

# Murphi-Class2

June 2, 2018

# DeadLock

No next state

- no rule to execute
- have one rule

# Running Example: Mutual Exclusion Protocol

$N$  symmetric processors, behaviour of processor  $i$  is described by:

- $try(i) := a[i] = I \rightarrow a[i]' = T$
- $crit(i) := (a[i] = T \wedge x = true \rightarrow a[i]' = C \wedge x' = false)$
- $exit(i) := a[i] = C \rightarrow a[i]' = E$
- $idle(i) := a[i] = E \rightarrow a[i]' = I \wedge x' = true$

Initial states:  $x = true$  and  $a[i] = I$  for all  $i$

Invariant property (where we assume parameters are pairwise disjoint):  
 $\neg(a[i] = C \wedge a[j] = C)$

T

The set of reachable states for a protocol  $\mathcal{P} = (I, R)$ , denoted as  $RS(\mathcal{P})$ , can be defined inductively:

- a state  $s$  is in  $RS(\mathcal{P})$  if there exists a formula  $f \in I$  such that  $s \models f$ ;
- a state  $s'$  is in  $RS(\mathcal{P})$  if there exists a state  $s$  and a guarded command  $r \in R$  such that  $s \in RS(\mathcal{P})$  and  $s \xrightarrow{r} s'$ .

# Important properties–Safety Properties

- Bad things never happen  $\Box P$ .
- Invariants properties of a protocol: mutual exclusion  
 $\neg(a[i] = C \wedge a[j] = C)$
- Data Coherence:  $(ExGntd = false \rightarrow MemData = AuxData)$   
 $\forall i \in NODE.Cache[i].State! = I \rightarrow Cache[i].Data = AuxDataend;$
- No deadLock.

## Important properties–Liveness Properties

- Good things eventually happen
- A request eventually is served  $\Box(P \rightarrow \Diamond Q)$
- A process is eventually scheduled
- A Loop is terminated

## Use Murphi to Compute Reachable state set

```
./mutualEx -ta -d ./
```

Use python to create the table from the trace

# Output Result

```
yj214@ubuntu: ~/Downloads/german2004.j  
b[7]:true  
b[8]:true  
  
State 246:  
a[1]:0  
a[2]:0  
a[3]:0  
a[4]:0  
a[5]:0  
a[6]:0  
a[7]:0  
a[8]:0  
b[1]:false  
b[2]:true  
b[3]:false  
b[4]:true  
b[5]:true  
b[6]:true  
b[7]:true  
b[8]:true  
  
State 247:  
a[1]:0  
a[2]:0  
a[3]:0  
a[4]:0  
a[5]:0  
a[6]:0  
a[7]:0  
a[8]:0  
b[1]:false  
b[2]:false  
b[3]:true  
b[4]:true  
b[5]:true  
b[6]:true  
b[7]:true  
b[8]:true  
  
State 248:  
a[1]:0  
a[2]:0  
a[3]:0  
a[4]:0  
a[5]:0  
a[6]:0  
a[7]:0  
a[8]:0  
b[1]:true  
b[2]:true  
b[3]:true  
b[4]:true  
b[5]:true  
b[6]:true  
b[7]:true  
b[8]:false
```



## A Table to illustrate a reachable state set

Table: a data table transformed from reachable state set

n[1]	n[2]	x
I	I	TRUE
T	I	TRUE
I	T	TRUE
C	I	FALSE
T	T	TRUE
I	C	FALSE
E	I	FALSE
C	T	FALSE
T	C	FALSE
I	E	FALSE
E	T	FALSE
T	E	FALSE