



CS3241 Computer Graphics

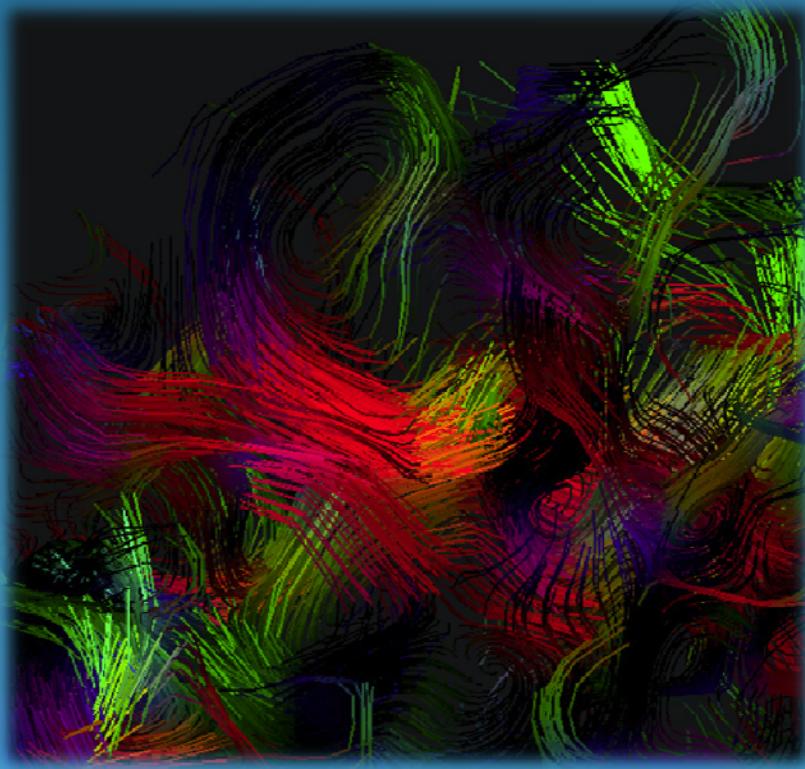
Remember there is a Facebook Page

<https://www.facebook.com/NUSCG>

C++

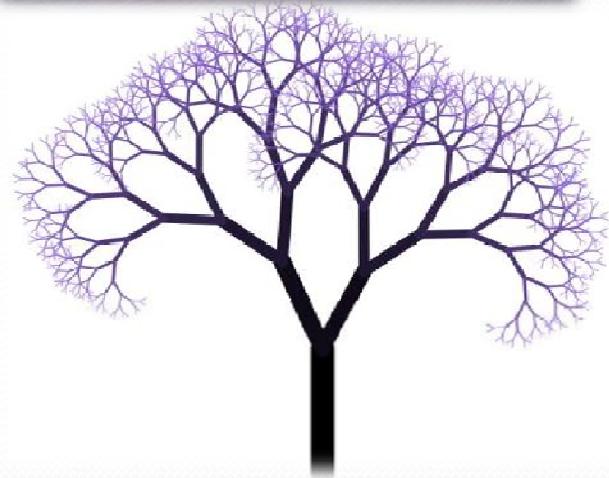
- Download “Microsoft Visual Studio Professional”
2008/2010/2012
 - Not Express!
 - You may need an SOC account if you are not from SOC
 - Please get an account from the helpdesk at COM1
- Please do it this week
- http://msdn70.e-academy.com/elms/Storefront/Home.aspx?campus=socnusingapore_cs

2D Graphics and OpenGL Primer



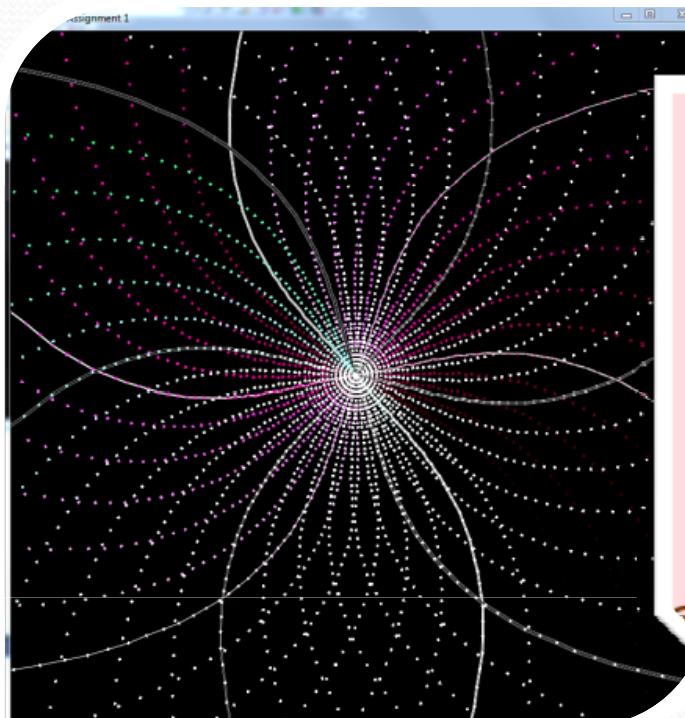
Goal of Today

- Everyone can draw some profound pictures in 2D



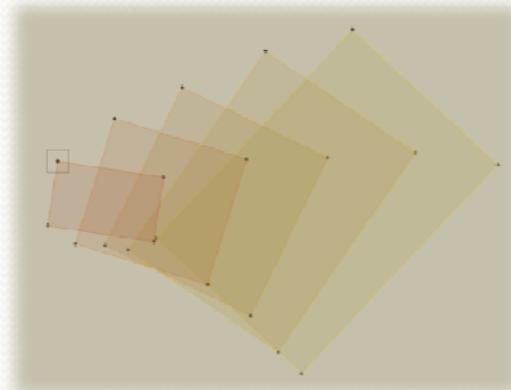
What you can do after today

- Games and animations in 2D
 - *With OpenGL, GLUT and C++*



Approach

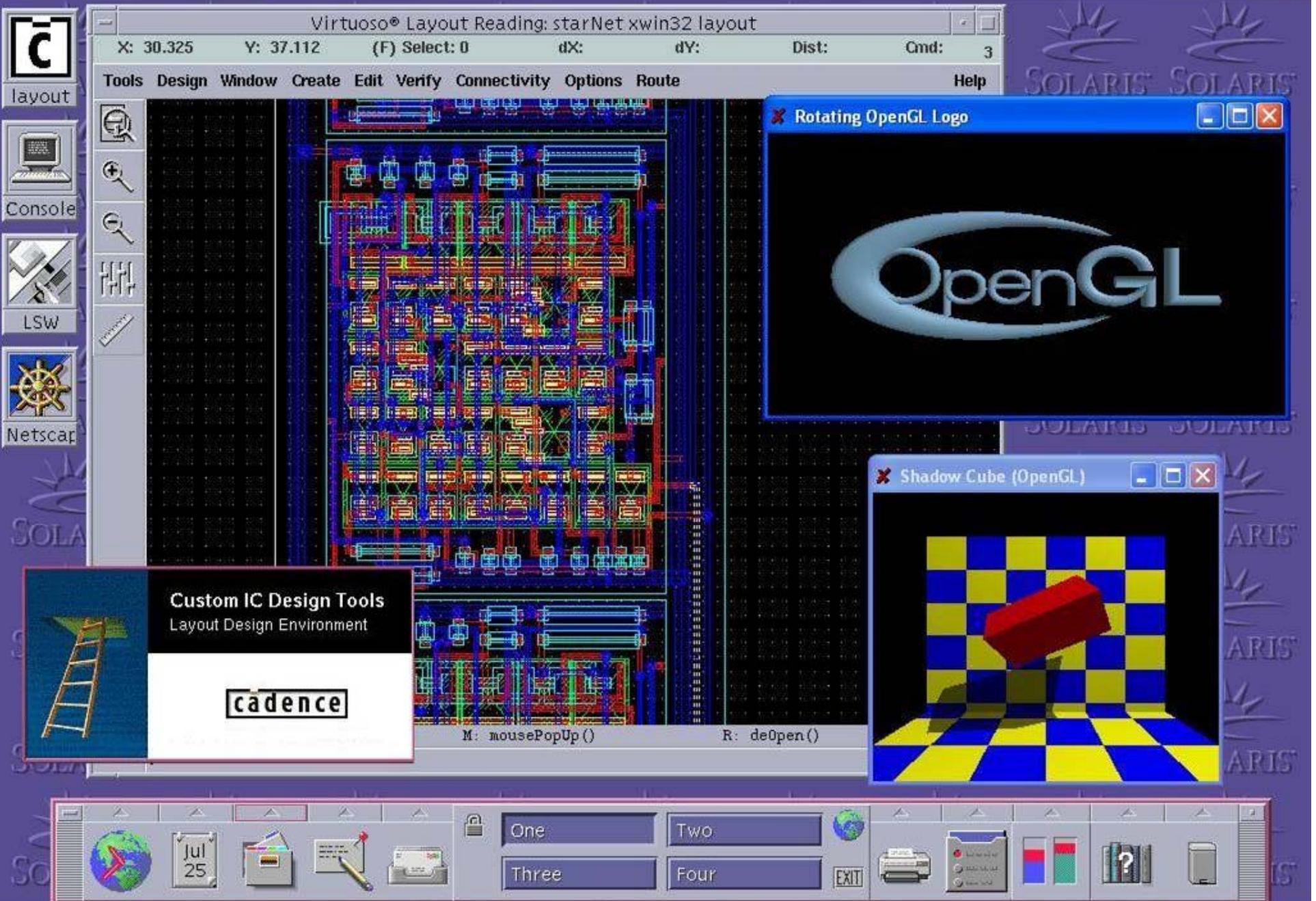
- Not top-down
 - Abstract/overall > details
- Bottoms-up !!
 - **Intuition/motivation first**
 - Teach-on-demand approach
 - Problem driven,
 - or I will rather say motivation driven
- Be arty-farty



OpenGL and GLUT

- In the old days, the first library for programming **window system** is called
 - X-windows
 - You need to program two pages of code to open 1 single window.... with nothing.
- OpenGL
 - From the GL library (1992) from Silicon Graphics
 - Handle graphics routines and window events handlings
- GLUT - The OpenGL Utility Toolkit
 - pronounced like the “glut” in gluttony
- In a word, save you a lot of trouble by
 - API: Application Programming Interface





Setup GLUT Library

- Download GLUT (from the link in the course website)
- If you are using MS Windows, follow the README file
- Copy the files:
 - glut32.dll to %WinDir%\System,
 - glut32.lib to %your vc directory%\lib, and
 - glut.h to %your vc directory%\include\GL
- DONE!

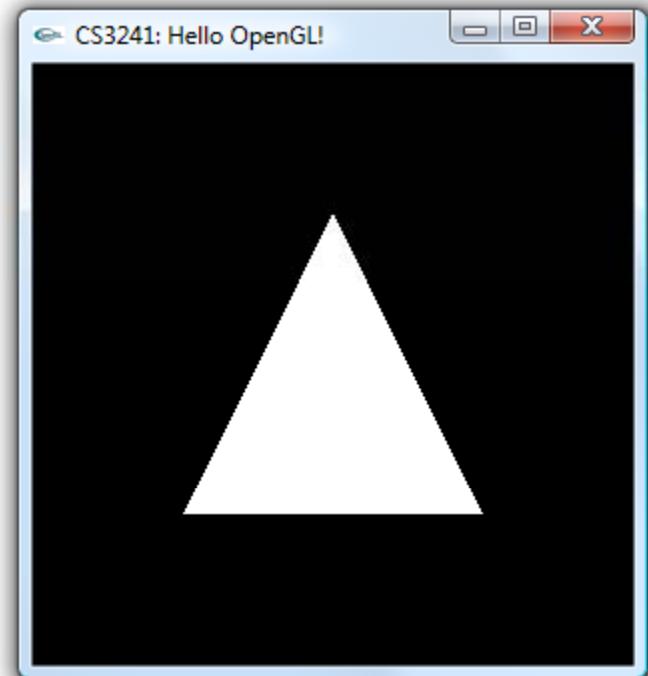
First OpenGL Program

```
#include <GL/glut.h>

void mydisplay(){
    glClear(GL_COLOR_BUFFER_BIT);

    glBegin(GL_POLYGON);
        glVertex2f(-0.5, -0.5);
        glVertex2f(0, 0.5);
        glVertex2f(0.5, -0.5);
    glEnd();
    glFlush();
}
```

Depends on
where do you
put your glut.h



```
int main()
{
    glutCreateWindow("CS3241: Hello OpenGL!");
    glutDisplayFunc(mydisplay);
    glutMainLoop();
}
```

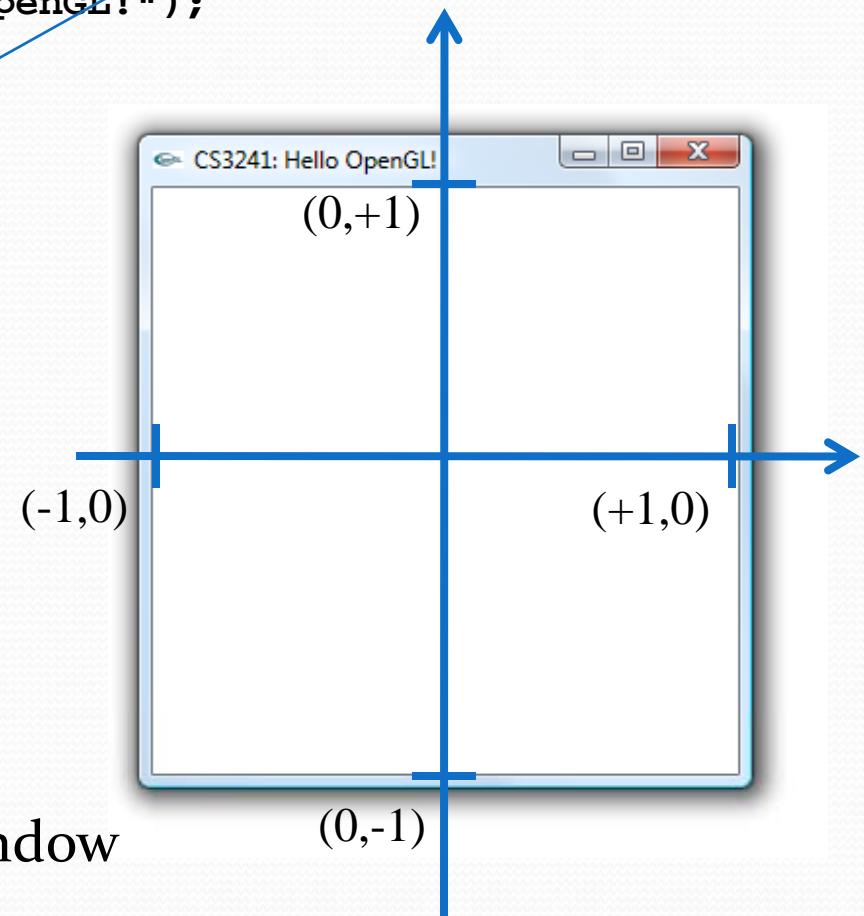
First OpenGL Program

```
int main()
{
    glutCreateWindow( "CS3241: Hello OpenGL!" );
        // simply create a window
        // with title

    glutDisplayFunc(mydisplay);
        // "register" the function
        // "mydisplay" for display

    glutMainLoop();
        // starts the window loop
}
```

May sound weird to you:
passing a “function” as a
parameter



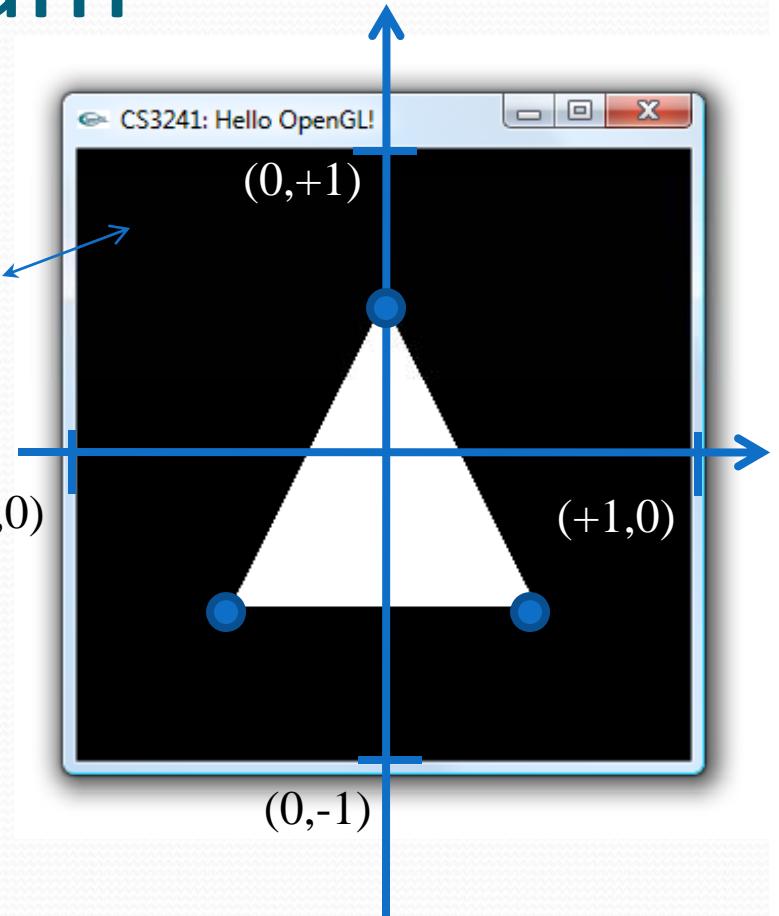
- Default window “dimension”:
 - $(-1,-1)$ to $(+1,+1)$
 - Not the “actual size” of the window

First OpenGL Program

```
#include <GL/glut.h>

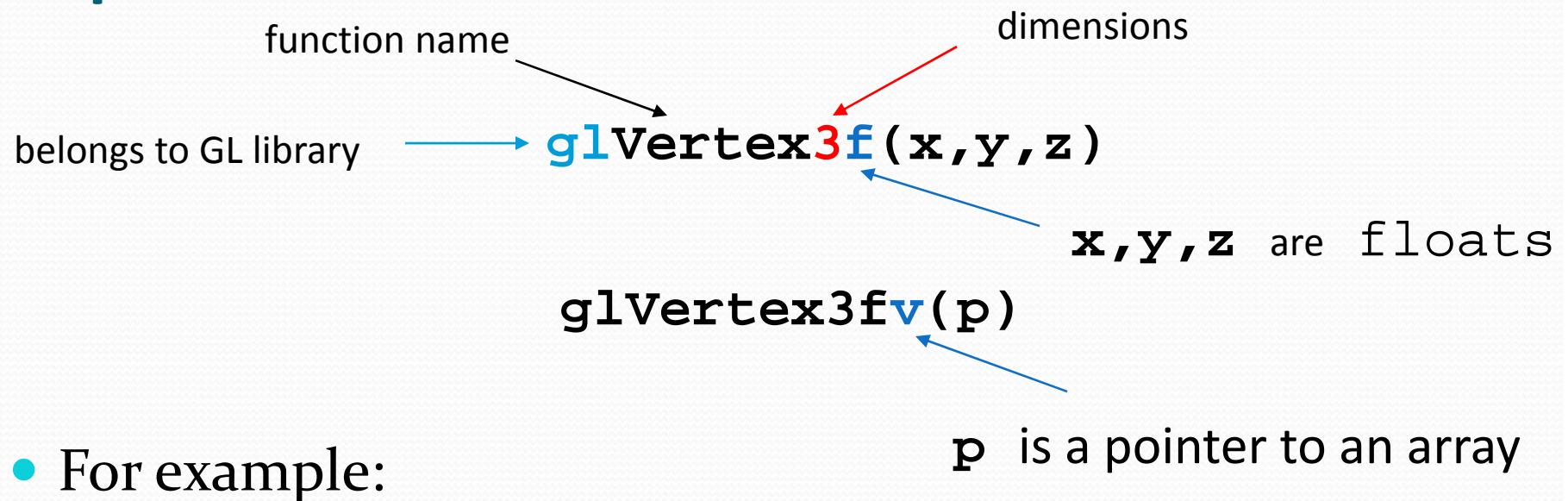
void mydisplay(){
    glClear(GL_COLOR_BUFFER_BIT);
    glBegin(GL_POLYGON);
        glVertex2f(-0.5, -0.5);
        glVertex2f(0, 0.5);
        glVertex2f(0.5, -0.5); (-1,0)
    glEnd();
    glFlush();
}
```

Clear a kind of buffer
(now it is the color buffer)
("buffer" means memory space)



Note: the default colors for background and drawing are black and white respectively

OpenGL Function Format



```
GLfloat p[2] = {-0.5,0.5};  
glBegin(GL_POLYGON);  
glvertex2fv(p);  
...
```

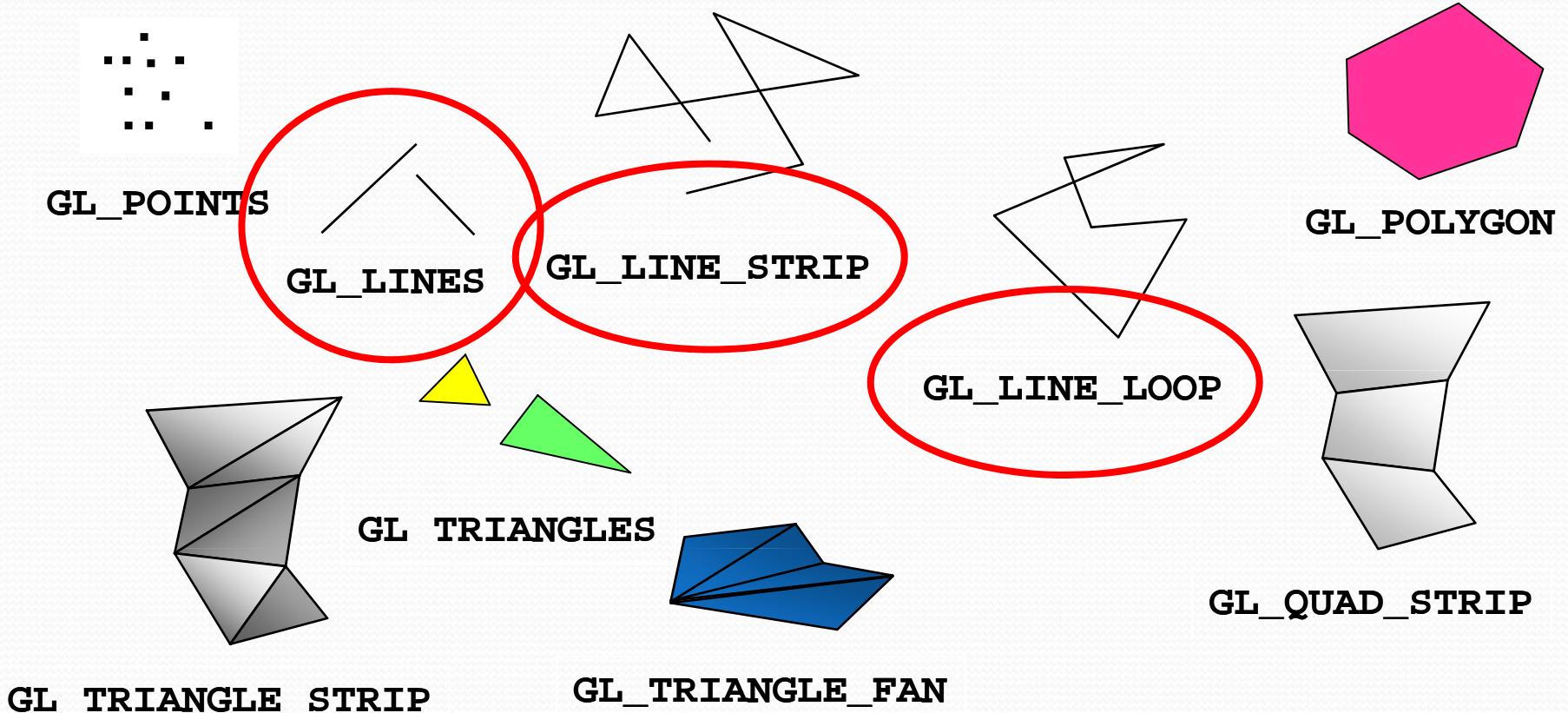
Usage for glBegin() and glEnd() pair

```
glBegin(GL_POLYGON);  
    glVertex2f(-0.5, -0.5);  
    glVertex2f(0, 0.5);  
    glVertex2f(0.5, -0.5);  
glEnd();
```

Begin to draw
some primitives,
e.g. polygon, lines,
points, etc.

A list of
commands, e.g.
vertex, normal,
texture, etc.

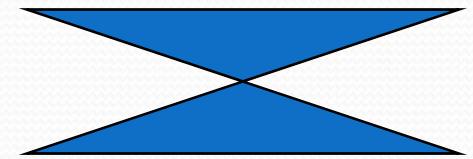
OpenGL Primitives for glBegin(?)



See: <http://www.opengl.org/sdk/docs/man/> [click `glBegin()`]

Polygon Issues

- OpenGL will only display polygons **correctly** if they are
 - Simple:
 - Edges cannot cross within a polygon
 - Convex:
 - All interior angles are less than 180 degree
 - Flat:
 - All vertices are in the same plane (in 3D)
- OpenGL **may or may not** produce desired output if these conditions are violated
- The best is to use triangles



non-simple polygon



non-convex polygon

Changing Colors

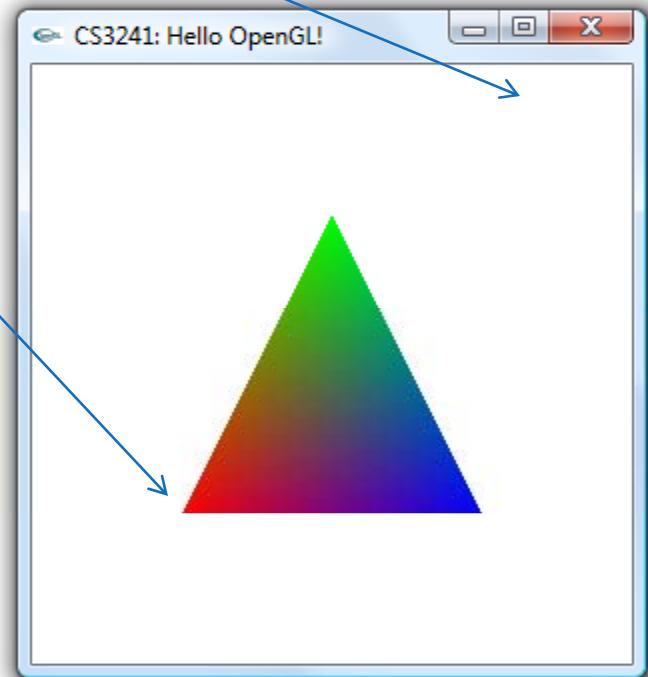
```
void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);
    glBegin(GL_POLYGON);

        glColor3f(1.0,0.0,0.0);
        glVertex2f(-0.5, -0.5);
        glColor3f(0.0,1.0,0.0);
        glVertex2f(0., 0.5);
        glColor3f(0.0,0.0,1.0); // Boxed
        glVertex2f(0.5, -0.5);
    glEnd();
    glFlush();
}
```

Set this vertex to be red

(red, green, blue)

Set Clear color to be white
(But **nothing changed** until
`glClear` is called)





2D Transformation

Here comes the mathematics

2D Transformation

- Vectors
- Reference Frame
- Transformation
 - Translation
 - Rotation
 - Scaling

Vector/Matrix Representations

- A vector (x,y) can be represented by a column or row matrices:

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \text{ or } [x \ y \ 1]$$

- Which is called Homogeneous coordinates
- What if the last coordinate is not 1?

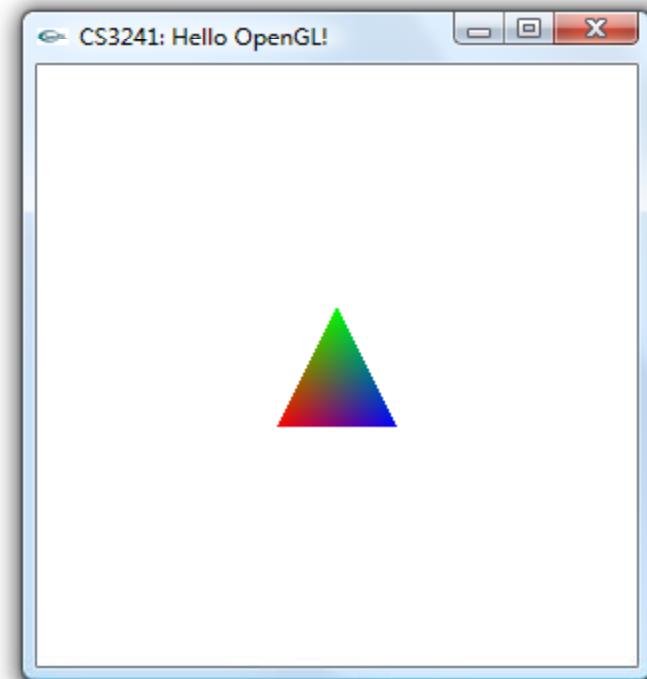
$$[x \ y \ w] = \left(\frac{x}{w}, \frac{y}{w} \right)$$

- If $w=0$, the point is at infinity in the direction (x,y)
 - E.g. $(0,1,0)$ is the point at the “north” most
- In this course, we will use the column matrix representation

Let's Start From This

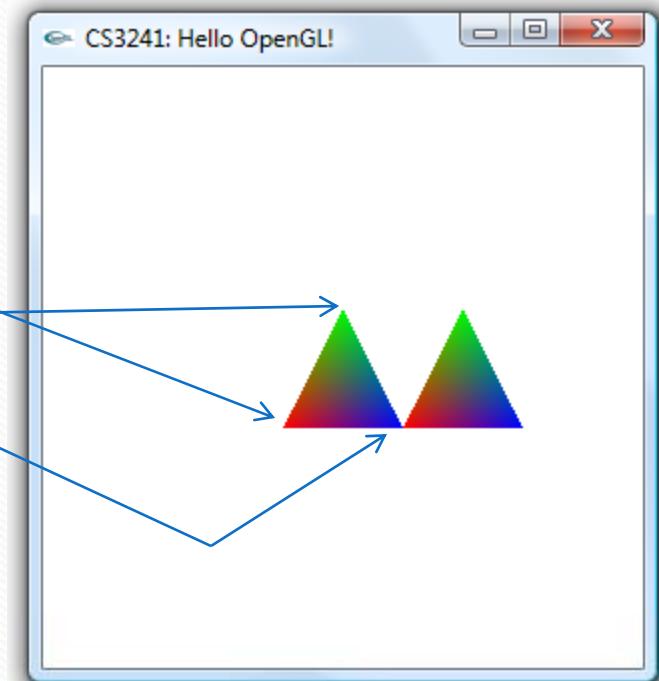
```
void drawASmallTri()
{
    glBegin(GL_POLYGON);
        glColor3f(1.0,0.0,0.0);
        glVertex2f(-0.2, -0.2);
        glColor3f(0.0,1.0,0.0);
        glVertex2f(0, 0.2);
        glColor3f(0.0,0.0,1.0);
        glVertex2f(0.2, -0.2);
    glEnd();
}

void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);
    drawASmallTri();
    glFlush();
}
```



How Do I Draw This?

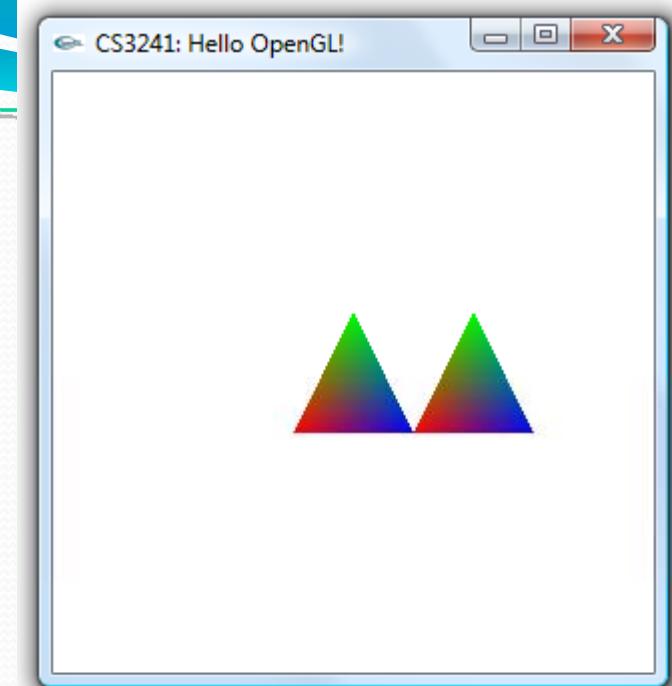
- The left triangle is the original one
 - \mathbf{a} : $(-0.2, -0.2)$
 - \mathbf{b} : $(0.2, -0.2)$
 - \mathbf{c} : $(0, 0.2)$
- The right one is
 - $(0.2, -0.2) = \mathbf{a} + (0.4, 0)$
 - $(0.6, -0.2) = \mathbf{b} + (0.4, 0)$
 - $(0.4, 0.2) = \mathbf{c} + (0.4, 0)$



Naïve (Bad) Way

```
void drawASmallTri()
{
    glBegin(GL_POLYGON);
        glColor3f(1.0,0.0,0.0);
        glVertex2f(-0.2, -0.2);
        glColor3f(0.0,1.0,0.0);
        glVertex2f(0, 0.2);
        glColor3f(0.0,0.0,1.0);
        glVertex2f(0.2, -0.2);
    glEnd();
}

void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);
    drawASmallTri();
    drawAnotherSmallTri();
    glFlush();
}
```



```
void drawAnotherSmallTri()
{
    glBegin(GL_POLYGON);
        glColor3f(1.0,0.0,0.0);
        glVertex2f(0.2, -0.2);
        glColor3f(0.0,1.0,0.0);
        glVertex2f(0.4, 0.2);
        glColor3f(0.0,0.0,1.0);
        glVertex2f(0.6, -0.2);
    glEnd();
}
```

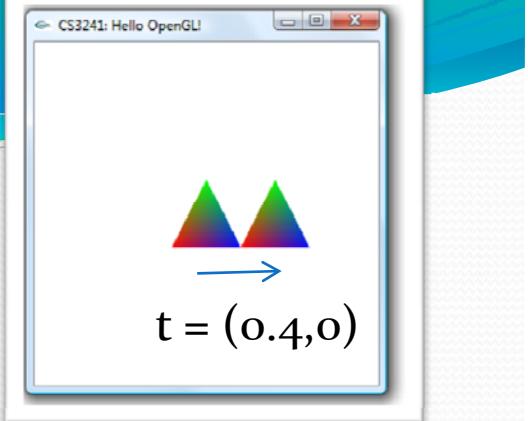
Translation

- We called this kind of movement a translation with a translation vector $t = (t_x, t_y)$
 - In the previous case $t = (0.4, 0)$
- **Every** vertex of the triangle adds the vector t
- With homogeneous coordinates, every vertex (x, y) will be moved to a new position (x', y') by

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix}$$

New position

Old position

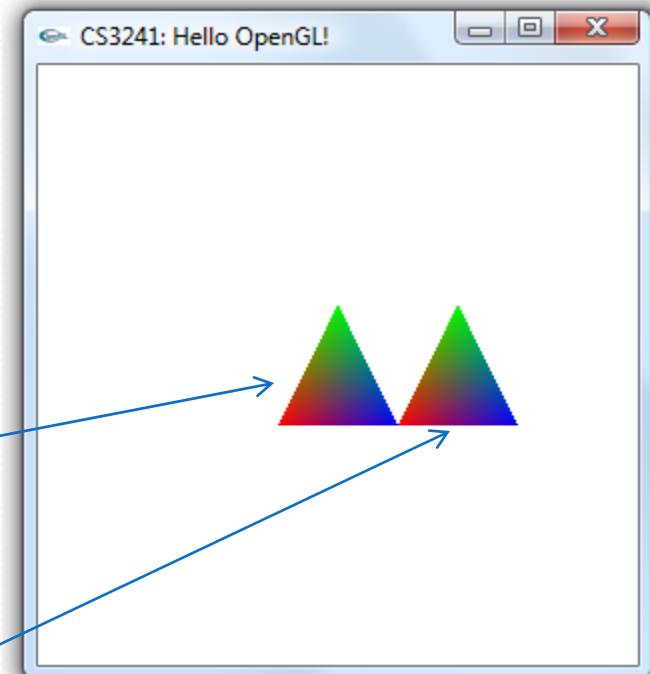


glTranslate(x,y,z)

```
void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);

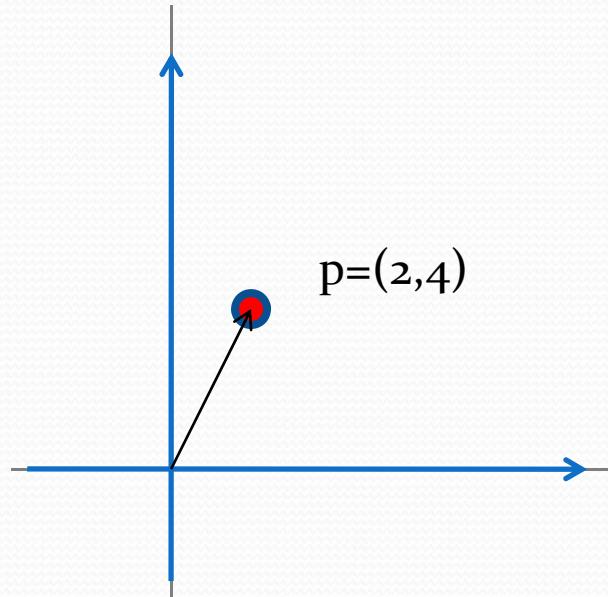
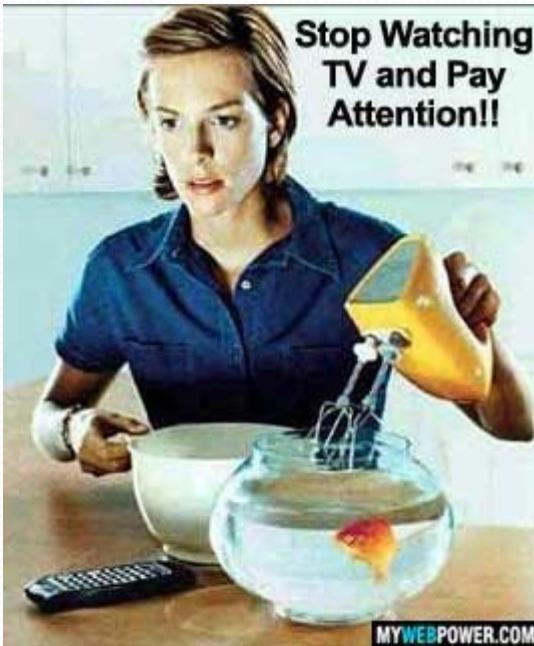
    glLoadIdentity(); 
    drawASmallTri(); ← Original Triangle

    glTranslatef(0.4,0,0);
    drawASmallTri(); ← New Triangle
    glFlush();
}
```



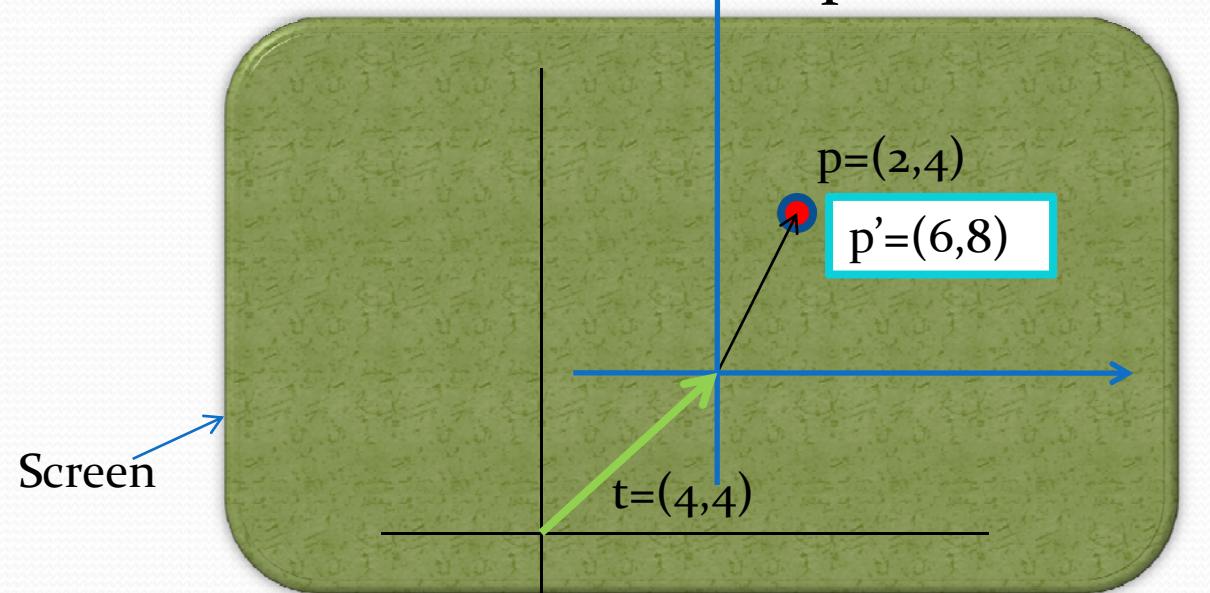
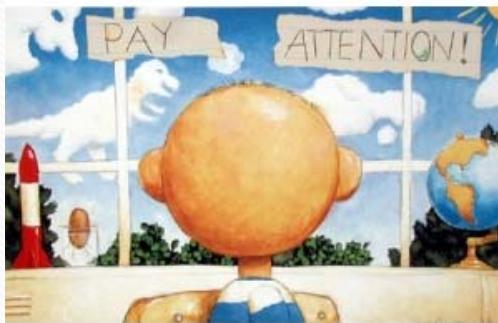
Reference Frame

- For every coordinates, there is a reference frame
- E.g. $p=(2,4)$ meaning p is 2 units right of and 4 units above the origin reference frame

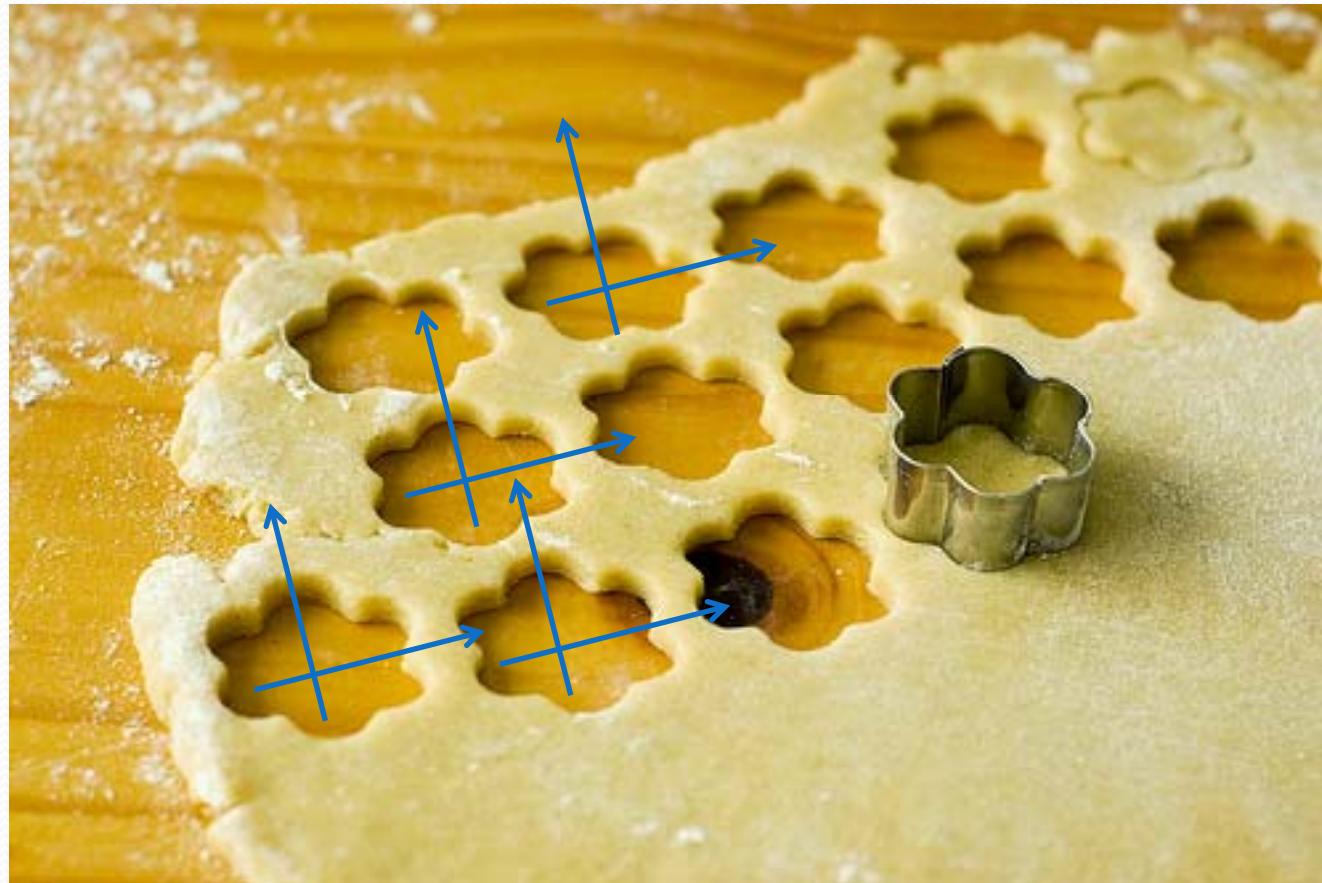


Reference Frame

- By applying a translation, it means moving the reference frame to a new position
- For example `glTranslatef(4.0,4.0,0)`
- Then when we draw p at $(2, 4)$ with respect to the **NEW** reference frame
- It finally becomes $p' = (6.0, 8.0)$ with respect to the original frame



Reference Frame



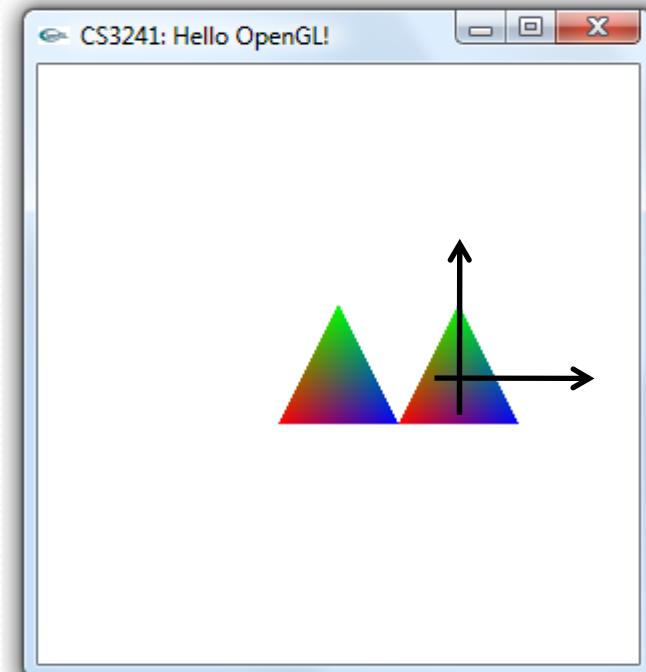
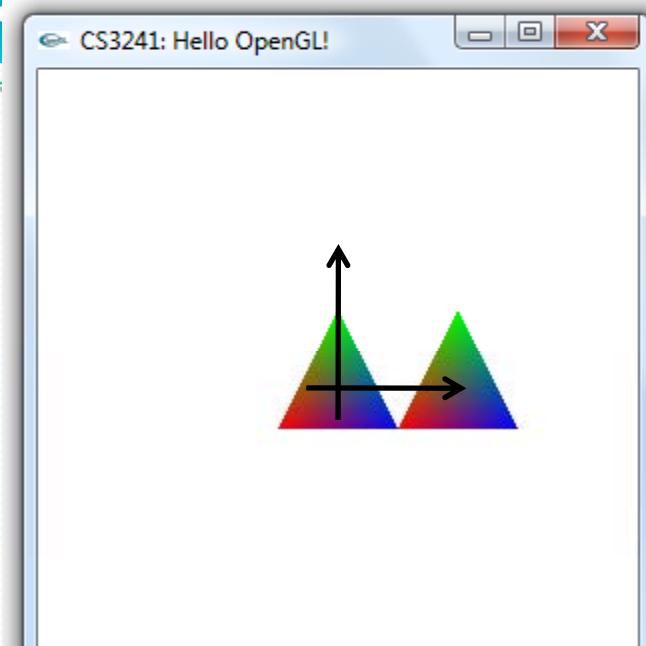
glTranslate(x,y,z)

```
void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);

    glLoadIdentity();
    drawASmallTri();

    glTranslatef(0.4,0,0);
    drawASmallTri();

    glFlush();
}
```



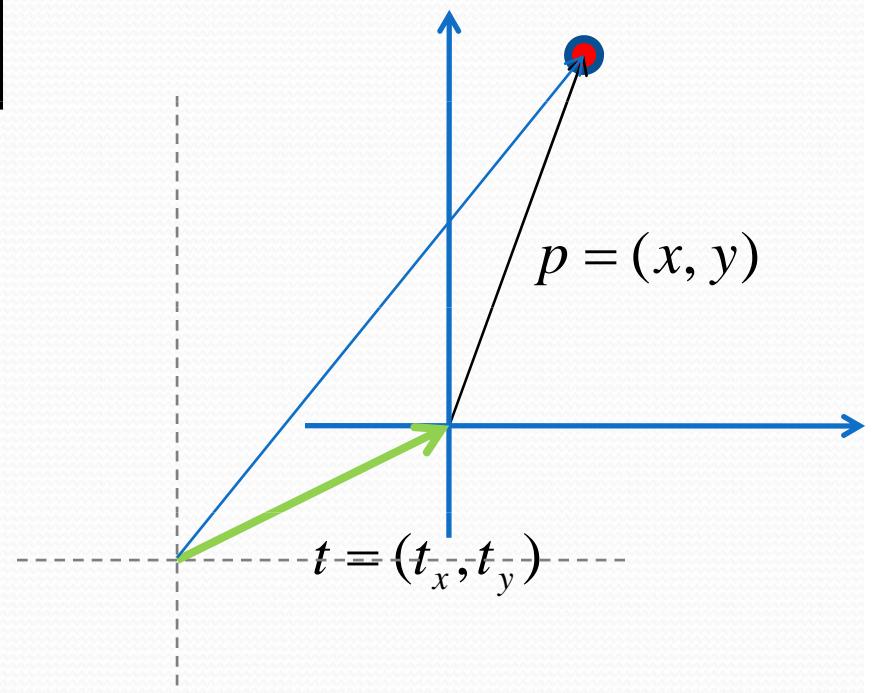
Translation

- Moving the reference frame by a vector

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x + t_x \\ y + t_y \\ 1 \end{bmatrix}$$
$$p' = (x + t_x, y + t_y)$$

- By a translation matrix

$$T(t_x, t_y) = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$$



glRotatef(angle,x,y,z)

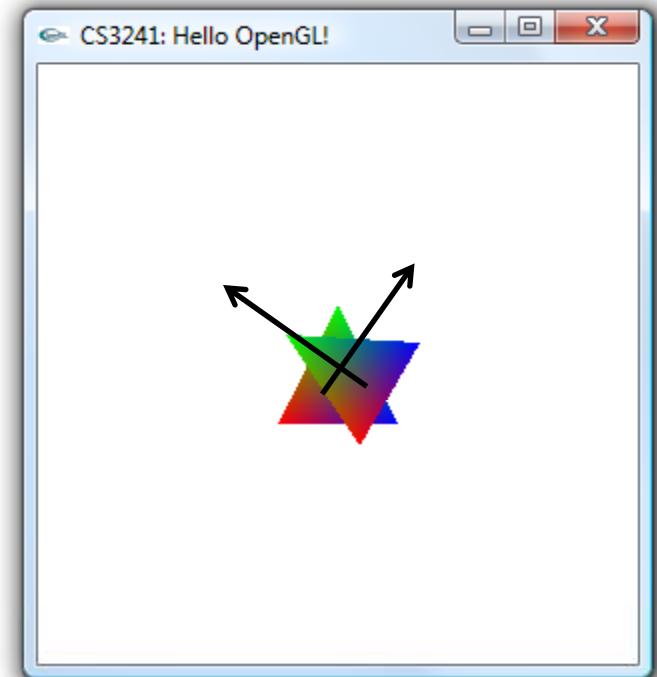
```
void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);

    glLoadIdentity();
    drawASmallTri();

    glRotatef(60,0,0,1);
    drawASmallTri();

    glFlush();
}
```

Actually a 3D rotation around
the axis of the vector (0,0,1),
namely the z-axis



Rotation

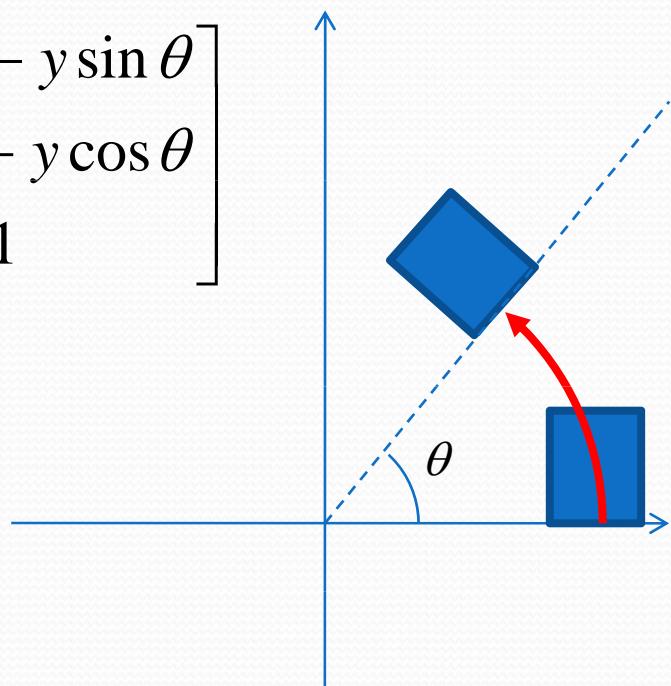
- Rotation all vertices around the origin
- Anti-clockwise

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x \cos \theta - y \sin \theta \\ x \sin \theta + y \cos \theta \\ 1 \end{bmatrix}$$

Old points New points

- By a **rotational matrix**

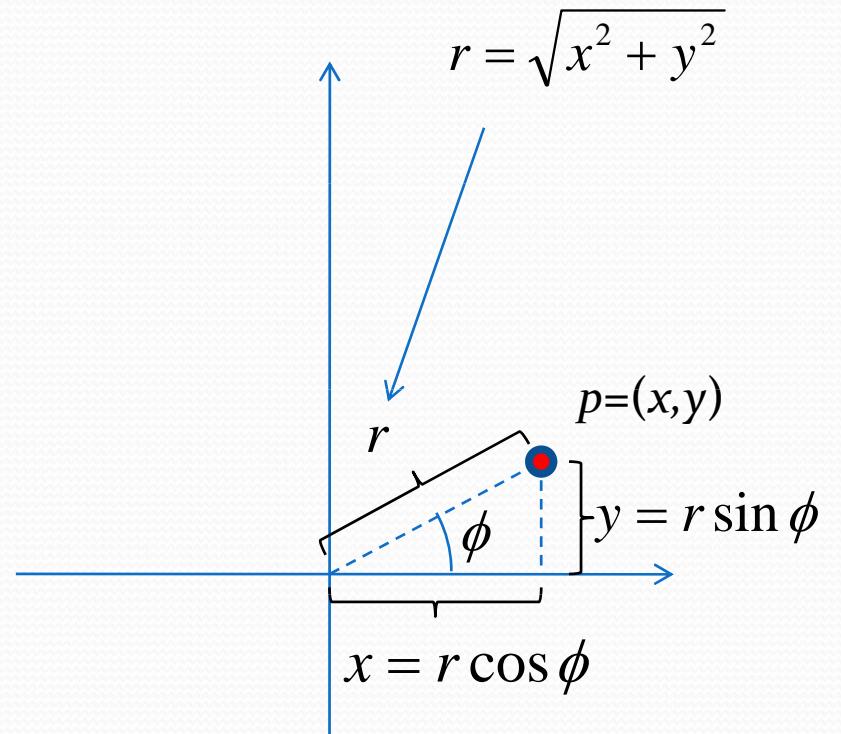
$$R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



Rotation (Derivation)

- Before rotation
- For any point $p = (x, y)$, we can represent p in the *polar coordinates*

$$p = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} r \cos \phi \\ r \sin \phi \\ 1 \end{bmatrix}$$

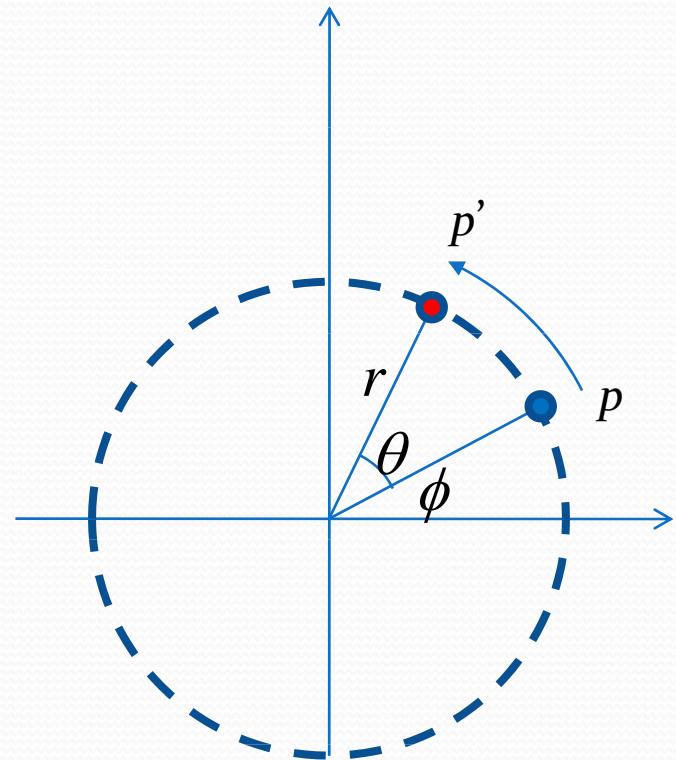


Rotation (Derivation)

- Rotate by an angle θ

$$\begin{bmatrix} r \cos(\theta + \phi) \\ r \sin(\theta + \phi) \\ 1 \end{bmatrix}$$

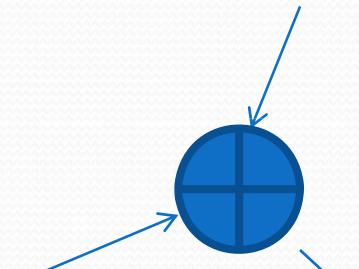
- The new point $p' =$



Rotation (Derivation)

$$p' = \begin{bmatrix} r \cos(\theta + \phi) \\ r \sin(\theta + \phi) \\ 1 \end{bmatrix} = \begin{bmatrix} r \cos \theta \cos \phi - r \sin \theta \sin \phi \\ r \sin \theta \cos \phi + r \cos \theta \sin \phi \\ 1 \end{bmatrix}$$

$$p = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} r \cos \phi \\ r \sin \phi \\ 1 \end{bmatrix}$$



$$p' = \begin{bmatrix} r \cos(\theta + \phi) \\ r \sin(\theta + \phi) \\ 1 \end{bmatrix} = \begin{bmatrix} x \cos \theta - y \sin \theta \\ x \sin \theta + y \cos \theta \\ 1 \end{bmatrix}$$

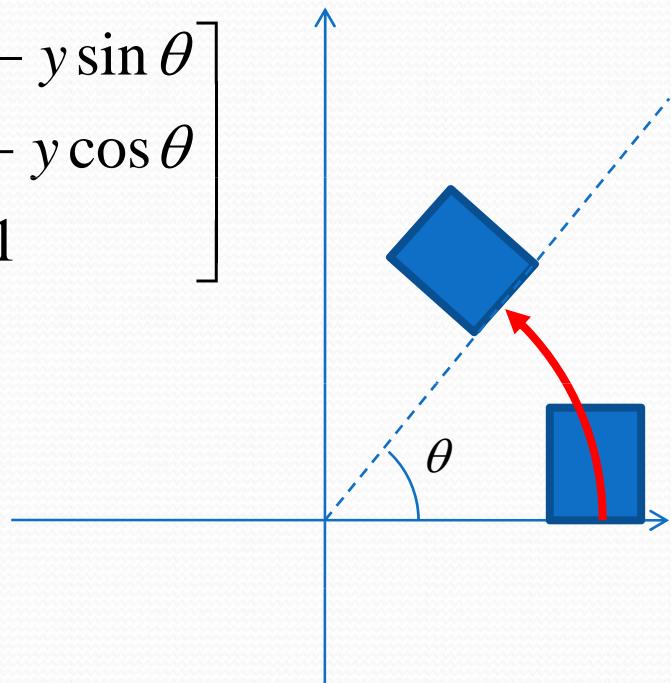
Rotation

- Rotation all vertices around the origin
- Anti-clockwise

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x \cos \theta - y \sin \theta \\ x \sin \theta + y \cos \theta \\ 1 \end{bmatrix}$$

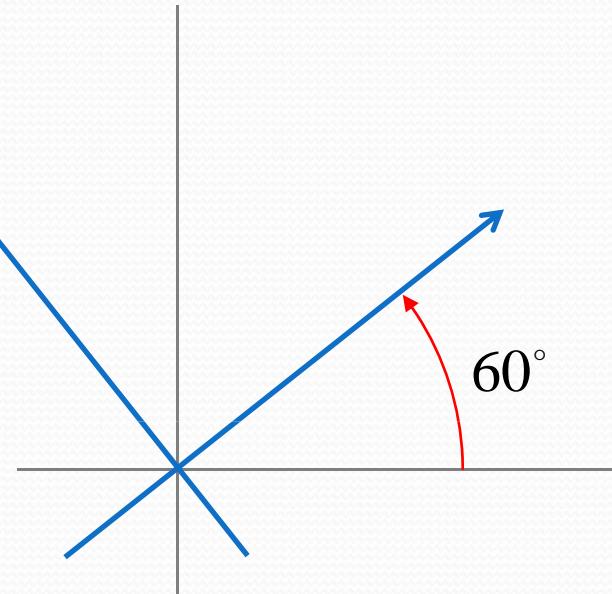
- By a **rotational matrix**

$$R(\theta) = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$



Reference Frame

- By applying a rotation, it means rotating the reference frame to a new orientation
- For example `glRotatef(60.0,0,0,1)`
 - Rotating 60 degree around the vector $(0,0,1)$



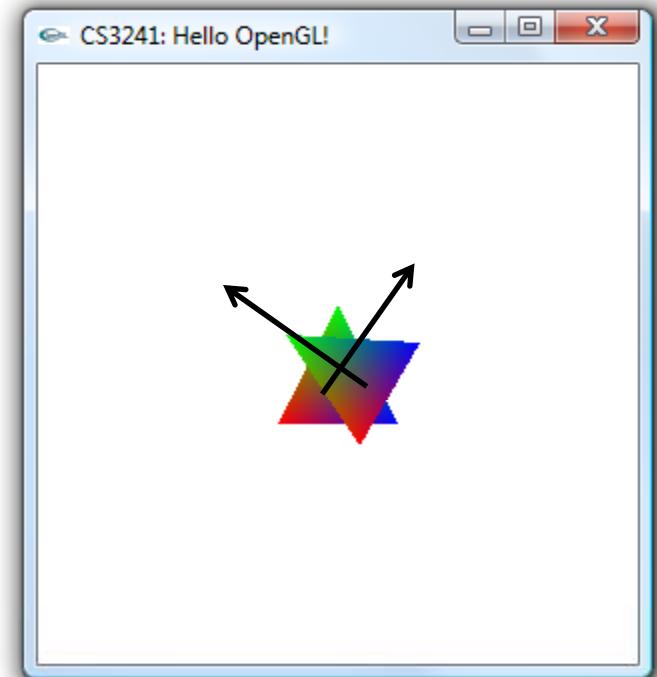
glRotatef(angle,x,y,z)

```
void mydisplay(){
    glClearColor(1.0,1.0,1.0,1.0);
    glClear(GL_COLOR_BUFFER_BIT);

    glLoadIdentity();
    drawASmallTri();

    glRotatef(60,0,0,1);
    drawASmallTri();

    glFlush();
}
```



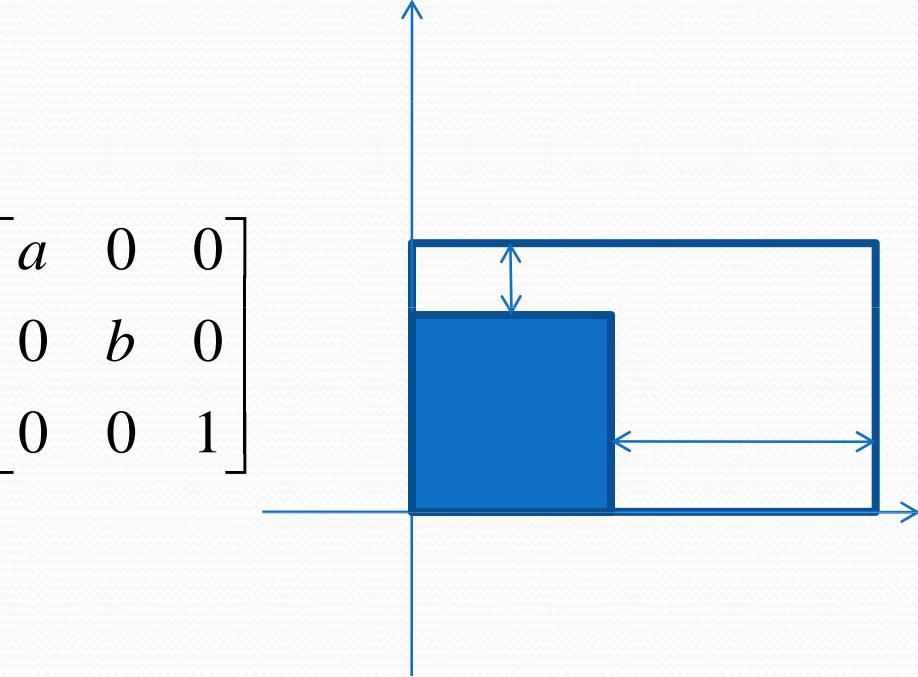
Scaling

- Shrink or grow
- Simply

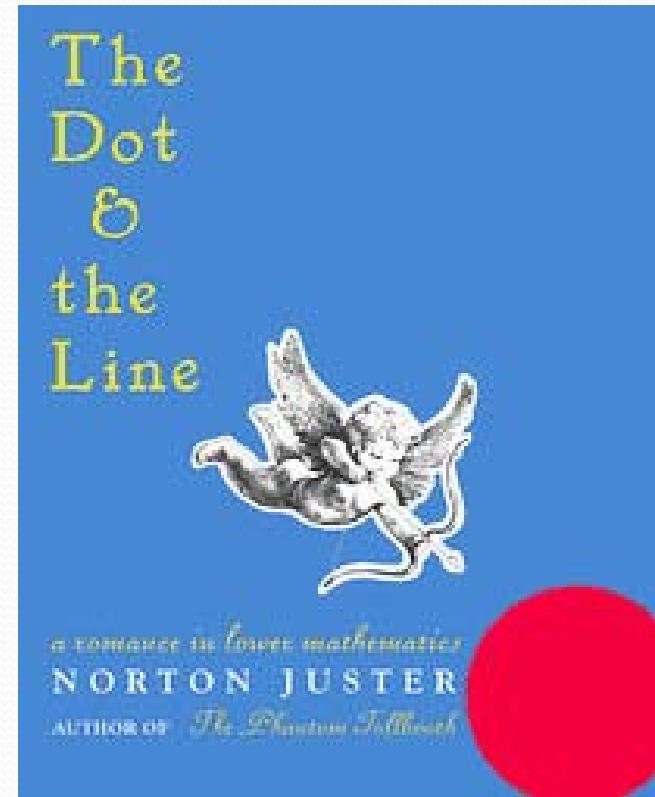
$$p' = \begin{bmatrix} ax \\ by \\ 1 \end{bmatrix} = S(a, b) \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$



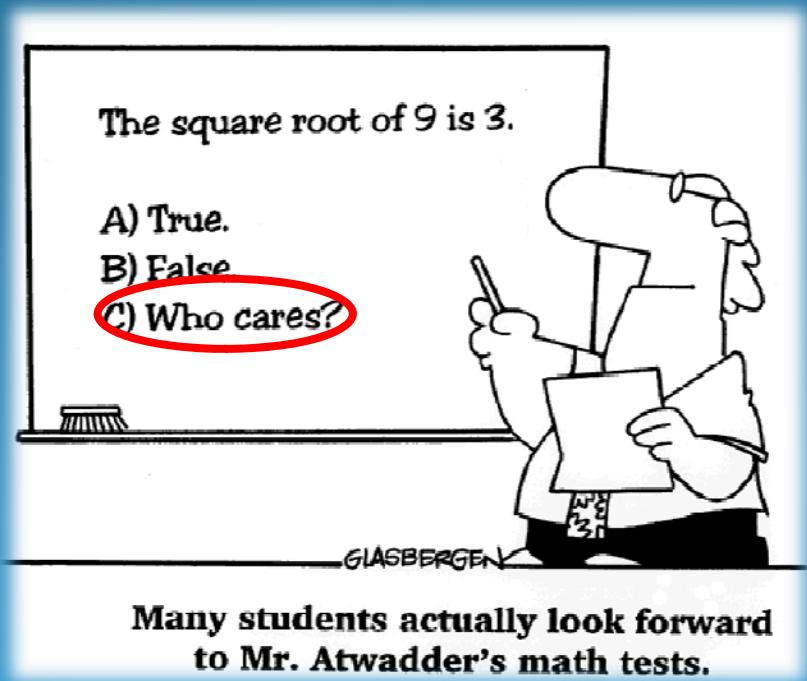
- a and b could be -ve
- By a scaling matrix $S(a, b) = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix}$
- OpenGL function:
 - **glScalef(x, y, z);**



Let's take a break



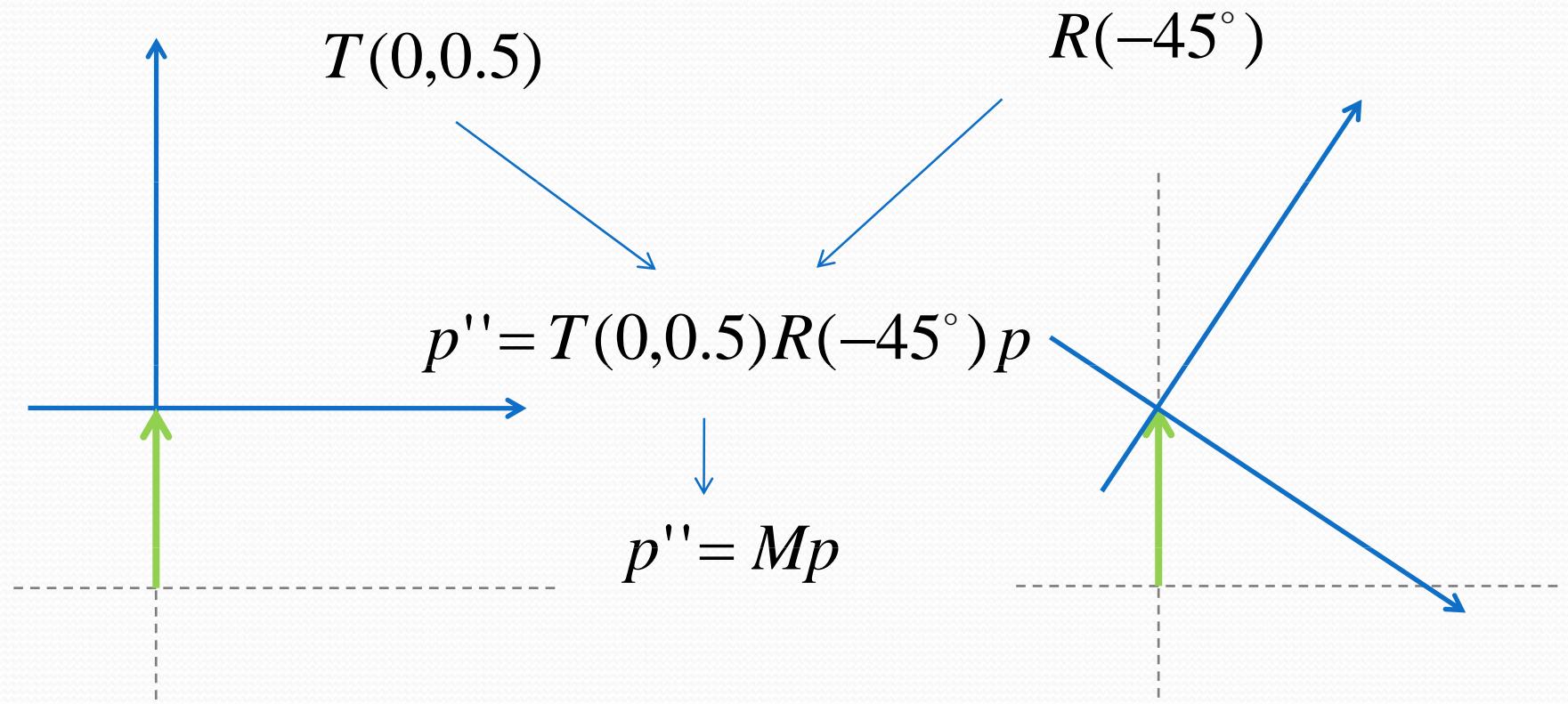
Why Matrix?



Why Matrices??



- Because we can combine many transformations into one matrix



Composite Transformation



- Note that you can do as many transformation as you can

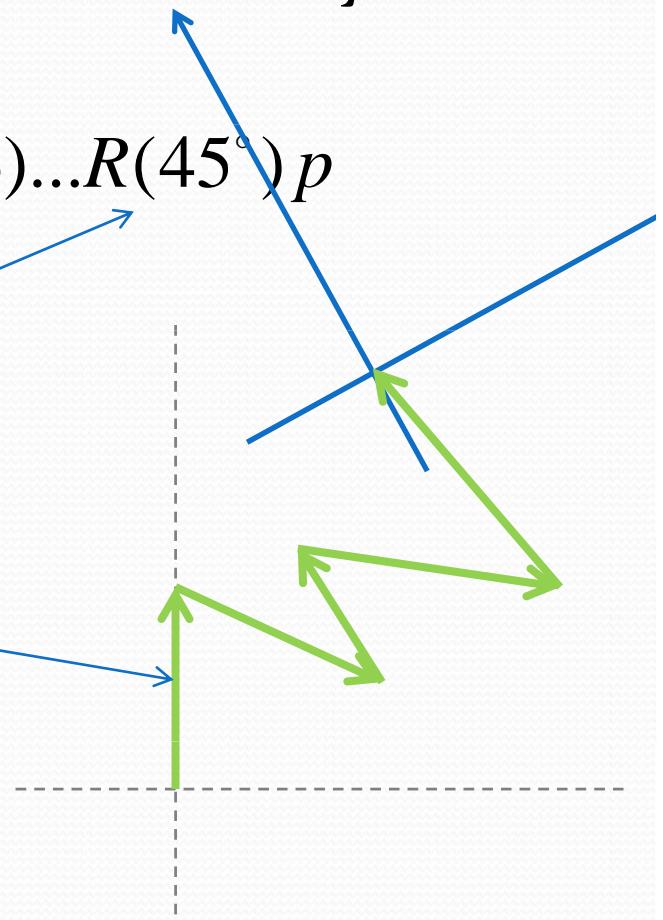
$$p'' = T(0,1)R(10^\circ)S(0.5,20)T(2,3)\dots R(45^\circ)p$$

first

- And also note the “order”

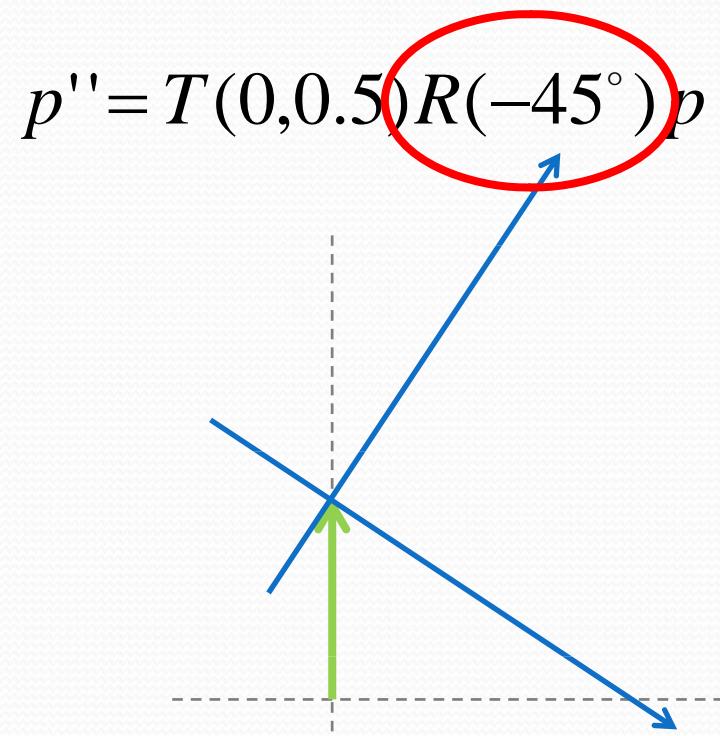
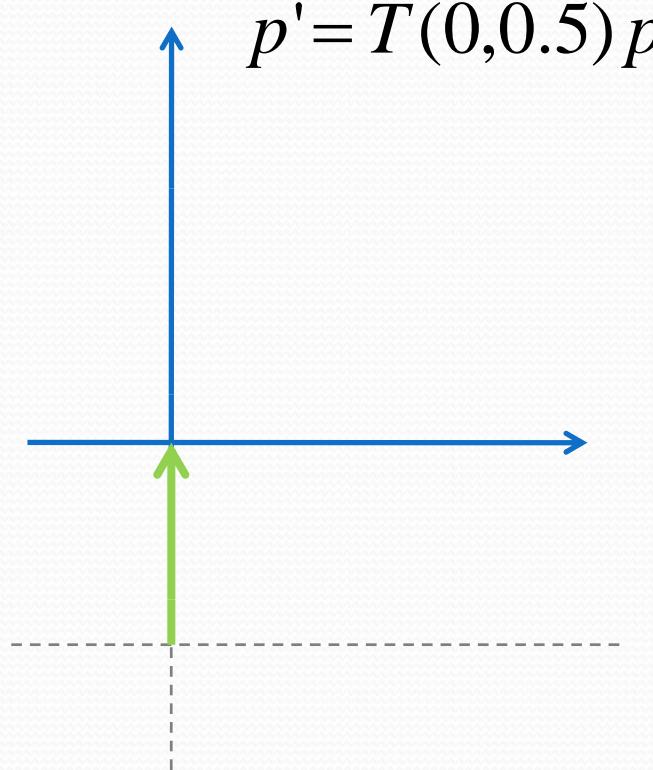


first



Composite Transformation

- Whenever you add a new transformation, you add it to the **RIGHT** of the matrices



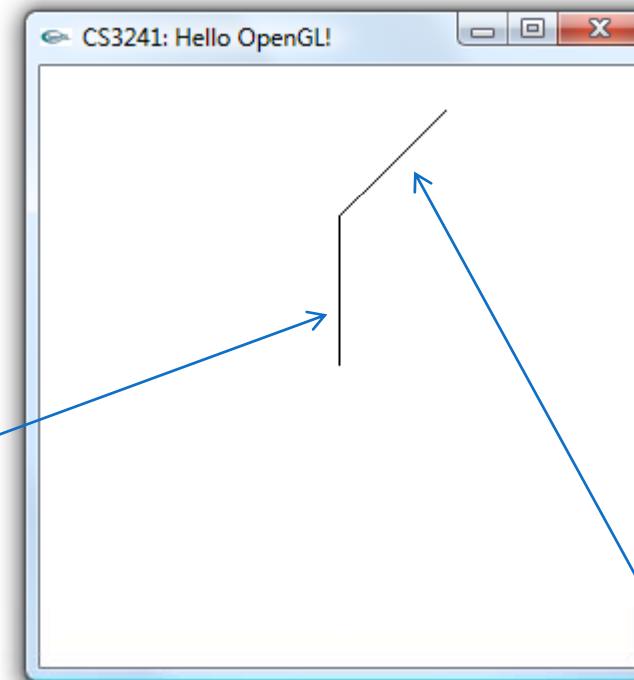
In OpenGL

```
void drawLine()
{
    glBegin(GL_LINES);
        glVertex2f(0,0);
        glVertex2f(0,0.5);
    glEnd();
}

void mydisplay(){
...
    glLoadIdentity();

    drawLine();
    glTranslatef(0,0.5,0);
    glRotatef(-45,0,0,1);
    drawLine();
    glFlush();
}
```

Clear the transformation matrix to identity

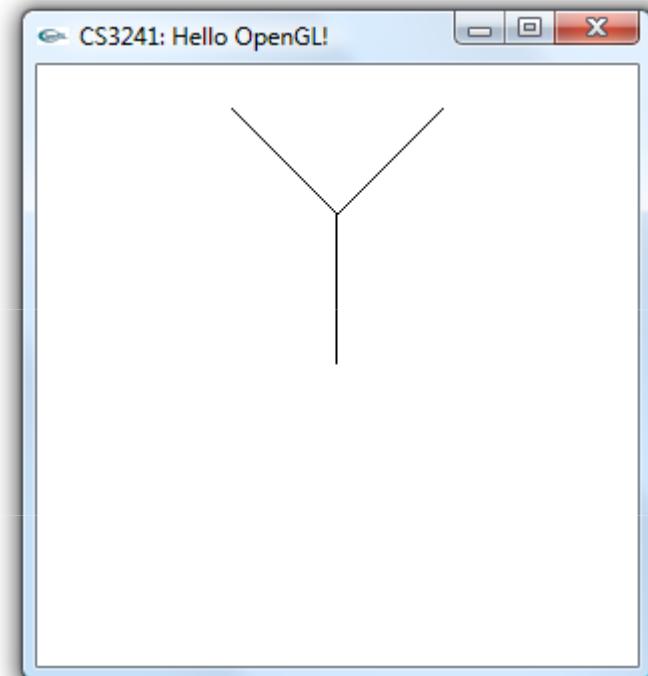


Matrix Stack



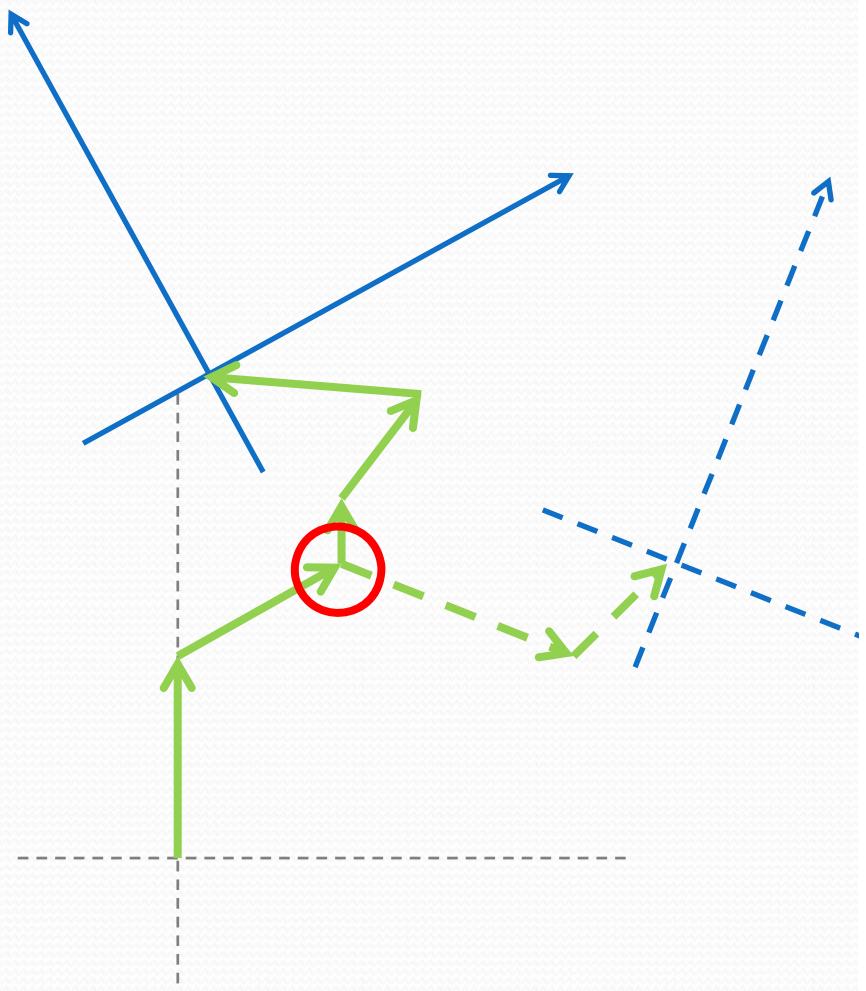
What if I want to draw this

- Draw the first vertical line
- Do two transformations and draw the right line:
 $T(0,0.5)R(-45)$
- **Reset** the transformation
- Do another two transformations to draw the left line
 $T(0,0.5)R(45)$



Transformation Stack in OpenGL

- You can **save** the transformation in any moment into a stack
- From there you can “**resume**” or “**save**” at anytime and add on new transformation
- Save a matrix
 - **glPushMatrix()**
- Retrieve a matrix
 - **glPopMatrix()**



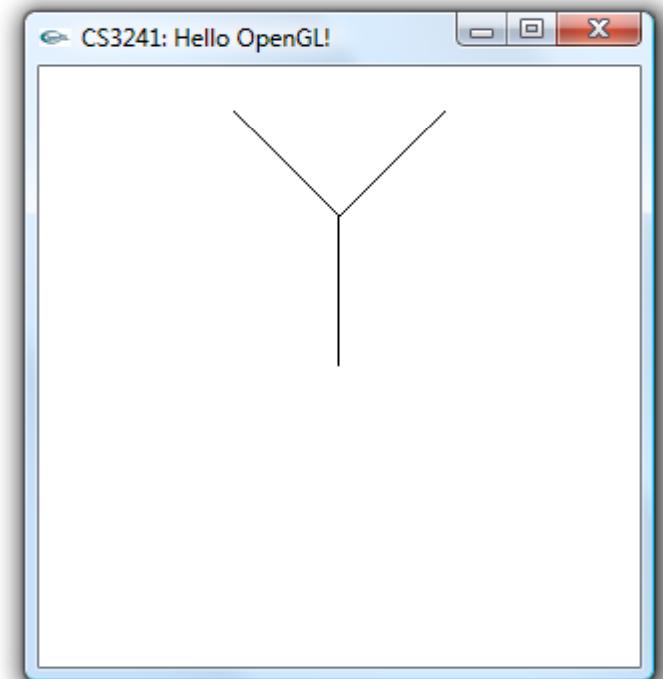
In OpenGL

```
void drawFork()
{
    drawLine();
    glPushMatrix();
        glTranslatef(0,0.5,0);
        glPushMatrix();
            glRotatef(-45,0,0,1);
            drawLine();
        glPopMatrix(); ←
        glPushMatrix();
            glRotatef(45,0,0,1);
            drawLine();
        glPopMatrix();
    glPopMatrix(); ←
    glPopMatrix();
}

void mydisplay(){
    glClear(GL_COLOR_BUFFER_BIT);
    glColor3f(0,0,0);
    glMatrixMode(GL_MODELVIEW);
    drawFork();
    glFlush();
}
```

Resume to
T(0,0.5)

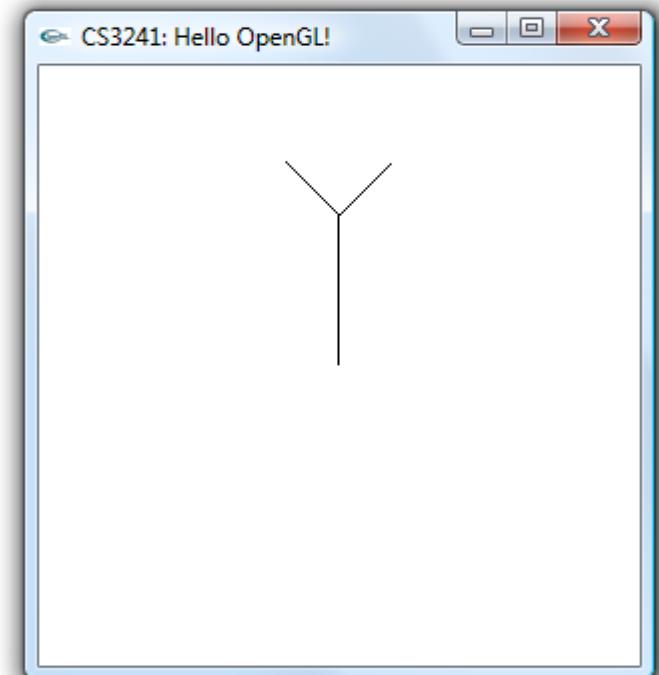
Resume to
nothing



A Nicer “Y”

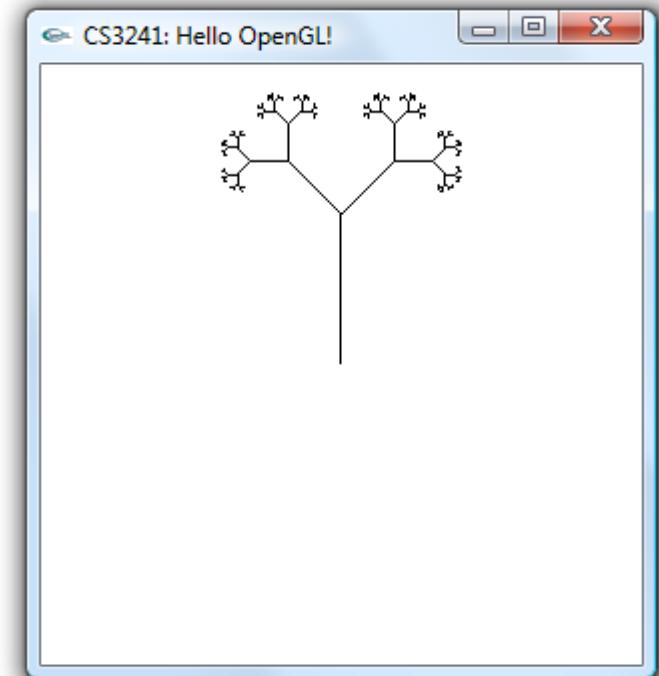
```
void drawFork()
{
    drawLine();
    glPushMatrix();
        glTranslatef(0,0.5,0);
        glPushMatrix();
            glRotatef(-45,0,0,1);
            glScalef(0.5,0.5,0.5);
            drawLine();
        glPopMatrix();
        glPushMatrix();
            glRotatef(45,0,0,1);
            glScalef(0.5,0.5,0.5);
            drawLine();
        glPopMatrix();
    glPopMatrix();
}
```

You can mess up the transformation within a pair of Push/Pop



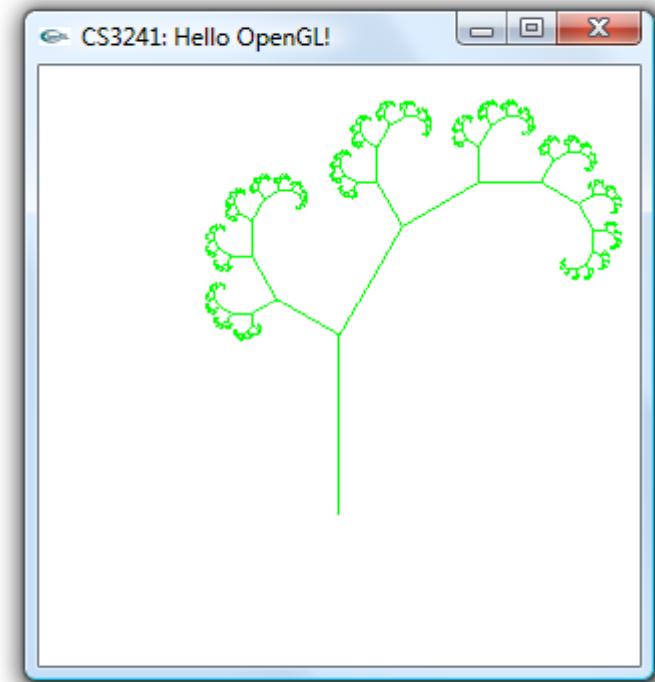
A Fractal Tree

```
void drawFork(int n)
{
    drawLine();
    if (n==0) return;
    glPushMatrix();
        glTranslatef(0,0.5,0);
        glPushMatrix();
            glRotatef(-45,0,0,1);
            glScalef(0.5,0.5,0.5);
            drawFork(n-1);
        glPopMatrix();
        glPushMatrix();
            glRotatef(45,0,0,1);
            glScalef(0.5,0.5,0.5);
            drawFork(n-1);
        glPopMatrix();
    glPopMatrix();
}
```

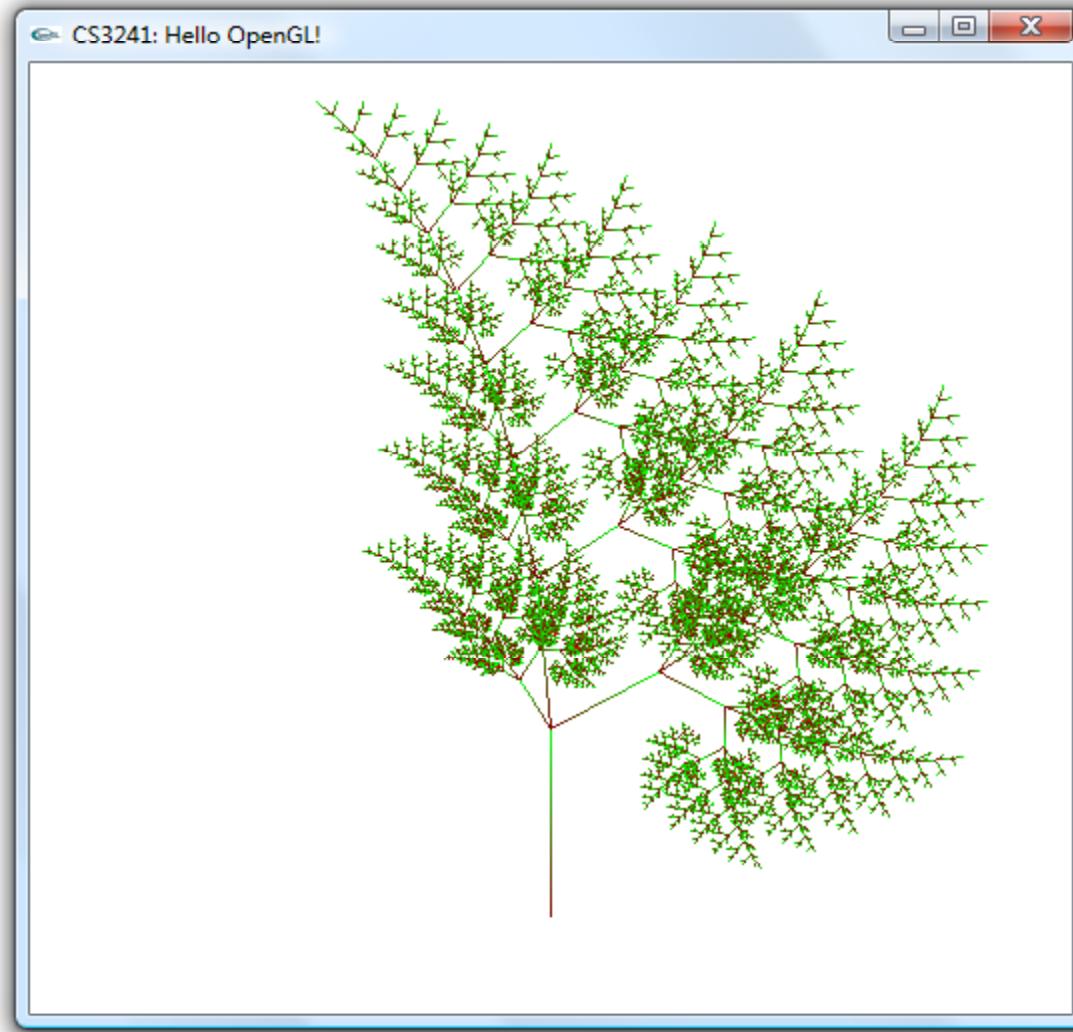


A Nicer Fractal Tree

```
void drawFork(int n)
{
    drawLine();
    if (n==0) return;
    glPushMatrix();
        glTranslatef(0,0.2,0);
        glPushMatrix();
            glRotatef(-30,0,0,1);
            glScalef(0.7,0.7,0.7);
            drawFork(n-1);
        glPopMatrix();
        glPushMatrix();
            glRotatef(60,0,0,1);
            glScalef(0.4,0.4,0.4);
            drawFork(n-1);
        glPopMatrix();
    glPopMatrix();
}
```



Finally, a colorful nicer fractal tree





Some Final Note

About Transformation

- Transformation is **NOT** effective within a pair of `glBegin()` and `glEnd()`
 - `GL_INVALID_OPERATION` is generated if `glTranslate` (and any other transformation) is executed between the execution of `glBegin` and the corresponding execution of `glEnd`.

Vector/Matrix Representations

- In this course, we will use a column matrix to represent a point

$$p = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \quad p'' = T(0,0.5)R(-45^\circ)p$$

- However, row matrices also work (in other textbooks)

$$q = [x \ y \ 1] = p^T \quad q'' = qR(-45^\circ)^T T(0,0.5)^T = (p'')^T$$

Announcement

- Tutorials and Labs will start at **NEXT** week
- First assignment will be issued **NEXT** Tuesday
- For any confusion, please refer to IVLE, lesson plan
- Remember there is a Facebook Page
 - <https://www.facebook.com/NUSCG>