

# Lecture 4f: Choice over Time

## Anticipatory Utility and Beliefs

EC 404: Behavioral Economics  
Professor: Ben Bushong

November 4, 2021

# Motivating Experiment

Based on Loewenstein (*EJ* 1987)

Motivating experiment: Ask subjects

- ▶ (1) their *WTP* for a kiss from a movie star of their choice at date  $x$ .
- ▶ (2) their *WTP* to avoid a 110-volt shock at date  $x$ .

He uses a within-subjects design, and uses  $x = \text{now}, 3 \text{ hrs}, 24 \text{ hrs}, 3 \text{ days}, 1 \text{ yr}, \text{ and } 10 \text{ yrs}$ .

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# Motivating Experiment

Let's denote the *WTP* for  $c$  at date  $x$  by  $WTP(c, x)$ .

Under the “standard” discounted-utility interpretation,

$$WTP(c, x) = D(x) * v(c)$$

- ▶  $v(c)$  is the instantaneous utility from  $c$ .
- ▶  $D(x)$  is discounting associated with delay  $x$ .

Normalizing  $D(0) = 1$ , this implies:

$$\frac{WTP(c, x)}{WTP(c, 0)} = \frac{D(x)v(c)}{D(0)v(c)} = D(x)$$

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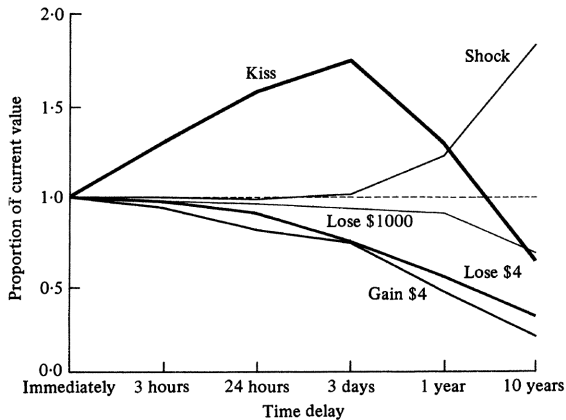
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# Motivating Experiment: Results



# Interpretation: Anticipatory Utility

Loewenstein interprets as evidence of “anticipatory utility”:

- ▶ Leading up to the kiss, you get positive utility from anticipating it; hence, you may prefer to delay the kiss so that you can properly anticipate it.
- ▶ Leading up to the shock, you get negative utility from anticipating it; hence, you may prefer to accelerate the shock so that you do NOT need to anticipate it.

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# A Model with Utility from Anticipation

Instantaneous utility in period  $t$  given by

$$u(c_t, c_{t+1}) = v(c_t) + w^A(c_{t+1}).$$

- ▶  $v(c_t)$  is utility from current consumption.
- ▶  $w^A(c_{t+1})$  is utility from anticipating future consumption.

In period 1, the person chooses  $(c_1, c_2, \dots)$  to maximize

$$U^1 \equiv \sum_{\tau=1}^{\infty} \delta^{\tau-1} u(c_{\tau}, c_{\tau+1}).$$

What is  $w^A(c_{t+1})$ ? Let's assume

$$w^A(c_{t+1}) = \phi * v(c_{t+1})$$

- ▶ Anticipatory utility is proportional to consumption utility, where  $\phi < 1$  reflects the “vividness”.

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- Kiss in period 1:  $v(\text{kiss})$
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If  $\phi + \delta > 1$ , optimal to have kiss in near future (in period 2).

# More Examples of Anticipatory Utility

Suppose you're thinking about going on vacation:

- ▶ For a long time, you thought probably no time for a 3-day vacation.
- ▶ Then one day find out that probably will have time off (80%).  
... and then confirmed as 100% likely when it happens.
- ▶ Belief evolution:



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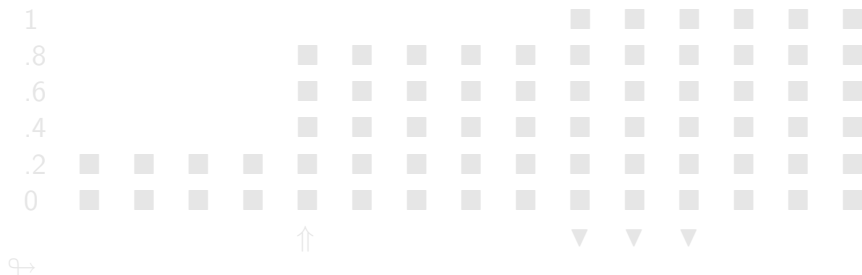
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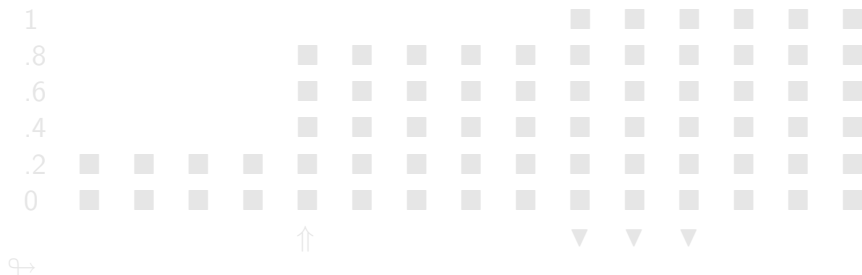
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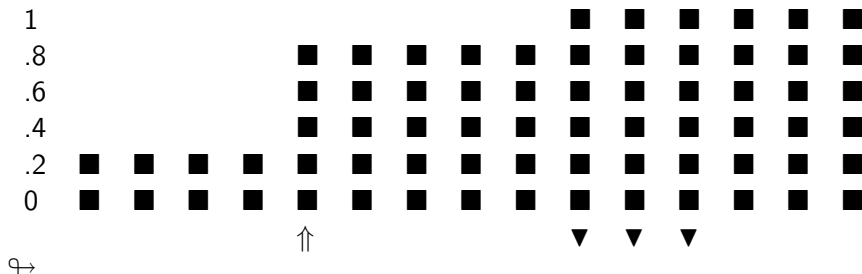
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As with other parts of this course, we'll discuss utility in time.

- ▶ That is, we will talk about real-time “happiness” without choice.

This isn't radical, even though it might seem even farther from mainstream. Stay calm.

- ▶ As before, this will have implications for choice.

So let's consider the utility of a person who has the beliefs from previous slide. Could be:



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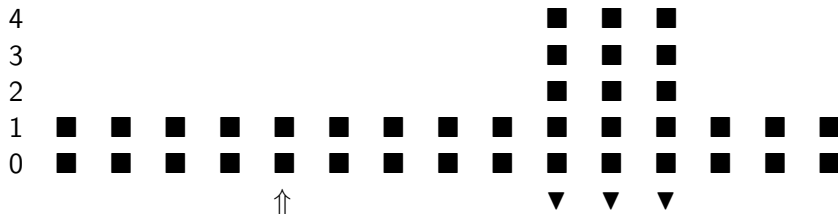
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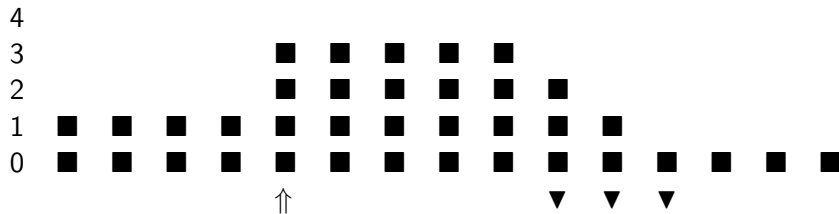
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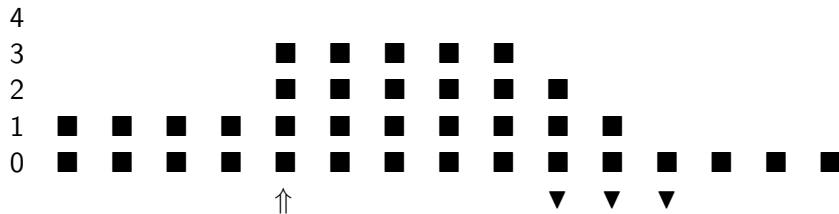


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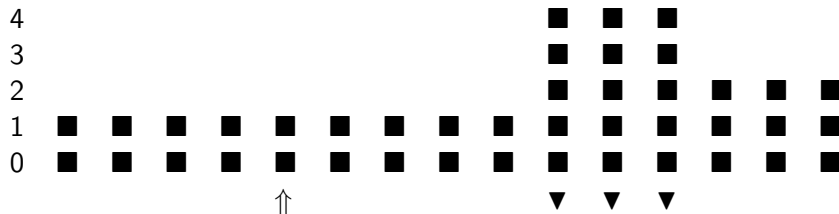


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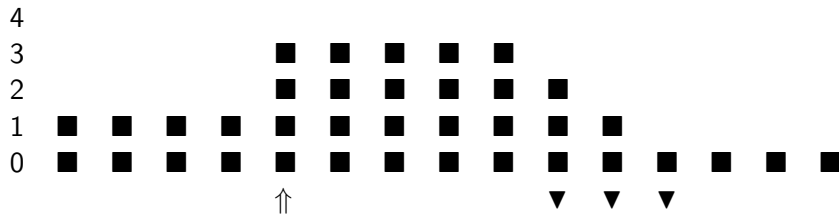


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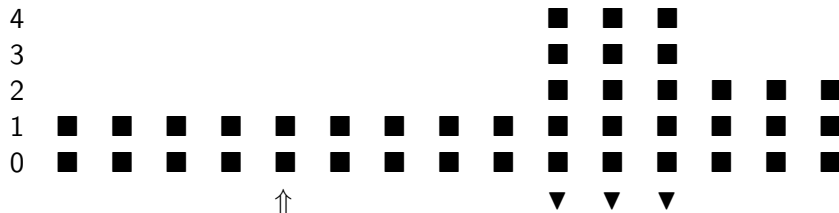


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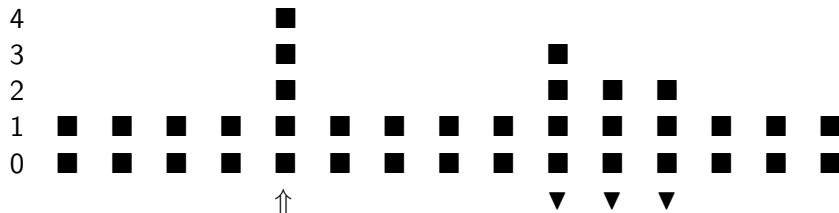
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↗

# Belief-Based Utility

Or could be (my personal vote):





So what?

- ▶ Why care about the timing or reason for enjoying a vacation?
- ▶ Often: We don't. All captured by  $u(\text{vacation})$ .
  - ▶ Reduced form probably best for “remembered utility”.

But can matter for various reasons. Three are:

- ▶ Use direct happiness data if and only if our theories specify timing of utility.
  - ▶ (Not a topic of this course, but interesting to think about).
- ▶ Beliefs/information matter even when behavior is unaffected.
- ▶ Affects choice: including time inconsistency, commitment, etc.

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# Belief-Based Utility

Suppose planning vacation:

- ▶ Have anticipatory preferences *for holiday-making only*.
- ▶ Club Cococabana holiday package, *total* anticipatory utility plus consumption and remembered utility well worth \$10,000.
- ▶ But without anticipatory utility, *not* nearly worth it.
- ▶ Can/must buy months in advance.

**Situation A:** All but \$50 is fully refundable if 24 hours in advance.

- ▶ What would a fully rational (sophisticated) person do?
- ▶ She **would/would not** (cross out one) buy the package, and then she **would/would not** (cross out one) go on the vacation.
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⇒ She **would not** buy the package, then **would not** go on the vacation.

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Suppose planning vacation:

- ▶ Have anticipatory preferences *for holiday-making only*.
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"Fully rational" defined (or, sophisticated):

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Instead be interested in realism, insight, and importance of assumptions.  
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## Consumption & Savings with Anticipatory Preferences

### Setting and Preferences

Yugi will live for 3 periods, has  $\$Y$  to spend over that time (no interest), seeks to maximize his (undiscounted) lifetime utility  $U^1 = u_1 + u_2 + u_3$ .

- ▶ In period  $t$ , “consumption utility”  $m_t$  that depends on  $c_t$ .
- ▶ Also gets utility from anticipating his future consumption utility.
- ▶ Why from anticipating solely his future consumption utility?
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Attempt to model this:

$$u_1 = m(c_1) + \phi[m(c_2) + m(c_3)]$$

$$u_2 = m(c_2) + \phi[m(c_3)]$$

$$u_3 = m(c_3)$$

- ▶ where  $\phi \geq 0$  is relative concern for anticipatory utility.

Question: what is *incoherent* about such preferences?

- ▶  $u_1$  cannot depend on  $c_2$  or  $c_3$ . Only **beliefs** about  $c_2, c_3$ .

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where  $E_t\{m(c_\tau)\}$  is period- $t$  expectations of period- $\tau$  consumption.

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When beliefs deterministic, shorthand:

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**Candidate solution:** Yugi solves

$$\text{Max}_{c_1, c_2} = m(c_1) + (1 + \phi)m(c_2) + (1 + 2\phi)m(Y - c_1 - c_2).$$

► E.g., if  $m(x) = \ln(x)$ , then:

$$\text{► } c_1^{**} = \frac{1}{3+3\phi} Y, \quad c_2^{**} = \frac{1+\phi}{3+3\phi} Y, \quad c_3^{**} = \frac{1+2\phi}{3+3\phi} Y$$

► How do these depend on  $\phi$ ?

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**Claim:** We have under-specified features of the environment.

- ▶ We need to say when Yugi is making (committed) choices.
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  - ▶ Yugi fully rational and can commit, then yes.
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What is interesting?

- ▶ Consumes more period 2 with commitment than without!
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- ▶ Precautionary savings.
- ▶ Backward-looking habit formation.

Reasons we may rarely see increasing consumption?

- ▶ Present bias: consumption smoothing may be self-control problem.
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