

MATH5004 TUTORIAL 2

Finite Difference Method

Exercise 1. Consider a Two-point BVP:

$$\begin{aligned} u_{xx} &= f(x), & x &\in (0,1) \\ u(0) &= 1, & u(1) &= -1, \end{aligned}$$

where $f(x) = -\pi^2 \cos(\pi x)$.

Exercise 2. Solve

$$\begin{aligned} \frac{\partial u}{\partial t} &= \frac{1}{10} \frac{\partial^2 u}{\partial x^2}, & (x, t) &\in (0,1) \times (0, \tau) \\ u(x, 0) &= 1, \\ u(0, t) &= 0, & \frac{\partial u}{\partial t}(1, t) &= 0. \end{aligned}$$

Assignment I

Question 1. (TUT-WK2)

Derive Finite Difference Scheme to solve the following steady state heat conduction problem

$$\begin{aligned} k(x) \frac{\partial^2 u}{\partial x^2} &= f(x), & 0 < x < 1 \\ u(0) &= 1, & \frac{\partial}{\partial x} u(1) &= 0, \end{aligned}$$

where $f(x) = -\cos(\pi x)$, $k = \pi x^2$.

Note: Assignments I & II (50%): Assignment Questions will be given weekly.

In this week, Questions 1 (TUT-WK2) is a part of Assignment I, please submit a document file with MATLAB code via Blackboard by the due date of Assignment I on Friday 11 September 2020

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