

# Topic 4D: Choice over Time

## An Alternative Model: Present Bias

EC 404: Behavioral Economics  
Professor: Ben Bushong

October 19, 2021

Exponential discounting implies constant discounting:

$$\frac{D(0)}{D(1)} = \frac{D(1)}{D(2)} = \frac{D(2)}{D(3)} = \dots = \frac{1}{\delta}.$$

But the evidence suggests more discounting in the short run than in the long run:

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# A Simplified Model

A simplified model: “ $\beta, \delta$  preferences” or “present bias”

Period- $t$  intertemporal utility is

$$U^t = u_t + \beta * \sum_{x=1}^{T-t} \delta^x u_{t+x}.$$

In other words, the discount function is:

$$D(x) = \begin{cases} 1 & \text{if } x = 0 \\ \beta * \delta^x & \text{if } x > 0. \end{cases}$$

Hence, under  $\beta, \delta$  preferences:

$$\frac{D(0)}{D(1)} = \frac{1}{\beta\delta} > \frac{1}{\delta} = \frac{D(1)}{D(2)} = \frac{D(2)}{D(3)} = \dots$$

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$\beta, \delta$  preferences capture in the simplest way possible that a person has a time-inconsistent preference for immediate gratification.

People who assume  $\beta, \delta$  preferences use many different names:

- ▶ present bias (present-biased preferences)
- ▶ hyperbolic discounting
- ▶ quasi-hyperbolic discounting
- ▶ preference for immediate gratification
- ▶ self-control problems

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## Example to Illustrate Time Inconsistency

Suppose there is a task that you must complete on one of the next three days. To complete this task, you incur costs as follows:

- ▶ If you complete the task in period 1, the cost is 3.
- ▶ If you complete the task in period 2, the cost is 5.
- ▶ If you complete the task in period 3, the cost is 8.

Suppose there is no reward, that you value costs linearly, and that you have  $\beta = 1/2$  and  $\delta = 1$ .



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Conditional on not doing it in period 1, your preferences from a period-2 perspective are:

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Hence:

## Example to Illustrate Time Inconsistency

To summarize, your period-1 preferences are

$$(\text{period 2}) \succ (\text{period 1}) \succ (\text{period 3})$$

while your period-2 preferences are

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Note the time inconsistency:

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An important issue: Are you aware of your future self-control problems (of your future present bias)?

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If you were asked to commit yourself in period 1, you'd commit yourself to do the task in period 2.

Suppose instead that in period 1 you only choose whether or not to do the task then. Then your choice will depend on what you expect to do in period 2 (if you were to wait).

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Suppose you are fully aware of future self-control problems — that is, you correctly predict your period-2 preferences.

- ▶ If so, you correctly predict that if you wait now, then in period 2 you'll prefer to wait again.
- ▶ Hence, you compare completing the task now to completing the task in period 3, and you prefer the former.

⇒ Complete task in period 1.

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Suppose you are **fully unaware** of future self-control problems — that is, you incorrectly think that you'll feel the same way in period 2 as you do now.

- ▶ If so, then since you currently prefer period 2 to period 3, you think that if you wait now, you'll just complete the task in period 2.
- ▶ Hence, you wait in period 1 planning to complete the task in period 2.
- ▶ Of course, when period 2 arrives, you'll change your mind and decide to wait.

⇒ End up completing task in period 3.

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# Sophistication vs. Naivete

## More generally:

Two extreme assumptions about people's awareness of their own future self-control problems:

- ▶ *Sophisticates* are fully aware of their future self-control problems and thus correctly predict future behavior.
- ▶ *Naifs* are fully unaware of their future self-control problems and thus expect to behave in future exactly as they currently would like themselves to behave in future.



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# Sophistication vs. Naivete

To solve for naifs:

- ▶ Each period, derive the optimal lifetime path, and follow this period's component. But when next period arrives, reassess this plan.
- ▶ **Note:** Naifs may not stick to their plans.

To solve for sophisticates:

- ▶ Treat each period-self as a separate agent, and solve for the subgame-perfect Nash equilibrium to the game played between these agents (use backward induction — start at the end, and work backward).
- ▶ Note: Sophisticates always stick to their plans.
- ▶ ... they just never plan to do something they won't later carry out.

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To solve for naifs:

- ▶ Each period, derive the optimal lifetime path, and follow this period's component. But when next period arrives, reassess this plan.
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## Some features of Example 1:

- ▶ For an onerous task that involves immediate costs, a preference for immediate gratification implies a tendency to procrastinate — to delay beyond the best time.
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# (Less Gentle) Introduction to Present-Biased Preferences

## Doing It Now or Later: The Simple Example

### Fibonacci's Fine Arts Cinema

- ▶ Week 1: mediocre movie, 3 utils
- ▶ Week 2: good movie, 5 utils.
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Assume  $\delta = 1$ ,  $\beta = \frac{1}{2}$ .

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Your (cinematic) life choices are  $(u_1, u_2, u_3, u_4) =$

- ▶  $(0, 5, 8, 13)$  or  $(3, 0, 8, 13)$  or  $(3, 5, 0, 13)$  or  $(3, 5, 8, 0)$ .

You cannot commit to which movie to miss—you must decide incrementally each week whether to see that movie or skip it.

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Have to consider two cases: naif vs sophisticate decision-maker.

**Case 1:** What will a sophisticate do?

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Note that even given  $\beta = \frac{1}{2}$ , all four selves agree that missing Vin Diesel is a bad thing to happen. Yet the naif does so.

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- ▶ In many applications, “pareto dominance” most common outcome.



# (Less Gentle) Introduction to Present-Biased Preferences

## Doing It Now or Later: The Simple Example

Note that even given  $\beta = \frac{1}{2}$ , all four selves agree that missing Vin Diesel is a bad thing to happen. Yet the naif does so.

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Aside: Let us see what we would infer from the observed behavior if we were an anachronistic economist who believed in  $\beta = 1$ .

An exponential discounter would have to have a *weekly* discount factor  $\tilde{\delta} \leq \text{Min}[\sqrt[3]{\frac{3}{13}}, \sqrt[2]{\frac{5}{13}}, \frac{8}{13}] \approx .61$  to be willing to miss F&F.

	Letting $\beta < 1$ ( $= \hat{\beta}$ )	Insisting $\beta = 1$
--	---	-----------------------

Week 1 weight on $u_2$ vs. $u_1$	.61	.61
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Week 1 weight on $u_4$ vs. $u_1$	.61	.23
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# (Less Gentle) Introduction to Present-Biased Preferences

## Doing It Now or Later: The Simple Example

And if we observed somebody missing the 52nd week (Fast and Furious marathon?) at the Fibonacci's Fine Arts Cinema with utilities (3,5,8,13,21,34,55...)

	Letting $\beta < 1$ ( $= \hat{\beta}$ )	Insisting $\beta = 1$
Week 1 $u_2$ vs. $u_1$	$\approx .61$	$\approx .61$
Week 1 $u_{52}$ vs. $u_1$	$\approx .618$	$\approx .618^{52} \approx 1.36 \times 10^{-11}$

Lesson: Some behavior looks more (absurdly) impatient if (mis)interpreted through the lens of exponential discounting.

► But less so through the lens of present-biased discounting.

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Now suppose: Person can go to only one movie, and must skip 3 of them. Same preferences as above.

- ▶ So life utility profiles are  $(u_1, u_2, u_3, u_4) =$
- ▶  $(3, 0, 0, 0)$  or  $(0, 5, 0, 0)$  or  $(0, 0, 8, 0)$  or  $(0, 0, 0, 13)$ .

What will the sophisticate do?

- ▶ Because  $8 > \frac{1}{2}(13)$ , if she has not seen it yet, the sophisticate will see the movie in Week 3.
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## Example 1

Suppose there is a task that you must complete on one of the next four days. To complete this task, you incur costs as follows:

- If you complete the task in period 1, the cost is 3.
- If you complete the task in period 2, the cost is 5.
- If you complete the task in period 3, the cost is 8.
- If you complete the task in period 4, the cost is 13.

Suppose there is no reward, that you value costs linearly, and that you have  $\beta = 1/2$  and  $\delta = 1$ .

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[illegible]

From a prior perspective, the best time is period 1.

Naifs complete the task in period 4.

Sophisticates complete the task in 1.

## Formal Welfare Implications

Our welfare criterion: A person's "long-run utility" — which reflects how she feels from a prior perspective — is given by

$$U^0 = \sum_{\tau=1}^T \delta^\tau u_\tau.$$

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Welfare loss for naifs is 10.

In this simple “do-it-once” environment, for onerous tasks, naifs can suffer large harm, sophisticates cannot.

## Welfare Implications

In Example 2:

Long-run utility from best option (do it in period 4) is 13.

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Long-run utility from best option (do it in period 4) is 13.

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Welfare loss for naifs is 5.

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In this simple “do-it-once” environment, for pleasurable tasks, sophisticates can suffer large harm, naifs cannot.

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In richer, real-world environments, sophistication is most likely better than naivete, because sophisticates will make use of commitment devices to overcome their self-control problems.

## Procrastination: Doing It ... Tomorrow

- ▶ Procrastination involves the “immediate gratification” of not doing something optimally onerous
- ▶ Often the main “cost” of doing some beneficial task is primarily the opportunity cost of doing something gratifying.
- ▶ Procrastination is in fact a wonderful vice: You can, and — ideally — should do it concurrently with other vices!
- ▶ Note: quitting smoking, etc. qualitatively similar to procrastination.

But what *is* it?

- ▶ Not just delaying unpleasant tasks, which is often right thing to do.
- ▶ It is delaying beyond when you yourself want to complete them.

# Procrastination

Important example of unpleasant task we procrastinate on: learning.

- ▶ Learning how to do something better is pervasive example of something with long-term benefits.
- ▶ Many people recognize the enormous benefits of financial planning and literacy. And so want to do so. And plan to do so.  
... tomorrow.

## Procrastination Example

Suppose that, with 120 minutes of effort today, you could reduce the effort by 10 minutes needed to undertake a task every day for rest of your life.

- ▶ E.g., learn some short cuts or tricks with your word-processing package, or “fix” some annoying problem in the current user set-up.
- ▶ So, within 2 weeks, you will on net save time. In a year, 58 hours, and in a decade, 600 hours.

Suppose that value of time the same each day. No deadlines, no commitment devices.

- ▶ Do you do the task? If so, when?

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If do the task today your intertemporal well-being is:

$$\begin{aligned}U^t &= -120 + \beta\delta \cdot 10 + \beta\delta^2 \cdot 10 + \beta\delta^3 \cdot 10 + \dots \\&= -120 + \beta \frac{\delta}{1-\delta} 10,\end{aligned}$$

relative to the utility you would get from doing nothing.

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Suppose time consistent, no taste for immediate gratification.

► E.g.,  $\beta = 1$ ,  $\delta = .999$ . Then:

$$U^t(\text{fix today}) = -120 + \frac{.999}{1-.999}10 = 9,870.$$

$$U^t(\text{fix tomorrow}) = .999(-120 + \frac{.999}{1-.999}10) = 9,861$$

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Suppose time consistent, no taste for immediate gratification.

► E.g.,  $\beta = 1$ ,  $\delta = .999$ . Then:

$$U^t(\text{fix today}) = -120 + \frac{.999}{1-.999}10 = 9,870.$$

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The Fundamental Theorem of TC (that is, non-present-biased)  
Task-Assessment in Stationary Environments: Either

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- ▶ This would never happen for a time-consistent person, by the FT-TC-TASE.
- ▶ In a stochastic or non-stationary environment, could be that a TC person happens to not want to do it today
- ▶ But the systematic congruence of these two inequalities is the feature of interest for present bias.
- ▶ If a task is worth doing, it is worth doing right away.
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Suppose some taste for immediate gratification (present bias).

- ▶ E.g.,  $\beta = .9$ ,  $\delta = .999$ .

$$U^t(\text{fix today}) = -120 + .9 \frac{.999}{1-.999} 10 = 8,871$$

$$U^t(\text{never}) = 0$$

Even with a taste for immediate gratification:

- ▶ Feels to you like you are saving about 150 hours in the future with the two hours today.
- ▶ Indeed, you would prefer doing the task today to never doing it even if it would take you 24 hours, not just 2 hours.

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So ...

- ▶ Do you do the task?
- ▶ If so, When?

If your choices were Today vs. Never, then:

- ▶ Do today.

But you could also plan to do the task tomorrow:

$$\text{▶ } U^t(\text{fix tomorrow}) = .9 \cdot .999(-120 + \frac{.999}{1-.999}10) = 8,874$$

You'd prefer to learn tomorrow rather than today.

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Intuition: Disadvantage of doing tomorrow is that you will delay the 10-minute savings by a day.

- ▶ But 2 hours tomorrow “feels like” 12 minutes less work than today.
- ▶ You’d prefer to put off the task for one day.

So: Your preferences are:

- ▶  $U^t(\text{fix tomorrow}) \succ U^t(\text{fix today})$
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Also:

- ▶  $U^t(\text{fix today}) \succ U^t(\text{fix two days hence})$

So, repeat the question: Do you do the task?

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So, repeat the question: Do you do the task?

Answer: It depends.

- ▶ If you think that not doing today means you will do tomorrow, then  
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- ▶ So what you do depends on your beliefs about own future behavior.
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Recall:

- ▶ If  $\beta = \frac{9}{10}$ :  $U^t(\text{fix tomorrow}) \succ U^t(\text{fix today}) \succ U^t(\text{never})$
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So if naively think that tomorrow you will have a  $\beta = 1$ , then you will not do today *believing* will do tomorrow.

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- ▶ If  $\beta = 1$ :  $U^t(\text{fix today}) \succ U^t(\text{fix tomorrow}) \succ U^t(\text{never})$

So if naively think that tomorrow you will have a  $\beta = 1$ , then you will not do today *believing* will do tomorrow.

- ▶ But when tomorrow comes:
  - ▶ You will not do, planning to do the next day.
- ▶ And when the next day comes:
  - ▶ You will not do, planning to do the day after ...
- ▶ You will (in this extreme example) procrastinate forever—always planning to do the task the next day.



# Procrastination

Sophisticates are (in this example) trickier to solve.

- ▶ **Solution:** would do the task either today or tomorrow.
- ▶ In both outcomes, their plan is to do it every other day (if they haven't yet done it).
  - ▶ Logic a bit complicated, but basic intuition simple.
- ▶ If aware of self-control problem, then properly nervous that you won't do it tomorrow, but delay it two or more days.
- ▶ Now you see choice not between today and two days hence.
- ▶ So (with the numbers at hand) you do it today.
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## The Fundamental Theorem of Present-Biased Task-Assessment in Stationary Environments:

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General principle: *Severe* procrastination for “one-shot” tasks requires some naivety.

- ▶ Intuition?

Simple style of rationality argument in economics.

- ▶ Sophisticates predict their future behavior correctly, and always have one simple action available to them ... doing the action now.
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## A mispecification/calibration exercise:

- ▶ A “deltoid” will never do task only if  $-120 + \frac{\delta}{1-\delta}10 \leq 0$ , so she would never do the task *only* if  $\delta \leq \frac{12}{13} \Rightarrow \delta^{365} \leq .000000000002$ .
- ▶ Hence, to reconcile behavior with the exponential model if we are confident in our assessment of the disutilities of effort, we would need a yearly  $\tilde{\delta} \leq (\frac{12}{13})^{365} = .000000000002$ .
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Of course, effort costs probably increasing rather than linear.

- ▶ And we shouldn't assume we know utility function when inferring discount factors.
- ▶ Suppose we didn't know  $\tilde{\mu} = \frac{u(120 \text{ minutes})}{u(10 \text{ minutes})}$ .

[?] What locus of  $(\tilde{\delta}, \tilde{\mu})$  would explain avoiding 2 hours of effort immediately to save 10 minutes every day rest of your life?

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## New Example:

- ▶ Consider  $\beta = .9$ ,  $\delta = .999$  naif again.
- ▶ But now:
- ▶ Suppose that the only choice available is “quick fix”: 1 minute of effort today  $\implies 9\frac{1}{2}$  minutes saved each day forever.
- ▶ Would she do this? If so, when? Answer: Yes, she would. No temptation to put off the 1 minute of work until tomorrow.

$$U^t(\text{quick fix today}) = -1 + .9 \frac{.999}{1-.999} 9.5 = 8540$$

$$U^t(\text{quick tomorrow}) = .9 \cdot .999 \left( -1 + \frac{.999}{1-.999} 9.5 \right) = 8532$$

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Now suppose **both** the 120/10 task and 1/9.5 task are available. Assume could do both sequentially, but don't save time on days when "fixing".

- ▶ The naif will compare her four choices:

- ▶  $U^t(\text{quick fix today}) = 8540$

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- ▶  $U^t(\text{full fix today}) = 8871$

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So she'll perpetually *plan* to do the full fix tomorrow—and meanwhile *never do either of them*.

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Suppose now naif has both the 120/10 and 1/9.5 options available—but that each only saves effort on 10% of days rest of her life. Then:

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So: She'll do the quick fix immediately.

- ▶ Naif makes a (quick) fix when it is **less** important/beneficial that she do so, but not if **more** important/beneficial.
- ▶ Maybe not **despite** its importance that we never do something, but **because** of its importance.

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### Cumulative Procrastination

- ▶ Suppose you *must* read 30 pages in 30 days— $\sum_{t=1}^{30} p_t \geq 30$ . If you spend  $h_t$  hours reading on day  $t$ , then  $u_t = -h_t$ , and get  $p_t = \sqrt{h_t}$  pages read.
- ▶ Key feature: *It is more efficient to spread out work regularly rather than doing it all in the space of a few days.*
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- ▶ Day 1: April Mae reads for  $15\frac{1}{2}$  minutes (planning to read 62 minutes each of the remaining 29 days). She is planning to increase future  $h$  by 58 minutes to decrease  $h$  today by 45 minutes.

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- ▶ Day 3: ... 17 minutes ... (and ... 67 minutes ...).
- ▶ Day 10: ... 22 minutes (and ... 90 minutes ...).

With a week left: Has read 16 pages in 11 hours.

- ▶ Day 24: 72 minutes (and ... more than 4 hours ...).
- ▶ Day 30: April Mae reads for  $23\frac{3}{4}$  hours. (an “all-nighter”).

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So:

June Mae: 30 hours total.

April Mae: 51 hours total.

Consider *September "Sally" Mae*:  $\delta = 1$ ,  $\beta = \hat{\beta} = \frac{1}{2}$ .

- ▶ Solution (to a fairly tedious problem):
- ▶ Sally Mae will read 39 hours total.
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Suppose April Mae and June Mae enjoy studying together; E.g.,  $u_t = -.99h_t$  if study together.

- ▶ But must schedule in advance to do so.
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- ▶ Suppose  $u_t = -1.01h_t$  from studying together:  
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## Procrastination: Final Comments

### Details Matter

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- ▶ Return to example: Can spend 120 minutes fixing your word-processor to make a 10-minutes-a-day saving.
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- ▶ Now you think your choice is between doing it this friday vs. next friday—seven days later, not tomorrow:

$$U^t(\text{this friday}) = -120 + .9 \frac{.999}{1-.999} 10 = 8871$$
$$U^t(\text{next friday}) = .9 \cdot .999^7 (-120 + \frac{.999}{1-.999} 10) = 8821$$

- ▶ Now you will do it this friday.
  - ▶ Intuition: Now you realize that waiting  $\implies$  waiting a week
  - ▶ Cost you 70 minutes extra work, not just 10 minutes. Not worth it.
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- ▶ Now you think your choice is between doing it this friday vs. next friday—seven days later, not tomorrow:

$$U^t(\text{this friday}) = -120 + .9 \frac{.999}{1-.999} 10 = 8871$$
$$U^t(\text{next friday}) = .9 \cdot .999^7 (-120 + \frac{.999}{1-.999} 10) = 8821$$

- ▶ Now you will do it this friday.
  - ▶ Intuition: Now you realize that waiting  $\implies$  waiting a week
  - ▶ Cost you 70 minutes extra work, not just 10 minutes. Not worth it.
- ▶ Changing switching opportunities from every day to every week can dramatically change (and improve) the outcome.

## Optimal design of incentives:

- ▶ Convince employees need help to improve word-processing, and schedule seminars/assistance so that they can't do it any time?
- ▶ Change cost from 120 minutes to 0 minutes by giving immediate time off from those who invest in self-improvement?
- ▶ The two big methods to combat procrastination:
  - ▶ Defaults
  - ▶ Deadlines

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