

Part 1B: $y'' - (x-2)y' + 2y = 0$

$$f(x) = f(x_0) + \frac{f'(x_0)}{1!} (x-x_0) + \frac{f''(x_0)}{2!} (x-x_0)^2 + \dots$$

$$x_0 = 3$$

$$f(3) = 6$$

$$f'(3) = 1$$

$$f(x) = f(3) + f'(3)(x-3) + \frac{1}{2} f''(3)(x-3)^2$$

$$f'' - (x-2)f' + 2f = 0$$

$$f'' = (x-2)f' - 2f$$

$$f''(3) = (3-2)f'(3) - 2f(3)$$

$$f''(3) = 1 - 12 = -11$$

$$f(x) = 6 + 1 \cdot (x-3) + \frac{1}{2} \cdot (-11) \cdot (x-3)^2$$

$$f(x) = 6 + (x-3) - \frac{11}{2} (x-3)^2$$