

BIOS512_FinalProject_Williams (1) (4) (1) (1)

November 27, 2025

BIOS512 FINAL PROJECT BELLA WILLIAMS

```
[22]: library(tidyverse)
```

```
[23]: install.packages('fivethirtyeight')
install.packages('fivethirtyeightdata', repos = 'https://fivethirtyeightdata.
      ↪github.io/drat/', type = 'source')
```

Installing package into ‘/srv/rlibs’
(as ‘lib’ is unspecified)

Installing package into ‘/srv/rlibs’
(as ‘lib’ is unspecified)

```
[24]: library(fivethirtyeight)
data("airline_safety")
```

Part I: Preparing the Data

```
[25]: head(airline_safety)
```

A tibble: 6 × 9

airline	incl_reg_subsidiaries	avail_seat_km_per_week	incidents_85_99
<chr>	<lgl>	<dbl>	<int>
Aer Lingus	FALSE	320906734	2
Aeroflot	TRUE	1197672318	76
Aerolineas Argentinas	FALSE	385803648	6
Aeromexico	TRUE	596871813	3
Air Canada	FALSE	1865253802	2
Air France	FALSE	3004002661	14

```
[26]: str(airline_safety)

summary(airline_safety)

mean(airline_safety$fatalities_85_99)
mean(airline_safety$fatalities_00_14)
```

```
tibble [56 × 9] (S3: tbl_df/tbl/data.frame)
 $ airline           : chr [1:56] "Aer Lingus" "Aeroflot" "Aerolineas
Argentinass" "Aeromexico" ...
 $ incl_reg_subsidiaries : logi [1:56] FALSE TRUE FALSE TRUE FALSE FALSE ...
 $ avail_seat_km_per_week: num [1:56] 3.21e+08 1.20e+09 3.86e+08 5.97e+08
1.87e+09 ...
 $ incidents_85_99      : int [1:56] 2 76 6 3 2 14 2 3 5 7 ...
 $ fatal_accidents_85_99 : int [1:56] 0 14 0 1 0 4 1 0 0 2 ...
 $ fatalities_85_99      : int [1:56] 0 128 0 64 0 79 329 0 0 50 ...
 $ incidents_00_14       : int [1:56] 0 6 1 5 2 6 4 5 5 4 ...
 $ fatal_accidents_00_14 : int [1:56] 0 1 0 0 0 2 1 1 1 0 ...
 $ fatalities_00_14      : int [1:56] 0 88 0 0 0 337 158 7 88 0 ...
```

```
      airline      incl_reg_subsidiaries avail_seat_km_per_week
Length:56      Mode :logical      Min.      :2.594e+08
Class :character FALSE:40      1st Qu.:4.740e+08
Mode  :character TRUE :16      Median :8.029e+08
      Mean      :1.385e+09
      3rd Qu.:1.847e+09
      Max.      :7.139e+09
```

```
incidents_85_99 fatal_accidents_85_99 fatalities_85_99 incidents_00_14
Min.      : 0.000   Min.      : 0.000   Min.      : 0.0   Min.      : 0.000
1st Qu.: 2.000   1st Qu.: 0.000   1st Qu.: 0.0   1st Qu.: 1.000
Median : 4.000   Median : 1.000   Median : 48.5   Median : 3.000
Mean    : 7.179   Mean    : 2.179   Mean    :112.4   Mean    : 4.125
3rd Qu.: 8.000   3rd Qu.: 3.000   3rd Qu.:184.2   3rd Qu.: 5.250
Max.    :76.000   Max.    :14.000   Max.    :535.0   Max.    :24.000
```

```
fatal_accidents_00_14 fatalities_00_14
Min.      :0.0000   Min.      : 0.00
1st Qu.:0.0000   1st Qu.: 0.00
Median :0.0000   Median : 0.00
Mean    :0.6607   Mean    : 55.52
3rd Qu.:1.0000   3rd Qu.: 83.25
Max.    :3.0000   Max.    :537.00
```

112.410714285714

55.5178571428571

- Checking Missingness

```
[13]: sum(is.na(airline_safety))
colSums(is.na(airline_safety))
```

0

```
airline      0 incl\_reg\_subsidiaries      0 avail\_seat\_km\_per\_week      0
incidents\_85\_99      0 fatal\_accidents\_85\_99      0 fatalities\_85\_99      0
incidents\_00\_14      0 fatal\_accidents\_00\_14      0 fatalities\_00\_14      0
```

- Checking Duplicates

```
[14]: nrow(airline_safety)
nrow(distinct(airline_safety))

airline_safety %>%
  group_by(airline) %>%
  tally() %>%
  filter(n > 1)
```

56

56

A tibble: 0 × 2

airline	n
<chr>	<int>

```
[15]: airline_safety %>%
  group_by(incl_reg_subsidiaries) %>%
  tally() %>%
  arrange(desc(n))
```

A tibble: 2 × 2

incl_reg_subsidiaries	n
<lgl>	<int>
FALSE	40
TRUE	16

Part II: Data Description (Codebook)

The `airline_safety` dataset contains safety records for 56 airlines from 1985–2014. The data were originally compiled by FiveThirtyEight and include operational exposure (airline size) and incident/fatality counts for two time periods. No missing values are present in this dataset.

Variable	Type	Description
airline	character	Airline name
incl_reg_subsidiaries	logical	TRUE if safety numbers include regional subsidiaries, otherwise FALSE
avail_seat_km_per_week	numeric	Airline size, measured as available seat-kilometers flown per week
incidents_85_99	integer	Total incidents from 1985–1999
fatal_accidents_85_99	integer	Fatal accidents from 1985–1999
fatalities_85_99	integer	Total fatalities from 1985–1999
incidents_00_14	integer	Total incidents from 2000–2014

Variable	Type	Description
<code>fatal_accidents_00_14</code>	integer	Fatal accidents from 2000–2014
<code>fatalities_00_14</code>	integer	Total fatalities from 2000–2014

Part III: Data Analysis/Visualization

Question 1. Which airlines have the highest total number of incidents between 1985 and 2014, and what is the range of total incidents across all airlines?

```
[16]: airline_safety$total_incidents <- airline_safety$incidents_85_99 +
airline_safety$incidents_00_14

p3 <- ggplot(
  airline_safety,
  aes(x = reorder(airline, total_incidents), y = total_incidents)
) +
geom_col() +
coord_flip() +
labs(
  title = "Total Incidents per Airline (1985-2014)",
  x = "Airline",
  y = "Total Incidents"
) +
theme_minimal()

ggsave("plot3_total_incidents_bar.png", p3, width = 6, height = 6)

print(p3)
```

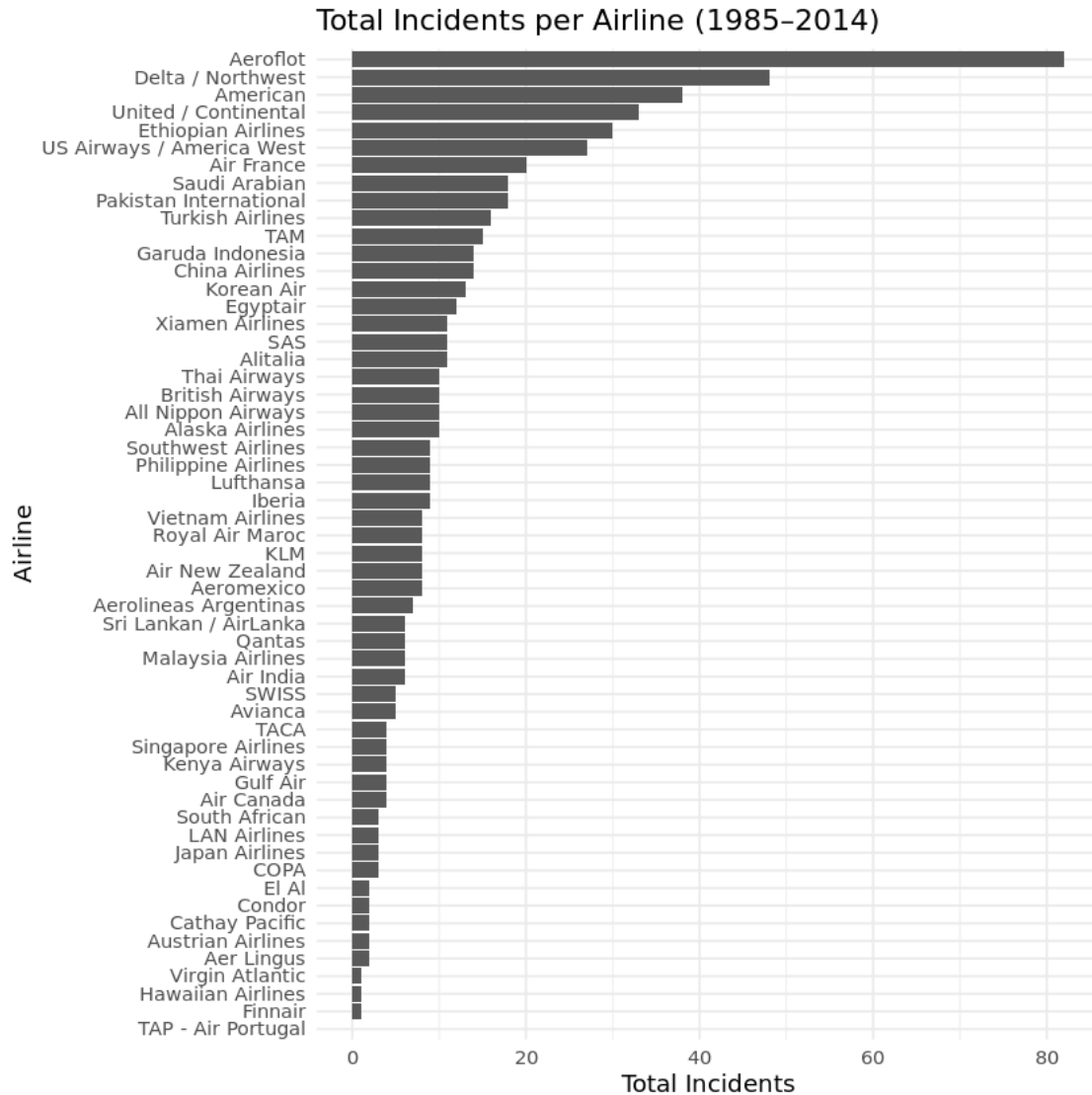


Figure 1. Horizontal bar chart displaying the Total Incidents recorded for each of the 56 airlines over the entire 30-year study period (1985–2014), sorted in descending order of incident count.

Conclusion: The bar chart of “Total Incidents per Airline (1985-2014)” shows that Aeroflot had the highest total number of incidents in the 30-year period. The next highest incidents belong to Delta/Northwest, American, and United/Continental. The total number of incidents across all 56 airlines ranges significantly, from a minimum of 0 for TAP Air Portugal to the maximum value of 76 for Aeroflot.

```
[17]: library(dplyr)

airline_safety <- airline_safety %>%
  mutate(
    incidents_85_99_rate = incidents_85_99 / (avail_seat_km_per_week / 1e9),
```

```
    incidents_00_14_rate = incidents_00_14 / (avail_seat_km_per_week / 1e9)
  )
```

Question 2. Which airlines have the highest incident rates?

```
[18]: install.packages('ggrepel')
```

Installing package into ‘/srv/rlibs’
(as ‘lib’ is unspecified)

```
[19]: library(ggplot2)
      library(ggrepel)

p1 <- ggplot(
  airline_safety,
  aes(
    x = avail_seat_km_per_week,
    y = incidents_85_99_rate,
    label = airline
  )
) +
  geom_point() +
  geom_text(aes(label = airline),
    vjust = -0.5,
    size = 3
  ) +
  labs(
    title = "Incident Rate (1985-1999) vs Operational Volume",
    x = "Available Seat KM per Week",
    y = "Incidents per Billion Seat-KM (1985-1999)"
  ) +
  theme_minimal()

print(p1)
```

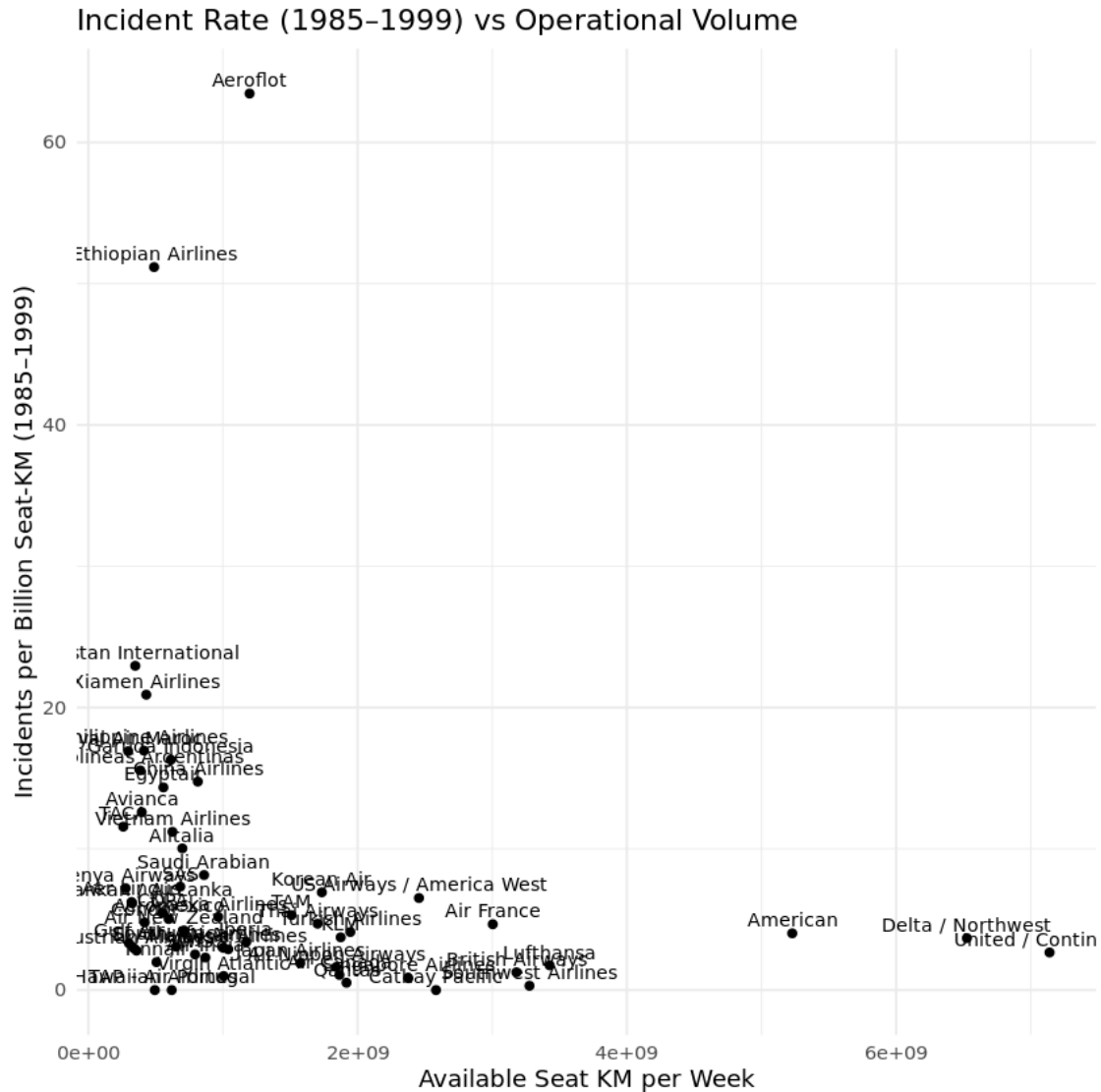


Figure 2. This scatterplot displays the relationship between each airline's operational volume, measured as available seat-kilometers per week, and its incident rate during 1985–1999, expressed per billion seat-kilometers.

```
[20]: p2 <- ggplot(
  airline_safety,
  aes(
    x = avail_seat_km_per_week,
    y = incidents_00_14_rate,
    label = airline
  )
) +
```

```

geom_point() +
geom_text(aes(label = airline),
          vjust = -0.5,
          size = 3) +
labs(
  title = "Incident Rate (2000-2014) vs Operational Volume",
  x = "Available Seat KM per Week",
  y = "Incidents per Billion Seat-KM (2000-2014)"
) +
theme_minimal()

print(p2)

```

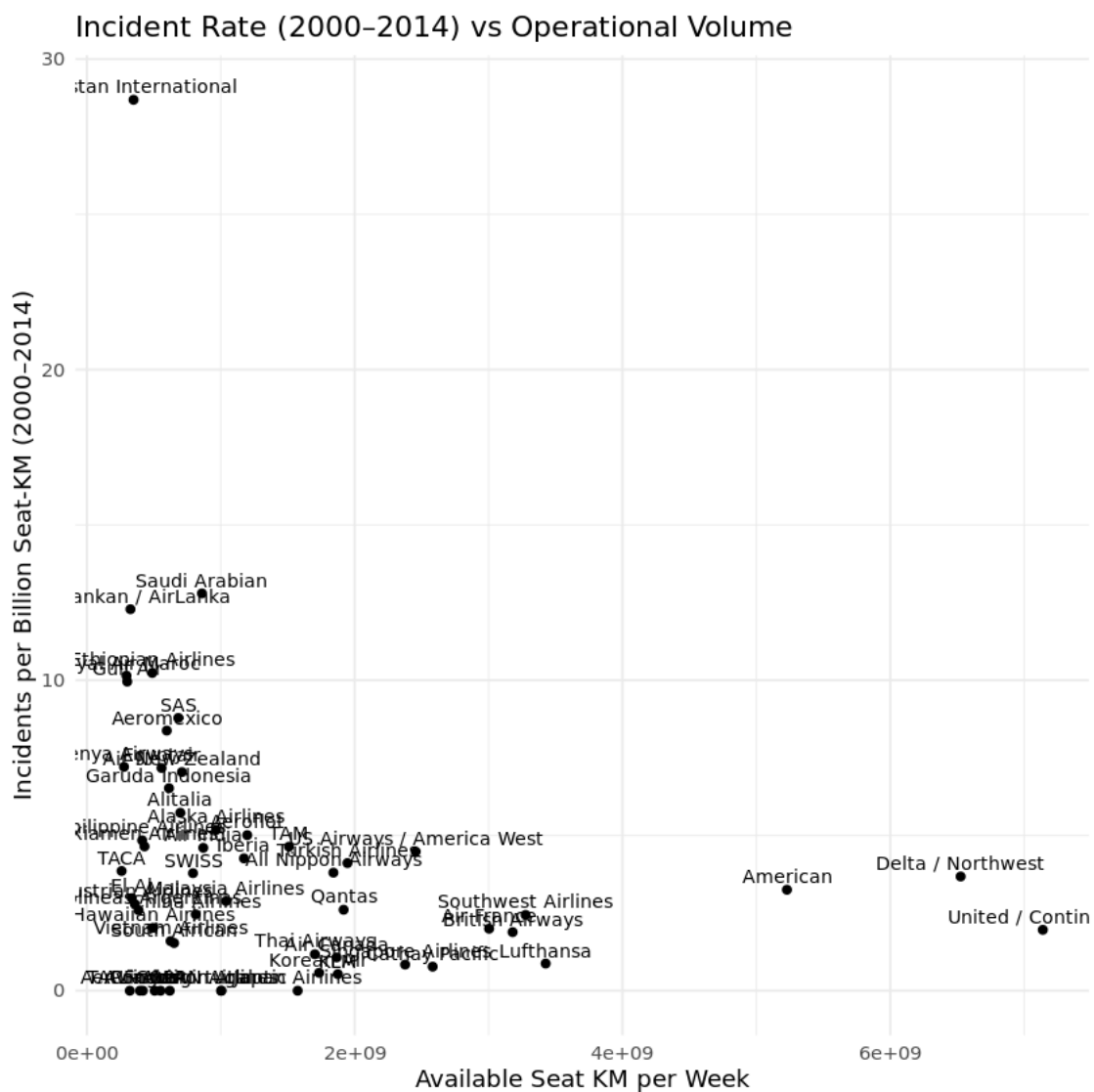


Figure 3. This scatterplot displays the relationship between each airline’s operational volume, measured as available seat-kilometers per week, and its incident rate during 2000-2014, expressed per billion seat-kilometers.

Conclusion: The incident rate scatterplots reveal that the highest incident rates are generally associated with lower operational volume (Available Seat KM per Week). For the period 1985–1999, Aeroflot had the highest incident rate, followed by Ethiopian Airlines and Pakistan International. For the period 2000–2014, Pakistan International had the highest rate, followed by Saudi Arabian and Sri Lankan/AirLanka. Notably, Aeroflot’s incident rate appears to have dropped significantly in the second period, moving from the highest rate in 1985–1999 to a much lower, clustered position in 2000–2014. Conversely, American, Delta/Northwest, and United/Continental maintain low incident rates relative to their high operational volume in both periods.

Question 3. How consistently did safety improvements occur across airlines from 1985–1999 to 2000–2014 after adjusting for operational volume?

```
[34]: library(dplyr)
library(tibble)

airline_safety <- airline_safety %>%
  mutate(
    incidents_85_99_rate      = incidents_85_99      /  

    ↪(avail_seat_km_per_week / 1e9),
    fatal_accidents_85_99_rate = fatal_accidents_85_99 /  

    ↪(avail_seat_km_per_week / 1e9),
    fatalities_85_99_rate     = fatalities_85_99     /  

    ↪(avail_seat_km_per_week / 1e9),

    incidents_00_14_rate      = incidents_00_14      /  

    ↪(avail_seat_km_per_week / 1e9),
    fatal_accidents_00_14_rate = fatal_accidents_00_14 /  

    ↪(avail_seat_km_per_week / 1e9),
    fatalities_00_14_rate     = fatalities_00_14     /  

    ↪(avail_seat_km_per_week / 1e9)
  )
```

```
[35]: p2 <- ggplot(
  airline_safety,
  aes(x = fatalities_85_99_rate,
      y = fatalities_00_14_rate,
      label = airline)
) +
  geom_point() +
  geom_text(
    vjust = -0.5,
    size = 3
  ) +
  labs(
```

```

title = "Fatality Rates: 1985-1999 vs 2000-2014 (Standardized by SKM)",
x = "Fatality Rate 1985-1999",
y = "Fatality Rate 2000-2014"
) +
theme_minimal()

ggsave("plot2_fatality_rates_comparison.png", p2, width = 6, height = 4)

print(p2)

```



Figure 4. Scatterplot comparing the raw number of fatalities between the period 1985–1999 (x-axis) and 2000–2014 (y-axis). This visualization helps identify airlines that experienced a change in the total number of fatalities between the two time periods.

Analysis Method 1: Dimensionality Reduction

```
[36]: airline_safety$class <- cut(
  airline_safety$fatalities_00_14_rate,
  breaks = c(-Inf, 0, 2, Inf),
  labels = c("none", "low", "high")
)

airline_safety$class <- as.factor(airline_safety$class)

sapply(airline_safety, class)
```

```
airline      'character' incl\_reg\_subsidiaries      'logical' avail\_seat\_km\_per\_week
'numeric' incidents\_85\_99      'integer' fatal\_accidents\_85\_99      'integer'
fatalities\_85\_99      'integer' incidents\_00\_14      'integer' fatal\_accidents\_00\_14
'integer' fatalities\_00\_14      'integer' fatal\_accidents\_85\_99\_rate      'numeric'
fatalities\_85\_99\_rate      'numeric' fatal\_accidents\_00\_14\_rate      'numeric'
fatalities\_00\_14\_rate      'numeric' class      'factor' incidents\_85\_99\_rate      'numeric'
incidents\_00\_14\_rate      'numeric'
```

```
[37]: sapply(
  airline_safety %>% select(where(is.numeric)),
  function(x) {
    c(
      Mean = mean(x),
      SD   = sd(x),
      Var  = var(x),
      Min  = min(x),
      Max  = max(x)
    )
  }
)
```

		avail_seat_km_per_week	incidents_85_99	fatal_accidents_85_99	fatal_accidents_00_14
A matrix: 5 × 13 of type dbl	Mean	1.384621e+09	7.178571	2.178571	1.178571
	SD	1.465317e+09	11.035656	2.861069	1.461069
	Var	2.147154e+18	121.785714	8.185714	2.147154
	Min	2.593733e+08	0.000000	0.000000	0.000000
	Max	7.139291e+09	76.000000	14.000000	5.139291

```
[40]: airline_scaled <- airline_safety %>%
  mutate(across(
    .cols = where(is.numeric),
    .fns  = ~ as.numeric(scale(.))
  ))
```

```
[41]: airline_numeric <- airline_scaled %>%
  select(
```

```

    incidents_85_99_rate,
    fatal_accidents_85_99_rate,
    fatalities_85_99_rate,
    incidents_00_14_rate,
    fatal_accidents_00_14_rate,
    fatalities_00_14_rate
  )

```

```

[42]: airline_pca <- prcomp(
      airline_numeric,
      center = FALSE,
      scale. = FALSE
    )

summary(airline_pca)
airline_pca$rotation

```

Importance of components:

	PC1	PC2	PC3	PC4	PC5	PC6
Standard deviation	1.6948	1.2464	0.8236	0.76597	0.41874	0.3658
Proportion of Variance	0.4787	0.2589	0.1130	0.09779	0.02922	0.0223
Cumulative Proportion	0.4787	0.7377	0.8507	0.94848	0.97770	1.0000

		PC1	PC2	PC3	PC4
A matrix: 6 × 6 of type dbl	incidents_85_99_rate	0.4534195	0.2620169	0.60339132	0.10198439
	fatal_accidents_85_99_rate	0.4789720	0.3838092	0.21237815	-0.08083012
	fatalities_85_99_rate	0.3779975	0.3060301	-0.60239564	-0.56383010
	incidents_00_14_rate	0.4268943	-0.1328973	-0.44871505	0.71068383
	fatal_accidents_00_14_rate	0.4322747	-0.4836178	0.01518499	-0.01321358
	fatalities_00_14_rate	0.2302484	-0.6624465	0.16235194	-0.39989397

```

[43]: pc_scores <- as_tibble(airline_pca$x) %>%
      mutate(class = airline_safety$class)

```

```

[44]: ggplot(pc_scores, aes(x = PC1, y = PC2, color = class, label =
      ↪airline_safety$airline)) +
      geom_point() +
      geom_text(aes(label = airline_safety$airline),
                vjust = -0.5,
                size = 3
      ) +
      labs(
        title = "PCA of Airline Safety Data",
        x = "Principal Component 1",
        y = "Principal Component 2",
        color = "Risk Class"
      ) +

```

```
theme_minimal() +  
coord_fixed()
```

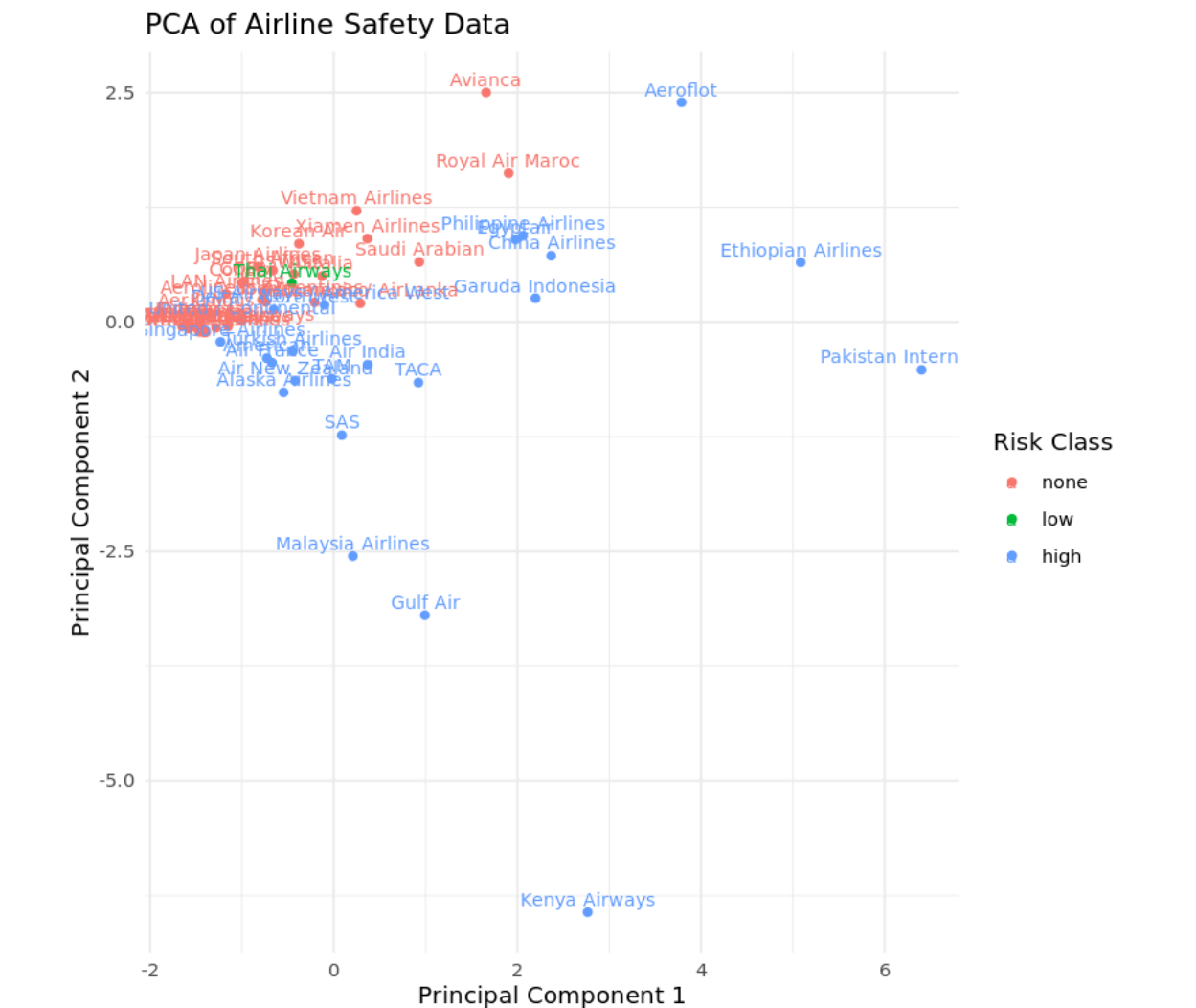


Figure 5.

Analysis Method 2: Clustering

```
[45]: label_randomly <- function(n_points, n_clusters){
      sample(1:n_clusters, size = n_points, replace = TRUE)
    }

    get_cluster_means <- function(data, labels){
      data %>%
        mutate(label__ = labels) %>%
```

```

    group_by(label__) %>%
    summarize(across(where(is.numeric), mean), .groups = "drop") %>%
    rename(label = label__) %>%
    arrange(label)
}

assign_cluster <- function(data, means){
  X <- as.matrix(data)
  C <- as.matrix(means %>% select(-label))
  X_sq <- rowSums(X*X)
  C_sq <- rowSums(C*C)
  dist_sq_matrix <- outer(X_sq, C_sq, "+") - 2*(X %*% t(C))
  max.col(-dist_sq_matrix)
}

kmeans_done <- function(old_means, new_means, eps = 1e-6){
  om <- as.matrix(old_means %>% select(-label))
  nm <- as.matrix(new_means %>% select(-label))
  mean(sqrt(rowSums((om - nm)^2))) < eps
}

mykmeans <- function(data, n_clusters, eps = 1e-6, max_iter = 100){
  labels <- label_randomly(nrow(data), n_clusters)
  old_means <- get_cluster_means(data, labels)
  iter <- 0
  repeat {
    labels <- assign_cluster(data, old_means)
    new_means <- get_cluster_means(data, labels)
    if (kmeans_done(old_means, new_means, eps) || iter >= max_iter) break
    old_means <- new_means
    iter <- iter + 1
  }
  if (iter >= max_iter) warning("K-means did not converge in max_iter.")
  cat("K-means converged after", iter, "iterations.\n")
  list(labels = labels, means = new_means)
}

```

```

[46]: n_clusters <- 3
my_results <- mykmeans(airline_numeric, n_clusters)

print("--- Custom mykmeans Results (Cluster Labels) ---")
print(my_results$labels)

print("--- Custom mykmeans Results (Cluster Means) ---")
print(my_results$means)

```

K-means converged after 4 iterations.

```

[1] "--- Custom mykmeans Results (Cluster Labels) ---"
[1] 2 1 2 2 2 2 2 2 2 2 2 2 1 2 2 1 2 2 2 1 2 1 2 1 3 2 2 2 3 2 2 2 3 1 1 2
[39] 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
[1] "--- Custom mykmeans Results (Cluster Means) ---"
# A tibble: 3 × 7
  label incidents_85_99_rate fatal_accidents_85_99_rate fatalities_85_99_rate
  <int>          <dbl>
<dbl>          <dbl>
1      1          1.58          2.00
1.57
2      2          -0.302
-0.363
-0.278
3      3          -0.309
-0.667
-0.619
# 3 more variables: incidents_00_14_rate <dbl>,
# fatal_accidents_00_14_rate <dbl>, fatalities_00_14_rate <dbl>

```

```

[47]: airline_matrix <- as.matrix(airline_numeric)

r_results <- kmeans(airline_matrix, centers = n_clusters, nstart = 25)

print("--- R's K-means Cluster Labels ---")
print(r_results$cluster)

print("--- R's K-means Means ---")
print(r_results$centers)

```

```

[1] "--- R's K-means Cluster Labels ---"
[1] 3 2 3 3 3 3 3 3 3 3 3 3 2 3 3 3 2 3 2 3 2 1 3 3 3 1 3 3 3 3 1 2 2 3
[39] 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
[1] "--- R's K-means Means ---"
  incidents_85_99_rate fatal_accidents_85_99_rate fatalities_85_99_rate
1      -0.3092078      -0.6670213      -0.6190439
2      1.5785394      1.9983701      1.5661191
3      -0.3018007      -0.3632788      -0.2781350
  incidents_00_14_rate fatal_accidents_00_14_rate fatalities_00_14_rate
1      0.5469733      2.1942863      3.6196243
2      0.9006838      0.8719603      0.1000995
3      -0.2215244      -0.3279659      -0.2672675

```

```

[48]: library(ggplot2)

pc_cluster_plot <- pc_scores %>%
  mutate(cluster = as.factor(my_results$labels))

```

```
ggplot(pc_cluster_plot, aes(PC1, PC2, color = cluster, label =  
  ↪airline_safety$airline)) +  
  geom_point() +  
  geom_text(aes(label = airline_safety$airline),  
            vjust = -0.5,  
            size = 3  
  ) +  
  labs(  
    title = "PCA of Airline Safety Data Colored by K-means Cluster",  
    color = "Cluster"  
  ) +  
  theme_minimal()
```

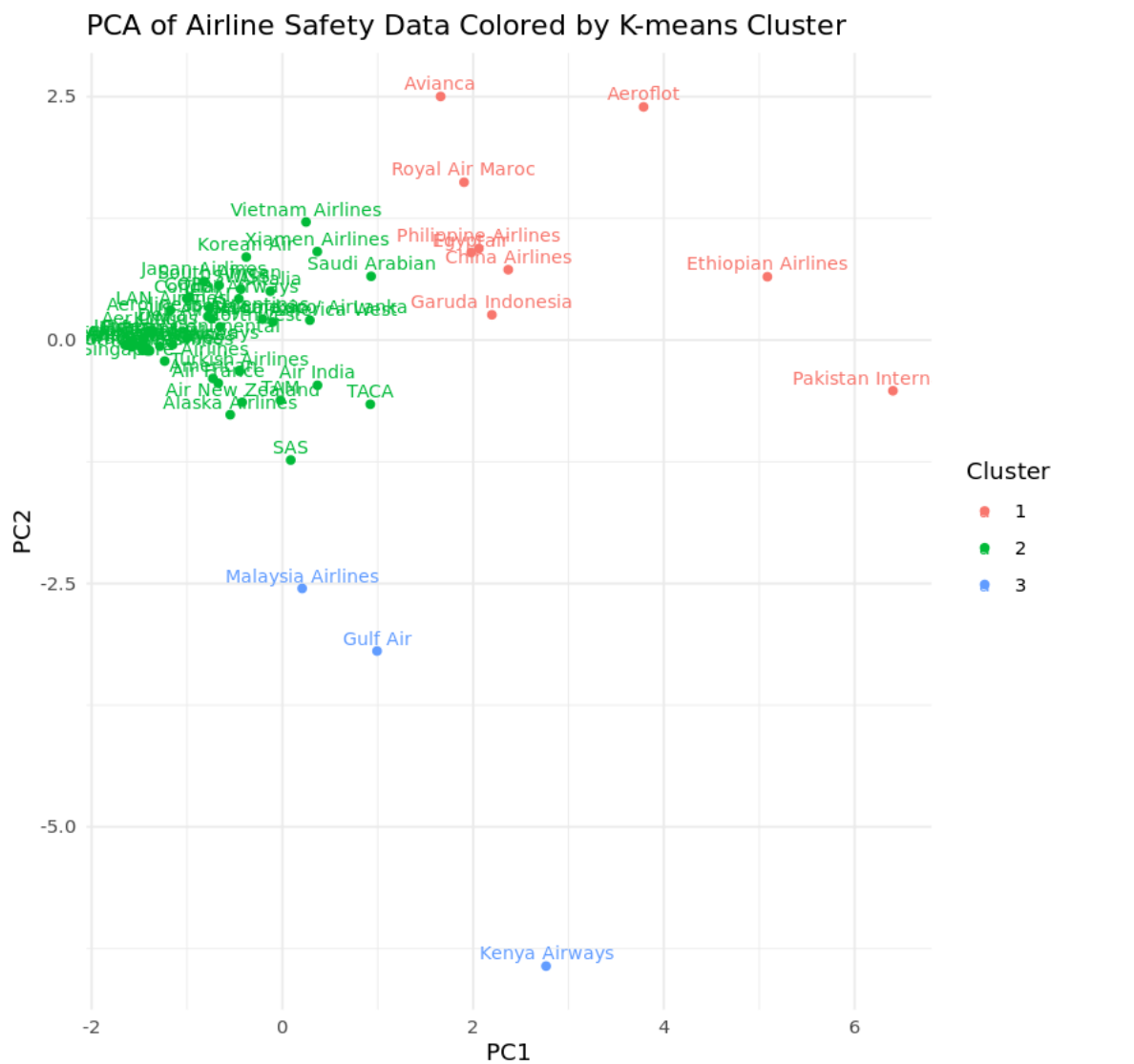


Figure 6.

Analysis Method 1: Regression

```
[49]: d <- airline_numeric
d$airline <- airline_safety$airline

glimpse(d)
summary(d)

set.seed(123)
train <- runif(nrow(d)) < 0.75
test  <- !train

f_model <- fatalities_00_14_rate ~
  incidents_85_99_rate +
  fatal_accidents_85_99_rate +
  fatalities_85_99_rate +
  incidents_00_14_rate +
  fatal_accidents_00_14_rate

m_improve <- lm(f_model, data = d %>% filter(train))
summary(m_improve)

dx <- d %>% filter(test)
dx <- dx %>% mutate(pred_fatal_rate = predict(m_improve, dx))

ggplot(dx, aes(x = fatalities_00_14_rate,
               y = pred_fatal_rate,
               label = airline)) +

  geom_point() +
  geom_text(vjust = -0.5, size = 3) +

  labs(
    x = "Actual Fatality Rate (00-14)",
    y = "Predicted Fatality Rate (00-14)",
    title = "Predicted vs Actual Fatality Rates (00-14)"
  ) +
  theme_minimal()

ggplot(dx, aes(x = fatalities_00_14_rate - pred_fatal_rate)) +
  geom_density(fill = "coral", alpha = 0.5) +
  labs(
    x = "Residuals (Actual - Predicted Fatality Rate)",
    y = "Density",
    title = "Residual Density Plot (Fatality Rate Model)"
  ) +
```

```
theme_minimal()
```

```
Rows: 56
```

```
Columns: 7
```

```
$ incidents_85_99_rate      <dbl> -0.1510810, 4.9876633,  
0.6858237, -0.259392...  
$ fatal_accidents_85_99_rate <dbl> -0.77289269, 3.08524002,  
-0.77289269, -0.21...  
$ fatalities_85_99_rate     <dbl> -0.6758657, -0.1190439,  
-0.6758657, -0.1172...  
$ incidents_00_14_rate      <dbl> -0.87882643, 0.18990017,  
-0.32587492, 0.908...  
$ fatal_accidents_00_14_rate <dbl> -0.5522797003,  
0.0002180767, -0.5522797003,...  
$ fatalities_00_14_rate     <dbl> -0.38717841, 0.05192897,  
-0.38717841, -0.38...  
$ airline                  <chr> "Aer Lingus", "Aeroflot",  
"Aerolineas Argen...
```

incidents_85_99_rate	fatal_accidents_85_99_rate	fatalities_85_99_rate
Min. : -0.7107	Min. : -0.7729	Min. : -0.6759
1st Qu.: -0.4891	1st Qu.: -0.7729	1st Qu.: -0.6759
Median : -0.3118	Median : -0.3449	Median : -0.4905
Mean : 0.0000	Mean : 0.0000	Mean : 0.0000
3rd Qu.: 0.0628	3rd Qu.: 0.1742	3rd Qu.: 0.2790
Max. : 4.9877	Max. : 3.0852	Max. : 3.5639

incidents_00_14_rate	fatal_accidents_00_14_rate	fatalities_00_14_rate
Min. : -0.8788	Min. : -0.5523	Min. : -0.3872
1st Qu.: -0.6606	1st Qu.: -0.5523	1st Qu.: -0.3872
Median : -0.2529	Median : -0.5523	Median : -0.3872
Mean : 0.0000	Mean : 0.0000	Mean : 0.0000
3rd Qu.: 0.1990	3rd Qu.: 0.1521	3rd Qu.: -0.1619
Max. : 5.2415	Max. : 4.2183	Max. : 5.7094

```
airline  
Length:56  
Class :character  
Mode :character
```

```
Call:
```

```
lm(formula = f_model, data = d %>% filter(train))
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-2.1574	-0.2410	-0.1021	0.2128	1.7337

Coefficients:

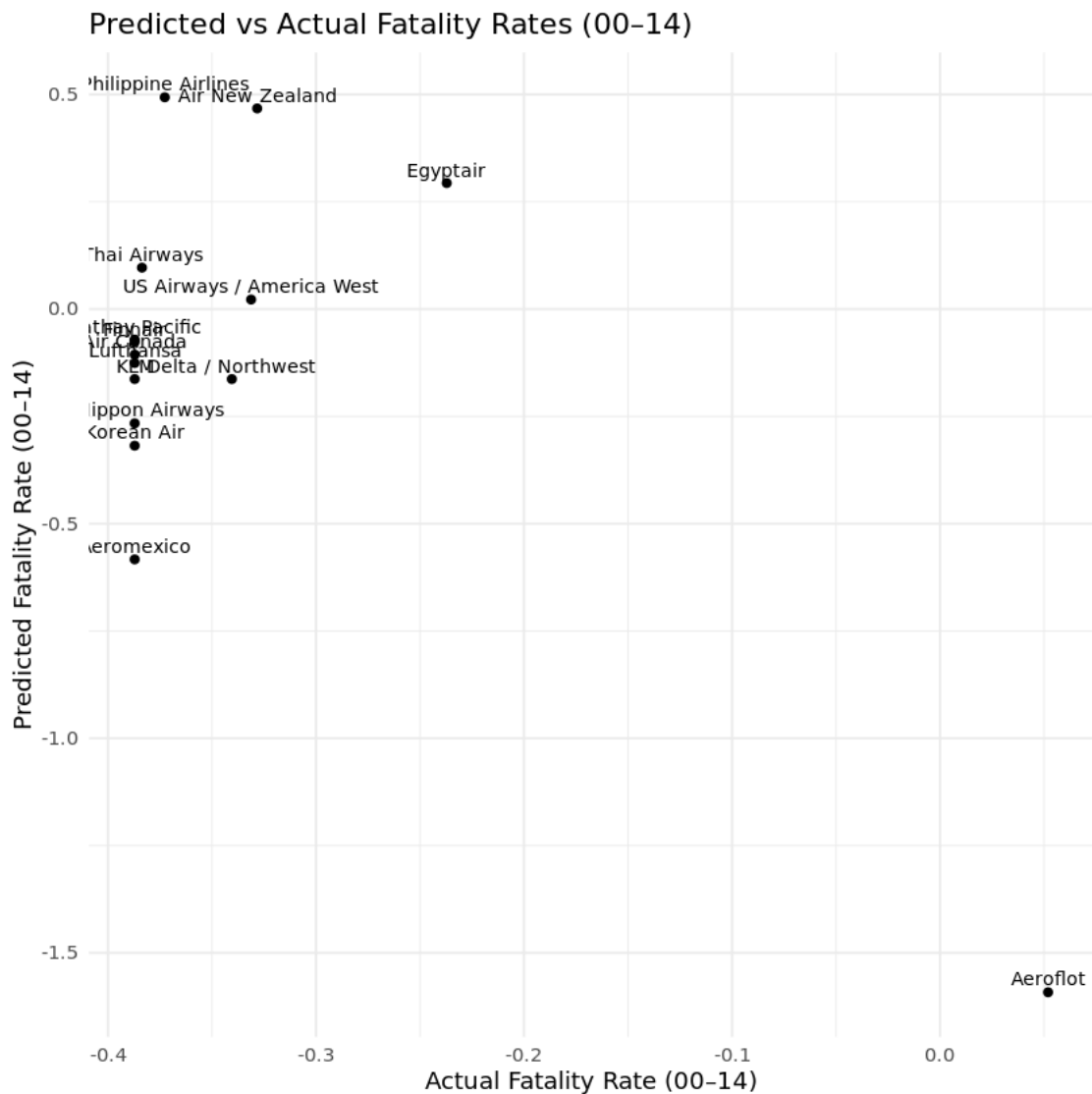
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	0.05264	0.11513	0.457	0.650
incidents_85_99_rate	-0.22765	0.23799	-0.957	0.345
fatal_accidents_85_99_rate	-0.15132	0.24225	-0.625	0.536
fatalities_85_99_rate	0.02293	0.14869	0.154	0.878
incidents_00_14_rate	-0.20880	0.13688	-1.525	0.136
fatal_accidents_00_14_rate	0.97016	0.13154	7.376	1.26e-08 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.7281 on 35 degrees of freedom

Multiple R-squared: 0.6466, Adjusted R-squared: 0.5961

F-statistic: 12.81 on 5 and 35 DF, p-value: 4.122e-07



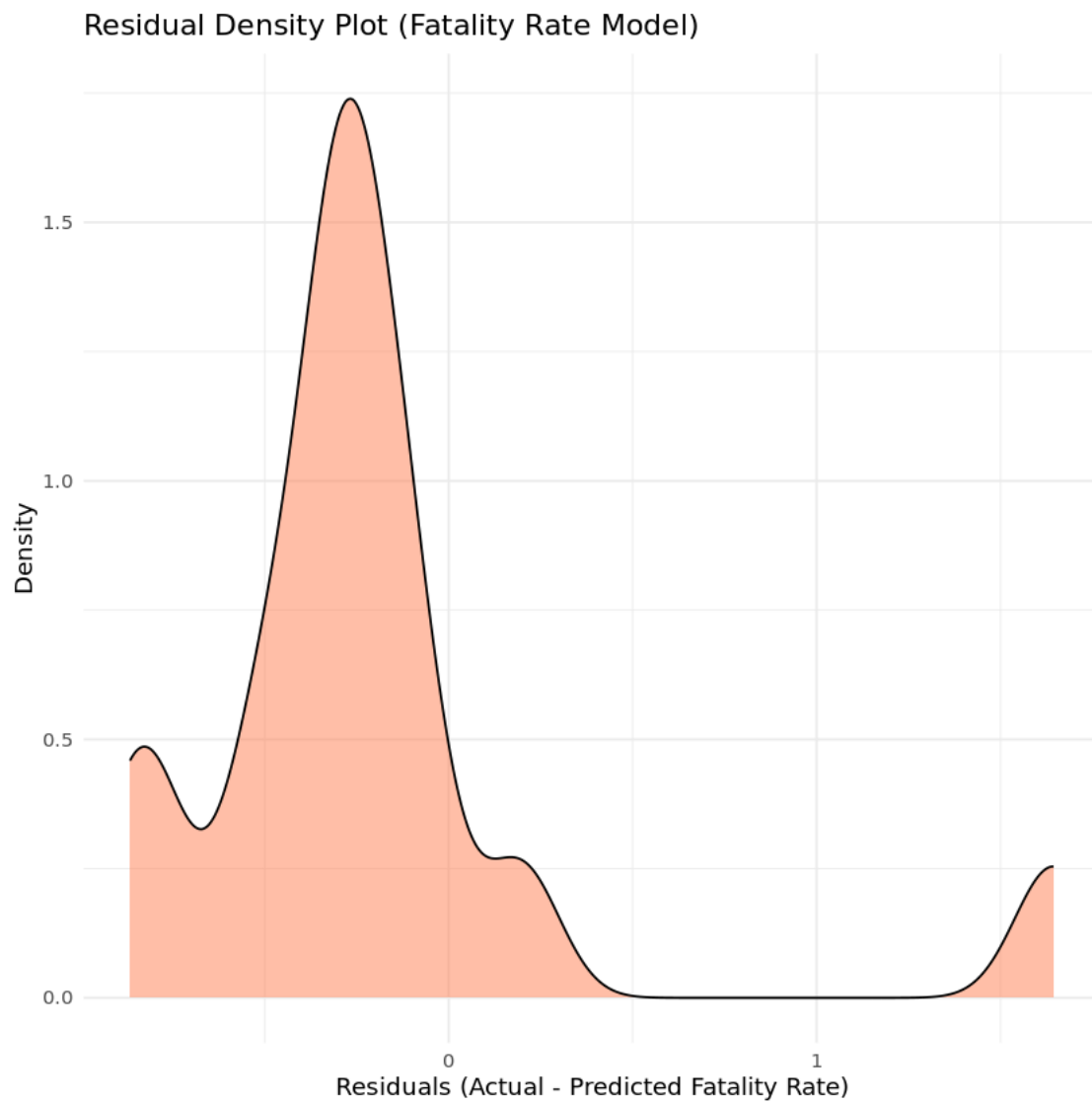


Figure 7.

Conclusion:

Next Steps:

[]: