

# What are the key quantities of astronomy and how do we measure them?

- Distance/Size                      Lecture 2
- Angular Size                      Lecture 2
- Time                              Lecture 2
- Speed/Velocity
- Mass
- Flux

# However, distances within the Solar System get awkward with km

- The planets are much smaller than the distances between them
- Distance from the Sun to the Earth:  
 $d = 150,000,000 \text{ km} = 1.5 \times 10^8 \text{ km}$
- So one approach is to use scientific notation
- Here is a case where we make up a new unit to deal with all of those zeros:

**1 AU = Sun-Earth distance =  $1.5 \times 10^8 \text{ km}$**

The astronomical unit was originally conceived as the average of Earth's aphelion and perihelion  
 $1.49597870700 \times 10^8 \text{ km}$

# Kepler's Laws, Newton's Laws, and Gravity

Understanding why the planets orbit  
around the Sun the way that they do  
Chapters 3.3-3.5, 4.1-4.2, 4.4

# Vocabulary for motions

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  - How fast something is moving regardless of direction

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# Vocabulary for motions

- Speed
  - How fast something is moving regardless of direction
- Velocity
  - A speed plus a direction
- Acceleration
  - A change in velocity (i.e., a change in speed or direction, or both)
- Orbit
  - The path through space that one object takes as it moves around another object

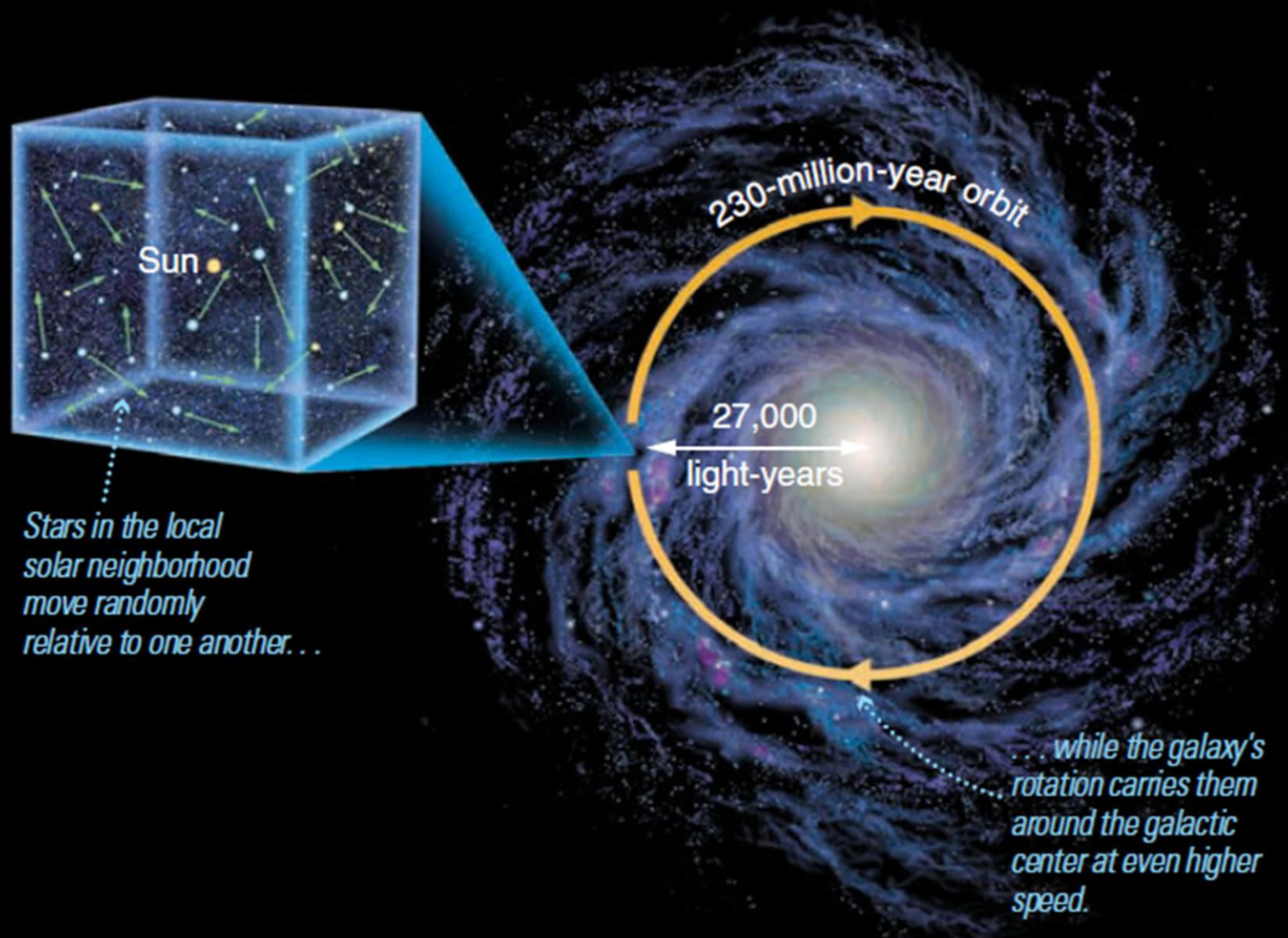
# Units for speeds and velocities

- In astronomy, we use metric units
- Kilometers per second (km/s)
- Or, meters per second (m/s)
- $1 \text{ km/s} = 2250 \text{ mph!}$



For more on the metric system, see appendix C.4 in your textbook

# Speeds

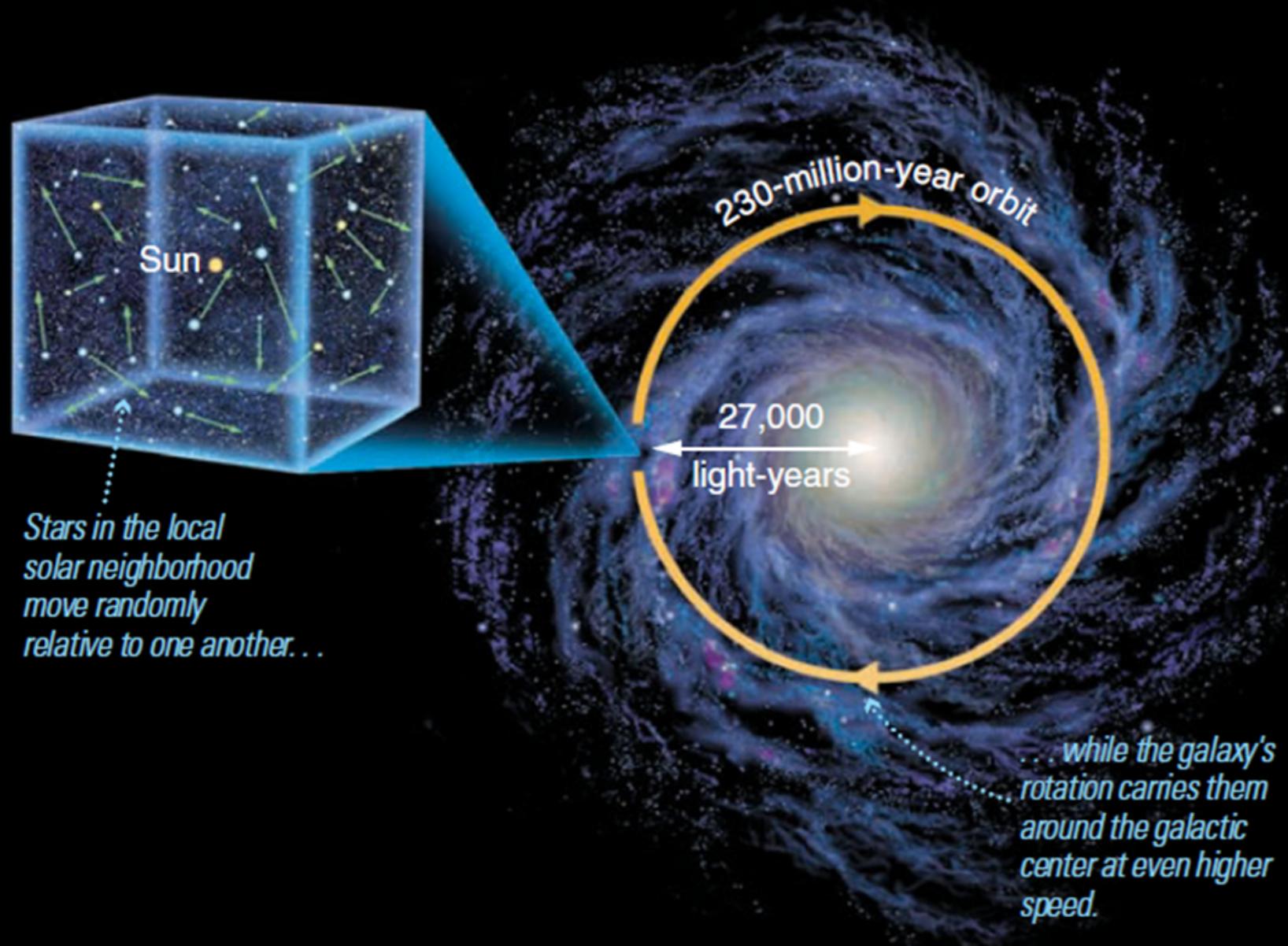


- Planets around a star  
~10 km/s or  
~22,500 miles/hr!

- Stars relative to the center of the galaxy  
~200 km/s

$$1 \text{ km/s} = 2250 \text{ mph}$$

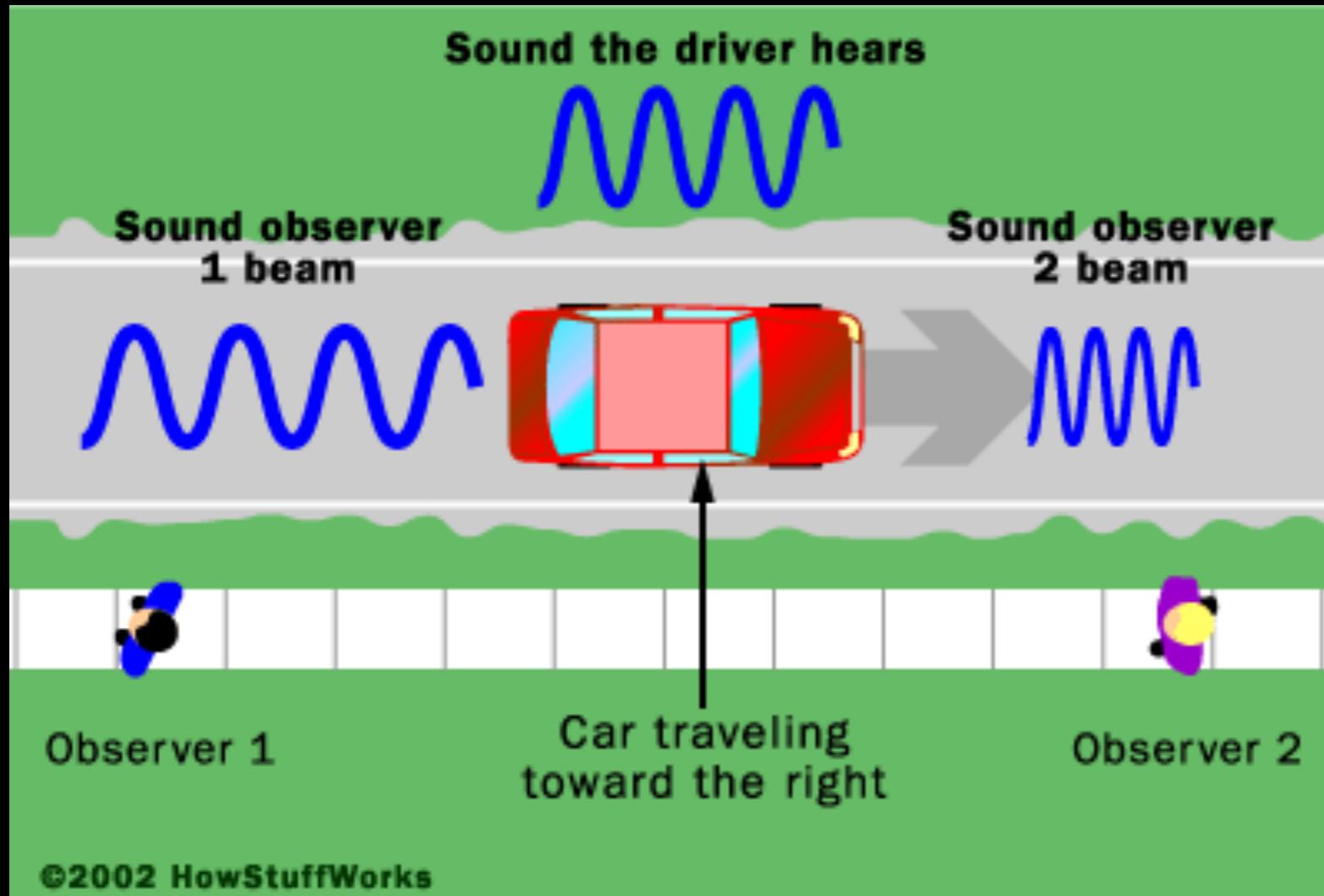
# Speeds



- Planets around a star  
~10 km/s or  
~22,500 miles/hr!
- Stars relative to the center of the galaxy  
~200 km/s
- Galaxies relative to other galaxies  
hundreds to ~1000 km/s
- Speed of light  
 $3 \times 10^5$  km/s

# How do we measure speeds?

- We use the Doppler shift of light
- We'll discuss this when we discuss spectroscopy in a few lectures.



The same process works for light.  
Higher frequency (blue) means that the object is moving toward you.  
Lower frequency (red) means that it is moving away

$$v = c (\lambda - \lambda_0) / \lambda_0$$

# To understand motions, we also need to discuss mass



This woman has a weight (on Earth) of about 120 lbs

... or a mass of about 54 kg.

In astronomy, one of the typical units of mass is the kilogram (kg)

# Mass vs Weight

**Mass** – a measure of the amount of matter in an object

**Weight** – the *force* that a scale measure exerts upon an object

# Mass vs Weight

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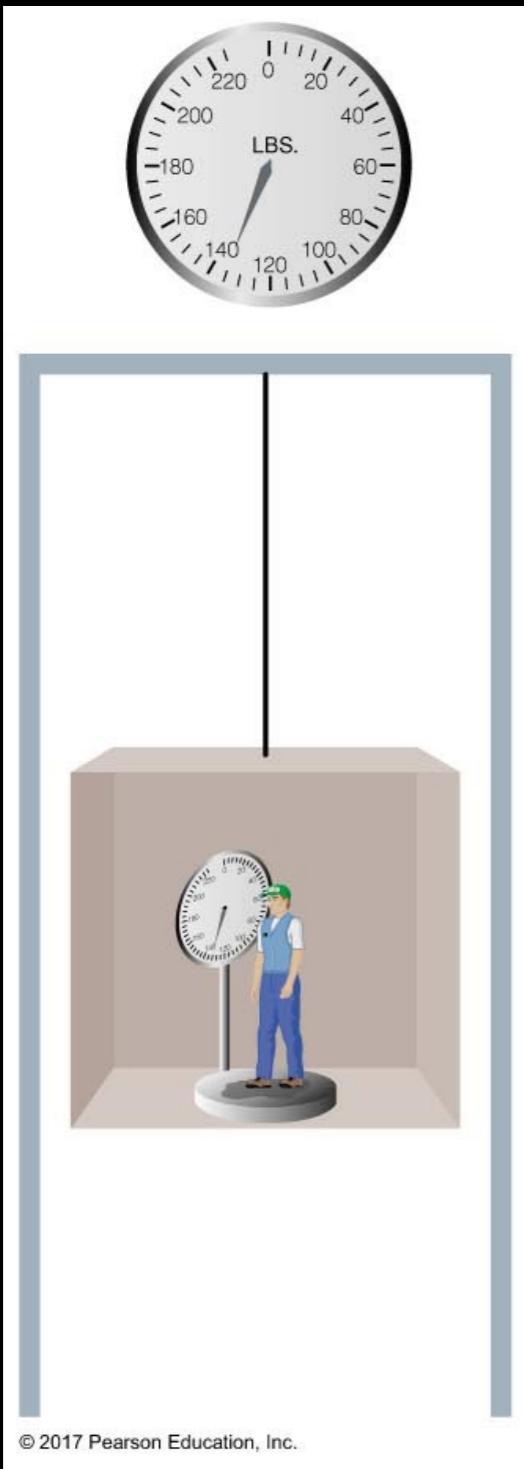
**Weight** – the *force* that a scale measure exerts upon an object

For example

**Your mass** – the amount of mass in your body

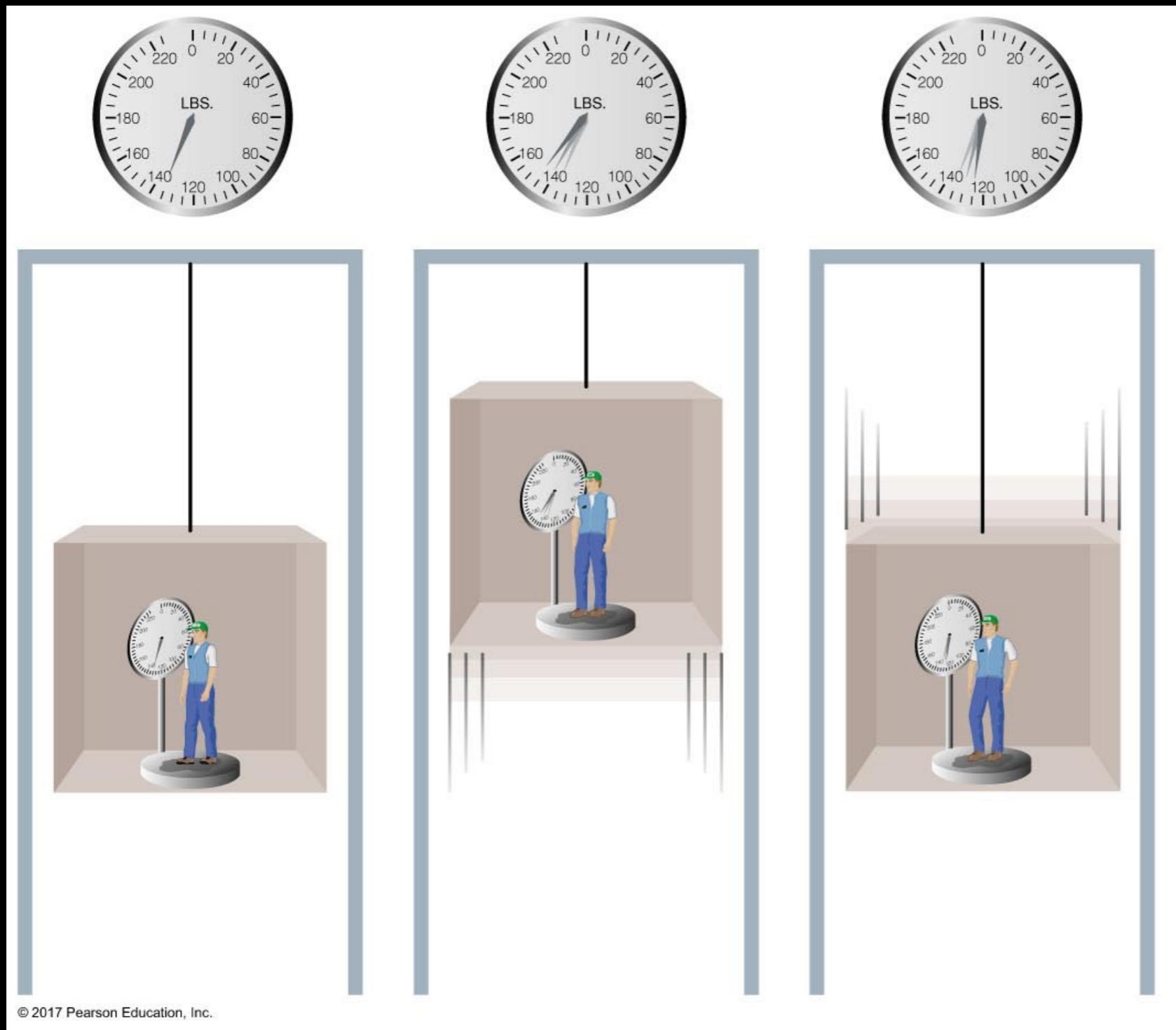
**Your Weight** – the *force* that a scale measure when you stand on it

# Mass vs Weight



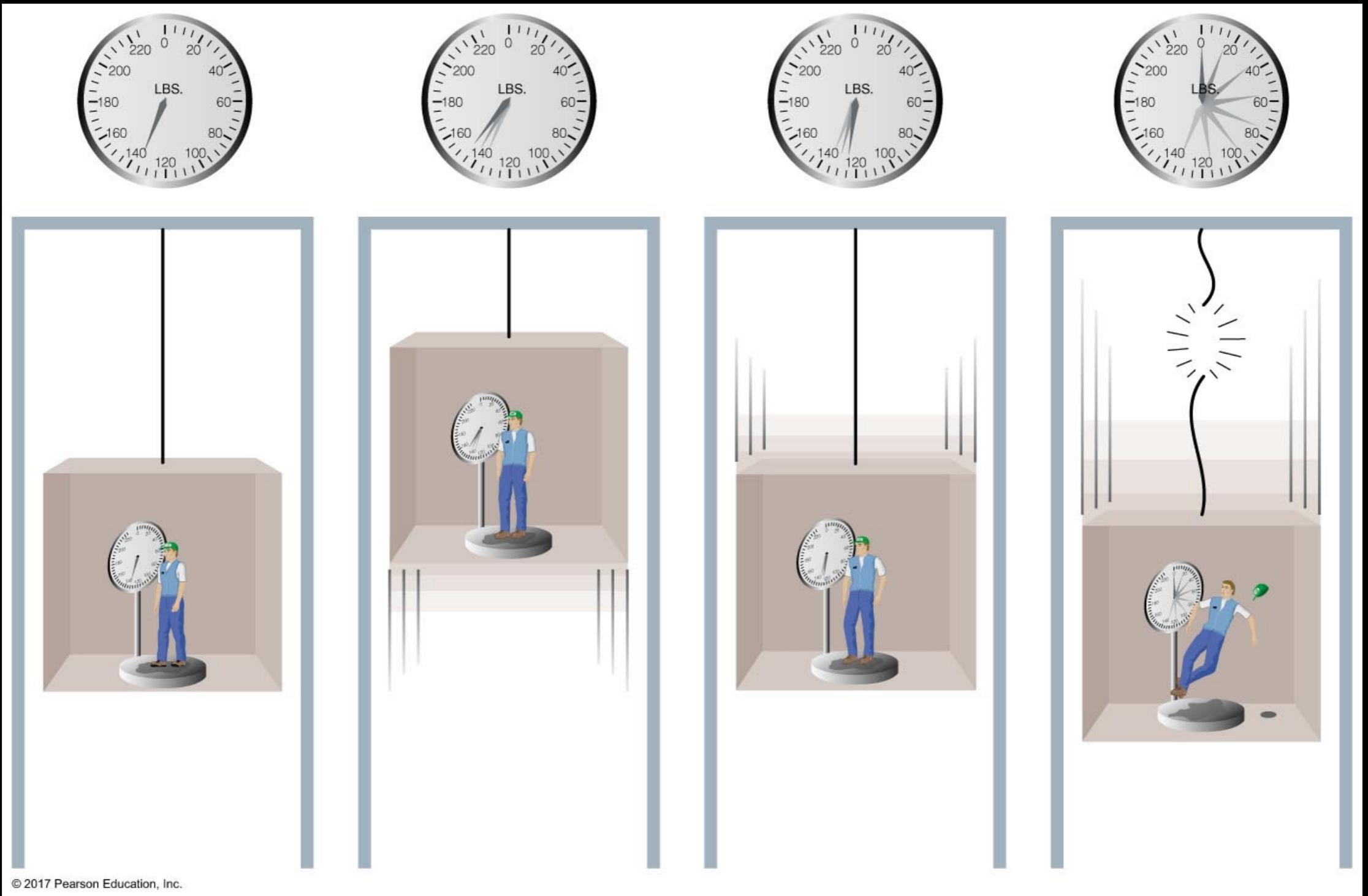
What is your mass in an elevator ?  
What is your weight?

# Mass vs Weight



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# Mass vs Weight



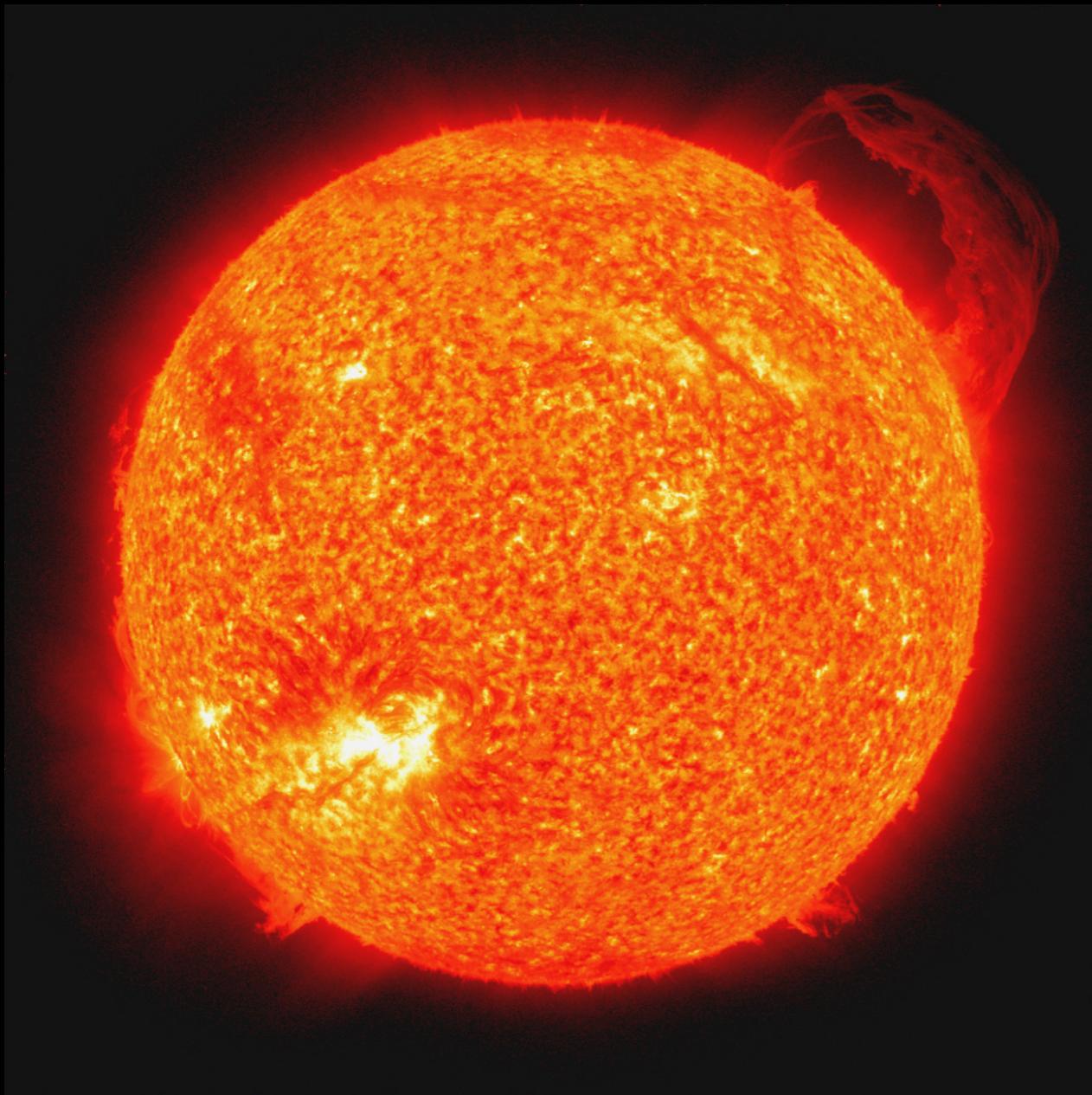
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What is your weight?

# But what is mass?

- The amount of matter in an object
- Equivalently, mass is a measurement of how hard it is to move something
- Huh? See discussion of Newton's Laws coming up



# Mass -- STARS



This star, our Sun, has a mass of about

2,000,000,000,000,000,000,000,000 kilograms

That's a lot of zeros, so instead, we'll make a new unit called the **SOLAR MASS**.

$$1M_{\odot} = 1 \text{ Solar Mass} = 2 \times 10^{30} \text{ kg}$$

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- We look at the speed of small things orbiting around the object that we want to study
  - Satellites around the Earth
  - Planets around a star
  - Gas around a star
  - Stars within a galaxy
  - Galaxies within a cluster
- To understand how this works, we need some more tools.

# Understanding motions in the Universe

The first question: How do astronomical objects (planets, stars, gas, etc.) move?

# Understanding motions in the Universe

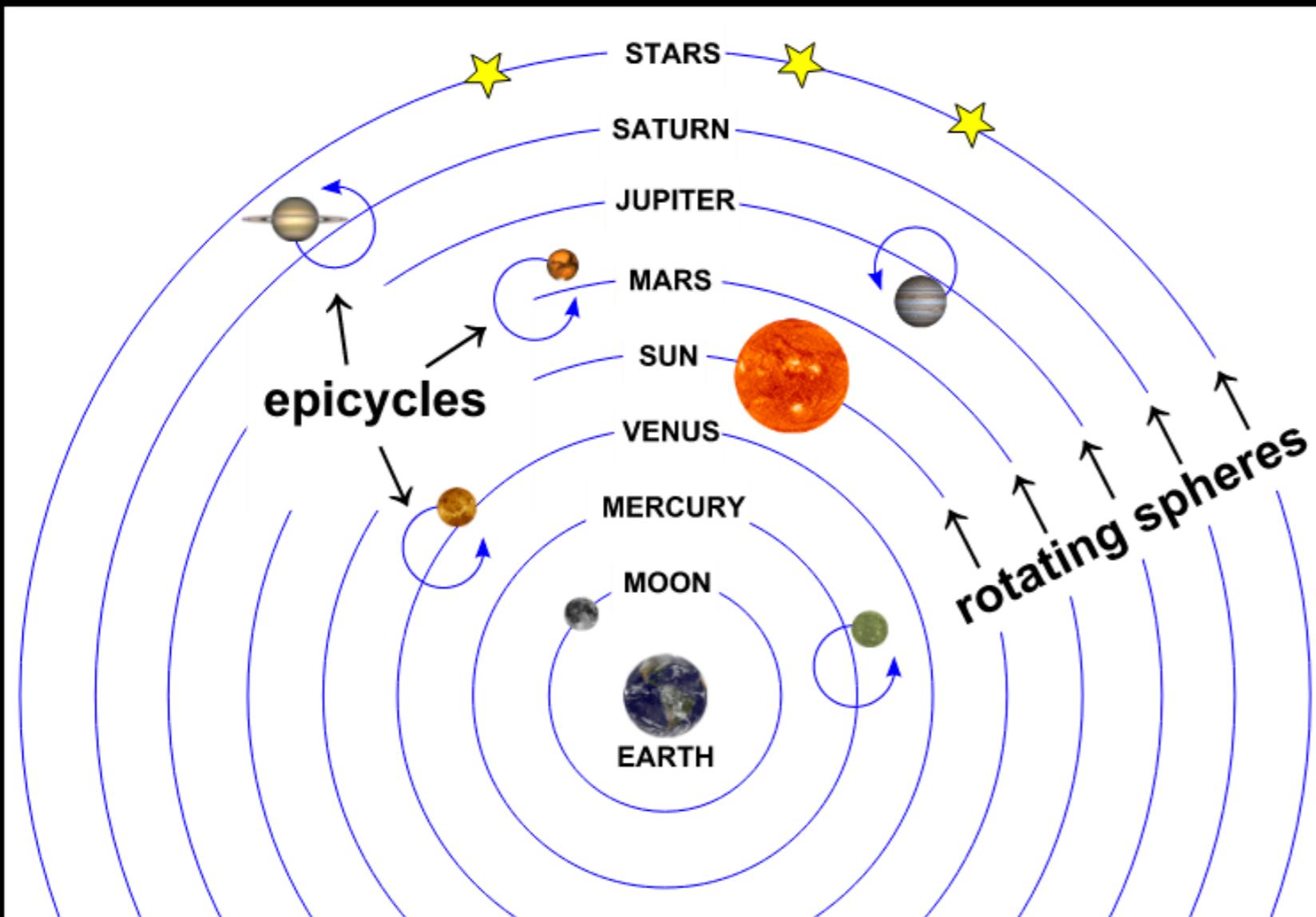
The first question: How do astronomical objects (planets, stars, gas, etc.) move?

The next question: Why do they move the way they do?

– This is where the physics really comes in

# Ptolemaic model

The most sophisticated geocentric model was that of Ptolemy (A.D. 100–170)

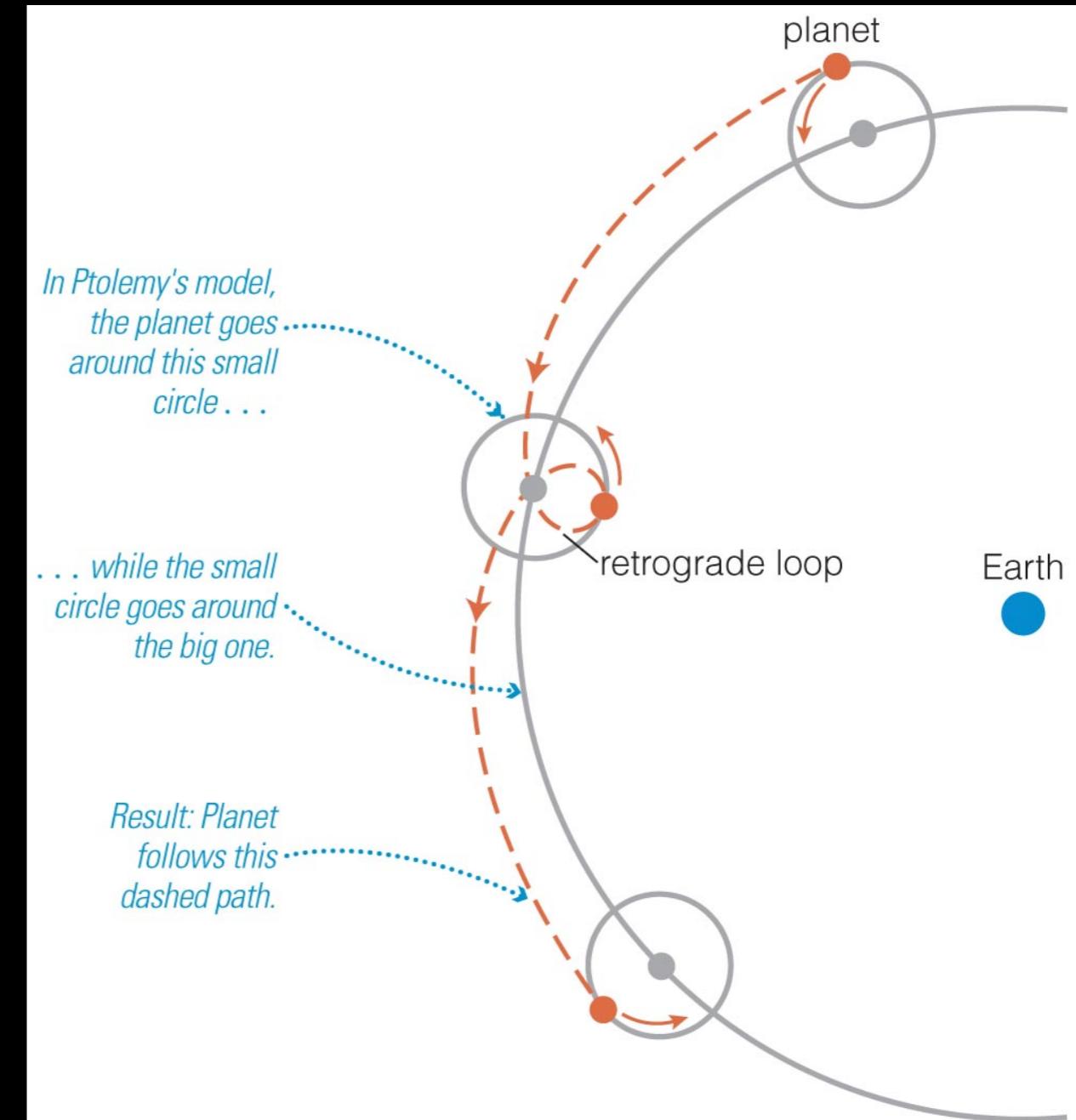


Sufficiently accurate to remain in use for 1,500 years.

# Ptolemaic model



Retrograde motion  
of Mars



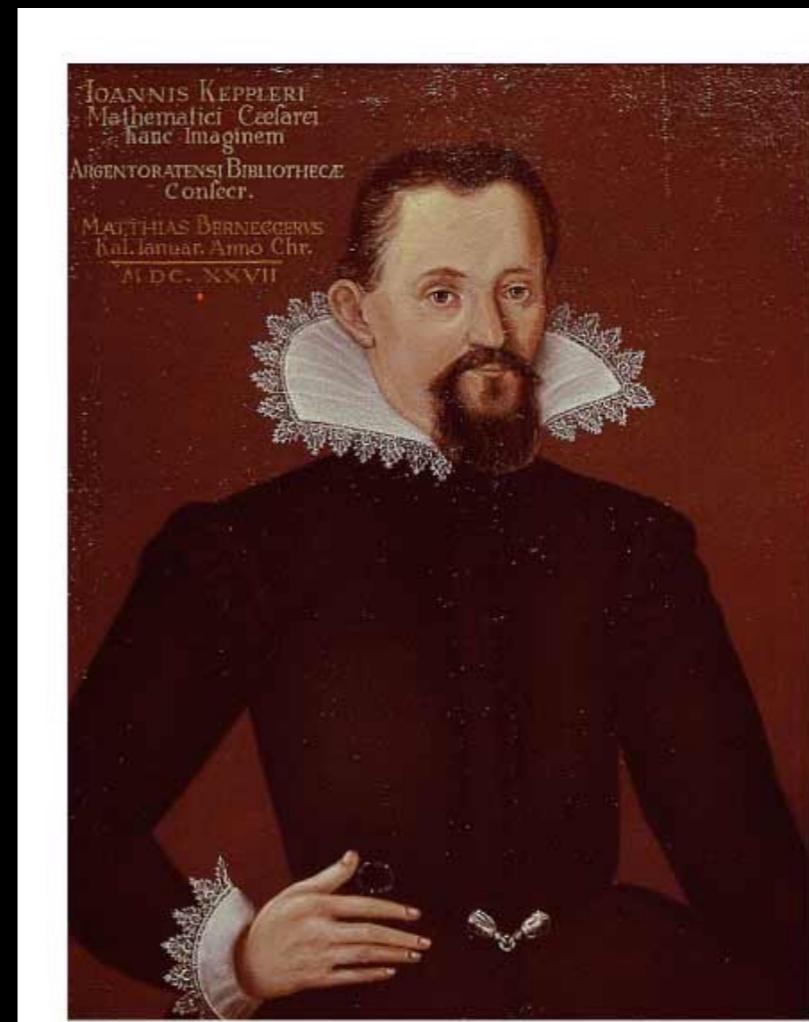
We will see this in the next slides

# An example of how things move:

## Kepler's Laws

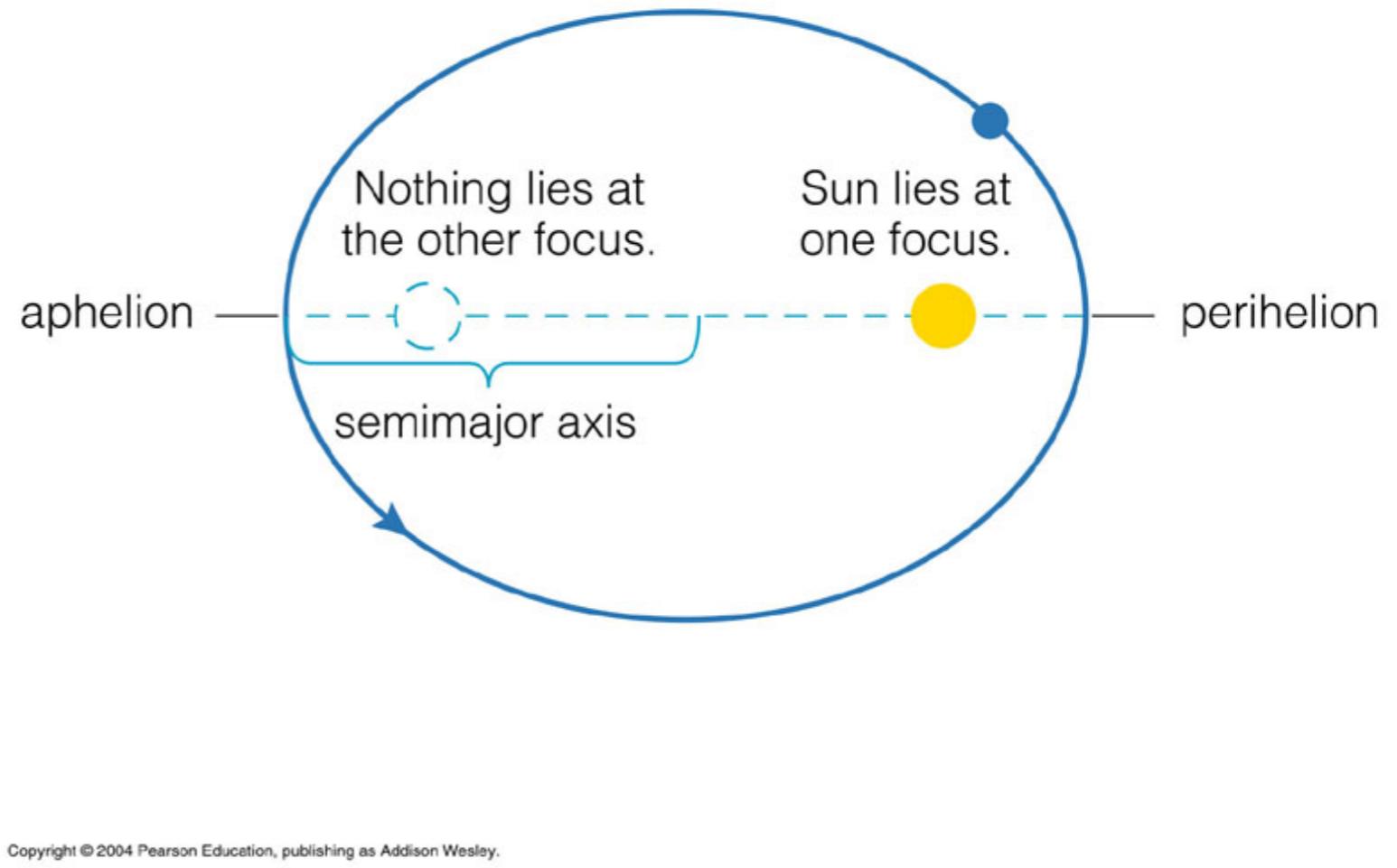
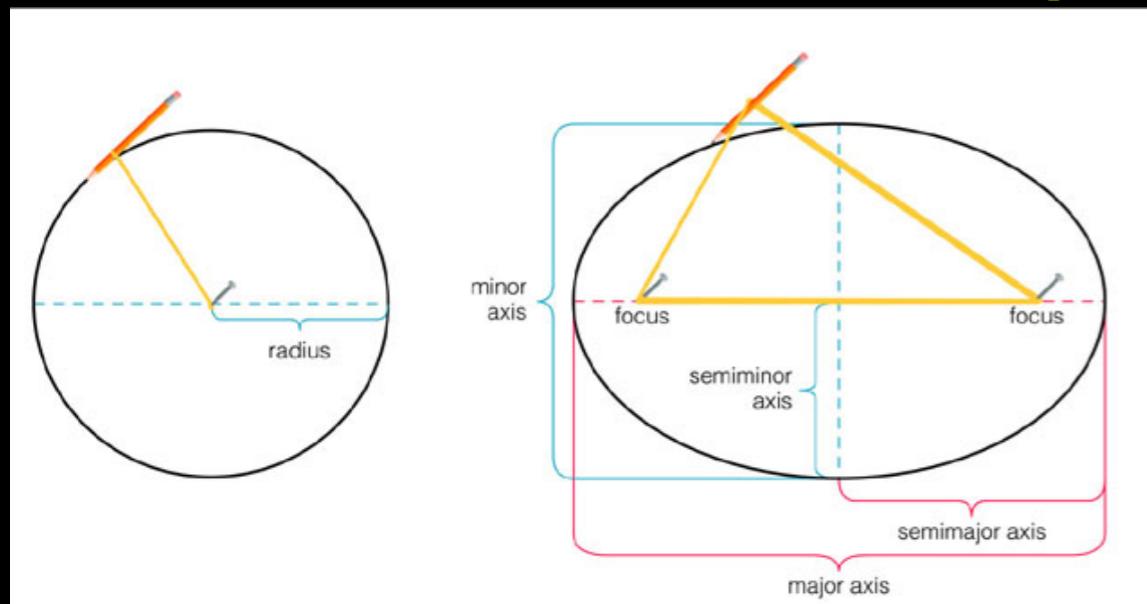
Copernicus, Tycho, Kepler and Galileo  
challenge the Earth-centered model

- Lots of very careful observations of motions of the planets in the Solar system
- Results brought together by Kepler in 3 laws of planetary motion



# Kepler's first law

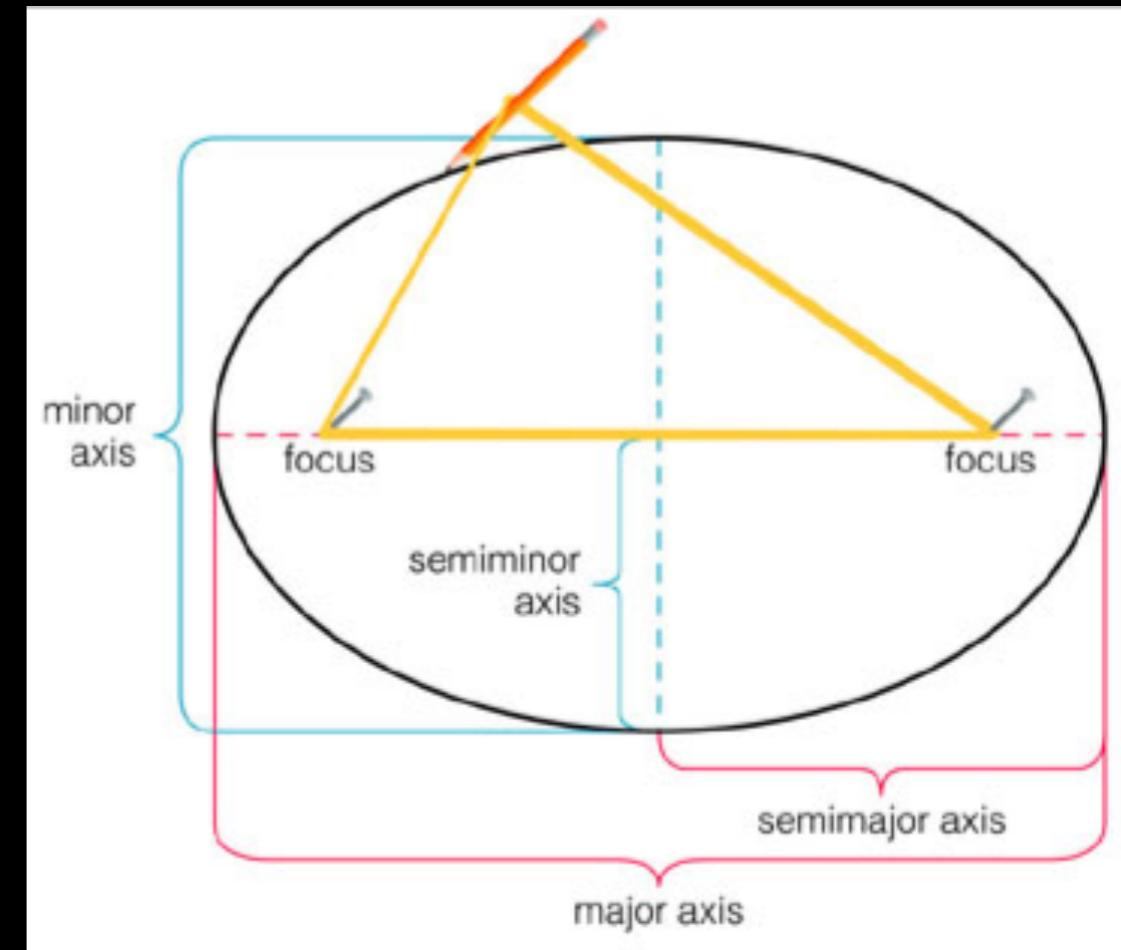
- Orbits are ellipses with Sun at one focus



# Describing ellipses

An ellipse has a center and two foci (focuses)

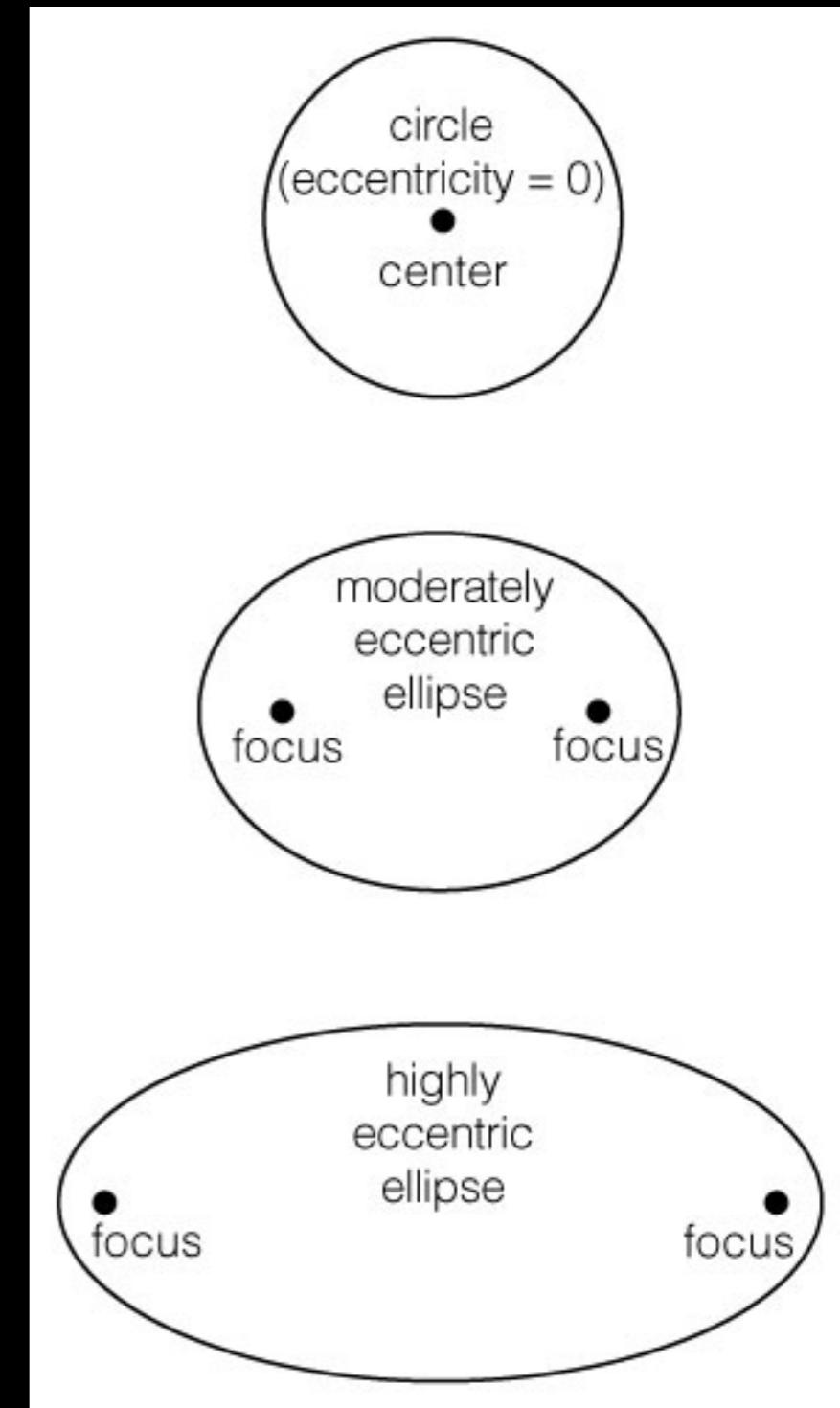
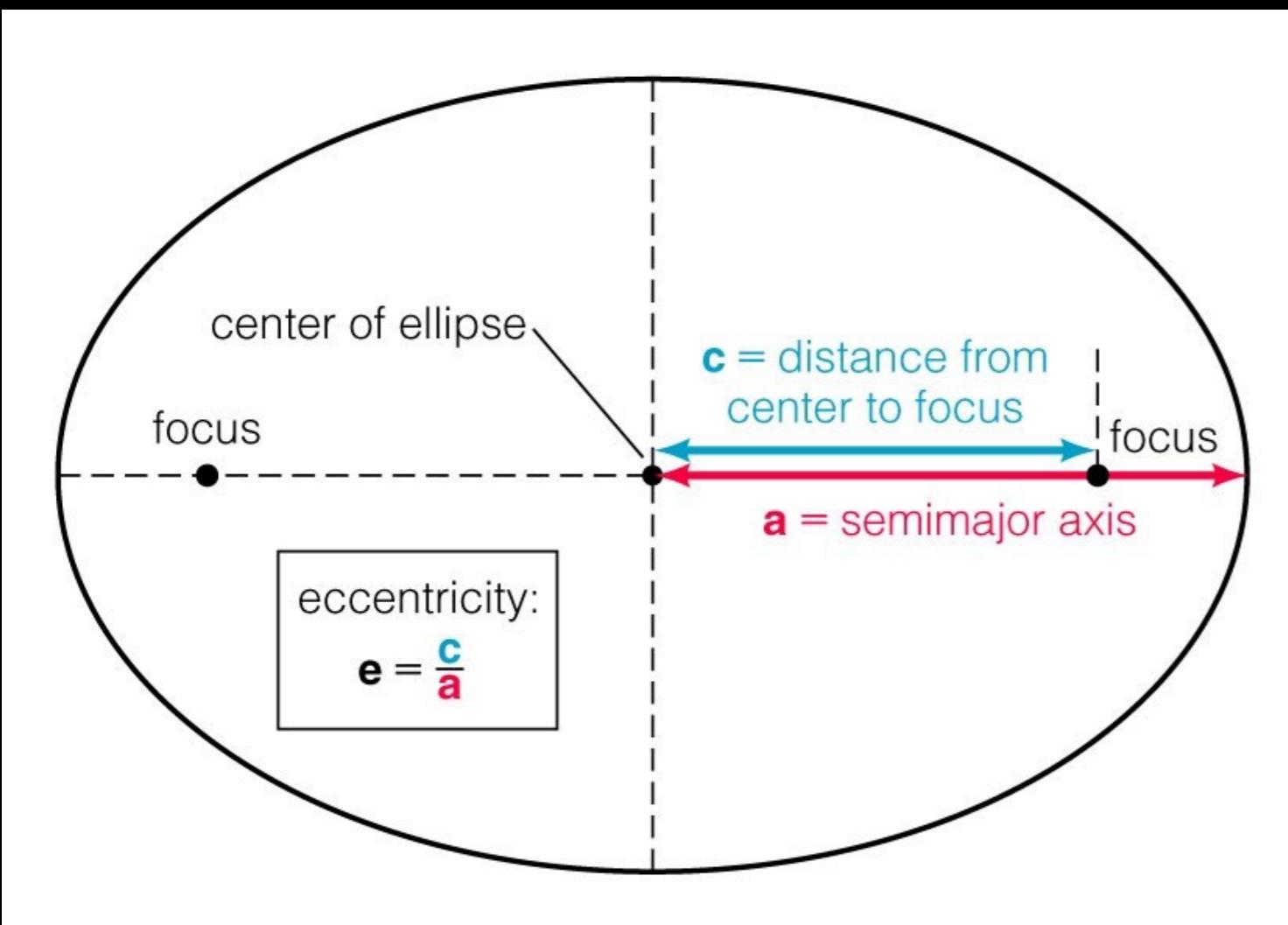
- Major axis: the long axis
  - the axis that goes through the center and the foci
- Minor axis: the short axis
  - perpendicular to the major axis
- Semimajor axis (a):  $1/2$  the length of major axis
- Semiminor axis (b):  $1/2$  the length of minor axis
- How “squished” is an ellipse?
  - Look at axis ratio ( $b/a$ )
  - What is the axis ratio of a circle?
  - Alternatively, look at eccentricity



# Eccentricity

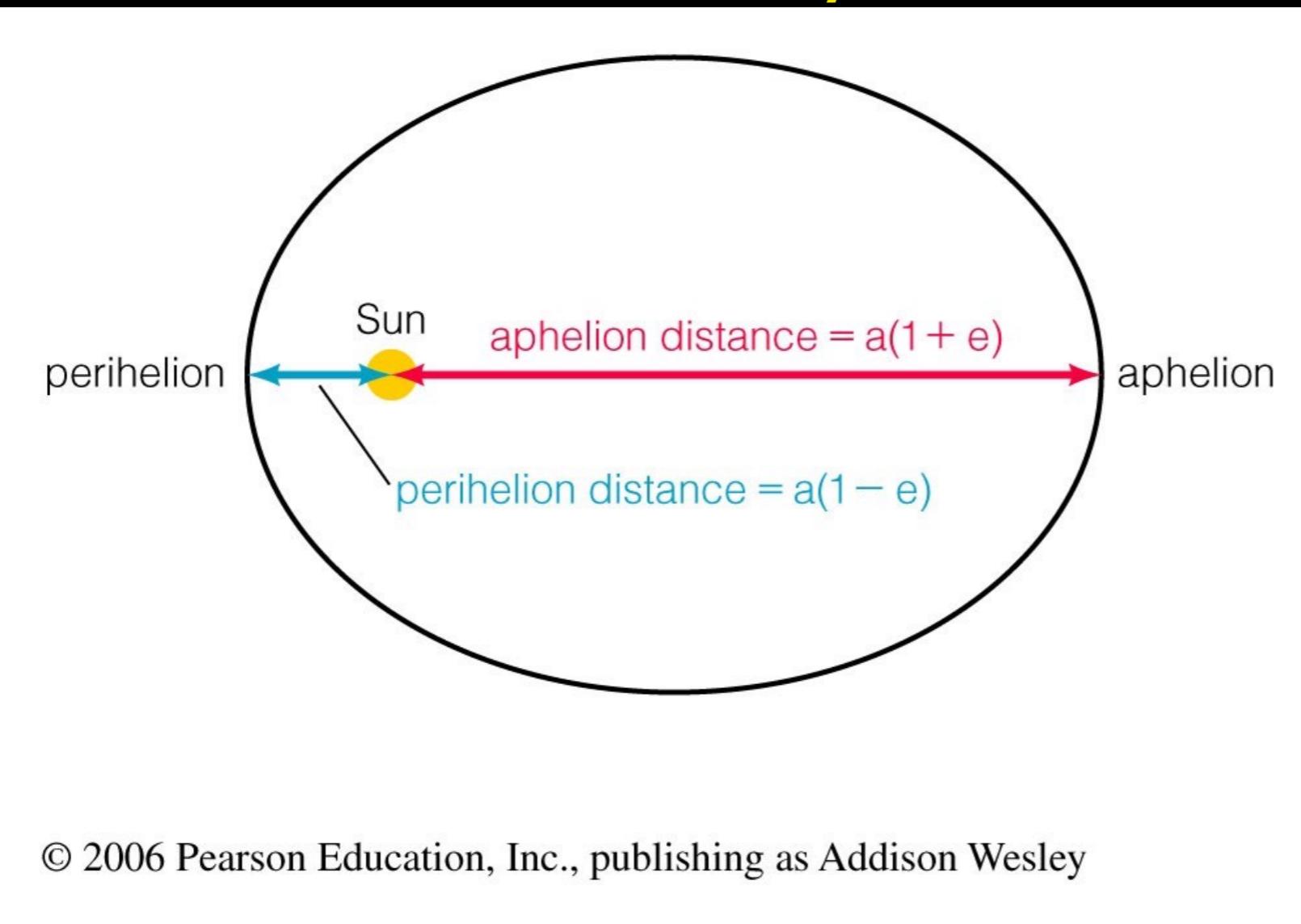
Eccentricity is defined as  $e=c/a$ , where  $c$  is the distance between the center and one of the foci.

- A circle has  $e=0$
- Earth's orbit has  $e=0.017$



# Perihelion and aphelion

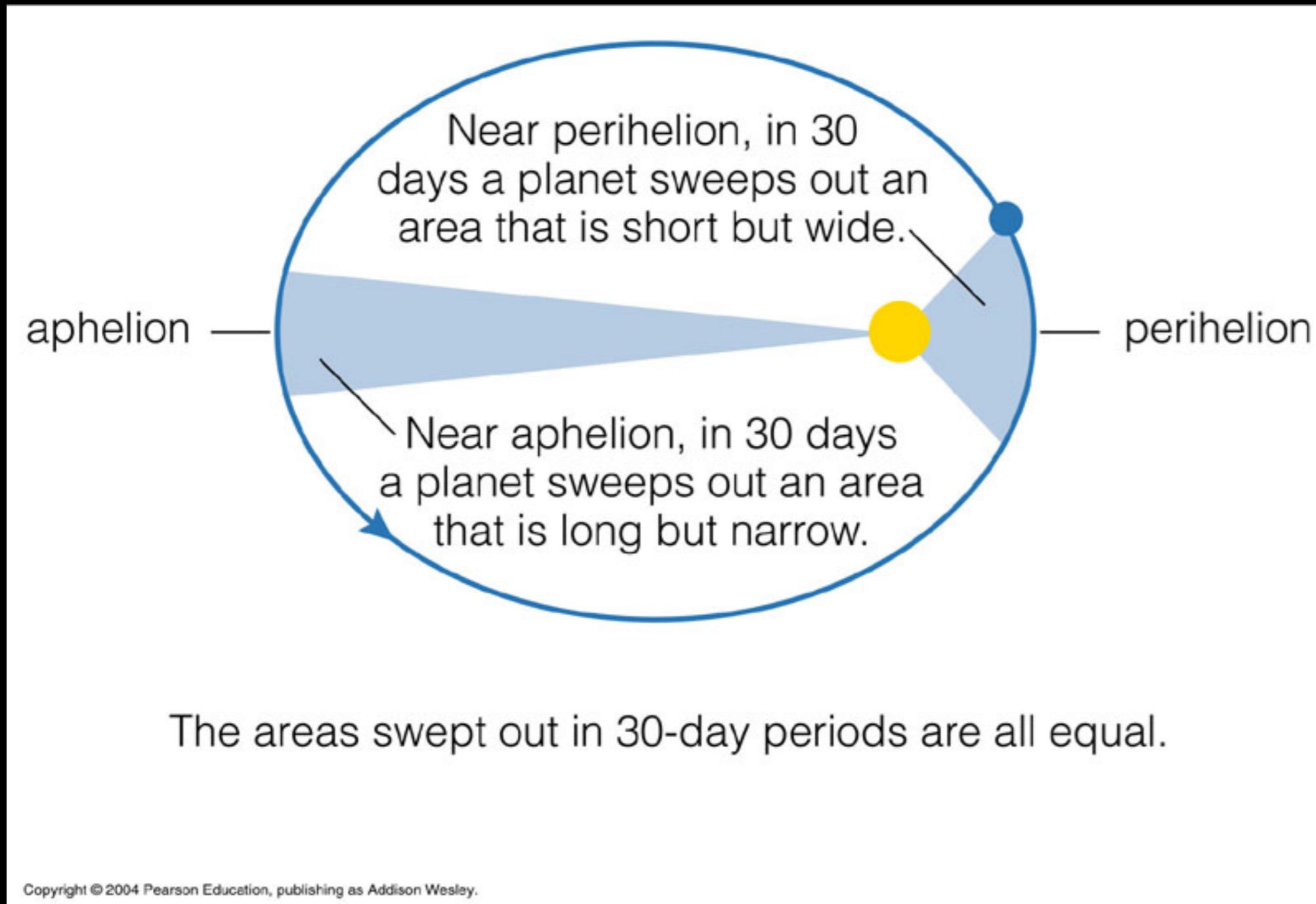
- **Perihelion:** Closest approach to the Sun
- **Aphelion:** Farthest point of the orbit
- You can calculate the perihelion and aphelion distances from the semimajor axis length and the eccentricity



# Kepler's second law

Equal areas in equal times

– (planets move faster when they are closer to the Sun)



# Toward Kepler's third law

- Use careful measurements of:
  - The semimajor axes ( $a$ ) of the planets' orbits
  - The period ( $P$ ) of the planets' orbits  
Period = time it takes to go around the Sun once

# Toward Kepler's third law

- Use careful measurements of:
  - The semimajor axes ( $a$ ) of the planets' orbits
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Period = time it takes to go around the Sun once

- Plot these quantities versus each other

Measure semimajor axes in astronomical units (AU)

1 AU = distance between the Earth and Sun

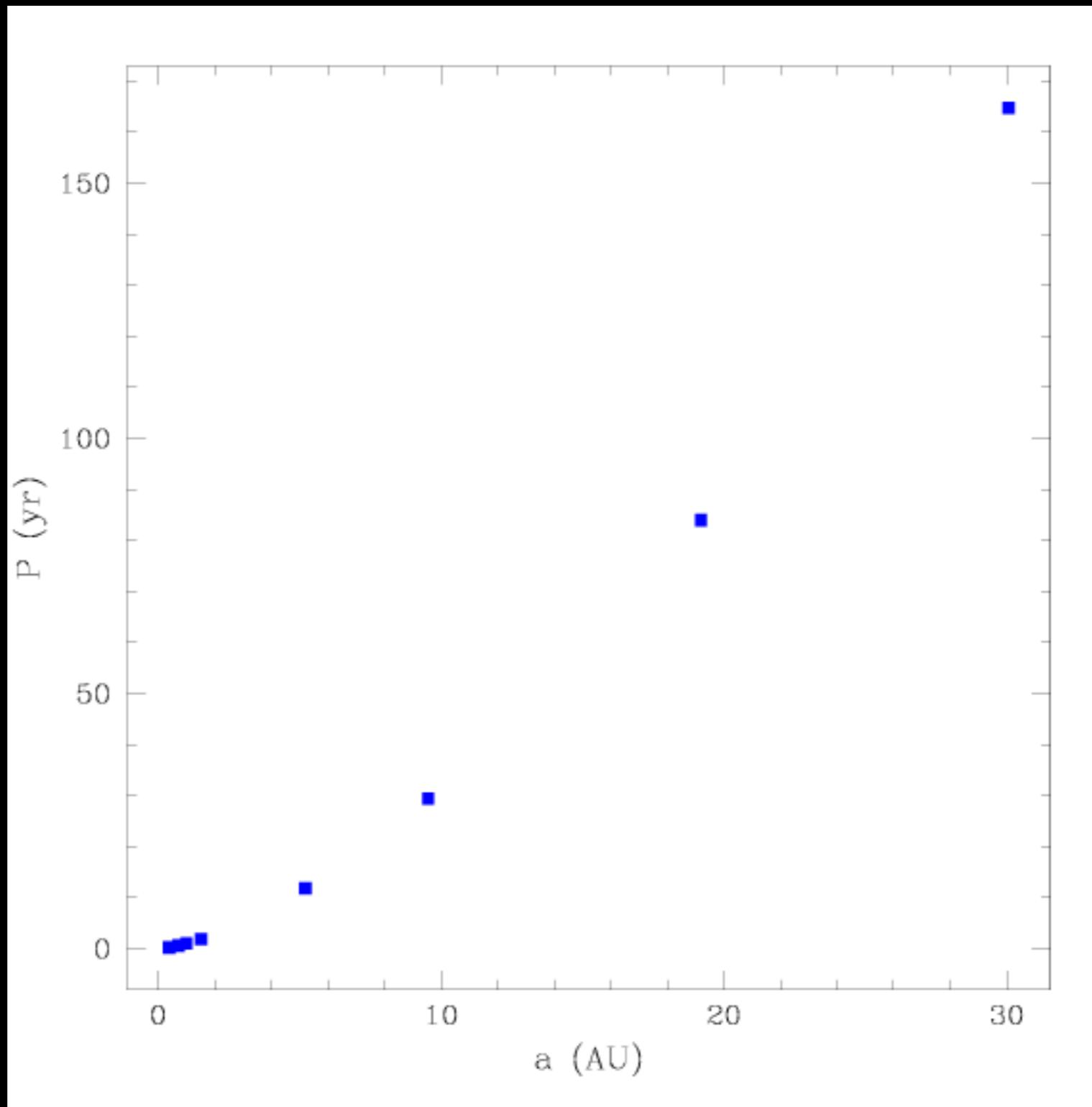
Measure period in years

.

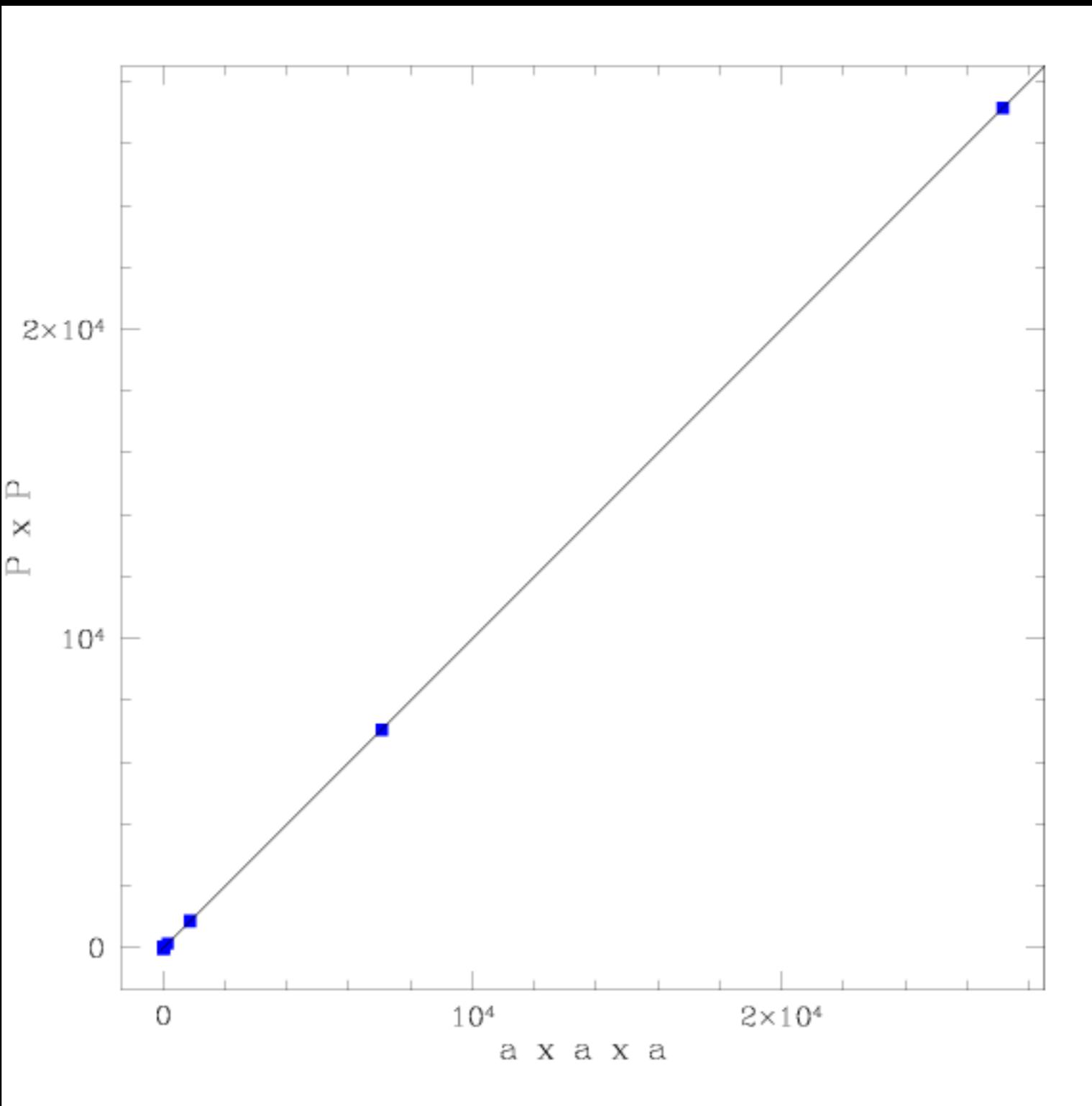
# Toward Kepler's third law

Planet	distance (A.U.)	Period
Mercury	0.387	87.969 d
Venus	0.723	224.701 d
Earth	1.000	365.256 d
Mars	1.524	686.98 d
Jupiter	5.203	11.862 y
Saturn	9.537	29.457 y
Uranus	19.191	84.011 y
Neptune	30.069	164.79 y

# Toward Kepler's third law



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- A clear relation between semimajor axis of ellipse (a) and the period of the orbit (P)

$$P^2 = a^3$$

P measured in years  
a measured in AU

- Period: time it takes planet to go around once
- This relationship could be defined even without knowing what the actual distances were
  - use ratios instead
  - defined a new unit: the Astronomical Unit (AU)
  - 1 AU = distance between the Sun and the Earth
- This law leads to an understanding of what causes the planets to move - more later...

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- In astronomy that force is usually due to **GRAVITY**

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they do?

1. Newton's Laws and Gravity

# Talk about FORCES we must!

In terms of physics, a force is a push or a pull that affects the motion of an object.

Newton's laws relate forces and the resulting motions, in terms of accelerations (changes of speed or direction)



# Newton's 1st Law

- Nature is lazy

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- Nature is lazy
- Or, with better phrasing:
  - “An object at rest tends to stay at rest”  
And
  - “An object in motion keeps the same speed and direction”

**UNLESS A NET FORCE ACTS UPON IT**

- “Net force” means that the forces on the object do not cancel out
- In other words: no net force **means** no acceleration

# FORCES

speed changes  
or  
direction changes



There must be a net  
force acting on the  
object

Both speed and  
direction are  
constant



All the forces are in  
balance

# Newton's 2<sup>nd</sup> Law of Motion:

If you apply a net force to an object, the amount of acceleration is directly proportional to the size of the force



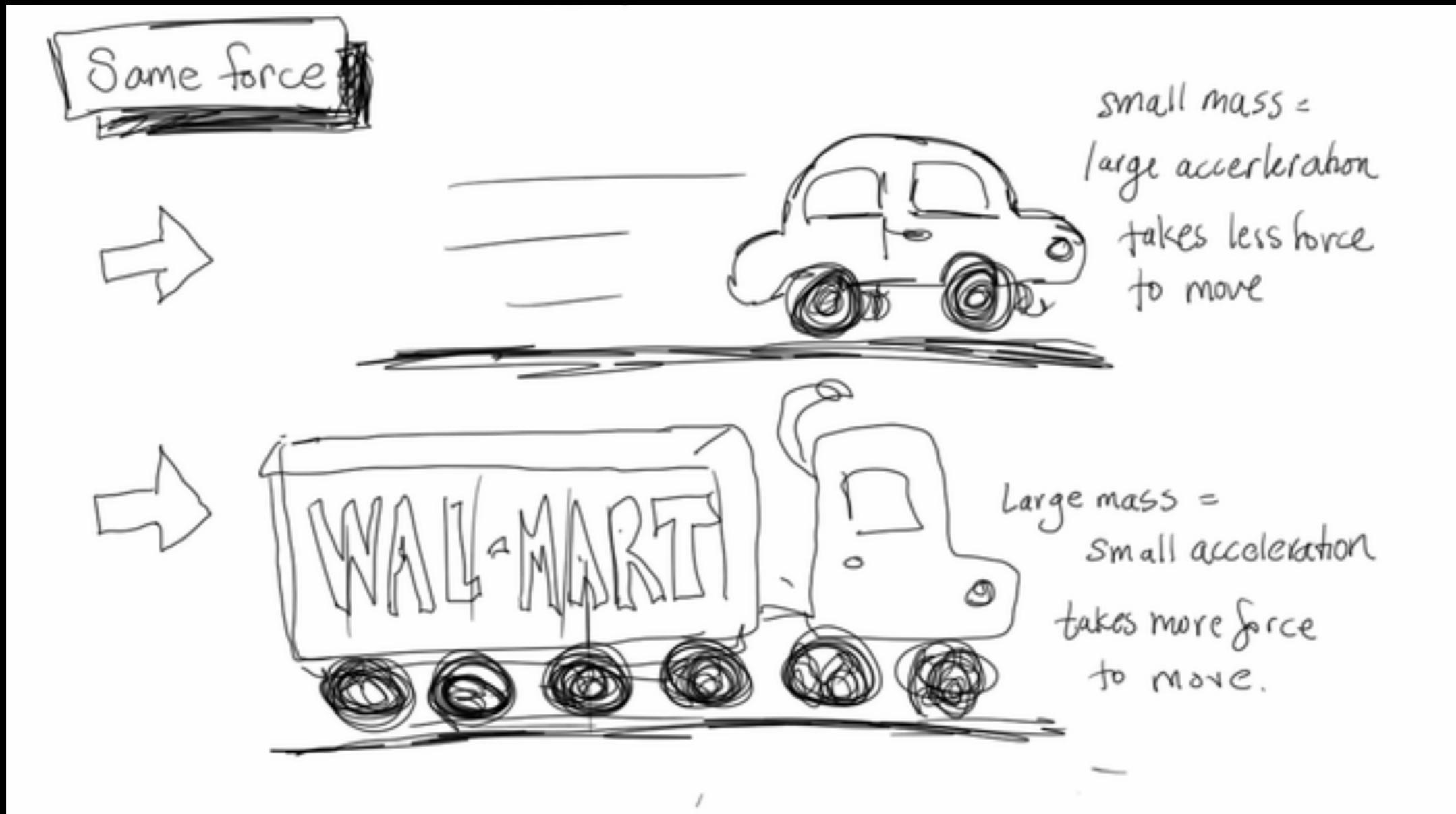
**Force = mass X acceleration**

Or in shorthand

$$F = m a$$

$$F=ma \text{ --or-- } a=F/m$$

Massive things are harder to accelerate



# A Thought Experiment

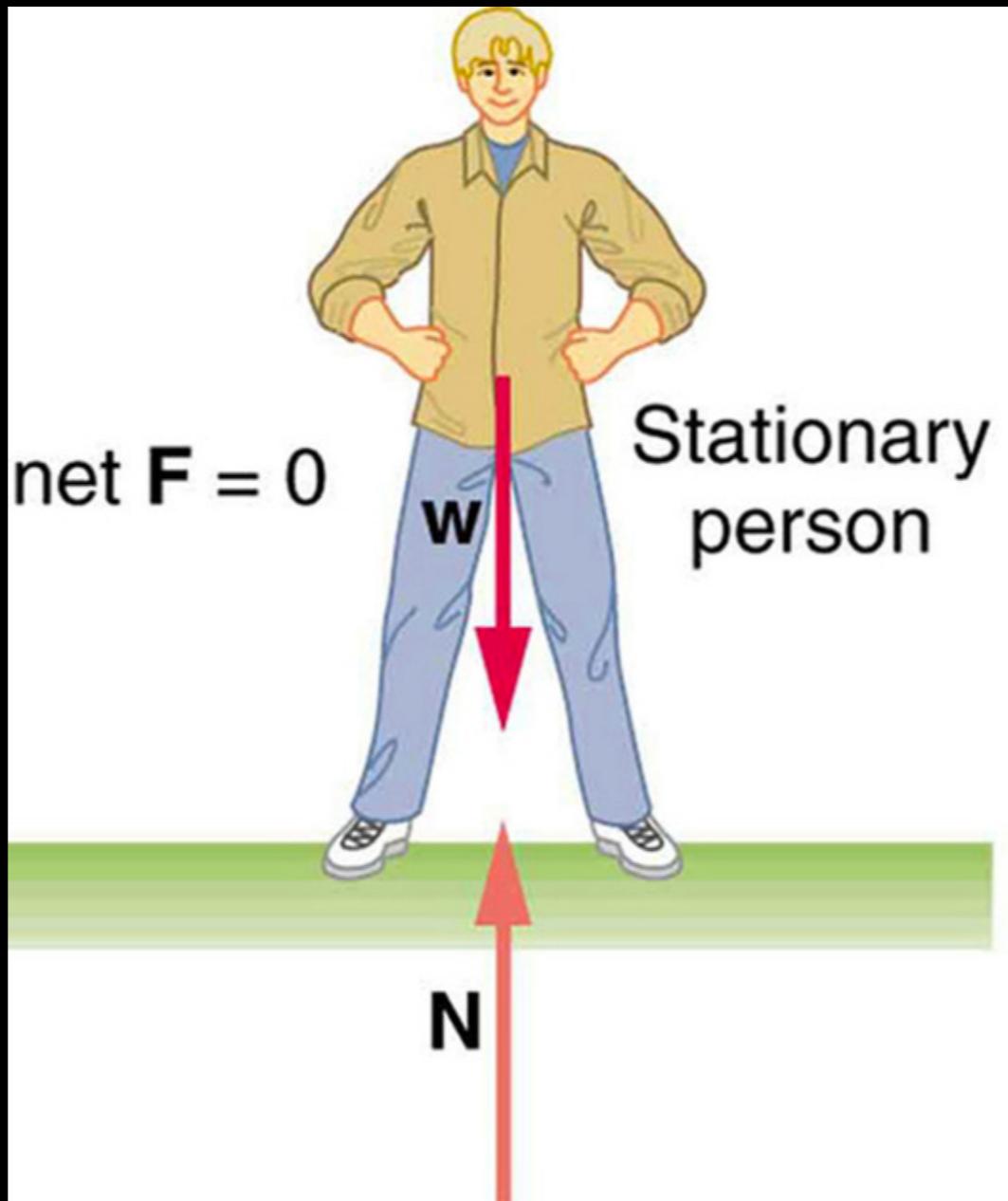
What are the forces acting on:

- Me?

# A Thought Experiment

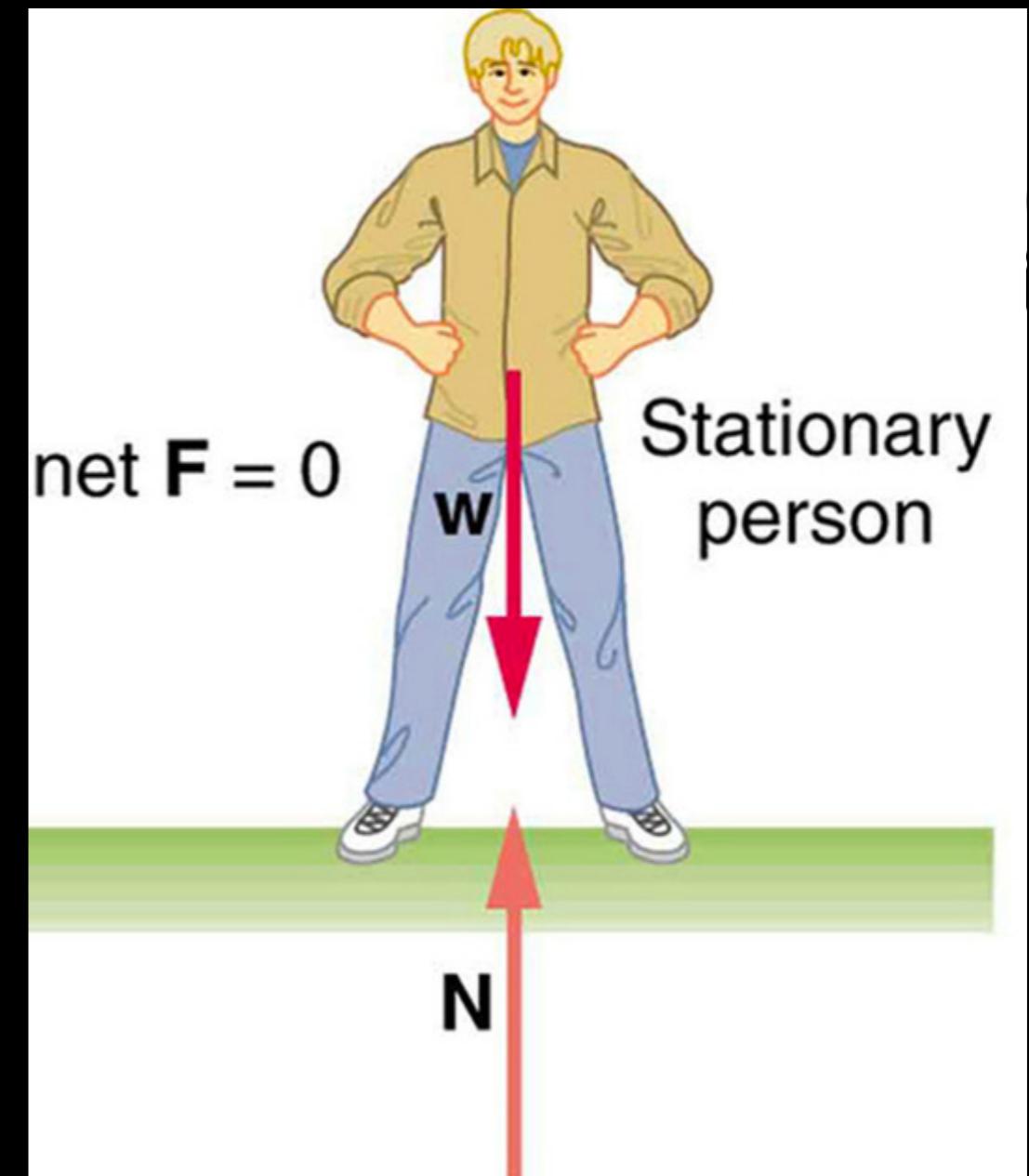
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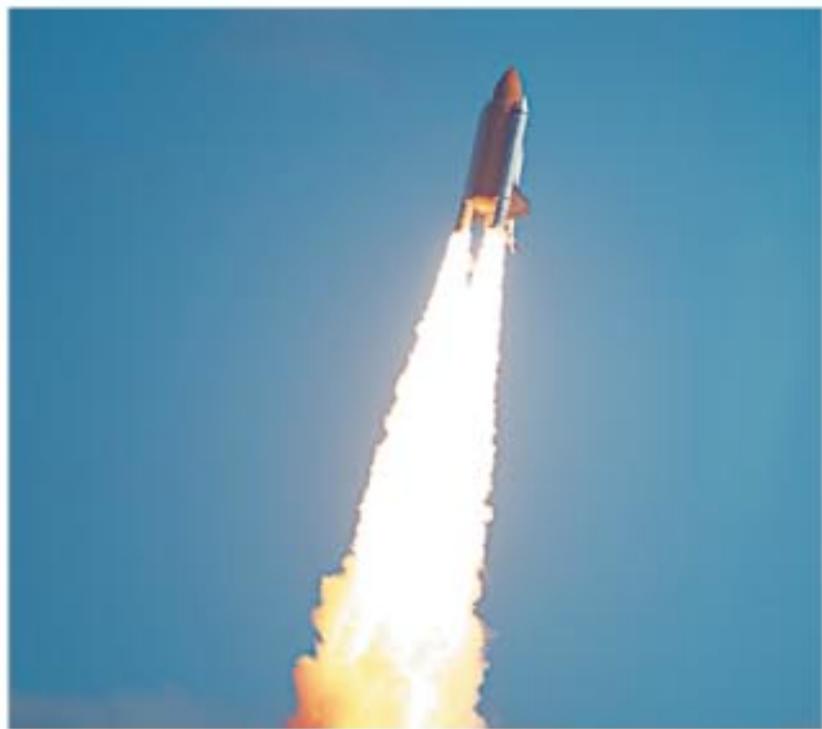
# Newton's 3<sup>rd</sup>:

*For any force there is always an equal and opposite reaction force.*

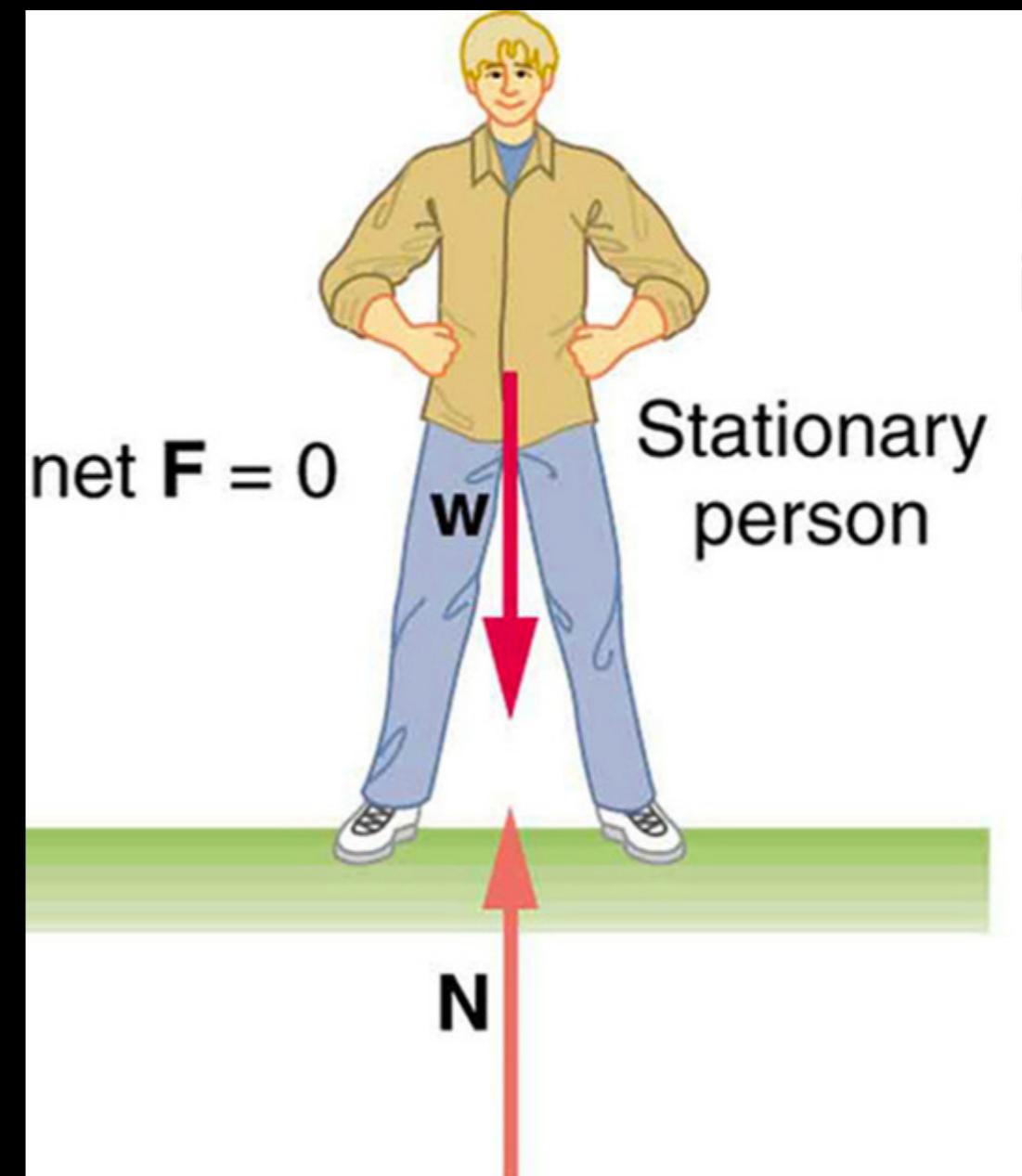


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**Example:** A rocket is propelled upward by a force equal and opposite to the force with which gas is expelled out its back.

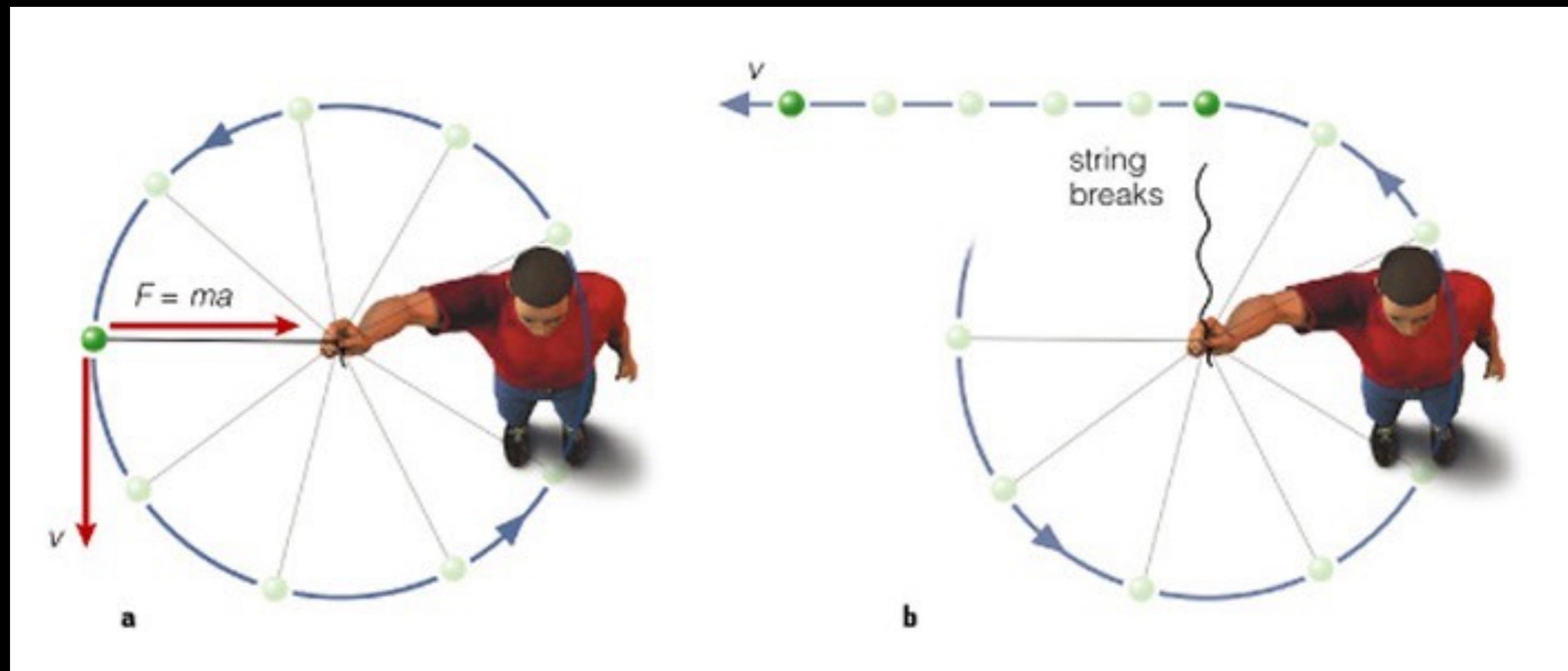


# A Thought Experiment

What are the forces acting on:

- Me?
- A ball on a string, swung in a circle?

There are “central forces” acting on objects moving in circles (or other curved paths)

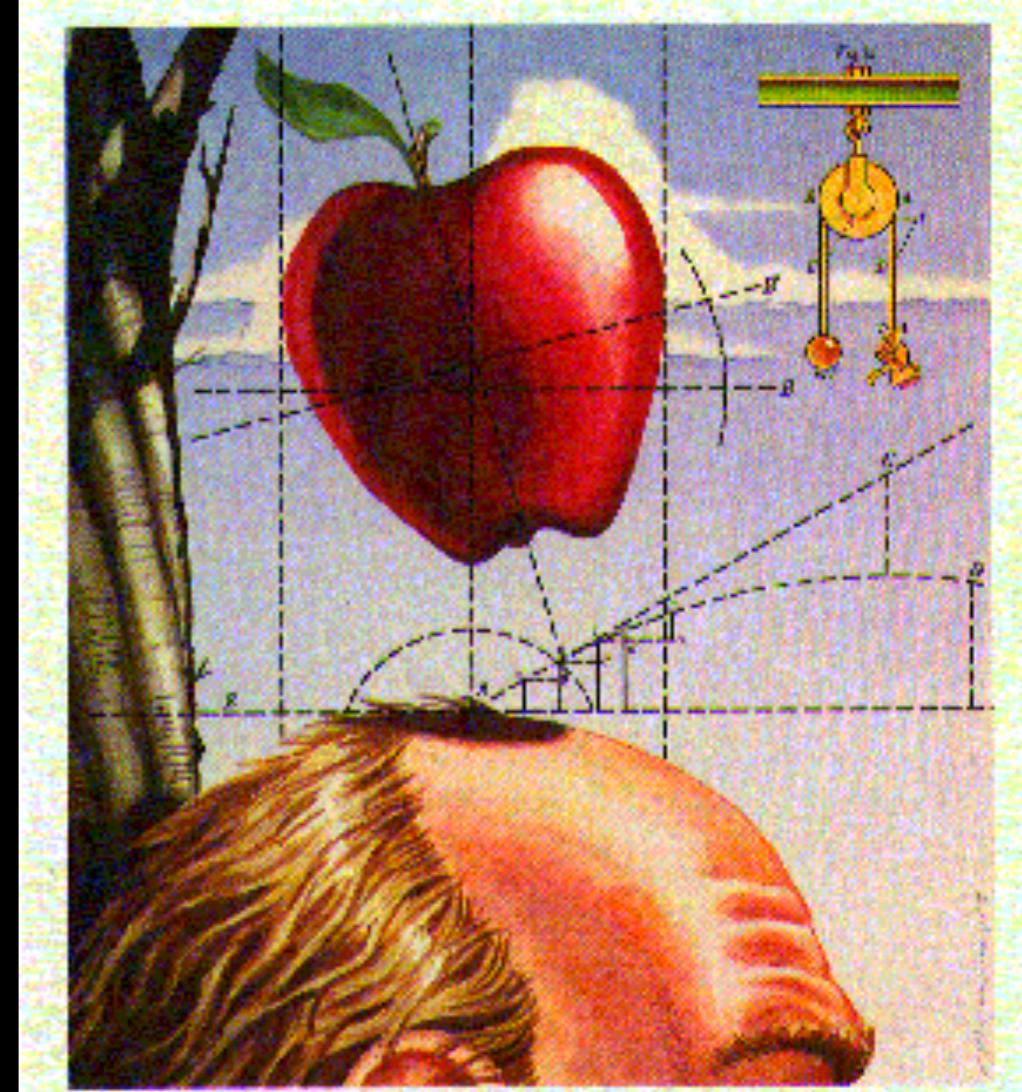


# Many things in astronomy travel on approximately circular paths

- Moons around planets
- Planets around stars
- Stars around the center of galaxies
- A change of direction means an acceleration means that a net force is being applied

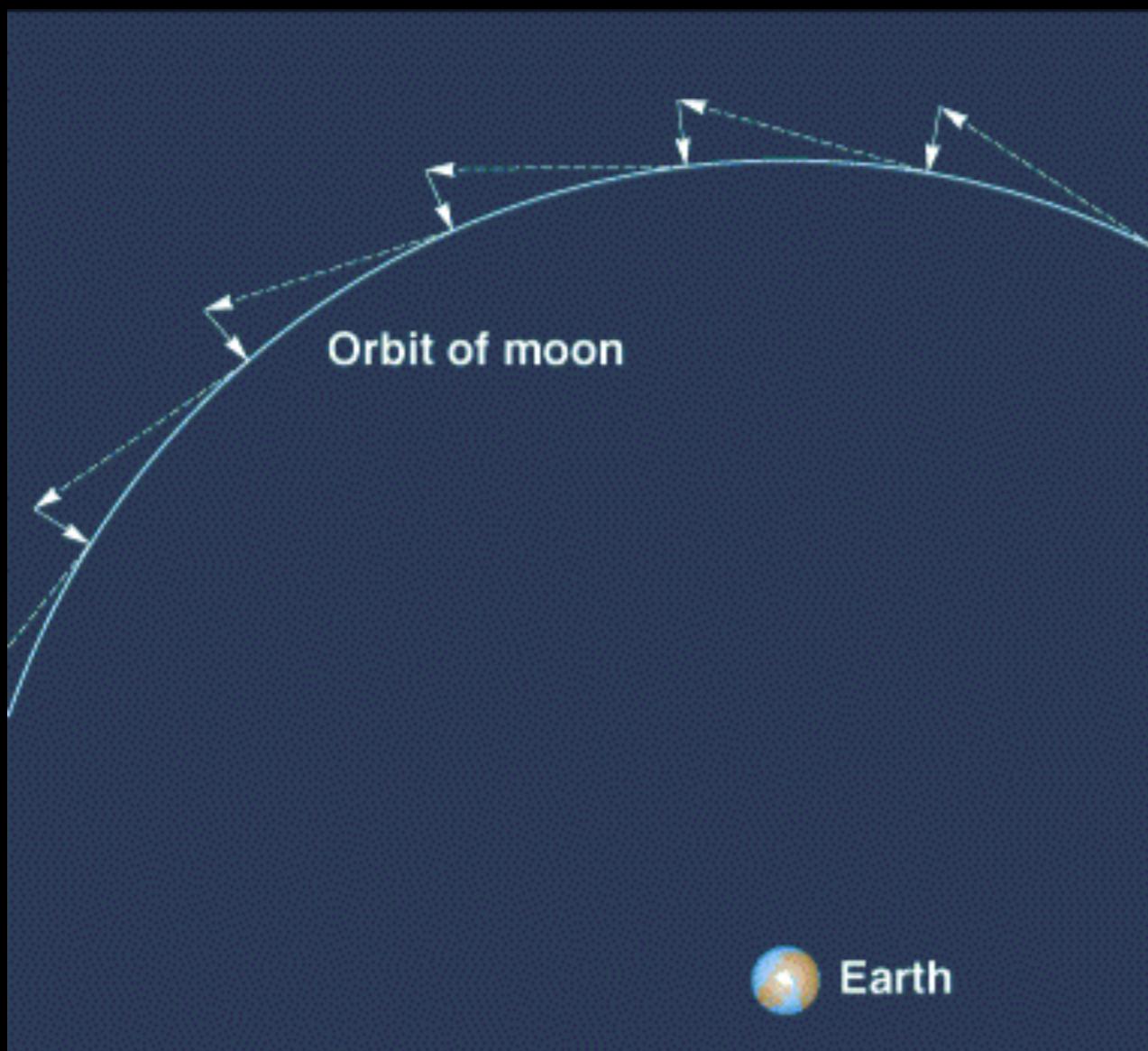
Elliptical orbits imply that there is some central force keeping the moon/planet/star from going in a straight line

# GRAVITY



**Gravity.  
It isn't just a good idea.  
It's the law.**

# Why does gravity lead to roughly circular orbits?



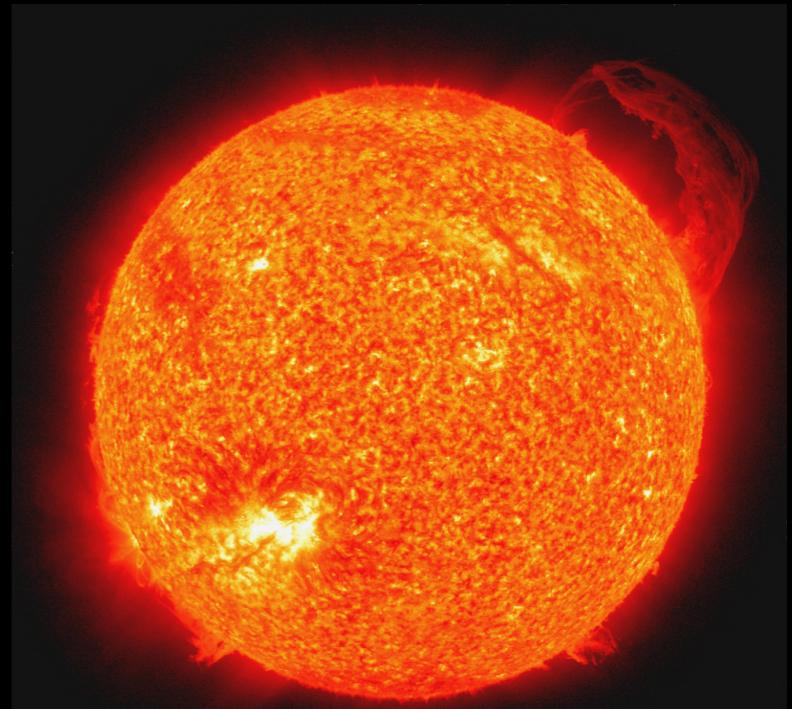
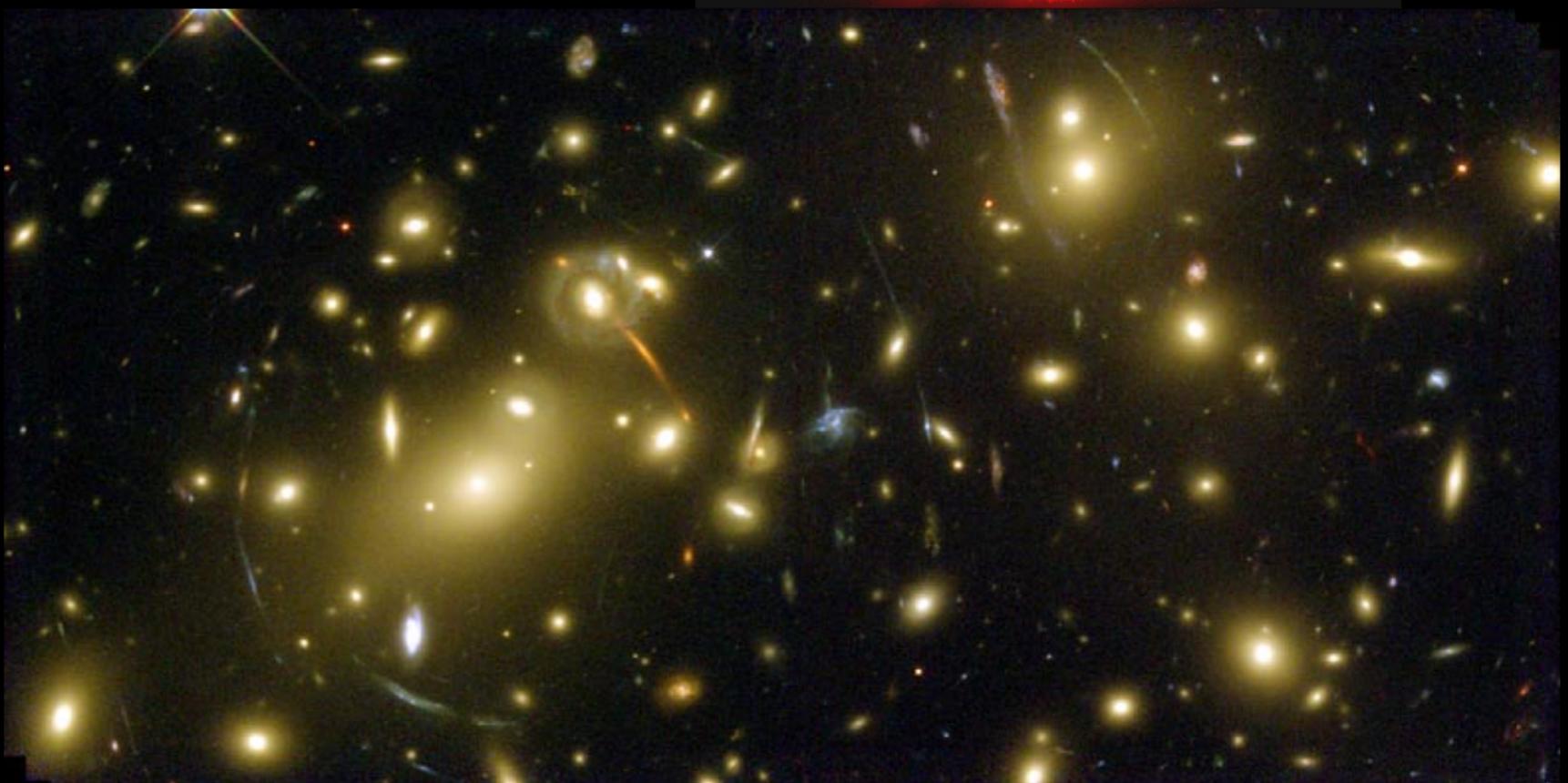
The Moon tries to travel in a straight path (Newton's 1<sup>st</sup> Law), but the gravitational pull of the Earth keeps tugging it back onto a circular path (Newton's 2<sup>nd</sup> Law).

So the Moon is constantly **FALLING** toward the Earth  
It's the same for the Earth around the Sun, or the Sun around the center of the Galaxy.

# Gravity also keeps astronomical objects bound together



© Caltech/David Malin



Nature has **FOUR** fundamental forces...

- 1. Gravity**
- 2. Electromagnetic**
- 3. Strong**
- 4. Weak**

# Gravity is the one that matters most for astronomy!

(Even though it is the weakest of the four)

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## BUT IN CONTRAST

- Gravity operates over any range, and affects anything with mass.

# Nature has FOUR fundamental forces...

	relative strength	Range (m)
<b>1. Gravity</b>	1	$\infty$
<b>2. Electromagnetic</b>	$10^{36}$	$\infty$
<b>3. Strong</b>	$10^{38}$	$\sim 10^{-12}$
<b>4. Weak</b>	$10^{25}$	$\sim 10^{-12}$

