# Topic 2D: Choice over Time An Alternative Model: Present Bias

EC 404: Behavioral Economics Professor: Ben Bushong

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#### Motivation

Exponential discounting implies constant discounting:

$$\frac{D(0)}{D(1)} = \frac{D(1)}{D(2)} = \frac{D(2)}{D(3)} = \dots = \frac{1}{\delta}.$$

But the evidence suggests more discounting in the short run than in the long run:

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#### A simplified model: " $\beta$ , $\delta$ preferences" or "present bias"

Period-t intertemporal utility is

$$U^t = u_t + \beta * \sum_{x=1}^{T-t} \delta^x u_{t+x}.$$

In other words, the discount function is:

$$D(x) = \begin{cases} 1 & \text{if } x = 0\\ \beta * \delta^x & \text{if } x > 0. \end{cases}$$

Hence, under  $\beta, \delta$  preferences

$$\frac{D(0)}{D(1)} = \frac{1}{\beta \delta} > \frac{1}{\delta} = \frac{D(1)}{D(2)} = \frac{D(2)}{D(3)} = \dots$$

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 $\beta,\delta$  preferences capture in the simplest way possible that a person has a time-inconsistent preference for immediate gratification.

- present bias (present-biased preferences)
- hyperbolic discounting
- quasi-hyperbolic discounting
- preference for immediate gratification
- self-control problems

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Suppose there is a task that you must complete on one of the next three days. To complete this task, you incur costs as follows:

- ▶ If you complete the task in period 1, the cost is 3.
- ▶ If you complete the task in period 2, the cost is 5.
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Your preferences from a period-1 perspective are:

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Conditional on not doing it in period 1, your preferences from a period-2 perspective are:

- ▶ If complete the task in period 2, your utility is
- ▶ If complete the task in period 3, your utility is

To summarize, your period-1 preferences are

$$(period 2) \succ (period 1) \succ (period 3)$$

while your period-2 preferences are

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Note the time inconsistency:

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An important issue: Are you aware of your future self-control problems (of your future present bias)?

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Suppose you are **fully aware** of future self-control problems — that is, you correctly predict your period-2 preferences.

- ▶ If so, you correctly predict that if you wait now, then in period 2 you'll prefer to wait again.
- ▶ Hence, you compare completing the task now to completing the task in period 3, and you prefer the former.

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- Hence, you wait in period 1 planning to complete the task in period 2.
- Of course, when period 2 arrives, you'll change your mind and decide to wait.

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- Sophisticates are <u>fully aware</u> of their future self-control problems and thus correctly predict future behavior.
- Naifs are <u>fully unaware</u> of their future self-control problems and thus expect to behave in future exactly as they currently would like themselves to behave in future.

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#### To solve for naifs:

- ► Each period, derive the optimal lifetime path, and follow this period's component. But when next period arrives, reassess this plan.
- Note: Naifs may not stick to their plans.

- ► Treat each period-self as a separate agent, and solve for the subgame-perfect Nash equilibrium to the game played between these agents (use backward induction start at the end, and work backward).
- ▶ Note: Sophisticates always stick to their plans
- ▶ ... they just never plan to do something they won't later carry out.

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Suppose there is no reward, that you value costs linearly, and that you have  $\beta=1/2$  and  $\delta=1.$ 

From a prior perspective, the best time is

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Suppose there is no reward, that you value costs linearly, and that you have  $\beta=1/2$  and  $\delta=1.$ 

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- ► For an onerous task that involves immediate costs, a preference for immediate gratification implies a tendency to procrastinate to delay beyond the best time.
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Doing It Now or Later: The Simple Example

### Fibonacci's Fine Arts Cinema

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Note that even given  $\beta=\frac{1}{2},$  all four selves agree that missing Vin Diesel is a bad thing to happen. Yet the naif does so.

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Aside: Let us see what we would infer from the observed behavior if we were an anachronistic economist who believed in  $\beta=1$ .

An exponential discounter would have to have a *weekly* discount factor  $\widetilde{\delta} \leq Min[\sqrt[3]{\frac{3}{13}}, \sqrt[2]{\frac{5}{13}}, \frac{8}{13}] \approx .61$  to be willing to miss F&F.

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And if we observed somebody missing the 52nd week (Fast and Furious marathon?) at the Fibonacci's Fine Arts Cinema with utilities (3,5,8,13,21,34,55...)

Lesson: Some behavior looks more (absurdly) impatient if (mis)interpreted through the lens of exponential discounting

▶ But less so through the lens of present-biased discounting.

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- $\blacktriangleright$  (3,0,0,0) or (0,5,0,0) or (0,0,8,0) or (0,0,0,13).

What will the sophisticate do?

- ▶ Because  $8 > \frac{1}{2}(13)$ , if she has not seen it yet, the sophisticate will see the movie in Week 3.
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### Example 1

Suppose there is a task that you must complete on one of the next four days. To complete this task, you incur costs as follows:

- ▶ If you complete the task in period 1, the cost is 3.
- ▶ If you complete the task in period 2, the cost is 5.
- ▶ If you complete the task in period 3, the cost is 8.
- ▶ If you complete the task in period 4, the cost is 13.

Suppose there is no reward, that you value costs linearly, and that you have  $\beta=1/2$  and  $\delta=1$ .

From a prior perspective, the best time is period 1.

Naifs complete the task in period 4.

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Our welfare criterion: A person's "long-run utility" — which reflects how she feels from a prior perspective — is given by

$$U^0 = \sum_{\tau=1}^T \delta^{\tau} u_{\tau}.$$

In Example 1:

Long-run utility from best option (do it in period 1) is -3. Long-run utility for sophisticates (who do it in period 2) is -5Long-run utility for naifs (who do it in period 4) is -13.

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Welfare loss for sophisticates is 2. Welfare loss for naifs is 10.

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In this simple "do-it-once" environment, for pleasurable tasks, sophisticates can suffer large harm, naifs cannot.

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# Welfare Implications

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In this simple "do-it-once" environment, for pleasurable tasks, sophisticates can suffer large harm, naifs cannot.

In richer, real-world environments, sophistication is most likely better than naivete, because sophisticates will make use of commitment devices to overcome their self-control problems.

# Procrastination: Doing It ... Tomorrow

- ► Procrastination involves the "immediate gratification" of not doing something optimally onerous
- ▶ Often the main "cost" of doing some beneficial task is primarily the opportunity cost of doing something gratifying.
- Procrastination is in fact a wonderful vice: You can, and ideally
   should do it concurrently with other vices!
- ▶ Note: quitting smoking, etc. qualitatively similar to procrastination.

#### But what is it?

- ▶ Not just delaying unpleasant tasks, which is often right thing to do.
- ▶ It is delaying beyond when you yourself want to complete them.

Important example of unpleasant task we procrastinate on: learning.

- ► Learning how to do something better is pervasive example of something with long-term benefits.
- ▶ Many people recognize the enormous benefits of financial planning and literacy. And so want to do so. And plan to do so.

... tomorrow.

# Procrastination Example

Suppose that, with 120 minutes of effort today, you could reduce the effort by 10 minutes needed to undertake a task every day for rest of your life.

- E.g., learn some short cuts or tricks with your word-processing package, or "fix" some annoying problem in the current user set-up
- So, within 2 weeks, you will on net save time. In a year, 58 hours, and in a decade, 600 hours.

Suppose that value of time the same each day. No deadlines, no commitment devices.

▶ Do you do the task? If so, when

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If do the task today your intertemporal well-being is:

$$U^{t} = -120 + \beta \delta \cdot 10 + \beta \delta^{2} \cdot 10 + \beta \delta^{3} \cdot 10 + \dots$$
$$= -120 + \beta \frac{\delta}{1 - \delta} 10,$$

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Suppose time consistent, no taste for immediate gratification.

▶ E.g., 
$$\beta = 1$$
,  $\delta = .999$ . Then:

$$U^{t}(fix \ today) = -120 + \frac{.999}{1 - .999} 10 = 9,870.$$
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- ▶  $U^t(fix\ today) \succ U^t(never)$ , but  $U^t(fix\ tomorrow) \succ U^t(fix\ today)$ .
- ► This would never happen for a time-consistent person, by the FT-TC-TASE.
- In a stochastic or non-stationary environment, could be that a TC person happens to not want to do it today
- But the systematic congruence of these two inequalities is the feature of interest for present bias.
- ▶ If a task is worth doing, it is worth doing right away.
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Suppose some taste for immediate gratification (present bias).

▶ E.g., 
$$\beta = .9$$
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$$U^{t}(fix \ today) = -120 + .9\frac{.999}{1 - .999}10 = 8,871$$

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- ► Feels to you like you are saving about 150 hours in the future with the two hours today.
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$$U^{t}(fix \ today) = -120 + .9\frac{.999}{1 - .999}10 = 8,871$$
  
 $U^{t}(never) = 0$ 

Even with a taste for immediate gratification:

- ► Feels to you like you are saving about 150 hours in the future with the two hours today.
- ▶ Indeed, you would prefer doing the task today to never doing it even if it would take you 24 hours, not just 2 hours.

## So ...

- ▶ Do you do the task?
- ▶ If so, When?

If your choices were Today vs. Never, then

▶ Do today.

But you could also plan to do the task tomorrow:

$$U^{t}(fix\ tomorrow) = .9 \cdot .999(-120 + \frac{.999}{1 - .999}10) = 8,874$$

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# Intuition: Disadvantage of doing tomorrow is that you will delay the 10-minute savings by a day.

- ▶ But 2 hours tomorrow "feels like" 12 minutes less work than today
- ▶ You'd prefer to put off the task for one day.

So: Your preferences are:

- ▶  $U^t(fix\ tomorrow) \succ U^t(fix\ today)$
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# Sophisticates are (in this example) trickier to solve.

- ► Solution: would do the task either today or tomorrow.
- ► In both outcomes, their plan is to do it every other day (if they haven't yet done it).
  - ▶ Logic a bit complicated, but basic intuition simple.
- If aware of self-control problem, then properly nervous that you won't do it tomorrow, but delay it two or more days.
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# So: Sophistication helps overcome procrastination.

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# The Fundamental Theorem of Present-Biased Task-Assessment in Stationary Environments:

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In this example, it happens to be that

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This implies

- If think will do the task tomorrow, you will not do it today.
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The naif will never do the task

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General principle: *Severe* procrastination for "one-shot" tasks requires some naivety.

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- ▶ Sophisticates predict their future behavior correctly, and always have one simple action available to them ... doing the action now.
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- ▶ A "deltoid" will never do task only if  $-120 + \frac{\delta}{1-\delta}10 \le 0$ , so she would never do the task *only* if  $\delta \le \frac{12}{13} \Rightarrow \delta^{365} \le .0000000000002$
- ▶ Hence, to reconcile behavior with the exponential model if we are confident in our assessment of the disutilities of effort, we would need a yearly  $\widetilde{\delta} \leq (\frac{12}{13})^{365} = .000000000002$ .
- ▶ By contrast, we're explaining this with very modest (first-)yearly discounting.

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- ▶ And we shouldn't assume we know utility function when inferring discount factors.
- ▶ Suppose we didn't know  $\widetilde{\mu} = \frac{u(120 \text{ minutes})}{u(10 \text{ minutes})}$
- [?] What locus of  $(\widetilde{\delta}, \widetilde{\mu})$  would explain avoiding 2 hours of effort immediately to save 10 minutes every day rest of your life?
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- ▶ Consider  $\beta = .9$ ,  $\delta = .999$  naif again.
- ▶ But now:
- ▶ Suppose that the only choice available is "quick fix": 1 minute of effort today  $\implies 9\frac{1}{2}$  minutes saved each day forever.
- ▶ Would she do this? If so, when? Answer: Yes, she would. No temptation to put off the 1 minute of work until tomorrow.

$$U^{t}(quick \ fix \ today) = -1 + .9 \frac{.999}{1 - .999} 9.5 = 8540$$
  
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Now suppose **both** the 120/10 task and 1/9.5 task are available. Assume could do both sequentially, but don't save time on days when "fixing".

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So she'll perpetually *plan* to do the full fix tomorrow—and meanwhile *never do either of them*.

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- ▶ Naif makes a (quick) fix when it is **less** important/beneficial that she do so, but not if **more** important/beneficial.
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## Note:

▶ Somebody who is unwilling to take 120 minutes of effort to save 10 minutes or to take 1 minute of effort to save  $9\frac{1}{2}$  minutes every day for the rest of her life seems, interpreted through the lens of exponential discounting, as if she is discounting at rate of

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# April is the Cruelest Month Cumulative Procrastination

- Suppose you *must* read 30 pages in 30 days— $\sum_{t=1}^{30} p_t \ge 30$ . If you spend  $h_t$  hours reading on day t, then  $u_t = -h_t$ , and get  $p_t = \sqrt{h_t}$  pages read.
- ▶ Key feature: It is more efficient to spread out work regularly rather than doing it all in the space of a few days.
  - Other models with this qualitative feature would yield similar results

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▶ June Mae will read 1 hour each day, for a total of 30 hours.

Consider *April Mae*:  $\delta = \widehat{\beta} = 1, \ \beta = \frac{1}{2}$ 

- ▶ Day 1: April Mae will  $Max_{h_1}U^1 \equiv -h_1 + \frac{1}{2}\left[-29\left(\frac{30-\sqrt{h_1}}{29}\right)^2\right]$ . If she reads  $h_1$  hours on Day 1, she'll need to read  $\frac{30-\sqrt{h_1}}{29}$  pages each remaining day, spending  $\left(\frac{30-\sqrt{h_1}}{29}\right)^2$  hours each day.
- Day 1: April Mae reads for 15½ minutes (planning to read 62 minutes each of the remaining 29 days). She is planning to increase future h by 58 minutes to decrease h today by 45 minutes.

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- ▶ Day 3: ... 17 minutes ... (and ... 67 minutes ...)
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# So:

June Mae: 30 hours total. April Mae: 51 hours total.

Consider September "Sally" Mae:  $\delta = 1, \ \beta = \widehat{\beta} = \frac{1}{2}$ .

- ▶ Solution (to a fairly tedious problem):
- ▶ Sally Mae will read 39 hours total.
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Suppose April Mae and June Mae enjoy studying together; E.g.,  $u_t = -.99h_t$  if study together.

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- ► The enjoyment of studying together would serve as a serendipitous commitment for naifs.
- ▶ Suppose  $u_t = -1.01h_t$  from studying together: But again must be planned in advance (where backing out of agreeing to study with somebody is more costly than refraining from planned studying)
- ► A principle: Providing "incremental incentives" may help combat "cumulative procrastination".
- Another principle: Providing deadlines may help combat "simple" procrastination.

# Procrastination: Final Comments

- Micro-structure of choices and incentives matter in a way that we don't ever need to worry about when  $\beta = 1$ .
- ▶ Return to example: Can spend 120 minutes fixing your word-processor to make a 10-minutes-a-day saving.
- Change one detail: You can't do the 120 minutes each day.
- Only can do (say) every friday. E.g., it is a weekly seminar, free to attend on your own time. You cannot do this on your own.

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 $U^{t}(next\ friday) = .9 \cdot .999^{7}(-120 + \frac{.999}{1 - .999}10) = 8821$ 

- Now you will do it this friday.
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  - ▶ Cost you 70 minutes extra work, not just 10 minutes. Not worth it
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