NATIONAL UNIVERSITY OF SINGAPORE

Department of Mathematics

MA1506 Laboratory 3 (MATLAB) Comments and Suggested Solutions Semester II 2010/2011

Exercise 3

1. 716.25

2. 70. From the information available,
$$M = \begin{bmatrix} 0.7 & 0.2 & 0.3 \\ 0.2 & 0.5 & 0.3 \\ 0.1 & 0.3 & 0.4 \end{bmatrix}$$
. The 'brute force' way

to compute the long run behaviour is to just calculate very large powers of M and compare the values of the entries.

In the first command, we can see that the difference between the entries in M^{200} and M^{100} are less than 10^{-14} . So we are sufficiently confident that M^{100} is close enough to the long run value. Alternatively, we can do things properly by diagonalizing M and taking limits.

```
>> [P D] =eig(M)
>> D1= diag( [ 1 0 0 ])
>> P*D1*inv(P)*[100; 100; 100]
```

The **diag** command creates a diagonal matrix with the entries specified. It is clear that D1 is the limit of D^n as n gets large.

- 3. 104 million
- 4. Eigenvalues are -4, 3 and 3.
- 5. In this case we have complex eigenvalues $\pm i$ and note that P is also a matrix with complex entries.

In this case, we have the eigenvalue 5 repeated 3 times, and the determinant of P is approximately zero. Actually, matrix A is not diagonalizable and the determinant of P should be exactly zero. This slight error is due to the algorithm used by the **eig** function.