- We sincerely thank the four reviewers for their valuable feedback. We address a common concern from R5 and R6:
- Boundedness of the iterates: Lemma 2 is needed to ensure that H1 is verified. We will change the notations to avoid
- any confusion. Lemma 2 indeed bounds the iterates of Algorithm 2 (OPT-AMSGrad) and should read $||w_t^{(\ell)}|| \le A_{(\ell)}$ where w_t are the weight estimates at iteration t. Then Lemma 2 holds for all iteration t > 0. While our result holds
- indeed for the MLP described in the paper, showing compactness of the sequence of iterates for other type of neural
- networks needs to be done on a case-by-case basis, but we hope that our techniques can inspire further anlaysis.
- R1: We thank the reviewer for valuable comments. Our point-to-point response is as follows:
- Comparison with OPT-FTRL: As stated in our introduction, we believe that the optimistic estimates presents an advantage over vanilla AMSGrad like OPT-FTRL presents over vanilla FTRL. Keeping in mind that the overall goal of our paper is to introduce a new method to solve a stochastic optimization problem where the objective function is a 10 (large) finite-sum, OPT-FTRL is not an option, hence our motivation for developing a counterpart of OPT-FTRL. 11
- R2: We thank the reviewer for valuable comments. A proofreading is being done we clarify that: 12
- Novelty of the contribution: Although combining gradient prediction to AMSGrad update seems natural, as pointed 13 out in the first paragraph of Section 3, we would like to stress on how the embedding of the prediction process 14 (represented Figure 1) led to the two-stage algorithm OPT-AMSGrad (unlike the sequential structure of the original 15 AMSGrad) where, first an auxiliary variable \tilde{w} is updated and then the global model w. Also, as discussed in the 16 paper, optimistic learning is typically used in two-player-games, which is an online learning problem, and to the best 17 of our knowledge, this is the first proposal to apply optimistic acceleration to stochastic optimization problems (e.g. training deep neural networks). Introducing the online optimization framework is a natural way to introduce our method, 19 providing related literature on optimistic methods.
- Comparison with other gradient prediction methods: Comparing the way we predict the gradients is indeed 21 important in our study. We have devoted in Section F of the appendix an illustrative example of how this process can 22 impact the performances of our method. 23
- **R3:** We thank the reviewer for the thorough analysis. Our remarks are listed below:
- Gradient prediction algorithm: We will add more explanations on why the average of the last gradients can be a 25 good approximation of the next one. While this may be counterintuitive, we invite the reviewer to read the citation we 26 make regarding our extrapolation method: "Regularized nonlinear acceleration" by Scieur, d'Aspremont and Bach, 27 NIPS 2016. We chose the latter reference mainly due to its success in training deep networks as observed in some prior works. Of course, there is room for improvement regarding this prediction process for future research projects.
- Numerical Experiments: The learning rates have been tuned over a grid search for all methods and the best performances over 5 repetitions have been reported. The main motivation behind those plots is to show that adding an 31 optimistic update to the AMSGrad actually speed up the convergence in terms of both losses and accuracies. Given the 32 well-known advantages of Adam-type methods such as ADAM or AMSGrad, we did not compare to slower methods. 33
- **R5:** We thank the reviewer for valuable comments and typos. Our response is as follows: 34
- **Discussion on the bounds:** There is actually a typo in Eq. (2), where the last term should be $\frac{\sqrt{T}}{\eta} \sum_{i=1}^{d} \hat{v}_{T}[i]^{1/2}$. See 35 the original AMSGrad paper for reference. We can show that $v_T[i]$ equals to the term in brackets in Corollary 1 by 36 recursively calculating v_t up to T. Thus, the last term in (2) is actually greater than the third term in Corollary 1 because 37 $\hat{v} \geq v$ by definition. 38
- Global convergence analysis: The term Global is employed in the sense that it does not restrict the initialization of the algorithm and our bound is true for any iteration (finite-time). In other words the result is global since it is true for any initial point. Of course this is not related to the stationary point, as the objective function is nonconvex, no guarantees 41 are given regarding the nature of the obtained stationary point. 42
- Numerical experiments: There are several works considering applying Alg. 3 in deep learning, e.g. [Nonlinear 43 Acceleration of Deep Neural Networks, Scieur et al., 2018], with positive results. As noted in their paper, in practice extrapolation on CPU is faster than a forward pass on mini-batch and can be further accelerated on GPU. Moreover, note 45 that at each iteration, we only change one past gradient, so we do not need to compute the whole linear system every 46 time leading to practical efficiency. Secondly, the main focus of our paper is essentially the framework of integrating 47 optimistic learning with AMSGrad. We chose Algorithm 3 mainly because of the empirical success reported in prior 48 works. The choice of gradient prediction method is actually flexible. So, OPT-AMSGrad will definitely benefit from an 49 algorithm with faster running time and good prediction quality.
- **R6:** We thank the reviewer for valuable comments. We clarify the following point on OPT-ADAM: 51
- **OPT-ADAM:** OPT-Adam has been developed in the particular case of an online problem, where the observations are 52 being presented in a streaming fashion. Here, our goal is to develop a method for the finite-sum stochastic optimization 53 problem. To the best of our knowledge, OPT-Adam has not been studied and no guarantees are given to claim that it 54 also performs well under this latter settings. Empirical evaluations actually show that OPT-AMSGrad is better.