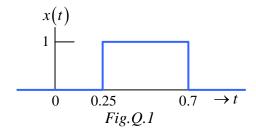
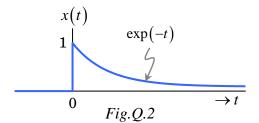
## EE2023 TUTORIAL 4 (PROBLEMS)

Q.1 The signal x(t) shown in Fig.Q.1 is sampled at 5 Hz to form a continuous-time signal  $\tilde{x}(t)$ . Let  $\tilde{X}(f)$  be the spectrum of  $\tilde{x}(t)$ . Sketch and label  $\tilde{x}(t)$ ,  $\left|\tilde{X}(f)\right|$  and  $\angle \tilde{X}(f)$ .



Q.2 The signal x(t) shown in Fig.Q.2 is sampled at 0.25 Hz to form a continuous-time signal  $\tilde{x}(t)$ . Let  $\tilde{X}(f)$  be the spectrum of  $\tilde{x}(t)$ . Determine  $\tilde{X}(f)$  and show that it is periodic.

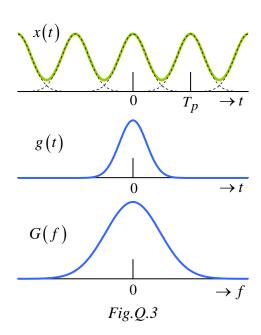


Q.3 Fig.Q.3 shows a periodic signal

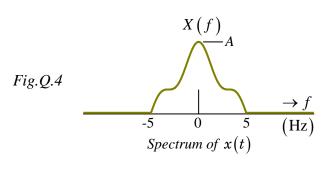
$$x(t) = \sum_{n = -\infty}^{\infty} g(t - nT_p)$$

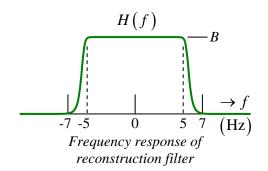
and its generating function g(t) which has a Fourier transform of G(f).

Let X(f) and  $X_k$  be the Fourier transform and Fourier series coefficients of x(t), respectively. Show how X(f) can be obtained directly from G(f). What is the relationship between  $X_k$  and G(f)? Is the generation function of a periodic signal unique, and why?



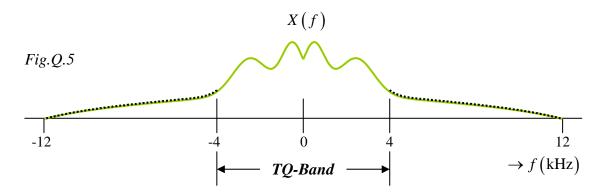
Q.4 A signal x(t) is sampled, stored and later reconstructed from the stored samples using a reconstruction filter. The spectrum of x(t) and the frequency response of the reconstruction filter are shown in Fig.Q.4. What is the Nyquist sampling frequency for x(t)? What sampling frequency would you recommend so that x(t) can be reconstructed from its samples without distortion, and why? Illustrate your answer.





Q.5 Speech studies have shown that perceptual cues pertaining to speech intelligibility and speaker identity are mainly found within the first 4 kHz of a speech spectrum. We shall refer to this frequency band as the TQ-Band, where TQ stands for 'Telephone Quality'.

The spectrum of a speech signal x(t) is shown in Fig.Q.5 where the TQ-Band is indicated.



In order to send x(t) over a digital telephone network, the first step is to sample x(t) without corrupting its TQ-Band. Suggest a method for sampling x(t) in each of the following situations.

**Situation A:** Anti-aliasing lowpass filter is not available and frequency aliasing

is prohibited.

**Situation B:** Lowest sampling frequency must be used at all cost.

**Situation C:** Anti-aliasing lowpass filter is not available and frequency aliasing

is permitted.

Comment on the advantage and disadvantage of each method.

## Additional Practice Problems

These problems will not be discussed in class.

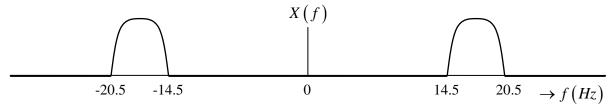
S.1 A bandlimited lowpass signal x(t) of bandwidth 20(kHz) is sampled at a rate of  $f_s$  samples/sec to form  $x_s(t)$ .  $x_s(t)$  is then sent through a reconstruction filter having frequency response H(f) so that x(t) is exactly reproduced at the filter's output. Find the smallest applicable value of  $f_s$  and specify the corresponding H(f).

Answer:  $f_S = 40 \text{ kHz}$ ,  $H(f) = \frac{1}{40000} \cdot \text{rect}\left(\frac{f}{40000}\right)$ 

- S.2 The sampled version of a signal x(t) in Problem S.1 has the form  $x_s(t) = \sum_{n=-5}^{5} x(5n)\delta(t-5n)$ .
  - (a) Determine the sampling frequency used.
  - (b) Can x(t) can be perfectly reconstructed from  $x_s(t)$ , and why?

Answer: (a) 0.2 Hz (b) No, (?)

S.3 The spectrum of a bandpass signal x(t) is shown in the figure below.



- (a) What is the Nyquist sampling frequency for x(t).
- (b) Determine the lowest sampling frequency that can be used so that x(t) may be reconstructed from its sampled version without distortion.

Answer: (a) 41 Hz (b) 7 Hz

Below is a list of solved problems selected from Chapter 5 of Hwei Hsu (PhD), 'The Schaum's series on Signals & Systems,' 2<sup>nd</sup> Edition.

The 1<sup>st</sup> Edition can be found in the following link: <a href="http://www.kousik.net/wp-content/uploads/2010/10/Schaums-Outline-Series-Signals\_Systems.pdf">http://www.kousik.net/wp-content/uploads/2010/10/Schaums-Outline-Series-Signals\_Systems.pdf</a>

Selected solved-problems: 5.58, 5.59, 5.60

These solved problems should be treated as supplementary module material catered for students who find the need for more examples or practice-problems