Introduction to Statistical Learning

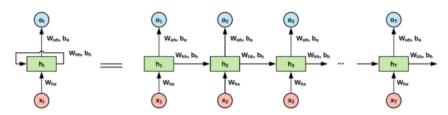
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RNN Structure



This structure allows RNNs to link information from earlier steps to a present step. However, if the RNN is very deep, meaning that it has many layers, it will be prone to vanishing or exploding gradients.

RNN model

Given a sequence of $X=(x_1,x_2,..,x_T)$ inputs , RNN estimates a sequence of $Y=(y_1,y_2,..,y_T)$ outputs by iterating the following equation:

$$h_t = Sigmoid(W^{hx}x_t + W^{hh}h_{t-1})$$

 $y_t = W^{yh}h_t$

Problem? T should be fixed in both input and output sequences. Solution? map input sequence to a fixed length vector and then map that vector to target sequence with another RNN.

Encoder - Decoder Architecture

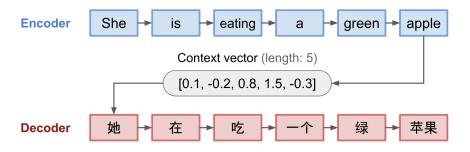
- proposed by Cho et al., 2014
- The encoder processes each item in the input sequence, it compiles the
 information it captures into context vector. After processing the entire
 input sequence, the encoder sends the context vector to the decoder, which
 begins producing the output sequence item by item.

Example Example

Sequence to Sequence models

- A Sequence to Sequence model,, is a model that takes a sequence of items (words, letters, features, ...) and outputs another sequence of items (with any length for both input and output).
- Applications: machine translation between multiple languages in either text or audio, question-answer dialog generation, or even parsing sentences into grammar trees.
- seq2seq is introduced by Sutskever et al., 2014 replaced RNN with LSTM models. Example

NMT Architecture



Use RNN networks (LSTM, GRU,...) for Encoder and Decoder sides. Also we need a Context Vector. (here fixed length).

Context Vector is also called sentence embedding or "thought" vector which represents a good summary of the meaning of the whole source sequence.

Attention Mechanism

Attention

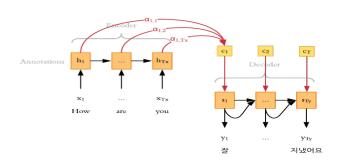
"Definition '

attention can be interpreted as a vector of importance weights: in order to predict or infer one element, such as a pixel in an image or a word in a sentence, we estimate using the attention vector how strongly it is correlated with ("attends to") other elements and take the sum of their values weighted by the attention vector as the approximation of the target.

Ref: Weng, 2018

Bottleneck problem

The last hidden state is actually the context we pass along to the decoder and it is big challenge for the models to deal with long sentences.



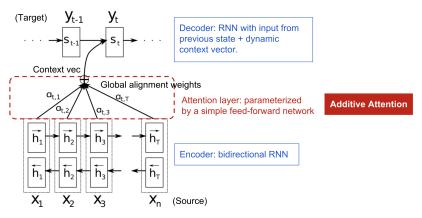
In the encoder-decoder architecture, the complete sequence of information must be captured by a single vector. This poses problems in holding on to information at the beginning of the sequence and encoding long-range dependencies.

Ref: Anusha Lihala

 $https://towards datascience.com/attention-and-its-different-forms-\ref{fig:prop-fig$

Attention

Attention allows the model to focus on the relevant parts of the input sequence as needed. First, the encoder passes a lot more data to the decoder. Instead of passing the last hidden state of the encoding stage, the encoder passes all the hidden states to the decoder:



Bahdanau et al., 2014

Attention

$$p(y) = \prod_{t}^{T} x(p(y_{t}|y_{1},...,y_{t-1}),c)$$

$$p((y_{t}|y_{1},...,y_{t-1}),c) = g(y_{t-1},s_{t},c)$$

$$s_{t} = f(s_{i-1},y_{i-1},c_{i})$$

$$c_{i} = \sum_{t}^{T} x(\alpha_{i_{j}}h_{j})$$

$$\alpha_{i_{j}} = \frac{exp(e_{i_{j}})}{\sum_{k}^{T} x(e_{i_{j}})}$$

$$e_{i_{j}} = a(s_{i-1},h_{j})$$

C: context vector of output y_t h: hidden state ; α_i : Softmax



attention-Encoder

First, the encoder passes a lot more data to the decoder. Instead of passing the last hidden state of the encoding stage, the encoder passes all the hidden states to the decoder Example

attention -Decoder

Second: the decoder does the following:

- Look at the set of encoder hidden states it received each encoder hidden states is most associated with a certain word in the input sentence
- Give each hidden states a score (lets ignore how the scoring is done for now)
- Multiply each hidden states by its softmaxed score, thus amplifying hidden states with high scores, and drowning out hidden states with low scores

Example

Attention - all steps:

- The attention decoder RNN takes in the embedding of the END token, and an initial decoder hidden state.
- The RNN processes its inputs, producing an output and a new hidden state vector (h4). The output is discarded.
- Attention Step: We use the encoder hidden states and the h4 vector to calculate a context vector (C4) for this time step.
- We concatenate h4 and C4 into one vector.
- We pass this vector through a feedforward neural network (one trained jointly with the model).
- The output of the feedforward neural networks indicates the output word of this time step.
- Repeat for the next time steps

Example



Categories of Attention Mechanisms

- Self Attention
- Local vs Global Attention
- Hard vs Soft Attention

Self – attention (intra-attention)

- Machine reading
- Abstractive
 Summarization
- Image description generation

Ref:Cheng et al., 2016

```
The FBI is chasing a criminal on the run.
The FBI is chasing a criminal on the run.
      FBI is chasing a criminal on the run.
The
      FBI is chasing a criminal on the run.
The
      FBI
                chasing a criminal on the run.
The
      FBI
                chasing a criminal on the run.
The
      FBI
                chasing
                            criminal on the run.
The
      FBI
                chasing
                            criminal on the run.
The
                chasing
                            criminal
                                           the run.
The
      FBI
                chasing
                            criminal
                                           the
```

Image Captioning with Attention

ref: Xu et al., 2015



A woman is throwing a frisbee in a park.



A dog is standing on a hardwood floor.



A <u>stop</u> sign is on a road with a mountain in the background.



A little <u>girl</u> sitting on a bed with a teddy bear.



A group of <u>people</u> sitting on a boat in the water.



A giraffe standing in a forest with trees in the background.

Transformers

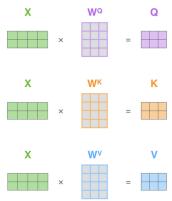
Self-attention mechanism

Ref:Vaswani et al., 2017 Embedding size: 512, q_1 (1*64), key(1*64), value(1*64)

Input	Thinking	Machines	` ,	
Embedding	X ₁	X ₂		
Queries	q ₁	q ₂		Wa
Keys	k1	k₂		Wĸ
Values	V1	V ₂		W

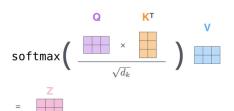
Matrix Notation

 W^Q , W^K , W^V : have 512*64 weights to learn. X dimensions is (maxlen * 512). So X represents a sentence with two words.



Calculate Self Attention Score

- $q_1 * k_1$ score for position 1
- $q_1 * k_2$ score for position 2
- $d_k = 64$



Tensorflow implementation

use tf.linalg.matmul for tensorflow 2

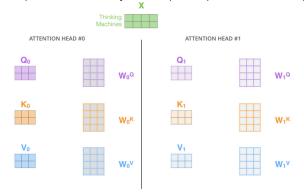
```
♠ □
def scaled_dot_product_attention(g, k, v, mask);
  """Calculate the attention weights.
 g. k. v must have matching leading dimensions.
 k, v must have matching penultimate dimension, i.e.: seq_len_k = seq_len_v
 The mask has different shapes depending on its type(padding or look ahead)
   q: query shape == (..., seq_len_q, depth)
   k: key shape == (..., seq_len_k, depth)
 matmul_qk = tf.matmul(q, k, transpose_b=True) # (..., seq_len_q, seq_len_k)
 dk = tf.cast(tf.shape(k)[-1], tf.float32)
  scaled_attention_logits = matmul_qk / tf.math.sqrt(dk)
  if mask is not None:
   scaled_attention_logits += (mask * -1e9)
  attention weights = tf.nn.softmax(scaled attention logits, axis=-1) # (..., seg len g, seg len k)
 output = tf.matmul(attention_weights, v) # (..., seq_len_q, depth_v)
  return output, attention_weights
```

Multi-Head attention mechanism

we have 512 input dimension and we have 64 as W dimensions. so we need 512/64 = 8 heads.

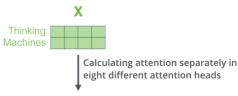
Note: 1. we need multi head to focus on different positions. z1 contains a little bit of every other encoding, but it could be dominated by the the actual word itself.

2. expand attention layer multiple "representation subspaces"



Multi-Head attention mechanism

model dimension =512, number of heads=8



ATTENTION HEAD #0

Z₀

ATTENTION HEAD #1

Z₁

...

ATTENTION HEAD #7

Z₇

Multi-Head attention mechanism

1) Concatenate all the attention heads



2) Multiply with a weight matrix W^o that was trained jointly with the model

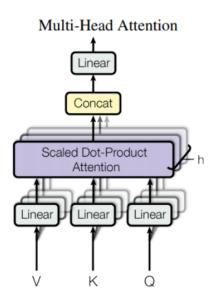
Х

Wo

3) The result would be the ${\mathbb Z}$ matrix that captures information from all the attention heads. We can send this forward to the FFNN

= Z

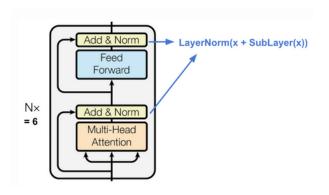
Multi-Head Attention



Multi-Head-Attention

```
class MultiHeadAttention(tf.keras.layers.Layer):
 def __init__(self, d_model, num_heads):
    super(MultiHeadAttention, self).__init__()
   self.num_heads = num_heads
   self.d model = d model
    assert d model % self.num heads == 0
    self.depth = d model // self.num heads
   self.wq = tf.keras.layers.Dense(d_model)
   self.wk = tf.keras.layers.Dense(d_model)
    self.wv = tf.keras.lavers.Dense(d_model)
                                                                  scaled_attention, attention_weights = scaled_dot_product_attention(
                                                                     q, k, v, mask)
    self.dense = tf.keras.lavers.Dense(d model)
                                                                  scaled_attention = tf.transpose(scaled_attention, perm=[0, 2, 1, 3]) # (batch_siz
 def split_heads(self, x, batch_size):
                                                                  concat_attention = tf.reshape(scaled_attention,
    """Split the last dimension into (num heads, depth).
                                                                                            (batch_size, -1, self.d_model)) # (batch_size, seq_
   Transpose the result such that the shape is (batch_size, no
                                                                  output = self.dense(concat_attention) # (batch_size, seq_len_q, d_model)
   x = tf.reshape(x, (batch_size, -1, self.num_heads, self.de)
   return tf.transpose(x, perm=[0, 2, 1, 3])
                                                                  return output, attention_weights
  def call(self, v. k. g. mask):
   batch_size = tf.shape(q)[0]
   q = self.wq(q) # (batch_size, seq_len, d_model)
   k = self.wk(k) # (batch_size, seq_len, d_model)
   v = self.wv(v) # (batch_size, seq_len, d_model)
   q = self.split_heads(q, batch_size) # (batch_size, num_heads, seq_len_q, depth)
   k = self.split_heads(k, batch_size) # (batch_size, num_heads, seq_len_k, depth)
   v = self.split heads(v. batch size) # (batch size, num heads, seg len v. depth)
```

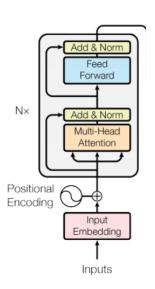
Encoder Layer



Encoder Layer Tensorflow Code

```
4} □
 class EncoderLayer(tf.keras.layers.Layer):
   def __init__(self, d_model, num_heads, dff, rate=8.1);
     super(EncoderLayer, self).__init__()
     self.mha = MultiHeadAttention(d_model, num_heads)
     self.ffn = point_wise_feed_forward_network(d_model. dff)
     self.layernorm1 = tf.keras.layers.LayerNormalization(epsilon=1e-6)
     self.layernorm2 = tf.keras.layers.LayerNormalization(epsilon=1e-6)
     self.dropout1 = tf.keras.layers.Dropout(rate)
     self.dropout2 = tf.keras.layers.Dropout(rate)
   def call(self, x, training, mask);
     attn_output. _ = self.mha(x, x, x, mask) # (batch_size, input_seq_len, d_model)
     attn_output = self.dropout1(attn_output, training=training)
     out1 = self.layernorm1(x + attn output) # (batch size, input seg len, d model)
     ffn output = self.ffn(out1) # (batch size, input seg len, d model)
     ffn_output = self.dropout2(ffn_output, training=training)
     out2 = self.layernorm2(out1 + ffn_output) # (batch_size, input_seq_len, d_model)
     return out2
def point_wise_feed_forward_network(d_model, dff):
  return tf.keras.Sequential([
       tf.keras.lavers.Dense(dff. activation='relu'), # (batch_size, seg_len, dff)
       tf.keras.layers.Dense(d_model) # (batch_size, seq_len, d_model)
```

Encoder Architecture



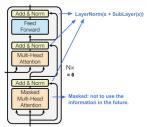
Encoder Tensorflow implementation

```
class Encoder(tf.keras.layers.Layer):
 def __init__(self, num_layers, d_model, num_heads, dff, input_vocab_size,
               maximum_position_encoding, rate=8.1):
   super(Encoder, self), init_()
   self.d model = d model
   self.num_layers = num_layers
   self.embedding = tf.keras.layers.Embedding(input_vocab_size, d_model)
   self.pos_encoding = positional_encoding(maximum_position_encoding,
                                            self.d_model)
   self.enc layers = [EncoderLayer(d model, num heads, dff, rate)
                       for _ in range(num_layers)]
   self.dropout = tf.keras.layers.Dropout(rate)
 def call(self, x, training, mask):
   seq_len = tf.shape(x)[1]
   x = self.embedding(x) # (batch_size, input_seg_len, d_model)
   x *= tf.math.sqrt(tf.cast(self.d model, tf.float32))
   x += self.pos_encoding[:, :seq_len, :]
   x = self.dropout(x, training=training)
   for i in range(self.num_lavers):
     x = self.enc_layers[i](x, training, mask)
```

Decoder Layer

In the decoder, the self-attention layer is only allowed to attend to earlier positions in the output sequence. This is done by masking future positions (setting them to -inf) before the softmax step in the self-attention calculation.

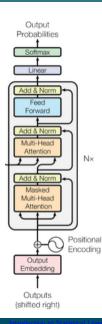
The "Encoder-Decoder Attention" layer works just like multiheaded self-attention, except it creates its Queries matrix from the layer below it, and takes the Keys and Values matrix from the output of the encoder stack.



Decoder Layer TF code

```
₽ □
class DecoderLayer(tf.keras.layers.Layer):
  def __init__(self, d_model, num_heads, dff, rate=0.1):
    super(DecoderLayer, self),__init__()
    self.mha1 = MultiHeadAttention(d model, num heads)
    self.mha2 = MultiHeadAttention(d_model, num_heads)
    self.ffn = point wise feed forward network(d model. dff)
    self.layernorm1 = tf.keras.layers.LayerNormalization(epsilon=1e-6)
    self.layernorm2 = tf.keras.layers.LayerNormalization(epsilon=1e-6)
    self.layernorm3 = tf.keras.layers.LayerNormalization(epsilon=1e-6)
    self.dropout1 = tf.keras.layers.Dropout(rate)
    self.dropout2 = tf.keras.layers.Dropout(rate)
    self.dropout3 = tf.keras.lavers.Dropout(rate)
  def call(self, x, enc output, training,
           look_ahead_mask, padding_mask):
    attn1, attn_weights_block1 = self.mha1(x, x, x, look_ahead_mask) # (batch_size, target_seq_len, d_mod
    attn1 = self.dropout1(attn1, training=training)
    out1 = self.layernorm1(attn1 + x)
    attn2, attn_weights_block2 = self.mha2(
        enc_output, enc_output, out1, padding_mask) # (batch_size, target_seq_len, d_model)
    attn2 = self.dropout2(attn2, training=training)
    out2 = self.layernorm2(attn2 + out1) # (batch_size, target_seq_len, d_model)
    ffn_output = self.ffn(out2) # (batch_size, target_seg_len, d_model)
    ffn output = self.dropout3(ffn output, training=training)
    out3 = self.layernorm3(ffn output + out2) # (batch size, target seg len, d model)
    return out3, attn weights block1, attn weights block2
```

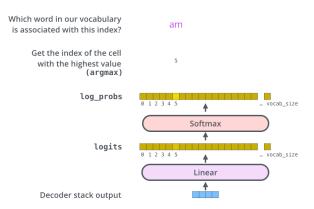
Decoder Architecture



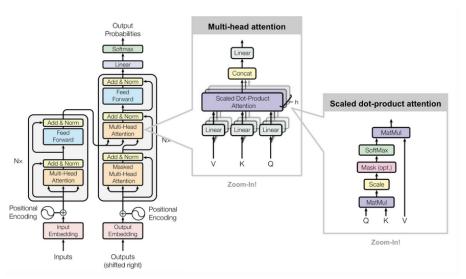
Decoder Architecture Tensorflow implementation

```
class Decoder(tf.keras.layers.Layer):
 def __init__(self, num_layers, d_model, num_heads, dff, target_vocab_size,
               maximum_position_encoding, rate=0.1):
    super(Decoder, self), init ()
    self.d model = d model
   self.num_layers = num_layers
    self.embedding = tf.keras.layers.Embedding(target_vocab_size. d_model)
    self.pos_encoding = positional_encoding(maximum_position_encoding, d_model)
   self.dec_layers = [DecoderLayer(d_model, num_heads, dff, rate)
                      for _ in range(num_layers)]
   self.dropout = tf.keras.layers.Dropout(rate)
 def call(self, x, enc_output, training,
          look_ahead_mask, padding_mask):
   seq_len = tf.shape(x)[1]
    attention_weights = {}
   x = self.embedding(x) # (batch_size, target_seq_len, d_model)
   x *= tf.math.sqrt(tf.cast(self.d_model, tf.float32))
   x += self.pos_encoding[:, :seq_len, :]
    x = self.dropout(x, training=training)
    for i in range(self.num_layers):
     x, block1, block2 = self.dec_layers[i](x, enc_output, training,
                                             look_ahead_mask, padding_mask)
      attention_weights['decoder_laver{}_block1',format(i+1)] = block1
     attention_weights['decoder_layer{}_block2'.format(i+1)] = block2
    return x, attention_weights
```

Transformer Decoder Output Softmax



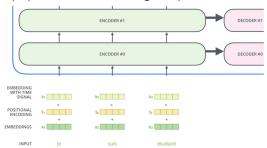
Full Architecture



Example

Positional Encoding

The intuition here is that adding these values to the embedding provides meaningful distances between the embedding vectors once they're projected into Q/K/V vectors and during dot-product attention.



Positional Encoding

Positional Encoding

```
def get_angles(pos, i, d_model):
  angle_rates = 1 / np.power(10000, (2 * (i//2)) / np.float32(d_model))
  return pos * angle_rates
                                                                                               ♠ □
def positional_encoding(position, d_model):
  angle_rads = get_angles(np.arange(position)[:, np.newaxis],
                          np.arange(d_model)[np.newaxis, :],
                          d_model)
  angle_rads[:. 0::2] = np.sin(angle_rads[:. 0::2])
  angle_rads[:, 1::2] = np.cos(angle_rads[:, 1::2])
 pos_encoding = angle_rads[np.newaxis, ...]
  return tf.cast(pos_encoding, dtype=tf.float32)
```

BERT

BERT

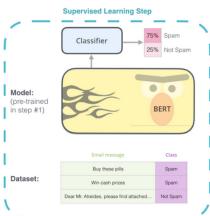
1 - Semi-supervised training on large amounts of text (books, wikipedia..etc).

The model is trained on a certain task that enables it to grasp patterns in language. By the end of the training process, BERT has language-processing abilities capable of empowering many models we later need to build and train in a supervised way.

Semi-supervised Learning Step



2 - Supervised training on a specific task with a labeled dataset.

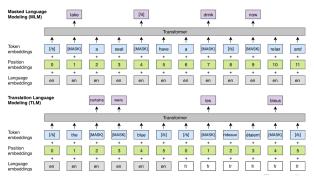


The two steps of how BERT is developed. You can download the model pre-trained in step 1 (trained on un-annotated data), and only worry about fine-tuning it for step 2. [Source for book icon].

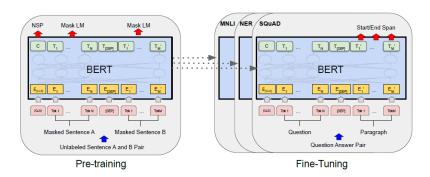
Masked Language Modeling

Ref: Devlin et al., 2018

- A [CLS] token is inserted at the beginning of the first sentence and a [SEP] token is inserted at the end of each sentence.
- A sentence embedding indicating Sentence A or Sentence B is added to each token.
- A positional embedding is added to each token to indicate its position in the sequence. The concept and implementation of positional embedding are presented in the Transformer paper.

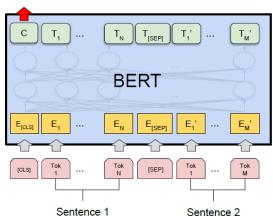


Sentence Classification with BERT

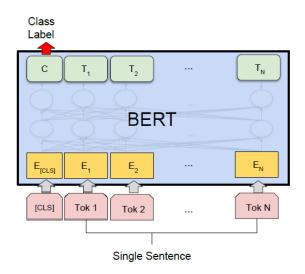


BERT Task: Sentence pair Classification

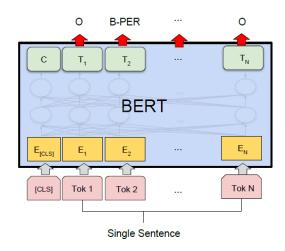
Class Label



BERT Task: Single Sentence Classification



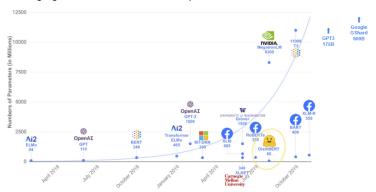
BERT Task: Name Entity Recognition



Model size and computational efficiency

Recent trends

☐ Going big on model sizes - over 1 billion parameters as become the norm for SOTA



References



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