

Ben Lirio

I pledge my honor that I have abided by the Stevens Honor System.

### Problem 1

S = Small  
M = Medium  
L = Large  
R = Regular  
D = Decaf

$$\begin{aligned} \text{a) } P(S) &= \\ P(SR) + P(SD) &= \\ 14\% + 20\% &= \\ \text{---}34\% \end{aligned}$$

$$\begin{aligned} P(D) &= \\ P(SD) + P(MD) + P(LD) &= \\ 20\% + 10\% + 10\% &= \\ \text{---}40\% \end{aligned}$$

$$\begin{aligned} \text{b) If } P(S) \text{ occurs what is } P(D)? \\ \text{Using the formula } P(A \cap B) &= P(A|B) * P(A) \\ P(D|S) &= \\ P(D \cap S) / P(S) &= \\ 20\% / 34\% &= \\ \text{---}58.823\% \\ \text{Interpretation:} \\ \text{Small cups of coffe are more likey to contain decaf than other sizes} \end{aligned}$$

$$\begin{aligned} \text{c) } P(D) \text{ occurs what is } P(S) \\ \text{Again using the formula } P(A \cap B) &= P(A|B) * P(A) \\ P(S|D) &= \\ P(S \cap D) / P(D) &= \\ 20\% / 40\% &= \\ \text{---}50\% \\ P(S|D) \text{ is } 10\% \text{ more likely than just } P(S) \end{aligned}$$

### Problem 2

A = U.S.  
B = Icemaker  
C = Extended Warenty  
 $P(A) = .75$   
 $P(B|A) = .9$   
 $P(B|A') = .8$   
 $P(C|A \cap B) = .8$   
 $P(C|A \cap B') = .6$   
 $P(C|A' \cap B) = .7$   
 $P(C|A' \cap B') = .3$

a) SEE ATTACHED

$$\begin{aligned} \text{b) } P(A) * P(A|B) * P(C|A \cap B) &= \\ .75 * .9 * .8 &= \\ \text{---}0.54 \end{aligned}$$

$$\begin{aligned} \text{c) } P(B \cap C) &= \\ P((B \cap C \cap A') \cup (B \cap C \cap A)) &= \\ P(A) * P(A|B) * P(C|A \cap B) + P(A') * P(B|A') * P(C|B \cap A') &= \\ .75 * .9 * .8 + .25 * .8 * .7 &= \\ \text{---}0.68 \end{aligned}$$

d)  $P(C) =$   
Trace all routes to C and multiply probabillites along the way. All events are dis joint so adding all the routes is valid.

$$\begin{aligned} P(A) * P(B|A) * P(C|A \cap B) + \\ P(A) * P(B'|A) * P(C|A \cap B') + \\ P(A') * P(B|A') * P(C|A' \cap B) + \\ P(A') * P(B'|A') * P(C|A' \cap B') &= \\ .75 * .9 * .8 + .75 * .1 * .6 + .25 * .8 * .7 + .25 * .2 * .3 &= \\ .54 + .045 + .14 + .015 &= \\ \text{---}0.74 \end{aligned}$$

$$\text{e) } P(A|B \cap C) =$$

$$P(A \cap B \cap C) / P(B \cap C) =$$

$$P(A \cap B \cap C) / (P(A) * P(B|A) * P(C|A \cap B) + P(A') * P(B|A') * P(C|A' \cap B))$$

$$.54 / .68$$

---0.79418

### Problem 3

Assume independence

A1 = Reciever works

A2 = Speaker works

A3 = CD playter works

$P(A1) = .95$

$P(A2) = .98$

$P(A3) = .80$

a)  $P(A1 \cap A2 \cap A3)$

Because A2 A2 and A3 are independent the followin is valid

$P(A1) * P(A2) * P(A3) =$

$.95 * .98 * .80 =$

---0.7448

b)  $P(A1' \cup A2' \cup A3') =$

$P(A1 \cap A2 \cap A3)' =$

$1 - P(A1 \cap A2 \cap A3) =$

$1 - .7748 =$

---0.2552

c)  $P(A1' \cap A2' \cap A3')$

$P(A1') * P(A2') * P(A3') =$

$.05 * .02 * .2$

---0.0002

d)  $P(A1' \cap A2 \cap A3) =$

$P(A1') * P(A2) * P(A3)$

$.05 * .98 * .8 =$

---.0392

e)  $P(A1' \cap A2 \cap A3) + P(A2' \cap A1 \cap A3) + P(A3' \cap A1 \cap A2) =$

$.05 * .98 * .8 + .02 * .95 * .80 + .20 * .95 * .98 =$

.233

d)  $P(A1 \cap A2 \cap A3) * P(? | P(A1 \cap A2 \cap A3))$

---less than 0.7448

### Problem 4

A1 = likes vehical #1

A2 = likes vehical #2

A3 = likes vehical #3

$P(A1) = .55$

$P(A2) = .65$

$P(A3) = .70$

$P(A1 \cup A2) = .80$

$P(A2 \cap A3) = .40$

$P(A1 \cup A2 \cup A3) = .88$

a)  $P(A1 \cap A2) =$

$P(A1) + P(A2) - P(A1 \cup A2) =$

$.55 + .65 - .80$

---0.4

b)  $P(A2|A3)$  - what does this mean

$P(A2 \cap A3) / P(A3) =$

$.40 / .70 =$

---0.571

Knowing an individual likes A3 increases the odds they like A2

c) Are  $P(A2)$  and  $P(A3)$  independent. Answer two ways

---1. No, because  $P(A2) \neq P(A2|A3)$

---2. No, becuse  $P(A3) \neq P(A3|A2)$

d) Given A1' what is  $P(A2 \cup A3) =$

$P(A1 \cup A2 \cup A3) - P(A1)$

$.88 - .55$

---.33