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Transfer function:

$$H(s) = \frac{\left(s - s_{z_1}\right)\left(s + s_{z_2}\right)}{\left(s - s_{p_1}\right)\left(s - s_{p_2}\right)} = \frac{s^2 + \omega_o^2}{s^2 + 2\omega_o\cos\left(\theta\right)s + \omega_o^2}$$

Frequency response:

$$H(\omega) = H(s)\Big|_{s=j\omega} = \frac{\omega_o^2 - \omega^2}{\omega_o^2 - \omega^2 + j2\omega_o\omega\cos(\theta)}$$

$$= \frac{1}{1+j\left(\frac{2\omega_o\omega\cos(\theta)}{\omega_o^2 - \omega^2}\right)}$$
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Magnitude response:

$$\left| H(\omega) \right| = \frac{\left| \omega_o^2 - \omega^2 \right|}{\left[\left(\omega_o^2 - \omega^2 \right)^2 + 4\omega_o^2 \omega^2 \cos^2\left(\theta\right) \right]^{0.5}}$$

Phase response:

$$\angle H(\omega) = -\tan^{-1}\left(\frac{2\omega_o\omega\cos(\theta)}{\omega_o^2 - \omega^2}\right)$$



