Lecture 2g: Choice over Time Projection Bias

EC 404: Behavioral Economics Professor: Ben Bushong

March 19, 2024

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Introduced by Loewenstein, O'Donoghue, & Rabin (QJE 2003)

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Step 1: A Model of Changing Tastes

To describe changes in tastes, we use "state-dependent utility":

▶ The instantaneous utility in period t is $u(c_t, s_t)$, where c_t is period-t consumption and s_t is the period-t "state".

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Step 2: Predictions of Future Tastes (cont)

Standard model: $\tilde{u}(c, s|s') = u(c, s)$

➤ The standard economic assumption is that people's predictions are accurate.

Two examples

- $ightharpoonup \tilde{u}$ (pie, full|hungry) = u (pie, full)
- \tilde{u} (coat, warm|cold) = u (coat, warm)

- ightharpoonup u (pie, full|hungry) < u (pie, hungry)
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[&]quot;Projection bias" means $\tilde{u}(c,s|s')$ in between u(c,s) & u(c,s').

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Step 3: A Simple Formulation

A person has "simple projection bias" if

$$\tilde{u}(c,s|s') = (1-\alpha)*u(c,s) + \alpha*u(c,s').$$

- $ightharpoonup lpha = 0 \Longleftrightarrow No Projection Bias$
- $ightharpoonup lpha \in (0,1) \Longleftrightarrow \mathsf{Projection} \; \mathsf{Bias}$

Examples

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- Except for these mispredictions, the person's intertemporal preferences are as in discounted utility model (for ease, think δ^{x} .)

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A first type of evidence: underappreciation of the endowment effect.

Loewenstein & Adler (EJ 1995)

Subjects: 27 CMU undergrads & 39 Pittsburgh MBA's.

- All subjects shown a mug, told they'll get one and have the opportunity to sell it for money.
- ▶ Half of the subjects predict how much they'd sell it for.
- ▶ After a delay, all subjects are given a mug and an opportunity to sell

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CMU:	Prediction Control	\$3.73	\$5.40 \$6.46
Pittsburgh:	Prediction Control	\$3.27	\$4.56 \$4.98

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Study 2: Subjects were 43 Cornell undergraduates.

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19 subjects randomly chosen to be "sellers".
24 subjects randomly chosen to be "buyers"
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- Ask buyers to predict average reservation price of sellers, and ask sellers to predict average reservation price of buyers.

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Sellers:	\$6.37	\$3.93
Buyers:	\$1.85	\$4.39

A second type of evidence: underappreciation of the effects of hunger.

Read & van Leeuwen (OBHDP 1998)

Subjects were 200 employees at several firms in Amsterdam.

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- They varied subjects' expected future hunger and their current hunger.

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		Future	Hunger
		Hungry	Satiated
Current	Hungry	78%	42%
Hunger	Satiated	56%	26%

$$\qquad \qquad \textbf{(Total Utility)} = \big(\textbf{Mug Utility} \big) + \big(\textbf{Money Utility} \big) \\$$

$$\qquad \qquad \mathsf{(Total\ Utility)} = \quad \mathit{u}(\mathit{c},\mathit{r}) \qquad + \qquad \mathit{m}$$

Mug utility is
$$u(c,r) = w(c) + v(c-r)$$
, where

$$w(c) = \mu * c$$
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Consumption is:

- $ightharpoonup c_1 = c_2 = 1$ if buy or keep.
- $ightharpoonup c_1 = c_2 = 0$ if don't buy or sell.

Initial reference point is exogenous:

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- $ightharpoonup c_1 = c_2 = 0$ if don't buy or sell.

Initial reference point is exogenous:

- $ightharpoonup r_1 = 0 \iff$ unendowed (buyers).
- $ightharpoonup r_1 = 1 \iff \text{ endowed (sellers)}.$

One can show:

- ▶ Sellers should sell iff $P \ge P_S^* \equiv$
- ▶ Sellers actually sell iff $P \ge P_S^A \equiv$
- ▶ Buyers should buy iff $P \le P_B^* \equiv$
- ▶ Buyers actually buy iff $P \le P_B^A \equiv$

Some Results:

(1)
$$p_S^A > p_S^* \& p_B^A > p_B^*$$
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▶ People are over-prone to consume goods to which they become accustomed because they underappreciate how they'll adapt — and more generally can lead to incorrect intertemporal utility maximization.

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$$p_S^A - p_B^A > p_S^* - p_B^*$$

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Application: Projection Bias and Durable Goods

(Discussion courtesy of O'Donoghue)

Underlying environment:

► A durable good — e.g., a winter coat — yields a utility stream

$$\mu_1, \mu_2, ..., \mu_T.$$

These μ 's typically vary from day to day in a somewhat random way — for simplicity, let's assume that for all days the expected value of μ_t is $\bar{\mu}$.

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On Day 1, when a person knows μ_1 but not the future μ_t 's, how much is the person willing to pay for this durable good (assuming no discounting)?

▶ Optimal:

$$WTP = \mu_1 + (T - 1)\bar{\mu}$$

► With Projection bias:

WTP =
$$\mu_1 + (T - 1)[(1 - \alpha)\bar{\mu} + \alpha\mu_1$$

= $\mu_1 + (T - 1)[\bar{\mu} + \alpha(\mu_1 - \bar{\mu})]$

Hence: If $\mu_1 > \bar{\mu}$ then overprone to buy. If $\mu_1 < \bar{\mu}$ then underprone to buy

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Recall: If $\mu_1>\bar{\mu}$ then overprone to buy. If $\mu_1<\bar{\mu}$ then underprone to buy.

<u>One extension</u>: Suppose that you have multiple opportunities to buy the durable good (and suppose that there are limits on your ability to return the good).

Case 1: Suppose $P < T\bar{\mu}$, so you SHOULD buy the good.

- You end up buying it as long as $\mu_t \geq \bar{\mu}$ on at least one occasion, which is quite likely.

 Under-buying is very unlikely.
- Case 2: Suppose $P > T\bar{\mu}$, so you should NOT buy the good.
 - Again, you end up buying it as long as $\mu_t \geq \bar{\mu}$ on at least one occasion, which is quite likely. \Longrightarrow Over-buying is very LIKELY.

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Second extension: Suppose returns are easy — perhaps we can use returns to test for projection bias in field data.

- ▶ If μ_t is large, more "over-buying", thus many returns
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Look at catalog orders — very easy to return!

Prediction: More returns for orders made on high-valuation days than for orders made on low-valuation days.

Big question: How can we assess whether a person orders on a high-valuation day vs. a low-valuation day?

Our answer: look at orders of winter-clothing items as a function of the weather.

- ▶ If order on a cold day, it's likely a high-valuation day.
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