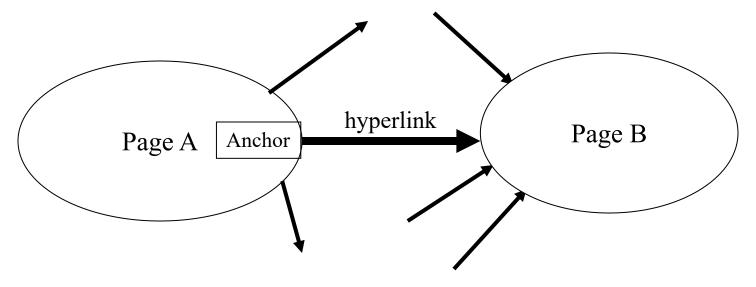
# Introduction to Information Retrieval

Lecture 18: Link analysis

## Today's lecture

- Anchor text
- Link analysis for ranking
  - Pagerank and variants

#### The Web as a Directed Graph



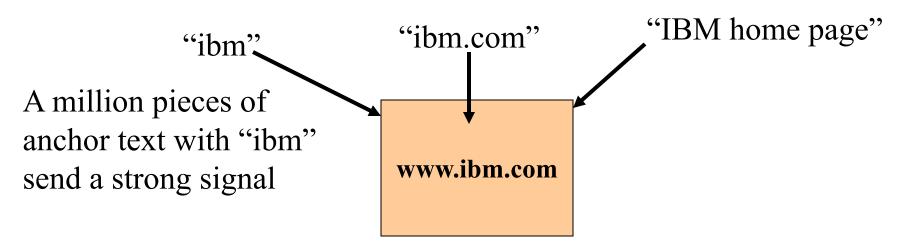
**Assumption 1:** A hyperlink between pages denotes author perceived relevance (quality signal)

**Assumption 2:** The text in the anchor of the hyperlink describes the target page (textual context)

#### **Anchor Text**

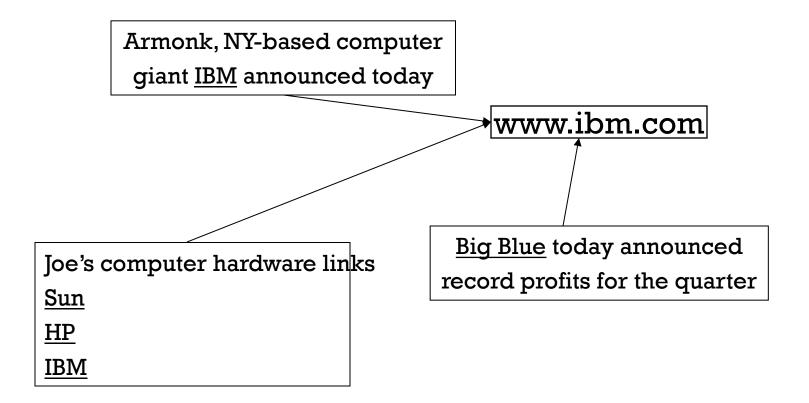
#### WWW Worm - McBryan [Mcbr94]

- For *ibm* how to distinguish between:
  - IBM's home page (mostly graphical)
  - IBM's copyright page (high term freq. for 'ibm')
  - Rival's spam page (arbitrarily high term freq.)



## Indexing anchor text

 When indexing a document D, include anchor text from links pointing to D.



Sec. 21.1.1

## Indexing anchor text

- Can sometimes have unexpected side effects e.g., evil empire.
- Can score anchor text with weight depending on the authority of the anchor page's website
  - E.g., if we were to assume that content from cnn.com or yahoo.com is authoritative, then trust the anchor text from them

#### **Anchor Text**

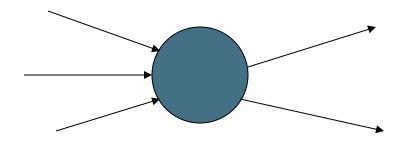
- Other applications
  - Weighting/filtering links in the graph
  - Generating page descriptions from anchor text

#### Citation Analysis

- Citation frequency
- Co-citation coupling frequency
  - Cocitations with a given author measures "impact"
  - Cocitation analysis
- Bibliographic coupling frequency
  - Articles that co-cite the same articles are related
- Citation indexing
  - Who is this author cited by? (Garfield 1972)
- Pagerank preview: Pinsker and Narin '60s

## Query-independent ordering

- First generation: using link counts as simple measures of popularity.
- Two basic suggestions:
  - Undirected popularity:
    - Each page gets a score = the number of in-links plus the number of out-links (3+2=5).
  - Directed popularity:
    - Score of a page = number of its in-links (3).



#### Query processing

- First retrieve all pages meeting the text query (say venture capital).
- Order these by their link popularity (either variant on the previous slide).
- More nuanced use link counts as a measure of static goodness (Lecture 7), combined with text match score

## Spamming simple popularity

- Exercise: How do you spam each of the following heuristics so your page gets a high score?
- Each page gets a static score = the number of inlinks plus the number of out-links.
- 2. Static score of a page = number of its in-links.

#### Ideas of Pagerank

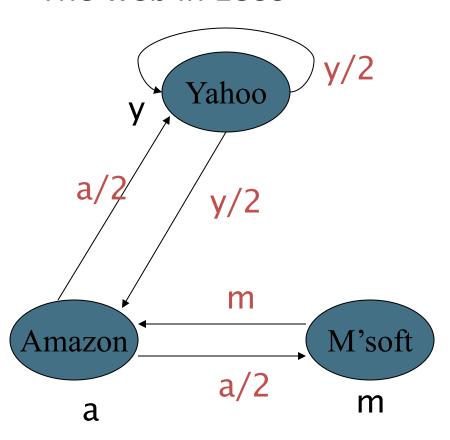
- Inlinks as votes
  - www.stanford.edu has 23,400 inlinks
  - www.joe-schmoe.com has 1 inlink
- Web pages are not equally "important"
  - www.joe-schmoe.com → p1
  - VS. <u>www.stanford.edu</u> → p2
- Are all inlinks equal?
  - Recursive question!

#### Pagerank scoring

- Imagine a browser doing a random walk on web pages:
  - Start at a random page
  - At each step, go out of the current page along one of the links on that page, equiprobably
- "In the steady state" each page has a long-term visit rate - use this as the page's score.

## Example – the Simple "Flow" Model

#### The web in 1839



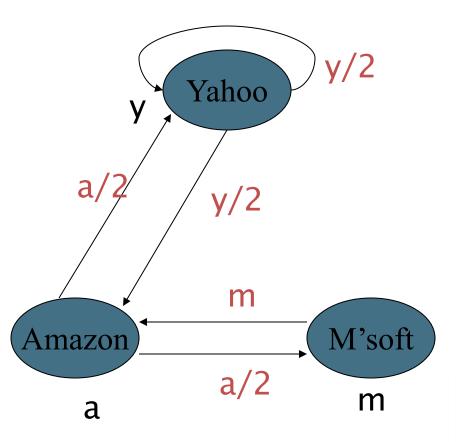
$$y = y/2 + a/2$$
  
 $a = y/2 + m$   
 $m = a/2$ 

#### Solving the flow equations

- 3 equations, 3 unknowns, no constants
  - No unique solution
  - All solutions equivalent modulo scale factor
- Additional constraint forces uniqueness
  - y+a+m = 1
  - y = 2/5, a = 2/5, m = 1/5
- Gaussian elimination method works for small examples, but we need a better method for large graphs

#### Example – the Simple "Flow" Model

#### The web in 1839



$$y_{new} = y_{old}/2 + a_{old}/2$$
  
 $a_{new} = y_{old}/2 + m_{old}$   
 $m_{new} = a_{old}/2$   
 $y = 1/3$  1/3 5/12 ... 2/5  
 $a = 1/3$  1/2 1/3 ... 2/5

Matrix-based characterization of the computation is simpler and more useful for the general case.

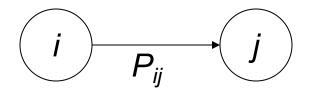
 $m = 1/3 \quad 1/6 \quad 1/4 \quad \dots 1/5$ 

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#### Markov chains

- A Markov chain consists of n states, plus an  $n \times n$  transition probability matrix **P**.
- At each step, we are in exactly one of the states.
- For  $1 \le i,j \le n$ , the matrix entry  $P_{ij}$  tells us the probability of j being the next state, given we are currently in state i.



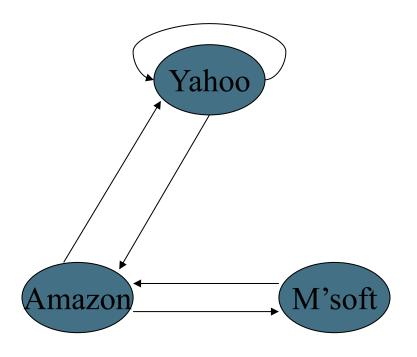


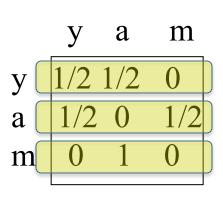
#### Markov chains

• Clearly, for all i,  $\sum_{j=1}^{n} P_{ij} = 1.$ 

$$\sum_{i=1}^{n} P_{ij} = 1.$$

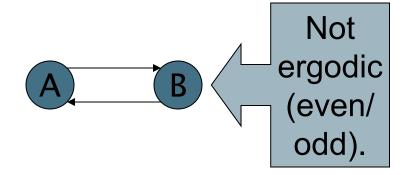
Markov chains are abstractions of random walks.





#### **Ergodic Markov chains**

- A Markov chain is <u>ergodic</u> if
  - you have a path from any state to any other
  - For any start state, after a finite transient time T<sub>0</sub>, the probability of being in any state at a fixed time T>T<sub>0</sub> is nonzero.



#### **Ergodic Markov chains**

- For any ergodic Markov chain, there is a unique long-term visit rate for each state.
  - Steady-state probability distribution.
- Over a long time-period, we visit each state in proportion to this rate.
- It doesn't matter where we start.

#### Probability vectors

- A probability (row) vector  $\mathbf{x} = (x_1, ... x_n)$  tells us where the walk is at any point.
- E.g., (000...1...000) means we're in state i.
   1 i n

More generally, the vector  $\mathbf{x} = (x_1, \dots x_n)$  means the walk is in state i with probability  $x_i$ .

$$\sum_{i=1}^{n} x_i = 1$$

#### Change in probability vector

- If the probability vector is  $\mathbf{x} = (x_1, ... x_n)$  at this step, what is it at the next step?
- Recall that row *i* of the transition prob.
   Matrix P tells us where we go next from state *i*.
- So from x, our next state is distributed as xP.

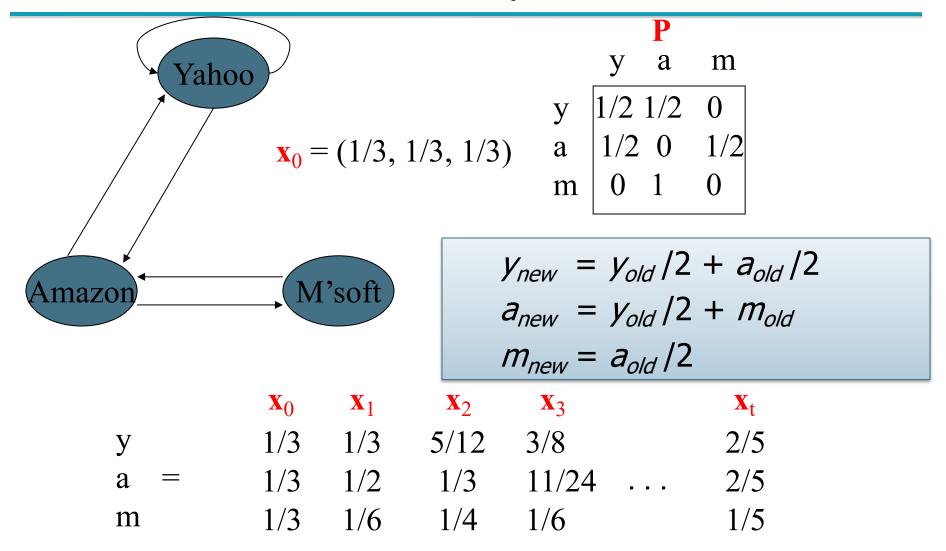
## How do we compute this vector?

- Let  $\mathbf{a} = (a_1, \dots a_n)$  denote the row vector of steadystate probabilities.
- If our current position is described by a, then the next step is distributed as aP.
- But a is the steady state, so a=aP.
- Solving this matrix equation gives us a.
  - So a is the (left) eigenvector for P.
  - (Corresponds to the "principal" eigenvector of P with the largest eigenvalue.)
  - Transition probability matrices always have largest eigenvalue 1.

#### One way of computing a

- Recall, regardless of where we start, we eventually reach the steady state a.
- Start with any distribution (say  $\mathbf{x} = (1/n, 1/n, ..., 1/n)$ ).
- After one step, we're at xP;
- after two steps at  $xP^2$ , then  $xP^3$  and so on.
- "Eventually" means for "large" k,  $\mathbf{xP}^k = \mathbf{a}$ .
- Algorithm: multiply x by increasing powers of P until the product looks stable.

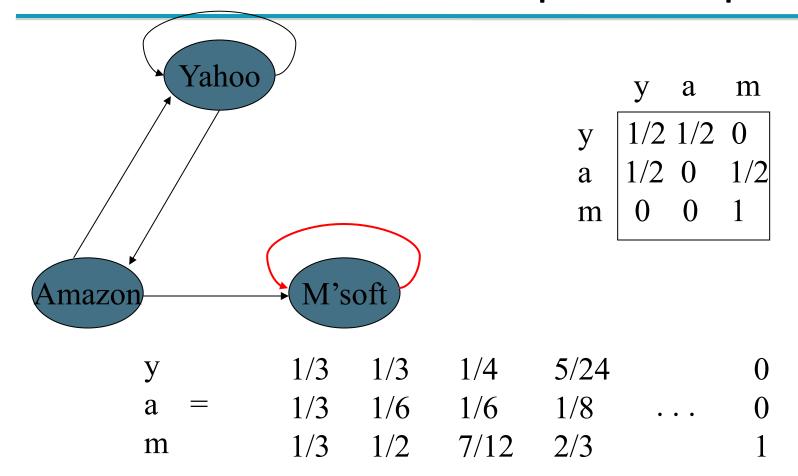
#### Power Iteration Example



#### Spider traps

- A group of pages is a spider trap if there are no links from within the group to outside the group
  - Random surfer gets trapped
- Spider traps violate the conditions needed for the random walk theorem

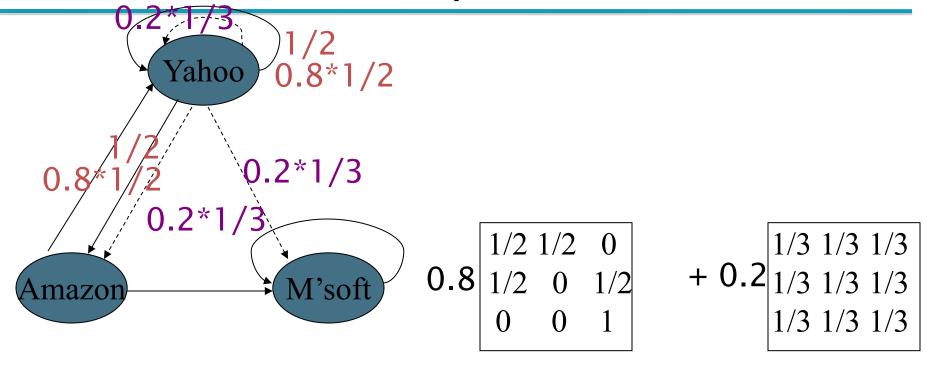
## Microsoft becomes a spider trap



#### Random teleports

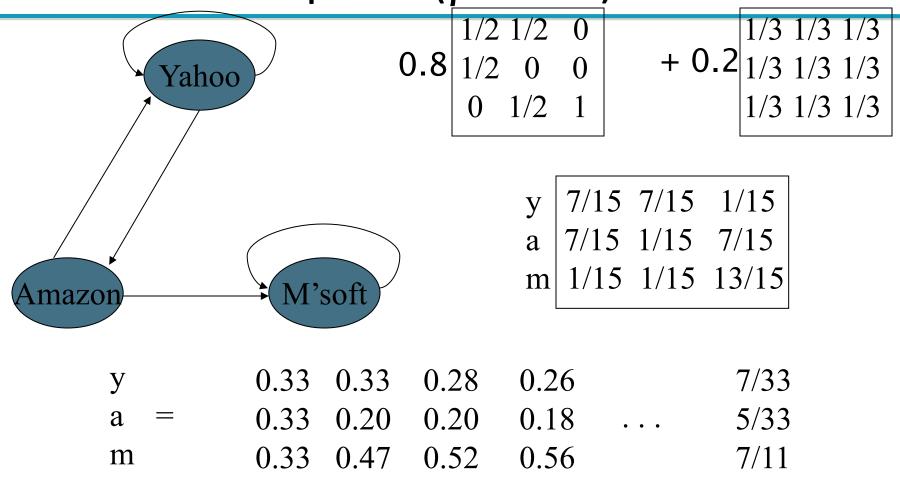
- The Google solution for spider traps
- At each time step, the random surfer has two options:
  - With probability  $\beta$ , follow a link at random
  - With probability 1- $\beta$ , jump to some page uniformly at random
  - Common values for  $\beta$  are in the range 0.8 to 0.9
- Surfer will teleport out of spider trap within a few time steps

## Random teleports ( $\beta = 0.8$ )



y 7/15 7/15 1/15 a 7/15 1/15 7/15 m 1/15 1/15 13/15

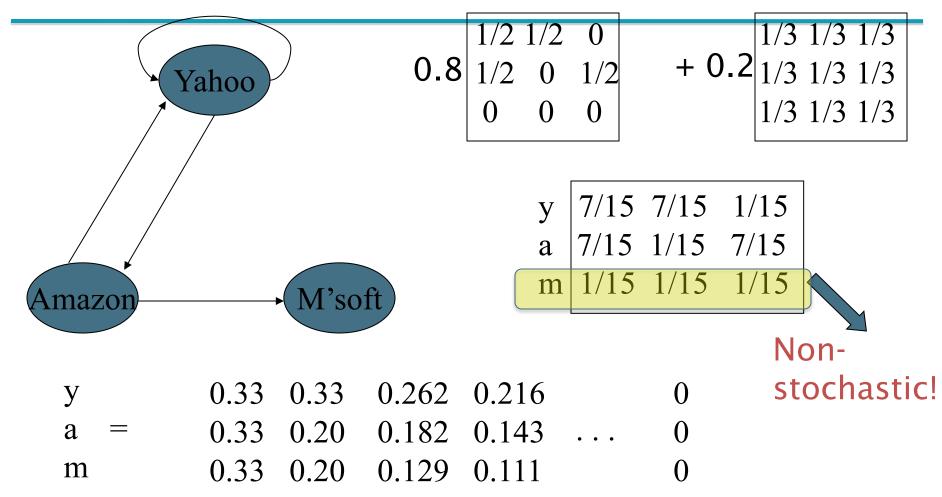
## Random teleports ( $\beta = 0.8$ )



#### Dead ends

- Pages with no outlinks are "dead ends" for the random surfer
  - Nowhere to go on next step
- Especially common for Web Search Engines
  - URLs that have not yet been crawled

#### Microsoft becomes a dead end



#### Dealing with dead-ends

- Teleport
  - Follow random teleport links with probability 1.0 from dead-ends
  - Adjust matrix accordingly
    - How?
- (Suggested by Google) prune and propagate
  - Preprocess the graph to eliminate dead-ends
  - Might require multiple passes
  - Compute page rank on reduced graph
  - Approximate values for deadends by propagating values from reduced graph

Q: Why approximate values and why errors are insignificant?

## Pagerank summary

- Preprocessing:
  - Given graph of links, build matrix P.
  - From it compute a.
    - lacksquare lacksquare is the principle eigen vector of a matrix  $ilde{\mathbf{P}}$

$$\tilde{\mathbf{P}} = (1 - \beta)\mathbf{P} + \beta\mathbf{T}, \qquad \mathbf{T}_{i,j} = \frac{1}{n}$$

- The entry  $a_i$  is a number between 0 and 1: the pagerank of page i.
- Query processing:
  - Retrieve pages meeting query.
  - Rank them by their pagerank.
  - Order is query-independent.

# The reality

- Pagerank is used in google, but is hardly the full story of ranking
  - Many sophisticated features are used
  - Some address specific query classes
  - Machine learned ranking (Lecture 15) heavily used
- Pagerank still very useful for things like crawl policy

#### Pagerank: Issues and Variants

- How realistic is the random surfer model?
  - (Does it matter?)
  - What if we modeled the back button?
  - Surfer behavior sharply skewed towards short paths
  - Search engines, bookmarks & directories make jumps nonrandom.
- Biased Surfer Models
  - Weight edge traversal probabilities based on match with topic/query (non-uniform edge selection)
  - Bias jumps to pages on topic (e.g., based on personal bookmarks & categories of interest)

#### Topic Specific Pagerank

- Goal pagerank values that depend on query topic
- Conceptually, we use a random surfer who teleports, with say 10% probability, using the following rule:
  - Selects a topic (say, one of the 16 top level ODP categories) based on a query & user -specific distribution over the categories
  - Teleport to a page uniformly at random within the chosen topic
- Sounds hard to implement: can't compute PageRank at query time!

#### Topic Specific Pagerank

- Offline:Compute pagerank for individual topics
  - Query independent as before
  - Each page has multiple pagerank scores one for each ODP category, with teleportation only to that category
- Online: Query context classified into (distribution of weights over) topics
  - Generate a dynamic pagerank score for each page weighted sum of topicspecific pageranks

#### Influencing PageRank ("Personalization")

- Input:
  - Web graph W
  - Influence vector v over topics

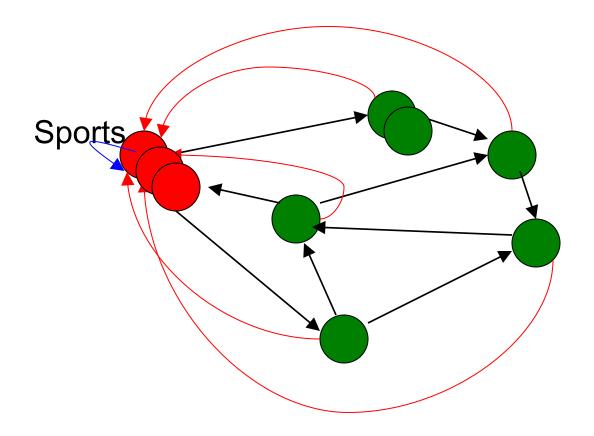
 $\mathbf{v}: (page \rightarrow degree of influence)$ 

Output:

- Rank vector  $\mathbf{r}$ : (page  $\rightarrow$  page importance wrt  $\mathbf{v}$ )
- $\mathbf{r} = PR(W, \mathbf{v})$

Vector has one component for each topic

## Non-uniform Teleportation



Teleport with 10% probability to a Sports page

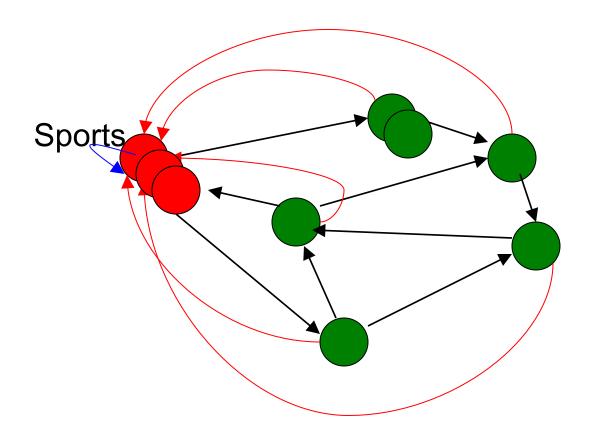
#### Interpretation of Composite Score

Given a set of personalization vectors {v<sub>i</sub>}

$$\sum_{j} [\mathbf{w}_{j} \cdot PR(W, \mathbf{v}_{j})] = PR(W, \sum_{j} [\mathbf{w}_{j} \cdot \mathbf{v}_{j}])$$

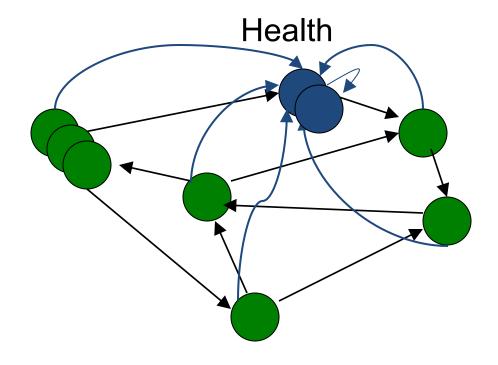
Given a user's preferences over topics, express as a combination of the "basis" vectors  $\mathbf{v}_i$ 

#### Interpretation



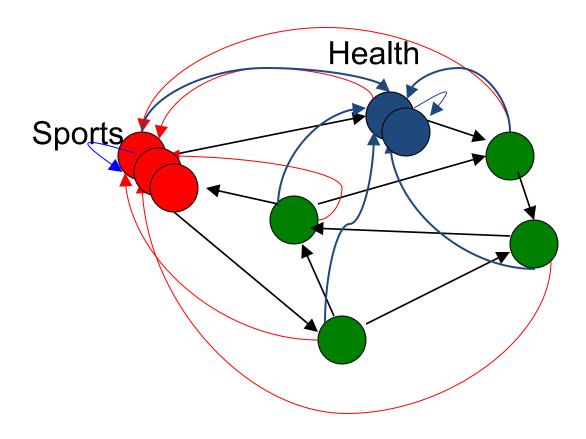
10% Sports teleportation

## Interpretation



10% Health teleportation

## Interpretation



 $pr = (0.9 PR_{sports} + 0.1 PR_{health})$  gives you: 9% sports teleportation, 1% health teleportation

#### Resources

- IIR Chap 21
- http://www2004.org/proceedings/docs/1p309.pdf
- http://www2004.org/proceedings/docs/1p595.pdf
- http://www2003.org/cdrom/papers/refereed/p270/ kamvar-270-xhtml/index.html
- http://www2003.org/cdrom/papers/refereed/p641/ xhtml/p641-mccurley.html