# Project 6

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1 Let  $L = \{a^nb^mc^{2n+m}|n,m \geq 0\}$ . Construct a context-free grammar, G, that generates L.

Our context free grammar, G, that generates L, starts with string S:

$$\begin{split} S &\Rightarrow AB \\ A &\Rightarrow aABCC|aACC|\lambda \\ B &\Rightarrow bBC|\lambda \\ C &\Rightarrow cC|\lambda \end{split}$$

# 2.1 State the rules for Chomsky Normal Form (CNF).

A CFG is in CNF if every rule is of the form:

$$A \Rightarrow BC$$

$$A \Rightarrow a$$

$$S \Rightarrow \lambda$$

Where:

$$a \in \Sigma$$

$$A, B, C \in V$$

S is the start variable

## 2.2 Convert the following grammar to CNF.

$$S \Rightarrow aA|ABA$$

$$A \Rightarrow AA|a$$

$$B \Rightarrow AbA|bb$$

#### 2.2.1 Guarantee Start Variable is only on LHS.

No action needed

### **2.2.2** Eliminate all rules of $A \Rightarrow \lambda$ where $A \neq S$ .

No action needed

#### 2.2.3 Eliminate all unit rules.

No action needed

#### 2.2.4 Fix remaining rules.

Let  $U_1 \Rightarrow a$  and  $U_2 \Rightarrow b$ 

$$S \Rightarrow U_1 A | ABA$$

$$A \Rightarrow AA|a$$

$$B \Rightarrow AU_2A|bb$$

$$U_1 \Rightarrow a$$

$$U_2 \Rightarrow b$$

Let  $B_1 \Rightarrow BA$  and  $B_2 \Rightarrow U_2A$ 

$$S \Rightarrow U_1 A | AB_1$$

$$A \Rightarrow AA | a$$

$$B \Rightarrow AB_2 | U_2 U_2$$

$$B_1 \Rightarrow BA$$

$$B_2 \Rightarrow U_2 A$$

$$U_1 \Rightarrow a$$

$$U_2 \Rightarrow b$$

This grammar is now in Chomsky Normal Form.

# 3 Using Example 2.14, show that the machine, M1 in Figure 2.15 recognizes 0011.

Input String	Stack Content	Rule	Description
$\epsilon$	\$	$\epsilon, \epsilon \Rightarrow \$$	Input $\epsilon$ , pop $\epsilon$ from stack, push \$.
0	0\$	$0, \epsilon \Rightarrow 0$	Input 0, pop $\epsilon$ from stack, push 0.
0	00\$	$0, \epsilon \Rightarrow 0$	Input 0, pop $\epsilon$ from stack, push 0.
1	0\$	$1,0\Rightarrow\epsilon$	Input 1, pop 0 from stack, push $\epsilon$ .
1	\$	$1,0\Rightarrow\epsilon$	Input 1, pop 0 from stack, push $\epsilon$ .
$\epsilon$		$\epsilon, \$ \Rightarrow \epsilon$	Input 1, pop \$ from stack, push $\epsilon$ .