

**Input:**  $\mathbf{Y} = \{Y_1, Y_2, \dots, Y_T\}, \pi, \mathbf{A}, \mathbf{B}$   
**Output:**  $\mathbf{X} = \{X_1, X_2, \dots, X_T\}$

```

begin
   $\mathbf{O} \leftarrow \{O_1, O_2, \dots, O_N\};$ 
   $\mathbf{S} \leftarrow \{S_1, S_2, \dots, S_K\};$ 
  for each state  $i \in \{1, 2, \dots, K\}$  do
     $T_1[i, 1] \leftarrow \pi \cdot \mathbf{B}_{iy_1};$ 
     $T_2[i, 1] \leftarrow 0$ 
  end
  for each observation  $i \in \{2, 3, \dots, T\}$  do
    for each state  $j \in \{1, 2, \dots, K\}$  do
       $T_1[j, i] \leftarrow \mathbf{B}_{jy_i} \cdot \max \{T_1[k, i-1] \cdot A_{kj}\};$ 
       $T_2[j, i] \leftarrow \operatorname{argmax} \{T_1[k, i-1] \cdot A_{kj}\}$ 
    end
  end
   $Z_T \leftarrow \operatorname{argmax} \{T_1[k, T]\};$ 
   $X_T \leftarrow S_{Z_T};$ 
  for  $i \leftarrow T, T-1, \dots, 2$  do
     $Z_{i-1} \leftarrow T_2[Z_i, i];$ 
     $X_{i-1} \leftarrow S_{Z_{i-1}}$ 
  end
end

```

**Algorithm 1:** Viterbi Algorithm