + L)S + 2R}}$$

Estabilidad en lazo abierto.

- Calcular los polos de la función de transferencia

$$\frac{V_s(s)}{V_e(s)} = \frac{(CLRS^2 + (CR^2 + L)S + R)}{3CLRS^2 + (5CR^2 + L)S + 2R}$$

$$\lambda_1 = -1666662.3682979832$$

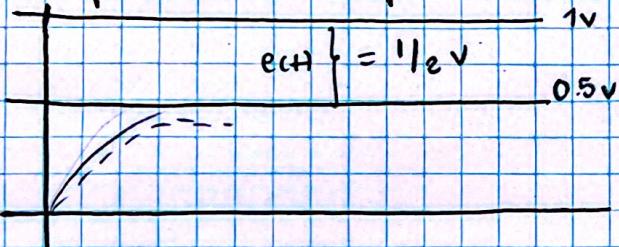
$$\lambda_2 = -25.789879536501907$$

$$\text{den} = [3 * C * L * R, 5 * C * R * R + L, 2 * R]$$

$$L = \text{np.roots(den)}$$

→ `print`: Las raíces son $\{L[0]\}$ y $\{L[1]\}$

El sistema presenta una respuesta estable y sobremortalizada.



$$V_e(t) = 1V$$

$$V_e(s) = \frac{1}{s}$$

Error en estado estacionario

$$e(s) = \lim_{s \rightarrow 0} S V_e(s) \left[1 - \frac{V_s(s)}{V_e(s)} \right]$$

$$= \lim_{s \rightarrow 0} S \times \frac{1}{s} \left[1 - \frac{CLRS^2 + (CR^2 + L)S + R}{3CLRS^2 + (5CR^2 + L)S + 2R} \right]$$

$$= \frac{R}{2R}$$

$$e(t) = \frac{1}{2} V$$