

# Project 6

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Section 1

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**1 Let  $L = \{a^n b^m c^{2n+m} \mid n, m \geq 0\}$ . Construct a context-free grammar,  $G$ , that generates  $L$ .**

Our context free grammar,  $G$ , that generates  $L$ , starts with string  $S$ :

$$S \Rightarrow AB$$

$$A \Rightarrow aABCC \mid aACC \mid \lambda$$

$$B \Rightarrow bBC \mid \lambda$$

$$C \Rightarrow cC \mid \lambda$$

## 2

### 2.1 State the rules for Chomsky Normal Form (CNF).

A CFG is in CNF if every rule is of the form:

$$A \Rightarrow BC$$

$$A \Rightarrow a$$

$$S \Rightarrow \lambda$$

Where:

$$a \in \Sigma$$

$$A, B, C \in V$$

$S$  is the start variable

### 2.2 Convert the following grammar to CNF.

$$S \Rightarrow aA|ABA$$

$$A \Rightarrow AA|a$$

$$B \Rightarrow AbA|bb$$

#### 2.2.1 Guarantee Start Variable is only on LHS.

No action needed

#### 2.2.2 Eliminate all rules of $A \Rightarrow \lambda$ where $A \neq S$ .

No action needed

#### 2.2.3 Eliminate all unit rules.

No action needed

#### 2.2.4 Fix remaining rules.

Let  $U_1 \Rightarrow a$  and  $U_2 \Rightarrow b$

$$S \Rightarrow U_1A|ABA$$

$$A \Rightarrow AA|a$$

$$B \Rightarrow AU_2A|bb$$

$$U_1 \Rightarrow a$$

$$U_2 \Rightarrow b$$

Let  $B_1 \Rightarrow BA$  and  $B_2 \Rightarrow U_2A$

$$S \Rightarrow U_1A|AB_1$$

$$A \Rightarrow AA|a$$

$$B \Rightarrow AB_2|U_2U_2$$

$$B_1 \Rightarrow BA$$

$$B_2 \Rightarrow U_2A$$

$$U_1 \Rightarrow a$$

$$U_2 \Rightarrow b$$

This grammar is now in Chomsky Normal Form.

**3 Using Example 2.14, show that the machine, M1 in Figure 2.15 recognizes 0011.**

Input String	Stack Content	Rule	Description
$\epsilon$	\$	$\epsilon, \epsilon \Rightarrow \$$	Input $\epsilon$ , pop $\epsilon$ from stack, push \$.
0	0\$	$0, \epsilon \Rightarrow 0$	Input 0, pop $\epsilon$ from stack, push 0.
0	00\$	$0, \epsilon \Rightarrow 0$	Input 0, pop $\epsilon$ from stack, push 0.
1	0\$	$1, 0 \Rightarrow \epsilon$	Input 1, pop 0 from stack, push $\epsilon$ .
1	\$	$1, 0 \Rightarrow \epsilon$	Input 1, pop 0 from stack, push $\epsilon$ .
$\epsilon$		$\epsilon, \$ \Rightarrow \epsilon$	Input 1, pop \$ from stack, push $\epsilon$ .