Lecture 2g: Choice over Time Projection Bias

EC 404: Behavioral Economics Professor: Ben Bushong

March 30, 2023

"Projection Bias"

Introduced by Loewenstein, O'Donoghue, & Rabin (QJE 2003)

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Step 1: A Model of Changing Tastes

To describe changes in tastes, we use "state-dependent utility":

▶ The instantaneous utility in period t is $u(c_t, s_t)$, where c_t is period-t consumption and s_t is the period-t "state".

- ightharpoonup u(pie,hungry) > u(pie,full)
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Step 2: Predictions of Future Tastes (cont)

Standard model: $\tilde{u}(c, s|s') = u(c, s)$.

The standard economic assumption is that people's predictions are accurate.

Two examples

- $ightharpoonup ilde{u}$ (pie, full|hungry) = u (pie, full)
- $ightharpoonup ilde{u}$ (coat, warm|cold) = u (coat, warm)

- ▶ u (pie, full) < \tilde{u} (pie, full|hungry) < u (pie, hungry)
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Step 3: A Simple Formulation

A person has "simple projection bias" if

$$\tilde{u}(c,s|s') = (1-\alpha)*u(c,s) + \alpha*u(c,s').$$

- $\alpha = 0 \iff$ No Projection Bias
- $ightharpoonup lpha \in (0,1) \Longleftrightarrow \mathsf{Projection} \; \mathsf{Bias}$

$$\tilde{u}$$
 (pie, full|hungry) = $(1 - \alpha) * u$ (pie, full) + $\alpha * u$ (pie, hungry)

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- ► The person is not aware of the bias (otherwise she could just correct for it).
- Except for these mispredictions, the person's intertemporal preferences are as in discounted utility model (for ease, think δ^{\times} .)

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A first type of evidence: underappreciation of the endowment effect.

Loewenstein & Adler (EJ 1995)

Subjects: 27 CMU undergrads & 39 Pittsburgh MBA's.

Procedure:

- All subjects shown a mug, told they'll get one and have the opportunity to sell it for money.
- ▶ Half of the subjects predict how much they'd sell it for.
- After a delay, all subjects are given a mug and an opportunity to sell

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CMU:	Prediction Control	\$3.73	\$5.40 \$6.46
Pittsburgh:	Prediction Control	\$3.27	\$4.56 \$4.98

VanBoven, Dunning, & Loewenstein (JPSP 2000)

Study 2: Subjects were 43 Cornell undergraduates.

19 subjects randomly chosen to be "sellers" 24 subjects randomly chosen to be "buyers"

Each seller given a coffee mug. Each buyer shown a coffee mug.

- ► Elicit people's reservation prices
- Ask buyers to predict average reservation price of sellers, and ask sellers to predict average reservation price of buyers.

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Sellers:	\$6.37	\$3.93
Buyers:	\$1.85	\$4.39

A second type of evidence: underappreciation of the effects of hunger.

Read & van Leeuwen (OBHDP 1998)

Subjects were 200 employees at several firms in Amsterdam.

- ► Each subject asked to choose between a healthy vs. unhealthy snack to be received in one week.
- ► They varied subjects' expected future hunger and their current hunger.

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Results: % of Subjects Choosing Unhealthy Snack

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		Future	Hunger
		Hungry	Satiated
Current	Hungry	78%	42%
Hunger	Satiated	56%	26%

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► (Total Utility) =
$$u(c,r)$$
 + m

Mug utility is
$$u(c,r) = w(c) + v(c-r)$$
, where

$$w(c) = \mu * c$$
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Suppose buy/sell the mug in period 1, and (possibly) consume the mug in periods 1 & 2.

Consumption is:

- $ightharpoonup c_1 = c_2 = 1$ if buy or keep.
- $ightharpoonup c_1=c_2=0$ if don't buy or sell.

Initial reference point is exogenous:

- $ightharpoonup r_1 = 0 \iff \text{unendowed (buyers)}.$
- $ightharpoonup r_1 = 1 \Longleftrightarrow \text{ endowed (sellers)}$

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One can show:

- ▶ Sellers should sell iff $P \ge P_S^* \equiv$
- ▶ Sellers actually sell iff $P \ge P_S^A \equiv$
- ▶ Buyers should buy iff $P \le P_B^* \equiv$
- ▶ Buyers actually buy iff $P \le P_B^A \equiv$

Some Results:

(1)
$$p_S^A > p_S^* \& p_B^A > p_B^*$$
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People are over-prone to consume goods to which they become accustomed because they underappreciate how they'll adapt — and more generally can lead to incorrect intertemporal utility maximization.

(2)
$$p_S^A - p_B^A > p_S^* - p_B^*$$

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Application: Projection Bias and Durable Goods

(Discussion courtesy of O'Donoghue)

Underlying environment:

▶ A durable good — e.g., a winter coat — yields a utility stream

$$\mu_1, \mu_2, ..., \mu_T.$$

▶ These μ 's typically vary from day to day in a somewhat random way — for simplicity, let's assume that for all days the expected value of μ_t is $\bar{\mu}$.

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On Day 1, when a person knows μ_1 but not the future μ_t 's, how much is the person willing to pay for this durable good (assuming no discounting)?

▶ Optimal

$$WTP = \mu_1 + (T - 1)\bar{\mu}$$

▶ With Projection bias:

WTP =
$$\mu_1 + (T - 1)[(1 - \alpha)\bar{\mu} + \alpha\mu_1]$$

= $\mu_1 + (T - 1)[\bar{\mu} + \alpha(\mu_1 - \bar{\mu})]$

Hence: If $\mu_1 > \bar{\mu}$ then overprone to buy. If $\mu_1 < \bar{\mu}$ then underprone to buy

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Recall: If $\mu_1>\bar{\mu}$ then overprone to buy. If $\mu_1<\bar{\mu}$ then underprone to buy.

<u>One extension</u>: Suppose that you have multiple opportunities to buy the durable good (and suppose that there are limits on your ability to return the good).

Case 1: Suppose $P < T\bar{\mu}$, so you SHOULD buy the good.

- You end up buying it as long as $\mu_t \geq \bar{\mu}$ on at least one occasion, which is quite likely.
 - ⇒ Under-buying is very unlikely.

Case 2: Suppose $P > T\bar{\mu}$, so you should NOT buy the good.

Again, you end up buying it as long as $\mu_t \geq \bar{\mu}$ or at least one occasion, which is quite likely. \Longrightarrow Over-buying is very LIKELY.

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- ▶ If μ_t is large, more "over-buying", thus many returns.
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Look at catalog orders — very easy to return!

Prediction: More returns for orders made on high-valuation days than for orders made on low-valuation days.

Big question: How can we assess whether a person orders on a high-valuation day vs. a low-valuation day?

Our answer: look at orders of winter-clothing items as a function of the weather.

- ▶ If order on a cold day, it's likely a high-valuation day.
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