- We would like to thank the four reviewers for their valuable feedback. Please find below the corresponding replies.
- **Reviewer 1.** Q1: More explanations on notations: Notations will be explained and simplified in the revised paper.
- 3 Q2: Better presentation of line 41-45: Line 41-45 simply highlights that our setting is different from [Reddi et al.,
- 4 2019], not arguing that their approach is incorrect. We will revise this part to avoid confusion.
- 5 Q3: Assumption A2 is strong: A2 is necessary for the analysis of adaptive gradient methods and is standard in the
- 6 literature. In the decentralized literature, this assumption might be viewed as strong since only the convergence of
- 7 SGD-like algorithms has been dealt with so far. Relaxing A2 is interesting but it is out of the scope of this work.
- 8 Q4: Similar ideas on consensus of step-size: Thanks for providing the relevant references. [2] averages the predefined
- 9 stepsize sequence across iterations to make it more tolerant to staleness in asynchronous updates. [3] does not explicitly
- apply consensus on stepsize but rather allows the stepsize on different nodes to be different (the maximum difference
- depends on the graph structure) for deterministic strongly convex problems. Our learning rate consensus is across
- 12 workers instead of across iterations and we allow the adaptive learning sequence on different nodes to be completely
- different. Our technique and motivation are thus different from these works. A discussion about this will be added.
- 14 Q5: More experiments: Experiments with larger datasets and complex models are under production.
- Reviewer 2. Q1: Connection to counter example in [Reddi et al., 2019]: Both our example and the one in [Reddi et al.,
- 16 2019] use the idea that sample dependent learning rate can lead to non-convergence. Yet, in decentralized setting, the
- sample dependent learning rate is caused by different nodes having different adaptive learning rate sequences, while in
- Reddi et al., 2019], the non-convergence is caused by over-adaptivity of adaptive learning rate of Adam.
- 19 Q2: Highlight the novelty of the algorithm design: The novelty of our design is twofold. First, we aim at bridging the
- 20 realms of decentralized optimization and adaptive gradient methods. The study of adaptive and decentralized methods
- 21 are conducted independently in the literature. To the best of our knowledge, this is the first success application (with
- 22 rigorous convergence guarantee) of adaptive methods in decentralized optimization. Second, our gossip technique is not
- 23 the direct average consensus mechanism used in the extensively studied DGD. We will add more discussion on why the
- 24 direct average consensus mechanism in DGD cannot be used in our case.
- Reviewer 3. Q1: More rigorous proof for Theorem 1: TO COMPLETE
- 26 Q2: More discussion of Theorem 2 and Algorithm 2/3: We will add more interpretation of the theoretical results and algorithms to improve clarity.
- 28 Q3: Tuning  $\epsilon$  for different algorithms: We will include this as a tunable hyperparameter in future experiments.
- 29 **Reviewer 4.** Q1: Is Theorem 1 stepsize dependent?: TO COMPLETE
- 20 Q2: Clarify line 164: [Nazari et al., 2019] claims that DADAM achieves  $O(\sqrt{T})$  regret as an online algorithm, but
- with a non-standard regret for online optimization. We prove that DADAM can fail to converge which is in some sense
- contradicting their convergent result. The reason might be that the convergence measure defined in [Nazari et al., 2019]
- 33 can hide this non-convergence issue.
- 34 Q3: A large N leads to high communication cost: Indeed, there will be a trade-off between communication and
- $^{35}$  computation in practice. Discussion on this will be added. The optimal N depends on the ratio between the speed of
- 36 computation and communication.
- 37 Reviewer 6. Q1:Bounded gradient assumption is strong: This assumption is commonly assumed in the literature
- of adaptive gradient methods since the analyses for these algorithms are way more complicated than that for SGD.
- Relaxing this assumption is an interesting question but it will be out of the scope of this paper.
- 40 Q2: Advantages over SGD in numerical experiments: Our experiments in the main paper aim at showing the advantages
- 41 over DADAM. The advantages over SGD are highlighted comparing Figure 3 and Figure 4 in Appendix D where we
- 42 note that the proposed algorithm is less sensitive to the learning rate, which is one advantage of adaptive methods.
- 43 *Q3*: Theorem 1 violates bounded gradient assumption: TO COMPLETE
- 44 Q4: The work seems incremental given the framework of DADAM and existing consensus algorithms: The main
- 45 contribution of this work is the rigorous convergence analysis of adaptive gradient methods in decentralized setting and
- 46 the proposed convergent algorithm Decentralized AMSGrad. In the literature, the study of decentralized optimization
- 47 and adaptive gradient methods are usually independent. Given the non convergence of DADAM, we believe provides
- 48 the first decentralized adaptive method.