HW 1 Report

Task 1

```
In [ ]:
```

```
! conda info
```

```
active environment : base
    active env location : /Users/dingzheyu/anaconda3
            shell level : 1
       user config file : /Users/dingzheyu/.condarc
populated config files : /Users/dingzheyu/.condarc
         conda version : 4.7.11
   conda-build version: 3.10.5
         python version: 3.6.5.final.0
       virtual packages :
       base environment : /Users/dingzheyu/anaconda3 (writable)
           channel URLs: https://repo.anaconda.com/pkgs/main/osx-64
                          https://repo.anaconda.com/pkgs/main/noarch
                          https://repo.anaconda.com/pkgs/r/osx-64
                          https://repo.anaconda.com/pkgs/r/noarch
          package cache : /Users/dingzheyu/anaconda3/pkgs
                          /Users/dingzheyu/.conda/pkgs
       envs directories : /Users/dingzheyu/anaconda3/envs
                          /Users/dingzheyu/.conda/envs
               platform : osx-64
             user-agent: conda/4.7.11 requests/2.18.4 CPython/3.6.5 Darwin/18.6.0
OSX/10.14.5
                UID:GID: 501:20
             netrc file : None
           offline mode : False
```

Task 2

```
In [1]:
```

```
import numpy as np
import scipy.linalg
```

```
In [2]:
```

```
a = np.random.randint(1, 10, (10, 10))
```

```
In [3]:
```

```
np.ndim(a)
```

Out[3]:

2

```
In [4]:
np.size(a)
Out[4]:
100
In [5]:
np.shape(a)
Out[5]:
(10, 10)
In [6]:
a.shape[1]
Out[6]:
10
In [7]:
np.array([[1.,2.,3.], [4.,5.,6.]])
Out[7]:
array([[1., 2., 3.],
       [4., 5., 6.]])
```

```
In [8]:
b = np.random.randint(1, 10, (10, 10))
c = np.random.randint(1, 10, (10, 10))
d = np.random.randint(1, 10, (10, 10))
np.block([[a,b], [c,d]])
Out[8]:
array([[3, 2, 9, 6, 1, 6, 1, 4, 5, 8, 2, 6, 2, 9, 6, 7, 4, 1, 5, 7],
                                                      2,
                                                         3, 4,
       [8, 5, 9, 3, 3,
                       5,
                          1, 9, 6, 8, 8, 9,
                                             2, 5,
                                                   5,
                                                               2,
       [2, 6, 9, 3, 1,
                       4,
                          1,
                             1,
                                7,
                                   7,
                                      6, 5, 1, 5, 9,
                                                      3,
                                                         3,
                                                            2,
                                                               9,
       [6, 7, 2, 5, 4, 8, 4, 5, 9, 9, 2, 3, 7, 8, 8, 4,
                                                        7, 9, 8, 3],
       [3, 5, 7, 8, 7, 8,
                          4, 6, 9, 8, 5, 2, 5, 4, 2, 8, 8, 8, 3, 7],
       [3, 8, 7, 9, 5, 4,
                             2, 4, 8, 2, 5,
                                             9, 2, 7,
                          9,
                                                      9,
                                                         3, 7, 7,
       [9, 6, 5, 2, 8,
                      4.
                          2,
                            7, 6, 6, 7, 4, 4, 6, 9, 9, 1,
       [9, 1, 6, 3, 1,
                      4,
                          3, 1, 8, 4, 2, 4, 3, 6, 5, 1,
                                                         7, 2, 1, 71,
                       6, 1, 7,
                                      3, 5, 1, 9, 7,
                                                      8,
       [6, 1,
              8, 9, 2,
                                7, 6,
                                                         8, 5, 7,
                                             6, 3, 4,
              3,
                 2, 6,
                       2,
                          2,
                             6,
                                2, 8,
                                      6, 4,
                                                      2,
                                                         3, 4,
       [9, 5, 6, 3, 3, 6, 8, 8, 9, 1, 1, 2, 9, 9, 7, 7,
                                                        3, 6, 6, 4],
       [8, 9, 2, 5, 6, 3, 2, 8, 1, 4, 1, 4, 5, 8, 9, 1, 2, 6, 5, 4],
                          2, 2, 5, 3, 1, 2,
                                             6, 6, 5, 2,
       [6, 9, 9, 7, 2, 6,
                                                         8, 6, 9,
                                                                  4],
       [2, 9, 8, 9, 1,
                       1, 8, 6, 6, 9, 2, 5,
                                            7, 3, 1, 5,
       [3, 4, 7, 2, 7, 3, 4, 5, 2, 7, 7, 2, 4, 6, 8, 9, 2, 4, 4, 8],
       [8, 3, 8, 8, 3, 4,
                          8, 5, 8, 2, 3, 6, 3, 5, 1, 2, 1, 2, 1, 2],
           2, 3, 4, 3, 1,
                          3,
                             3, 5, 3, 7, 6, 3, 3, 1, 9,
                                                         7, 1, 4,
       [6, 1, 4, 8, 9, 6, 2, 3, 4, 6, 6, 6, 8, 9, 4, 6, 3, 3, 7, 1],
       [8, 3, 5, 9, 5, 2, 9, 5, 5, 8, 2, 6, 8, 4, 7, 3, 2, 2, 2, 1],
       [3, 4, 9, 7, 9, 5, 4, 2, 9, 8, 7, 3, 9, 7, 2, 8, 3, 5, 1, 2]])
In [9]:
a[-1]
Out[9]:
array([9, 4, 3, 2, 6, 2, 2, 6, 2, 8])
In [10]:
a[1,4]
```

Out[10]:

3

```
In [11]:
print(a[0:5])
print(a[:5])
print(a[0:5,:])
[[3 2 9 6 1 6 1 4 5 8]
[8 5 9 3 3 5 1 9 6 8]
 [2 6 9 3 1 4 1 1 7 7]
 [6 7 2 5 4 8 4 5 9 9]
 [3 5 7 8 7 8 4 6 9 8]]
[[3 2 9 6 1 6 1 4 5 8]
 [8 5 9 3 3 5 1 9 6 8]
 [2 6 9 3 1 4 1 1 7 7]
 [6 7 2 5 4 8 4 5 9 9]
 [3 5 7 8 7 8 4 6 9 8]]
[[3 2 9 6 1 6 1 4 5 8]
 [8 5 9 3 3 5 1 9 6 8]
 [2 6 9 3 1 4 1 1 7 7]
 [6 7 2 5 4 8 4 5 9 9]
 [3 5 7 8 7 8 4 6 9 8]]
In [12]:
a[-5:]
Out[12]:
array([[3, 8, 7, 9, 5, 4, 9, 2, 4, 8],
       [9, 6, 5, 2, 8, 4, 2, 7, 6, 6],
       [9, 1, 6, 3, 1, 4, 3, 1, 8, 4],
       [6, 1, 8, 9, 2, 6, 1, 7, 7, 6],
       [9, 4, 3, 2, 6, 2, 2, 6, 2, 8]])
In [13]:
a[0:3][:,4:9]
Out[13]:
array([[1, 6, 1, 4, 5],
       [3, 5, 1, 9, 6],
       [1, 4, 1, 1, 7]])
In [14]:
a[([1,3],[0,2])]
Out[14]:
array([8, 2])
In [15]:
a[ 2:1:2,:]
Out[15]:
array([], shape=(0, 10), dtype=int64)
```

```
In [16]:
a[::2,:]
Out[16]:
array([[3, 2, 9, 6, 1, 6, 1, 4, 5, 8],
       [2, 6, 9, 3, 1, 4, 1, 1, 7, 7],
       [3, 5, 7, 8, 7, 8, 4, 6, 9, 8],
       [9, 6, 5, 2, 8, 4, 2, 7, 6, 6],
       [6, 1, 8, 9, 2, 6, 1, 7, 7, 6]])
In [17]:
a[::-1,:]
Out[17]:
array([[9, 4, 3, 2, 6, 2, 2, 6, 2, 8],
       [6, 1, 8, 9, 2, 6, 1, 7, 7, 6],
       [9, 1, 6, 3, 1, 4, 3, 1, 8, 4],
       [9, 6, 5, 2, 8, 4, 2, 7, 6, 6],
       [3, 8, 7, 9, 5, 4, 9, 2, 4, 8],
       [3, 5, 7, 8, 7, 8, 4, 6, 9, 8],
       [6, 7, 2, 5, 4, 8, 4, 5, 9, 9],
       [2, 6, 9, 3, 1, 4, 1, 1, 7, 7],
       [8, 5, 9, 3, 3, 5, 1, 9, 6, 8],
       [3, 2, 9, 6, 1, 6, 1, 4, 5, 8]])
In [18]:
a[:len(a),0]
Out[18]:
array([3, 8, 2, 6, 3, 3, 9, 9, 6, 9])
In [19]:
a.transpose()
Out[19]:
array([[3, 8, 2, 6, 3, 3, 9, 9, 6, 9],
       [2, 5, 6, 7, 5, 8, 6, 1, 1, 4],
       [9, 9, 9, 2, 7, 7, 5, 6, 8, 3],
       [6, 3, 3, 5, 8, 9, 2, 3, 9, 2],
       [1, 3, 1, 4, 7, 5, 8, 1, 2, 6],
       [6, 5, 4, 8, 8, 4, 4, 4, 6, 2],
       [1, 1, 1, 4, 4, 9, 2, 3, 1, 2],
       [4, 9, 1, 5, 6, 2, 7, 1, 7, 6],
       [5, 6, 7, 9, 9, 4, 6, 8, 7, 2],
       [8, 8, 7, 9, 8, 8, 6, 4, 6, 8]])
```

```
In [20]:
```

```
a.conj().transpose()
Out[20]:
array([[3, 8, 2, 6, 3, 3, 9, 9, 6, 9],
       [2, 5, 6, 7, 5, 8, 6, 1, 1, 4],
       [9, 9, 9, 2, 7, 7, 5, 6, 8, 3],
       [6, 3, 3, 5, 8, 9, 2, 3, 9, 2],
       [1, 3, 1, 4, 7, 5, 8, 1, 2, 6],
       [6, 5, 4, 8, 8, 4, 4, 4, 6, 2],
       [1, 1, 1, 4, 4, 9, 2, 3, 1, 2],
       [4, 9, 1, 5, 6, 2, 7, 1, 7, 6],
       [5, 6, 7, 9, 9, 4, 6, 8, 7, 2],
       [8, 8, 7, 9, 8, 8, 6, 4, 6, 8]])
In [21]:
a @ b
Out[21]:
array([[183, 208, 189, 245, 297, 207, 206, 205, 309, 243],
       [232, 280, 201, 326, 347, 256, 270, 219, 327, 323],
       [197, 213, 143, 225, 268, 189, 179, 179, 276, 211],
       [245, 289, 249, 333, 353, 317, 280, 290, 339, 311],
       [270, 293, 277, 360, 401, 342, 326, 338, 390, 352],
       [290, 278, 247, 328, 382, 301, 251, 317, 356, 253],
       [230, 265, 196, 318, 308, 283, 276, 235, 283, 314],
       [152, 196, 135, 260, 271, 239, 184, 167, 264, 241],
       [186, 237, 217, 320, 348, 258, 272, 245, 339, 306],
       [186, 207, 167, 250, 237, 210, 209, 179, 230, 235]])
In [22]:
a * b
Out[22]:
array([[ 6, 12, 18, 54, 6, 42,
                                 4, 4, 25, 561,
       [64, 45, 18, 15, 15, 10,
                                 3, 36, 12,
                                              8],
                        9, 12,
       [12, 30,
                9, 15,
                                 3,
                                    2, 63, 421,
       [12, 21, 14, 40, 32, 32, 28, 45, 72, 27],
       [15, 10, 35, 32, 14, 64, 32, 48, 27, 56],
       [ 6, 40, 63, 18, 35, 36, 27, 14, 28, 56],
       [63, 24, 20, 12, 72, 36,
                                2, 49, 30, 121,
             4, 18, 18, 5, 4, 21, 2, 8, 28],
       [18,
             5, 8, 81, 14, 48,
                                 8, 35, 49, 54],
       [18,
       [54, 16, 18, 6, 24,
                                 6, 24, 18, 24]])
                             4,
```

```
In [23]:
```

```
a / b
```

Out[23]:

```
, 0.33333333, 4.5
                                     , 0.66666667, 0.16666667,
array([[1.5
                                     , 1. , 1.14285714],
       0.85714286, 0.25 , 4.
                                                 , 0.6
      [1.
               , 0.55555556, 4.5
                                     , 0.6
                , 0.33333333, 2.25
                                      , 3.
                                                  , 8.
                                                             1,
                                      , 0.6
                                                 , 0.11111111,
      [0.33333333, 1.2
                      , 9.
                                  , 0.77777778, 1.16666667],
       1.33333333, 0.33333333, 0.5
               , 2.33333333, 0.28571429, 0.625
                                               , 0.5
      [3.
                , 0.57142857, 0.55555556, 1.125
                                                 , 3.
                                                             ],
       2.
                , 2.5
                         , 1.4
                                    , 2.
                                                 , 3.5
      [0.6
                , 0.5
                          , 0.75
                                                 , 1.142857141,
                                      , 3.
       1.
                , 1.6
                                                 , 0.71428571,
                           , 0.77777778, 4.5
      [1.5
                           , 0.28571429, 0.57142857, 1.14285714],
       0.44444444 . 3.
      [1.28571429, 1.5
                           , 1.25
                                    , 0.33333333, 0.88888889,
      0.44444444 2.
                          , 1.
                                     , 1.2
                                               , 3.
                          , 2.
                                     , 0.5
                                                 , 0.2
      [4.5]
               , 0.25
                                      , 8.
                                                 , 0.57142857],
      4.
                , 0.42857143, 0.5
               , 0.2
                                                 , 0.28571429,
      [2.
                       , 8.
                                     , 1.
               , 0.125
                           , 1.4
                                     , 1.
                                                 , 0.666666671,
       0.75
                                     , 0.66666667, 1.5
                , 1. , 0.5
      [1.5
                , 0.66666667, 1.5
                                    , 0.22222222, 2.6666666711)
       1.
```

In [24]:

```
a ** 3
```

Out[24]:

```
array([[ 27, 8, 729, 216, 1, 216,
                                    1, 64, 125, 512],
      [512, 125, 729, 27, 27, 125,
                                   1, 729, 216, 5121,
      [ 8, 216, 729, 27,
                                   1, 1, 343, 343],
                          1, 64,
                8, 125,
                                   64, 125, 729, 729],
                         64, 512,
      [216, 343,
      [ 27, 125, 343, 512, 343, 512,
                                  64, 216, 729, 512],
      [ 27, 512, 343, 729, 125, 64, 729, 8, 64, 512],
      [729, 216, 125, 8, 512, 64,
                                   8, 343, 216, 2161,
      [729, 1, 216,
                    27, 1, 64, 27, 1, 512, 64],
      [216, 1, 512, 729, 8, 216, 1, 343, 343, 216],
                     8, 216, 8,
      [729, 64, 27,
                                   8, 216, 8, 51211)
```

In [25]:

```
a > 0.5
```

Out[25]:

```
True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
array([[ True,
                 True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
                         True,
                                         True,
        [ True,
                 True,
                                 True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True],
        [ True,
                 True,
                         True,
                                 True,
                                         True,
                                                 True,
                                                        True,
                                                                True,
                                                                        True,
          True]])
```

```
In [26]:
```

```
np.nonzero(a>0.5)
Out[26]:
(array([0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2,
2,
        2, 2, 2, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 3, 3, 3, 3, 4, 4, 4,
4,
        4, 4, 4, 4, 4, 5, 5, 5, 5, 5, 5, 5, 5, 5, 6, 6, 6, 6, 6,
6,
        6, 6, 6, 6, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 8, 8, 8, 8, 8, 8, 8,
8,
        8, 8, 9, 9, 9, 9, 9, 9, 9, 9, 91),
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0,
1,
        2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2,
3,
        4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4,
5,
        6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, 1, 2, 3, 4, 5, 6,
7,
        8, 9, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9]))
In [27]:
v = np.random.randint(-2, 10, 10)
a[:,np.nonzero(v>0.5)[0]]
Out[27]:
array([[3, 2, 1, 1, 4, 8],
       [8, 5, 3, 1, 9, 8],
       [2, 6, 1, 1, 1, 7],
       [6, 7, 4, 4, 5, 9],
       [3, 5, 7, 4, 6, 8],
       [3, 8, 5, 9, 2, 8],
       [9, 6, 8, 2, 7, 6],
       [9, 1, 1, 3, 1, 4],
       [6, 1, 2, 1, 7, 6],
       [9, 4, 6, 2, 6, 8]])
In [28]:
a[:,v.T>0.5]
Out[28]:
array([[3, 2, 1, 1, 4, 8],
       [8, 5, 3, 1, 9, 8],
       [2, 6, 1, 1, 1, 7],
       [6, 7, 4, 4, 5, 9],
       [3, 5, 7, 4, 6, 8],
       [3, 8, 5, 9, 2, 8],
       [9, 6, 8, 2, 7, 6],
       [9, 1, 1, 3, 1, 4],
       [6, 1, 2, 1, 7, 6],
       [9, 4, 6, 2, 6, 8]])
```

```
In [29]:
a[a<0.5]=0
In [30]:
a * (a>0.5)
Out[30]:
array([[3, 2, 9, 6, 1, 6, 1, 4, 5, 8],
       [8, 5, 9, 3, 3, 5, 1, 9, 6, 8],
       [2, 6, 9, 3, 1, 4, 1, 1, 7, 7],
       [6, 7, 2, 5, 4, 8, 4, 5, 9, 9],
       [3, 5, 7, 8, 7, 8, 4, 6, 9, 8],
       [3, 8, 7, 9, 5, 4, 9, 2, 4, 8],
       [9, 6, 5, 2, 8, 4, 2, 7, 6, 6],
       [9, 1, 6, 3, 1, 4, 3, 1, 8, 4],
       [6, 1, 8, 9, 2, 6, 1, 7, 7, 6],
       [9, 4, 3, 2, 6, 2, 2, 6, 2, 8]])
In [31]:
a[:] = 3
In [32]:
y = a.copy()
In [33]:
y = a[1,:].copy()
In [34]:
y = a.flatten()
In [35]:
np.arange(1.,11.)
Out[35]:
array([ 1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
In [36]:
np.arange(10.)
Out[36]:
array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
In [37]:
np.arange(1.,11.)[:]
Out[37]:
array([ 1., 2., 3., 4., 5., 6., 7., 8., 9., 10.])
```

```
In [38]:
np.zeros((3,4))
Out[38]:
array([[0., 0., 0., 0.],
      [0., 0., 0., 0.],
       [0., 0., 0., 0.]]
In [39]:
np.ones((3,4))
Out[39]:
array([[1., 1., 1., 1.],
       [1., 1., 1., 1.],
       [1., 1., 1., 1.]])
In [40]:
np.eye(3)
Out[40]:
array([[1., 0., 0.],
       [0., 1., 0.],
       [0., 0., 1.]])
In [41]:
np.diag(a)
Out[41]:
array([3, 3, 3, 3, 3, 3, 3, 3, 3])
In [42]:
np.diag(a,0)
Out[42]:
array([3, 3, 3, 3, 3, 3, 3, 3, 3])
In [43]:
np.random.rand(3,4)
Out[43]:
array([[0.30684848, 0.98428237, 0.76974404, 0.95529201],
       [0.94798779, 0.64498183, 0.61244636, 0.92778866],
       [0.69491876, 0.89019147, 0.18871753, 0.09431126]])
```

```
In [44]:
np.linspace(1,3,4)
Out[44]:
                  , 1.66666667, 2.333333333, 3.
array([1.
                                                       ])
In [45]:
np.mgrid[0:9.,0:6.]
Out[45]:
array([[[0., 0., 0., 0., 0., 0.],
        [1., 1., 1., 1., 1., 1.],
        [2., 2., 2., 2., 2., 2.],
        [3., 3., 3., 3., 3., 3.],
        [4., 4., 4., 4., 4., 4., 4.]
        [5., 5., 5., 5., 5., 5.],
        [6., 6., 6., 6., 6., 6.],
        [7., 7., 7., 7., 7., 7.],
        [8., 8., 8., 8., 8., 8.]],
       [[0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.],
        [0., 1., 2., 3., 4., 5.]])
In [46]:
np.ogrid[0:9.,0:6.]
Out[46]:
[array([[0.],
        [1.],
        [2.],
        [3.],
        [4.],
        [5.],
        [6.],
        [7.],
        [8.]]), array([[0., 1., 2., 3., 4., 5.]])]
In [47]:
np.meshgrid([1,2,4],[2,4,5])
Out[47]:
[array([[1, 2, 4],
        [1, 2, 4],
        [1, 2, 4]]), array([[2, 2, 2],
        [4, 4, 4],
        [5, 5, 5]])]
```

```
In [48]:
np.tile(a, (100, 1))
Out[48]:
array([[3, 3, 3, ..., 3, 3, 3],
       [3, 3, 3, \ldots, 3, 3, 3]])
In [49]:
np.concatenate((a,b),1)
np.hstack((a,b))
np.column stack((a,b))
Out[49]:
array([[3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 2, 6, 2, 9, 6, 7, 4, 1, 5, 7],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 8, 9, 2, 5, 5, 2, 3, 4, 2, 1],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 6, 5, 1, 5, 9, 3, 3, 2, 9, 6],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 2, 3, 7, 8, 8, 4, 7, 9, 8, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 5, 2, 5, 4, 2, 8, 8, 8, 3, 7],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 2, 5, 9, 2, 7, 9, 3, 7, 7, 7],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 7, 4, 4, 6, 9, 9, 1, 7, 5, 2],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 2, 4, 3, 6, 5, 1, 7, 2, 1, 7],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 5, 1, 9, 7, 8, 8, 5, 7, 9],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 6, 4, 6, 3, 4, 2, 3, 4, 9, 3]])
In [50]:
a.max()
Out[50]:
3
In [51]:
a.max(0)
```

array([3, 3, 3, 3, 3, 3, 3, 3, 3])

Out[51]:

```
In [52]:
```

```
np.maximum(a, b)
Out[52]:
array([[3, 6, 3, 9, 6, 7, 4, 3, 5, 7],
       [8, 9, 3, 5, 5, 3, 3, 4, 3, 3],
       [6, 5, 3, 5, 9, 3, 3, 3, 9, 6],
       [3, 3, 7, 8, 8, 4, 7, 9, 8, 3],
       [5, 3, 5, 4, 3, 8, 8, 8, 3, 7],
       [3, 5, 9, 3, 7, 9, 3, 7, 7,
       [7, 4, 4, 6, 9, 9, 3, 7, 5, 3],
       [3, 4, 3, 6, 5, 3, 7, 3, 3, 7],
       [3, 5, 3, 9, 7, 8, 8, 5, 7, 9],
       [6, 4, 6, 3, 4, 3, 3, 4, 9, 3]])
In [53]:
np.sqrt(v @ v)
Out[53]:
10.14889156509222
In [54]:
np.logical and(a,b)
Out[54]:
array([[ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                               True,
                                                                      True,
         True],
       [ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                              True,
                                                                      True,
         True],
       [ True,
                                                       True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                               True,
                                                                      True,
         True],
       [ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                               True,
                                                                      True,
         True],
       [ True,
                         True,
                                                       True,
                                                               True,
                 True,
                                True,
                                        True,
                                               True,
                                                                      True,
         True],
       [ True,
                                        True,
                 True,
                         True,
                                True,
                                               True,
                                                       True,
                                                              True,
                                                                      True,
         True],
       [ True,
                                                              True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                                      True,
         True],
       [ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                               True,
                                                                      True,
         True],
       [ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                               True,
                                                                      True,
         True],
       [ True,
                 True,
                         True,
                                True,
                                        True,
                                               True,
                                                       True,
                                                               True,
                                                                      True,
         True]])
```

```
In [55]:
a & b
Out[55]:
array([[2, 2, 2, 1, 2, 3, 0, 1, 1, 3],
       [0, 1, 2, 1, 1, 2, 3, 0, 2, 1],
       [2, 1, 1, 1, 1, 3, 3, 2, 1, 2],
       [2, 3, 3, 0, 0, 0, 3, 1, 0, 3],
       [1, 2, 1, 0, 2, 0, 0, 0, 3, 3],
       [2, 1, 1, 2, 3, 1, 3, 3, 3, 3],
       [3, 0, 0, 2, 1, 1, 1, 3, 1, 2],
       [2, 0, 3, 2, 1, 1, 3, 2, 1, 3],
       [3, 1, 1, 1, 3, 0, 0, 1, 3, 1],
       [2, 0, 2, 3, 0, 2, 3, 0, 1, 3]])
In [56]:
a b
Out[56]:
array([[ 3, 7,
                  3, 11,
                          7,
                               7,
                                   7,
                                       3,
                                            7,
                                                7],
                                   3,
                                        7,
       [11, 11,
                  3,
                      7,
                          7,
                               3,
                                            3,
                                                31,
       [7,
              7,
                  3,
                      7, 11,
                               3,
                                   3,
                                        3, 11,
                                                7],
                  7, 11, 11,
                              7,
       [ 3,
              3,
                                   7, 11, 11,
                                                3],
                  7,
                           3, 11, 11, 11,
       [ 7,
             3,
                      7,
                                            3,
                                                7],
                          7, 11,
       [ 3,
              7, 11,
                      3,
                                   3,
                                        7,
                                            7,
                                                7],
                      7, 11, 11,
       [7,
              7,
                  7,
                                   3,
                                       7,
                                            7,
                                                3],
                      7,
                              3,
       [ 3,
             7,
                 3,
                          7,
                                   7,
                                       3, 3,
                                                71,
                          7, 11, 11,
       [ 3,
             7,
                  3, 11,
                                       7,
                                           7, 11],
       7,
                           7,
                  7,
                      3,
                               3,
                                   3,
                                        7, 11,
                                                3]])
In [57]:
np.linalg.inv(a[1:2, 1:2])
```

Out[57]:

```
array([[0.33333333]])
```

```
In [58]:
```

```
np.linalg.pinv(a)
```

```
Out[58]:
```

```
array([[0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.00333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333331,
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.00333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333331,
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333331,
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.003333333, 0.003333333, 0.003333333, 0.003333333],
       [0.00333333, 0.00333333, 0.00333333, 0.00333333, 0.00333333,
        0.00333333, 0.00333333, 0.003333333, 0.003333333, 0.003333331])
```

In [59]:

```
np.linalg.matrix_rank(a)
```

Out[59]:

1

```
In [60]:
```

```
np.linalg.lstsq(a,b)
```

/Users/dingzheyu/anaconda3/lib/python3.6/site-packages/ipykernel_launc her.py:1: FutureWarning: `rcond` parameter will change to the default of machine precision times ``max(M, N)`` where M and N are the input m atrix dimensions.

To use the future default and silence this warning we advise to pass `rcond=None`, to keep using the old, explicitly pass `rcond=-1`.
"""Entry point for launching an IPython kernel.

```
Out[60]:
```

```
(array([[0.14333333, 0.15666667, 0.13333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                       , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.133333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                        , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                       , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.1733333
3]]),
array([], dtype=float64),
array([3.00000000e+001, 5.83700565e-016, 8.75811540e-047, 5.48350007e
-078,
        2.62450743e-109, 5.36630706e-142, 2.95853564e-175, 0.00000000e
+000,
        0.00000000e+000, 0.0000000e+000]))
```

In [61]:

```
U, S, Vh = np.linalg.svd(np.random.randint(1, 9, (10, 10, 10)))
V = Vh.T
```

In [62]:

```
np.linalg.cholesky(np.random.randint(1, 2, (1, 1))).T
```

Out[62]:

array([[1.]])

In [63]:

```
D,V = np.linalg.eig(a)
```

In [64]:

```
D,V = scipy.linalg.eig(a,b)
```

In [65]:

```
Q,R = scipy.linalg.qr(a)
```

In [66]:

```
LU,P = scipy.linalg.lu_factor(a)
```

/Users/dingzheyu/anaconda3/lib/python3.6/site-packages/ipykernel_launc her.py:1: LinAlgWarning: Diagonal number 2 is exactly zero. Singular m atrix.

"""Entry point for launching an IPython kernel.

In [67]:

```
np.fft.fft(a)
```

Out[67]:

```
0.+0.j, 0.+0.j, 0.+0.j,
array([[30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                                                 0.+0.j
         0.+0.j
                  0.+0.j,
                           0.+0.j1,
       [30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j,
                                              0.+0.j
                                                        0.+0.j,
                                                                 0.+0.j
         0.+0.j,
                  0.+0.j,
                           0.+0.j],
       [30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j,
                                              0.+0.j,
                                                       0.+0.j,
                                                                 0.+0.j,
         0.+0.j,
                  0.+0.j
                           0.+0.j1,
                  0.+0.j,
                           0.+0.j,
                                              0.+0.j
                                                        0.+0.j
       [30.+0.j,
                                     0.+0.j,
                                                                 0.+0.j
         0.+0.j,
                  0.+0.j,
                           0.+0.j1,
                                                                 0.+0.j,
       [30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j,
                                              0.+0.j,
                                                        0.+0.j,
         0.+0.j,
                  0.+0.j,
                           0.+0.j],
                           0.+0.j,
                                     0.+0.j,
                                              0.+0.j,
                                                        0.+0.j,
       [30.+0.j,
                  0.+0.j,
                                                                 0.+0.j,
         0.+0.j,
                  0.+0.j,
                           0.+0.j],
       [30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j
                                              0.+0.j,
                                                        0.+0.j
                                                                 0.+0.j
         0.+0.j,
                  0.+0.j,
                           0.+0.j],
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j,
                                              0.+0.j,
                                                        0.+0.j,
       [30.+0.j,
                                                                 0.+0.j
                           0.+0.j],
         0.+0.j,
                  0.+0.j,
       [30.+0.j,
                  0.+0.j
                           0.+0.j,
                                     0.+0.j
                                              0.+0.j,
                                                        0.+0.j
                                                                 0.+0.j
         0.+0.j,
                  0.+0.j,
                           0.+0.j],
       [30.+0.j,
                  0.+0.j,
                           0.+0.j,
                                     0.+0.j,
                                             0.+0.j, 0.+0.j, 0.+0.j,
         0.+0.j,
                  0.+0.j,
                           0.+0.j]])
```

```
In [68]:
```

np.fft.ifft(a)

```
Out[68]:
array([[3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.])
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j]
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j],
       [3.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j, 0.+0.j
j,
        0.+0.j, 0.+0.j]])
In [69]:
np.sort(a)
Out[69]:
array([[3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3],
       [3, 3, 3, 3, 3, 3, 3, 3, 3]])
In [70]:
I = np.argsort(a[:,1])
```

```
In [71]:
```

```
np.linalg.lstsq(a,b)
```

/Users/dingzheyu/anaconda3/lib/python3.6/site-packages/ipykernel_launc her.py:1: FutureWarning: `rcond` parameter will change to the default of machine precision times ``max(M, N)`` where M and N are the input m atrix dimensions.

To use the future default and silence this warning we advise to pass `rcond=None`, to keep using the old, explicitly pass `rcond=-1`.
"""Entry point for launching an IPython kernel.

```
Out[71]:
```

```
(array([[0.14333333, 0.15666667, 0.13333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                       , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                        , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                        , 0.20666667,
        [0.14333333, 0.15666667, 0.133333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                       , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
                                                        , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.156666667, 0.163333333, 0.18666667, 0.17333333],
                                                        , 0.20666667,
        [0.14333333, 0.15666667, 0.13333333, 0.19
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.13333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.17333333],
        [0.14333333, 0.15666667, 0.133333333, 0.19
                                                        , 0.20666667,
         0.17666667, 0.15666667, 0.16333333, 0.18666667, 0.1733333
3]]),
 array([], dtype=float64),
array([3.0000000e+001, 5.83700565e-016, 8.75811540e-047, 5.48350007e
-078,
        2.62450743e-109, 5.36630706e-142, 2.95853564e-175, 0.00000000e
+000,
        0.0000000e+000, 0.0000000e+000]))
```

In [72]:

```
np.unique(a)
```

```
Out[72]:
```

array([3])

```
In [73]:
```

Task 3

```
In [74]:
```

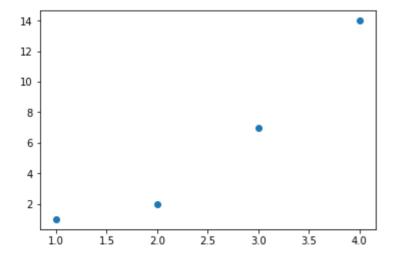
```
import matplotlib.pyplot as plt
plt.plot([1,2,3,4], [1,2,7,14])
plt.axis([0, 6, 0, 20])
plt.show()
```

<Figure size 640x480 with 1 Axes>

Task 4

```
In [75]:
```

```
plt.scatter([1,2,3,4], [1,2,7,14])
plt.show()
```



Task 5

Acccount name: BenDing96

Task 6

https://github.com/BenDing96/Deep-Learning (https://github.com/BenDing96/Deep-Learning)

In []:		