

**NATIONAL UNIVERSITY OF SINGAPORE  
SCHOOL OF COMPUTING**

EXAMINATION FOR  
Semester 2, 2009/2010

**CS3241 - COMPUTER GRAPHICS**

Apr/May 2010

Time Allowed: 2 Hours

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**INSTRUCTION TO CANDIDATES**

1. This is an OPEN book examination.
2. This examination paper contains **EIGHT (8)** questions and comprises **EIGHT (8)** printed pages.
3. Answer **ALL** questions within the spaces provided in this booklet.
4. You are allowed to use the back of the paper but please remember to state "P.T.O."
5. ***Cross out any draft*** or otherwise we will mark the poorer answers.
6. No calculator should be needed in this exam. You can leave your answer in surd form, namely, you can write  $\sqrt{2}$  instead of 1.4142...
7. In the programming questions, you can assume some basic normal vector arithmetic functions are provided for the 2D vector class `Vector`.
8. Please write your matriculation number below, but NOT your name.

**TIDINESS COUNTS!**

We will deduct marks if your writing is too messy.

**MATRICULATION NUMBER:** \_\_\_\_\_

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**(this portion is for examiner's use only)**

Question	Max. Marks	Score	Check
Q1	9		
Q2	8		
Q3	5		
Q4	8		
Q5	4		
Q6	5		
Q7	4		
Q8	7		
Total	50		

**Question 1 [9 marks]**

You are given 9 statements below. State if each statement is True (T) or False (F) by writing your answer in the box provided. A correct answer will give you 1 mark. An empty answer will give you zero, but **a wrong answer will result in -1 mark**. (Lowest mark for this question is 0)

☐

Texture mapping is done after projection transformation

☐

If we clip a convex polygon with the screen, the clipped polygon could have more than one connected components (meaning, more than one piece).

☐

If we have a lot of opaque polygons overlapping each other on the screen after projection and each of them has a very large area by itself before overlapping, depth sort is faster than z-buffer algorithm.

☐

We use high pass filters to filter the low frequency portion of an image to do anti-aliasing.

☐

In OpenGL, if we called `glRotatef` to rotate an object, e.g. a Bezier surface, we have to calculate the new normal vectors by ourselves after rotation when we call `glNormal` because the objects are rotated and the normal vectors will all have new directions.

☐

We can call OpenGL function `glScalef()` with only one parameter, e.g. `glScalef(2.0)`, to scale our objects if all the scaling factors are the same for the three dimensions  $x, y$  and  $z$ .

☐

In ray-tracing, we can apply Gouraud shading techniques if the shadow ray does not intersect any objects but only reaching a light source.

☐

The bottle neck of ray-tracing is object-ray intersection.

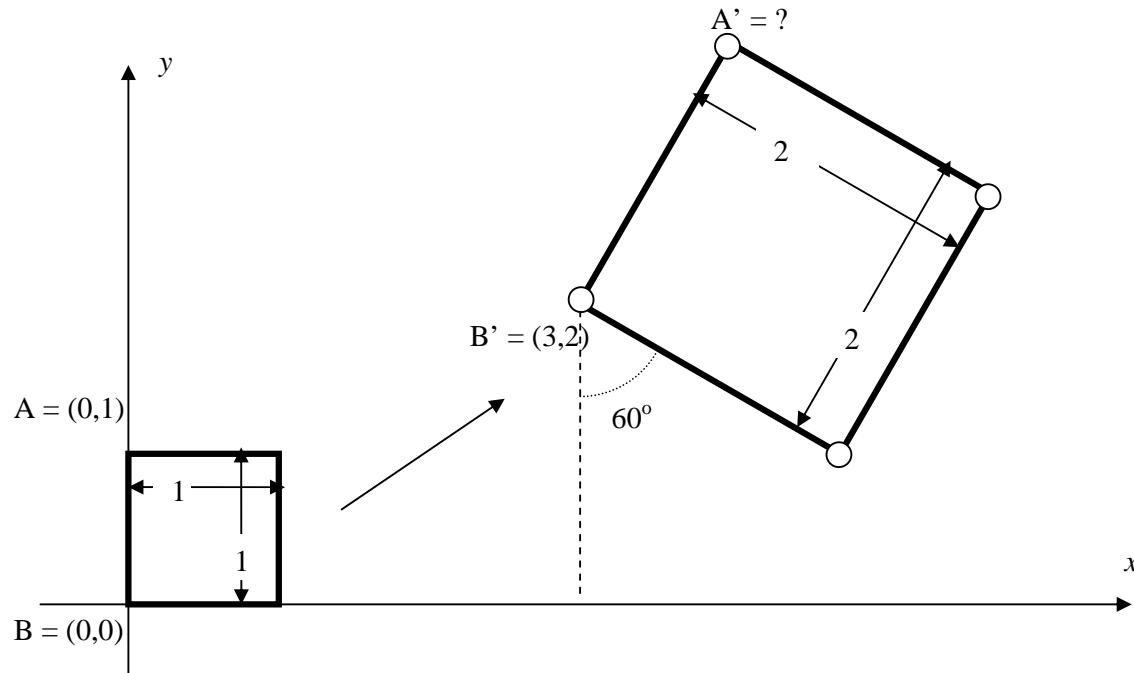
☐

Diffuse reflection is not viewer dependent.

**Question 2 [8 marks]**

The below diagram shows a complicated 2D transformation applied to a unit square.

- The overall transformation can be described in terms of a number of simpler transformations. Describe each of these simple transformations and write them down in OpenGL code. Note that the order of the transformation is important. Assuming the function `drawAUnitSquare()` will do the job of drawing a unit square (the left one) as shown in the diagram.
- Calculate the coordinate of  $A'$  after transformation.



```
void myDisplay()
{
    // Assuming the color buffer is cleared, the correct
    // model matrix is selected, etc..

    glLoadIdentity();

    drawAUnitSquare();
}
```

**Question 2 (Cont.)****Question 3 [5 marks]**

Please describe one or two special techniques used in modeling the following objects/phenomena (1 mark for each correct technique, maximum 5 marks):

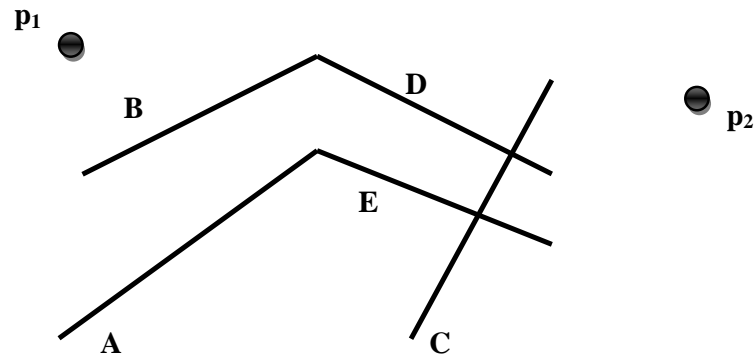
- a.* A piece of newspaper
  
  
  
  
  
  
  
  
  
  
- b.* The scales of a fish (when they are on the fish)
  
  
  
  
  
  
  
  
  
  
- c.* The trajectory of a flying homing missile in the sky.
  
  
  
  
  
  
  
  
  
  
- d.* The thousands of audience sitting in the stadium in a real time football video game

**Question 4 Tree [8 marks]**

The following FIVE lines are the cross sections of five polygons in a 3D space.

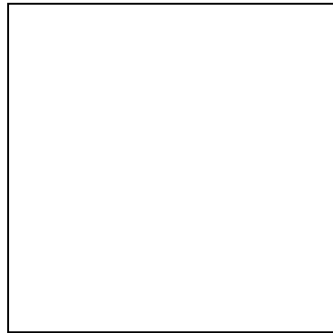
- Construct their BSP tree according to the priority  $A > B > C > D > E$ .
- Give the order of polygons to be drawn from the viewpoints  $p_1$  and  $p_2$ .

(Use dash lines in the diagram to help AND show your construction)

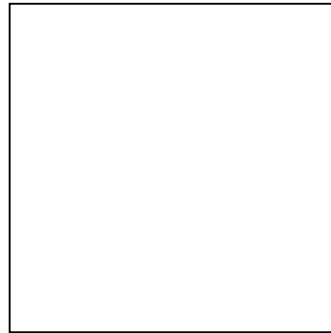


**Question 5 [4 marks]**

A stage is set by a square (a single polygon) on the  $xz$ -plane with  $y=0$ . The four corners of the squares are  $(-10, 0, -10)$ ,  $(-10, 0, 10)$ ,  $(10, 0, 10)$  and  $(10, 0, -10)$ . A white spot light (the only lighting, and all ambient lights are set to be 0) is set up at the position  $(0, 5, 0)$  with a direction downwards  $(0, -1, 0)$  and cut off angle 45 degree. We just want the spot light to be a simple circle and that is why we set the spotlight exponent to be  $n = 0$ . Briefly draw what the highlight of the stage by using Gouraud and Phong shadings separately. The squares below are the stage squares.



Gouraud  
Shading



Phong  
Shading

**Question 6 [5 marks]**

A student wants to draw a unit sphere (with radius 1) centered at the origin with OpenGL. He set the viewing as following:

```
glMatrixMode(GL_MODELVIEW);
gluLookAt( 10, 10, 10, 0, 0, 0, 0, 0, 1);
glMatrixMode(GL_PROJECTION);
glLoadIdentity();
gluPerspective(45, 1.0, 1.0, 10.0 );
```

Can he see the sphere? Give explanation to support your “yes” or “no”. If it’s a “yes”, draw and explain why the sphere can be seen. If it is a “no”, give the best and minimal correction to the code so that he can see the sphere.

**Question 7 [4 marks]**

Given three control points  $p_0$ ,  $p_1$ , and  $p_2$  and the Bezier equation:

$$p(t) = \sum_{i=0}^2 b_{2,i}(t) p_i \qquad b_{2,i}(t) = \binom{2}{i} (1-t)^{2-i} t^i$$

- a) Compute the differentiation  $p'(t)$  of  $p(t)$
- b) Compute  $p'(0)$  and  $p'(1)$

**Question 8 [7 marks]**

There are four spheres in the space with centers  $A:(0,4,7)$ ,  $B:(0,1,-10)$ , and  $C:(0,2,8)$  and  $D:(0, 1 \ 13)$ . They all have the same radius of 2 units. A ray starts tracing from the eye which is at the point,  $(0,1,0)$  with direction  $(0,0,1)$ . Compute all the intersections of the ray with the spheres and their “ $t$ ” values. Which is the first sphere that is hit by the ray? Explain your answers.

- END OF PAPER -