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Pledge: I pledge my honor that I have abided by the Stevens Honor System

Description: Homework 1

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Problem 1

$n = \text{AND}$

$u = \text{OR}$

a) $A = \{SSF, SFS, SFF\}$

b) $B = \{SSS, SSF, SFS, FSS\}$

c) $C = \{SSS, SSF, SFS\}$

d) $C' = \{SFF, FSS, FSF, FFS, FFF\}$

$A \cup C = \{SSS, SSF, SFS, SFF\}$

$A \cap C = \{SSF, SFS\}$

$B \cup C = \{SSS, SSF, SFS, FSS\}$

$B \cap C = \{SSS, SSF, SFS\}$

Problem 2

a) $S = \{3, 4, 5, 13, 14, 15, 23, 24, 25, 123, 124, 125, 213, 214, 215\}$

b) $A = \{3, 4, 5\}$

c) $B = \{5, 15, 25, 125, 215\}$

d) $C = \{3, 4, 5, 23, 24, 25\}$

Problem 3

a) 7%

b) $15\% + 10\% + 5\% = 30\%$

c) $100\% - (18\% + 25\%) = 57\%$

Problem 4

$P(A1) = .22$

$P(A2) = .25$

$P(A3) = .28$

$P(A1 \cap A2) = .11$

$P(A1 \cap A3) = .05$

$P(A2 \cap A3) = .07$

$P(A1 \cap A2 \cap A3) = .01$

a) $A1 \cup A2 = P(A1) + P(A2) - P(A1 \cap A2) =$
 $.22 + .25 - .11 =$
 $.46$

b) $A1' \cap A2' = (A1 \cup A2)' =$
 $1 - (A1 \cup A2) =$
 $1 - .46 \quad // \text{ as defined in 4.a}$
 $.54$

c) $A1 \cup A2 \cup A3 = P(A1) + P(A2) + P(A3) - P(A1 \cap A2) - P(A1 \cap A3) - P(A2 \cap A3) +$
 $P(A1 \cap A2 \cap A3) =$
 $.22 + .25 + .28 - .11 - .05 - .07 + .01 =$
 $.53$

d) $A1' \cap A2' \cap A3' = (A1 \cup A2 \cup A3)' =$
 $1 - .53 \quad // \text{ as defined in 4.c}$

e) $A1' \cap A2' \cap A3 = P(A3) - P(A2 \cap A3) - P(A1 \cap A3) + P(A1 \cap A2 \cap A3) =$
 $.28 - .05 - .07 + .01 =$
 $.17$

f) $(A1' \cap A2') \cup A3 = (A1 \cup A2)' \cup A3$
 $P(A1' \cap A2') + P(A3) - P(A1' \cap A2' \cap A3) =$

$.54 + .28 - .17$ // .54 defined in 4.b and .17 is defined in 4.e
.65

Problem 5

key = D => Day
 S => Swing
 N => Night

 US => Unsafe Conditions

 UR => Unrelated to Conditions

a) Simple Events = {DUS, DUR, SUS, SUR, NUS, NUR}

b) $P(US) = P(DUS) + P(SUS) + P(NUS) =$ // No need for calculating $P(DUS \cap SUS)$
because these events are simple

$10\% + 8\% + 5\% =$

23%

c) $P(D') = 100\% - P(D) =$

$100\% - P(DUC) + P(DUR)$ // $P(DUC)$ and $P(DUR)$ are simple events

$100\% - 10\% - 35\% =$

55%

Problem 6

a) 3A's 3B's 3C's 3D's =

$9! / (3! * 3! * 3! * 3!) =$

15120

// 9! comes from the number of total possible combinations given A1, A2, etc.

// dividing by $3! * 3! * 3! * 3!$ comes from removing the Permutations A1, A2,
etc.

b) Assuming all the outcomes are equally likely,

I computed the number of outcomes that satisfy adjacency

The result 4! can then be divided by the total number of outcomes

Which gives me $24/15120 =$

$1/630$