# Lecture 2g: Choice over Time Projection Bias

EC 404: Behavioral Economics Professor: Ben Bushong

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### "Projection Bias"

### Introduced by Loewenstein, O'Donoghue, & Rabin (QJE 2003)

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### Step 1: A Model of Changing Tastes

To describe changes in tastes, we use "state-dependent utility":

▶ The instantaneous utility in period t is  $u(c_t, s_t)$ , where  $c_t$  is period-t consumption and  $s_t$  is the period-t "state".

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### Step 2: Predictions of Future Tastes

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- ▶ Current tastes are u(c, s')
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### Step 2: Predictions of Future Tastes (cont)

Standard model:  $\tilde{u}(c, s|s') = u(c, s)$ .

The standard economic assumption is that people's predictions are accurate.

#### Two examples

- $ightharpoonup ilde{u}$  (pie, full|hungry) = u (pie, full)
- $ightharpoonup ilde{u}$  (coat, warm|cold) = u (coat, warm)

- ▶ u (pie, full) <  $\tilde{u}$  (pie, full|hungry) < u (pie, hungry)
- ightharpoonup u (coat, warm|cold) < u (coat, cold)

<sup>&</sup>quot;Projection bias" means  $\tilde{u}(c,s|s')$  in between u(c,s) & u(c,s').

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### Step 3: A Simple Formulation

A person has "simple projection bias" if

$$\tilde{u}(c,s|s') = (1-\alpha)*u(c,s) + \alpha*u(c,s').$$

- $\alpha = 0 \iff$  No Projection Bias
- $ightharpoonup lpha \in (0,1) \Longleftrightarrow \mathsf{Projection} \; \mathsf{Bias}$

$$\tilde{u}$$
 (pie, full|hungry) =  $(1 - \alpha) * u$  (pie, full) +  $\alpha * u$  (pie, hungry)

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- Except for these mispredictions, the person's intertemporal preferences are as in discounted utility model (for ease, think  $\delta^{\times}$ .)

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A first type of evidence: underappreciation of the endowment effect.

### Loewenstein & Adler (EJ 1995)

Subjects: 27 CMU undergrads & 39 Pittsburgh MBA's.

#### Procedure:

- All subjects shown a mug, told they'll get one and have the opportunity to sell it for money.
- ▶ Half of the subjects predict how much they'd sell it for.
- After a delay, all subjects are given a mug and an opportunity to sell

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CMU:	Prediction Control	\$3.73	\$5.40 \$6.46
Pittsburgh:	Prediction Control	\$3.27	\$4.56 \$4.98

#### VanBoven, Dunning, & Loewenstein (JPSP 2000)

Study 2: Subjects were 43 Cornell undergraduates.

19 subjects randomly chosen to be "sellers" 24 subjects randomly chosen to be "buyers"

Each seller given a coffee mug. Each buyer shown a coffee mug.

- ► Elicit people's reservation prices
- Ask buyers to predict average reservation price of sellers, and ask sellers to predict average reservation price of buyers.

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	Reservation Price	Prediction for Other Group
Sellers:	\$6.37	\$3.93
Buyers:	\$1.85	\$4.39

A second type of evidence: underappreciation of the effects of hunger.

Read & van Leeuwen (OBHDP 1998)

Subjects were 200 employees at several firms in Amsterdam.

- ► Each subject asked to choose between a healthy vs. unhealthy snack to be received in one week.
- ► They varied subjects' expected future hunger and their current hunger.

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Results: % of Subjects Choosing Unhealthy Snack

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		Future	Hunger
		Hungry	Satiated
Current	Hungry	78%	42%
Hunger	Satiated	56%	26%

$$\blacktriangleright \ (\mathsf{Total} \ \mathsf{Utility}) = (\mathsf{Mug} \ \mathsf{Utility}) + (\mathsf{Money} \ \mathsf{Utility})$$

► (Total Utility) = 
$$u(c,r)$$
 +  $m$ 

Mug utility is 
$$u(c,r) = w(c) + v(c-r)$$
, where

$$w(c) = \mu * c$$
 and  $v(x) = \begin{cases} \phi x & \text{if } x \ge 0 \\ \lambda \phi x & \text{if } x \le 0 \end{cases}$ 

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Suppose buy/sell the mug in period 1, and (possibly) consume the mug in periods 1 & 2.

#### Consumption is:

- $ightharpoonup c_1 = c_2 = 1$  if buy or keep.
- $ightharpoonup c_1=c_2=0$  if don't buy or sell.

#### Initial reference point is exogenous:

- $ightharpoonup r_1 = 0 \iff \text{unendowed (buyers)}.$
- $ightharpoonup r_1 = 1 \Longleftrightarrow \text{ endowed (sellers)}$

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#### One can show:

- ▶ Sellers should sell iff  $P \ge P_S^* \equiv$
- ▶ Sellers actually sell iff  $P \ge P_S^A \equiv$
- ▶ Buyers should buy iff  $P \le P_B^* \equiv$
- ▶ Buyers actually buy iff  $P \le P_B^A \equiv$

#### Some Results:

(1) 
$$p_S^A > p_S^* \& p_B^A > p_B^*$$
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People are over-prone to consume goods to which they become accustomed because they underappreciate how they'll adapt — and more generally can lead to incorrect intertemporal utility maximization.

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$$p_S^A - p_B^A > p_S^* - p_B^*$$

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# Application: Projection Bias and Durable Goods

#### (Discussion courtesy of O'Donoghue)

#### Underlying environment:

▶ A durable good — e.g., a winter coat — yields a utility stream

$$\mu_1, \mu_2, ..., \mu_T.$$

▶ These  $\mu$ 's typically vary from day to day in a somewhat random way — for simplicity, let's assume that for all days the expected value of  $\mu_t$  is  $\bar{\mu}$ .

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On Day 1, when a person knows  $\mu_1$  but not the future  $\mu_t$ 's, how much is the person willing to pay for this durable good (assuming no discounting)?

▶ Optimal

$$WTP = \mu_1 + (T - 1)\bar{\mu}$$

▶ With Projection bias:

WTP = 
$$\mu_1 + (T - 1)[(1 - \alpha)\bar{\mu} + \alpha\mu_1]$$
  
=  $\mu_1 + (T - 1)[\bar{\mu} + \alpha(\mu_1 - \bar{\mu})]$ 

Hence: If  $\mu_1 > \bar{\mu}$  then overprone to buy. If  $\mu_1 < \bar{\mu}$  then underprone to buy

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<u>One extension</u>: Suppose that you have multiple opportunities to buy the durable good (and suppose that there are limits on your ability to return the good).

Case 1: Suppose  $P < T\bar{\mu}$ , so you SHOULD buy the good.

- You end up buying it as long as  $\mu_t \geq \bar{\mu}$  on at least one occasion, which is quite likely.
  - ⇒ Under-buying is very unlikely.

Case 2: Suppose  $P > T\bar{\mu}$ , so you should NOT buy the good.

Again, you end up buying it as long as  $\mu_t \geq \bar{\mu}$  or at least one occasion, which is quite likely.  $\Longrightarrow$  Over-buying is very LIKELY.

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Prediction: More returns for orders made on high-valuation days than for orders made on low-valuation days.

Big question: How can we assess whether a person orders on a high-valuation day vs. a low-valuation day?

Our answer: look at orders of winter-clothing items as a function of the weather.

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