

Gravitational Waves

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What are Gravitational Waves?

Einstein's Theory of Relativity

Space is not flat!

Warped by GRAVITY

Larger Objects



Bigger effect on Space Time

As two large celestial objects orbit and
accelerate

Ripples that distort Space
Time are created

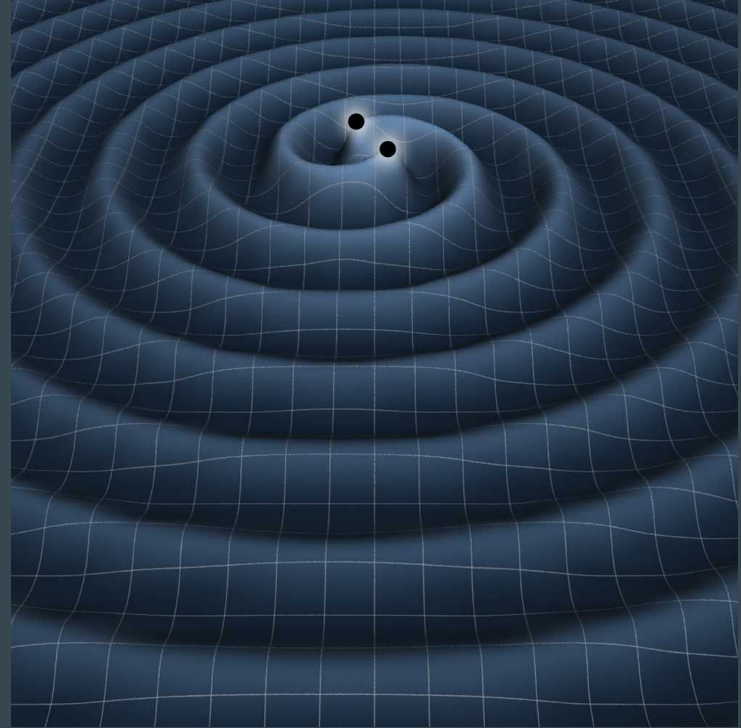
These ripples are known as
Gravitational Waves

What Produces Gravitational Waves ?

Gravitational Waves originate from the merging events of two celestial objects

Black Holes and White Dwarfs (neutron stars) are common objects which emit gravitational waves

As the two orbiting objects get closer the frequencies of the waves increase and eventually hit a maximum before rippling out into space



How Can we Find Gravitational Waves ?

- LIGO is a laser detector built to detect the low frequencies of gravitational waves emitted by merger events
- The lasers are each 4 km long
- There are two LIGO detectors, one in Hanford, Washington and the other in Livingston Louisiana
- The location of the detectors helps researchers gather accurate data and eliminate inaccurate frequencies

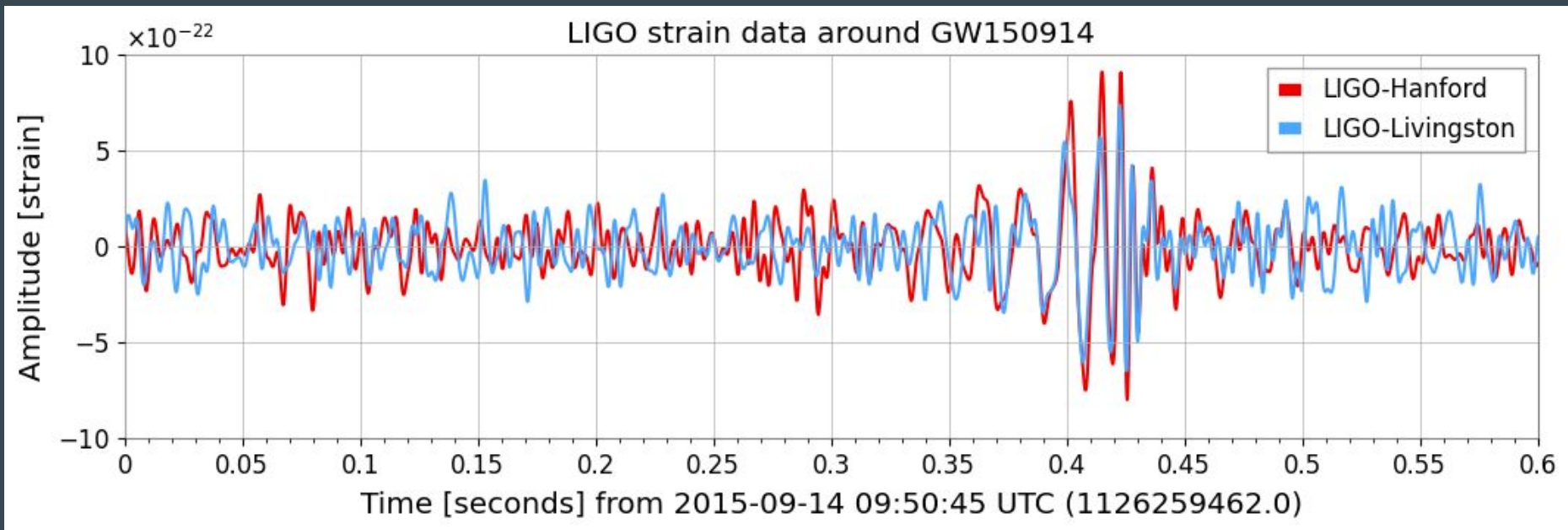


GW150914

Using data from the LIGO data base we plotted the frequencies of the gravitational wave event due to a merge of two black holes

Steps Taken:

- Imported the data with the Time Series function
- Filtered the powerline frequency from the data
- Plotted the Hanford data with the Livingston Data
- Visually transformed the data to analyze the signal
- Converted the data into an audio file



Estimation of black holes masses

Orbital Period: $\Delta t = 0.01$

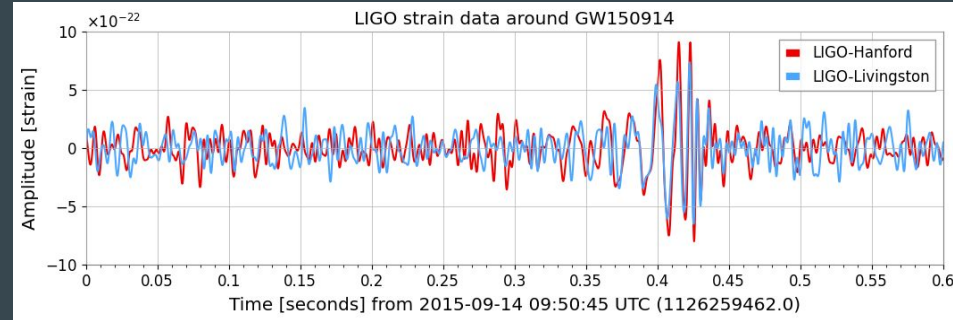
Orbital velocity: $v = \sqrt{GM/a}$,

Schwarzschild radius: $R_{\text{sch}} = 2GM/c^2$

$$\delta t = 2\pi a/v = 2\pi \frac{4GM}{c^2} / (c/2) = 16\pi GM/c^3.$$

$M_{\text{black holes}} = \Delta t \cdot c^3 / 16\pi G$

40.3906 Solar mass

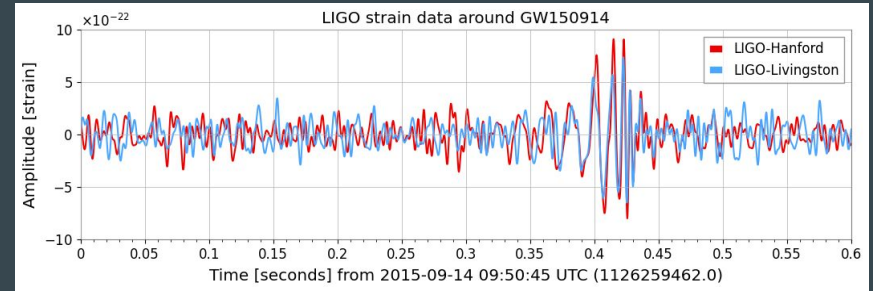


Estimation of black holes distance

Schwarzschild radius: $R_{sch} = 2G M_{blackholes} / c^2$

$M_{black holes} = 40.3906$ Solarmass

$R_{sch} \approx 59.64 \text{ km}$



Gravitational wave strain Amplitude: $h \approx 10^{-21}$

$D = R_{sch} / h \approx 1932.86 \text{ mpc}$ (6.3 billion light-years)

Estimation of Released Energy

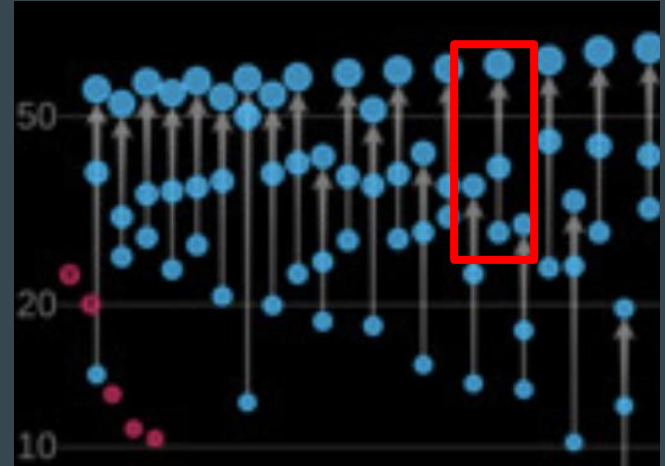
Einstein's mass-energy equivalence: $E = \Delta M \cdot c^2$

Let $\Delta M = 0.1 \cdot M_{\text{blackholes}}$

$$E = 4.039 \text{ solar mass} \cdot c^2 = 7.23 \cdot 10^{47} \text{ Joules}$$

Results

- The estimated mass of the two black holes came to be 40.39 solar masses
- The estimated distance of the merger events was 1932.86 mpc
- The estimated energy released is $7.23 \cdot 10^{47}$ Joules



LIGO-Virgo / Aaron Geller / Northwestern University.