Electrical & Computer Engineering Department National University of Singapore

EE2011 Engineering Electromagnetics Tutorial 5: Magnetic Fields

The tutorial discussion will focus on Questions 2 and 3 (which are marked by asterisks *).

1. BASICS

- (a) A charged particle is initially travelling with velocity $\vec{v} = v_1 \hat{u}_x + v_2 \hat{u}_z$ (where v_1 and v_2 are constants). What do you expect to observe after it enters a region with uniform magnetic field $\vec{B} = B_0 \hat{u}_z$ (where B_0 is a constant)?
- (b) Figure 1(b) depicts a current-carrying wire (formed by circular segments and radial lengths). Derive an expression for the magnetic flux density vector at P (which is the common center of the circular segments with radii a and b).

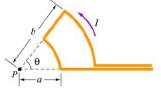


Figure 1(b)

- (c) A thin circular disk of radius r_0 rotates with angular speed ω . Show that the magnetic field strength at the center of the disk (with uniform surface charge density σ) is given by $B = \frac{1}{2} \mu_0 \sigma \omega r_0$.
- 2. * Figure 2 depicts a rectangular wire loop (of length *l* and width *w*) which is placed in the vicinity of a long straight wire. Determine the mutual impedance between these two (with separation *s*).

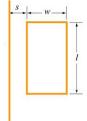
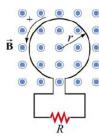


Figure 2

3. * Figure 3(a) depicts a circular wire loop (with radius r = 50 cm) which is connected to a resistor (with resistance $R = 100 \Omega$). The uniform magnetic field \vec{B} in the vicinity varies with time t in accordance with the plot reproduced in Figure 3(b). Sketch the variation of the current flowing in R as a function of time t, given that \vec{B} is in the +z direction (as denoted by the circles with enclosed dots) and the corresponding positive convention for the circular loop is given by the faint arrow.



5.0 0 2 4 6 8 10 second

Figure 3(a)

Figure 3(b)

4. Engineers often employ Helmholz coils to provide a region with sufficiently uniform magnetic field. As shown in Figure 4, the basic set-up comprises two identical coils that are symmetrically equidistant from the origin of the Cartesian coordinate system. Both coils have N turns of wire, radius R, current I and +z orientation.

Derive an expression for the magnetic field at any point on the z-axis and show that its first-order derivative is zero (i.e. $\frac{\partial B}{\partial z} = 0$) at the coordinate-system origin.

Derive the design condition for its second-order derivative to be zero (i.e. $\frac{\partial^2 B}{\partial z^2} = 0$) as well at the coordinate-system origin.

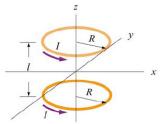


Figure 4

Answers:

$$1(b)$$
 $\frac{\mu_o I \theta}{4\pi} \left(\frac{1}{a} - \frac{1}{b} \right)$

$$2 \qquad \frac{\mu_0 l}{2\pi} \ln \left(1 + \frac{w}{s}\right)$$